

New Challenges in Unified Theories

SM very successful!

But with > 20 free parameters

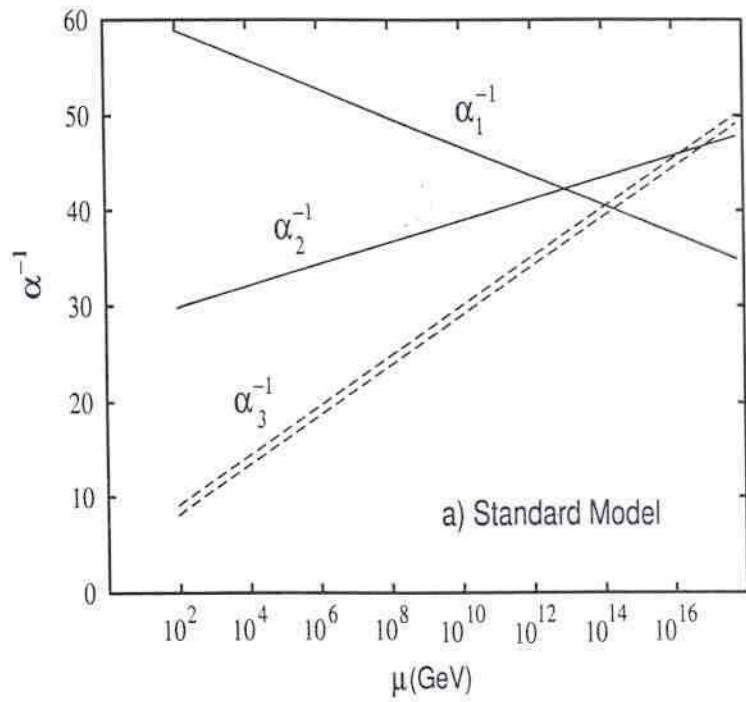
ad hoc Higgs sector

ad hoc Yukawa couplings

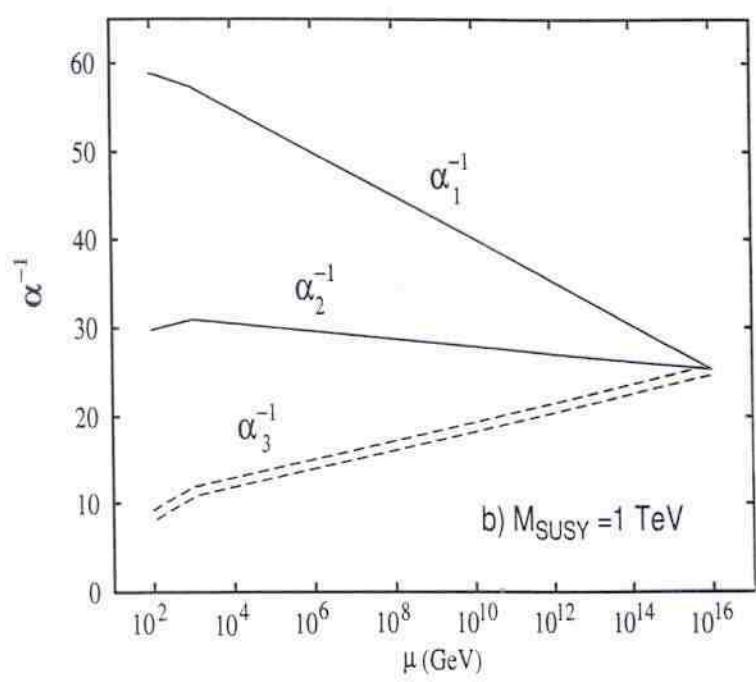
Best candidate for Physics Beyond SM

MSSM with $> 100!$ free parameters
mostly in its SSB sector.

- cures problem of quadratic divergencies of SM (hierarchy problem)
- restricts the Higgs sector



a) Standard Model



b) $M_{\text{SUSY}} = 1 \text{ TeV}$

• $\tilde{S}M$ with two - Higgs doublets

$$V = m_1^2 |H_1|^2 + m_2^2 |H_2|^2 + (m_3^2 H_1 H_2 + h.c.) \\ + \frac{1}{2} \lambda_1 (H_1^+ H_1)^2 + \frac{1}{2} \lambda_2 (H_2^+ H_2)^2 \\ + \lambda_3 (H_1^+ H_1) (H_2^+ H_2) + \lambda_4 (H_1 H_2) (H_1^+ H_2^+) \\ + \left\{ \frac{1}{2} \lambda_5 (H_1 H_2)^2 + [\lambda_6 (H_1^+ H_1) + \lambda_7 (H_1^+ H_2^+)] (H_1 H_2) + h.c. \right\}$$

Supersymmetry provides tree level relations among couplings

$$\lambda_1 = \lambda_2 = \frac{1}{4} (g^2 + g'^2)$$

$$\lambda_3 = \frac{1}{4} (g^2 - g'^2), \quad \lambda_4 = -\frac{1}{4} g^2$$

$$\lambda_5 = \lambda_6 = \lambda_7 = 0$$

With $v_1 = \langle \text{Re } H_1^\circ \rangle, \quad v_2 = \langle \text{Re } H_2^\circ \rangle$

and $v_1^2 + v_2^2 = (246 \text{ GeV})^2, \quad \frac{v_2}{v_1} \equiv \tan \theta$

$\Rightarrow h^\circ, H^\circ, H^\pm, A^\circ$

At tree level

$$M_{h^0, H^0}^2 = \frac{1}{2} \left\{ M_A^2 + M_Z^2 \mp \left[(M_A^2 + M_Z^2)^2 - 4 M_A^2 M_Z^2 \cos^2 2\theta \right]^{1/2} \right\}$$

$$M_{H^\pm}^2 = M_W^2 + M_A^2$$

$$\begin{cases} M_{h^0} < M_Z |\cos 2\theta| \\ M_{H^0} > M_Z \\ M_{H^\pm} > M_W \end{cases}$$

Radiative corrections

$$M_{h^0}^2 \approx M_Z^2 \cos^2 2\theta + \frac{3g^2 m_t^4}{16\pi^2 M_W^2} \log \frac{\tilde{m}_{t_1}^2 \tilde{m}_{t_2}^2}{m_t^4}$$

- Finite Unified Theories
(from Quantum Reduction
of Couplings)
- Higher Dimensional Unified Theories
and Coset Space Dimensional
Reduction (Classical Reduction
of Couplings)
- Fuzzy Extra Dimensions
and Renormalizable Unified Theories

Quantum Reduction of Couplings

Consider a GUT with

g - gauge coupling

g_i - other couplings (Yukawa, self-couplings)

Any relation among the couplings

$$\Phi(g, g_1, \dots) = \text{const}$$

which is RGI should satisfy

$$\frac{d}{dt} \Phi = 0, \quad \ell = \text{lyc}$$

$$\frac{d}{dt} \Phi = \frac{\partial \Phi}{\partial g} \frac{dg}{dt} + \sum_i \frac{\partial \Phi}{\partial g_i} \frac{dg_i}{dt} = 0$$

which is equivalent to

$$\frac{dg}{g} = \frac{dg_1}{g_1} = \frac{dg_2}{g_2} = \dots \quad \begin{matrix} \text{characteristic} \\ \text{system} \end{matrix}$$

$$\Rightarrow \frac{dg}{d\bar{g}} \frac{d\bar{g}_i}{d\bar{g}} = \bar{g}_i$$

Reduction
egs

Oehme
Zimmermann

Demand power series solution to the REs

$$\bar{g}_i = \sum_{n=0}^{\infty} p_i^{(n+1)} g^{2n+1}$$

Remarkably, uniqueness of these solutions can be decided already at 1-loop!

