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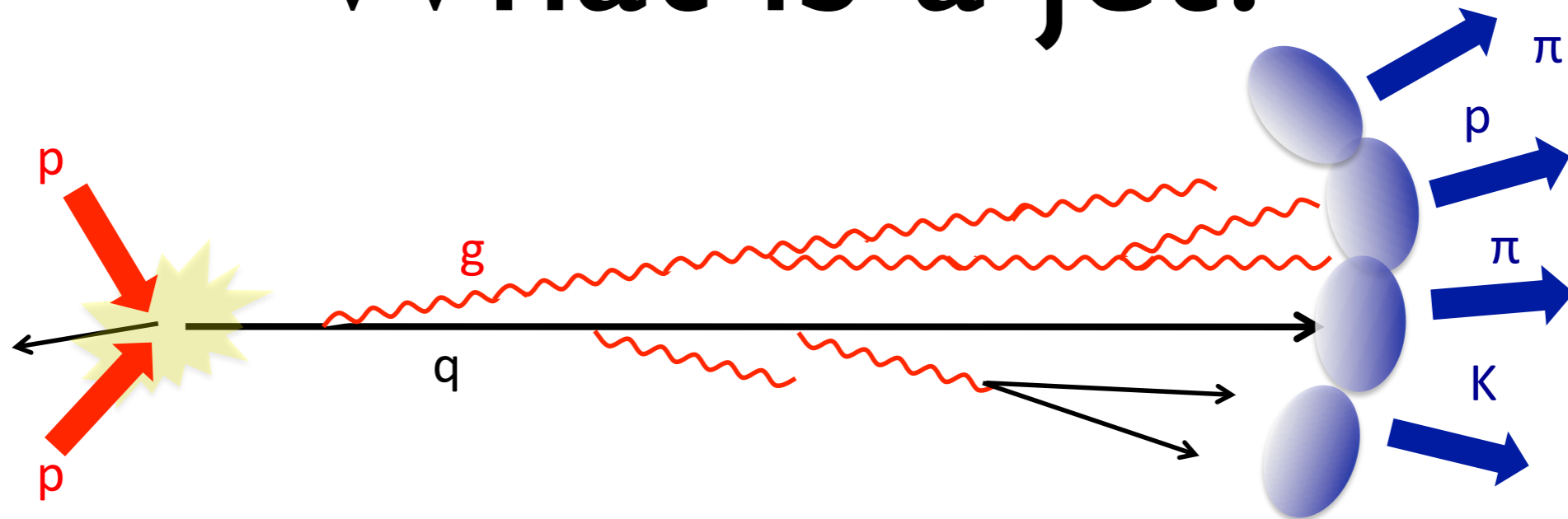
Decoherence of QCD radiation in a quark-gluon plasma

Konrad Tywoniuk

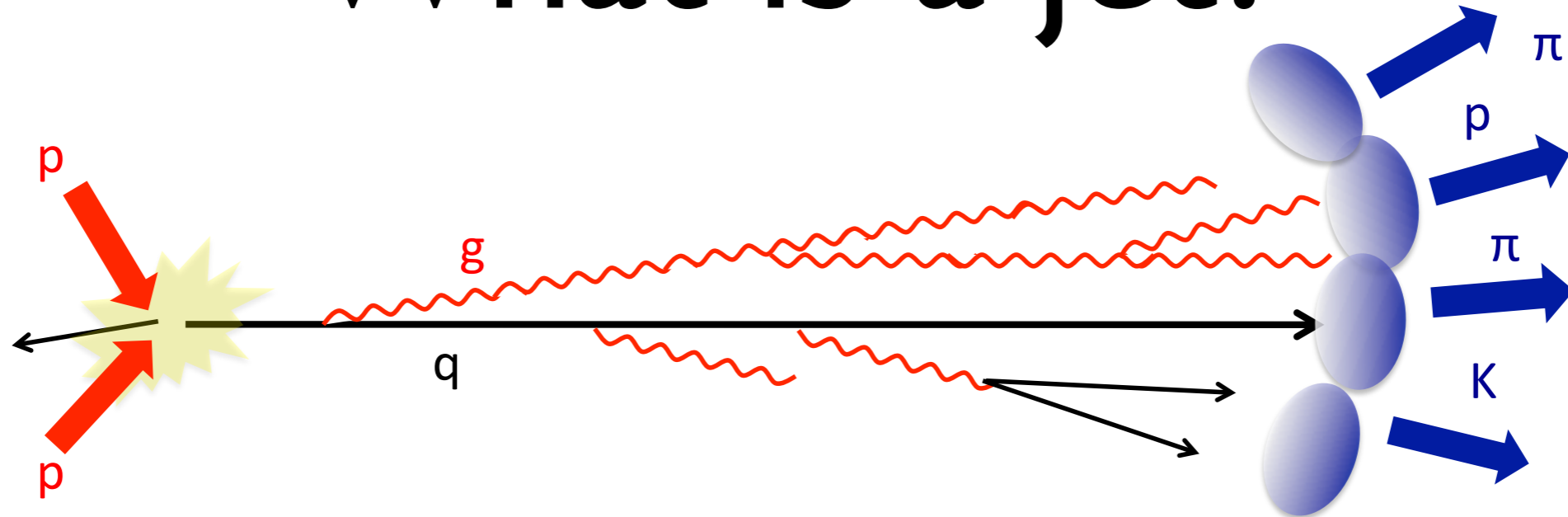
1st International Conference on New
Frontiers in Physics

Kolymbari, Greece, 11-16 June 2012

What is a jet?

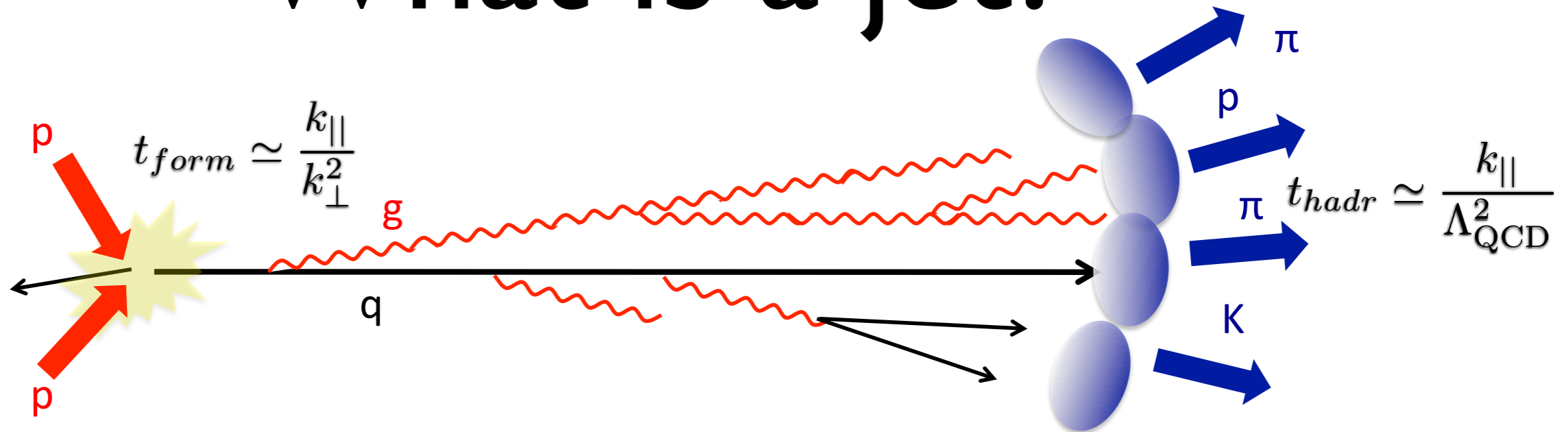


What is a jet?



- Originally a **hard parton** (quark/gluon) which fragments into many partons with virtuality down to a non-perturbative scale where it **hadronizes**

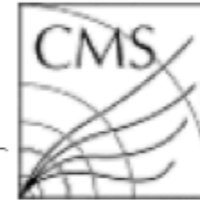
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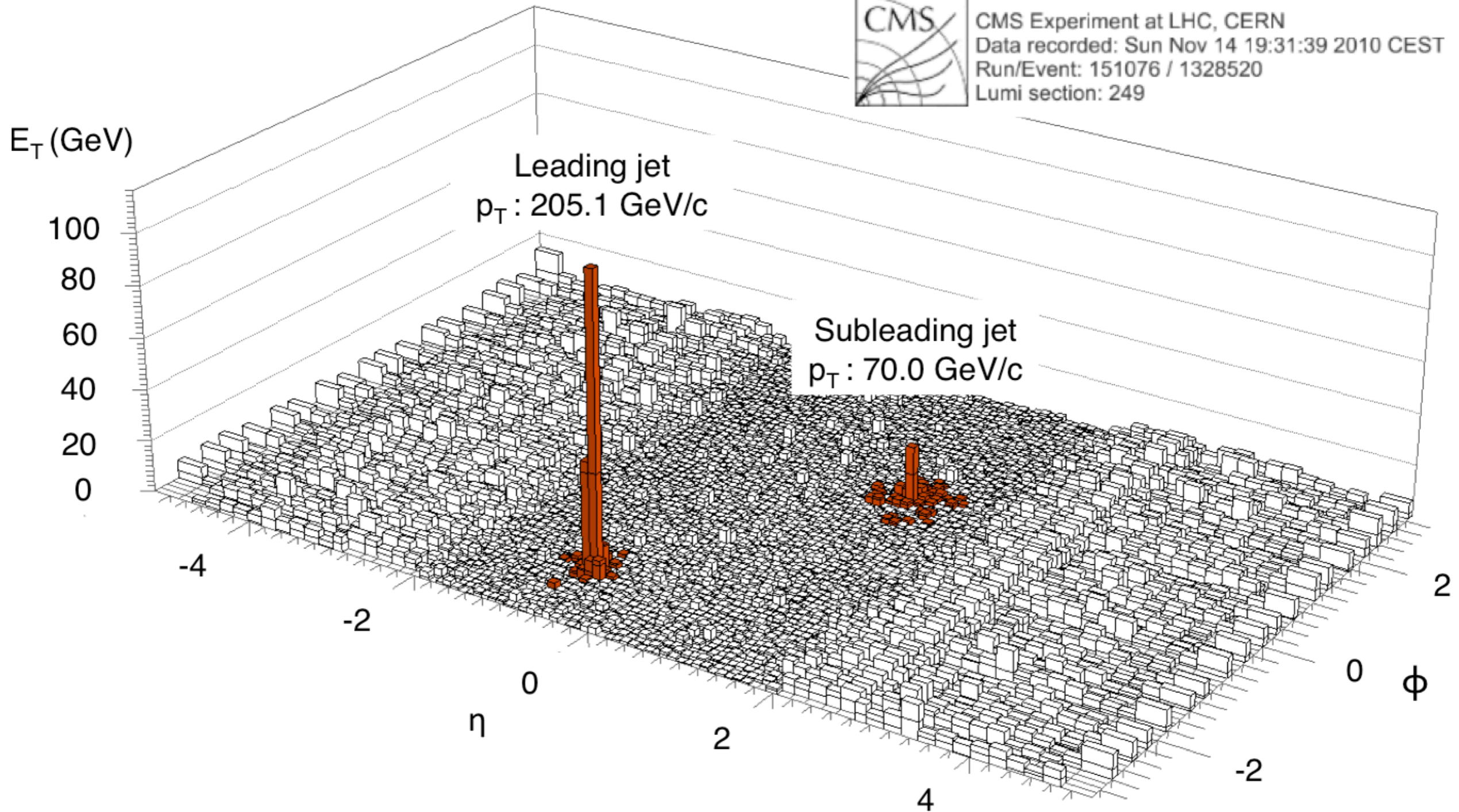
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Large time domain for pQCD: $\frac{1}{\sqrt{s}} < t < \frac{\sqrt{s}}{\Lambda_{QCD}^2}$

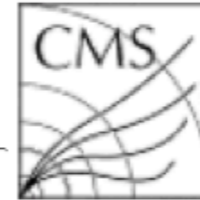
Jets in HIC @ LHC



CMS Experiment at LHC, CERN
Data recorded: Sun Nov 14 19:31:39 2010 CEST
Run/Event: 151076 / 1328520
Lumi section: 249



Jets in HIC @ LHC

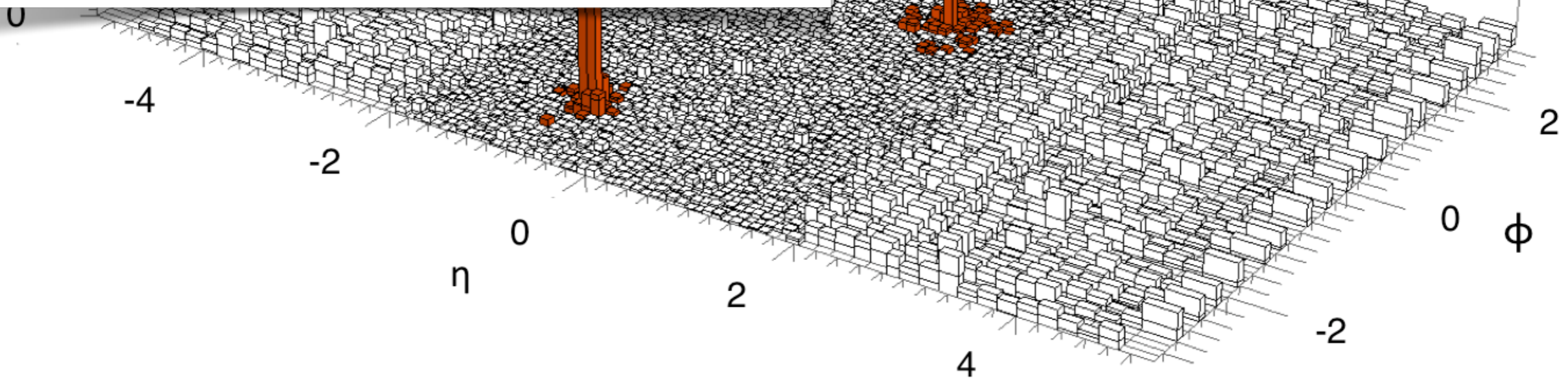


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Main features:

- significant dijet energy asymmetry
- soft particles at large angles
- vacuum-like fragmentation of hard jets

Subleading jet
 $p_T : 70.0 \text{ GeV}/c$



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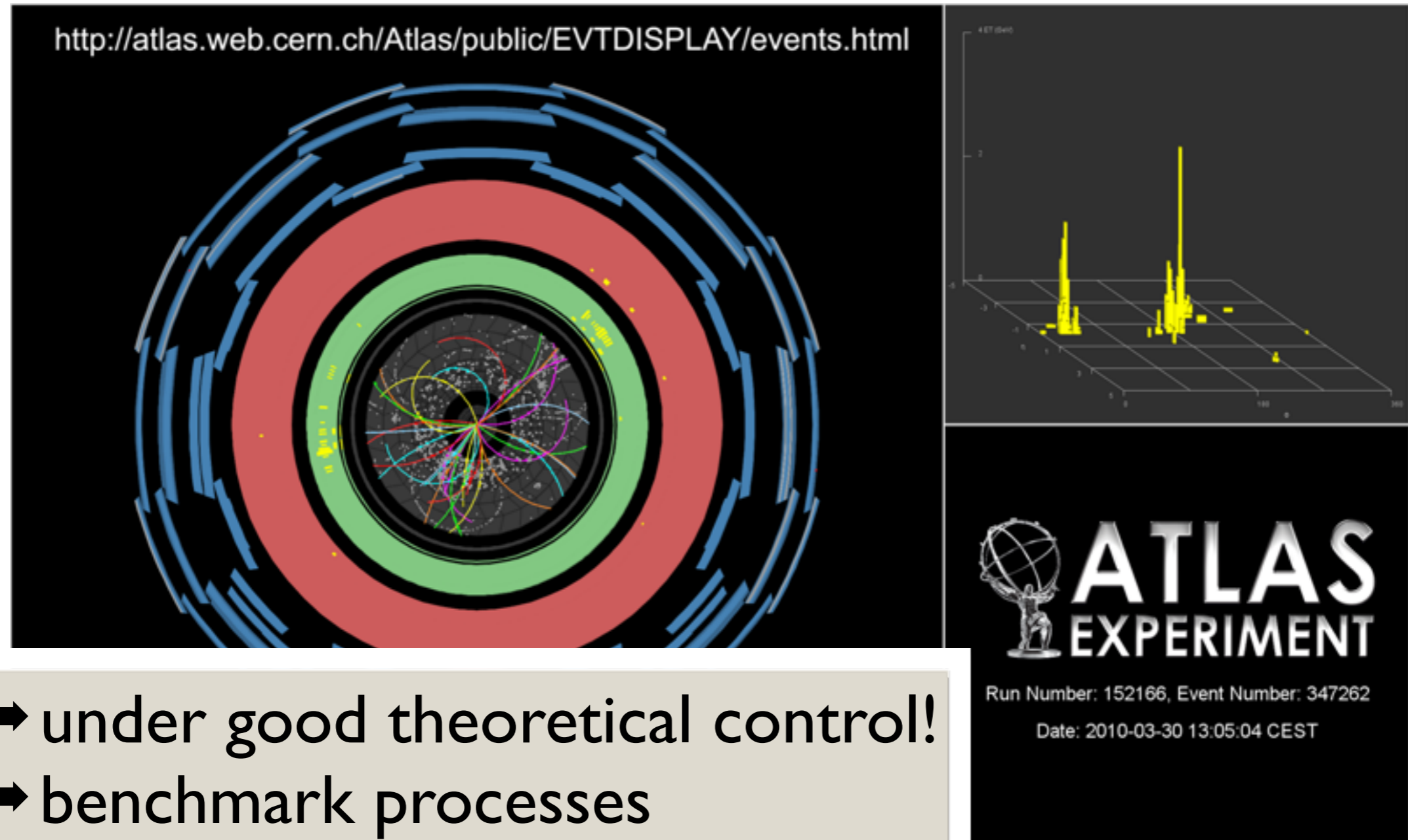
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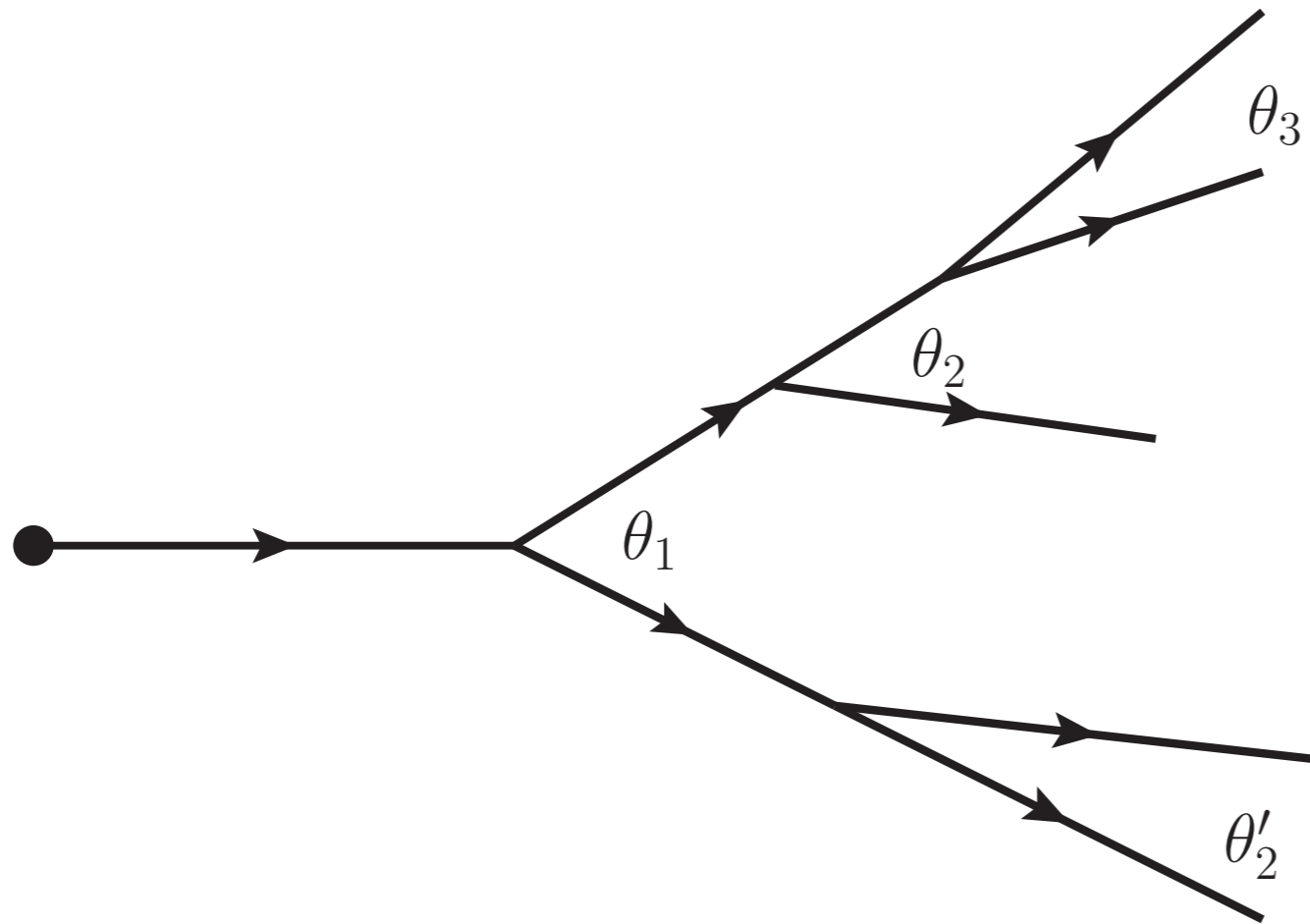
Medium interacts via color interactions.
pQCD in the presence of dense fields.



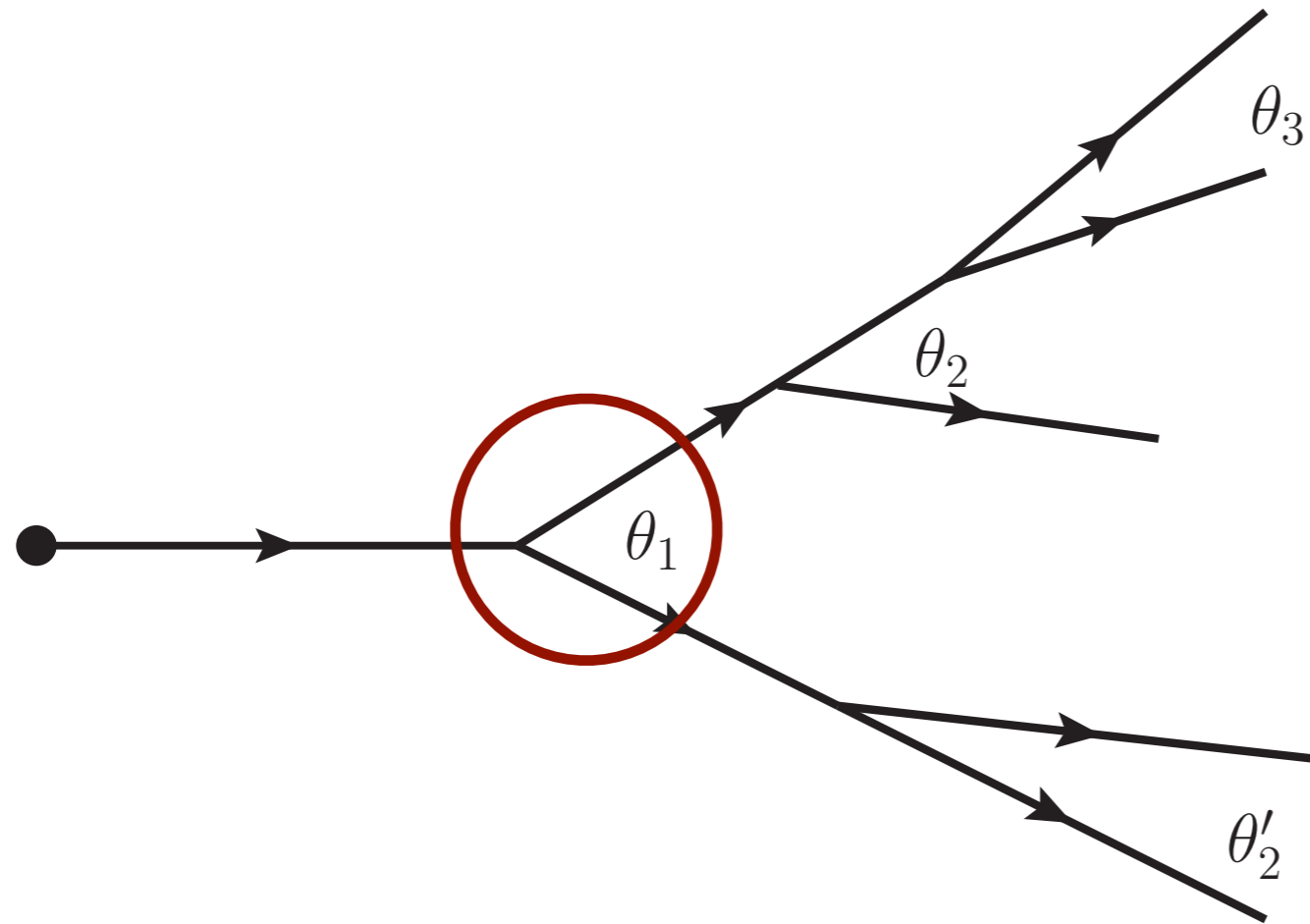
Jets in pp @ LHC



Parton branching in vacuum



Parton branching in vacuum

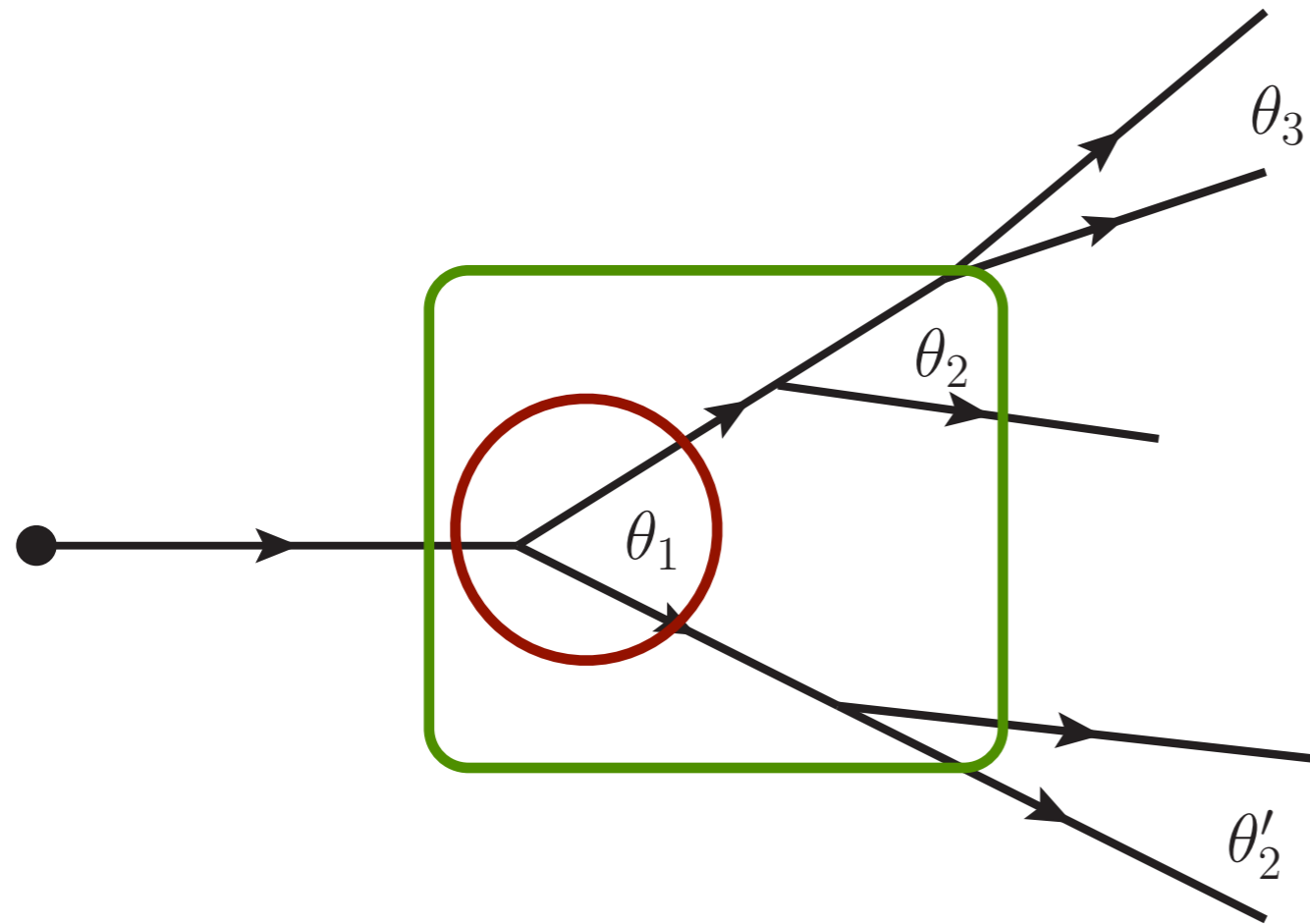


Leading singularities

$$\propto \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{d\theta}{\theta}$$



