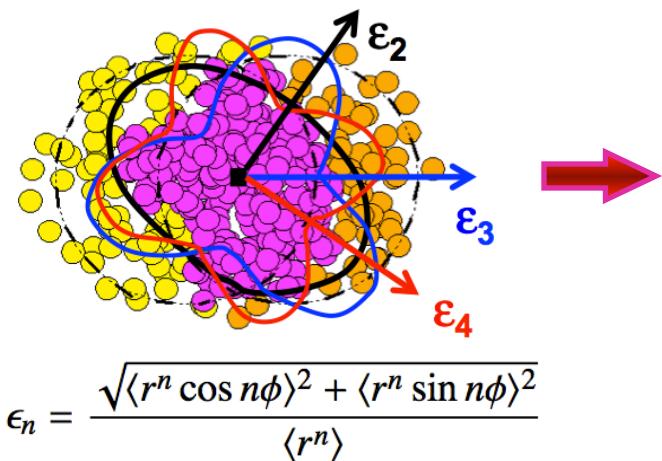


# Initial Geometry & jet quenching



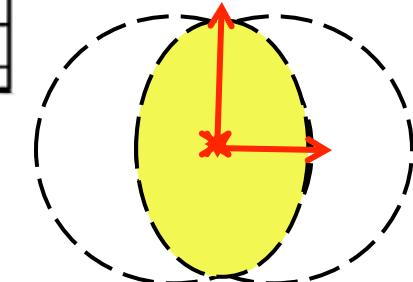
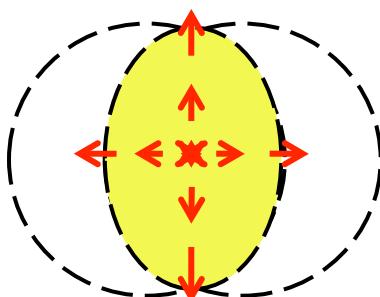
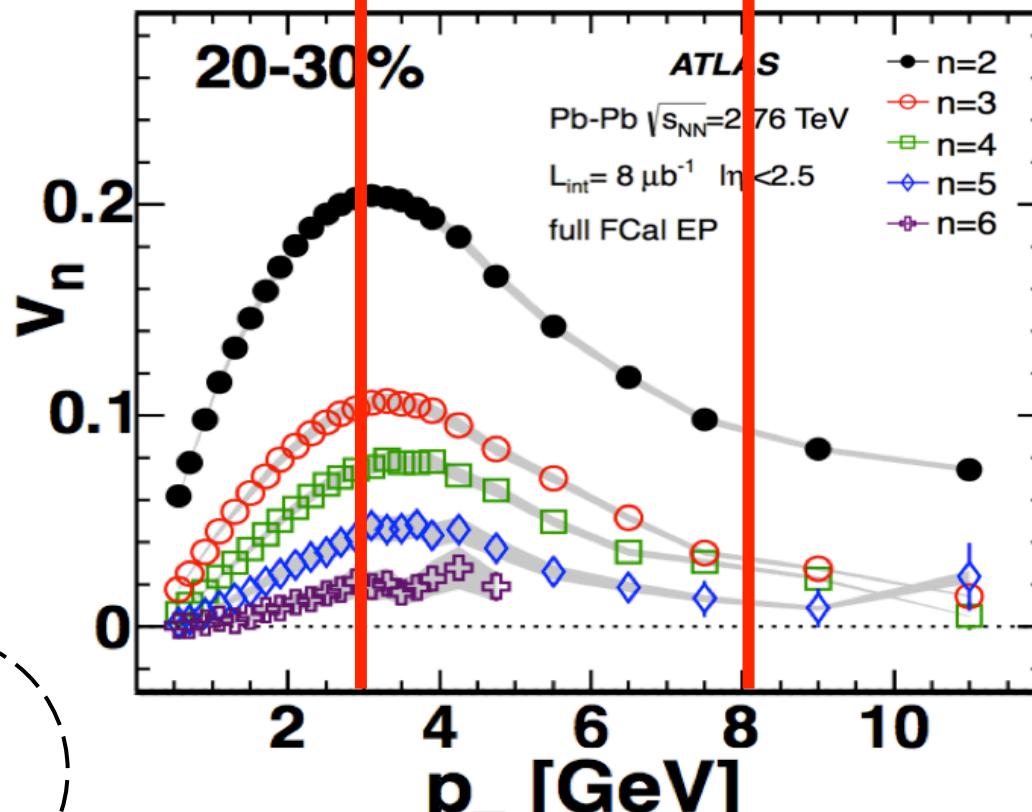
$$\frac{dN}{d\phi} \propto 1 + \sum_n 2v_n \cos n(\phi - \Phi_n)$$

$$\frac{dN}{d\Delta\phi} = \left[ \frac{dN}{d\phi_a} * \frac{dN}{d\phi_b} \right] \propto 1 + \sum_n 2v_n^a v_n^b \cos(n\Delta\phi)$$

- Event averaged quantities:  $v_n(p_T, \eta, \text{cent}, n, \text{PID})$ 
  - Geometry & high  $p_T$   $v_n$
  - Dipole asymmetry and  $v_1$
- Event-by-event quantities
  - Correlations between  $\Phi_n$ .
  - Distribution of  $v_n$
  - Event shape engineering.

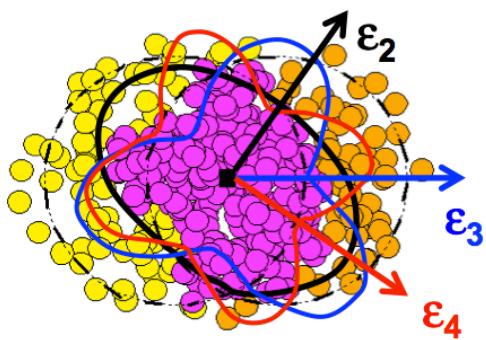
# Origin of single particle $v_n(p_T, \eta, \text{cent}, n)$

Hydrodynamics ← → Jet quenching

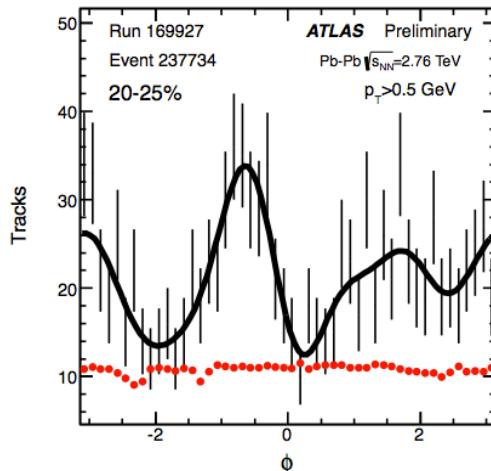


- Both effects are related to global geometry → ridge & factorization

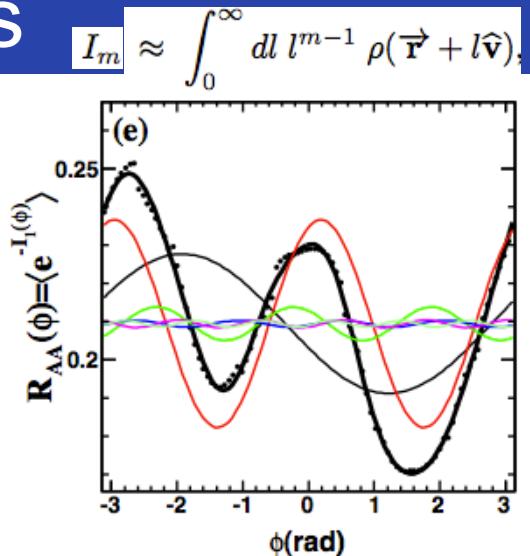
# Three different planes



Participant plane (PP)

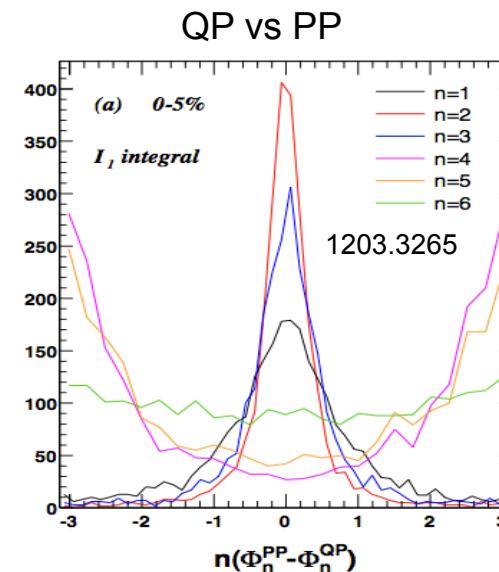
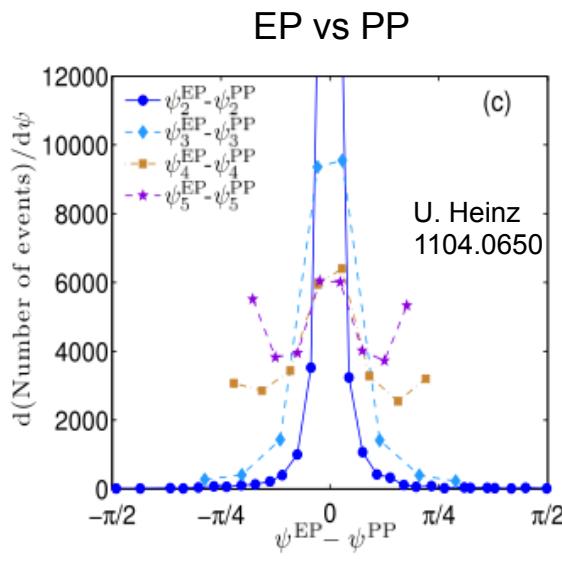


Event plane (EP)