Assume

$$\bar{g}_i = \frac{1}{16\pi^2} \left[\sum_{j,k,l} \bar{g}_i^{(1)jkl} g_j g_k g_l + \sum_{i \neq j} \bar{g}_i^{(1)i} g_i g_j \right] + \dots$$

$$\bar{g}_g = \frac{1}{16\pi^2} \bar{g}_g^{(1)} g^3 + \dots$$

Assume $p_i^{(n)}$, $n \leq r$ have been uniquely determined

To obtain $p_i^{(r+1)}$, insert \bar{g}_i in REs and collect terms of $O(g^{2r+1})$

$$\Rightarrow \sum_{\ell \neq g} M(r)_i^\ell p_e^{(r+1)} = \text{lower order quantities}$$

Known by assumption

where

$$M(r)_i^\ell = 3 \sum_{j, k \neq g} b_i^{(1)jk\ell} p_j^{(1)} p_k^{(1)} + b_i^{(1)\ell} - (2r+1) b_g^{(1)\ell} p_i^\ell$$

$$0 = \sum_{j, k, \ell \neq g} b_i^{(1)jk\ell} p_j^{(1)} p_k^{(1)} p_\ell^{(1)} + \sum_{\ell \neq g} b_i^{(1)\ell} p_e^{(1)} - b_g^{(1)\ell} p_i^{(1)}$$

\Rightarrow for a given set of $p_i^{(1)}$, the $p_i^{(n)}$ for all $n > 1$ can be uniquely determined if

$$\det M(n)_i^\ell \neq 0$$

for all n

Consider an $SU(N)$ (non-susy) theory with

$\phi^i(n), \dot{\phi}_i(\bar{n})$ - complex scalars

$\psi^i(n), \dot{\psi}_i(\bar{n})$ - Weyl spinors

$J^a (a=1, \dots, N^2-1)$ - "

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu} + i\sqrt{2} [g_Y \bar{\psi}_j J^a T^a \phi - g_Y \bar{\psi}_j J^a T^a \dot{\phi} + h.c.] - V(\phi, \dot{\phi}),$$

$$\begin{aligned} V(\phi, \dot{\phi}) = & \frac{1}{4} J_1 (\phi^i \phi_i^*)^2 + \frac{1}{4} J_2 (\dot{\phi}_i \dot{\phi}_i^*)^2 \\ & + J_3 (\phi^i \phi_i^*) (\dot{\phi}_j \dot{\phi}_j^*) \\ & + J_4 (\phi^i \phi_j^*) (\dot{\phi}_i \dot{\phi}_j^*) \end{aligned}$$

Searching for power series solution of the R.E.s we find

$$g_Y = \dot{g}_Y = g; J_1 = J_2 = \frac{N-1}{N} g^2; J_3 = \frac{1}{2N} g^2; J_4 = -\frac{1}{2} g^2$$

i.e. SUSY

$N=1$ gauge theories

Consider a chiral, anomaly free $N=1$ globally supersymmetric gauge theory based on a group G with gauge coupling g .

Superpotential

$$W = \frac{1}{2} m_{ij} \phi^i \phi^j + \frac{1}{6} C_{ijk} \phi^i \phi^j \phi^k$$

m_{ij} , C_{ijk} - gauge invariant tensors
 ϕ^i - matter fields transforming as an ir. rep. R_i of G .

Renormalization constants associated with W

$$\phi^{oi} = (Z_j^i)^{1/2} \phi^i, m_{ij}^o = Z_{ij}^{i'j'} m_{i'j'}, C_{ijk}^o = Z_{ijk}^{i'j'k'} C_{i'j'k'}$$

$N=1$ non-renormalization theorem ensures absence of mass and cubic-int-term infinities

$$Z_{i''j''k''}^{ijk} Z_{i''}^{1/2 i'} Z_{j''}^{1/2 j'} Z_{k''}^{1/2 k'} = \delta_{(i''}^i \delta_{j''}^j \delta_{k''}^k$$

$$Z_{i''j''}^{ij} Z_{i''}^{1/2 i'} Z_{j''}^{1/2 j'} = \delta_{(i''}^i \delta_{j''}^j$$

(In the background field method)

$$Z_g Z_V^{1/2} = 1$$

Only surviving infinities are $Z_{jj}^i(Z_V)$
i.e. one infinity for each field.

The 1-loop β -function of the gauge coupling is

$$\beta_g^{(1)} = \frac{dg}{dt} = \frac{g^3}{16\pi^2} \left[\sum_i l(R_i) - 3C_2(G) \right]$$

$l(R_i)$ - Dynkin index of R_i

$C_2(G)$ - quadratic Casimir of the adjoint rep.

β -functions of C_{ijk} , by virtue of the non-renormalization thm, are related with the anomalous dim. matrix γ_{ij}^k of ϕ^i

$$\beta_{ijk}^{(1)} = \frac{dC_{ijk}}{dt} = C_{ije} \gamma_k^e + C_{ike} \gamma_j^e + C_{jke} \gamma_i^e$$

$$\gamma_i^{(1)j} = z^{-\frac{1}{2}} i \cdot \frac{d}{dt} z^{\frac{1}{2} j}$$

$$= \frac{1}{32\pi^2} [C^{ske} C_{ike} - 2g^2 C_2(R_i) \delta_i^j]$$

$C_2(R_i)$ - quadratic Casimir of R_i

$$C^{ijk} = C^{*}_{ijk}$$

$$\mathcal{L}_g^{(2)} = \frac{1}{(16\pi^2)^2} 2 g^5 \left[\sum_i \ell(R_i) - 3 C_2(G) \right]$$

$$- \frac{1}{(16\pi^2)^2} \frac{g^3}{r} C_2(R_i) \left[C^{ijk\ell} (C_{ijk\ell} - 2g^2 C_2(R_i) \delta_{ij}^k) \right]$$

Parkes, West, Jones
 Mezincescu, Yam
 Machacek, Vaughn

$$\gamma^{(2)i}_{\cdot j} = \frac{1}{(16\pi^2)^2} 2 g^4 C_2(R_i) \left[\sum_i \ell(R_i) - 3 C_2(G) \right]$$

$$- \frac{1}{(16\pi^2)^2} \frac{1}{2} \left[C^{ik\ell} C_{jikm} + 2g^2 (R^a)_m^i (R^a)_j^\ell \right]$$

$$\cdot \left[C^{mpq} (\delta_{pq} - 2 \delta_e^m g^2 C_2(R_i)) \right]$$

$$\mathcal{L}_g^{NSVZ} = \frac{g^3}{16\pi^2} \left[\frac{\sum_i \ell(R_i) (1 - 2 \gamma_i) - 3 C_2(G)}{1 - g^2 C_2(G)/8\pi^2} \right]$$

Novikov - Shifman - Vainshtein - Zakharov

Finite Unification

Old days...

... divergences are "hidden under
the carpet" (Dirac, Lects on Q.F.T., '64)

Recent years ...

... divergences reflect existence
of a higher scale where new
degrees of freedom are excited.

Not just artifacts of pert. th.

However the presence of quadratic
divergences means that physics at
one scale are very sensitive to unknown
physics at higher scales.

→ SUSY theories which are free of quadratic divergences in spite of any experimental evidence...

→ Natural to expect that beyond unification scale the theory should be completely finite.

- $N=4 \rightarrow$ finite to all orders in pert.
- $N=2 \rightarrow$ only 1-loop contributions to β -function. Possible to arrange the spectrum so that theory is finite.