Parton branching in vacuum



Leading singularities

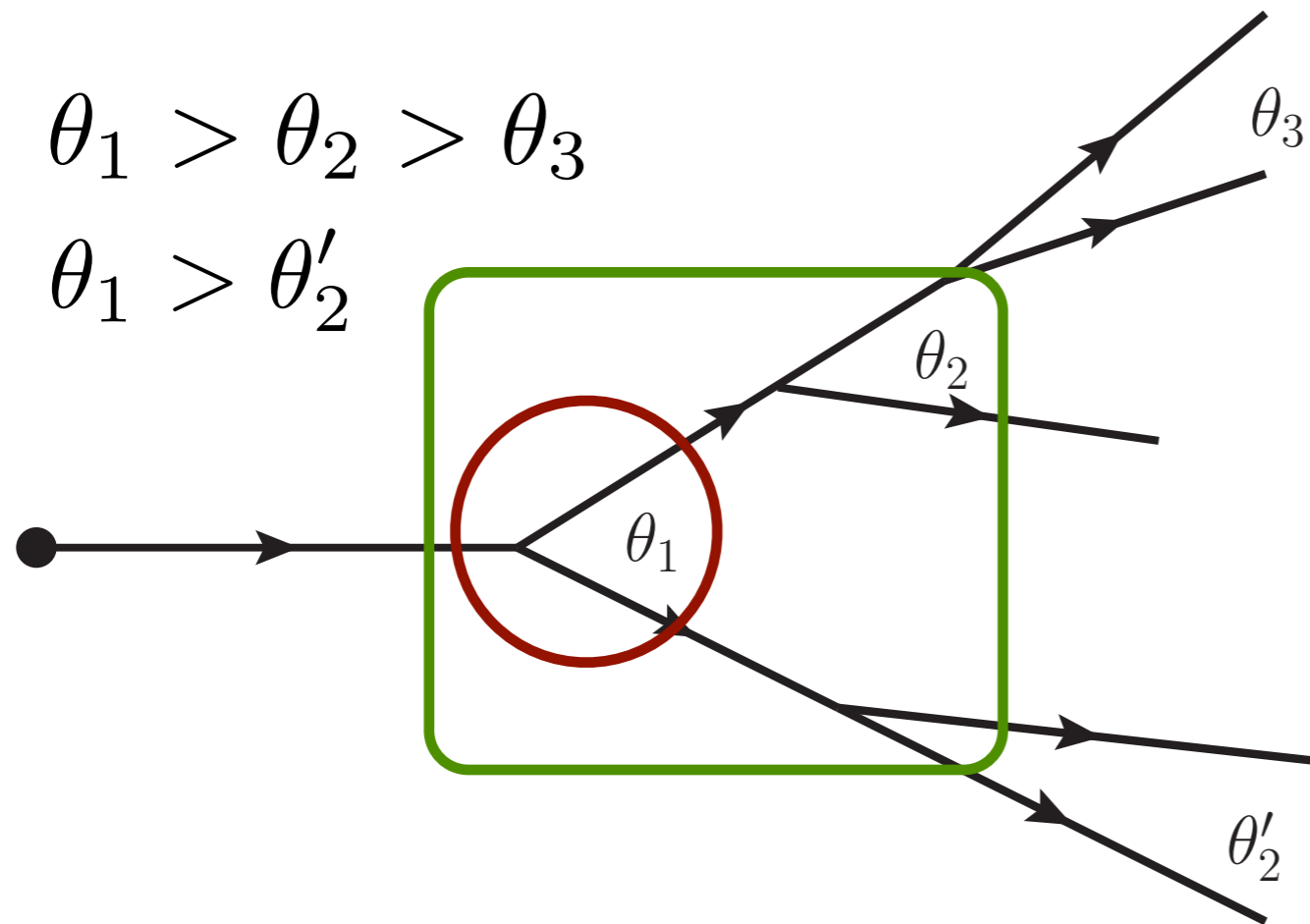
$$\propto \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{d\theta}{\theta}$$

Angular ordering

$$\propto \Theta(\theta_1 - \theta_2)$$



Parton branching in vacuum



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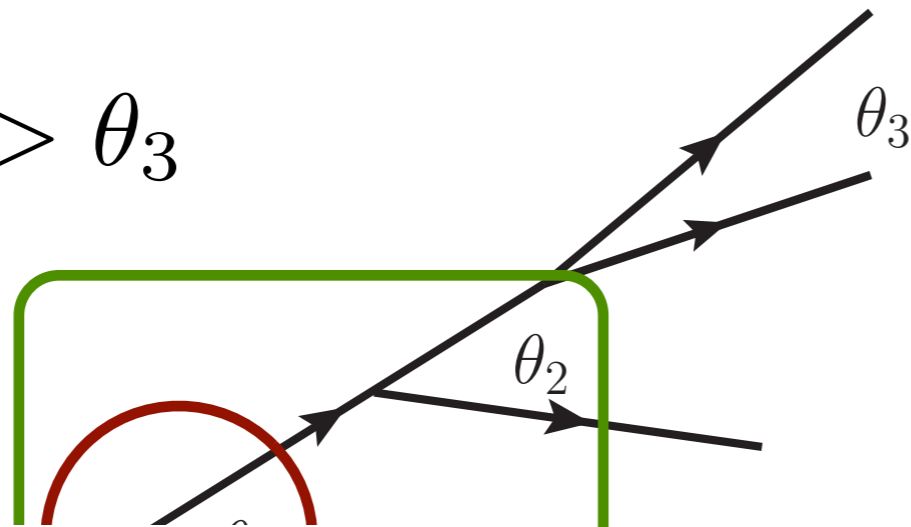
Markovian process!



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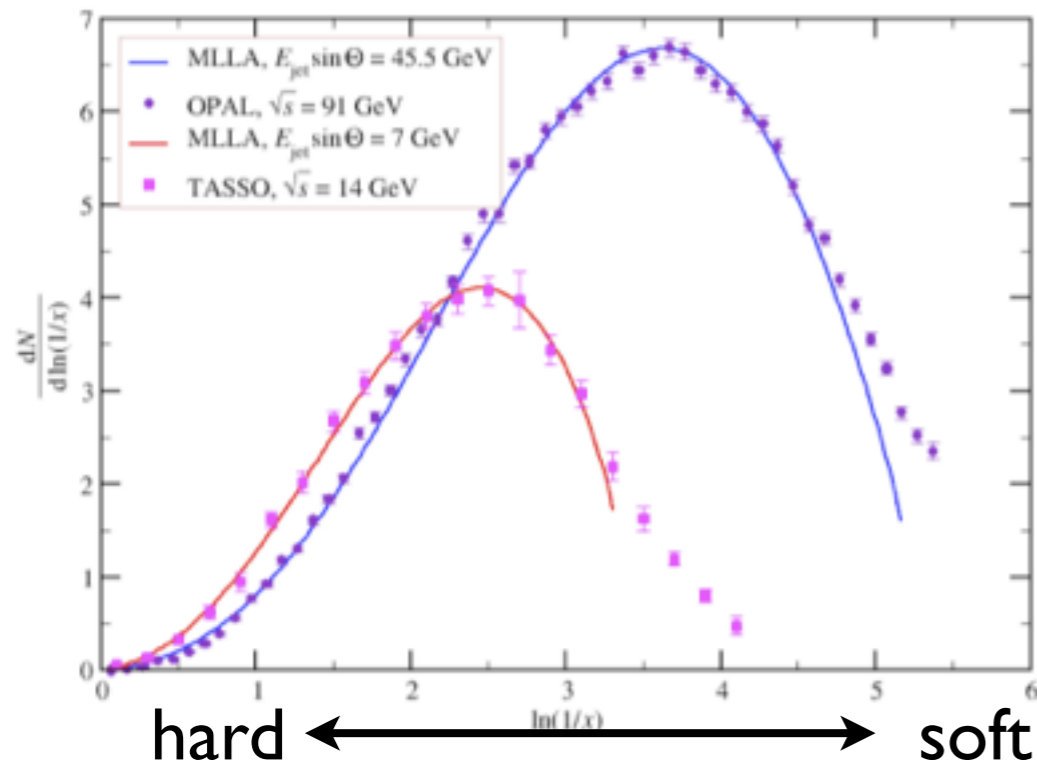
$$\theta_1 > \theta_2 > \theta_3$$

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TASSO Collaboration, Z. Phys. C 47 (1990) 187

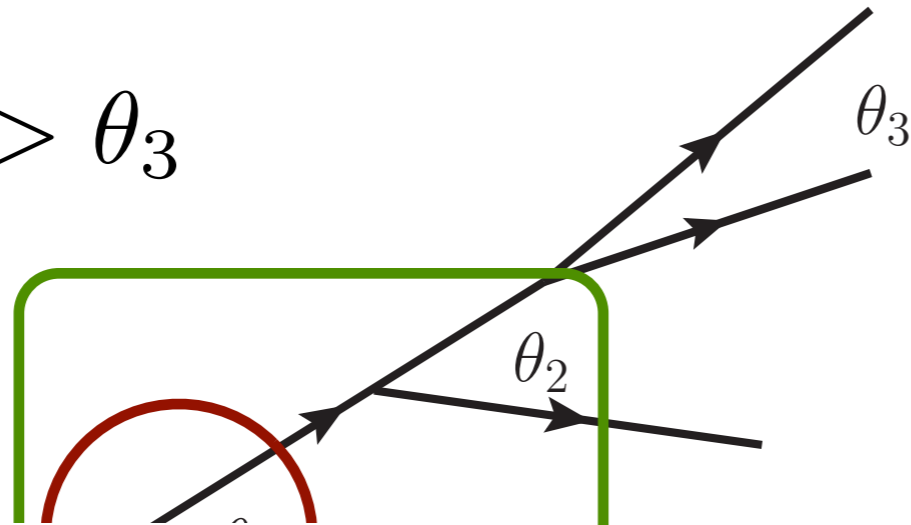
OPAL Collaboration, Phys. Lett. B 247 (1990) 617



Parton branching in vacuum

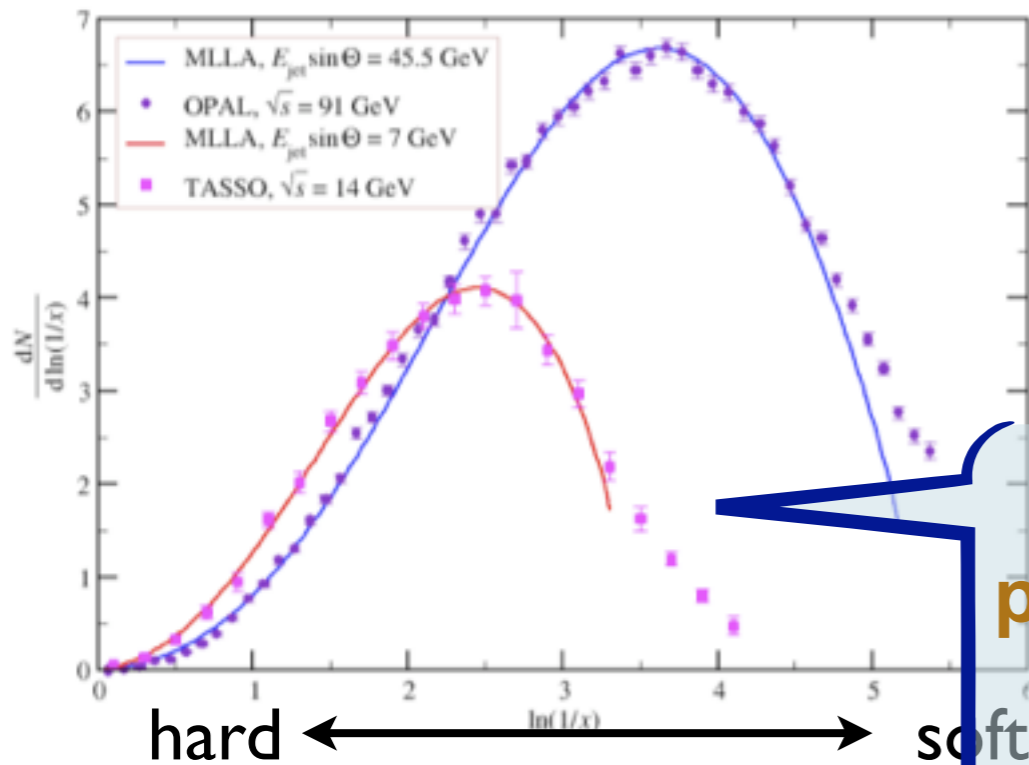
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AO limits phase space for soft emissions!

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OPAL Collaboration, Phys. Lett. B 247 (1990) 617

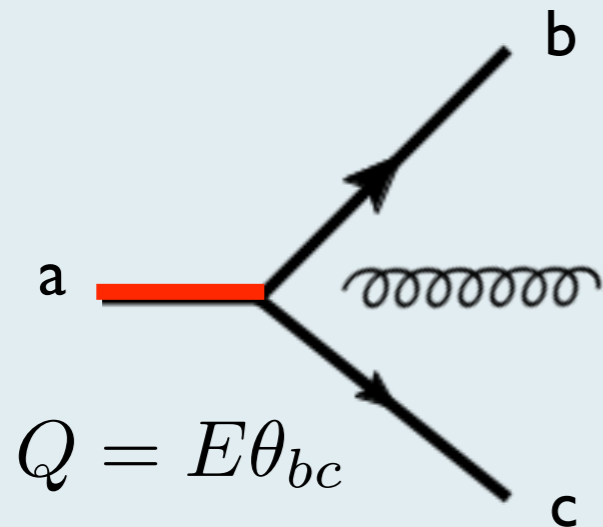


Antenna spectrum in vacuum

- decay of a **highly virtual** particle
- a **laboratory** to study coherence effects
- contains necessary elements of transverse color coherence



Antenna spectrum in vacuum

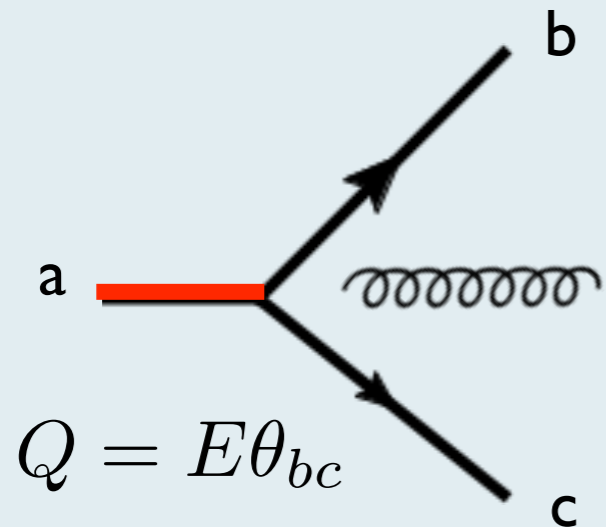


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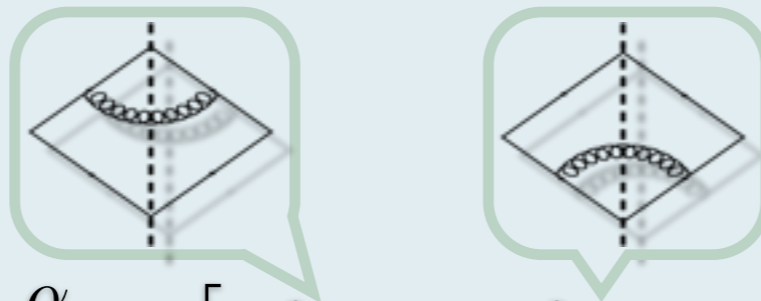
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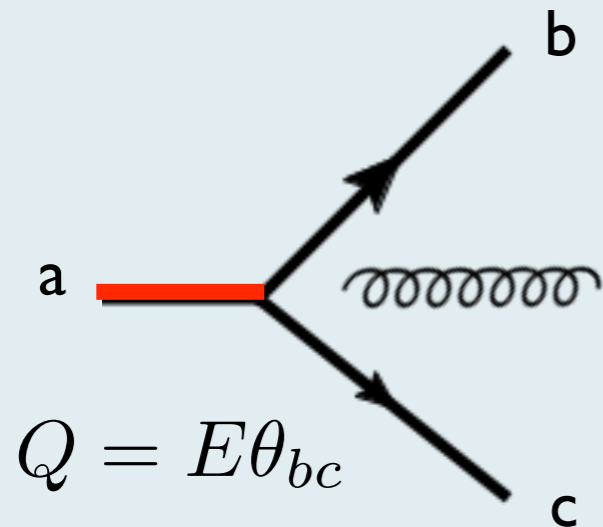
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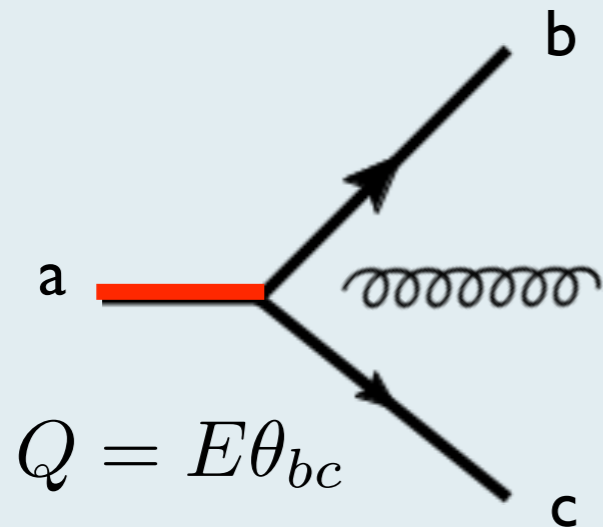
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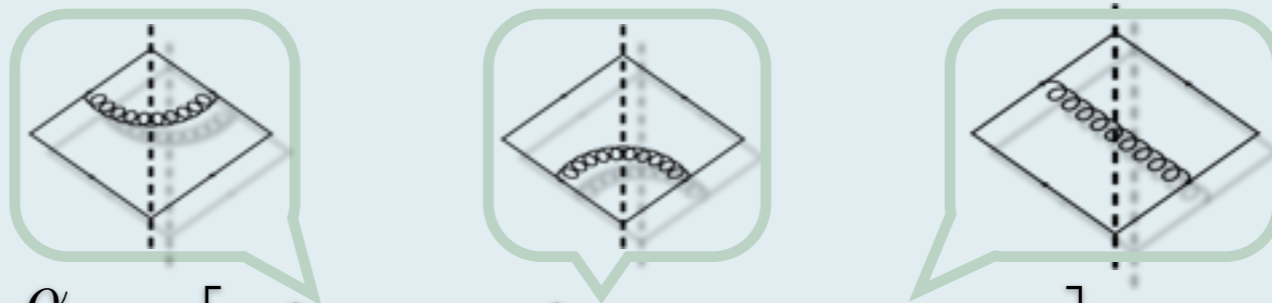
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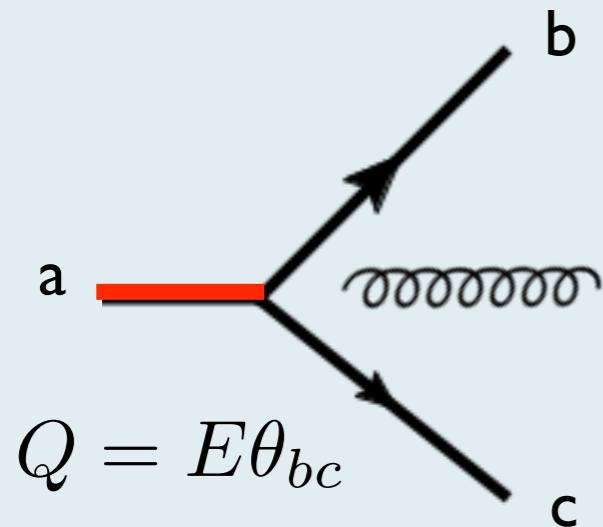
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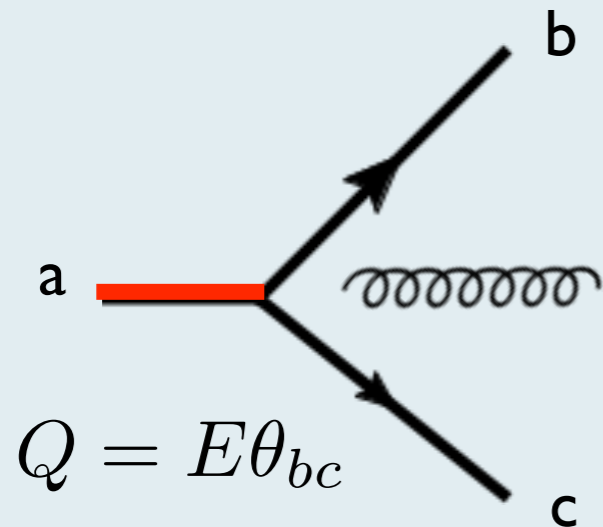


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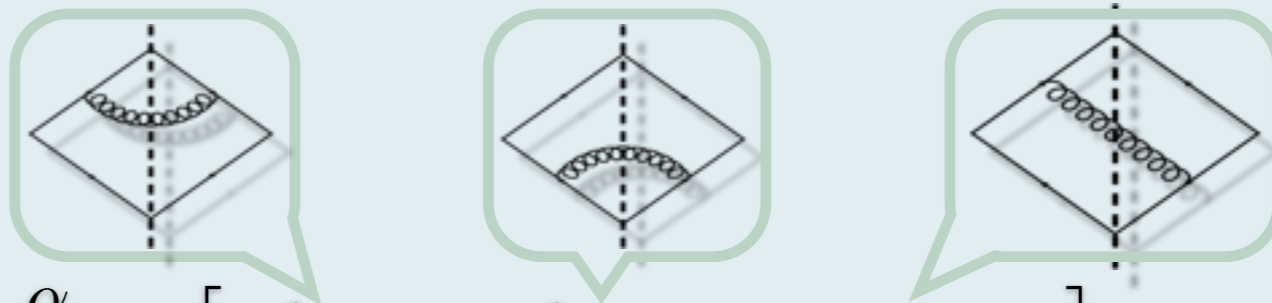
coherent spectra



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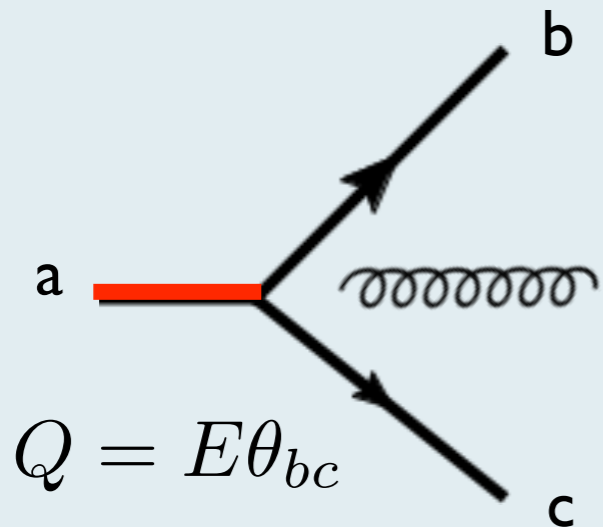


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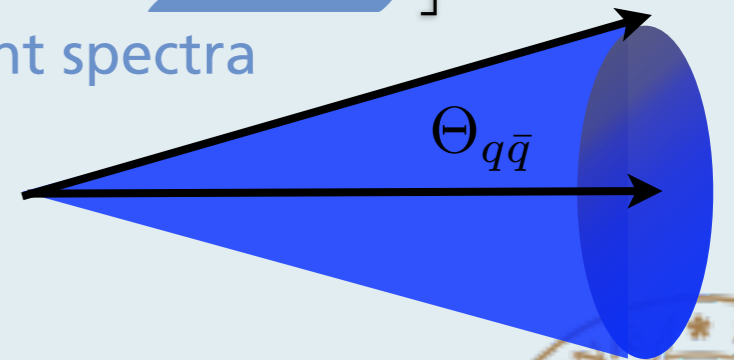
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$$\langle dN_q \rangle_\varphi = \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{d\theta}{\theta} \Theta(\cos \theta - \cos \theta_{q\bar{q}})$$



Fundamental building block of the QCD cascade!



How is the jet modified?

No established theory of jets in medium!