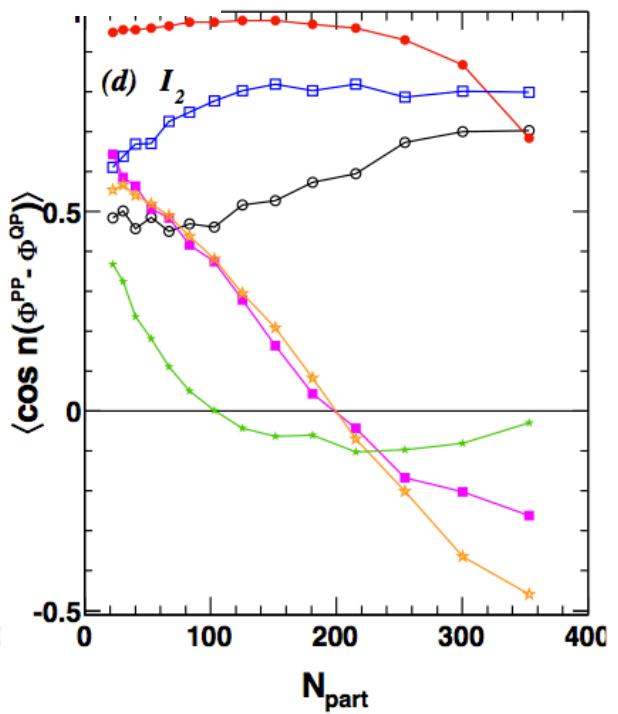
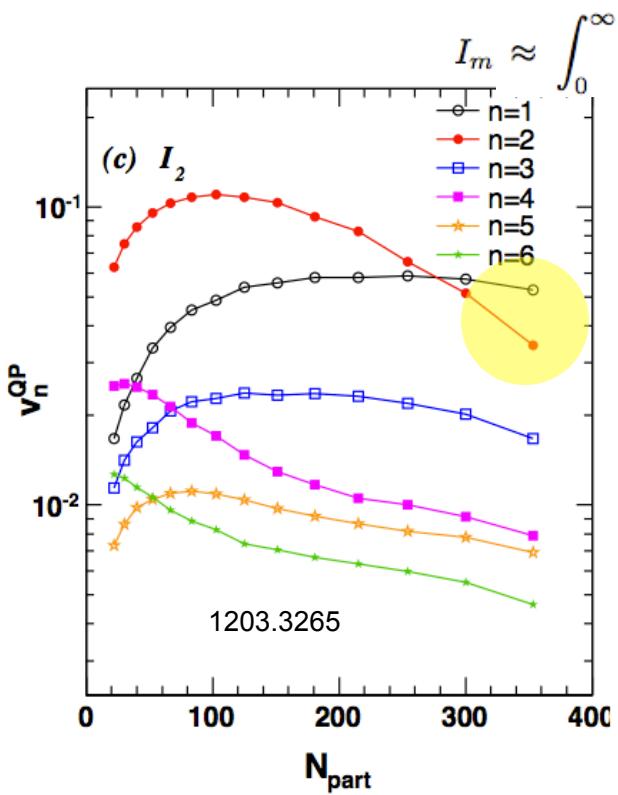
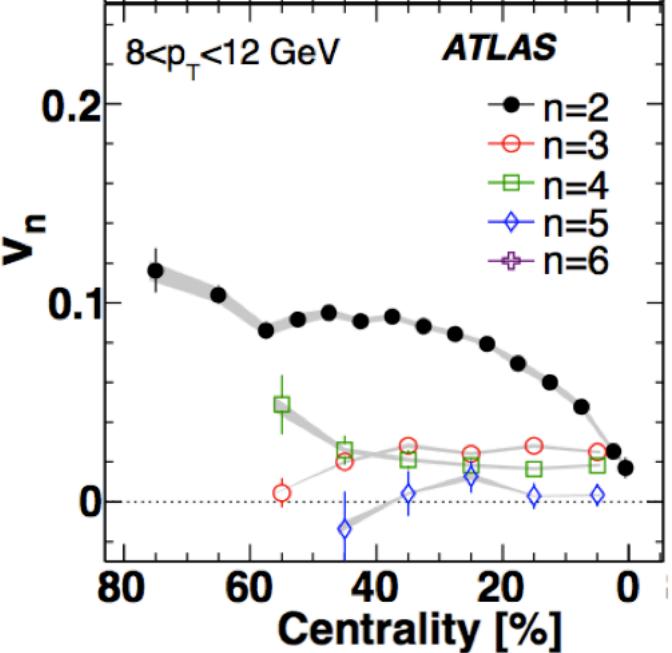
Quenching plane (QP)

- PP, EP and QP can be different from each other



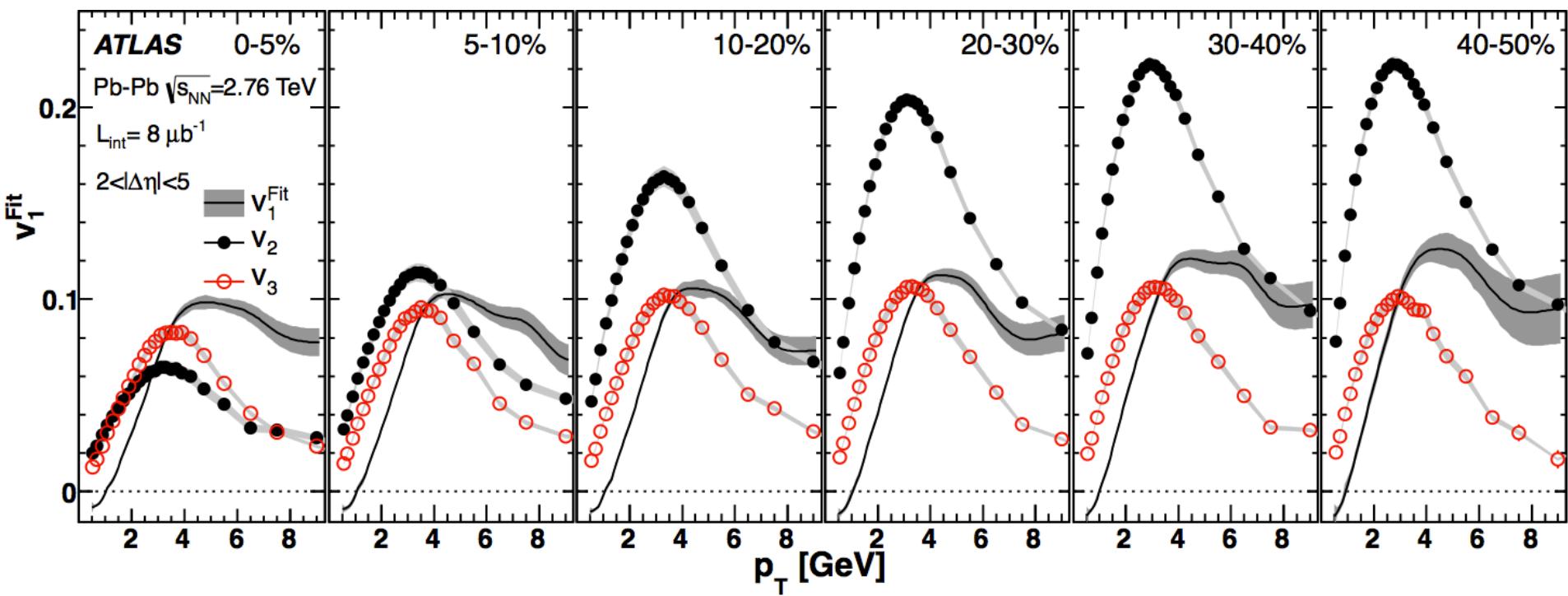
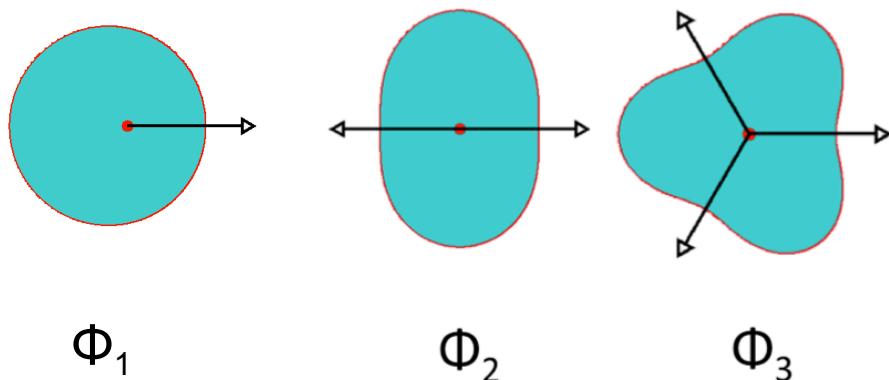
# Consequence on high $p_T$ $v_n$

- Intrinsic anisotropy due to jet quenching can be sizable
  - But QP de-correlated with the PP, so possibly also with EP.
  - Interpretation of  $v_n$  for  $n > 3$  can be complicated.

