

# Pre-Big Bang, spinorial space-time, asymptotic Universe

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**Abstract -** Planck data can open the way to controversial analyses on the early Universe and its possible ultimate origin. Alternatives to standard Cosmology include pre-Big Bang approaches and new space-time geometries [1995 ->]. Basic issues related to a possible new cosmology along these lines deserve being discussed.

A generalization of the usual Friedmann approach using a spinorial space-time [1996 ->] deserves particular attention. The relation  $H.t = 1$  where  $H$  is the ratio between relative speeds and distances at cosmic scale and  $t$  the cosmic time (age of the Universe) is automatically satisfied in the absence of matter and dark energy, and space curvature can play a stronger cosmological role than in the standard Friedmann equations. It can then be conjectured that the relation  $H.t = 1$  provides the asymptotic limit of the Universe expansion as the cosmic time tends to infinity, and that the observed acceleration vanishes in this limit. Other scenarios can be considered.

also **Related papers :**

**arXiv:astro-ph/9601090 , arXiv:astro-ph/9610089**

**arXiv:hep-ph/9610474 , physics/9702026 ,**

**physics/9704017**

**arXiv:09020994 , arXiv:0905.4146 ,**

**arXiv:0908.4070 , arXiv:0912.0725 ,**

**arXiv:1011.4889 , arXiv:1110.6171 ,**

**arXiv:1202.1277 ,**

**HEP 2011 EPS-HEP2011\_479 (PoS)**

**ICFP 2012, mp\_arc 13-18 and mp\_arc 13-19**

***Planck data, spinorial space-time and***

***asymptotic universe, mp\_arc 13-33***

## Beyond the notions of Big Bang and Planck scale ?

More than eighty years after the Big Bang (quantum) hypothesis formulated by Georges Lemaître :

G. Lemaître, *The Beginning of the World from the Point of View of Quantum Theory*, *Nature* 127, 706 (1931).

and, on the expansion of the Universe :

G. Lemaître, *Un Univers homogène de masse constante et de rayon croissant rendant compte de la vitesse radiale des nébuleuses extra-galactiques*, *Ann. Soc. Sci. Brux. A* 47, 49 <http://adsabs.harvard.edu/abs/1927ASSB...47...49L>

E. Hubble, *A relation between distance and radial velocity among extra-galactic nebulae*, *PNAS* 15, 168 (1929).

WMAP, Planck and subsequent programs may allow to explore the origin of the Universe, as well as the structure of matter and space-time, beyond the “primeval quanta” and, possibly, beyond quantum mechanics, relativity...

Together with UHECR experiments.

## MANY OPEN QUESTIONS :

- **Is there a « grand unification » of standard particles and interactions ?**
- **How « ultimate » are standard particles ? What can be beyond them ?**
- **How ultimate are standard principles of Physics? Is there a new physics beyond standard quantum mechanics, relativity... ?**
- **Does the Planck scale itself make sense ?**
- **What can be the ultimate space-time geometry ? What can be its cosmological role ?**

(...)

## Space-time as seen by « elementary » particles

**Standard Particle Physics and Cosmology use a space-time with four real dimensions.**

**But in the real world, spin-1/2 particles seem to « see » a spinorial space-time described by two complex dimensions.**

**For space rotations, the spinorial  $SU(2)$  group contains twice the standard  $SO(3)$  : a 360 degrees rotation changes the sign of the spinor.**

**May look like a minor difference, but... Are there other (more subtle) differences ?**

**Why not to use a spinorial space-time instead of the conventional one ?**

# SPINORIAL SPACE-TIME

Half-integer spins exist in Nature, they cannot be generated through standard orbital angular momentum. => **What is “inside” the standard particles assumed to be “elementary” ?**

**=> A possible way to start exploring fermion structure :**

- **Replace the standard four-dimensional space-time by a SU(2) spinorial one, so that spin-1/2 particles become representations of the actual group of space transformations.**
- **Examine also possible cosmological implications of the spinorial space-time.**

⇒ Associate to each point of space-time a spinor  $\xi$  (two components, two complex numbers instead of the usual four real ones) with a SU(2) group that contains the space rotations SO(3).

Then, extracting from a cosmic spinor  $\xi$  the scalar  $|\xi|^2 = \xi^\dagger \xi$  where the dagger stands for hermitic conjugate, a positive cosmic time  $t = |\xi|$  is defined ⇒ naturally expanding universe, arrow of time.

