

Pre-Big Bang, spinorial space-time, asymptotic Universe

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Abstract - Planck data can open the way to controversial analyses on the early Universe and its possible ultimate origin. Alternatives to standard Cosmology include pre-Big Bang approaches and new space-time geometries [1995 ->]. Basic issues related to a possible new cosmology along these lines deserve being discussed.

A generalization of the usual Friedmann approach using a spinorial space-time [1996 ->] deserves particular attention. The relation $H.t = 1$ where H is the ratio between relative speeds and distances at cosmic scale and t the cosmic time (age of the Universe) is automatically satisfied in the absence of matter and dark energy, and space curvature can play a stronger cosmological role than in the standard Friedmann equations. It can then be conjectured that the relation $H.t = 1$ provides the asymptotic limit of the Universe expansion as the cosmic time tends to infinity, and that the observed acceleration vanishes in this limit. Other scenarios can be considered.

also **Related papers :**

arXiv:astro-ph/9601090 , arXiv:astro-ph/9610089

arXiv:hep-ph/9610474 , physics/9702026 ,

physics/9704017

arXiv:09020994 , arXiv:0905.4146 ,

arXiv:0908.4070 , arXiv:0912.0725 ,

arXiv:1011.4889 , arXiv:1110.6171 ,

arXiv:1202.1277 ,

HEP 2011 EPS-HEP2011_479 (PoS)

ICFP 2012, mp_arc 13-18 and mp_arc 13-19

Planck data, spinorial space-time and

asymptotic universe, mp_arc 13-33

Beyond the notions of Big Bang and Planck scale ?

More than eighty years after the Big Bang (quantum) hypothesis formulated by Georges Lemaître :

G. Lemaître, *The Beginning of the World from the Point of View of Quantum Theory*, *Nature* 127, 706 (1931).

and, on the expansion of the Universe :

G. Lemaître, *Un Univers homogène de masse constante et de rayon croissant rendant compte de la vitesse radiale des nébuleuses extra-galactiques*, *Ann. Soc. Sci. Brux. A* 47, 49 <http://adsabs.harvard.edu/abs/1927ASSB...47...49L>

E. Hubble, *A relation between distance and radial velocity among extra-galactic nebulae*, *PNAS* 15, 168 (1929).

WMAP, Planck and subsequent programs may allow to explore the origin of the Universe, as well as the structure of matter and space-time, beyond the “primeval quanta” and, possibly, beyond quantum mechanics, relativity...

Together with UHECR experiments.

MANY OPEN QUESTIONS :

- **Is there a « grand unification » of standard particles and interactions ?**
- **How « ultimate » are standard particles ? What can be beyond them ?**
- **How ultimate are standard principles of Physics? Is there a new physics beyond standard quantum mechanics, relativity... ?**
- **Does the Planck scale itself make sense ?**
- **What can be the ultimate space-time geometry ? What can be its cosmological role ?**

(...)

Space-time as seen by « elementary » particles

Standard Particle Physics and Cosmology use a space-time with four real dimensions.

But in the real world, spin-1/2 particles seem to « see » a spinorial space-time described by two complex dimensions.

For space rotations, the spinorial SU(2) group contains twice the standard SO(3) : a 360 degrees rotation changes the sign of the spinor.

May look like a minor difference, but... Are there other (more subtle) differences ?

Why not to use a spinorial space-time instead of the conventional one ?

SPINORIAL SPACE-TIME

Half-integer spins exist in Nature, they cannot be generated through standard orbital angular momentum. => **What is “inside” the standard particles assumed to be “elementary” ?**

=> A possible way to start exploring fermion structure :

- **Replace the standard four-dimensional space-time by a SU(2) spinorial one, so that spin-1/2 particles become representations of the actual group of space transformations.**
- **Examine also possible cosmological implications of the spinorial space-time.**

⇒ Associate to each point of space-time a spinor ξ (two components, two complex numbers instead of the usual four real ones) with a SU(2) group that contains the space rotations SO(3).

Then, extracting from a cosmic spinor ξ the scalar $|\xi|^2 = \xi^\dagger \xi$ where the dagger stands for hermitic conjugate, a positive cosmic time $t = |\xi|$ is defined ⇒ naturally expanding universe, arrow of time.