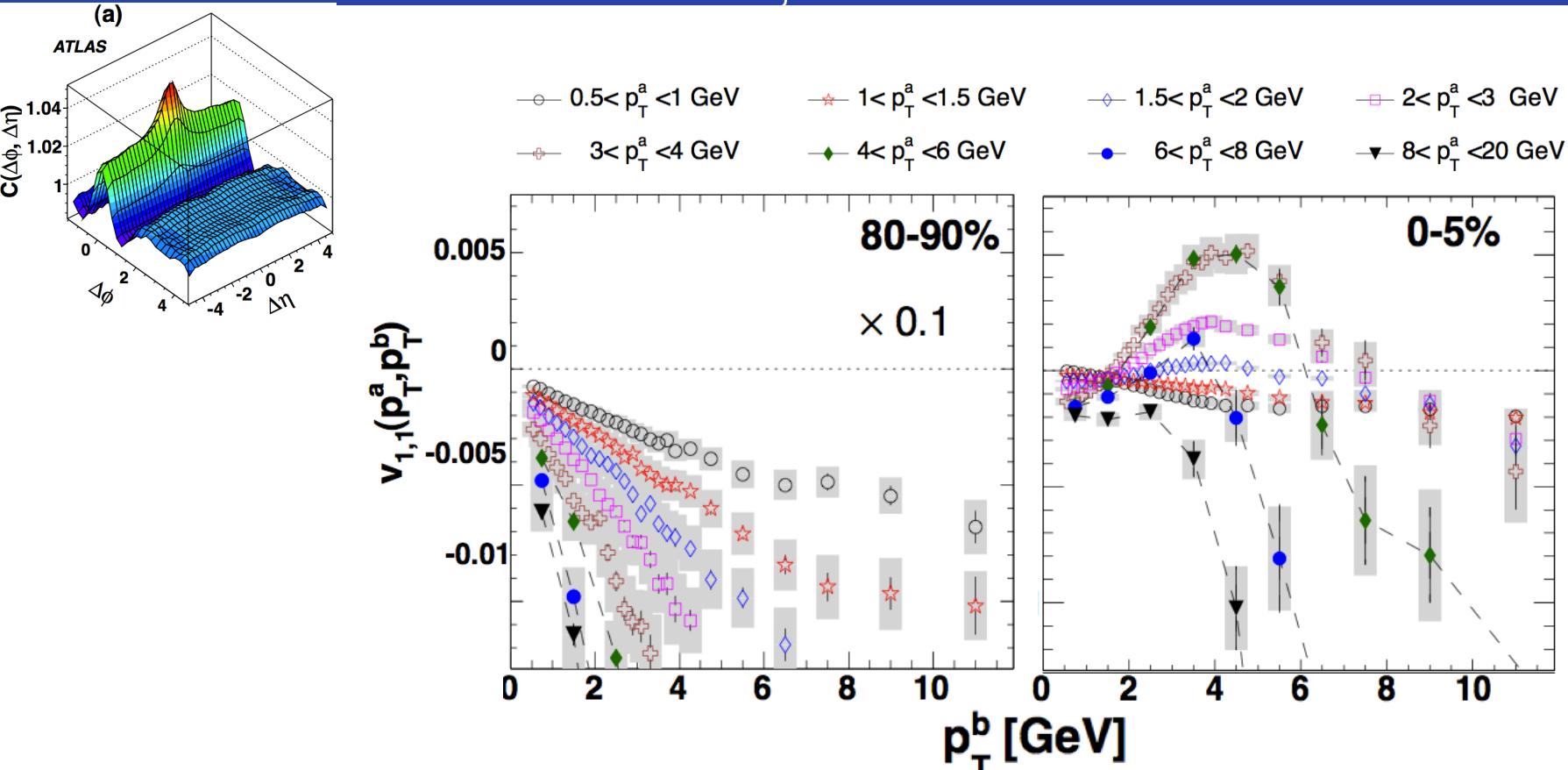


# “Surprisingly” large rapidity-even (dipolar) $v_1$

- Sizable dipole asymmetry in initial geometry



# First coefficient $v_{1,1} = \langle \cos \Delta\phi \rangle$ from 2PC

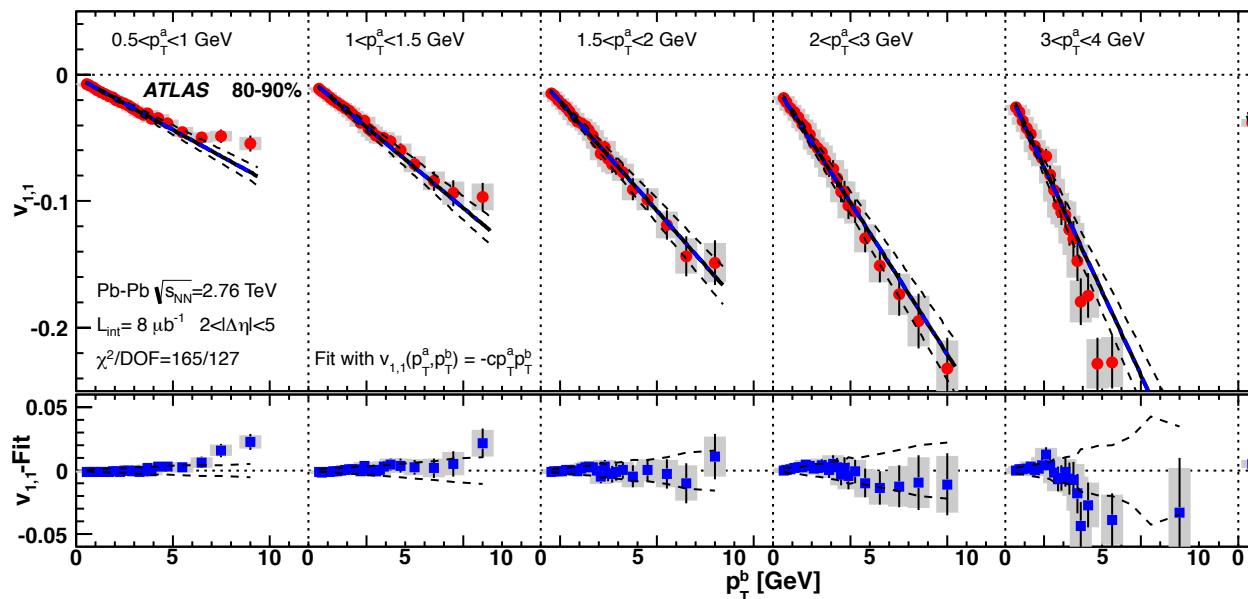


- Peripheral collisions (GMC dominated):  $v_{1,1}$  negative, linear in  $p_T^a, p_T^b$ .
- Central collisions (flow dominated):  $v_{1,1}$  becomes positive at 1.5-6 GeV range, but on top of a negative momentum conservation component
- Cross each other at low  $p_T \rightarrow$  where flow driven  $v_{1,1} \sim$  zero.

# Dipolar $v_1$ from 2PC via two-component fit

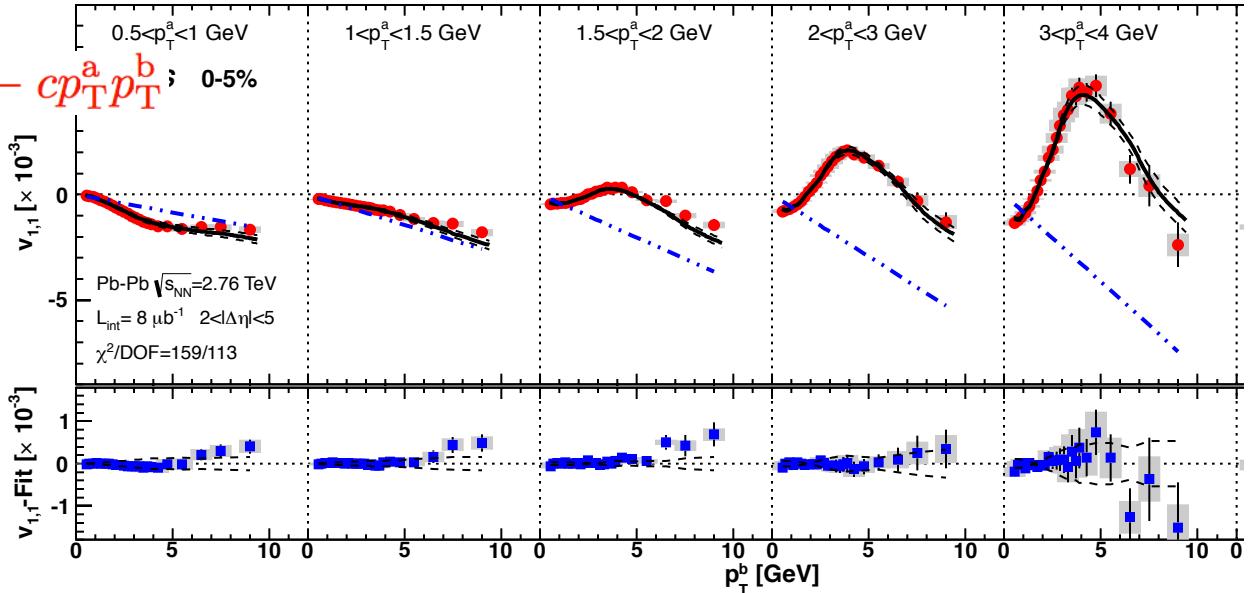
$$v_{1,1}(p_T^a, p_T^b) = -cp_T^a p_T^b$$

Momentum conservation  
describe the  $\cos\Delta\phi$  even  
at 10 GeV!

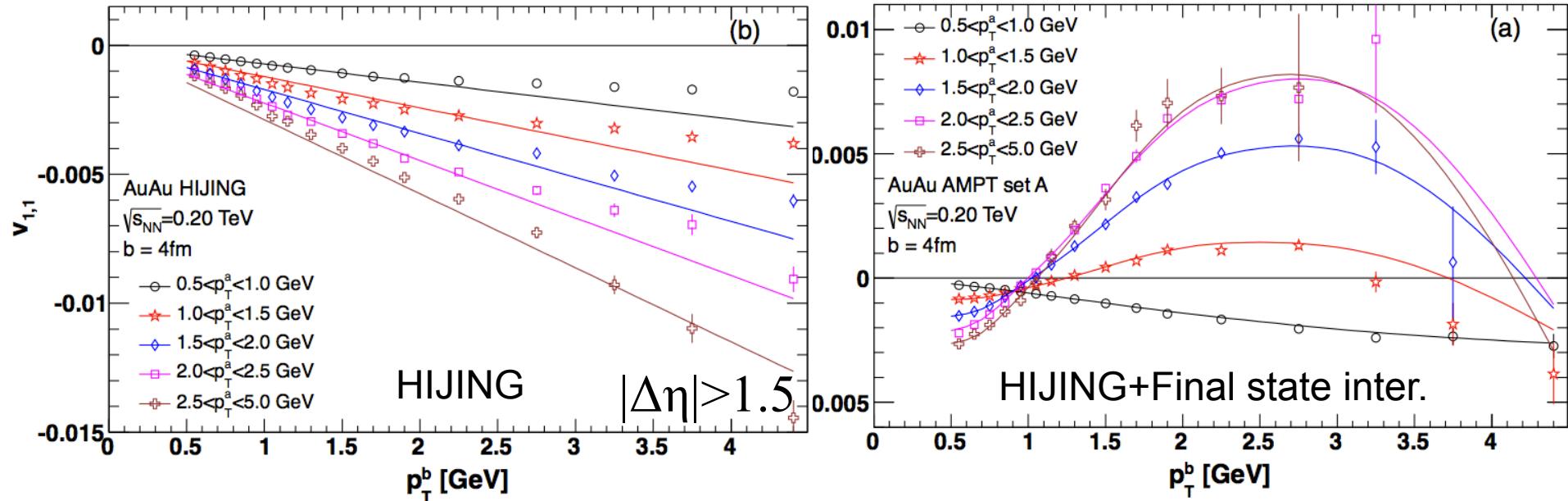


$$v_{1,1}(p_T^a, p_T^b) = v_1^{\text{Fit}}(p_T^a) v_1^{\text{Fit}}(p_T^b) - cp_T^a p_T^b; \quad 0-5\%$$

