

Search for the Cosmic Neutrino Background and the Nuclear Beta Decay.

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Cosmic Microwave Background Radiation

(Photons in the Maximum 2 mm)

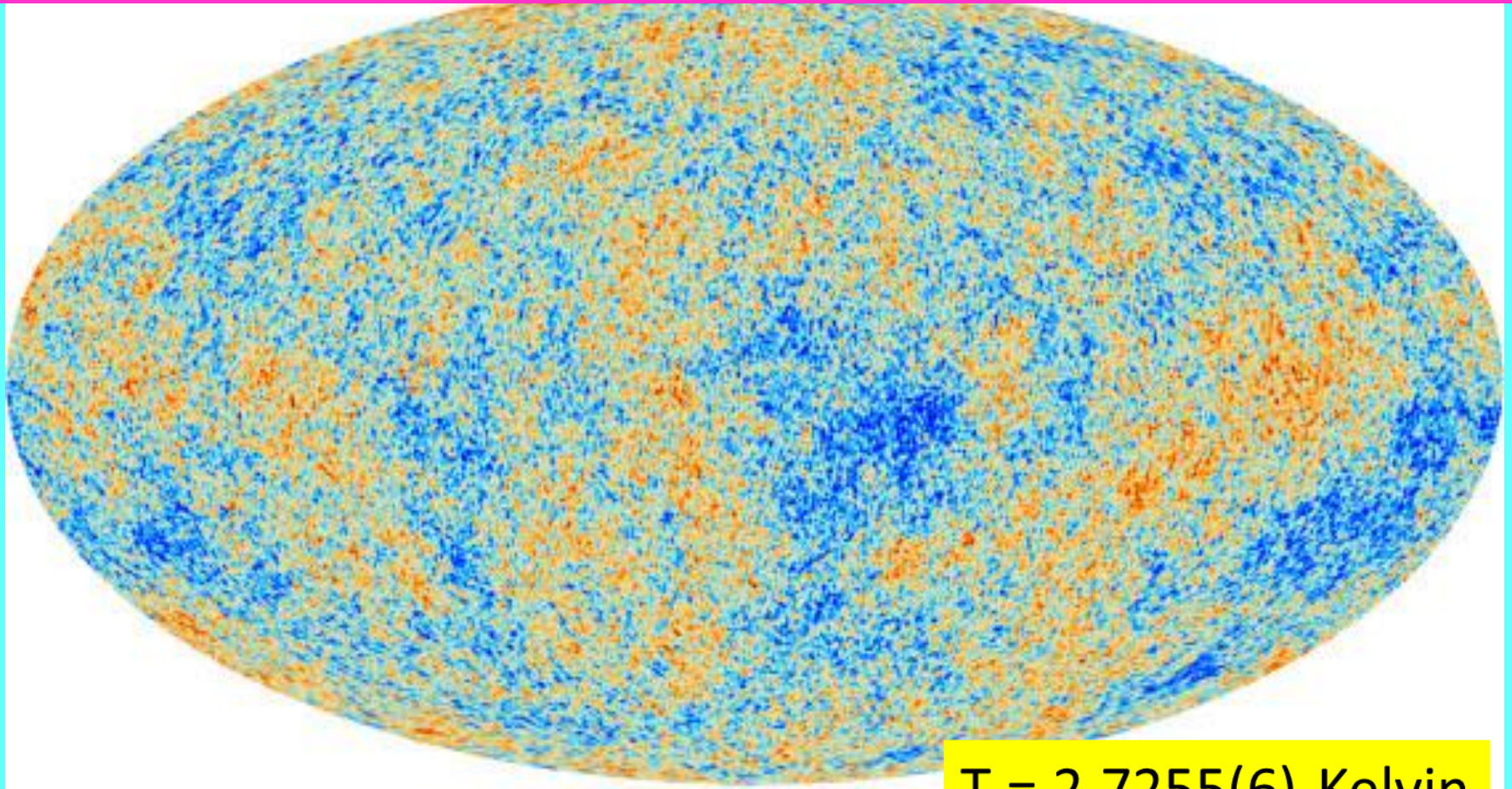
Decoupling of the photons from matter about 300 000 years after the Big Bang, when the electrons are captured by the protons and He4 nuclei and the universe gets neutral. Photons move freely.