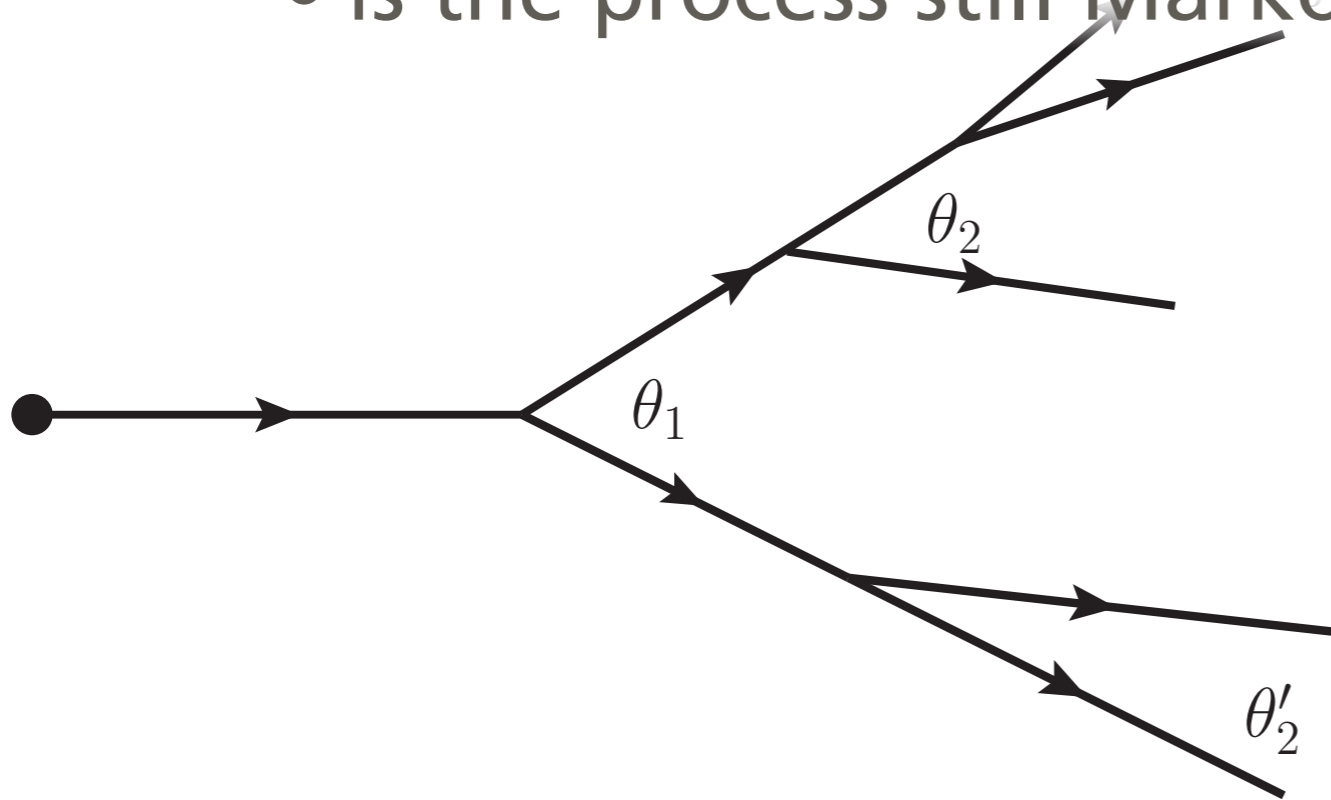
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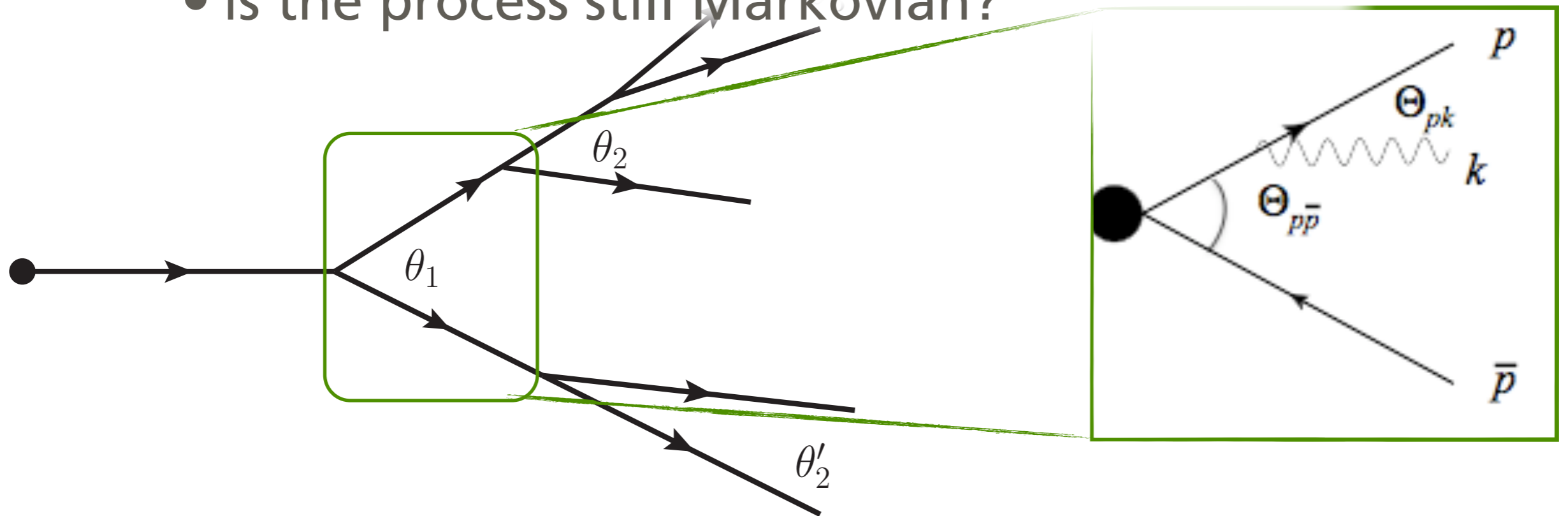
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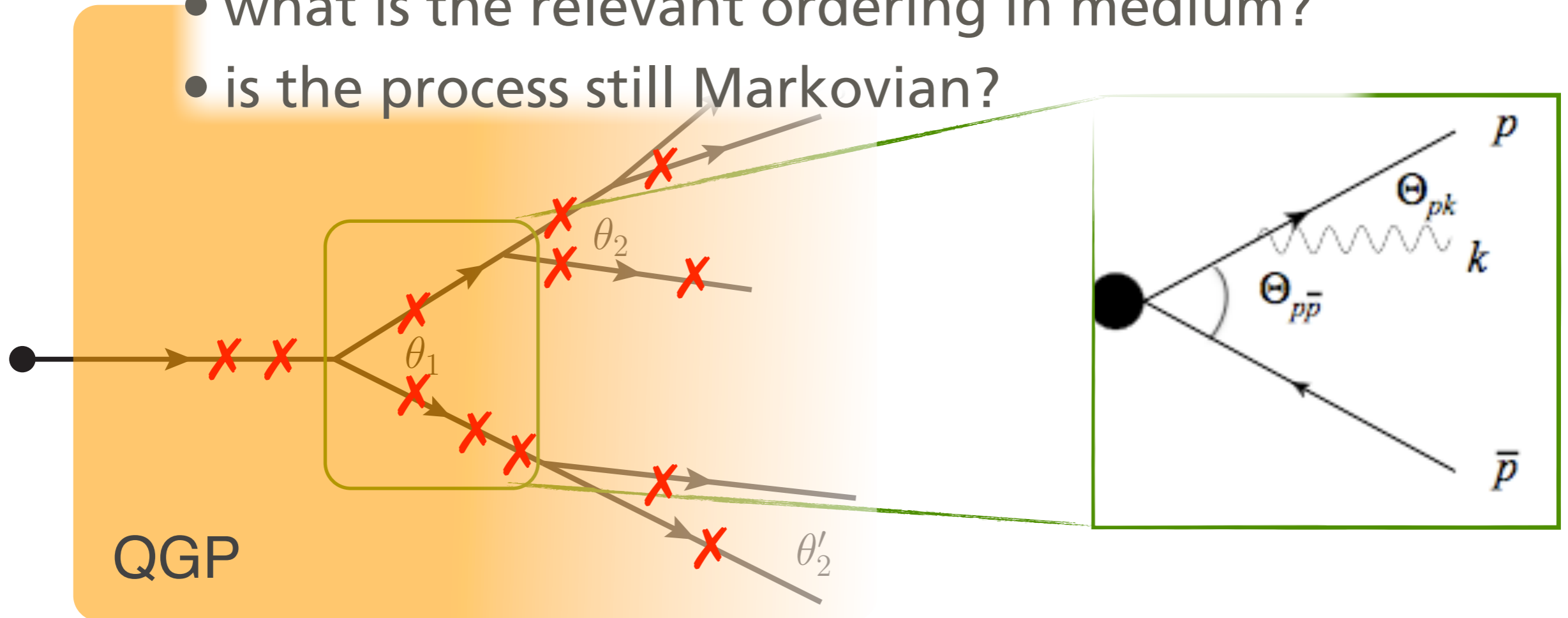
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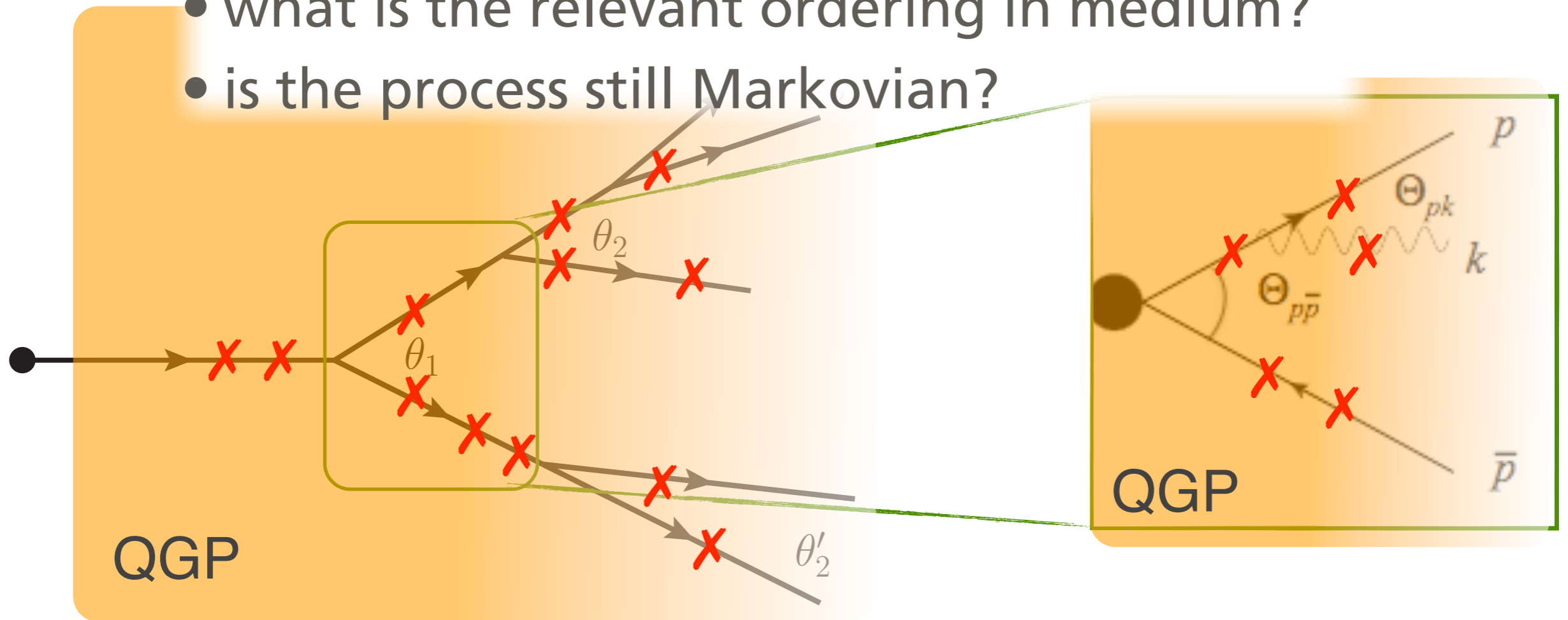
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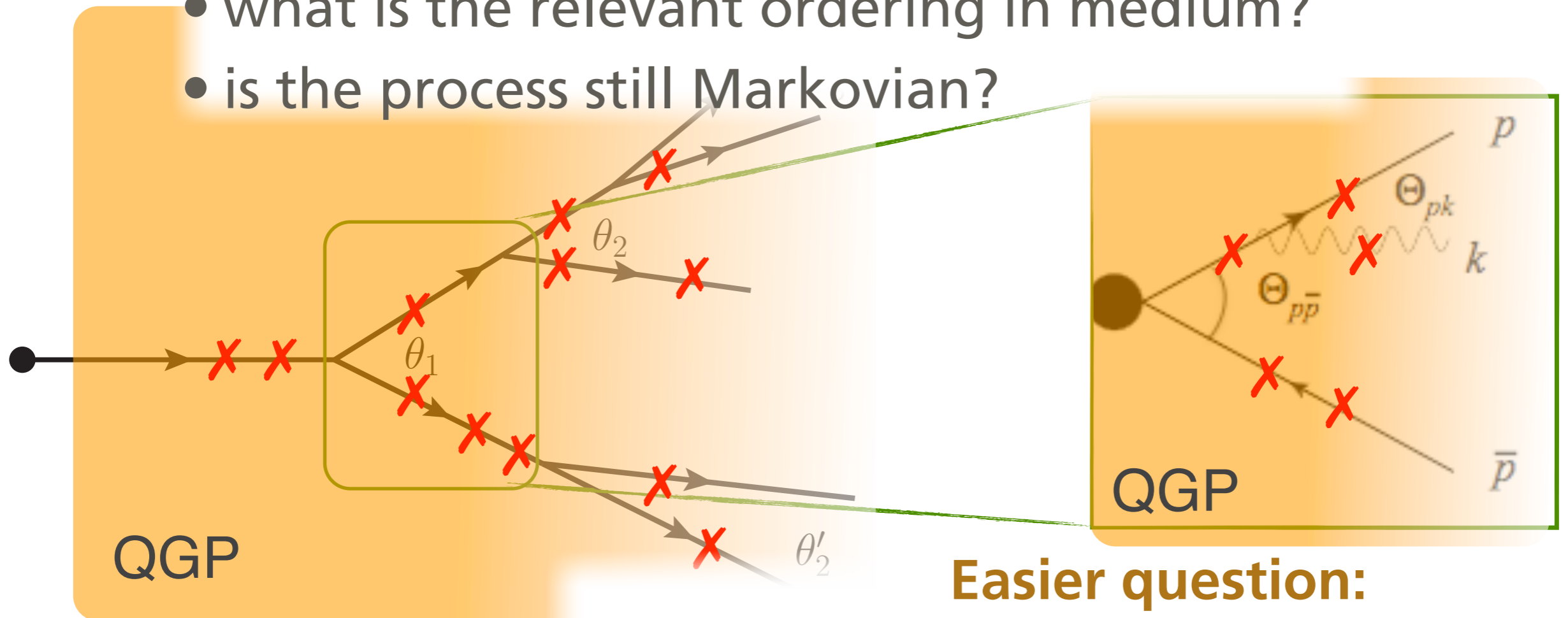
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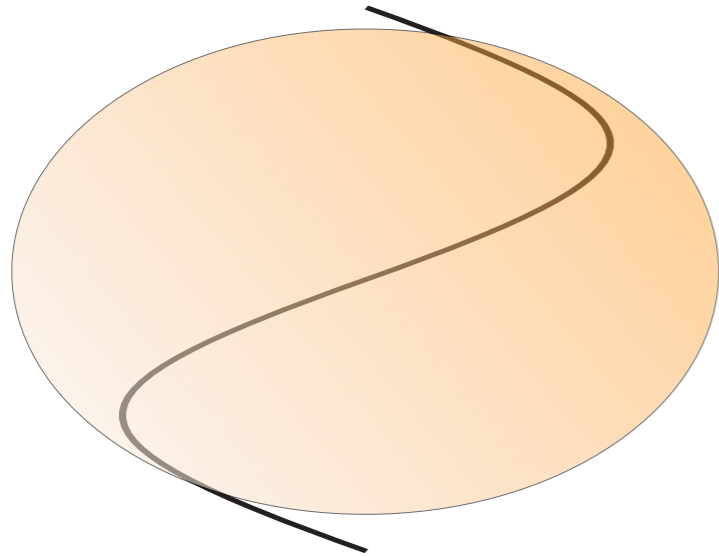
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- how is the antenna spectrum modified in a medium?



Decoherence of radiation in media

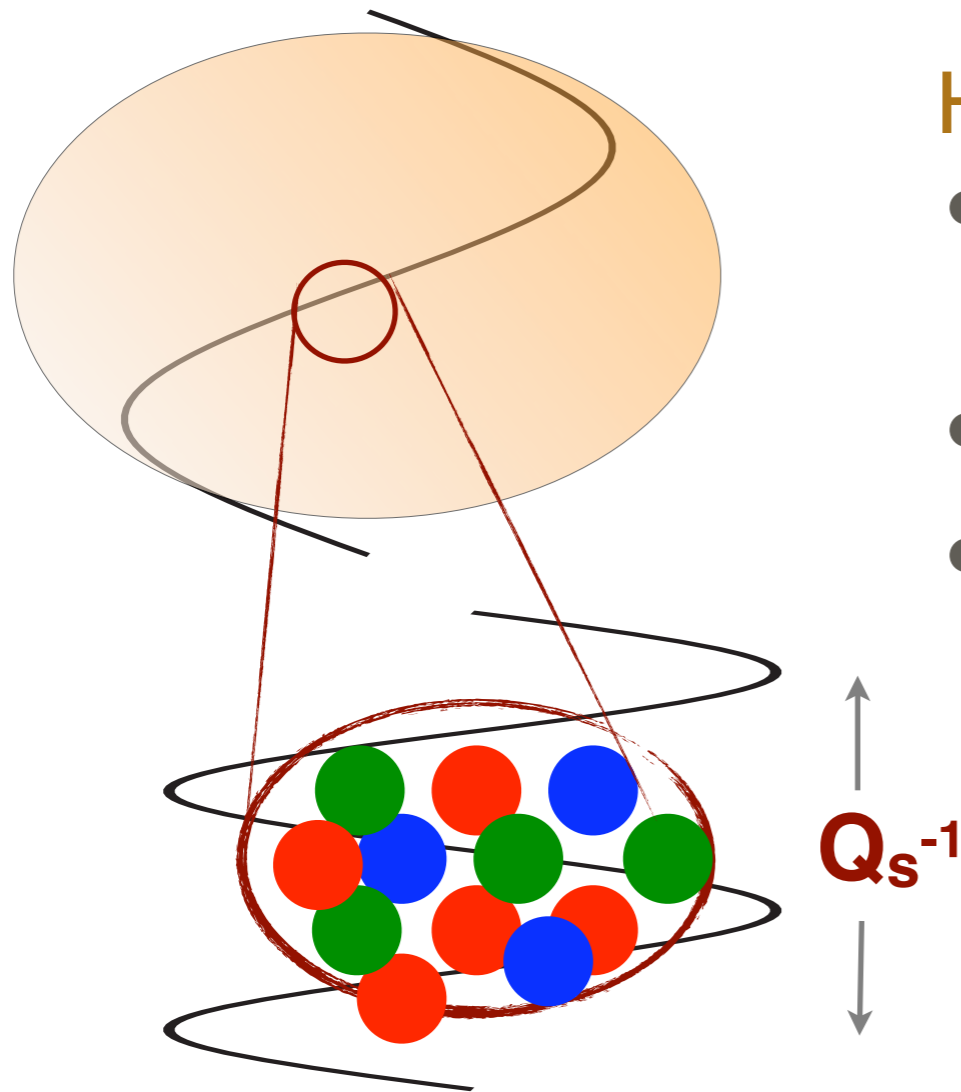


How is the medium resolved

- medium fluctuates with typical transverse wave length Q_s^{-1}
- zero color on average, $\lambda > Q_s^{-1}$
- resolved by $\lambda < Q_s^{-1}$