Dipolar flow is  
dominates over GMC  
over 2-6 GeV



# Comparison with AMPT model: arxiv:1203.3410<sup>8</sup>



$$v_{1,1}(p_T^a, p_T^b) = -cp_T^a p_T^b$$

$$v_{1,1}(p_T^a, p_T^b) = v_1^{\text{Fit}}(p_T^a)v_1^{\text{Fit}}(p_T^b) - cp_T^a p_T^b$$

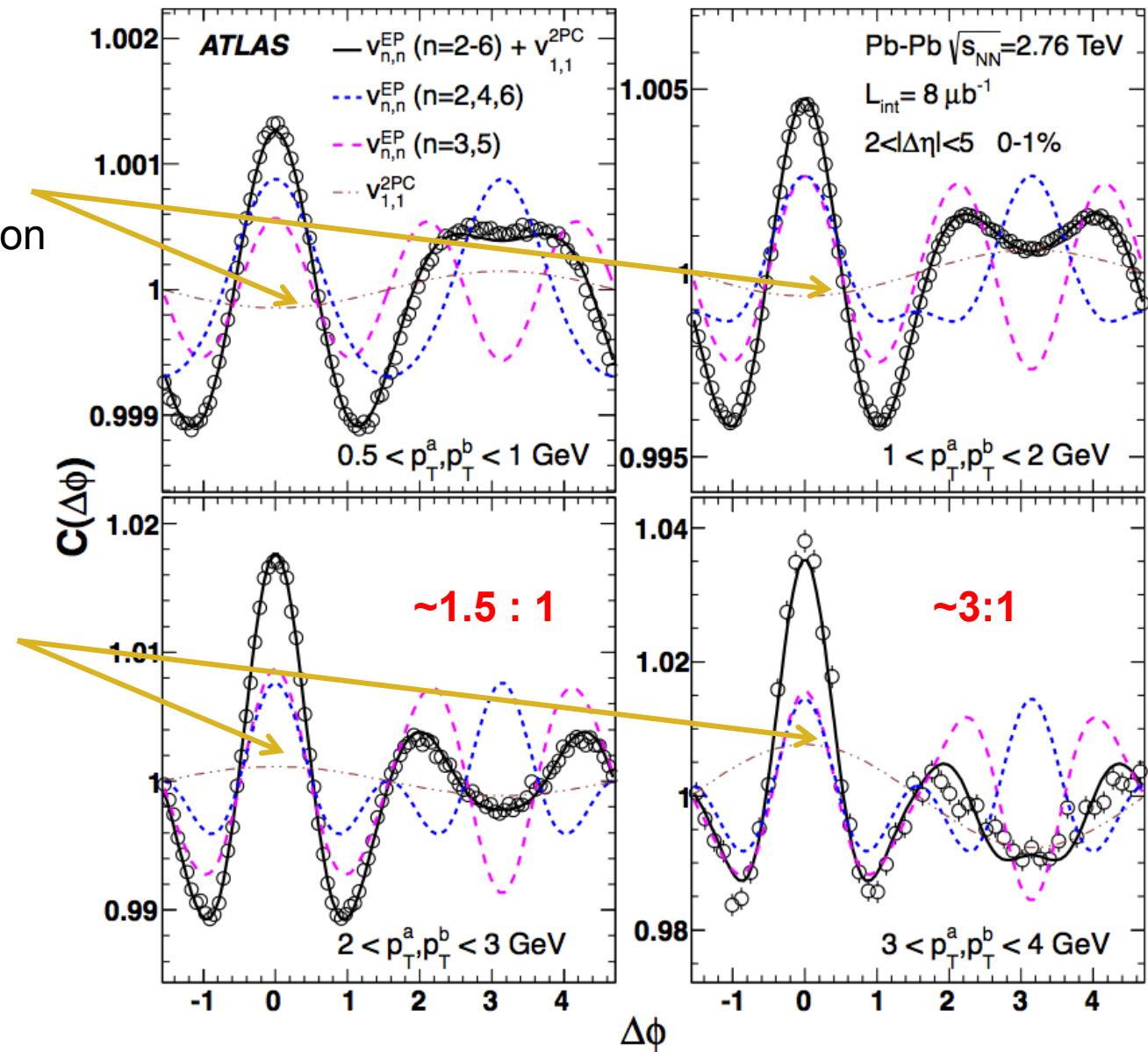
- HIJING only need momentum conservation, while AMPT need both

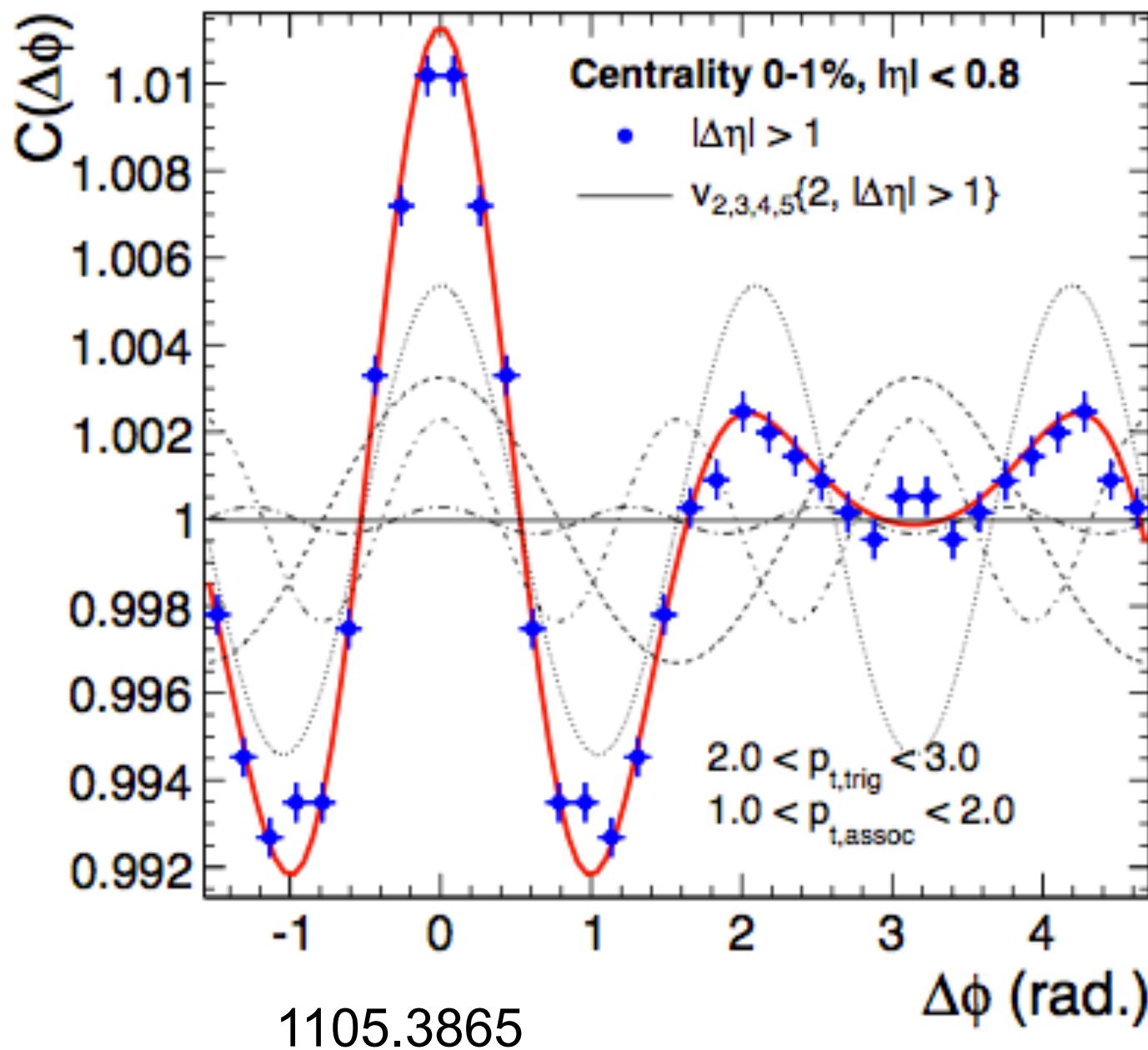
The complex  $p_T$  dependence of  $v_{1,1}$  naturally generated from final state interactions