Today: ~ 550 Photons / cm^3 (~ 340 Neutrinos/ cm^3)

Planck Satellite Temperature Fluctuations

Comic Microwave Background (Release March 21, 2013)

$$\varepsilon(f) = (8\pi h/c^3) f^3 df / [\exp(hf/k_B T) - 1] [\text{Energy/Volume}]$$



$T = 2.7255(6)$ Kelvin

Neutrino Decoupling and Cosmic Neutrino Background

For massless-massive Neutrinos:

$$N_{Fermions}(f) \propto \frac{1}{\exp((h \cdot f)/(k_B T)) + 1}$$

$f =$ frequency; $h =$ Planck's Wirkungsquantum

$$\Omega_\nu = 3 \cdot \frac{7}{8} \cdot \left(\frac{4}{11}\right)^{4/3} \cdot \Omega_{rad} = 0.68 \cdot \Omega_{rad}$$

$$\Omega(m)_\nu = \Omega(m=0)_\nu \frac{\sum m_\nu c^2}{\text{kinetic Energy} = 3k_B T} = \frac{\sum m_\nu c^2}{45\text{eV}}$$

Estimate of Neutrino Decoupling

Universe Expansion rate: $H = (da/dt)/a$;

$a \sim 1/T$; (today, Planck) $\rightarrow H = 67 \text{ km}/(\text{sec} * \text{Mpc})$

$\sim \nu$ Interaction rate: $\Gamma = n_{e-e+} \langle \sigma v_{\text{relative}} \rangle$

Neutrino Decoupling

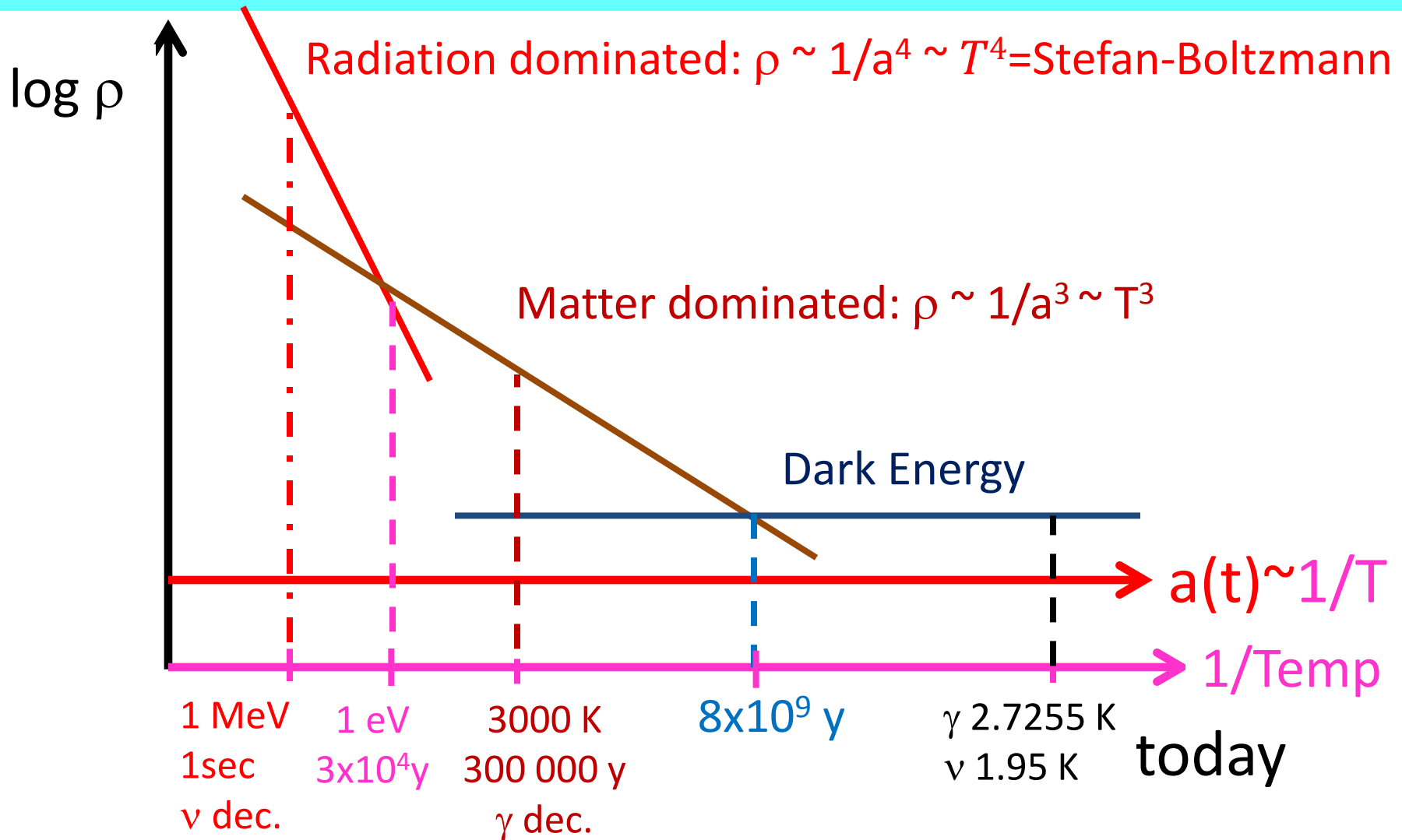
$$\Gamma/H = (k_B T / 1\text{MeV})^3 \sim 1$$