Decoherence of radiation in media

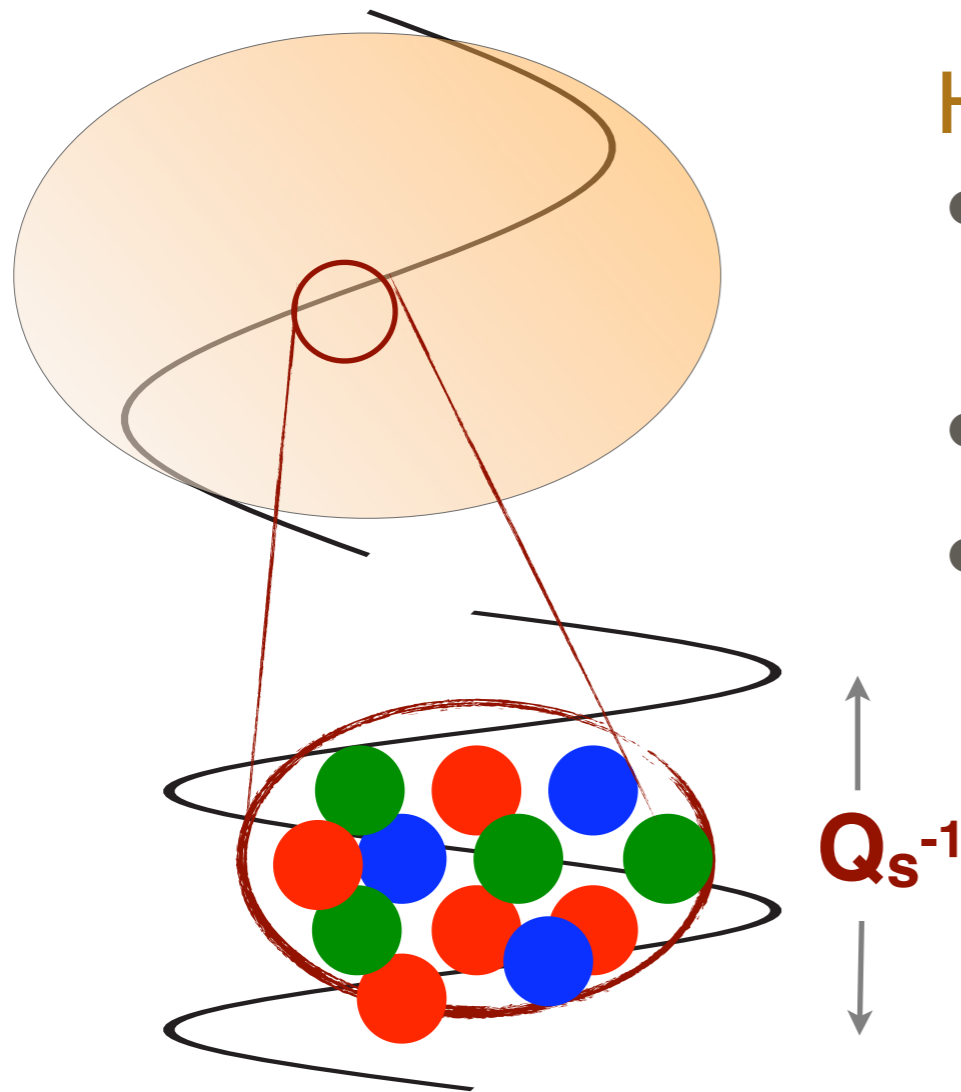


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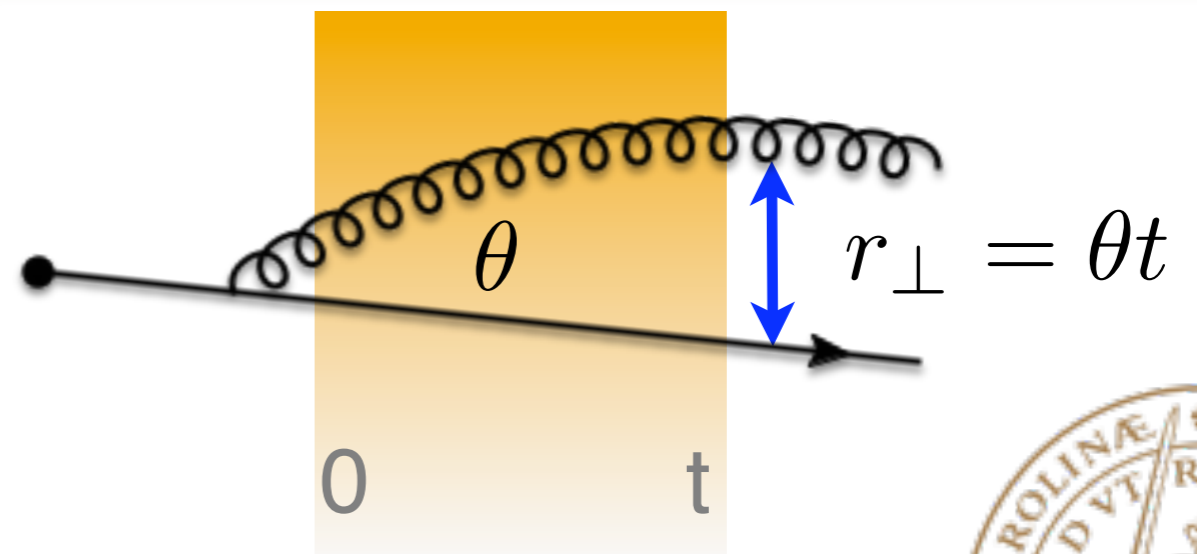
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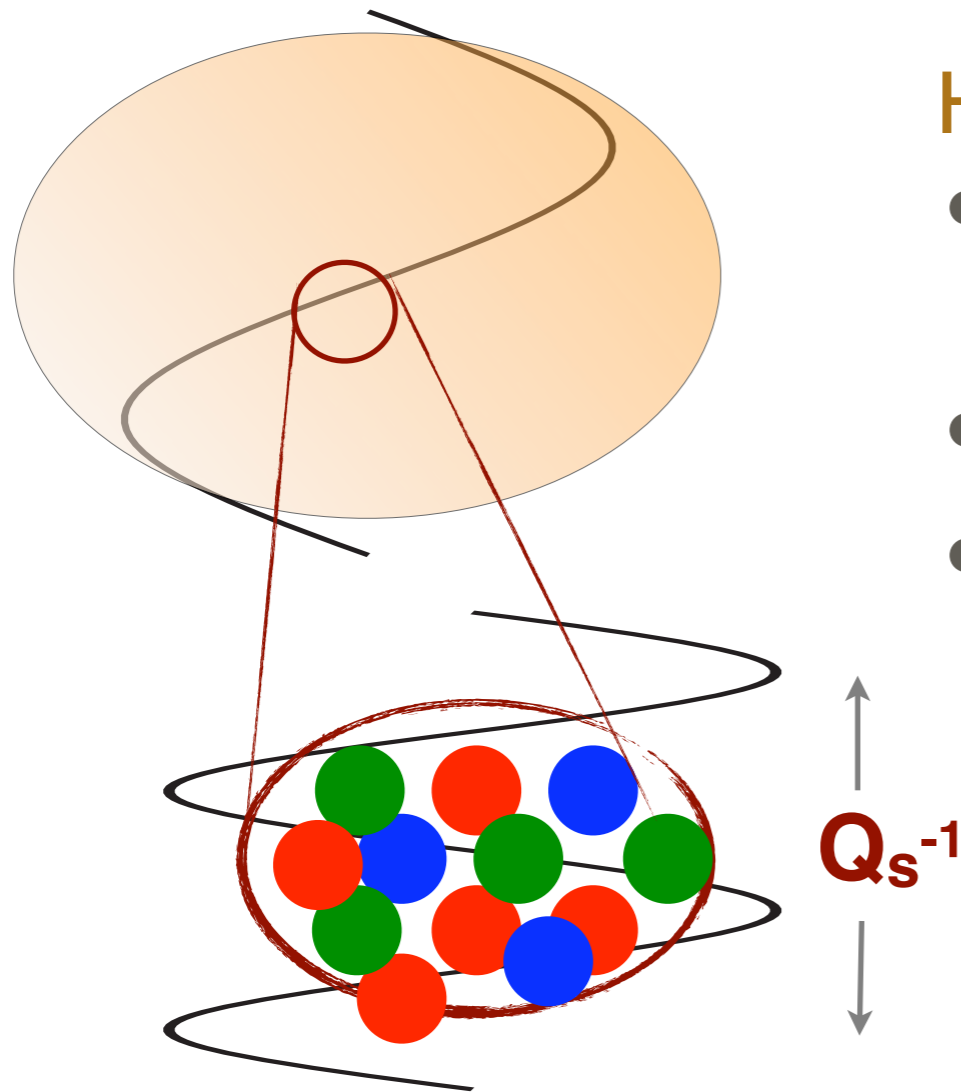
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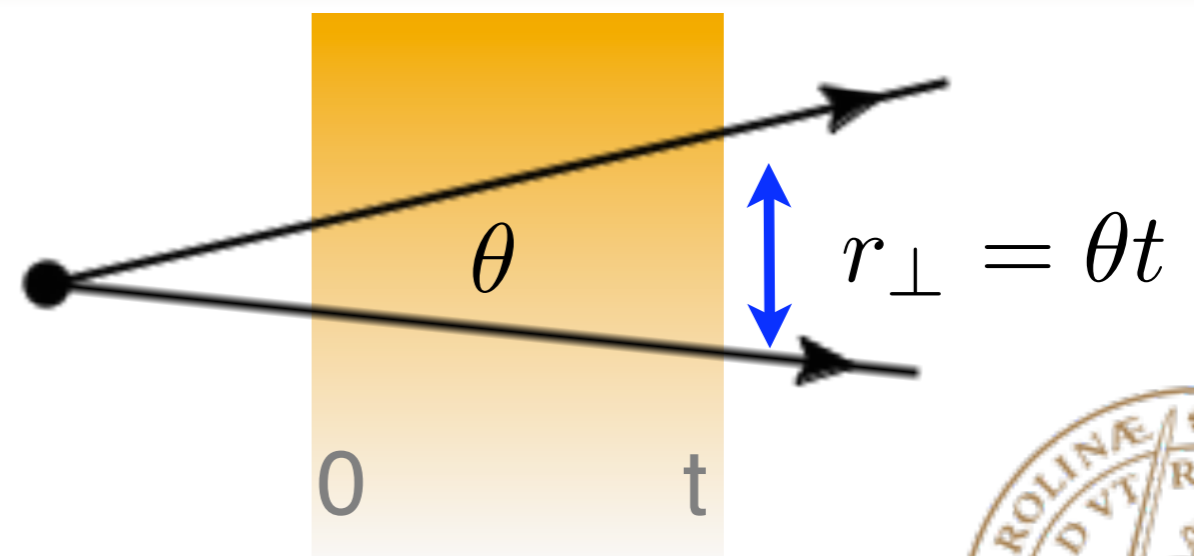
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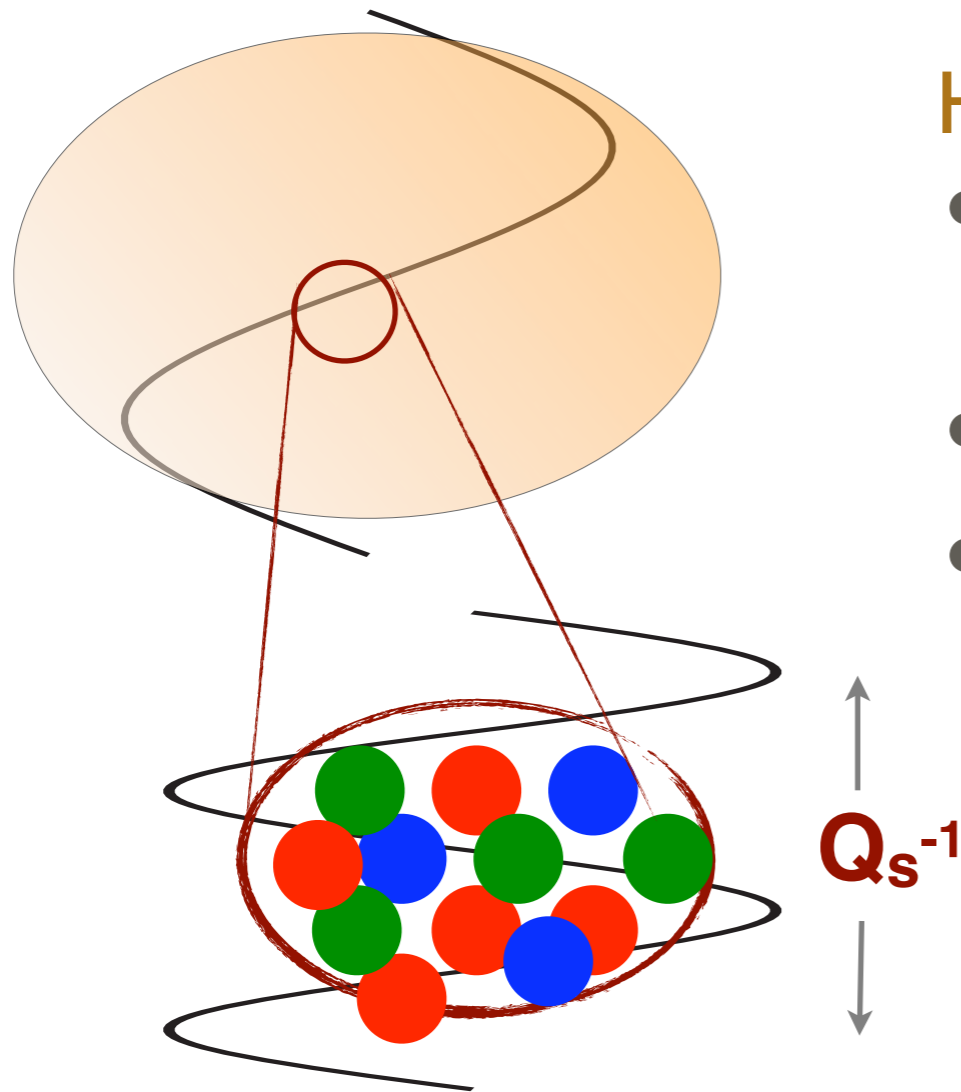
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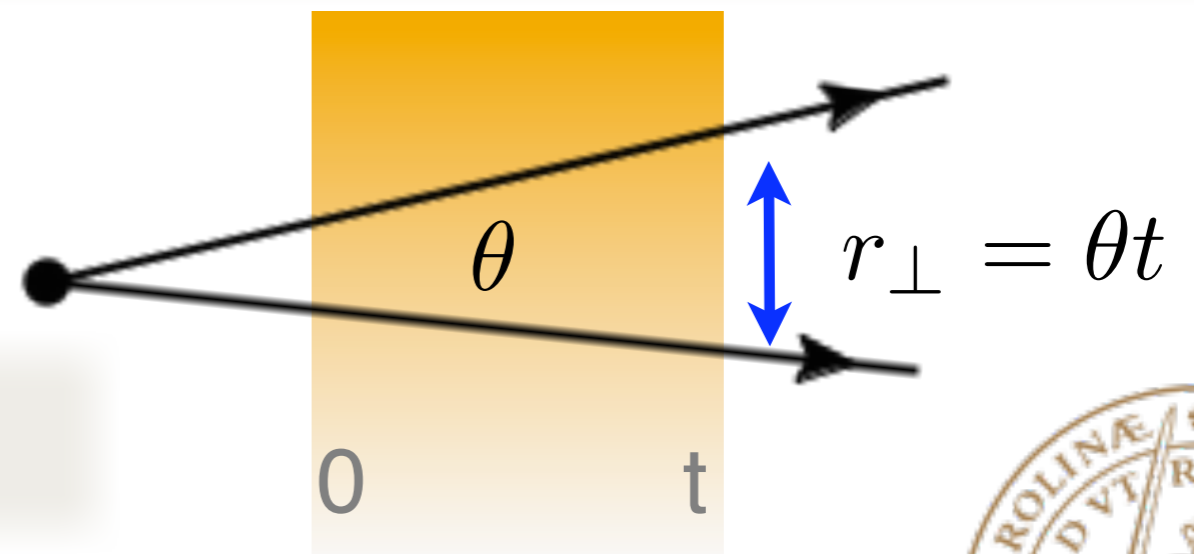
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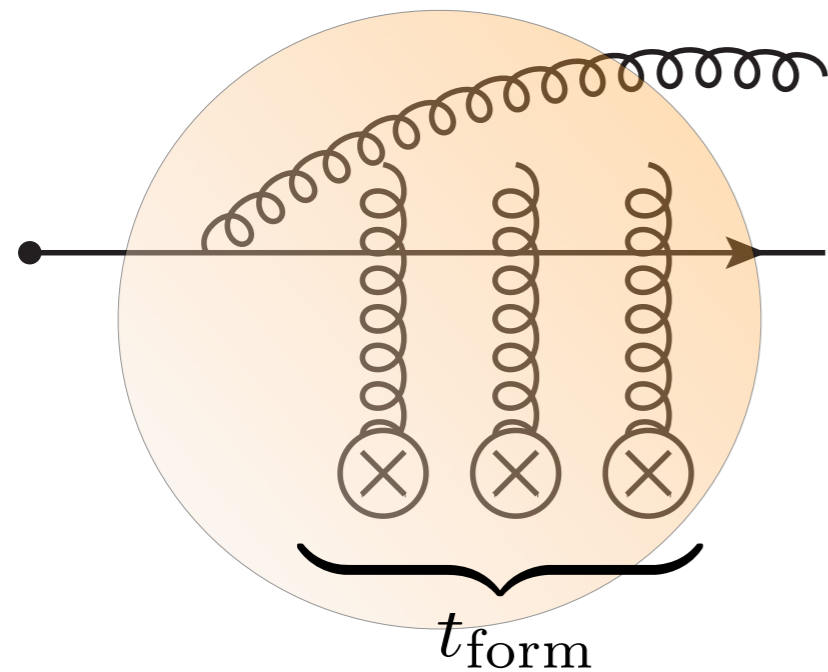
What are the typical dipole transverse sizes?



Medium-induced radiation

Longitudinal coherence

- induces a characteristic formation time larger than mean free path



$$\left. \begin{aligned} t_{\text{form}} &= \lambda_{\text{mfp}} N_{\text{coh}} \\ k_{\text{ind}}^2 &= \mu^2 N_{\text{coh}} \end{aligned} \right\} \begin{aligned} t_{\text{form}} &= \sqrt{\omega / \hat{q}} \\ k_{\text{ind}}^2 &= \sqrt{\hat{q} \omega} \end{aligned}$$

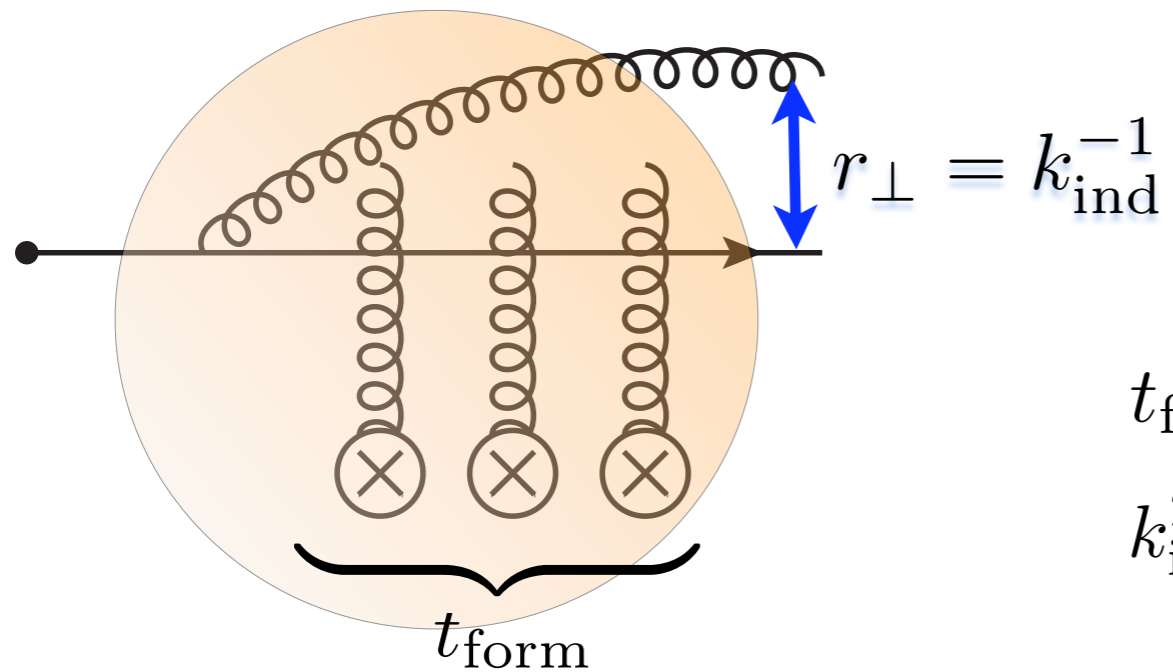
Baier, Dokshitzer, Mueller, Peigné, Schiff (1997-2000), Zakharov (1996)



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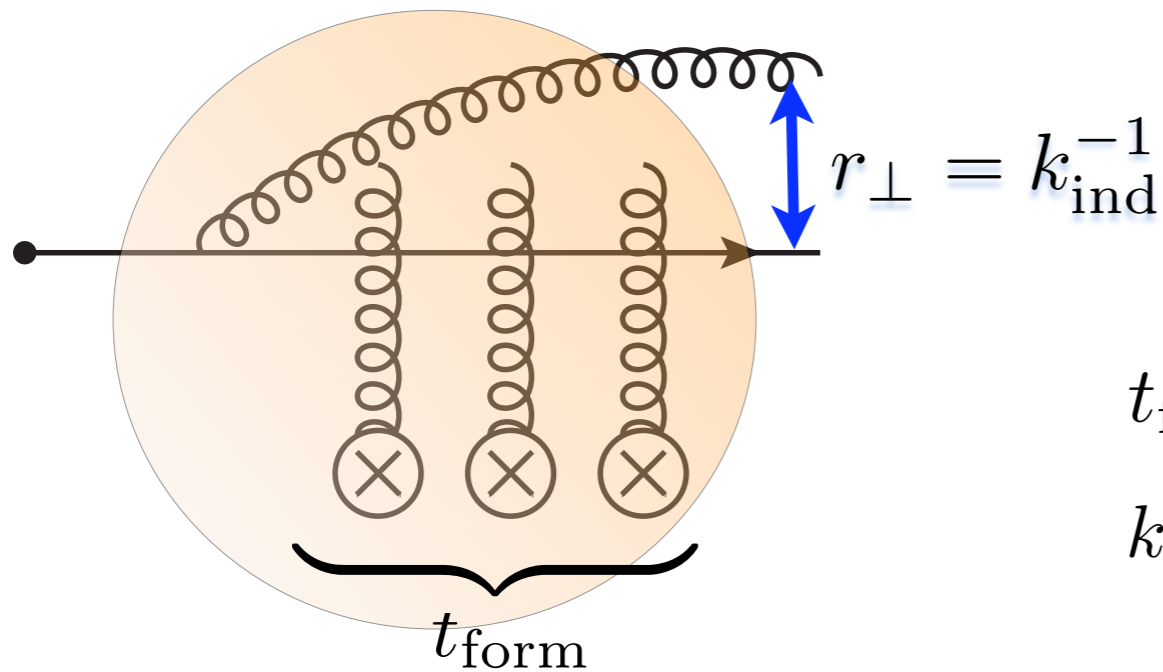
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Coherent spectrum

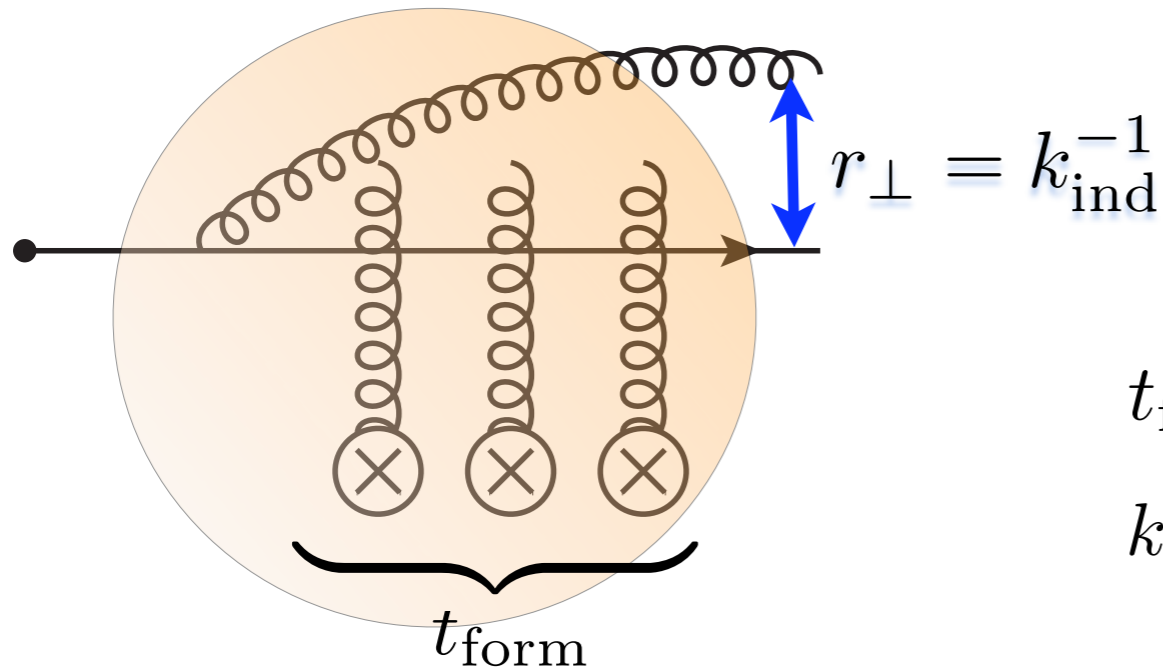
$$\omega \frac{dN}{d\omega} \propto \alpha_s \frac{L}{t_{\text{form}}} = \alpha_s \sqrt{\frac{\hat{q} L^2}{\omega}}$$

Energy loss: $\Delta E \propto \hat{q} L^2$

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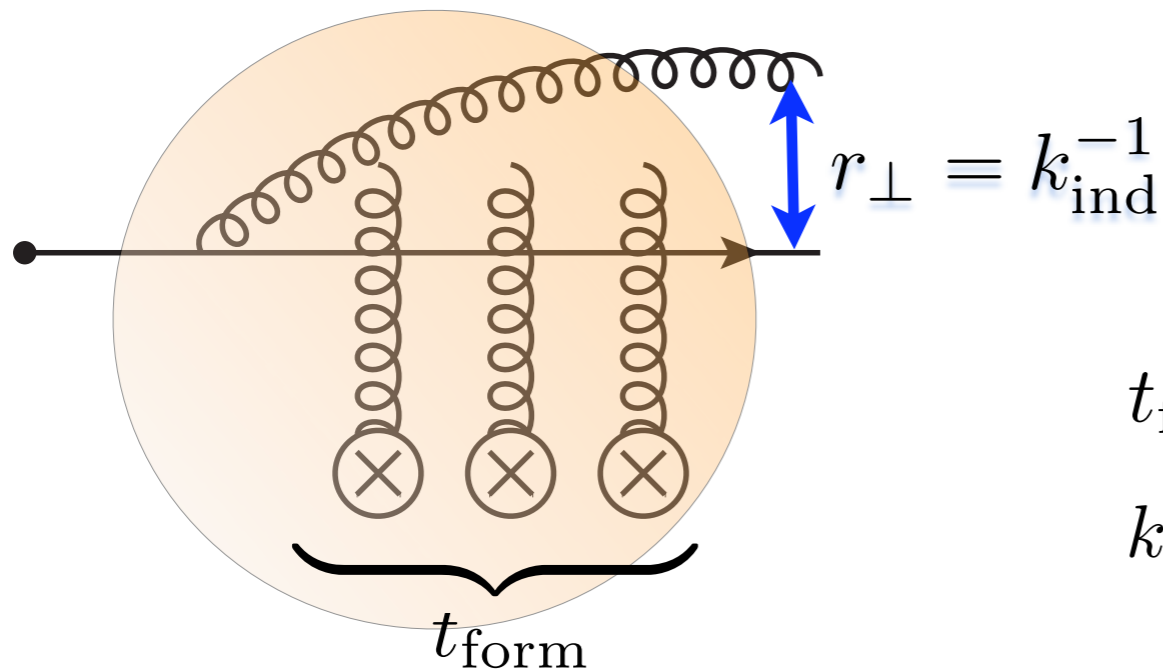
LPM effect in QCD:

- spectrum suppressed $t_{\text{form}} \gg L$

Baier, Dokshitzer, Mueller, Peigné, Schiff (1997-2000), Zakharov (1996)



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Local transport parameter(s): $\hat{q}(t) = \frac{d\langle p_{\perp}^2 \rangle}{dt}$

Baier, Dokshitzer, Mueller, Peigné, Schiff (1997-2000), Zakharov (1996)

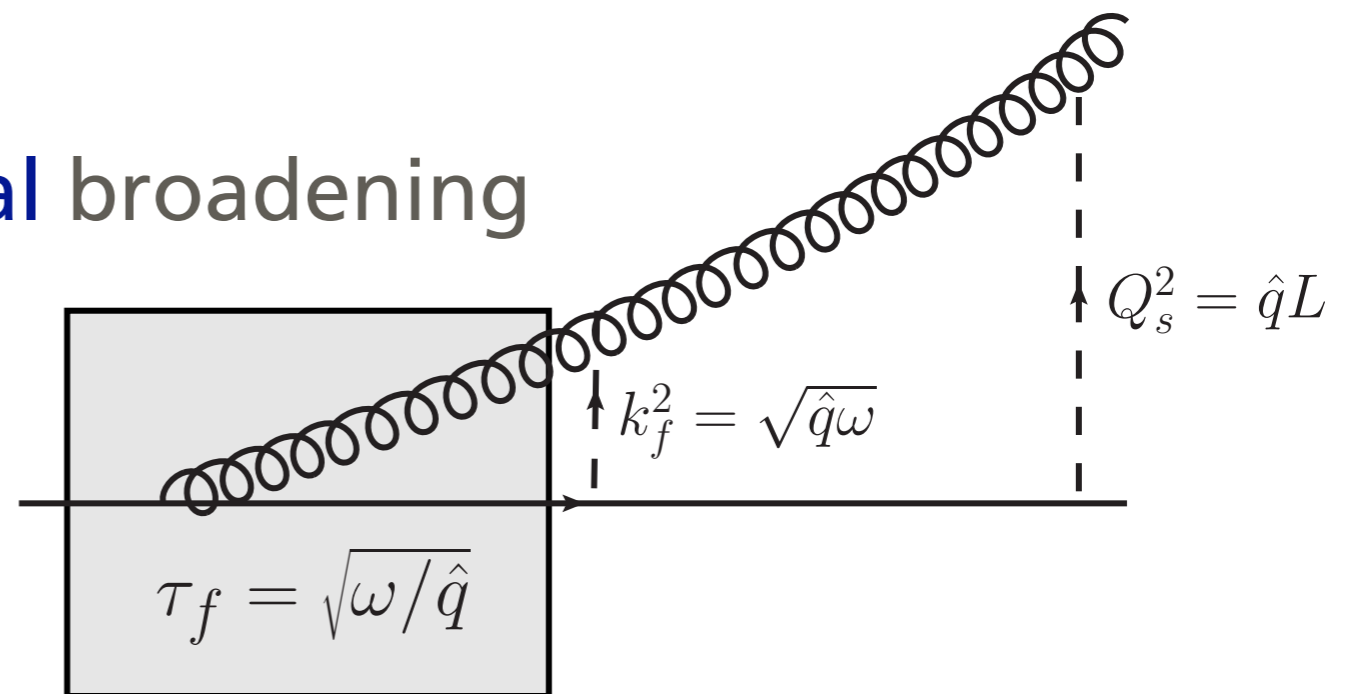


Induced gluon spectrum

$$\mathcal{R}_q \simeq 4\omega \int_0^L dt \int \frac{d^2 \mathbf{k}'}{(2\pi)^2} \mathcal{P}(\mathbf{k} - \mathbf{k}', L - t) \sin\left(\frac{\mathbf{k}'^2}{2\sqrt{\hat{q}\omega}}\right) \exp\left(-\frac{\mathbf{k}'^2}{2\sqrt{\hat{q}\omega}}\right)$$

Two step process

- **quantum** emission + **classical** broadening
- emission all along L
- collinear safe!
- basis for **phenomenology!**



Mehtar-Tani, Salgado, KT arXiv:1205:5739



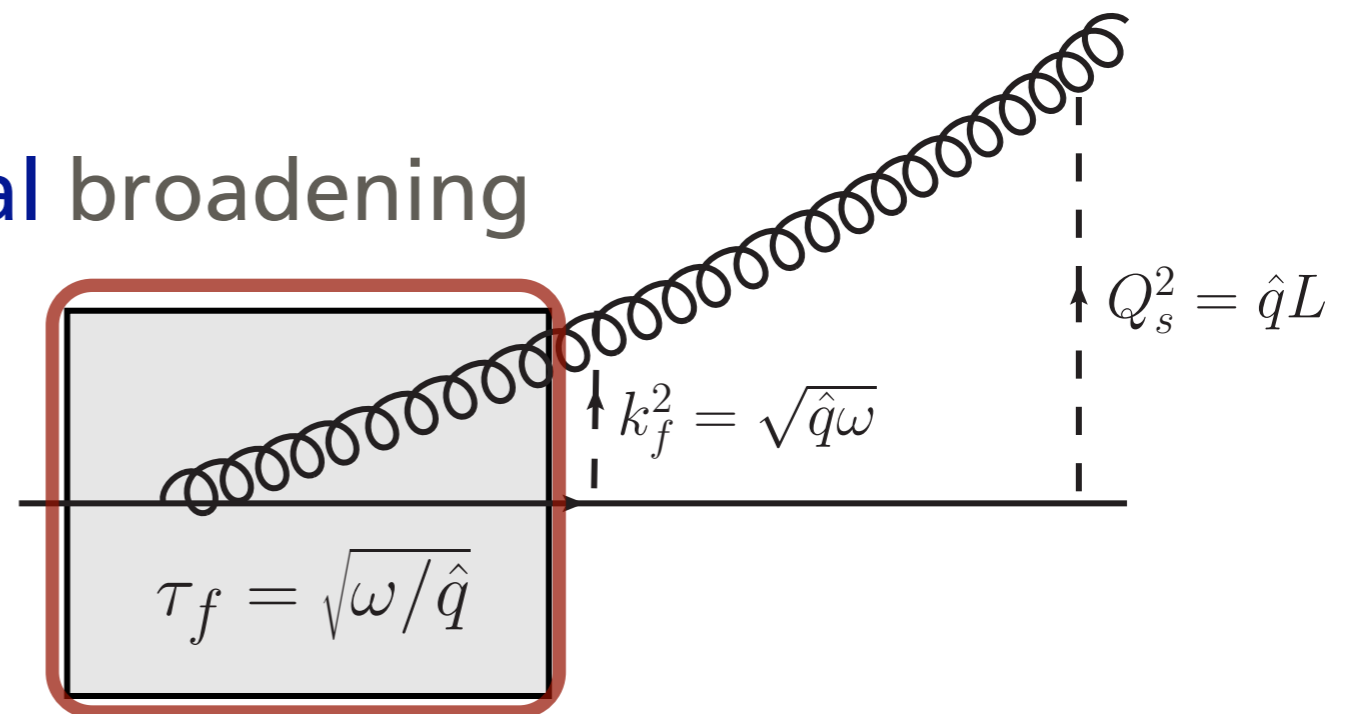
Induced gluon spectrum

$$\mathcal{R}_q \simeq 4\omega \int_0^L dt \int \frac{d^2 \mathbf{k}'}{(2\pi)^2} \mathcal{P}(\mathbf{k} - \mathbf{k}', L - t) \sin\left(\frac{\mathbf{k}'^2}{2\sqrt{\hat{q}\omega}}\right) \exp\left(-\frac{\mathbf{k}'^2}{2\sqrt{\hat{q}\omega}}\right)$$

quantum emission of gluon with mom. \mathbf{k}'