Multiplicities for massless irreducible reps with maximal helicity 1

$N \setminus \text{Spin}$	1	1	2	2	4
1	-	1	-	1	1
$\frac{1}{2}$	1	1	2	2	4
0	2	-	4	2	6

$$N=2 : B(g) = \frac{2g^3}{(4\pi)^2} \left(\sum_i T(\rho_i) - C_2(G) \right)$$

e.g. $SU(N)$ with $2N$ fundamental
reps $\rightarrow B(g) = 0$

$SU(5)$: $p(5 + \bar{5})$; $q(10 + \bar{10})$; $r(15 + \bar{15})$
with $p + 3q + 7r = 10$

$SO(10)$: $p(10 + \bar{10})$; $q(16 + \bar{16})$
with $p + 2q = 8$

E_6 : $4(27 + \bar{27})$

Finite Unified Theories

$$N=1$$

- 1-loop finiteness conditions

$$\mathcal{B}_g^{(1)} = 0$$

$\gamma^{(1)i}_{j} = 0$ - anomalous dimensions
of all chiral superfields

- Exists complete classification
of all chiral $N=1$ models with
 $\mathcal{B}_g^{(1)} = 0$
Hamidi - Patera - Schwarz
Jiang - Zhou

- 1-loop finiteness Parkes - West
Jones
- 2-loop finiteness Mezincescu

- Exist simple criteria
 that guarantee all loop finiteness
 (vanishing of all-loop beta functions)
- All-loop finite $SU(5)$
 \Rightarrow top quark mass ✓
-

Lucchesi-Piquet
 Sibold
 Ermushev
 Kazakov
 Tarasov
 Leigh-Susskind

- ~~Susy~~ sector
- 1-loop finiteness cond.
 (require in particular universal soft ~~susy~~ scalar masses
 $(m^2)_j^i = \frac{1}{3} MM^* \delta_j^i$)

Jones
 Mezincescu
 Yao

.. 1-loop finiteness

Jack
Jones

→ 2-loop finiteness

Reduction of couplings

• Extension of method in SSB sector

+ application in min susy SU(5) Kubo
Mondragon₂

.. 1-loop sum rule for soft scalar masses in non-finite susy ths. Kawamura
Kobayashi Kubo

... 2-loop sum rule for soft scalar masses in finite ths. Kubo
Mondragon₂

* All-loop RGI relations in finite and non-finite ths Yamada
Hisano,
Shifman
Kazakov
Jack, Jones,
Pickering

** All-loop sum rule for
soft scalar masses is finite
and non-finite thes

Kobayashi
Kubo
 Σ

• • SU(5) FUTs

Kobayashi
Kubo
Mondragon

• Prediction of s-spectrum in
terms of few parameters starting
from several hundreds GeV.

• The LSP is neutralino ✓ (see e.g.
Kazakov et al.
Yoshioka)

• Radiative E-W breaking ✓ (see e.g.
Brignole
Ibanez, Munoz)

• No funny colour, charge ✓ (see e.g.
Casas et al.)

* Prediction of Higgs masses

Lightest $\sim 118 - 129$ GeV
Similar results also for min susy SU(5)

Consider a chiral, anomaly free, $N=1$ gauge theory with group G .

The superpotential is

$$W = \frac{1}{6} Y^{ijk} \bar{\Phi}_i \bar{\Phi}_j \bar{\Phi}_k + \frac{1}{2} \mu^{ij} \bar{\Phi}_i \bar{\Phi}_j$$

$\begin{matrix} Y^{ijk} \\ \mu^{ij} \end{matrix}$ } gauge invariant
Yukawa couplings

$\bar{\Phi}_i$ - matter superfields
in irreducible reps of G

Necessary and sufficient conditions
for $N=1$ 1-loop finiteness

- Vanishing of $\delta g^{(1)}$ implies

$$\sum_i l(R_i) = 3 C_2(G) \quad ||$$

$l(R_i)$ - Dynkin index of R_i

$C_2(G)$ - Quadratic Casimir of G (adjoint)

\Rightarrow Selection of the field content
(representations) of the theory

- • Vanishing of $\gamma^{(1)i}_j$ implies

$$Y^{ik\ell} Y_{jkl} = 2 \delta^i_j g^2 C_2(R_i) //$$

↑ Yukawa ↑ gauge

$C_2(R_i)$ - quadratic Casimir of R_i

$$Y_{ijk} = (Y_{ijk})^*$$

\Rightarrow Yukawa and gauge couplings are related.

Note: μ 's are not restricted

.. Appearance of $U(1)$ is incompatible
with 1st cond.

... 2nd would forbids the presence of singlets with nonvanishing couplings.

$\therefore \Rightarrow$ ~~Susy~~ by G-invariant
soft terms

- * 1-loop finiteness condts necessary and sufficient to guarantee 2-loop finiteness
- * 1-loop finiteness condts ensure that $\mathcal{B}_g^{(3)}$ in 3-loops vanishes but in general $\gamma^{(3)}$ does not.

Grisaru - Milewski - Zayon
 Parkes - West

What happens in higher loops?

So far 1-loop finiteness condts (on γ_s) are telling us

$$\gamma^{ijk} = \gamma^{ijk}(g)$$

$$\mathcal{B}_\gamma^{(1)ijk} = 0$$

* * Necessary and sufficient condts
for vanishing \mathcal{B}_g and \mathcal{B}_{ijk} to all
orders

$$1. \quad \mathcal{B}_g^{(1)} = 0$$

$$2. \quad \gamma_{\ j}^{(1)i} = 0$$

$$3. \quad \mathcal{B}_Y^{ijk} = \mathcal{B}_g \frac{d Y^{ijk}}{d g}$$

Lucchesi
Piquet
Sibold

admit power series solutions which
in lowest order is a solution of
condt 2.

- 3'. There exist solutions to $\gamma_{\ j}^{(1)i} = 0$
of the form

$$Y^{ijk} = \rho^{ijk} g, \rho^{ijk} - \text{complex}$$
3. 

4. These solutions are isolated
and non-degenerate considered
as solutions of $\mathcal{B}_Y^{(1)ijk} = 0$

Recall

R-invariance, axial anomaly

In massless $N=1$ this

$U(1)$ chiral transformation \mathcal{R} :

$$A_\mu \rightarrow A_\mu , \bar{\gamma} \rightarrow e^{-i\alpha} \bar{\gamma} ,$$

$$\phi \rightarrow e^{-i\frac{2}{3}\alpha} \phi , \psi \rightarrow e^{i\frac{1}{3}\alpha} \psi , \dots$$

$$\psi_D = \begin{pmatrix} \psi \\ \chi \end{pmatrix} \rightarrow e^{i\alpha \gamma_5} \psi_D$$

Noether current $J_\alpha^\mu = \bar{\gamma}_D \gamma^\mu \gamma^5 \gamma_D + \dots$

$$\leadsto \partial_\mu J_\alpha^\mu = r (\epsilon^{\mu\nu\rho\sigma} F_{\mu\nu} F_{\rho\sigma} + \dots)$$

$$r = G_g^{(1)} !$$

Only 1-loop contributions
due to non-renormalization thus.

Adler, Bardeen, Jackiw, Pi, Shie, Zee

Supercurrent

$$J = \{ J_R^{\mu}, Q_{\alpha}^{\mu}, T^{\mu} \}, \quad \begin{matrix} & & \text{vector} \\ & | & \text{super} \\ & | & \text{multiplet} \end{matrix}$$

associated to R -invariance associated to susy associated to translation inv.

Ferrara + Zumino

(supercurrent is represented as vector superfield)

$$V_{\mu}(x, \theta, \bar{\theta}) = Q_{\mu}(x) - i\theta^{\alpha}Q_{\mu\alpha}(x) + i\bar{\theta}_{\dot{\alpha}}\bar{Q}_{\mu}^{\dot{\alpha}}(x) - 2(\theta\sigma^{\nu}\bar{\theta})T_{\mu\nu}(x) + \dots$$

- $J_R^{\mu} \neq \bar{J}_R^{\mu}$

- .. $J_R^{\mu} = \bar{J}_R^{\mu} + O(t)$

In addition

Clan K
Piguet
Sibold

$$S = \{ \text{bg } F^{\mu\nu} F_{\mu\nu} + \dots, \text{bg } \epsilon^{\mu\nu\rho\sigma} F_{\mu\nu} F_{\rho\sigma} + \dots, \text{ trace anomaly of } T^{\mu}_{\mu} \text{, anomaly of R-current, } \text{bg } \bar{J}^{\mu} G_{\alpha\beta}^{\mu\nu} F_{\nu\alpha} + \dots, \dots \}, \quad \begin{matrix} & & \text{chiral} \\ & & \text{super} \\ & & \text{multiplet} \end{matrix}$$

Super trace anomaly

trace anomaly of susy current

There is a relation, whose structure is independent from the renormalization scheme, although individual coefficients (except the 1-loop values of β -functions) may be scheme dependent

$$r = \beta_g (1 + x_g) + C_{ijk} x^{ijk} - \delta_A r^A$$

radiative corrections

unrenormalized
coefficients of anomalies
associated to chiral inv.
of superpotential

Linear combinations
of anomalous dims

Thm: If (i) no gauge anomaly

(ii) $\beta''(g) = 0$ i.e. no Q -current anomaly

(iii) $\gamma^{(1)i} = 0$ implies also $r^A = 0$

(iv) exist solutions to $\gamma^{(1)} = 0$ of the form $C_{ijk} = \rho_{ijk} g$, ρ_{ijk} - complex

(v) these solutions are isolated + non-degenerate

- when considered as solutions of $B_{ijk}^{(1)} = 0$
- Then each of the solutions can be uniquely extended to a formal power series in g , and the $N=1$ YM models depend on the single coupling constant g with a β -function vanishing to all orders.