The conventional space at cosmic time t_0 corresponds to the $|\xi| = t_0 \mathbf{S}^3$ hypersphere from the four real numbers contained in the two spinor components ⇒ local (global) SU(2) transformations provide the spinorial space rotations (translations)

TRANSLATIONS = SU(2) rotations
around $\xi = 0$ at cosmic time t_0

$$\xi = U \xi_0 \text{ with } U = \exp (i/2 t_0^{-1} \underline{\sigma} \cdot \underline{x}) \equiv U (\underline{x})$$

\underline{x} = position vector of ξ with respect to ξ_0
 $\underline{\sigma}$ = vector of σ matrices

ROTATIONS = SU(2) transformations
acting on the translations
and leaving invariant a point $\xi_0 \neq 0$

$$U (\underline{x}') = U (\underline{y})^\dagger U (\underline{x}) U (\underline{y})$$

\underline{x}' = new position vector of ξ
with respect to ξ_0

\underline{y} defines rotation axis and angle

No matter, no critical speed, yet.

Arbitrariness in the definition of cosmic time : t can also be a different fonction of the spinor modulus $|\xi| \Rightarrow$ f.i. $t = |\xi|^2$ closer to identifying cosmic space-time variables with : ξ^\dagger (sigma quadrivector) $\xi \Rightarrow$ Does not change the analysis that follows.

Spatial distances at a given cosmic time must be measured on the constant time S^3 hypersphere.

At this stage, no space units other than the implicit time units associated to the cosmic time $t = |\xi|$.

\Rightarrow For a given age of the Universe, this geometry can describe a Universe of any size as compared to our usual distance scales.

Comoving frames in this space-time are **straight lines through $\xi = 0$**

The distance between two such straight lines at a given time is : **angular distance x cosmic time**

=> the relative velocity is given by the angular distance => Lemaître – Lundmark –Hubble law.

=> $H.t = 1$ is natural law in this context, as t is the only available scale.

A natural hypothesis :

The $H.t = 1$ law can remain asymptotically true at very large t if the matter density in the Universe decreases with time, as usually assumed.

LEMAITRE – HUBBLE LAW FROM PURE GEOMETRY

In a simple approach using the spinorial space-time with only a time scale, the Lundmark - Lemaître – Hubble constant turns out to be naturally equal to the inverse of the age of the Universe. **$H.t = 1$ on purely geometrical grounds.**

There is also a privileged space direction at each point of space-time (the sigma matrix of which ξ is an eigenstate) => Planck data ? =>POSTER

WHAT ABOUT STANDARD MATTER ?

A possible answer: just vacuum excitations similar to phonons, solitons... in condensed matter.

Standard relativity would be a low-energy limit of these excitations (similar to phonon Physics)

SPINORIAL SPACE-TIME LINKED TO NEW VACUUM PROPERTIES ?

A deeper vacuum structure, involving more fundamental matter or pre-matter with new physical properties (critical speed, mechanics...) and pre-Big Bang instead of inflation ?

An example : superbradyons, superluminal preons with critical speed in vacuum $C_s \gg C$ (C = speed of light), or “something” beyond them.

Standard matter would “nucleate” at some stage during the evolution of the Universe. **When ?**

Everywhere or only in some regions?

=> A privileged local rest frame (straight line)

A NEW COSMOLOGY WITH A (NOT REALLY) NEW SPACE-TIME AND NEW PHYSICS

The speed of light **c** is no longer a fundamental quantity in space-time geometry, and no explicit reference to standard matter, relativity or gravitation is required to get the **$H.t = 1$** law.

The usual standard laws of Physics (relativity, quantum mechanics...) can be just a low-energy limit applying in the sectors of the Universe where standard matter has nucleated => **Interaction between standard matter and the pre-existing geometry**

=> could the apparent acceleration of the expansion of our Universe be just a fluctuation due to such an interaction? **$H.t = 1$** preserved asymptotically ?