$T(\text{Neutrinos})_{\text{decoupl}} \sim 1\text{MeV} \sim 10^{10}$ Kelvin;

today: $T_\nu = 1.95$ K

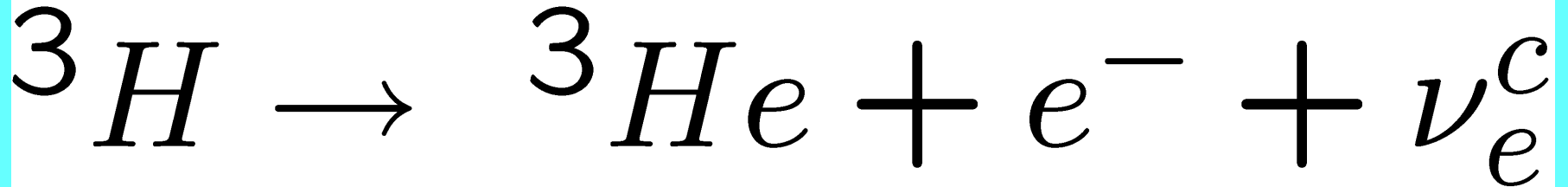
Time after Big Bang: 1 Second

(Energy=Mass)-Density of the Universe



Mass of the Electron Neutrino?

Tritium decay (Mainz + Troisk)



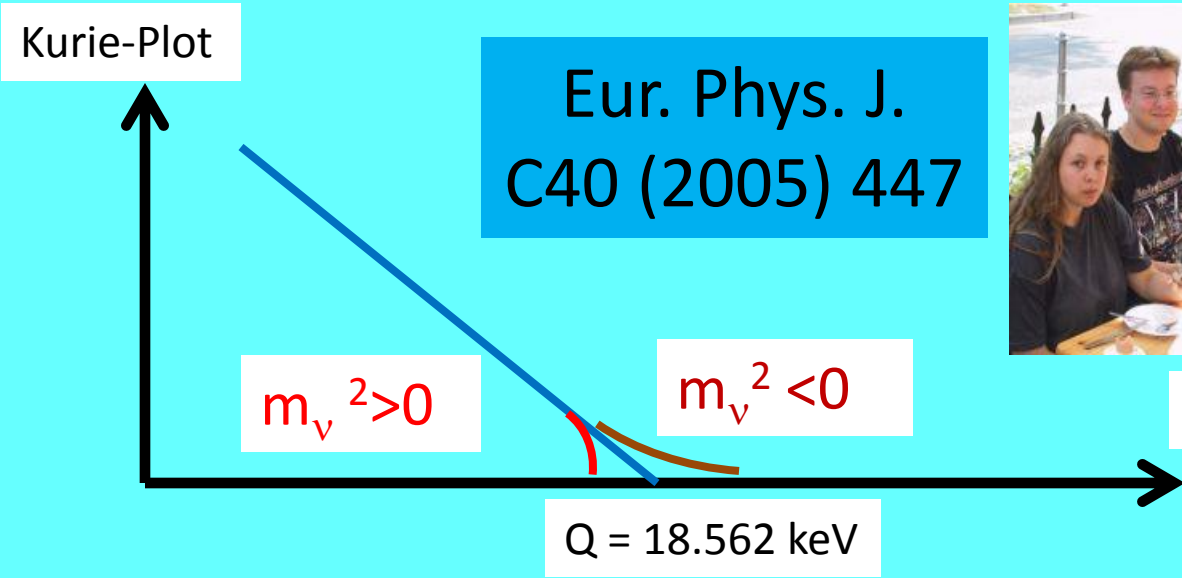
With $E_0 = Q + m_e$; $Q = 18.562\text{keV}$