The conventional space at cosmic time  $t_0$  corresponds to the  $|\xi| = t_0 \mathbf{S}^3$  hypersphere from the four real numbers contained in the two spinor components ⇒ local (global) SU(2) transformations provide the spinorial space rotations (translations)

**TRANSLATIONS = SU(2) rotations**  
around  $\xi = 0$  at cosmic time  $t_0$

$\xi = U \xi_0$  with  $U = \exp (i/2 t_0^{-1} \underline{\sigma} \cdot \underline{x}) \equiv U (\underline{x})$   
 $\underline{x}$  = position vector of  $\xi$  with respect to  $\xi_0$   
 $\underline{\sigma}$  = vector of  $\sigma$  matrices

**ROTATIONS = SU(2) transformations**  
acting on the translations  
and leaving invariant a point  $\xi_0 \neq 0$

$U (\underline{x}') = U (\underline{y})^\dagger U (\underline{x}) U (\underline{y})$   
 $\underline{x}'$  = new position vector of  $\xi$   
with respect to  $\xi_0$

$\underline{y}$  defines rotation axis and angle

**No matter, no critical speed, yet.**

**Arbitrariness in the definition of cosmic time :  $t$  can also be a different fonction of the spinor modulus  $|\xi| \Rightarrow$  f.i.  $t = |\xi|^2$  closer to identifying cosmic space-time variables with :  $\xi^\dagger$  (sigma quadrivector)  $\xi \Rightarrow$  Does not change the analysis that follows.**

**Spatial distances at a given cosmic time must be measured on the constant time  $S^3$  hypersphere.**

**At this stage, no space units other than the implicit time units associated to the cosmic time  $t = |\xi|$  .**

**$\Rightarrow$  For a given age of the Universe, this geometry can describe a Universe of any size as compared to our usual distance scales.**

Comoving frames in this space-time are **straight lines through  $\xi = 0$**

The distance between two such straight lines at a given time is : **angular distance x cosmic time**

**=> the relative velocity is given by the angular distance => Lemaître – Lundmark –Hubble law.**

**=>  $H.t = 1$  is natural law in this context, as  $t$  is the only available scale.**

**A natural hypothesis :**

**The  $H.t = 1$  law can remain asymptotically true at very large  $t$  if the matter density in the Universe decreases with time, as usually assumed.**

# LEMAITRE – HUBBLE LAW FROM PURE GEOMETRY

In a simple approach using the spinorial space-time with only a time scale, the Lundmark - Lemaître – Hubble constant turns out to be naturally equal to the inverse of the age of the Universe.  **$H.t = 1$  on purely geometrical grounds.**

There is also a privileged space direction at each point of space-time (the sigma matrix of which  $\xi$  is an eigenstate) => Planck data ? =>POSTER

## **WHAT ABOUT STANDARD MATTER ?**

A possible answer: just vacuum excitations similar to phonons, solitons... in condensed matter.

Standard relativity would be a low-energy limit of these excitations (similar to phonon Physics)

# SPINORIAL SPACE-TIME LINKED TO NEW VACUUM PROPERTIES ?

**A deeper vacuum structure, involving more fundamental matter or pre-matter with new physical properties (critical speed, mechanics...) and pre-Big Bang instead of inflation ?**

**An example : superbradyons, superluminal preons with critical speed in vacuum  $C_s \gg C$  ( $C$  = speed of light), or “something” beyond them.**

**Standard matter would “nucleate” at some stage during the evolution of the Universe. **When ?****

**Everywhere or only in some regions?**

**=> A privileged local rest frame (straight line)**

# A NEW COSMOLOGY WITH A (NOT REALLY) NEW SPACE-TIME AND NEW PHYSICS

The speed of light  **$c$**  is no longer a fundamental quantity in space-time geometry, and no explicit reference to standard matter, relativity or gravitation is required to get the  **$H.t = 1$**  law.

The usual standard laws of Physics (relativity, quantum mechanics...) can be just a low-energy limit applying in the sectors of the Universe where standard matter has nucleated => **Interaction between standard matter and the pre-existing geometry**

=> could the apparent acceleration of the expansion of our Universe be just a fluctuation due to such an interaction?  **$H.t = 1$**  preserved asymptotically ?