Proof: Inserting $B_{ijk} = \frac{\partial g}{\partial t} f_{ijk}$

in the identity and taking into account the vanishing of r, r^A

$$\rightarrow 0 = \frac{\partial g}{\partial t} (1 + O(t))$$

its solution (as formal power series in t) is: $\frac{\partial g}{\partial t} = 0$ //

and $B_{ijk} = 0$ too. //

2-loop RGEs for SSB parameters

Martin-Vaughn-Yamada-Jack-Jones
1994

Consider $N=1$ gauge thy with

$$W = \frac{1}{6} Y^{ijk} \bar{\Phi}_i \bar{\Phi}_j \bar{\Phi}_k + \frac{1}{2} \mu^{ij} \bar{\Phi}_i \bar{\Phi}_j$$

and SSB terms

$$\begin{aligned} -\mathcal{L}_{SB} = & \frac{1}{6} h^{ijk} \phi_i \phi_j \phi_k + \frac{1}{2} b^{ij} \phi_i \phi_j \\ & + \frac{1}{2} (m^2)_j^i \phi^{*i} \phi_j + \frac{1}{2} M \lambda \lambda + h.c. \end{aligned}$$

• 1-loop finiteness conditions

$$h^{ijk} = -M Y^{ijk}$$

$$(m^2)_j^i = \frac{1}{3} M M^* \delta_j^i \quad \text{universality}$$

in addition to $\partial_g^{(1)} = \gamma^{(1)i} = 0$

• 1-loop finiteness

→ 2-loop finiteness

Assuming

- $\mathcal{L}_g^{(1)} = \gamma^{(1)i}{}_j = 0$
- the reduction eq

$$\mathcal{L}_Y^{ijk} = \mathcal{L}_g d\gamma^{ijk}/dg$$

admits power series solution

$$\gamma^{ijk} = g \sum_{n=0} P_{(n)}^{ijk} g^{2n}$$

- $(m^2)_j^i = m_j^2 \delta_j^i$

$$\Rightarrow (m_i^2 + m_j^2 + m_k^2)/MM^* = 1 + \frac{g^2}{16\pi^2} \Delta^{(2)}$$

for i, j, k with $P_{(0)}^{ijk} \neq 0$

where $\Delta^{(2)} = -2 \sum_\ell \left[(m_\ell^2/MM^*) - \frac{1}{3} \right] \ell(\chi_\ell)$

- $\Delta^{(2)} = 0$ for $N=4$ with 5Tr cond
- $\Delta^{(2)} = 0$ for the $N=1, SU(5)$ FUTs!

The $SU(5)$ finite model

Kapetanakis, Mondragon, Z

Kobayashi, Kubo, Mondragon, Z

Content

$$H_\alpha \quad \bar{H}_\alpha$$

$$3(\bar{5} + 10) + 4(5 + \bar{5}) + 24$$

Jones-Raby

Hamidi-Schwarz

Quinos et.al

Kazakov

Babu-Enkhba

Gogoladze

↑
fermion
supermultiplets

scalar

supermultiplets

$$\Rightarrow W = \sum_{i=1}^3 \left[\frac{1}{2} g_i^u L_0^i \bar{L}_0^i H_i + g_i^d L_0^i \bar{5}_i \bar{H}_i \right] \\ + g_{23}^u L_0^2 L_0^3 H_4 + g_{23}^d L_0^2 \bar{5}_3 \bar{H}_4 + g_{32}^d L_0^3 \bar{5}_2 \bar{H}_4 \\ + \sum_{\alpha=1}^4 g_\alpha^f H_\alpha \bar{24} \bar{H}_\alpha + g^f / 3 (24)^3$$

(with enhanced discrete symmetry
after reduction of couplings)

We find

$$B_g^{(1)} = 0$$

$$B_{i\alpha}^{(u)} = \frac{1}{16\pi^2} \left[-\frac{96}{5} g^2 + \sum_{\theta=1}^4 (g_{i\theta}^u)^2 + 3 \sum_{j=1}^3 (g_{j\alpha}^u)^2 + \frac{24}{5} (g_\alpha^f)^2 + 4 \sum_{\theta=1}^4 (g_{i\theta}^d)^2 \right] g_{i\alpha}^u$$

$$B_{i\alpha}^{(d)} = \frac{1}{16\pi^2} \left[-\frac{84}{5} g^2 + 3 \sum_{\theta=1}^4 (g_{i\theta}^u)^2 + \frac{24}{5} (g_\alpha^f)^2 + 4 \sum_{j=1}^3 (g_{j\alpha}^d)^2 + 6 \sum_{\theta=1}^4 (g_{i\theta}^d)^2 \right] g_{i\alpha}^d$$

$$B^{(1)} = \frac{1}{16\pi^2} \left[-30 g^2 + \frac{63}{5} (g^\lambda)^2 + 3 \sum_{\alpha=1}^4 (g_\alpha^f)^2 \right] g^\lambda$$

$$B_\alpha^{(f)} = \frac{1}{16\pi^2} \left[-\frac{98}{5} g^2 + 3 \sum_{i=1}^3 (g_{i\alpha}^u)^2 + 4 \sum_{i=1}^3 (g_{i\alpha}^d)^2 + \frac{48}{5} (g_\alpha^f)^2 + \sum_{\theta=1}^4 (g_\theta^f)^2 + \frac{21}{5} (g^\lambda)^2 \right] g_\alpha^f$$

Considering g as the primary coupling, we solve the Red. Eqs.

$$\beta_g = \frac{\partial \alpha}{\partial g_\alpha} \frac{dg}{d\alpha}$$

requiring power series ansatz.

$$\Rightarrow (g_{ii}^a)^2 = \frac{8}{5} g^2 + \dots, (g_{ii}^f)^2 = \frac{6}{5} g^2 + \dots$$

$$(g^\lambda)^2 = \frac{15}{7} g^2 + \dots, (g_4^f)^2 = g^2, (g_\alpha^f)^2 = 0 + \dots (\alpha=1,2,3)$$

Higher order terms can be uniquely determined.

\Rightarrow All 1-loop β -functions vanish

Moreover

All 1-loop anomalous dimensions of chiral fields vanish.

$$\gamma_{10i}^{(1)} = \frac{1}{16\pi^2} \left[-\frac{36}{5} g^2 + 3 \sum_{b=1}^4 (g_{ib}^u)^2 + 2 \sum_{b=1}^4 (g_{ib}^d)^2 \right]$$

$$\gamma_{\bar{s}i}^{(1)} = \frac{1}{16\pi^2} \left[-\frac{24}{5} g^2 + 4 \sum_{b=1}^4 (g_{ib}^d)^2 \right]$$

$$\gamma_{H\alpha}^{(1)} = \frac{1}{16\pi^2} \left[-\frac{24}{5} g^2 + 3 \sum_{i=1}^3 (g_{i\alpha}^u)^2 + \frac{24}{5} (g_\alpha^f)^2 \right]$$

$$\gamma_{\bar{H}\alpha}^{(1)} = \frac{1}{16\pi^2} \left[-\frac{24}{5} g^2 + 4 \sum_{i=1}^3 (g_{i\alpha}^d)^2 + \frac{24}{5} (g_\alpha^f)^2 \right]$$

$$\gamma_{24}^{(1)} = \frac{1}{16\pi^2} \left[-\frac{10}{5} g^2 + \sum_{\alpha=1}^4 (g_\alpha^f)^2 + \frac{21}{5} (g_\lambda)^2 \right]$$

\Rightarrow Necessary and sufficient conditions for finiteness to all orders are satisfied

- $SU(5)$ breaks down to the standard model due to $\langle 24 \rangle$
- Use the freedom in mass parameters to obtain only a pair of Higgs fields light, acquiring v.e.v.
- Get rid of unwanted triplets rotating the Higgs sector (after a fine tuning)
see Quiros et. al., Kazakov et. al
Yoshioka
- Adding soft terms we can achieve SUSY breaking.