$$E_e = \sqrt{m_e^2 + p_e^2} \quad E = T_e = E_e - m_e$$

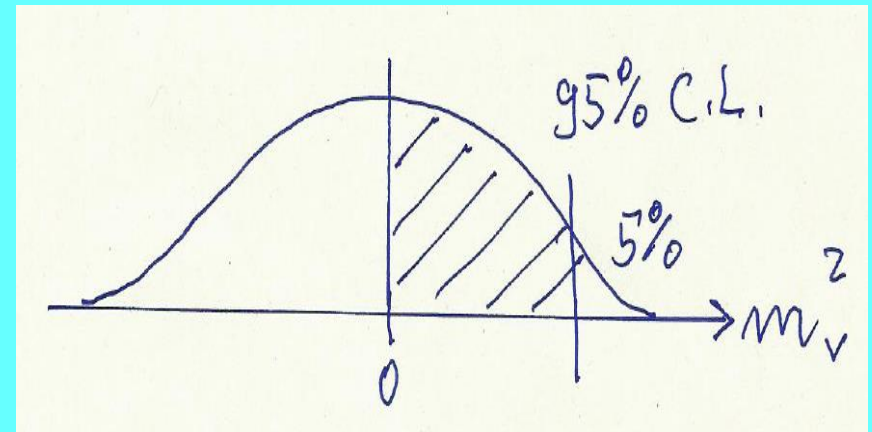
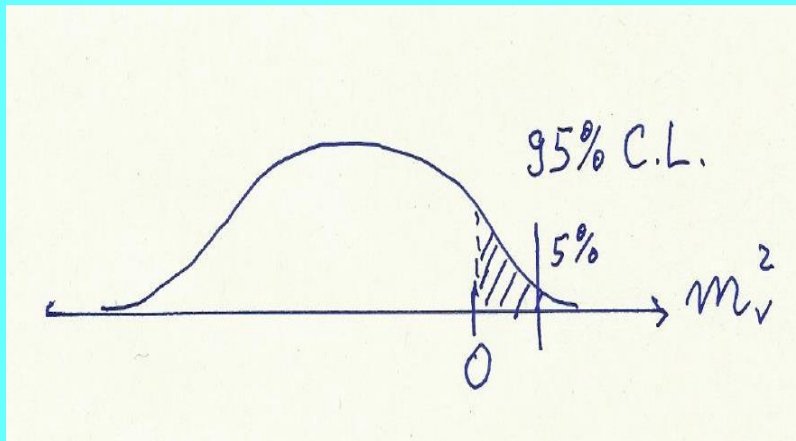
$$\frac{dN_e}{dE} = K \cdot F(E, Z) \cdot p_e E_e (E_0 - E_e) \sum_{j=1}^3 |U_{ej}|^2 \sqrt{(E_0 - E_e)^2 - m(\nu_j)^2}$$

Distinguish flavor (production) e, μ, τ
and mass $i = 1, 2, 3$ eigenstates.

Measurement of the upper Limit of the Neutrino Mass in Mainz: $m_\nu < 2.2$ eV 95% C.L.