SPINORIAL SPACE-TIME AND SPATIAL CURVATURE

Such as just presented, the spinorial space-time accounts for a space hypersphere (positive curvature). However, no specific global space units have been introduced and a transformation is possible

= > send to infinity to antipodal point (ξ rotated by 360 degrees) => turns the hypersphere in to a hyperbolic structure

For a distance d on the hypersphere bewteen 0 and $\pi |\xi|$, replace d by d' with a relation of the type

$$d^2 = \pi^2 |\xi|^2 d'^2 (\pi |\xi|^2 + d'^2)^{-1}$$

USUAL FRIEDMANN-LIKE EQUATIONS

First Friedmann equation :

$$H^2 = 8\pi G\rho/3 - k R^{-2} c^2 + \Lambda c^2/3$$

$H = a_s^{-1} da_s/dt =$ LLH constant

$a_s =$ scale factor

$G =$ gravitational constant,

$\rho =$ energy density,

$k R^{-2} =$ curvature parameter,

$R =$ present curvature distance scale of the Universe

(curvature radius, and possibly the radius of the Universe,
for $k = 1$)

$\Lambda =$ cosmological constant.

What if c is no longer a fundamental constant ?

In the cosmology based on the spinorial space-time, with $\rho = 0$ and $\Lambda = 0$, one has $H = t^{-1}$

$\Rightarrow t^{-2}$ replaces $-k R^{-2} c^2$ in the Friedmann-like equation \Rightarrow amounts to :

\Rightarrow replacing c by a much larger effective speed

\Rightarrow changing the sign of the curvature term

\Rightarrow CAN DRASTICALLY CHANGE THE COSMOLOGICAL ROLE OF THE CURVATURE TERM IN FRIEDMANN-LIKE EQUATIONS.

IN PARTICULAR :

\Rightarrow NO NEED FOR DARK MATTER AND DARK ENERGY AT THAT STAGE, AS THE CURVATURE TERM ALONE CAN GENERATE THE RIGHT VALUE OF $H \Rightarrow$ NO NEED FOR A COSMOLOGICAL CONSTANT

THE COSMOLOGICAL CONSTANT IS NO LONGER NEEDED, EVEN FROM THE POINT OF VIEW OF PARTICLE PHYSICS (different vacuum dynamics)

ALSO, A NEW APPROACH TO THE SIGN AND WEIGHT OF THE CURVATURE TERM :

-The spinorial space-time can describe both spherical and hyperbolic space configurations, having in both cases the relation $H.t = 1$ in the absence of matter and dark energy.

-The contribution to the curvature term in a Friedmann-like equation is the same in both cases, has the same (positive) sign and is able to play a leading role.

ON COSMIC ACCELERATION

In the Λ CDM model, cosmic acceleration is linked to the second Friedmann equation:

$$A = -4/3 \pi G (\rho + 3 p_U c^{-2}) + \Lambda c^2/3$$

$$A = dH/dt + H^2 = a_s^{-1} d^2 a_s / dt^2$$

p_U = pressure parameter

Dark energy contributions decreasing like the matter density as the Universe expands would not alter the relation $H = t^{-1}$ as a limit at large t .
New forms of Λ consistent with this requirement would still be acceptable (new vacuum Physics)

BUT WHY THE PRESENT ACCELERATION ?

New mechanisms can be imagined to explain the observed cosmic acceleration in our region of the Universe. In particular, a new term describing the reaction of standard matter to the pre-existing geometric expansion of the Universe can provide a natural way out, together with a term describing the counter-reaction of the geometry itself.

As an example, two possible phases :

- 1. In our region of the Universe, standard matter opposes to the Universe expansion and slows it down around us.
- 2. As the matter density decreases, its reaction to the pre-existing space-time geometry becomes weaker. At some point, the counter-reaction of the geometry becomes stronger and the Universe expansion starts accelerating until it reaches the asymptotic $H.t = 1$ law.

Observed approximate value : $H.t = 0.96$

CONCLUSION AND COMMENTS

Considering a possible pre-Big Bang, as well as possible new ultimate constituents of matter and a new fundamental space-time can lead to important effects and to a new approach to cosmological observations => **Where does the $H.t = 1$ law really come from ? What will it become ?**

It is of fundamental importance to elucidate the ultimate real origin of the expansion of our Universe => **is it standard cosmology, or a more primordial geometry such as the spinorial space-time considered here ?**

Considering the intrinsic properties of the spinorial space-time and the purely geometric origin of this property, we conjecture that the $H.t = 1$ law will remain valid as t tends to infinity, up to possible small corrections.