1) Gauge Couplings Unification

$$\sin^2 \theta_W, \alpha_{em} \rightarrow \alpha_3(M_Z)$$

Marciano + Sejanovic

Analoli et. al.

2) Bottom-Tau Yukawa Unif.

SU(5)-type

Barger et. al.

$$\rightarrow m_t \sim 100 - 200 \text{ GeV}$$

Carena et. al.

*3) Top-Bottom-Tau Yuk Unif.

$$h_t^2 = \frac{4}{3} h_{b,\tau}^2 \quad \text{in } SU(5) - \text{FUT}$$

Ananthanarayan et. al.

Similar to SO(10)

Barger et. al.

$$\rightarrow m_t \sim 160 - 200 \text{ GeV}$$

Carena et. al.

*4) Gauge-Top-Bottom-Tau Unif.

$$\text{e.g. FUT-SU(5)}: h_t^2 = \frac{8}{5} g_V^2; h_{b,\tau}^2 = \frac{6}{5} g_V^2$$

M_s [GeV]	$\alpha_{3(5f)}(M_Z)$	$\tan \beta$	M_{GUT} [GeV]	M_b [GeV]	M_t [GeV]
300	0.123	54.1	2.2×10^{16}	5.3	183
500	0.122	54.2	1.9×10^{16}	5.3	183
10^3	0.120	54.3	1.5×10^{16}	5.2	184

FUTA

M_s [GeV]	$\alpha_{3(5f)}(M_Z)$	$\tan \beta$	M_{GUT} [GeV]	M_b [GeV]	M_t [GeV]
800	0.120	48.2	1.5×10^{16}	5.4	174
10^3	0.119	48.2	1.4×10^{16}	5.4	174
1.2×10^3	0.118	48.2	1.3×10^{16}	5.4	174

FUTB

M_s [GeV]	$\alpha_{3(5f)}(M_Z)$	$\tan \beta$	M_{GUT} [GeV]	M_b [GeV]	M_t [GeV]
300	0.123	47.9	2.2×10^{16}	5.5	178
500	0.122	47.8	1.8×10^{16}	5.4	178
1000	0.119	47.7	1.5×10^{16}	5.4	178

MIN SU(5)

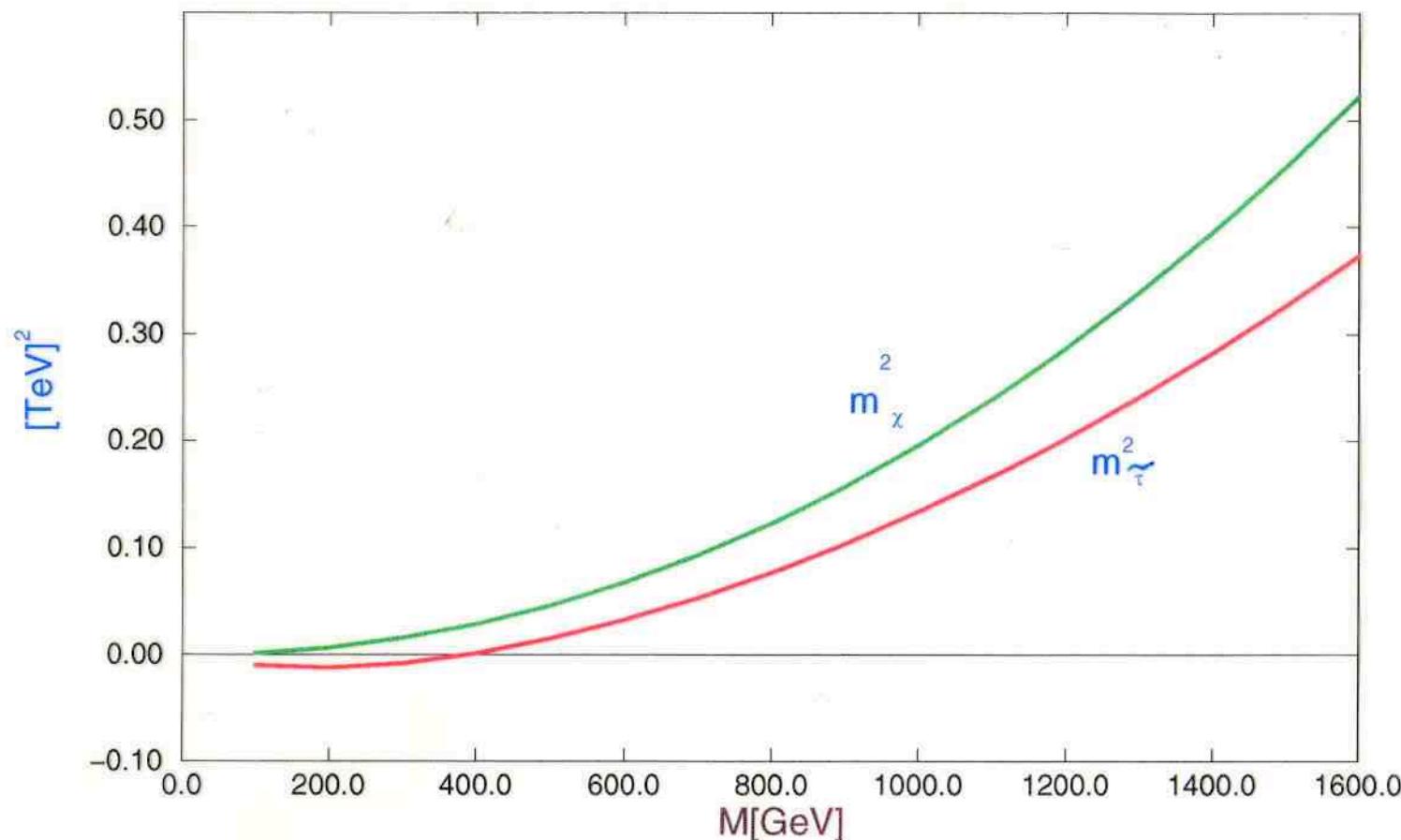
The predictions for the three models for different M_s