Two step process

- **quantum** emission + **classical** broadening
- emission all along L
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Mehtar-Tani, Salgado, KT arXiv:1205:5739



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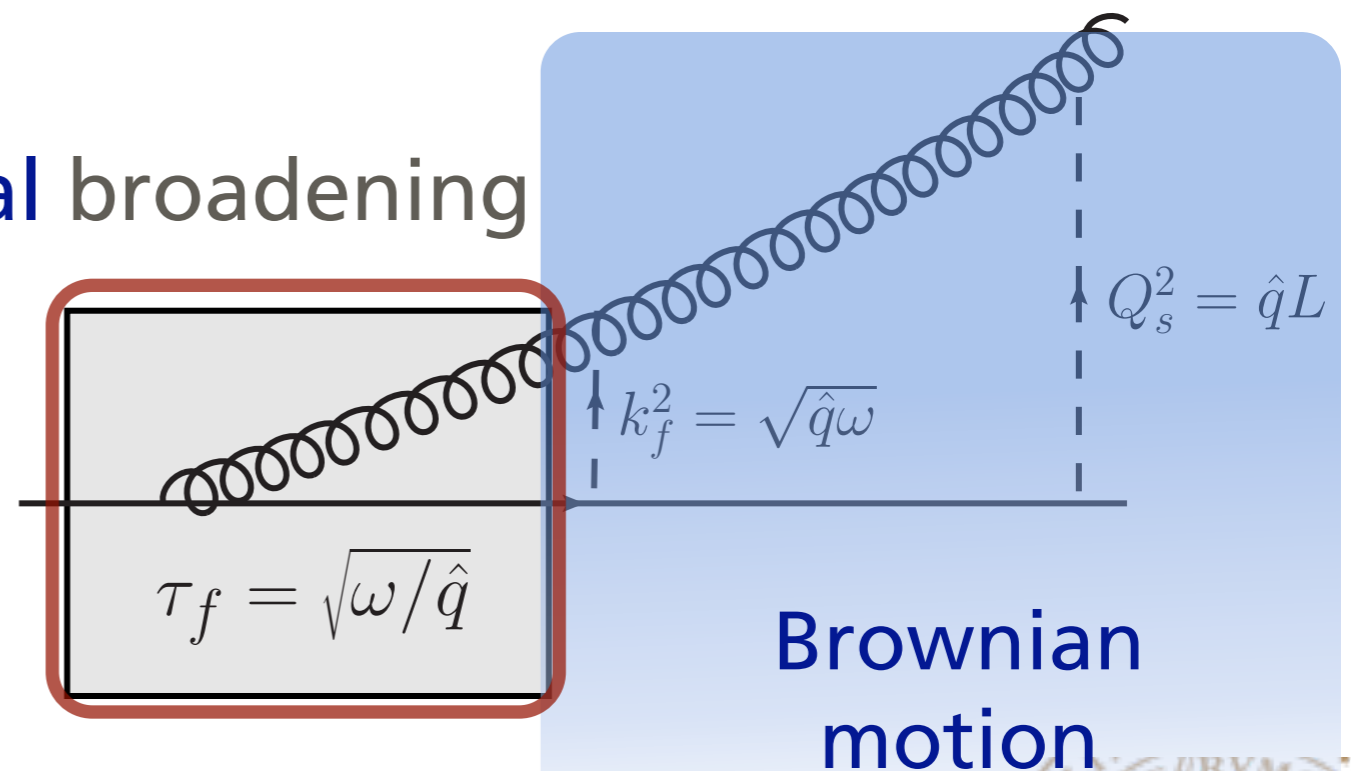
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prob. of acquiring
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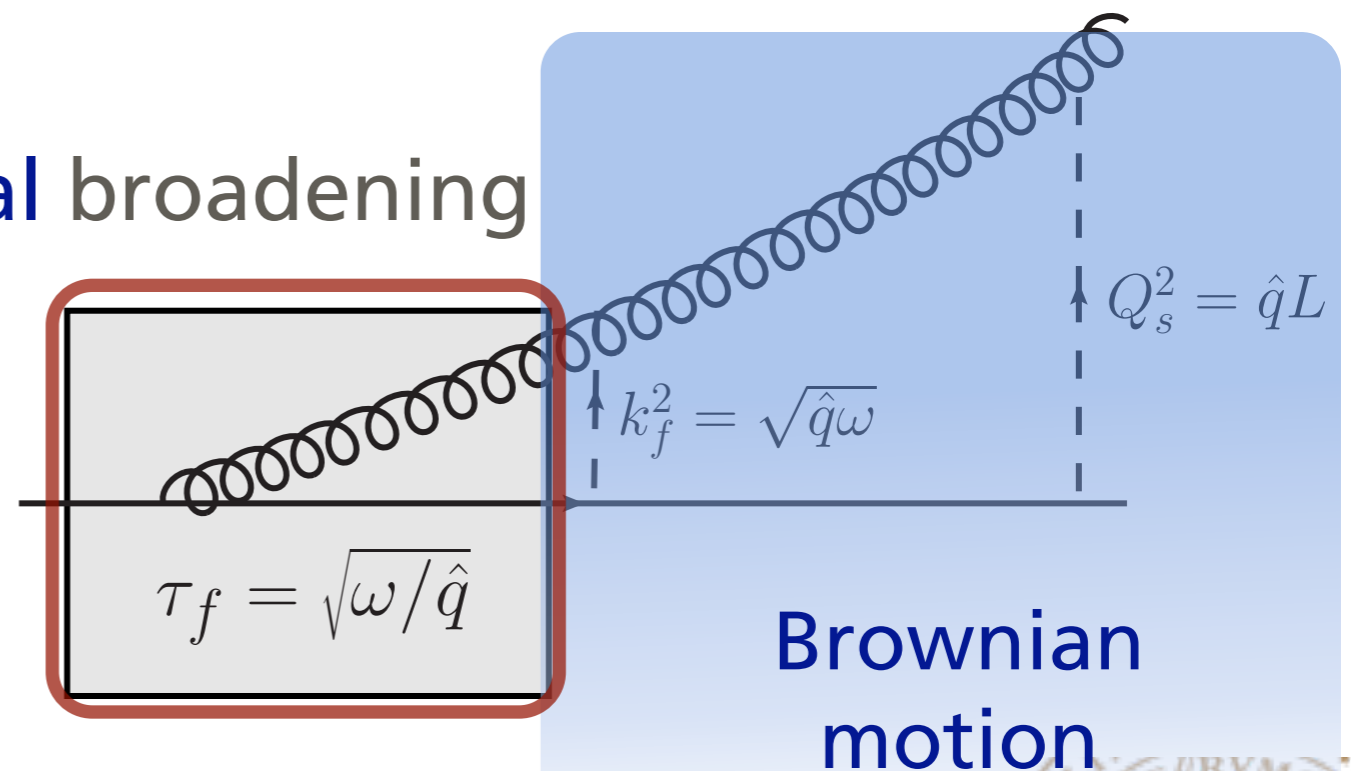
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...a missing
ingredient...



Mehtar-Tani, Salgado, KT arXiv:1205:5739



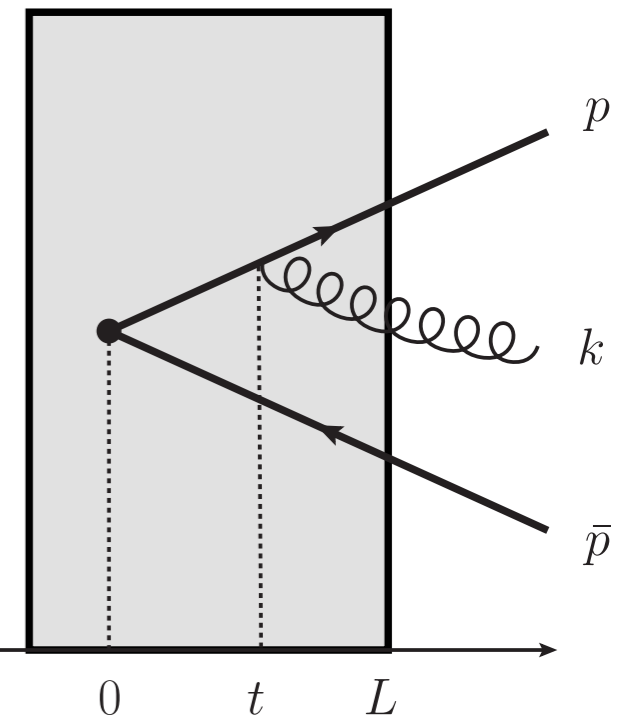
Multiple emitters in medium

Mehtar-Tani, Salgado, KT PRL106 (2011) 122002, PLB 707 (2011) 156, JHEP 1204 (2012) 064

Casalderrey-Solana, Iancu JHEP 1108 (2011) 015

Armesto, Ma, Mehtar-Tani, Salgado, KT JHEP 1201 (2012) 019

- need **more emitters** to see coherence
- first step toward **multi-gluon emissions**
- calculating the interference spectrum



$$\begin{aligned}
 \mathcal{J} = & \operatorname{Re} \int_0^\infty dt' \int_0^{t'} dt (1 - \Delta_{\text{med}}(t, 0)) \\
 & \times \int d^2 \mathbf{z} \exp \left[-i \bar{\mathbf{k}} \cdot \mathbf{z} - \frac{1}{2} \int_t^\infty d\xi n(\xi) \sigma(\mathbf{z}) + i \frac{\omega}{2} \delta n^2 t \right] \\
 & \times (\partial_y - i \omega \delta \mathbf{n}) \cdot \partial_z \mathcal{K}(t', \mathbf{z}; t, \mathbf{y} | \omega) \Big|_{\mathbf{y} = \delta \mathbf{n} t} + \text{sym.}
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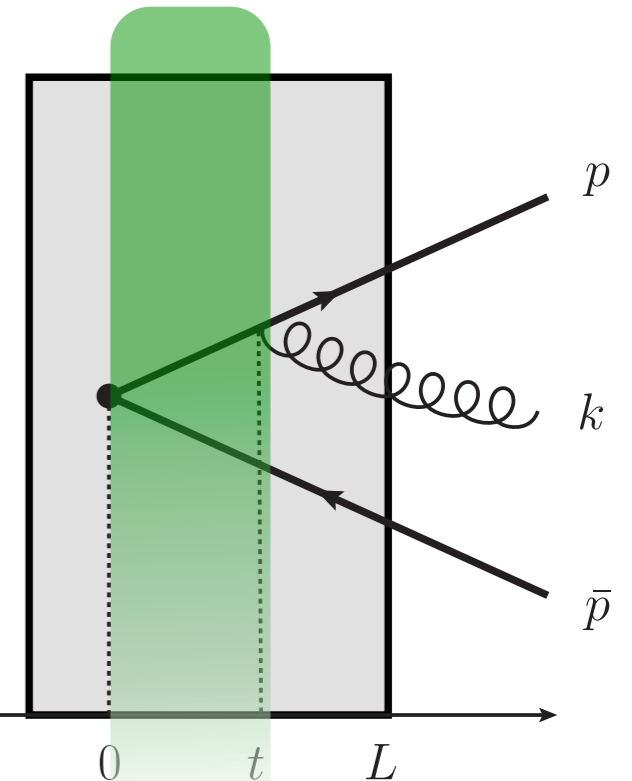
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Three stage process:

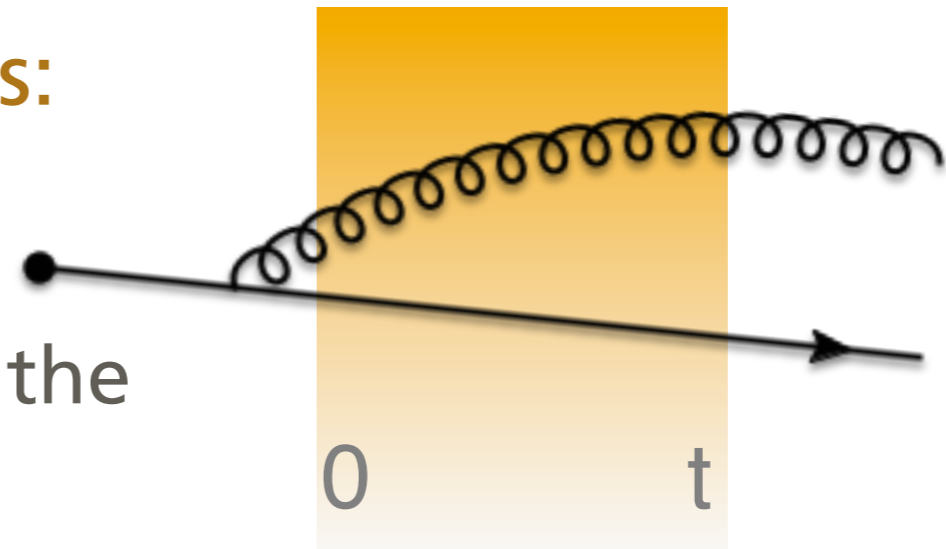
- **q \bar{q} propagation** + **gluon decoherence** + **gluon broadening**



Interferences: analysis

Importance of interferences:

- **condition:** color correlation between emitters
- what is the probability that the pair **remains correlated**?



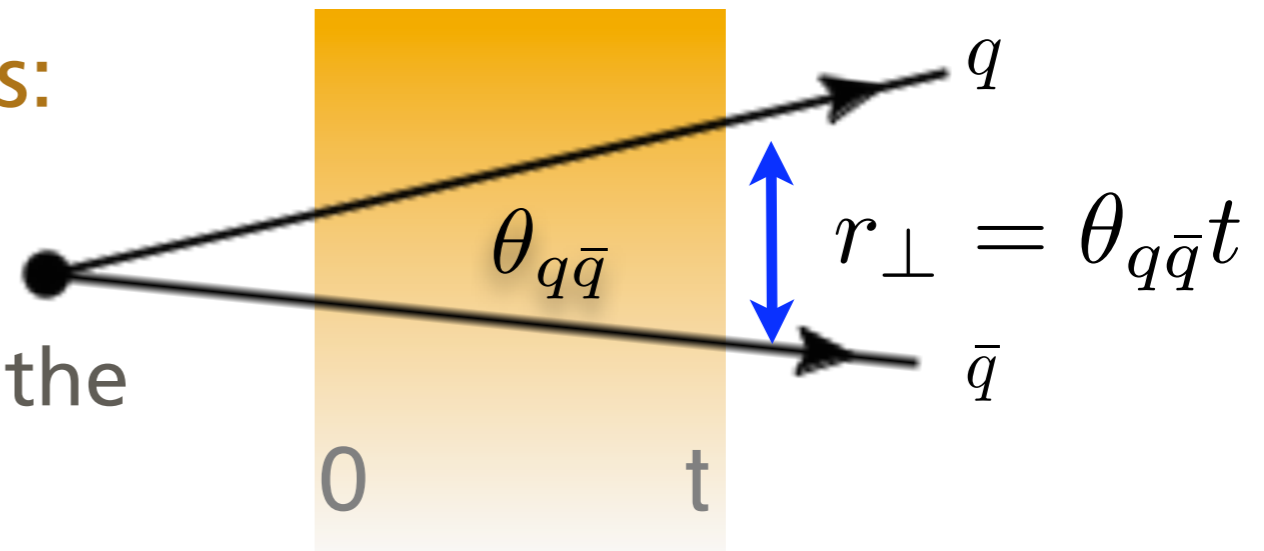
Mehtar-Tani, Salgado, KT *JHEP* 1204, 064; arXiv:1205.5739
Casalderrey-Solana, Iancu *JHEP* 1108 (2011) 015



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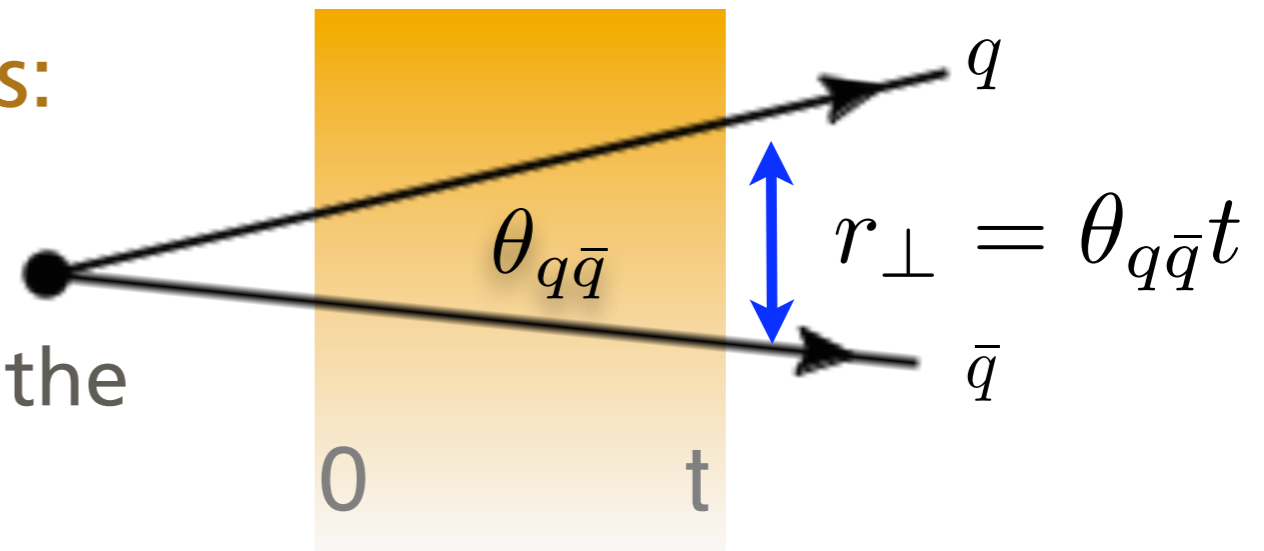
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decoherence parameter

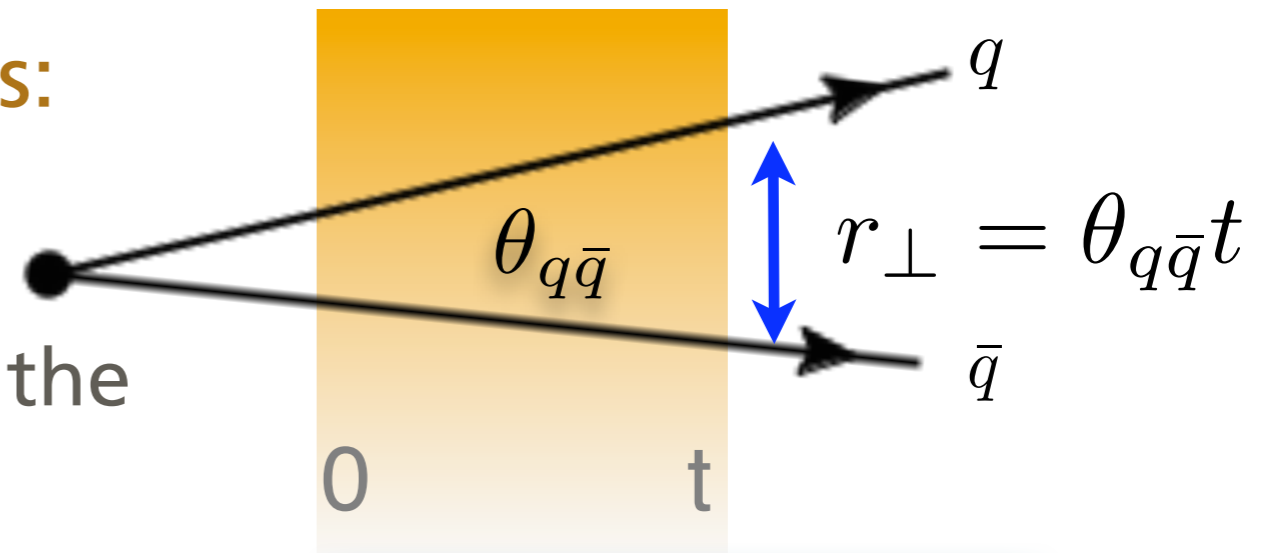
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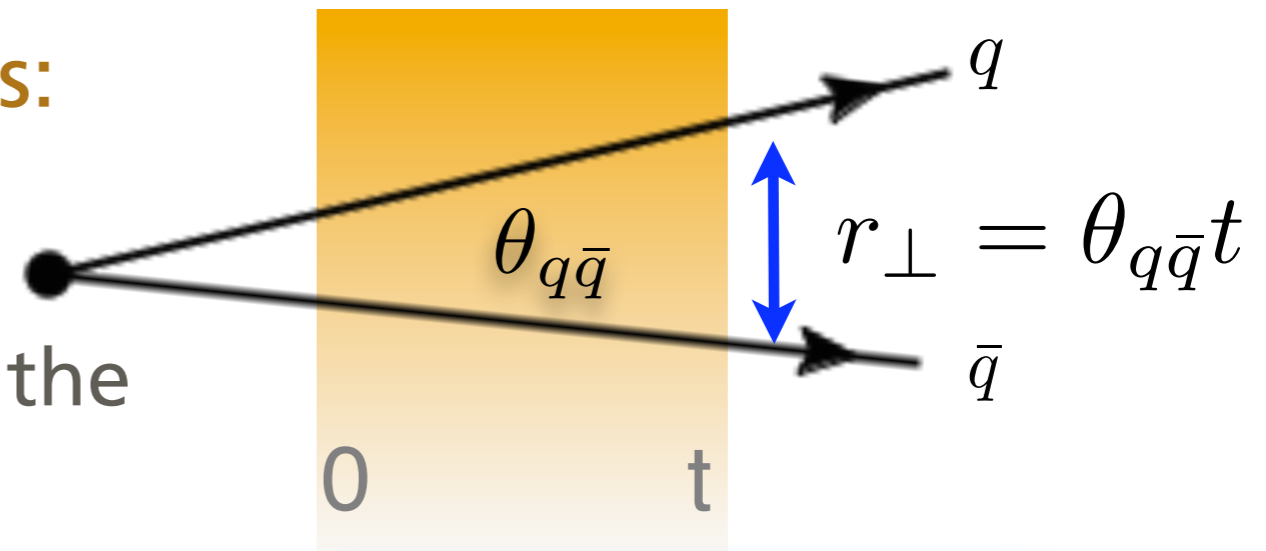
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- processes at $t > \tau_d$: independent radiation
- processes at **short timescales** sensitive to interferences

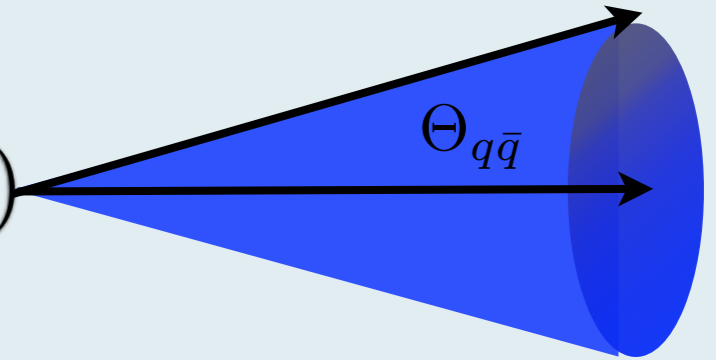
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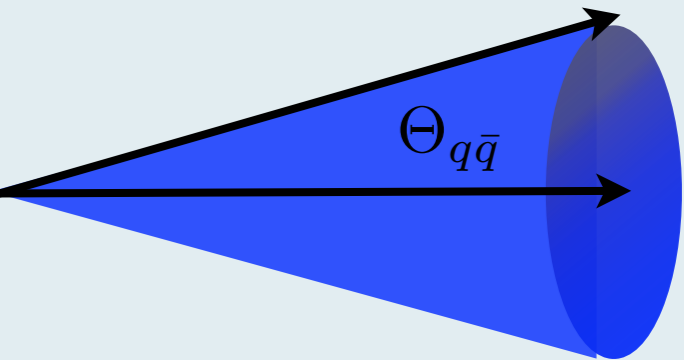
Vacuum: a reminder

$$\langle dN_q \rangle_\varphi = \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{d\theta}{\theta} \Theta(\cos \theta - \cos \theta_{q\bar{q}})$$

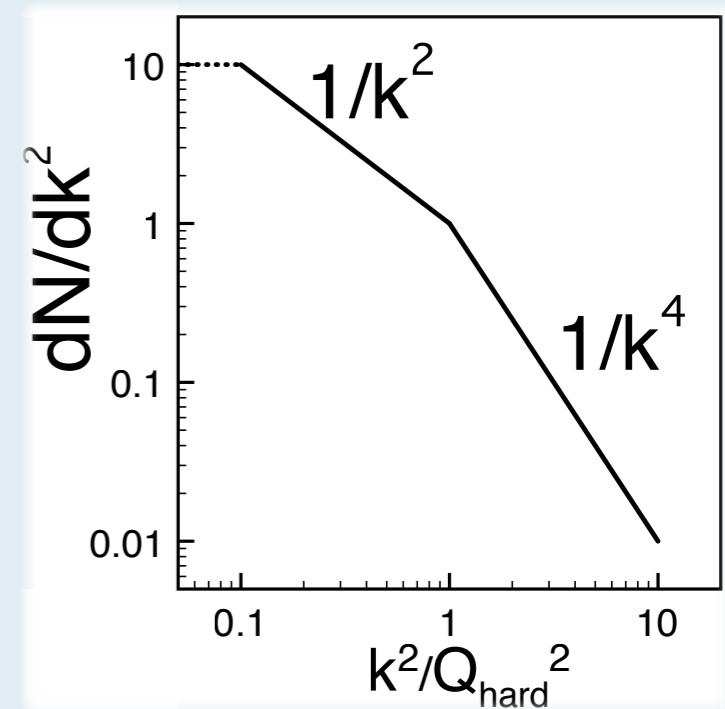


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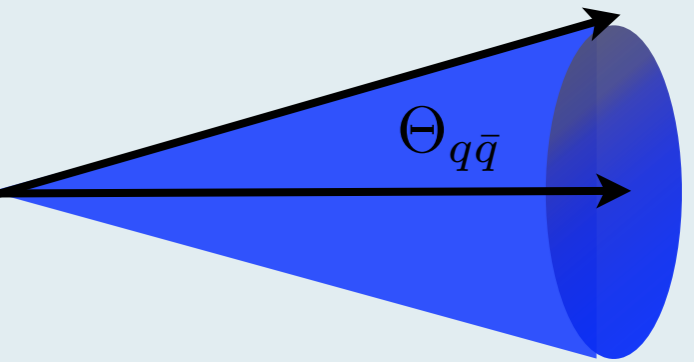


$$\omega \frac{dN_{\gamma^*}}{d^3 k} = \frac{\alpha_s C_F}{\pi} \begin{cases} \frac{1}{k^2} & \mathbf{k} \ll \delta \mathbf{k}, \text{ or } \theta \ll \theta_{q\bar{q}} \\ \frac{\delta k^2}{k^4} & \mathbf{k} \gg \delta \mathbf{k}, \text{ or } \theta \gg \theta_{q\bar{q}} \end{cases}$$