# $v_{1,1} = \langle \cos \Delta\phi \rangle$ in 2PC (0-5%)

- Correlation function well described by  $v_2-v_6$  and  $v_{1,1}$

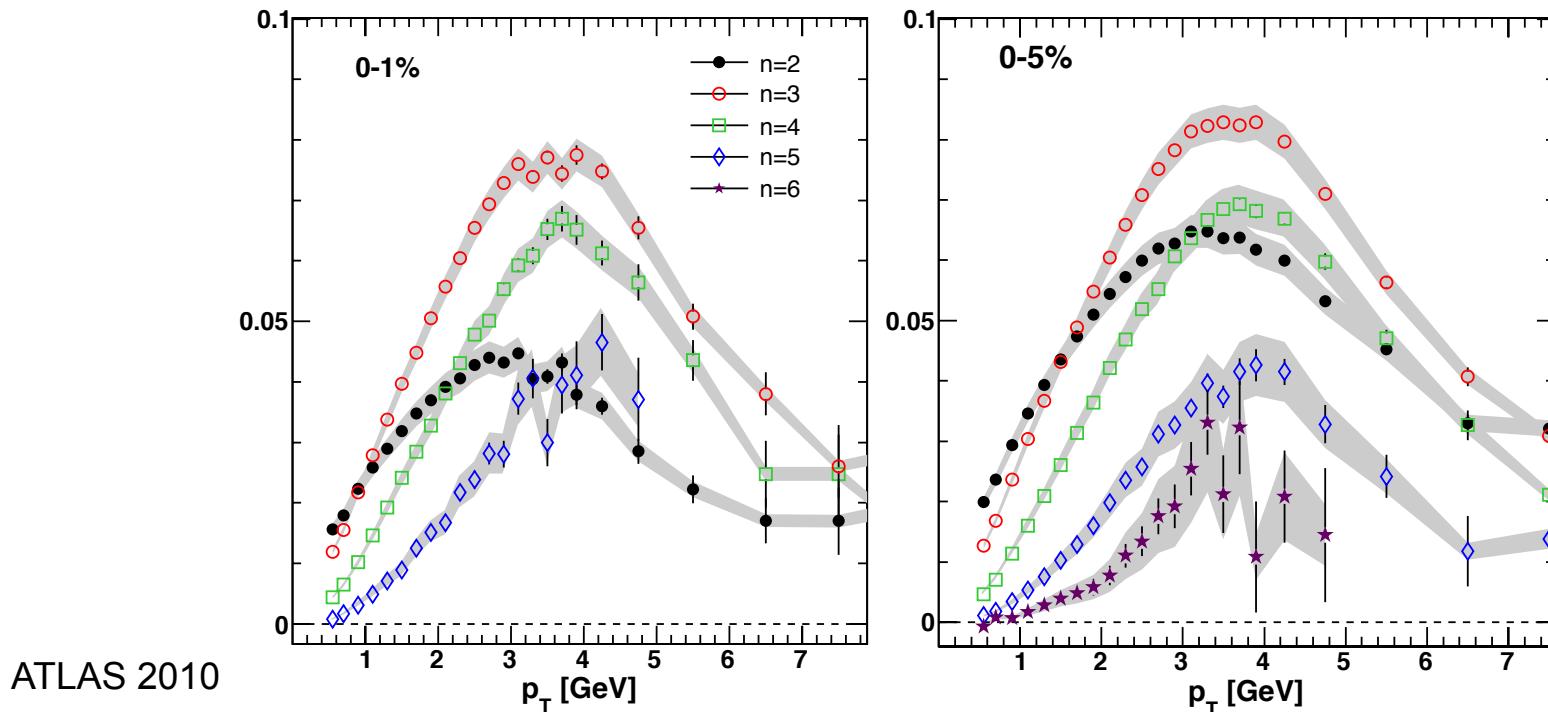
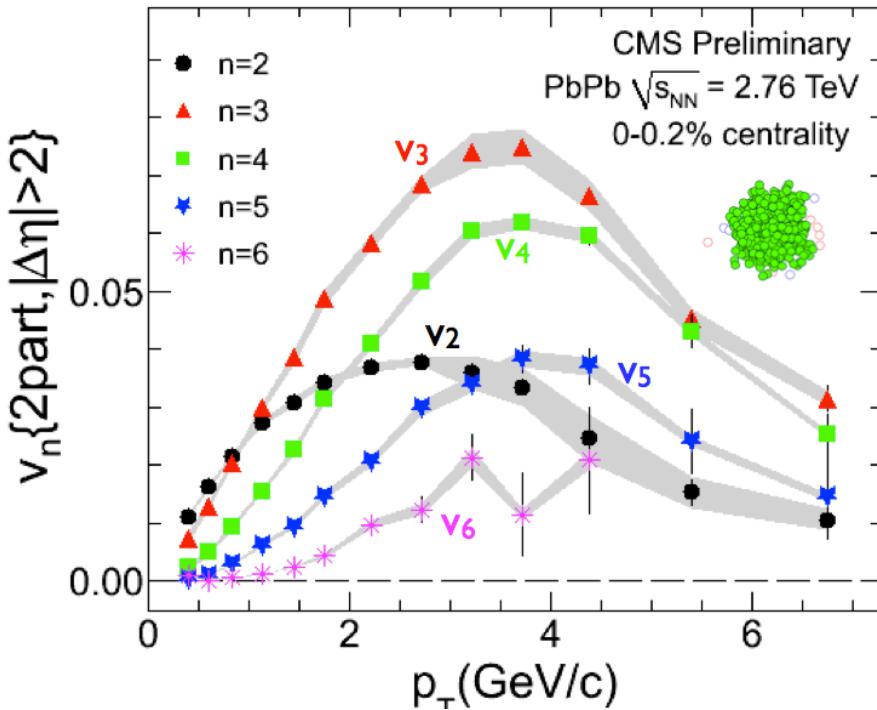
Most of  $v_{1,1}$  is due to momentum conservation



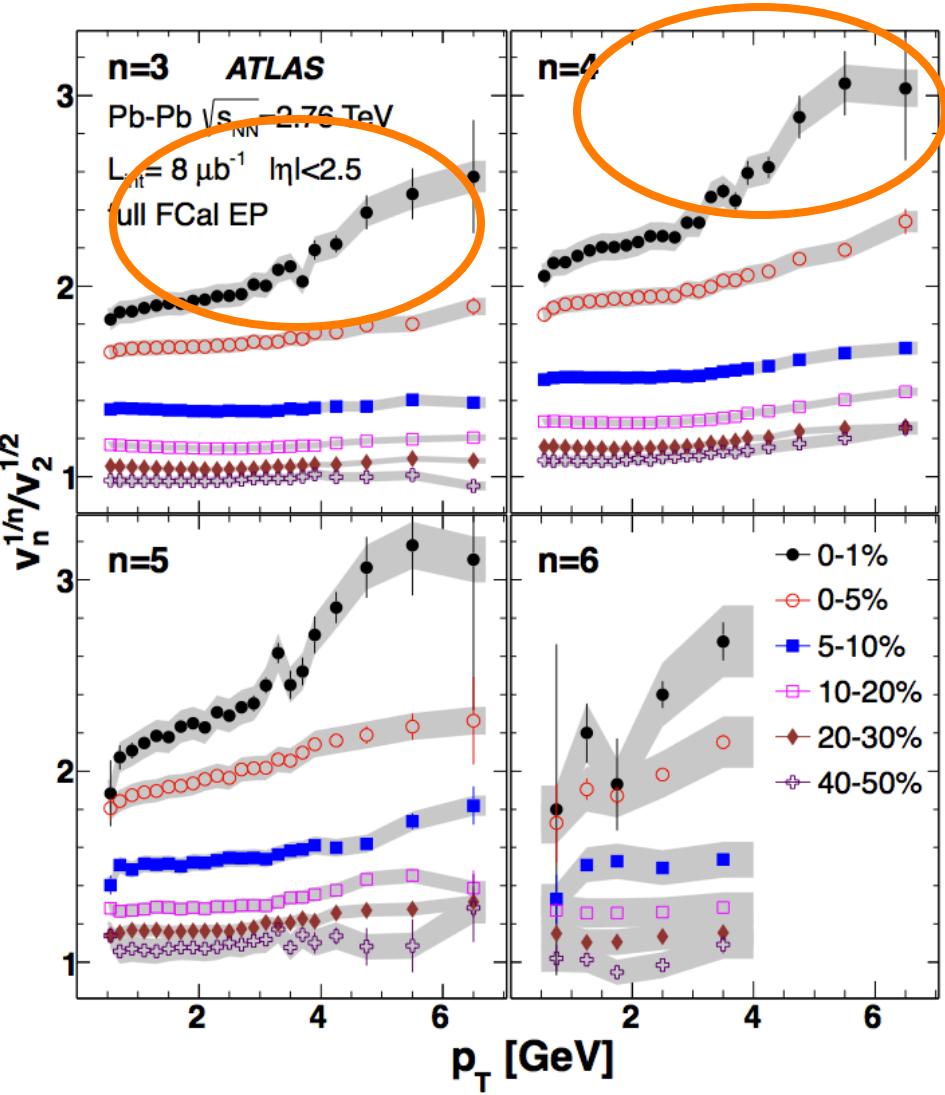
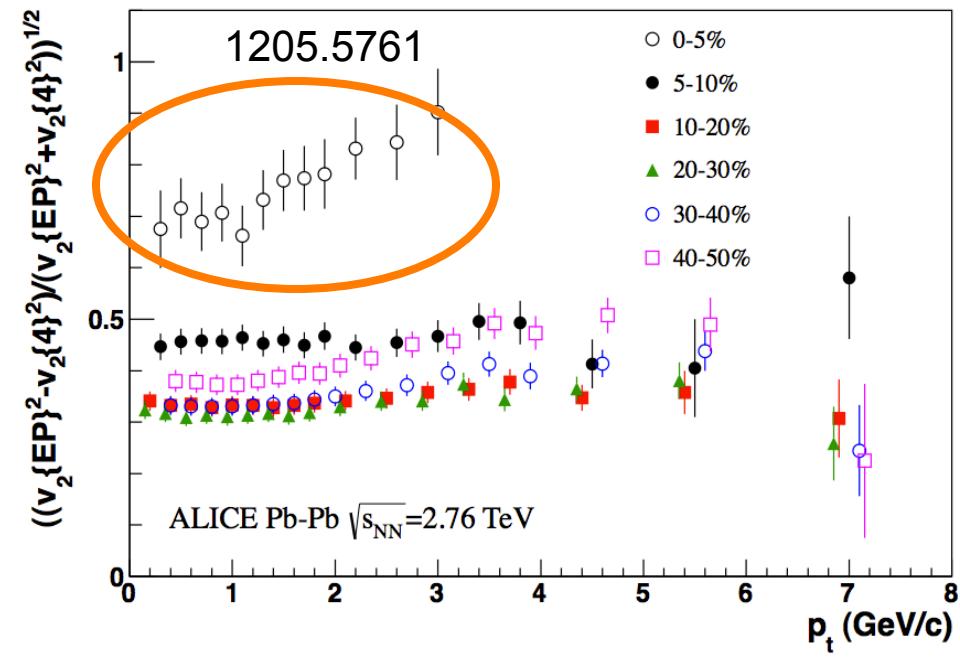


# Ultra Central Collisions

- The shape of  $v_n$  is very different from  $v_2$ .
- $p_T$  of the peak increase with  $n$ .