With theoretical corrections and uncertainties⁸
 $\sim 4\%$

$M_t = 173.8 \pm 5$ GeV 178.0 ± 4.3 GeV
CDF + D0

Model A

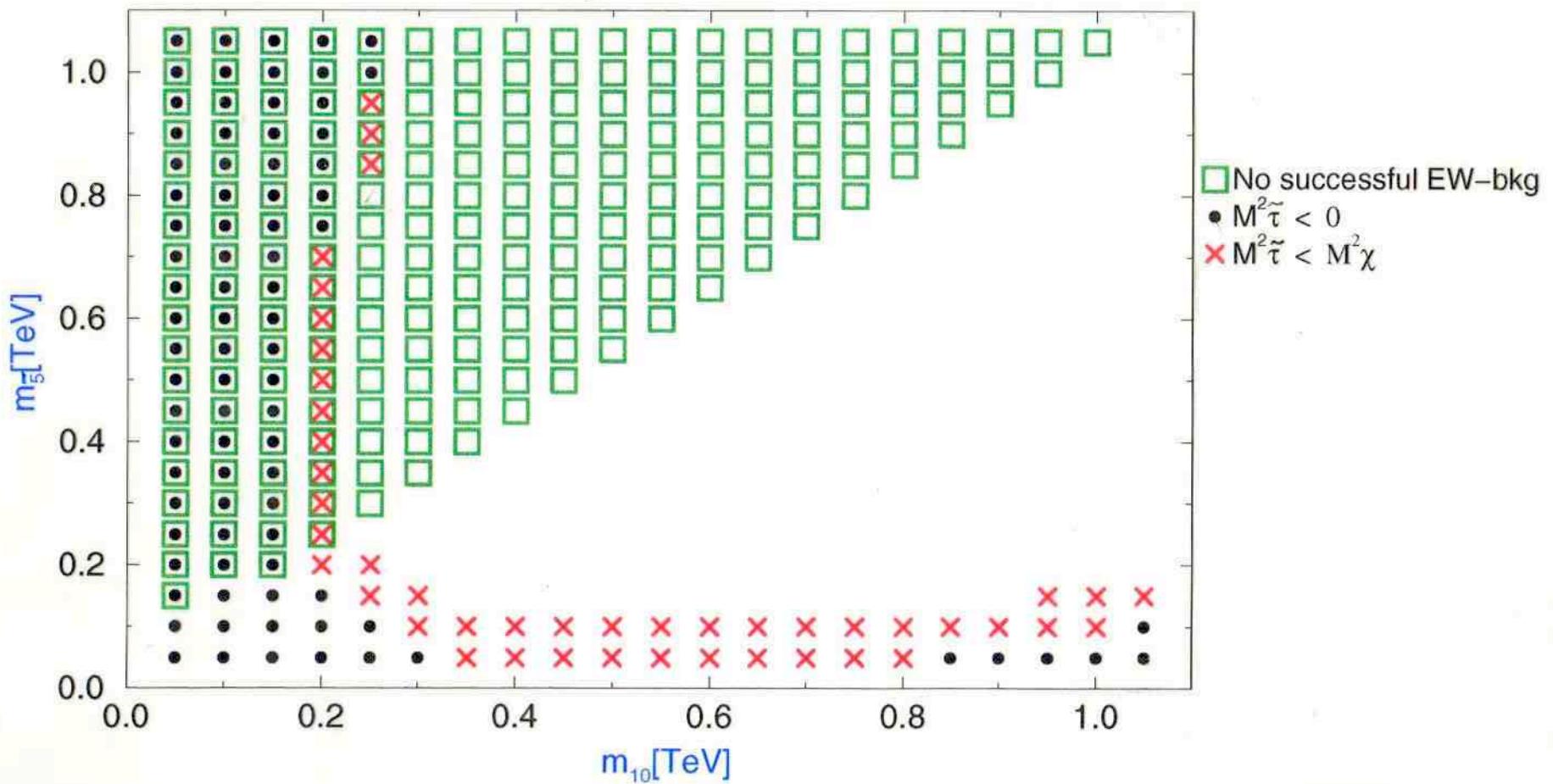
Similar behaviour holds for Model B too



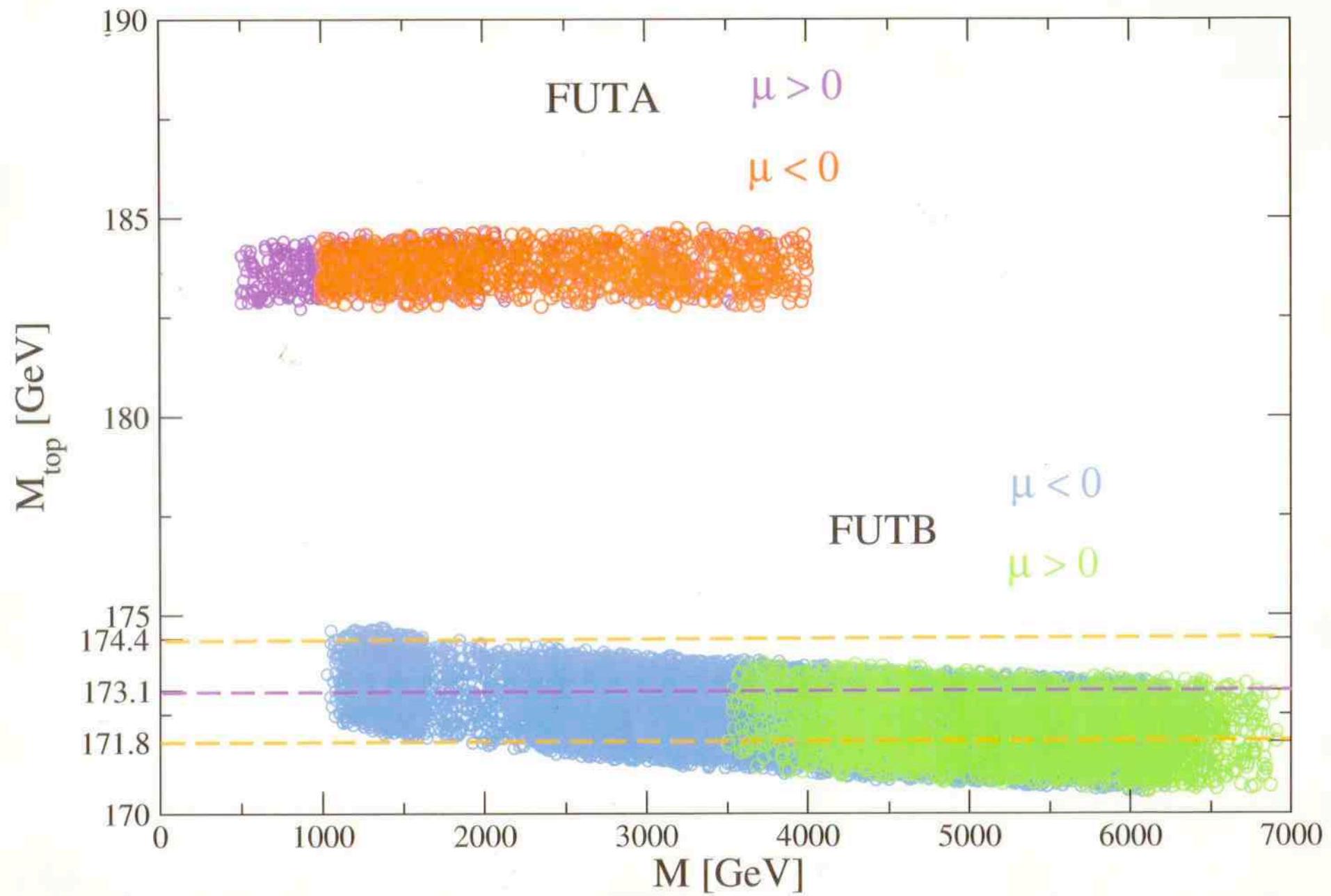
$m_{\tilde{\tau}}^2$ and m_χ^2 for the universal choice of soft scalar masses