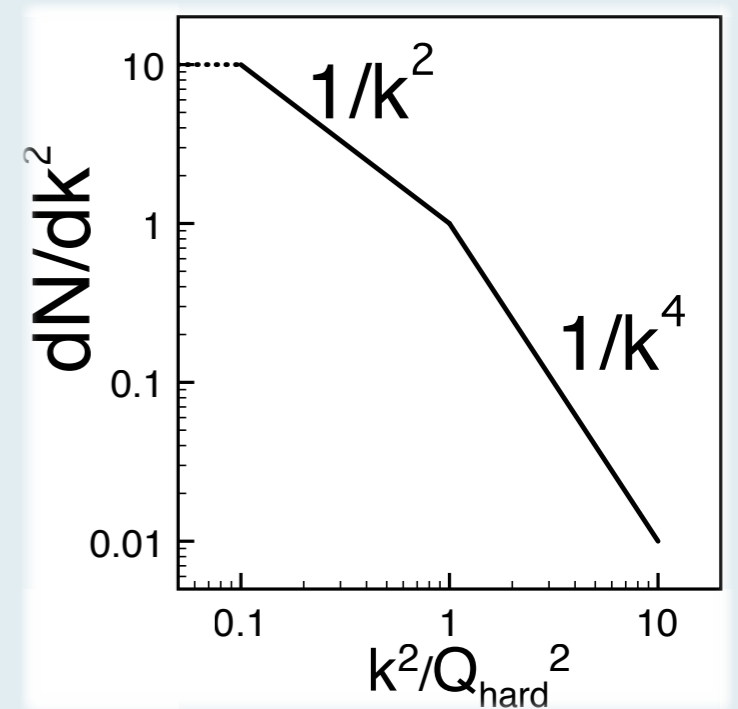


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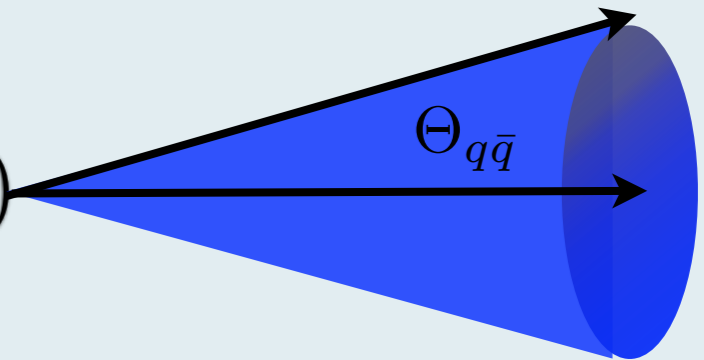
Hard scale of the problem: $|\delta \mathbf{k}| \simeq \omega \theta_{q\bar{q}}$

- determines the **maximal transverse momentum** of gluons

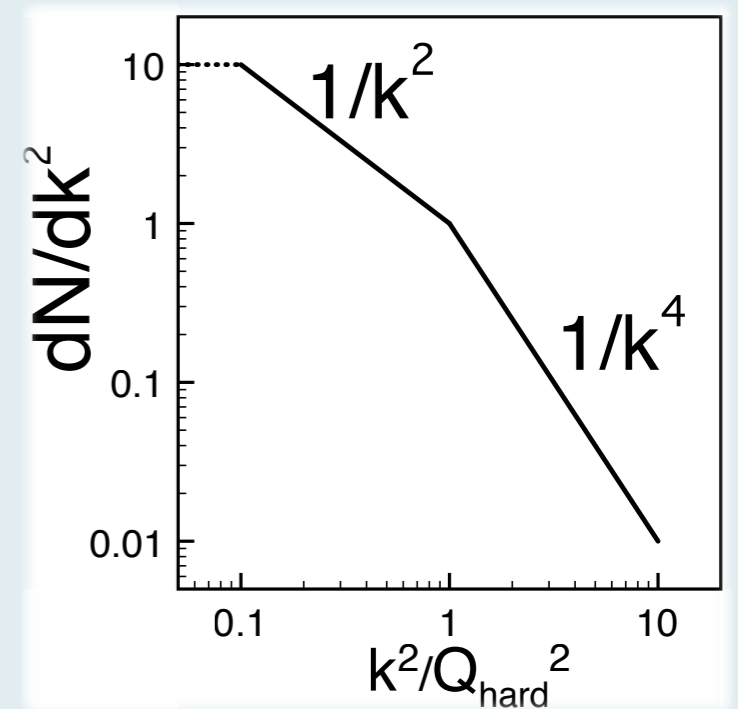


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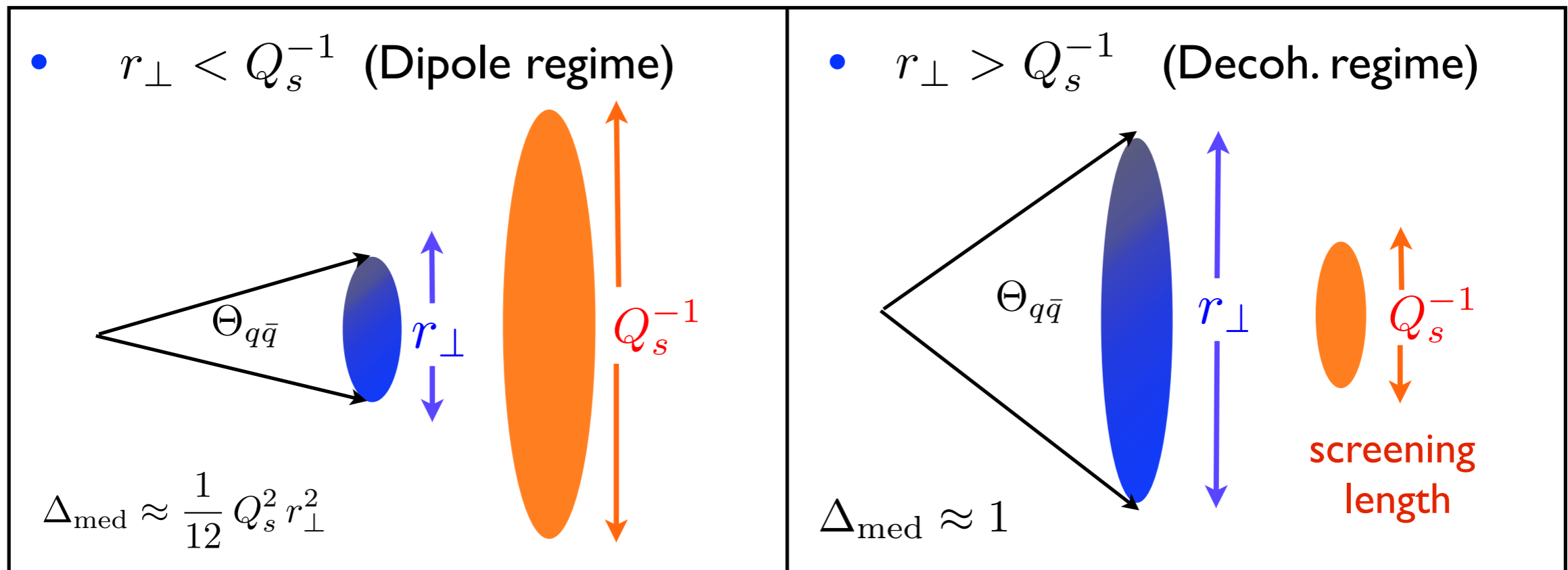
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What are the relevant hard scales in the medium?



Hard scale analysis



$$\Delta_{\text{med}} \approx 1 - \exp\left[-\frac{1}{12} Q_s^2 r_{\perp}^2\right]$$

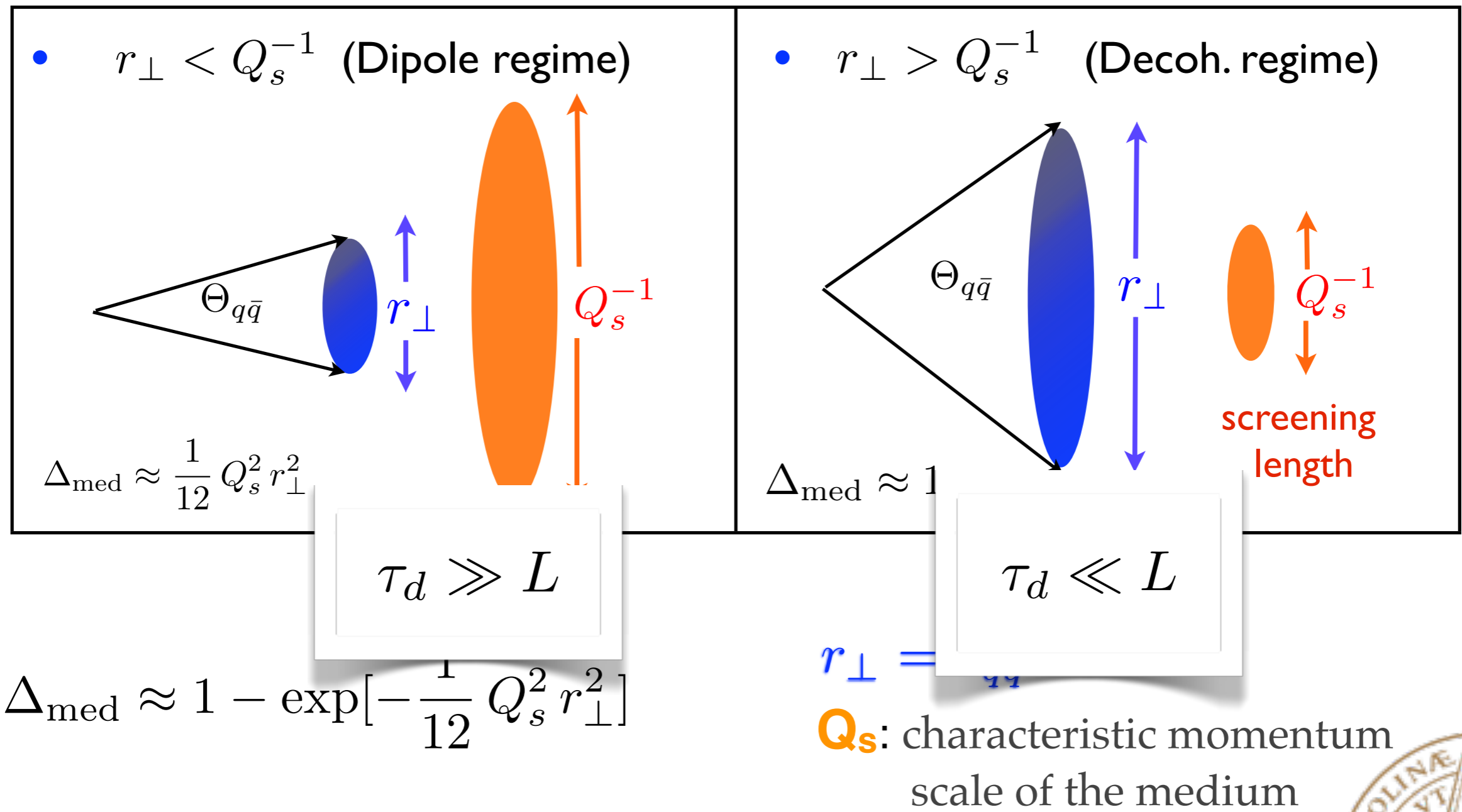
$$r_{\perp} = \theta_{q\bar{q}} L$$

Q_s : characteristic momentum scale of the medium

Mehtar-Tani, Salgado, KT JHEP 1204 (2012) 064



Hard scale analysis



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$$r_\perp = \dots$$

Q_s : characteristic momentum scale of the medium



Finite energies

Hard scale of the problem: $Q_{\text{hard}} = \max(r_{\perp}^{-1}, Q_s, \delta\mathbf{k})$

$k_{\perp} > Q_{\text{hard}}$: coherence!

Mehtar-Tani, Salgado, KT JHEP 1204 (2012) 064

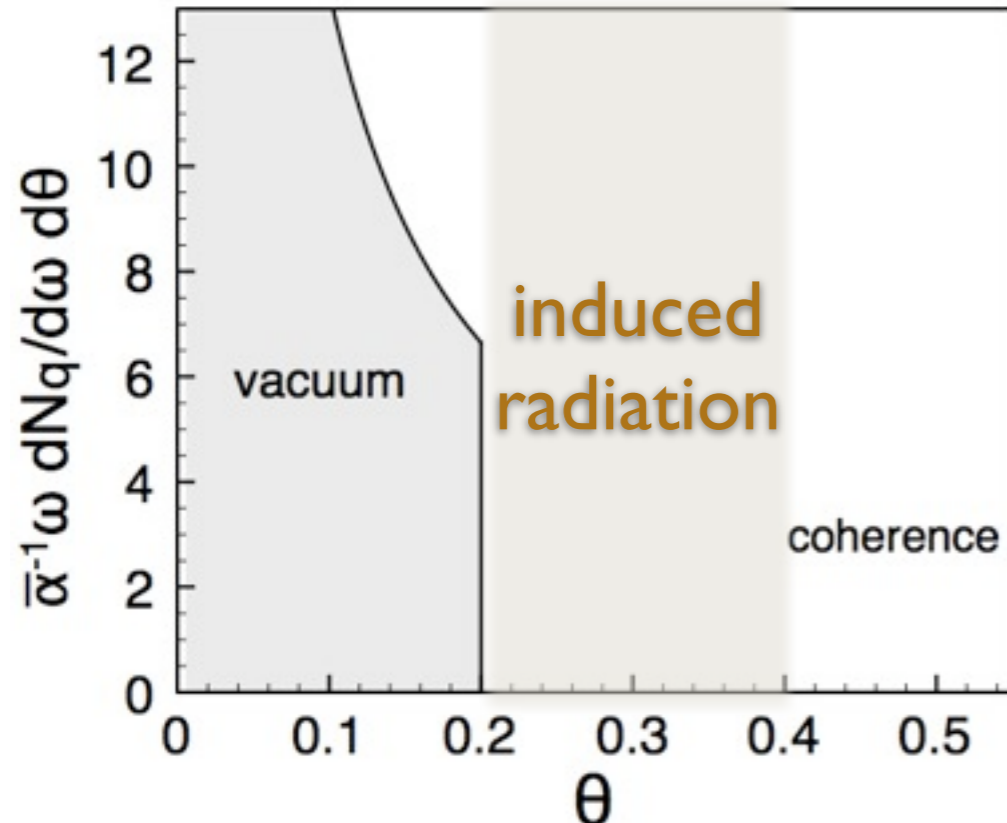


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$\theta > Q_{\text{hard}}/\omega$: coherence!



Medium scales open phase space

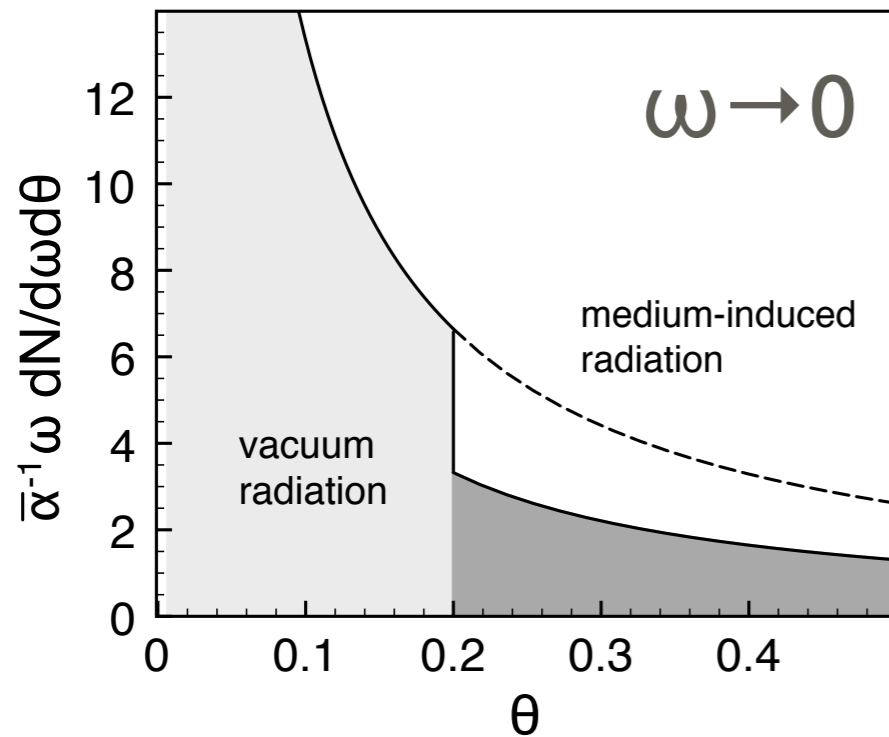
- "out-of-cone" radiation
- no interferences inside

Mehtar-Tani, Salgado, KT JHEP 1204 (2012) 064



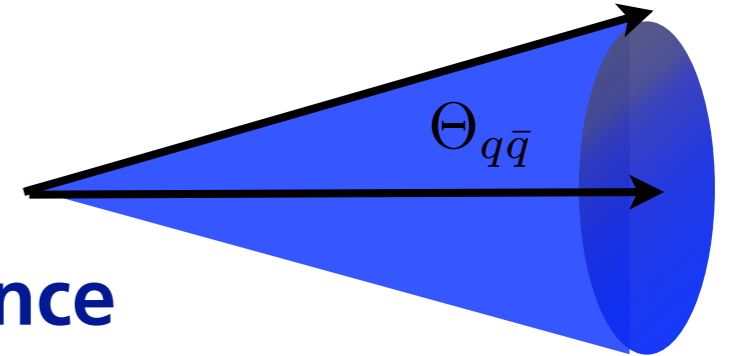
Onset of decoherence

- in the soft sector



$$\Delta_{\text{med}} \rightarrow 0$$

Coherence

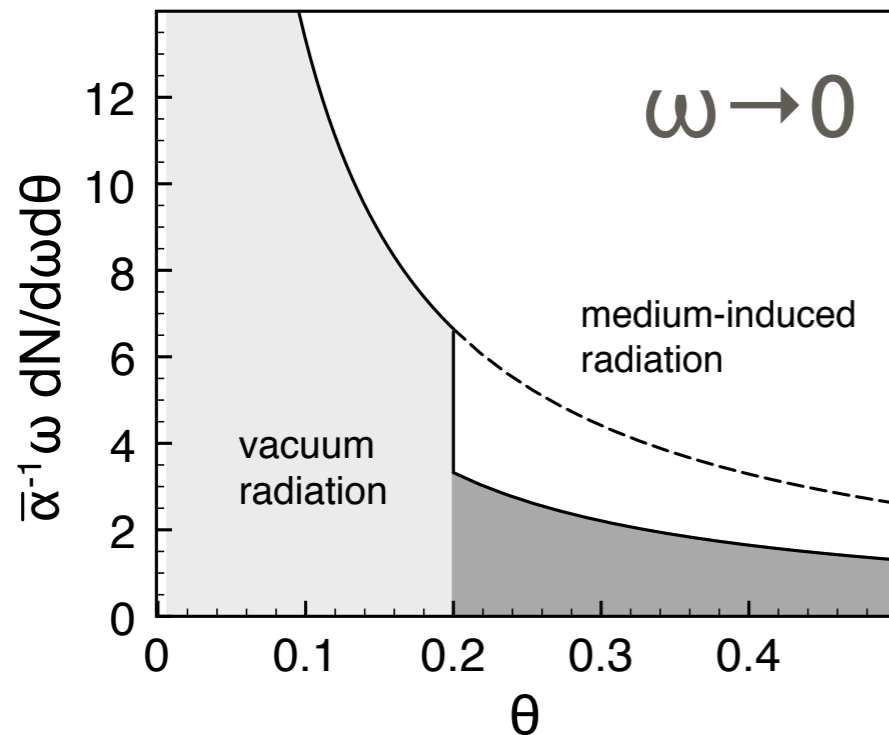


Mehtar-Tani, Salgado, KT PRL106 (2011) 122002; PLB 707 (2011) 156



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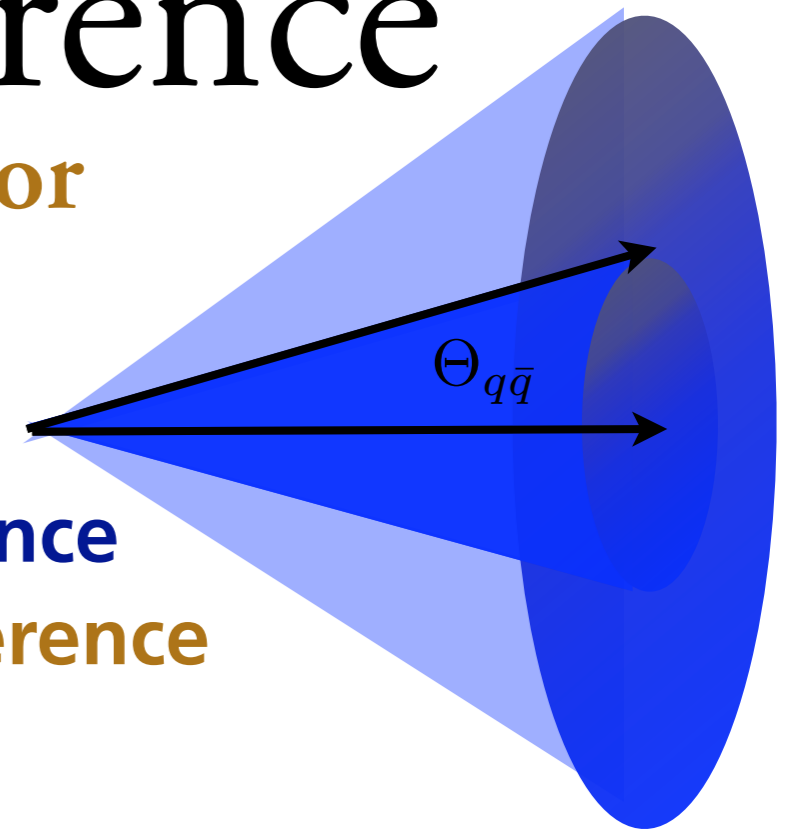


$$\Delta_{\text{med}} \rightarrow 0$$

$$\Delta_{\text{med}} \rightarrow 1$$

Coherence

Decoherence

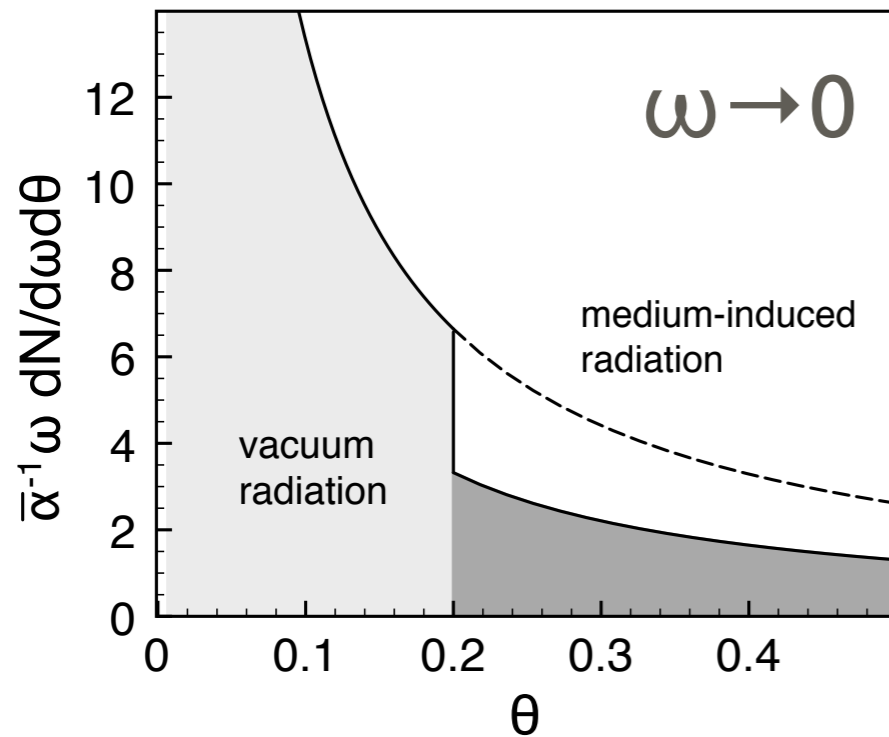


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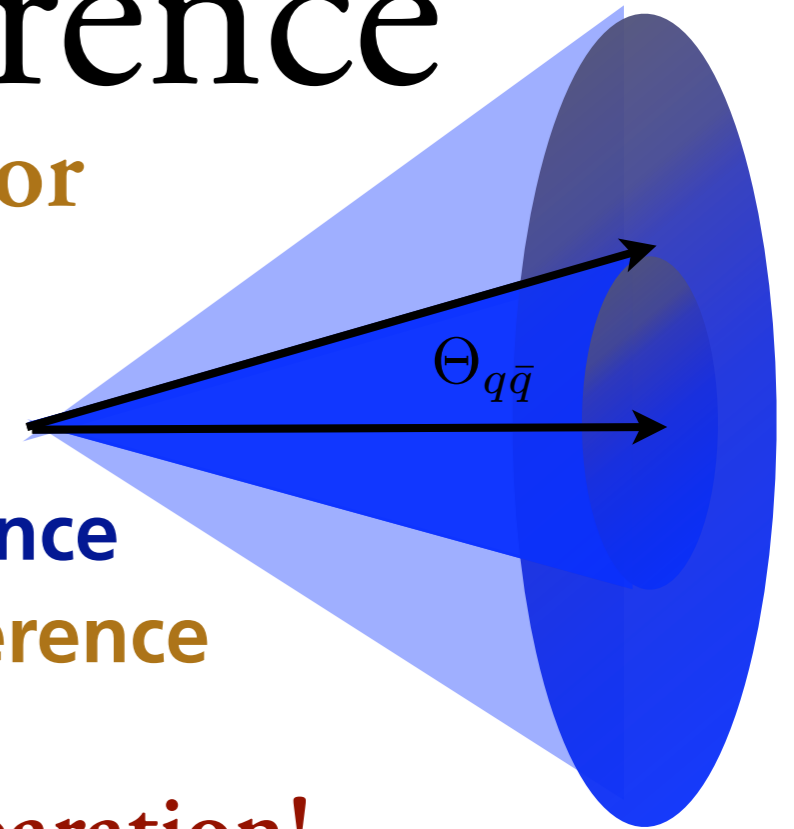
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Decoherence

Geometrical separation!