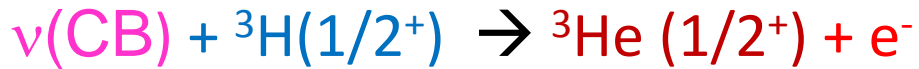


Electron Energy

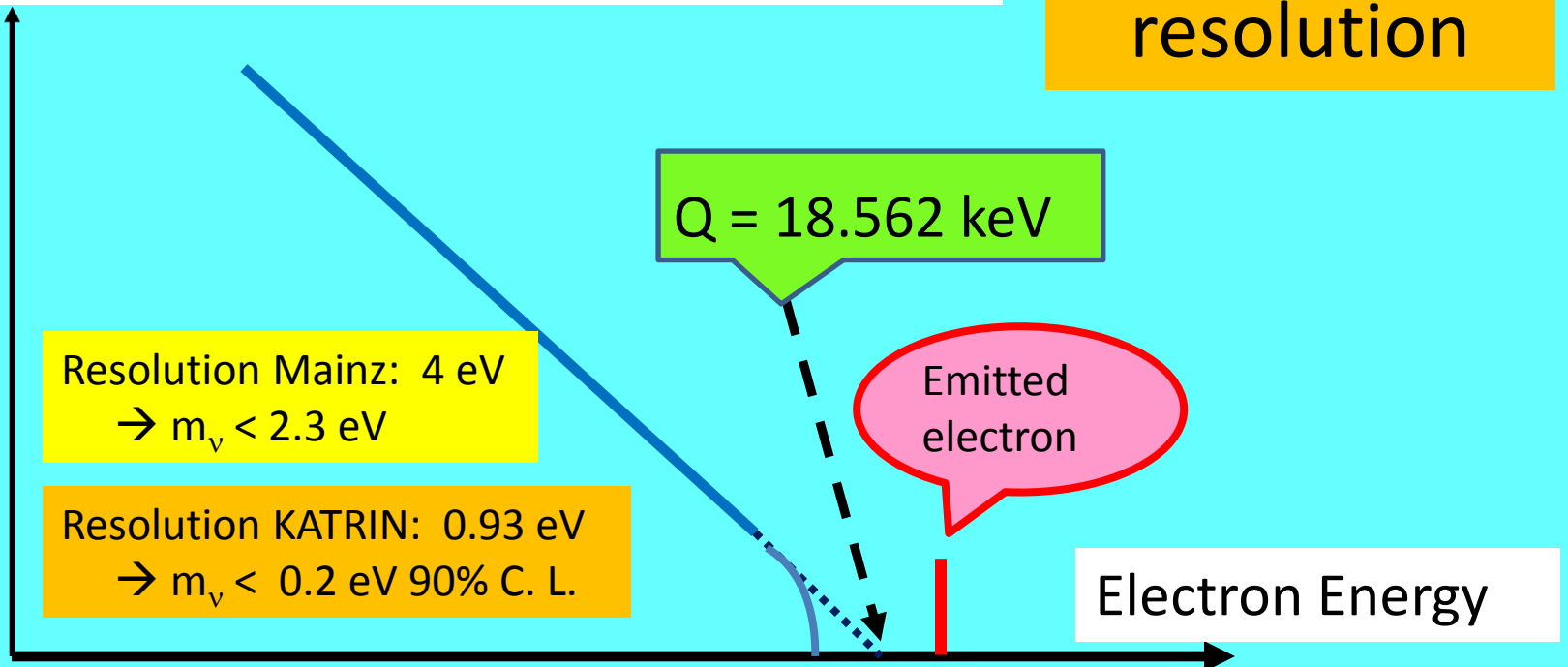


Search for Cosmic Neutrino Background CνB by Beta decay: Tritium

Kurie-Plot of Beta and induced Beta Decay:



Infinite good resolution



Fit parameters:

m_ν^2 and Q value meV

Additional fit: only intensity of CνB

Neutrino Capture: $\nu(\text{relic}) + {}^3\text{H} \rightarrow {}^3\text{He} + e^-$

$$\Gamma^\nu({}^3\text{H}) = \frac{1}{\pi} (G_F \cos(\vartheta_C))^2 \cdot F_0(Z+1, E_e) \cdot [B_F({}^3\text{H}) + B_{GT}({}^3\text{H})] p_e E_e \cdot \frac{n_{\nu e}}{\langle n_{\nu e} \rangle} \cdot \langle n_{\nu e} \rangle$$

$$\Gamma^\nu({}^3\text{H}) = 4.2 \cdot 10^{-25} \frac{n_{\nu e}}{\langle n_{\nu e} \rangle} [\text{year}^{-1}]; \text{ for one Tritium atom}$$