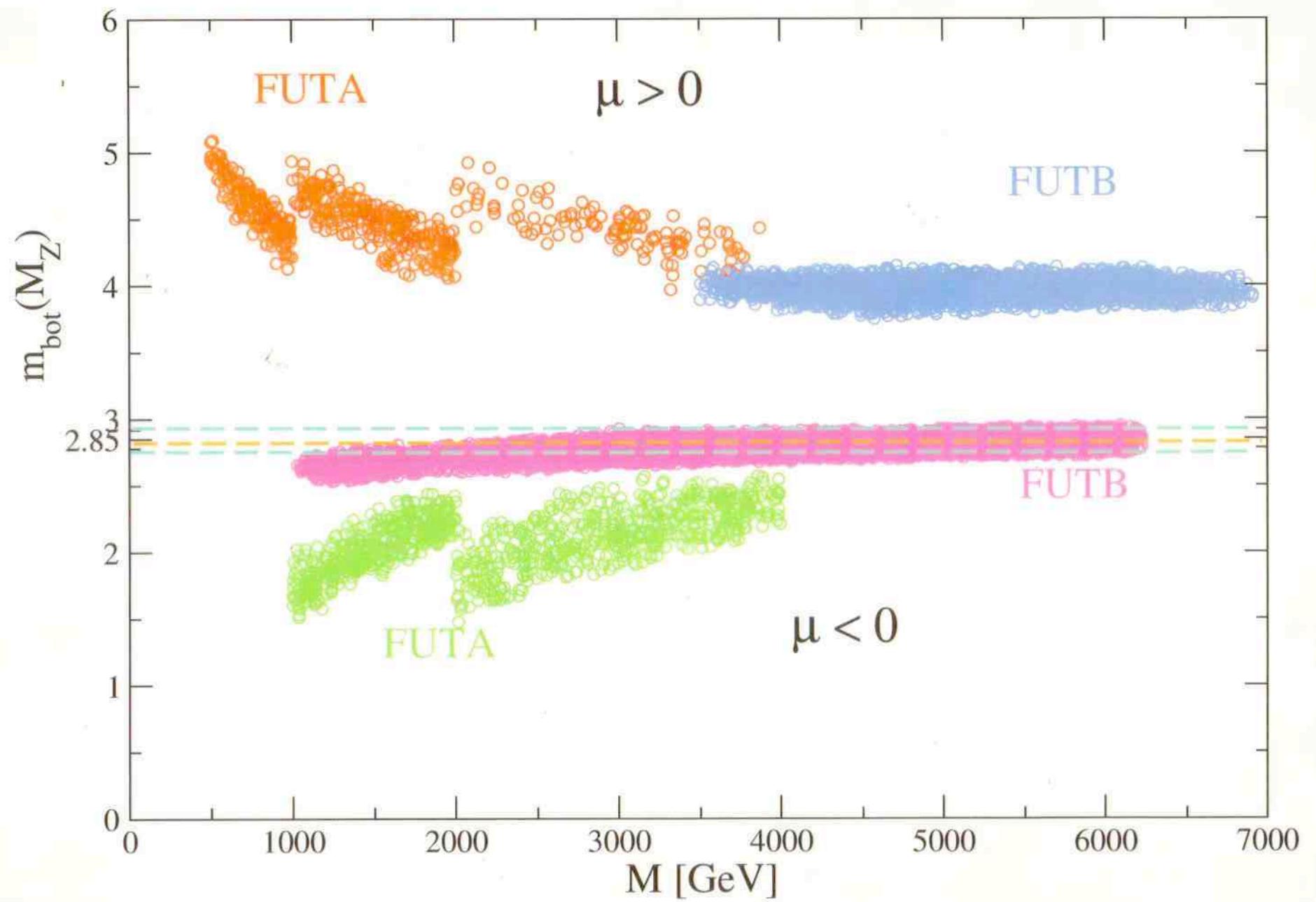
Model A

$M_{\text{susy}} = 0.3 \text{ TeV}$

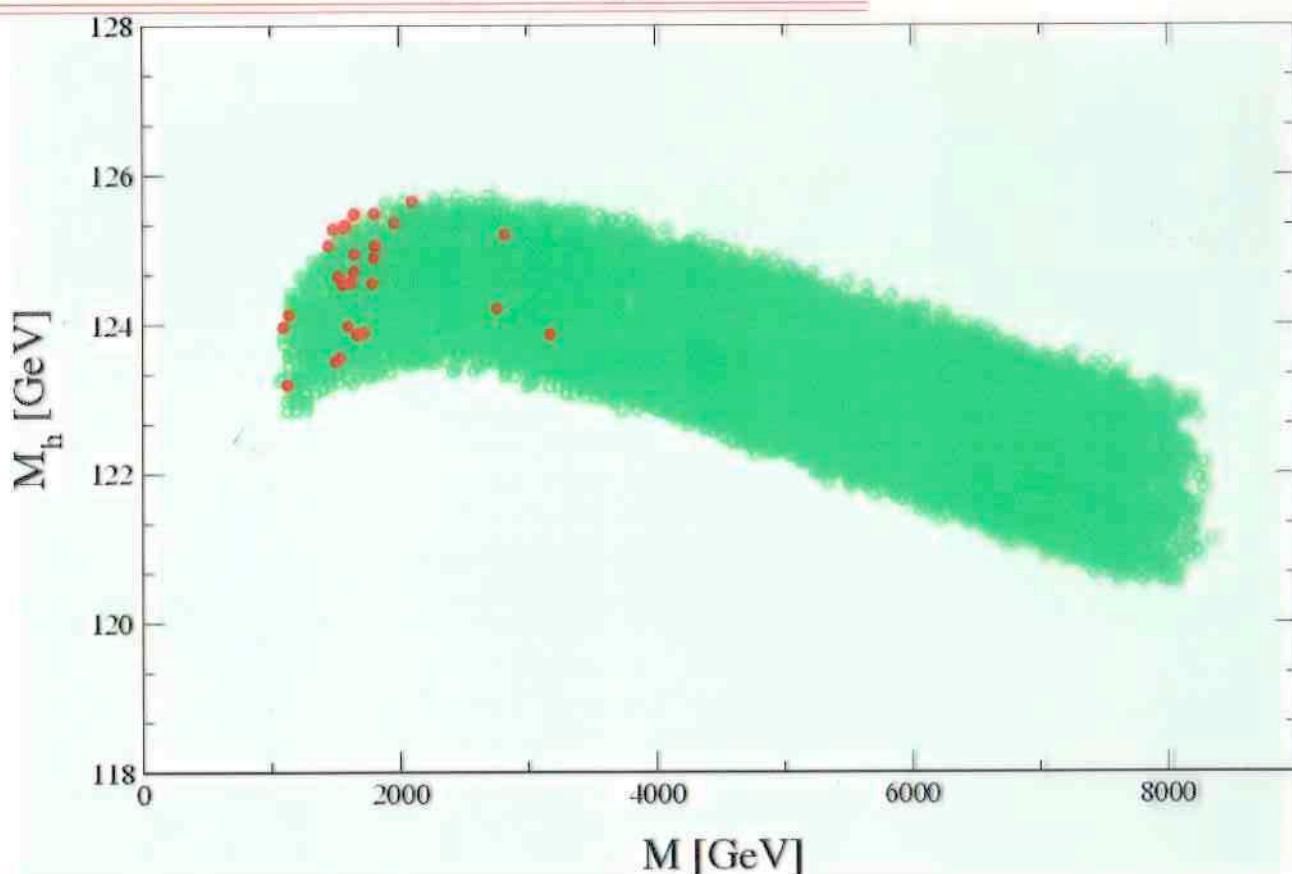


The empty region yields a neutralino as LSP





3D) Predictions for the light Higgs boson

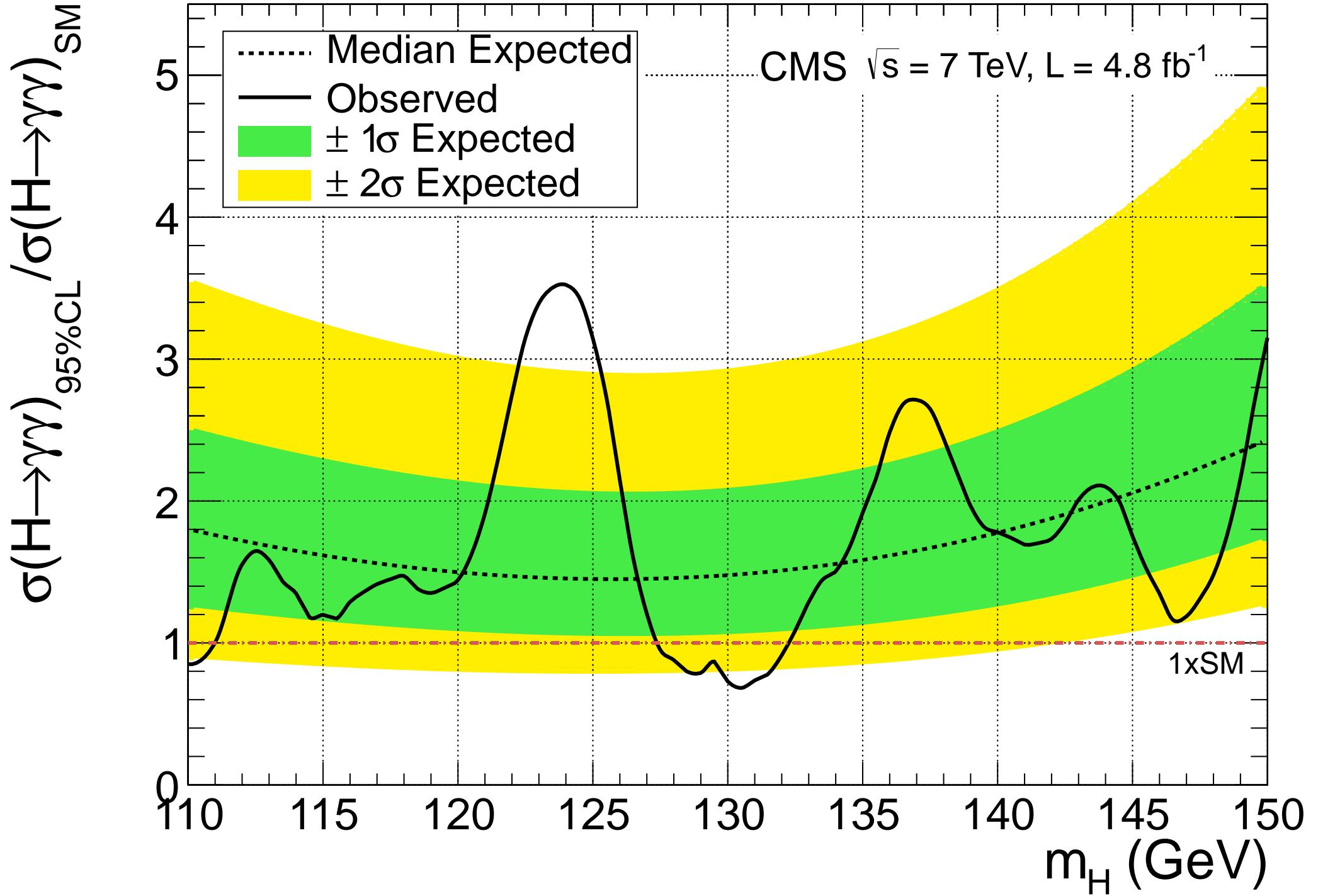


green: consistent with B physics constraints

red: agreement with (loose) CDM bound

$$118 \text{ GeV} \leq M_h \leq 129 \text{ GeV} \quad (\text{incl. theor. unc.})$$

⇒ “easy” to find for LHC (but “only” SM-like . . .)



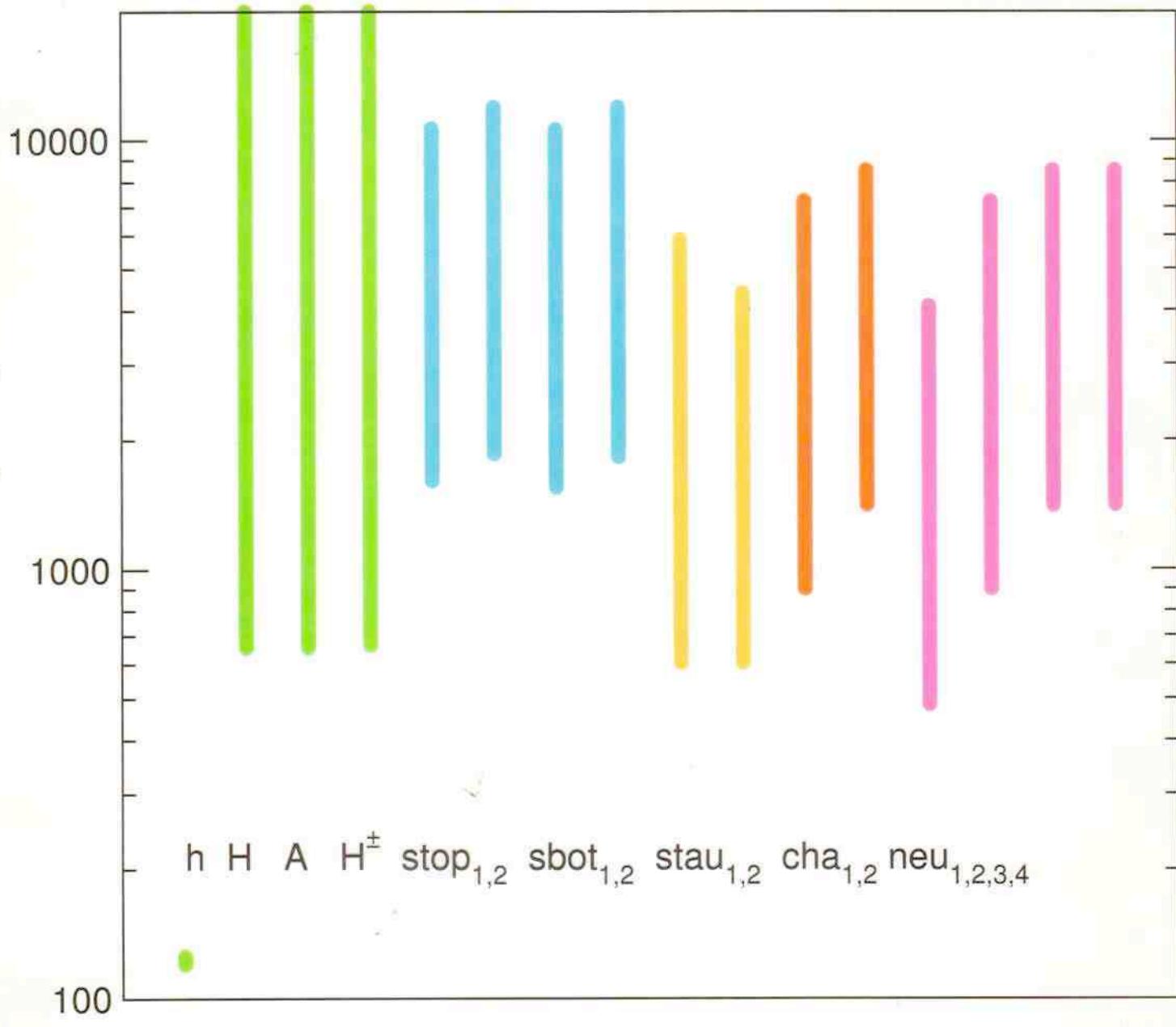
Typical mass spectrum for FUTB- :

m_t	172	$\overline{m_b}(M_Z)$	2.7
$\tan \beta =$	46	α_s	0.116
$m_{\tilde{\chi}_1^0}$	796	$m_{\tilde{\tau}_2}$	1268
$m_{\tilde{\chi}_2^0}$	1462	$m_{\tilde{\nu}_3}$	1575