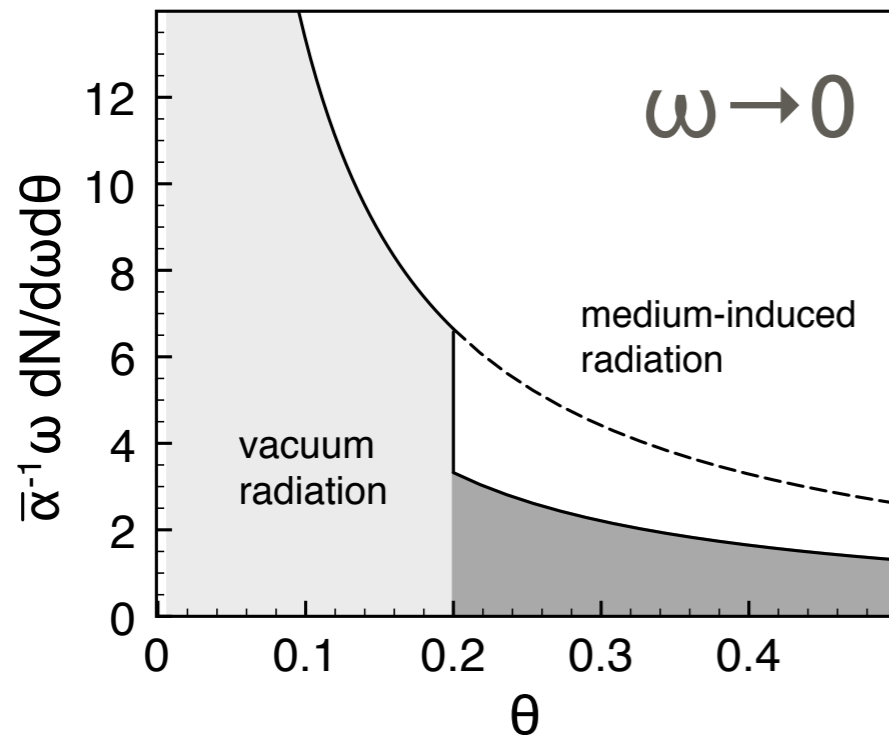


Mehtar-Tani, Salgado, KT PRL106 (2011) 122002; PLB 707 (2011) 156



Onset of decoherence

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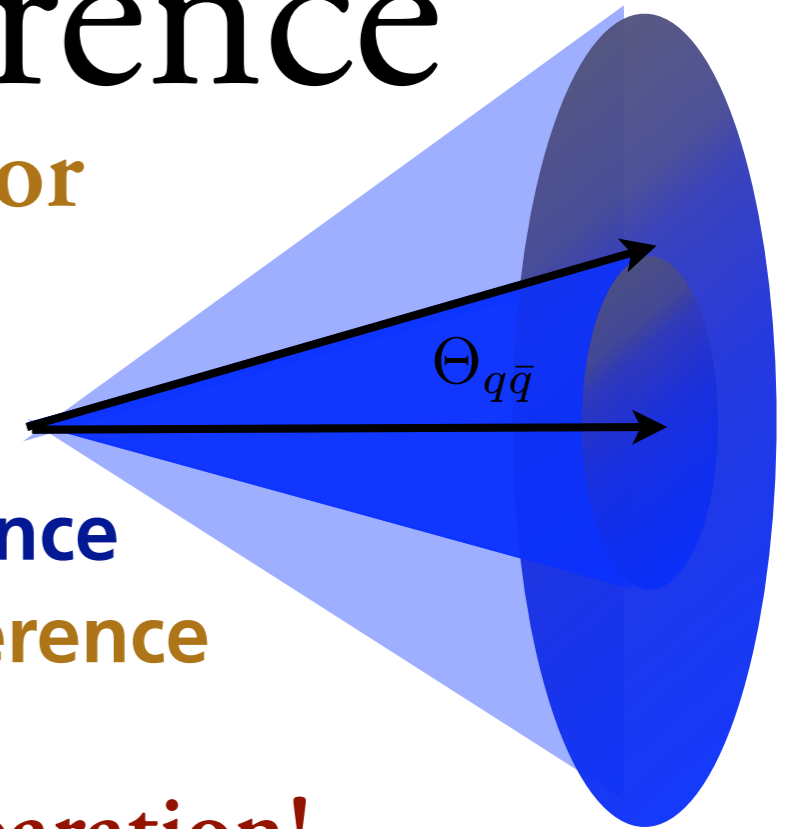
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Soft gluons with long formation times

- particles radiate independently
- "memory loss": no color correlation to parent

Mehtar-Tani, Salgado, KT PRL106 (2011) 122002; PLB 707 (2011) 156



Conclusions

- spectrum governed by the **hardest scale**
- establishing a understanding of jet dynamics in medium in terms of **hard scales**
- developing a space-time picture of radiation **inside the medium**
- from multiple emitters to **multiple emissions**



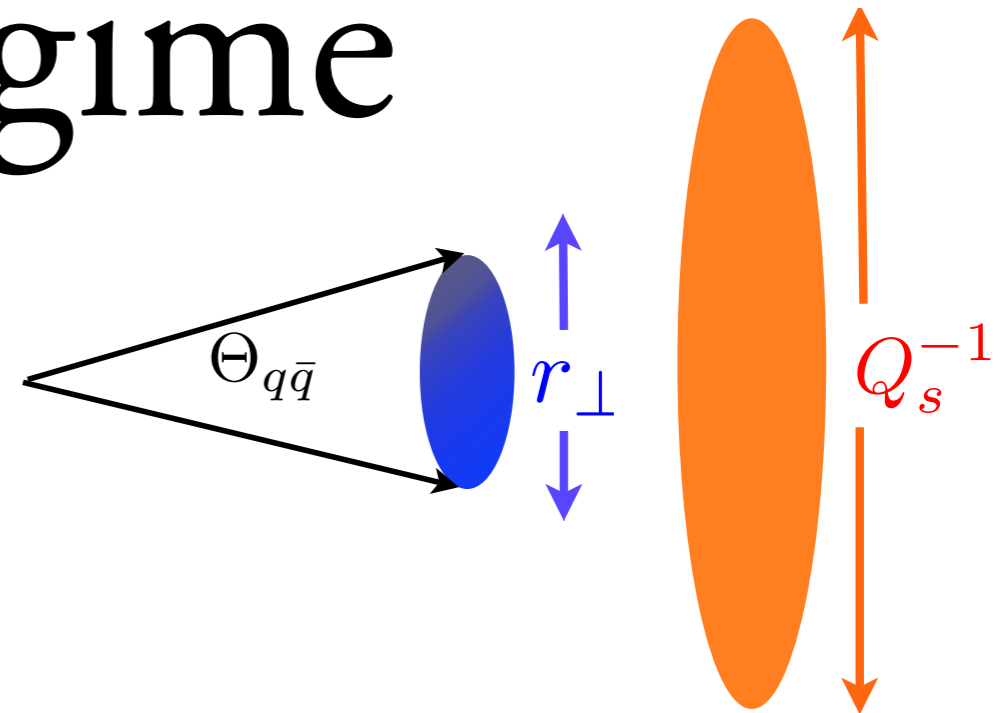
Backup



“Dipole” regime

Color transparency

- pair remains color correlated
- radiates coherently: **antiangular**
- **no medium-induced component!**



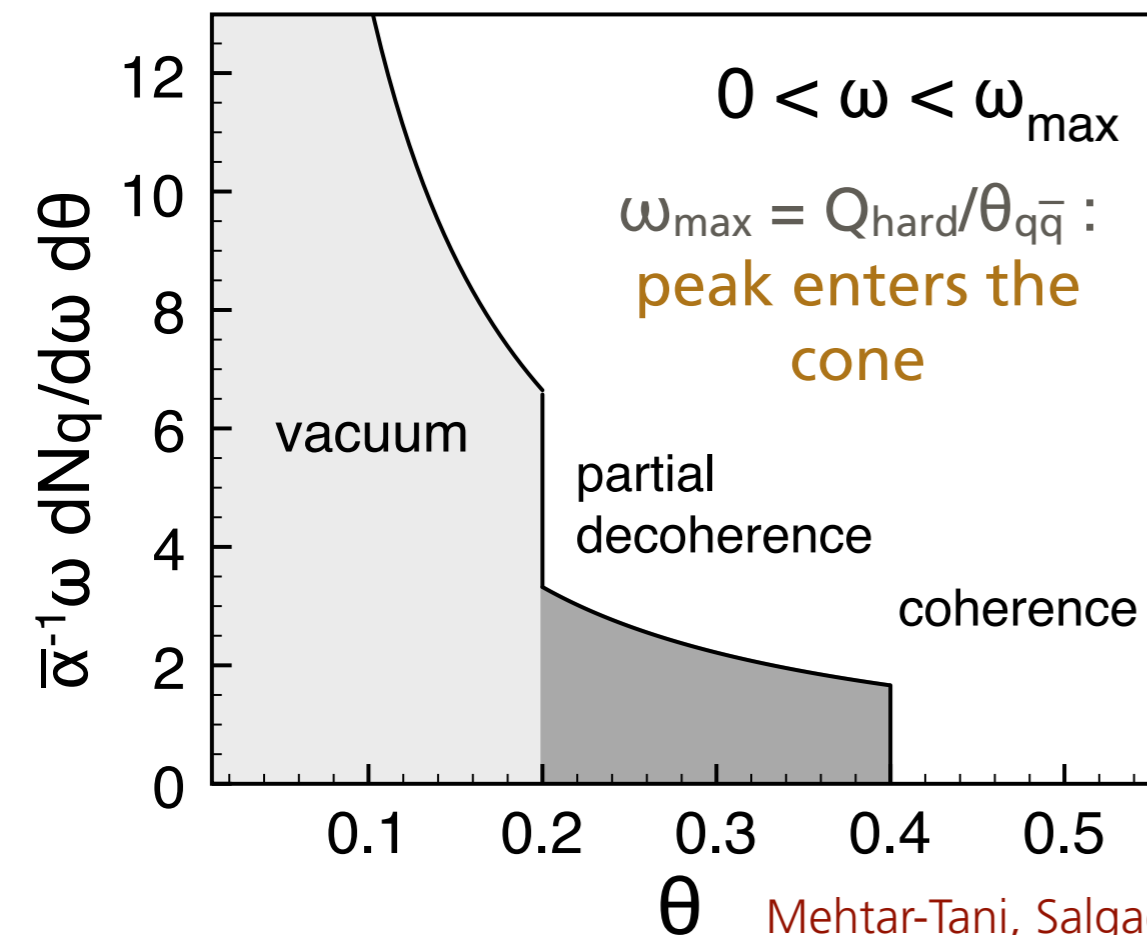
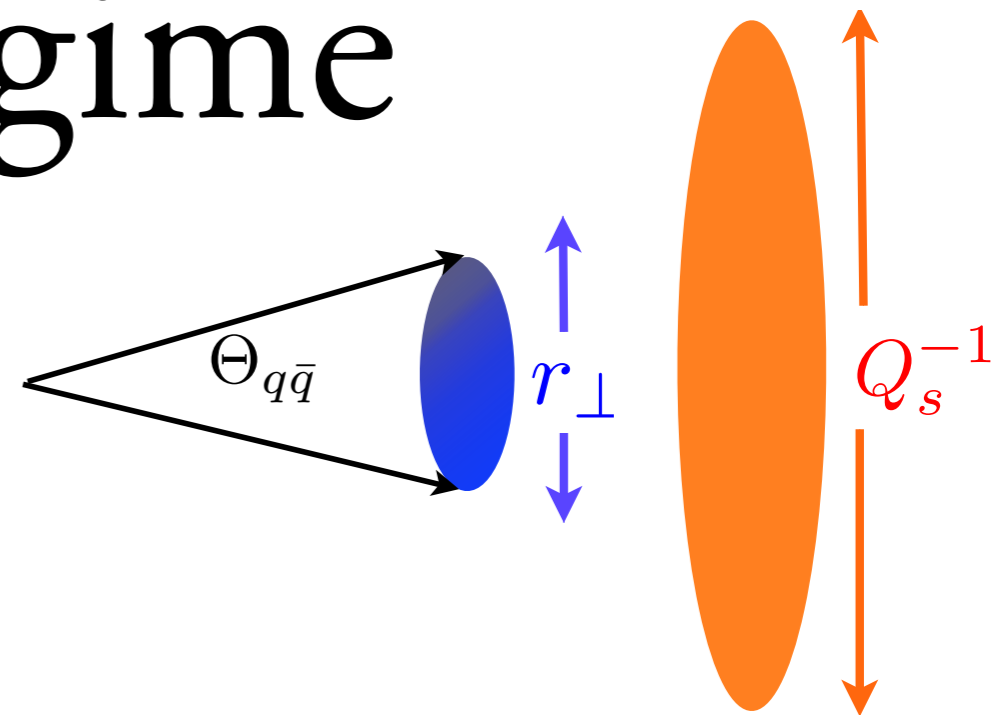
Mehtar-Tani, Salgado, KT PRL106 (2011) 122002, JHEP 1204 (2012) 064



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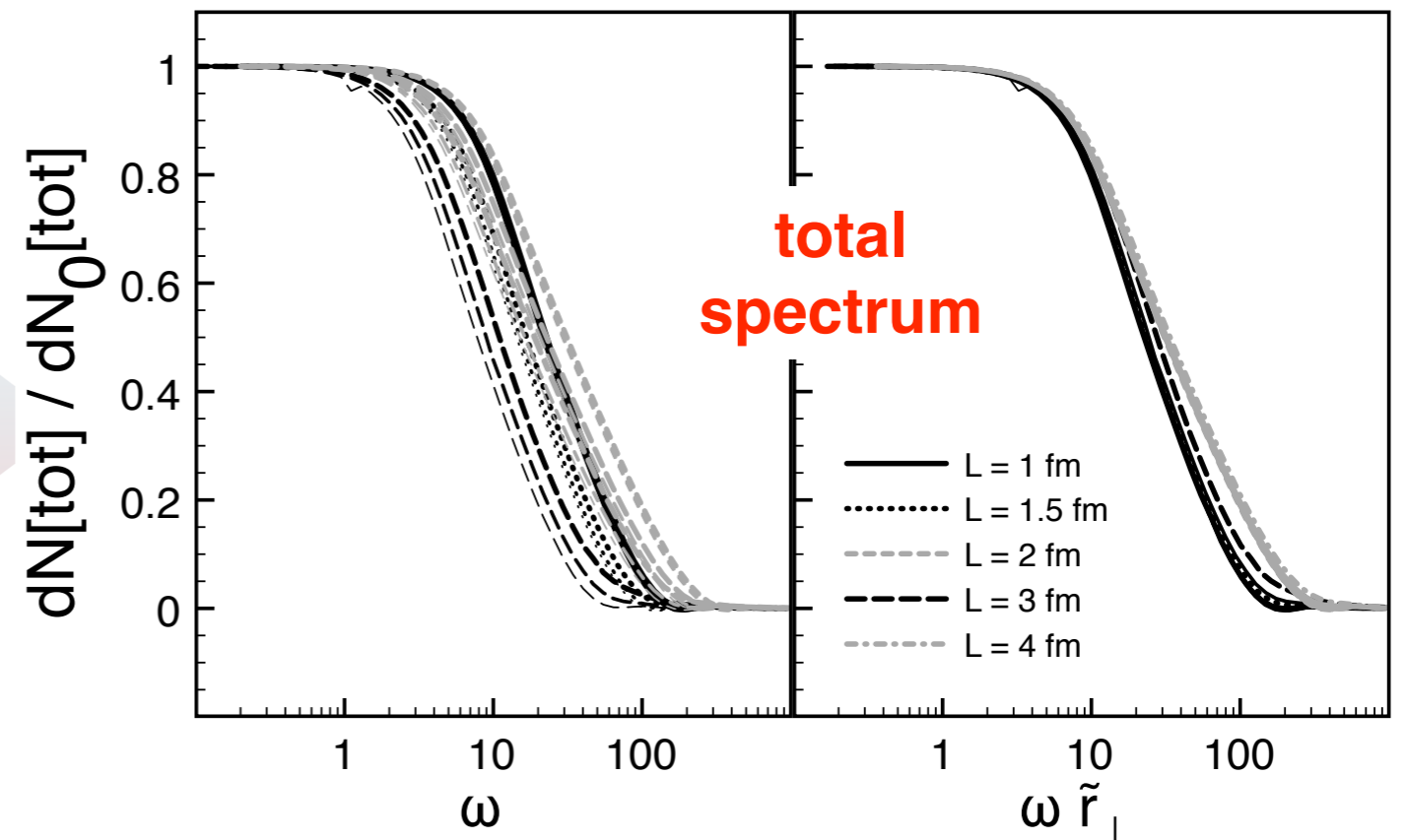
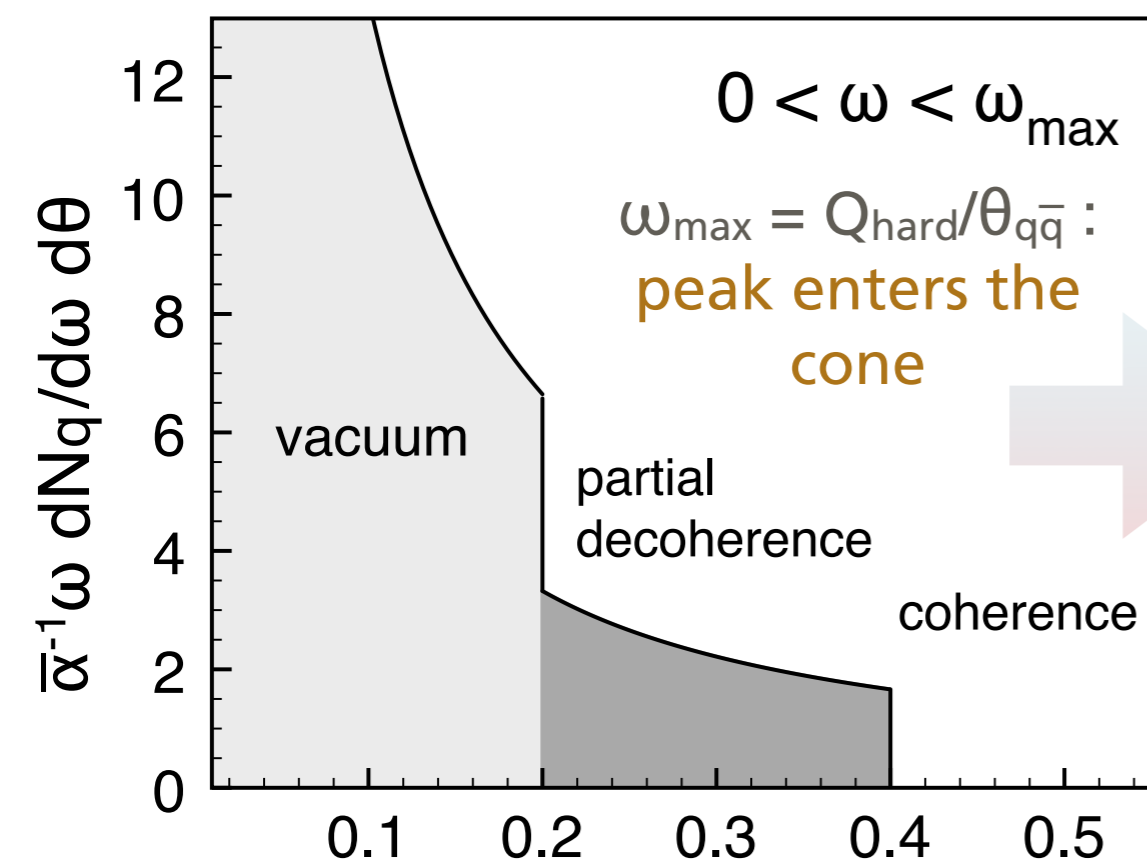
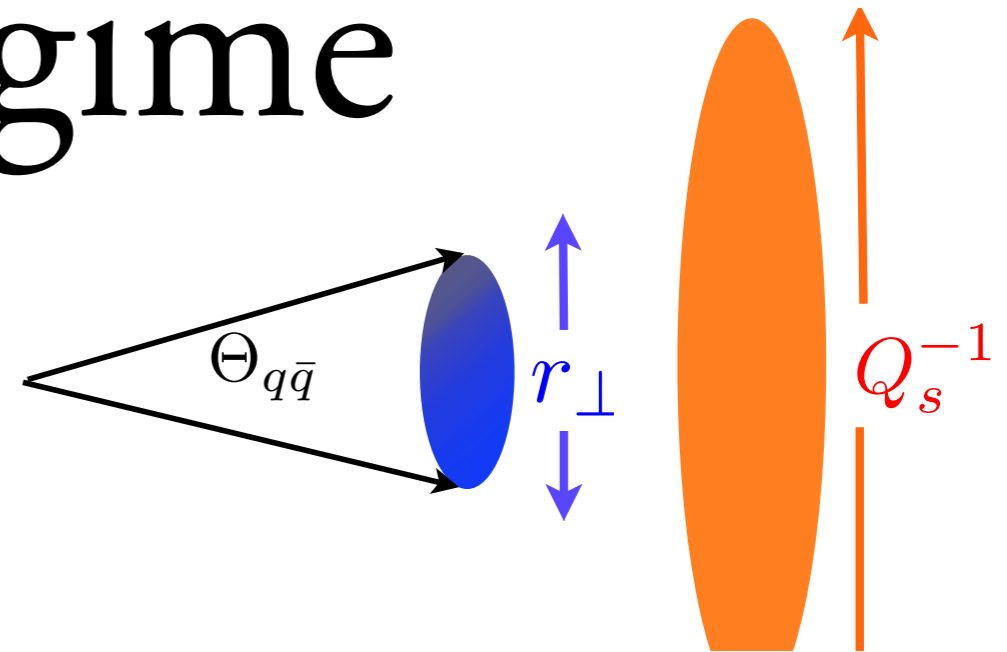
θ Mehtar-Tani, Salgado, KT PRL106 (2011) 122002, JHEP 1204 (2012) 064



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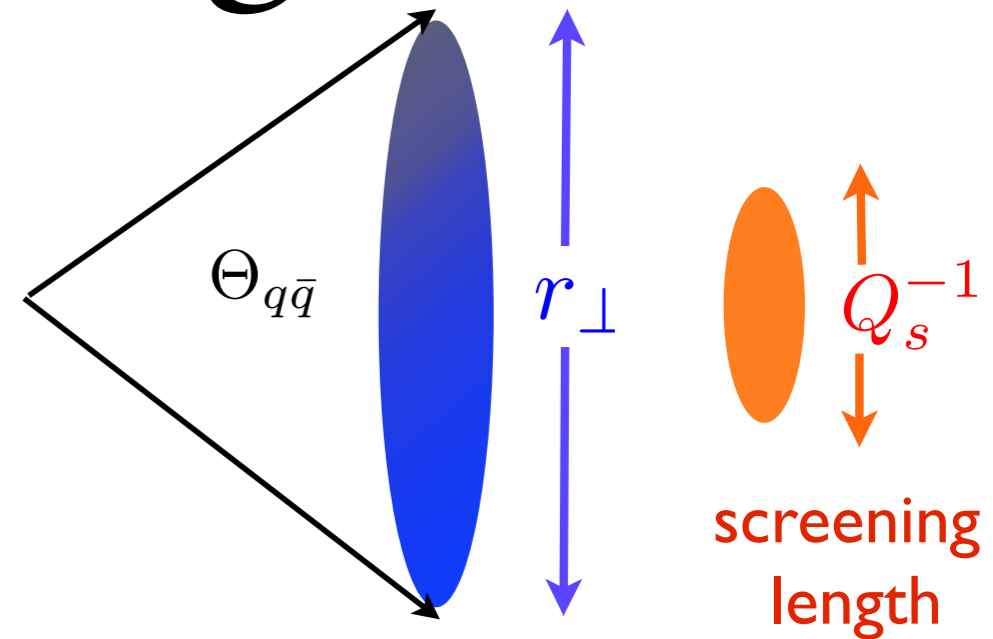
θ Mehtar-Tani, Salgado, *KT PRL*106 (2011) 122002, *JHEP* 1204 (2012) 064



“Decoherence” regime

Two-component spectrum

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- medium induces radiation off each of the legs independently
 - interferences scale like τ_d
- vacuum-radiation up to Q_s !