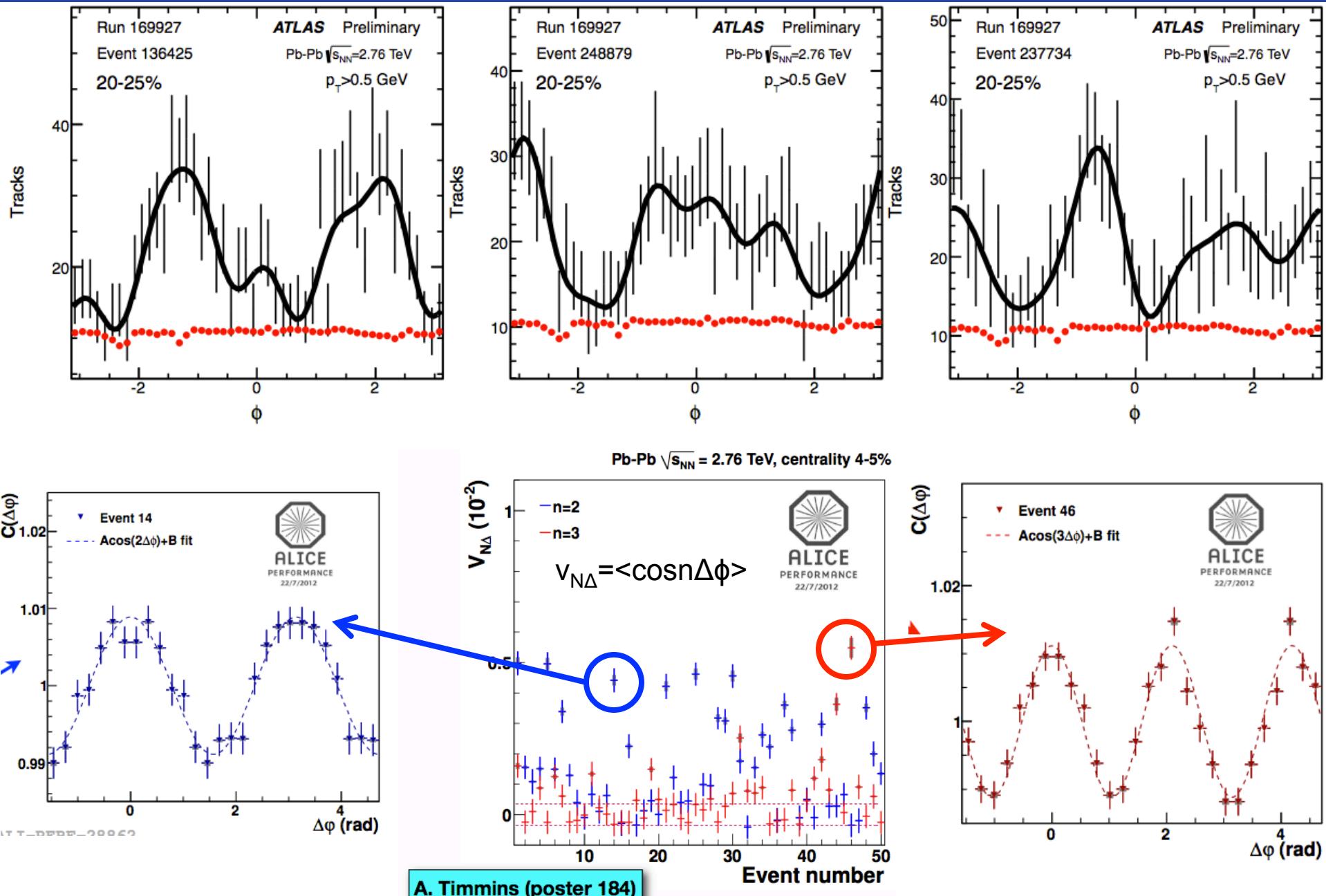


# Seen in the $v_n$ scaling and fluctuation



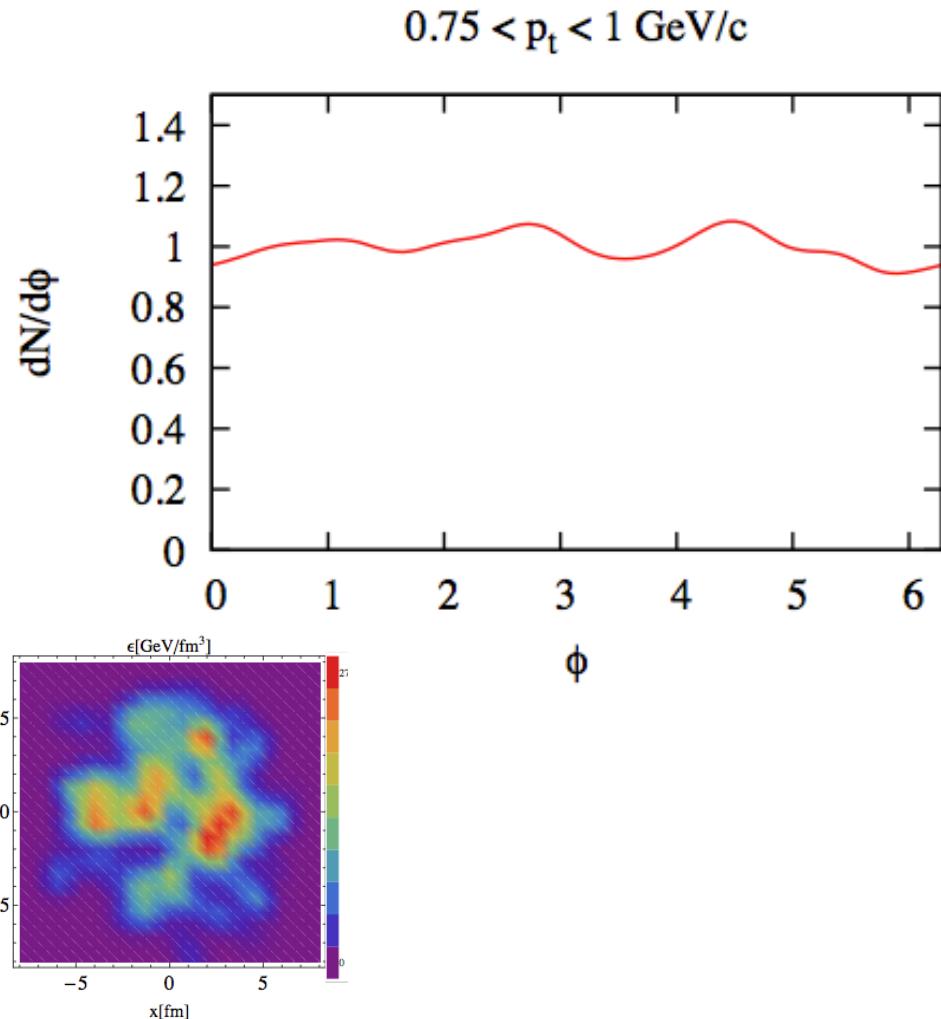
## Event-by-event quantities

# EbE $v_n$ fluctuations

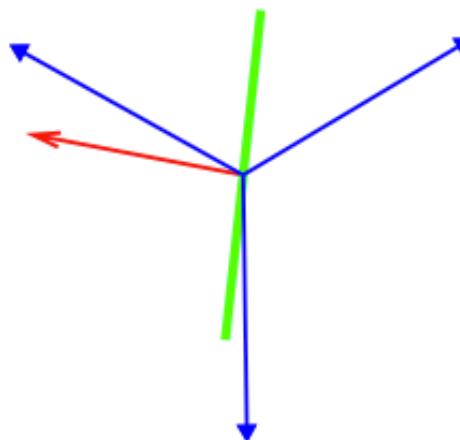


# A close look at a hydro event

Jean-Yves QM2012, central event, NeXus+Ideal hydro

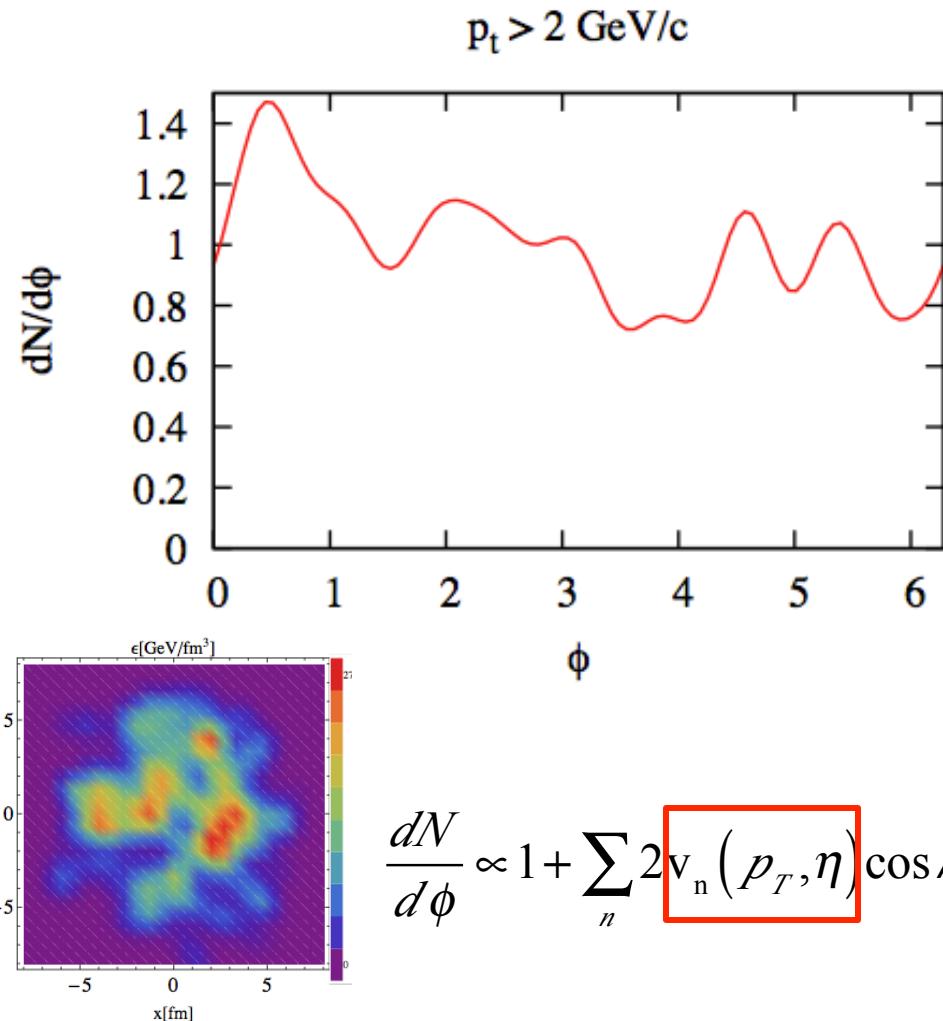


As  $p_t$  increases,  
anisotropic flow increases.  
 $\Psi_2$  and  $\Psi_3$  change mildly ,  
 $\Psi_1$  rotates more strongly