$m_{\tilde{\chi}_3^0}$	2048	μ	-2046
$m_{\tilde{\chi}_4^0}$	2052	B	4722
$m_{\tilde{\chi}_1^\pm}$	1462	M_A	870
$m_{\tilde{\chi}_2^\pm}$	2052	M_{H^\pm}	875
$m_{\tilde{t}_1}$	2478	M_H	869
$m_{\tilde{t}_2}$	2804	M_h	124
$m_{\tilde{b}_1}$	2513	M_1	796
$m_{\tilde{b}_2}$	2783	M_2	1467
$m_{\tilde{\tau}_1}$	798	M_3	3655

M1	580 GeV
M2	1077 GeV
Mgluino	2754 GeV
Stop1	1876 GeV
Stop2	2146 GeV
Sbot1	1849 GeV
Sbot2	2117 GeV
Mstau1	635 GeV
Mstau2	867 GeV
Char1	1072 GeV
Char2	1597 GeV
Neu1	579 GeV
Neu2	1072 GeV
Neu3	1591 GeV
Neu4	1596 GeV
Mh	123.1 GeV
MH	679 GeV
MA	680 GeV
MH \pm	685 GeV
Mtop	172.2 GeV
Mbot(M_Z)	2.71 GeV

FUTB, $\mu < 0$

masses [GeV]



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