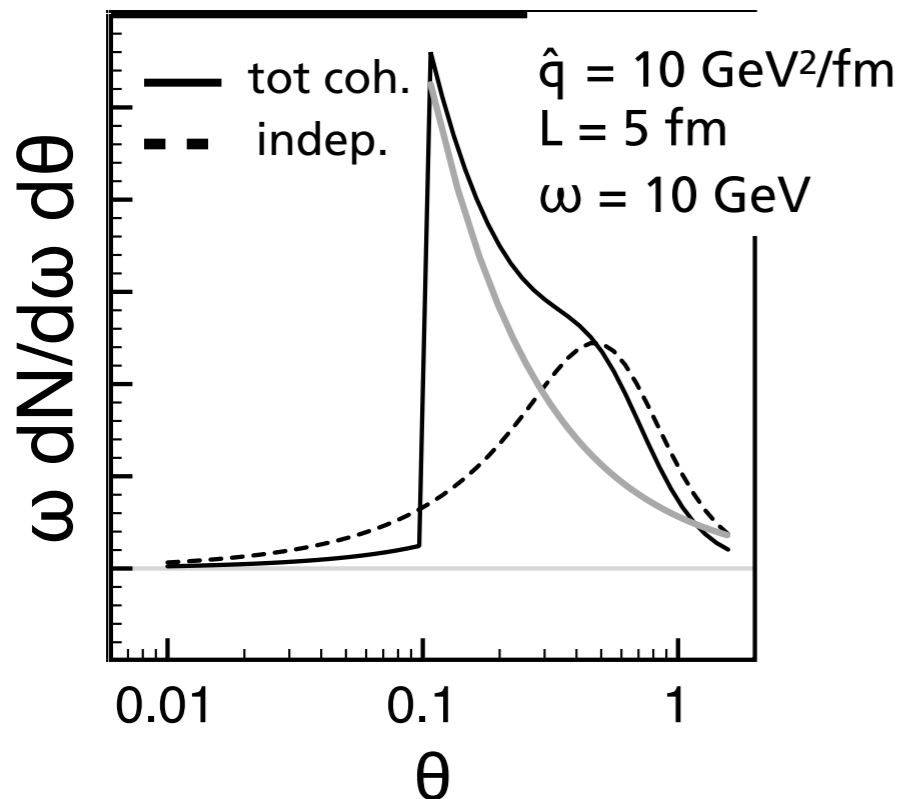
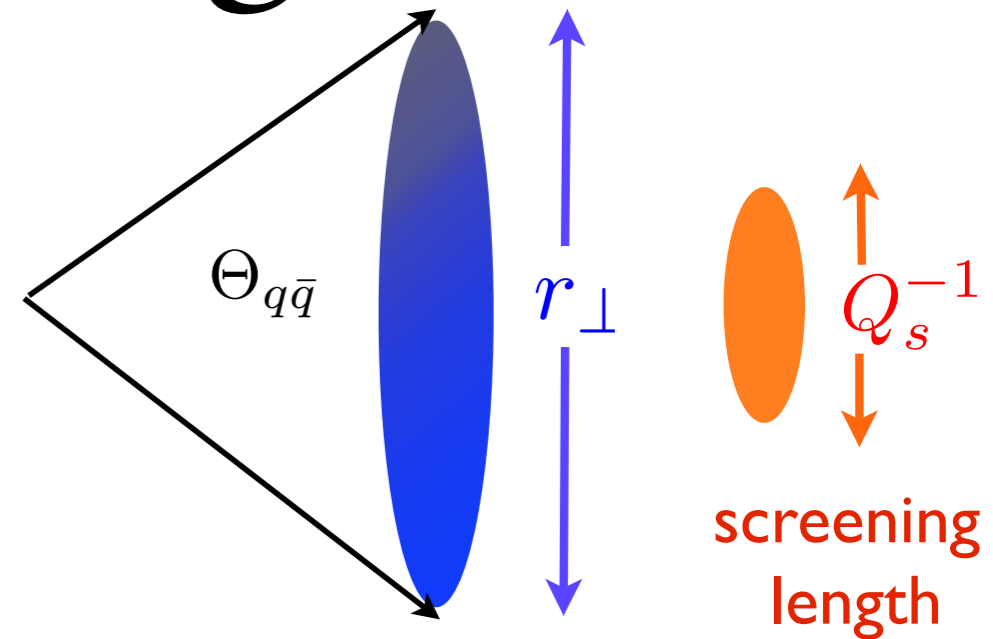
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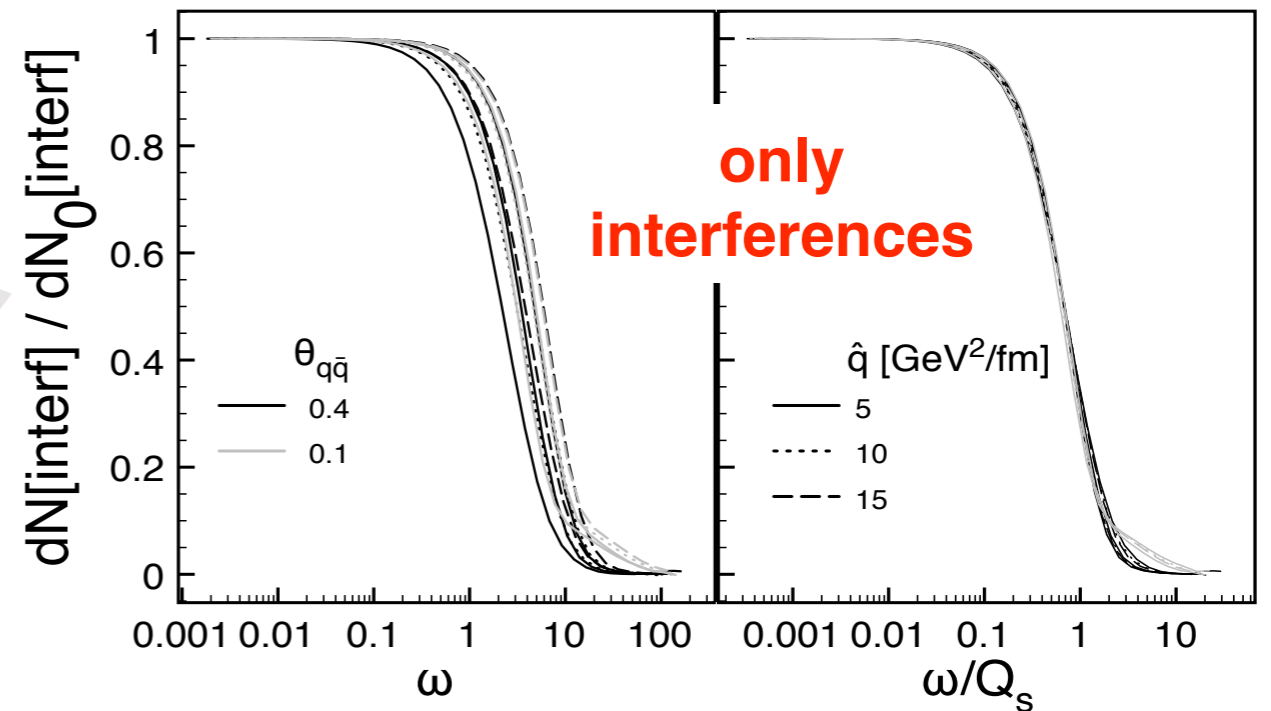
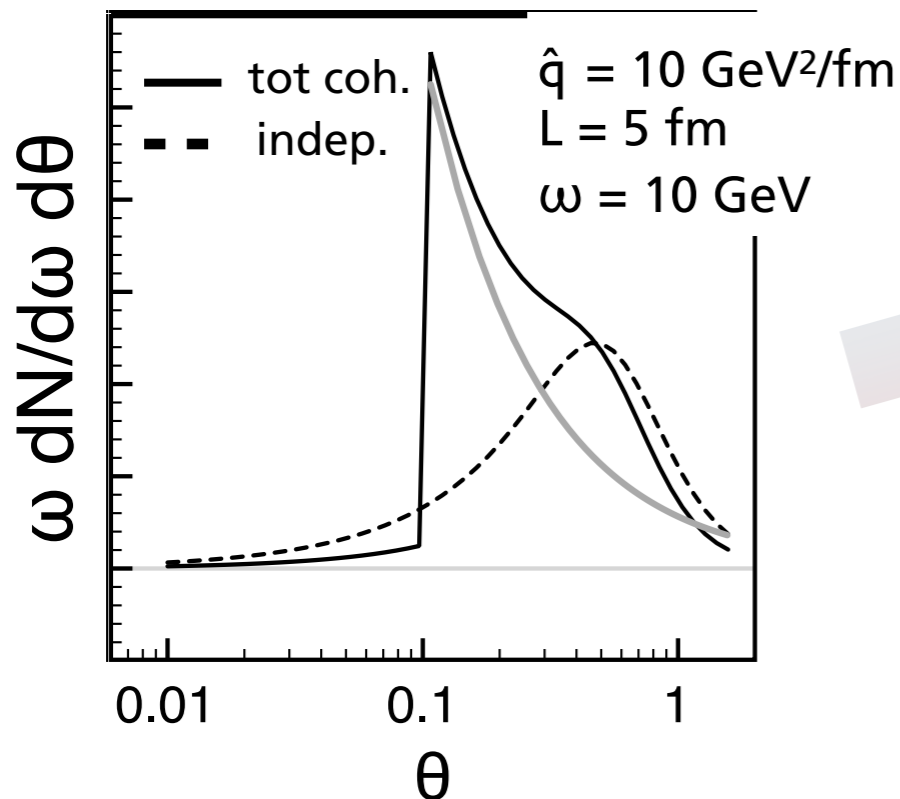
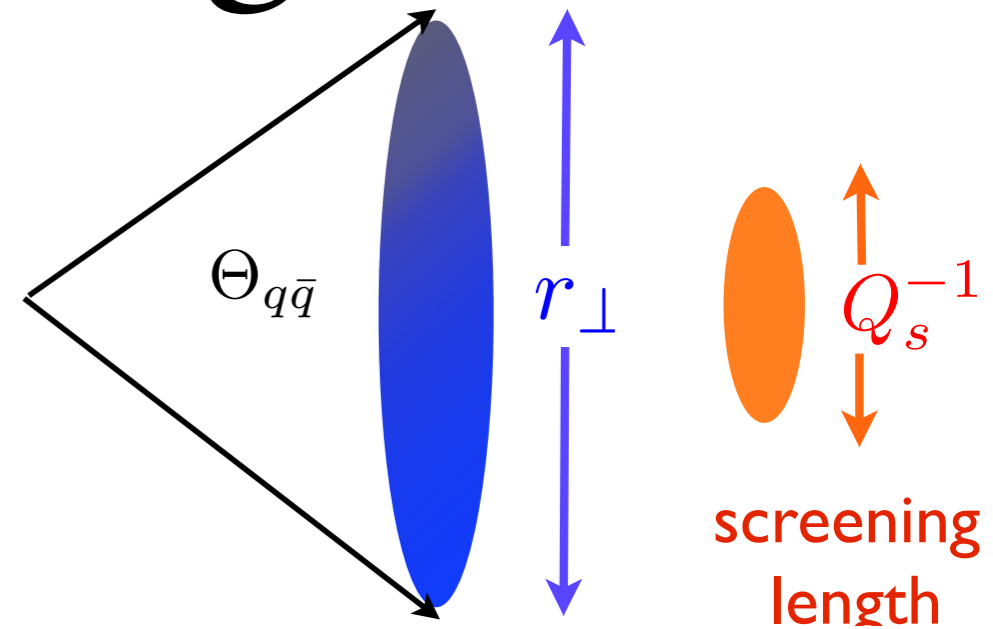
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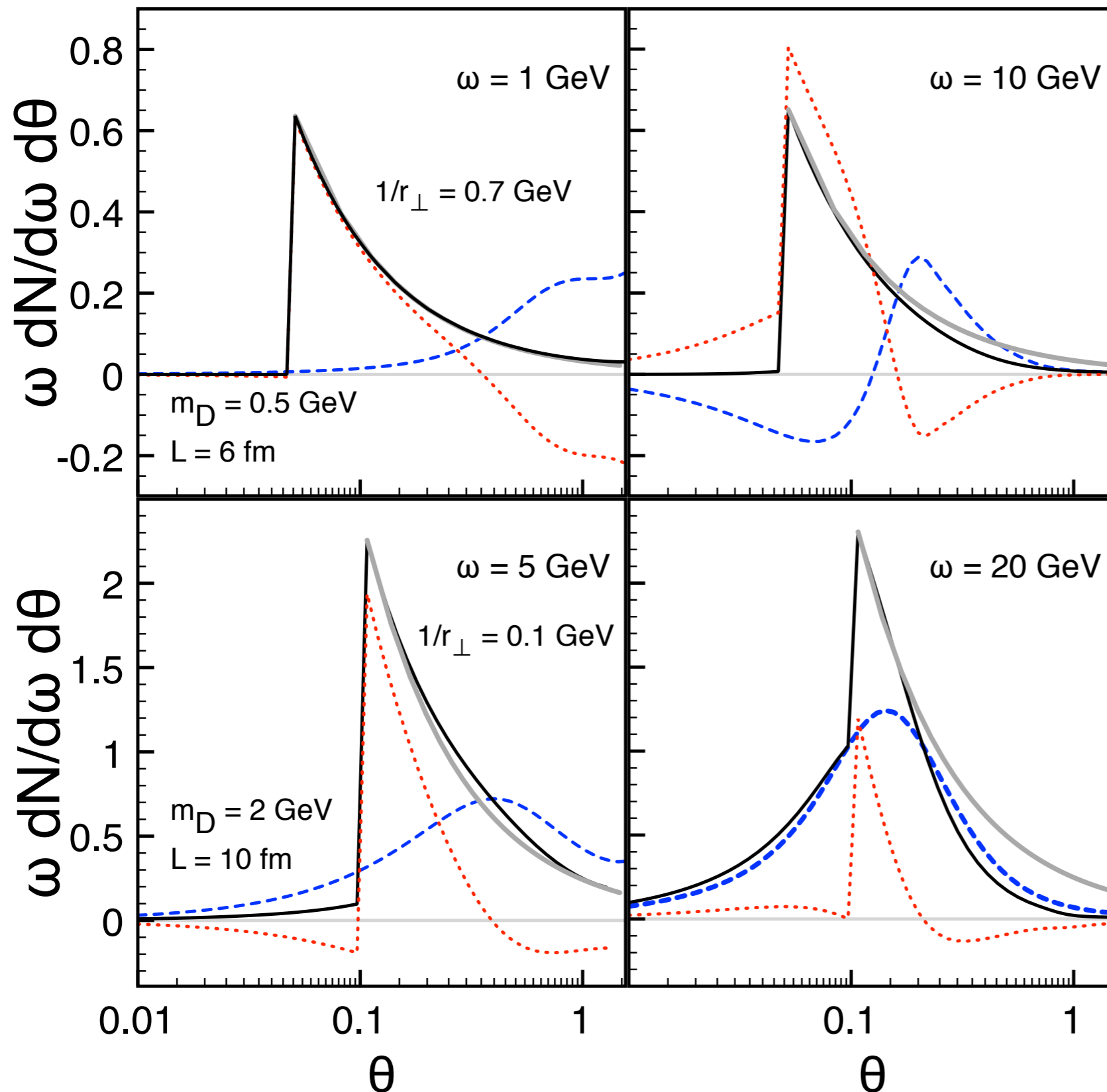
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Mehtar-Tani, Salgado, KT *JHEP* 1204 (2012) 064
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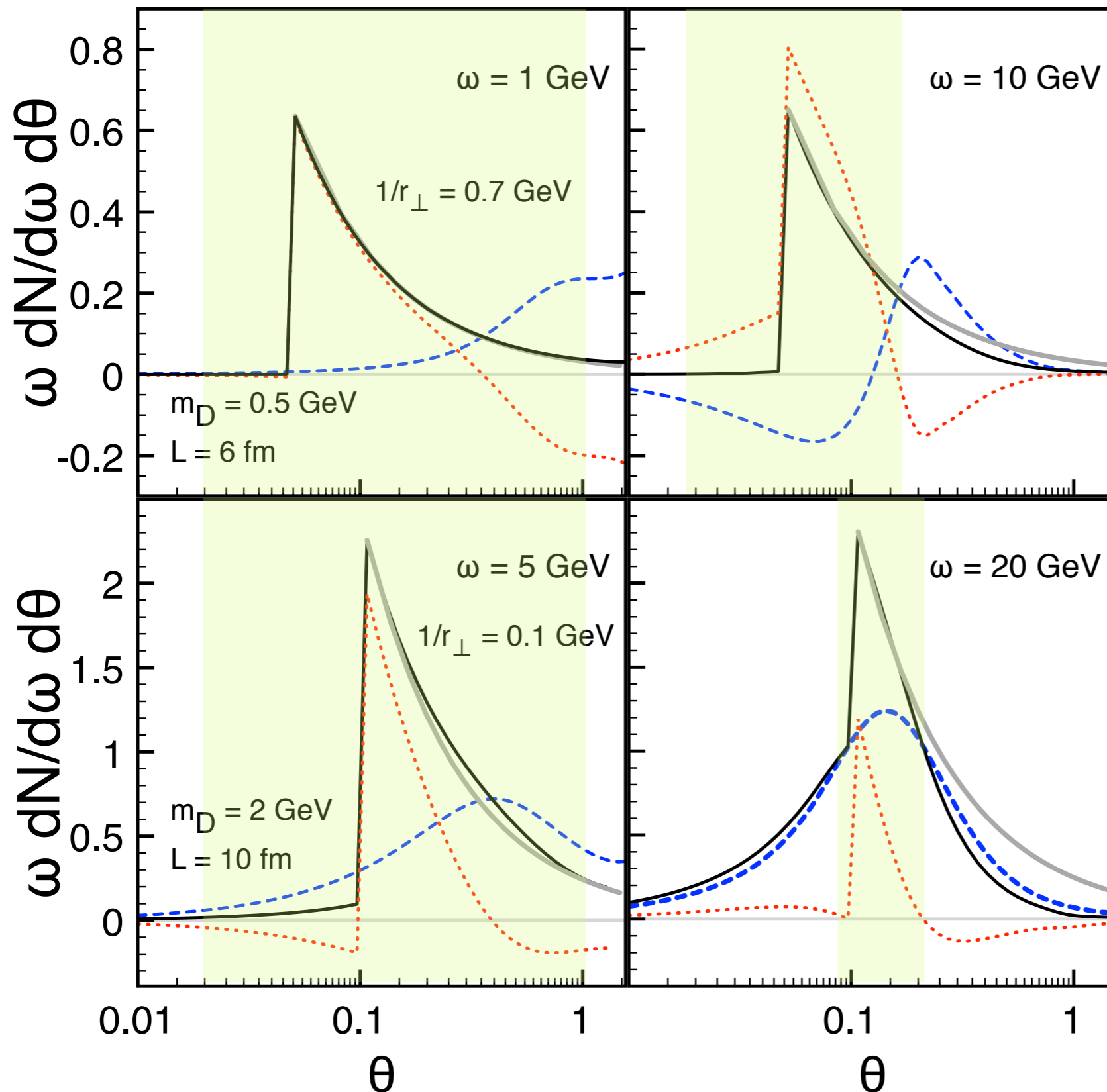
$$\mathcal{R}_q^{\text{med}}$$

$$\mathcal{J}_q^{\text{med}}$$

$$1/\theta$$

[N=1 case]





$$\mathcal{R}_q^{\text{med}}$$

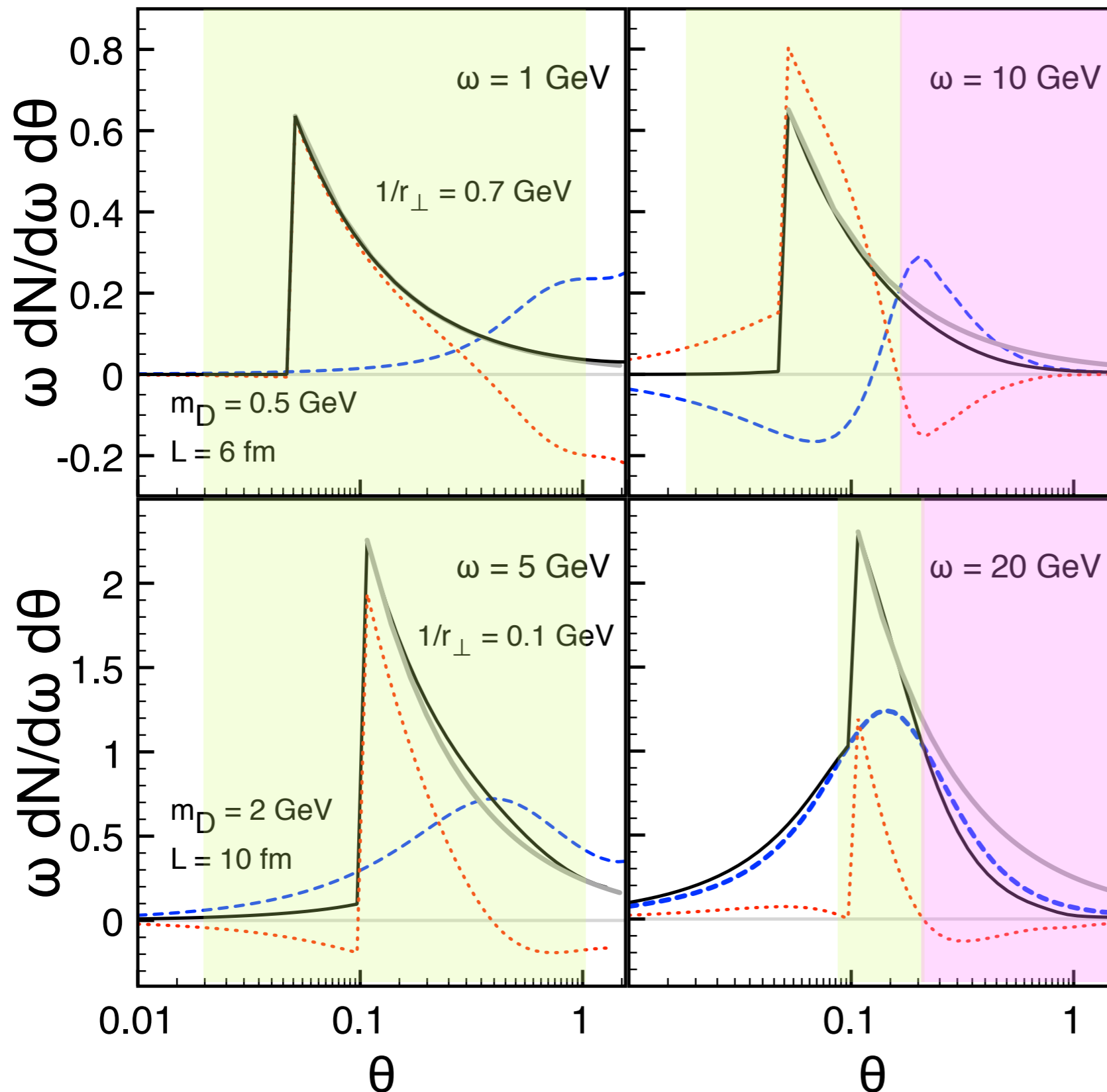
$$\mathcal{J}_q^{\text{med}}$$

$$1/\theta$$

antiangular ordering

[N=1 case]





$$\mathcal{R}_q^{\text{med}}$$

$$\mathcal{J}_q^{\text{med}}$$

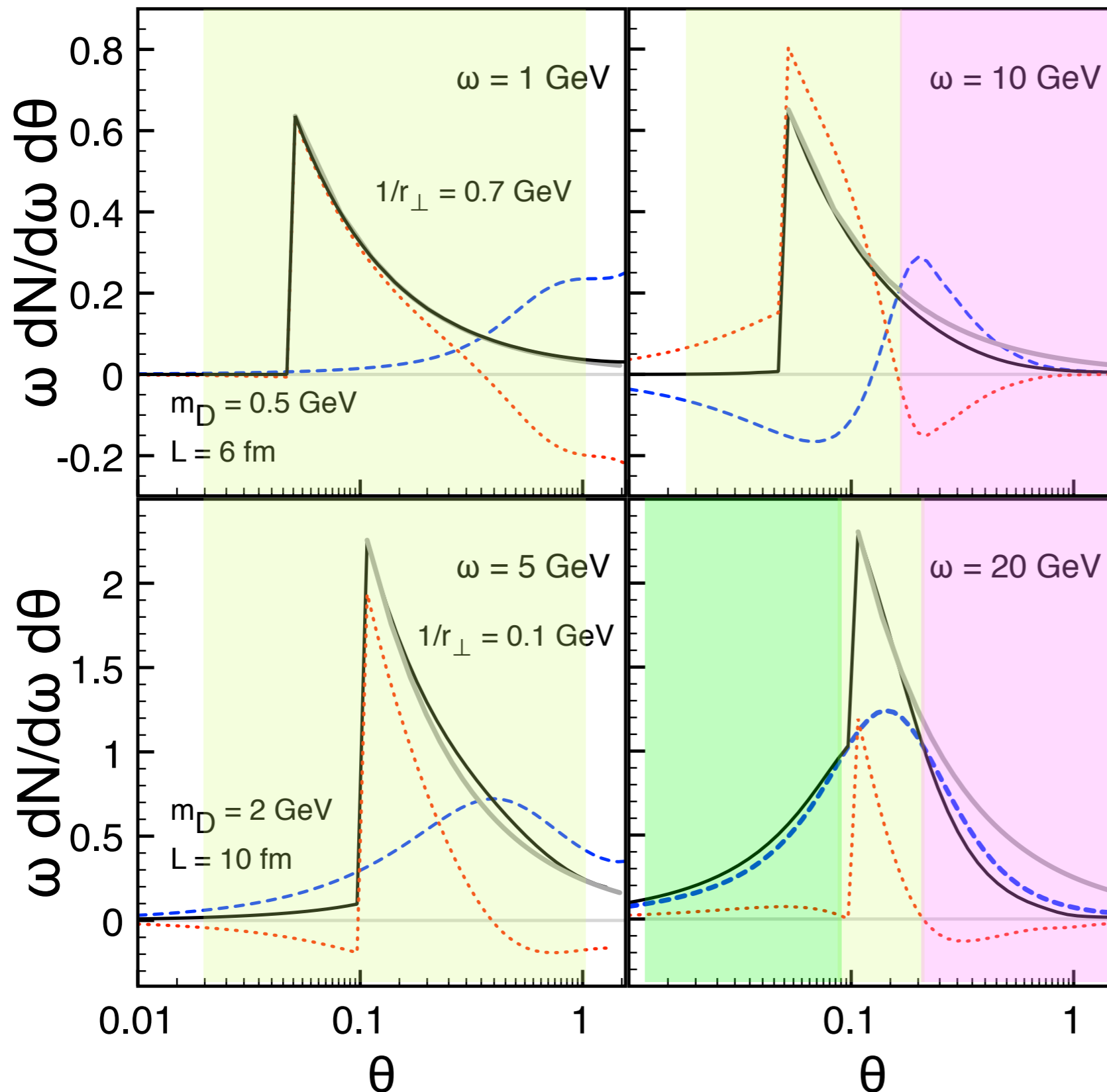
$$1/\theta$$

antiangular ordering

coherence

[N=1 case]





$$\mathcal{R}_q^{\text{med}}$$

$$\mathcal{J}_q^{\text{med}}$$

$$1/\theta$$

antiangular ordering

coherence

inside cone

[N=1 case]



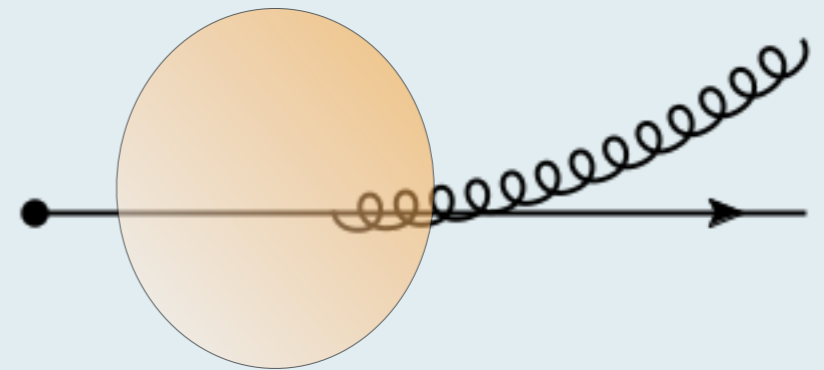
The vacuum component

Usually neglected/subtracted from medium-induced spectrum.

- bremsstrahlung off accelerated charge

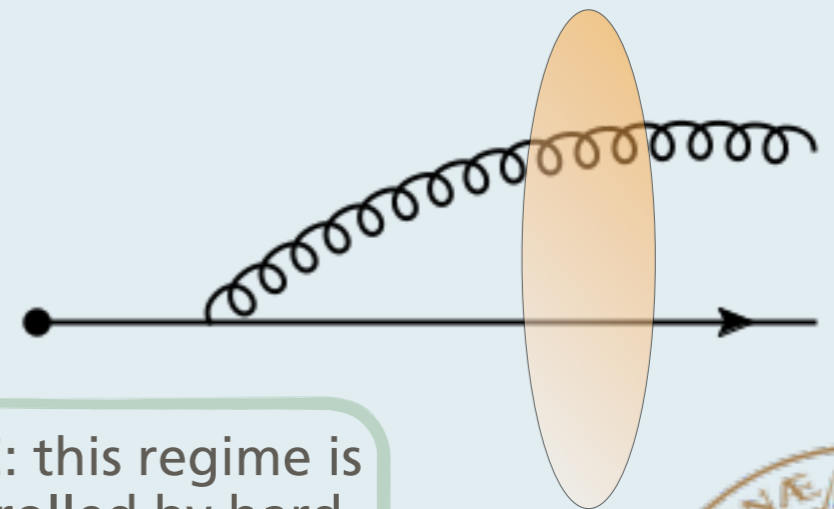
- after the medium

- does not resolve the medium
- soft radiation ($t_{\text{form}} > L$)



- early in the medium

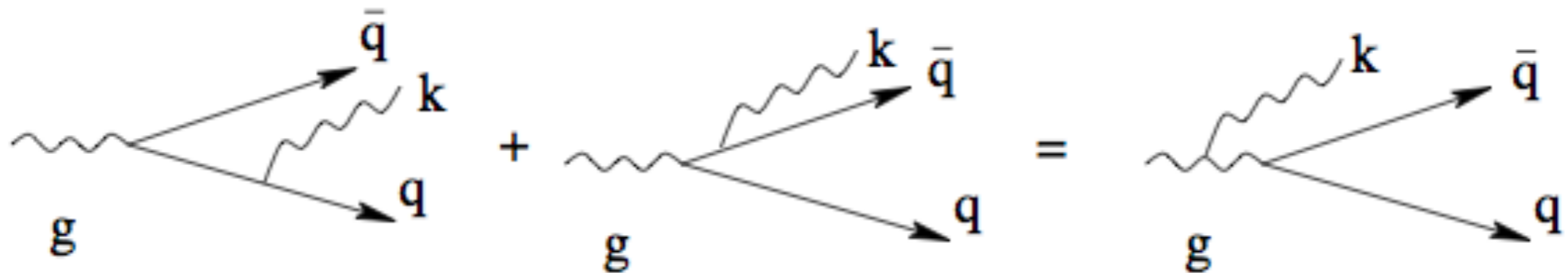
- medium does not resolve it ($t_{\text{form}} < \lambda_{\text{mfp}}$)
- can feel broadening



NOTE: this regime is controlled by hard medium interactions



Reshuffling of radiation



- radiation is reinstated as coming off the **total charge**
- in the soft limit:

$$(2\pi)^2 \omega \frac{dN_{g^*}^{\text{tot}}}{d^3k} = \frac{\alpha_s}{\omega^2} \left[C_F (\mathcal{R}_{\text{sing}} + 2\Delta_{\text{med}} \mathcal{J}) + C_A (1 - \Delta_{\text{med}}) \mathcal{J} \right]$$

$$\mathcal{R}_{\text{sing}} \equiv \mathcal{R}_q + \mathcal{R}_{\bar{q}} - 2\mathcal{J}$$