# SPINORIAL SPACE-TIME AND SPATIAL CURVATURE

Such as just presented, the spinorial space-time accounts for a space hypersphere (positive curvature). However, no specific global space units have been introduced and a transformation is possible

= > send to infinity to antipodal point ( $\xi$  rotated by 360 degrees) => turns the hypersphere in to a hyperbolic structure

For a distance  $d$  on the hypersphere bewteen  $0$  and  $\pi |\xi|$ , replace  $d$  by  $d'$  with a relation of the type

$$d^2 = \pi^2 |\xi|^2 d'^2 (\pi |\xi|^2 + d'^2)^{-1}$$

# USUAL FRIEDMANN-LIKE EQUATIONS

First Friedmann equation :

$$H^2 = 8\pi G\rho/3 - k R^{-2} c^2 + \Lambda c^2/3$$

$H = a_s^{-1} da_s/dt =$  LLH constant

$a_s =$  scale factor

$G =$  gravitational constant,

$\rho =$  energy density,

$k R^{-2} =$  curvature parameter,

$R =$  present curvature distance scale of the Universe

(curvature radius, and possibly the radius of the Universe, for  $k = 1$ )

$\Lambda =$  cosmological constant.

What if  $c$  is no longer a fundamental constant ?

In the cosmology based on the spinorial space-time, with  $\rho = 0$  and  $\Lambda = 0$ , one has  $H = t^{-1}$

$\Rightarrow t^{-2}$  replaces  $-k R^{-2} c^2$  in the Friedmann-like equation  $\Rightarrow$  amounts to :

$\Rightarrow$  replacing  $c$  by a much larger effective speed

$\Rightarrow$  changing the sign of the curvature term

$\Rightarrow$  CAN DRASTICALLY CHANGE THE COSMOLOGICAL ROLE OF THE CURVATURE TERM IN FRIEDMANN-LIKE EQUATIONS.

IN PARTICULAR :

$\Rightarrow$  NO NEED FOR DARK MATTER AND DARK ENERGY AT THAT STAGE, AS THE CURVATURE TERM ALONE CAN GENERATE THE RIGHT VALUE OF  $H \Rightarrow$  NO NEED FOR A COSMOLOGICAL CONSTANT

**THE COSMOLOGICAL CONSTANT IS NO LONGER NEEDED, EVEN FROM THE POINT OF VIEW OF PARTICLE PHYSICS (different vacuum dynamics)**

**ALSO, A NEW APPROACH TO THE SIGN AND WEIGHT OF THE CURVATURE TERM :**

**-The spinorial space-time can describe both spherical and hyperbolic space configurations, having in both cases the relation  $H.t = 1$  in the absence of matter and dark energy.**

**-The contribution to the curvature term in a Friedmann-like equation is the same in both cases, has the same (positive) sign and is able to play a leading role.**

## ON COSMIC ACCELERATION

In the  $\Lambda$ CDM model, cosmic acceleration is linked to the second Friedmann equation:

$$A = - 4/3 \pi G (\rho + 3 p_U c^{-2}) + \Lambda c^2/3$$

$$A = dH/dt + H^2 = a_s^{-1} d^2 a_s / dt^2$$

$p_U$  = pressure parameter

Dark energy contributions decreasing like the matter density as the Universe expands would not alter the relation  $H = t^{-1}$  as a limit at large  $t$ .  
New forms of  $\Lambda$  consistent with this requirement would still be acceptable (new vacuum Physics)

**BUT WHY THE PRESENT ACCELERATION ?**

New mechanisms can be imagined to explain the observed cosmic acceleration in our region of the Universe. In particular, a new term describing the reaction of standard matter to the pre-existing geometric expansion of the Universe can provide a natural way out, together with a term describing the counter-reaction of the geometry itself.

**As an example, two possible phases :**

- 1. In our region of the Universe, standard matter opposes to the Universe expansion and slows it down around us.
- 2. As the matter density decreases, its reaction to the pre-existing space-time geometry becomes weaker. At some point, the counter-reaction of the geometry becomes stronger and the Universe expansion starts accelerating until it reaches the asymptotic  $H.t = 1$  law.

**Observed approximate value :  $H.t = 0.96$**

# CONCLUSION AND COMMENTS

Considering a possible pre-Big Bang, as well as possible new ultimate constituents of matter and a new fundamental space-time can lead to important effects and to a new approach to cosmological observations => **Where does the  $H.t = 1$  law really come from ? What will it become ?**

It is of fundamental importance to elucidate the ultimate real origin of the expansion of our Universe => **is it standard cosmology, or a more primordial geometry such as the spinorial space-time considered here ?**

Considering the intrinsic properties of the spinorial space-time and the purely geometric origin of this property, we conjecture that the  $H.t = 1$  law will remain valid as  $t$  tends to infinity, up to possible small corrections.