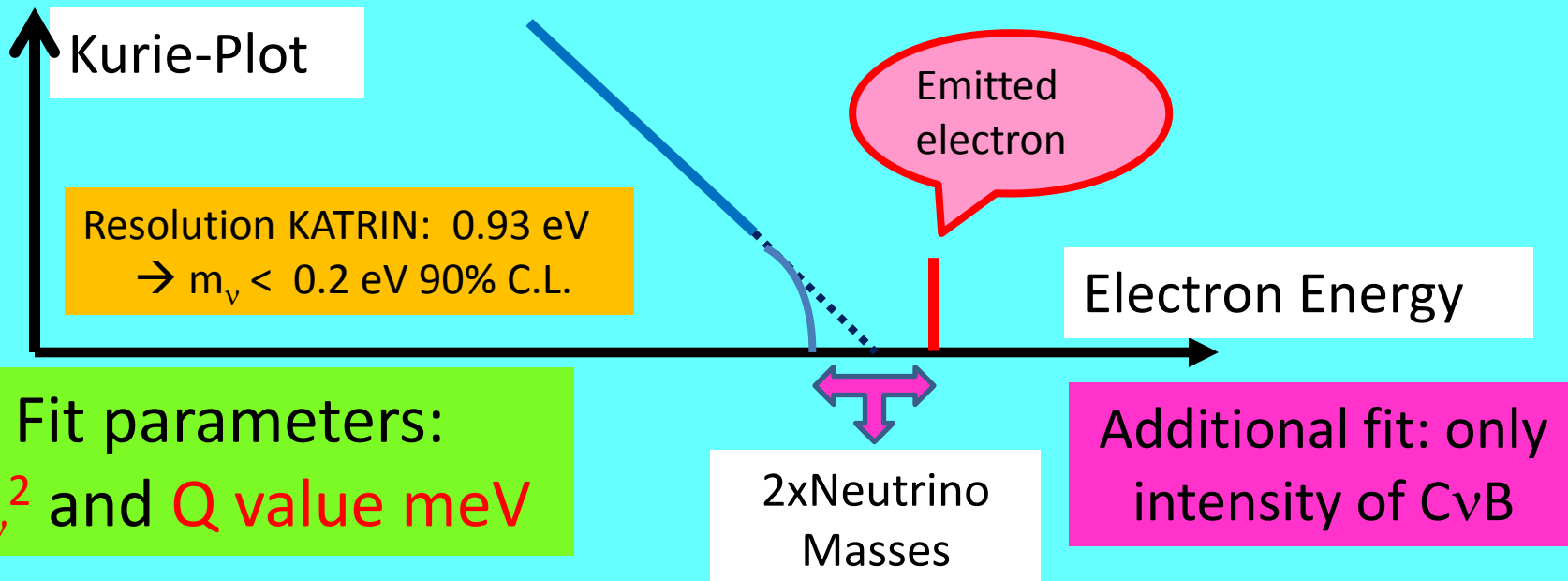
20 $\mu\text{g}(\text{eff})$ of Tritium $\rightarrow 2 \times 10^{18}$ T_2 -Molecules:

$$N_{\nu \text{ capture}}(\text{KATRIN}) = 1.7 \times 10^{-6} n_{\nu} / \langle n_{\nu} \rangle [\text{year}^{-1}]$$

Every 590 000 years a count!! for $\langle n_{\nu} \rangle = 56 \text{ cm}^{-3}$

Two Problems

1. Number of Events with average Neutrino Density of $n_{\nu_e} = 56$ [Electron-Neutrinos/cm⁻³]
KATRIN: 1 Count in 590 000 Years
Gravitational Clustering of Neutrinos!!!???
2. Energy Resolution (KATRIN) $\Delta E \sim 0.93$ eV



Gravitational Clustering of Neutrinos

R.Lazauskas, P. Vogel and C.Volpe, J. Phys.g. 35 (2008) 025001;

Light neutrinos: Gravitate only on 50 Mpc (Galaxy Cluster) scale: $n_\nu / \langle n_\nu \rangle \sim n_b / \langle n_b \rangle \sim 10^3 - 10^4$; $\langle n_b \rangle = 0.22 \cdot 10^{-6} \text{ cm}^{-3}$

A. Ringwald and Y. Wong: Vlasov trajectory simulations. Clustering on Galactic Scale possible (30 kpc to 1 Mpc)
 $n_\nu / \langle n_\nu \rangle = n_b / \langle n_b \rangle \sim 10^6$; (R = 30 kpc)

$$N_\nu \text{capture(KATRIN)} = 1.7 \times 10^{-6} n_\nu / \langle n_\nu \rangle \text{ (year}^{-1}\text{)} \\ = 1.7 \text{ [counts per year]}$$

Effective Tritium Source: 20 microgram \rightarrow 2 milligram
 $N_\nu \text{capture(KATRIN}^*) = 1.7 \times 10^{-4} n_\nu / \langle n_\nu \rangle \text{ (year}^{-1}\text{)} \\ = 170 \text{ [counts per year]}$

Summary 1

- The Cosmic Microwave Background allows to study the Universe 300 000 year after the BB.
- The Cosmic Neutrino Background 1 sec after the Big Bang (BB):
 $T_{\nu}(\text{today}) = 1.95 \text{ Kelvin}$

Summary 2

1. Average Density: $n_{\nu_e} = 56$ [Electron-Neutrinos/cm⁻³]
KATRIN: 1 Count in 590 000 Years
Gravitational Clustering of Neutrinos $n_{\nu}/\langle n_{\nu} \rangle < 10^6$
→ 1.7 counts per year (2 milligram ³H → 170 per year)

2. Measure only an upper limit of n_{ν}