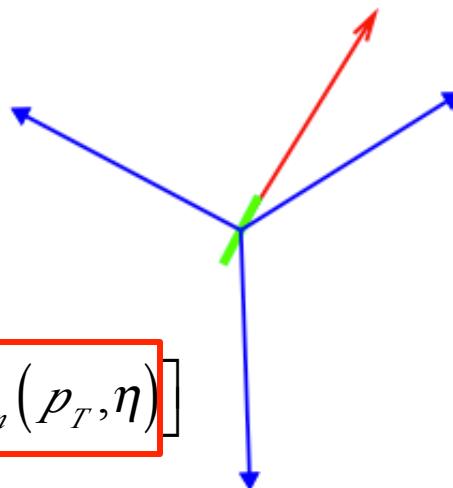
# A close look at a hydro event

Jean-Yves QM2012, central event, NeXus+Ideal hydro

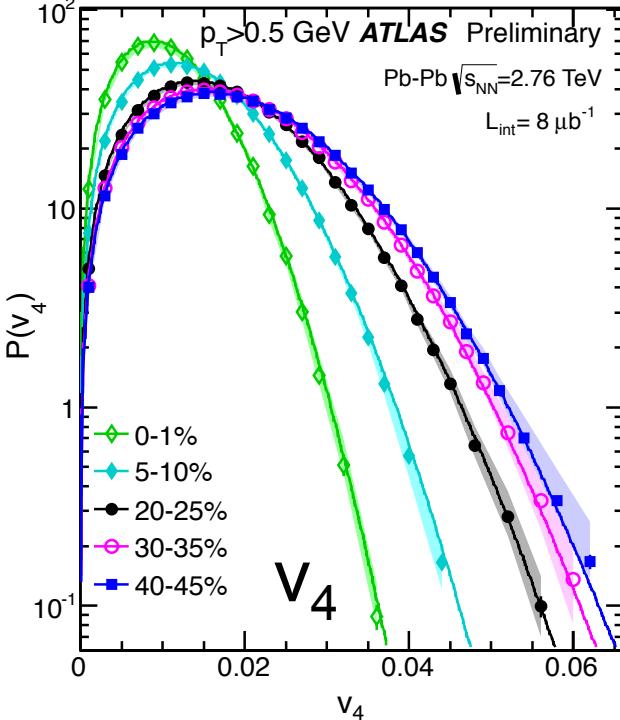
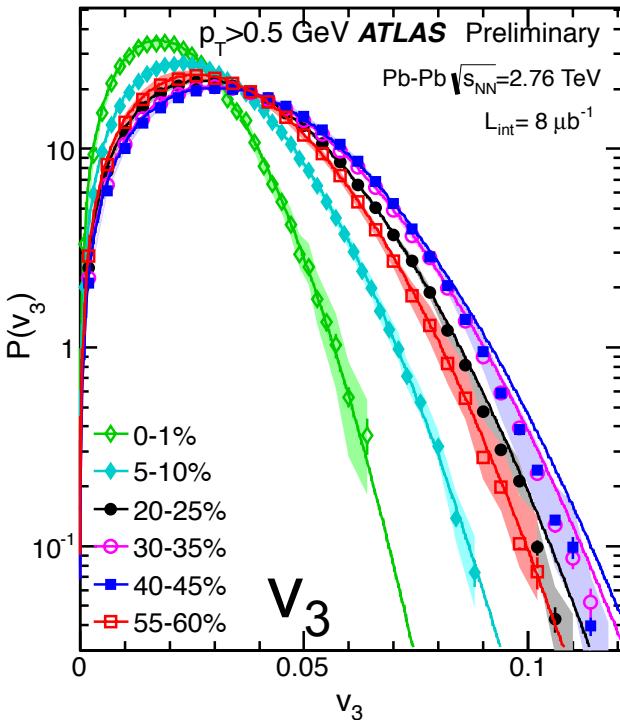
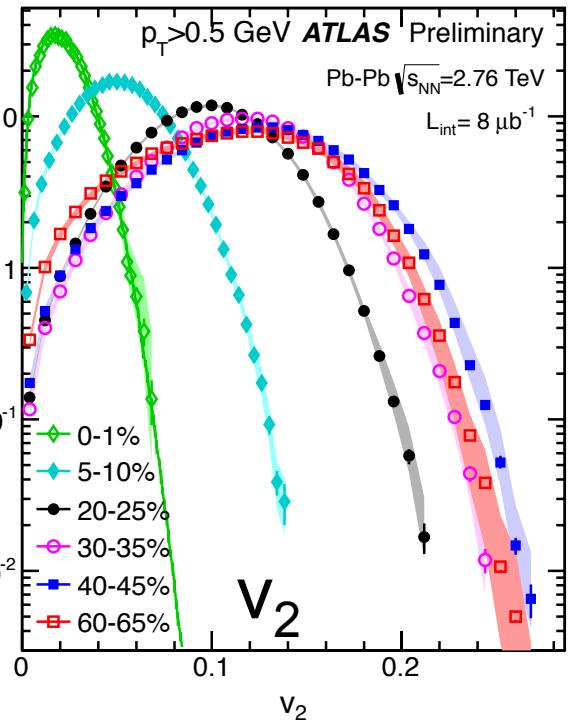


$\Psi_I$  rotates by  $\pi$  between low  $p_t$  and high  $p_t$ , because the total transverse momentum  $\int p_t v_I e^{i\Psi_I} \sim 0$ .

scale 1/4



# EbE distribution of $v_n$

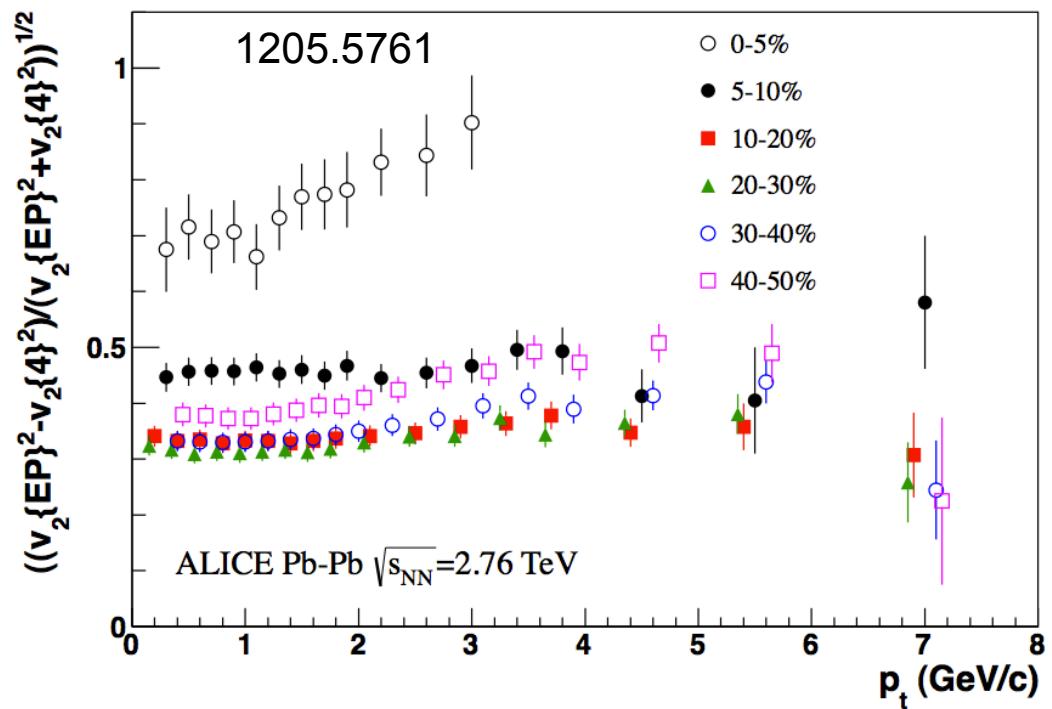
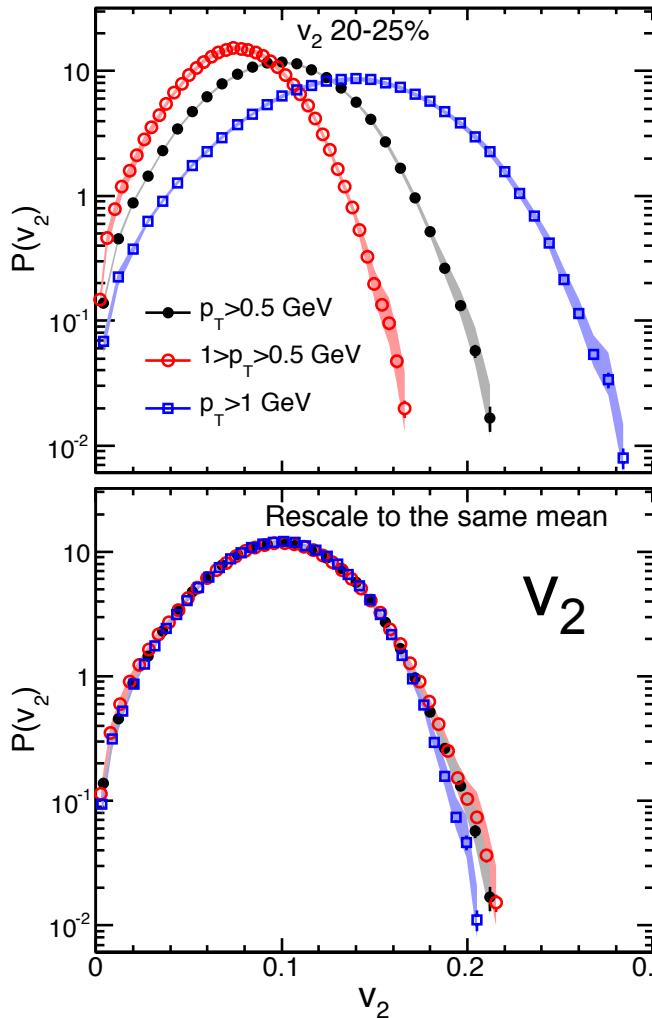


- $p(v_n)$  distributions with shape uncertainty only
- Overlaid with Gaussian function adjust to the same mean (curves)

Gaussian PDF  $P(v_n) = \frac{v_n}{\sigma^2} e^{-\frac{v_n^2}{2\sigma^2}}, \sigma = \sqrt{\frac{2}{\pi}} \langle v_n \rangle$

$$\frac{\sigma_{v_n}}{\langle v_n \rangle} = \sqrt{\frac{4}{\pi} - 1} = 0.523 \quad \sqrt{\langle v_n^2 \rangle} = \frac{2}{\sqrt{\pi}} \langle v_n \rangle = 1.13 \langle v_n \rangle$$

# $p_T$ dependence of $v_n$ shape



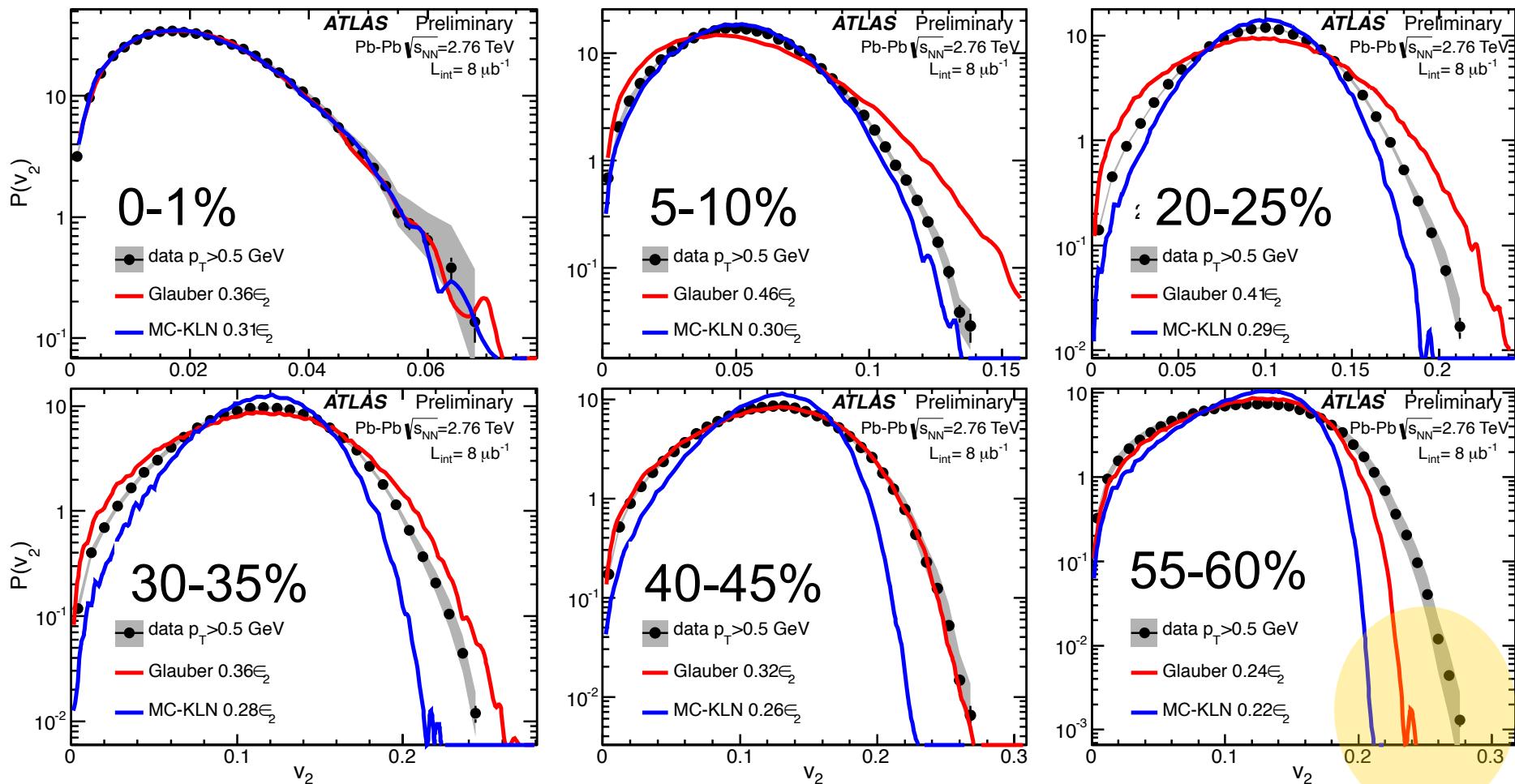
- Distributions for higher  $p_T$  bin is broader, but they all have  $\sim$ same reduced shape. Also works at higher  $p_T$ .  
 Hydrodynamic/jet-quenching response  $\sim$  geometry.

# Measuring the hydrodynamic response: $v_2$

- Check:  $v_n \propto \epsilon_n = \frac{\sqrt{\langle r^n \cos n\phi \rangle^2 + \langle r^n \sin n\phi \rangle^2}}{\langle r^n \rangle}$

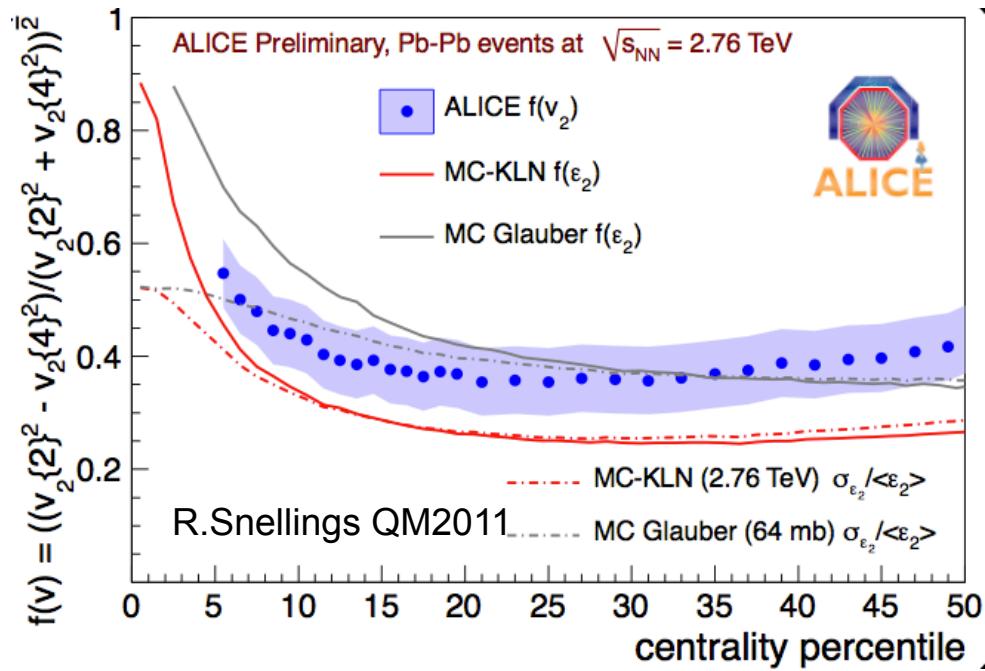
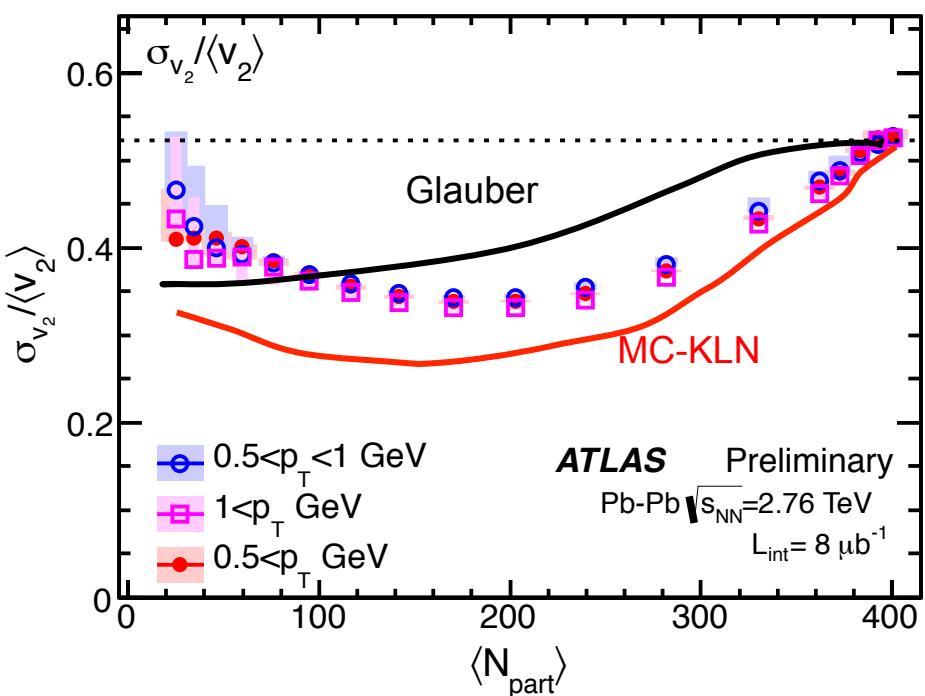
**Rescale  $\epsilon_n$  distribution to the mean of data**

For Glauber and CGC mckln 3.46



Both models fail describing  $p(v_2)$  across the full centrality range

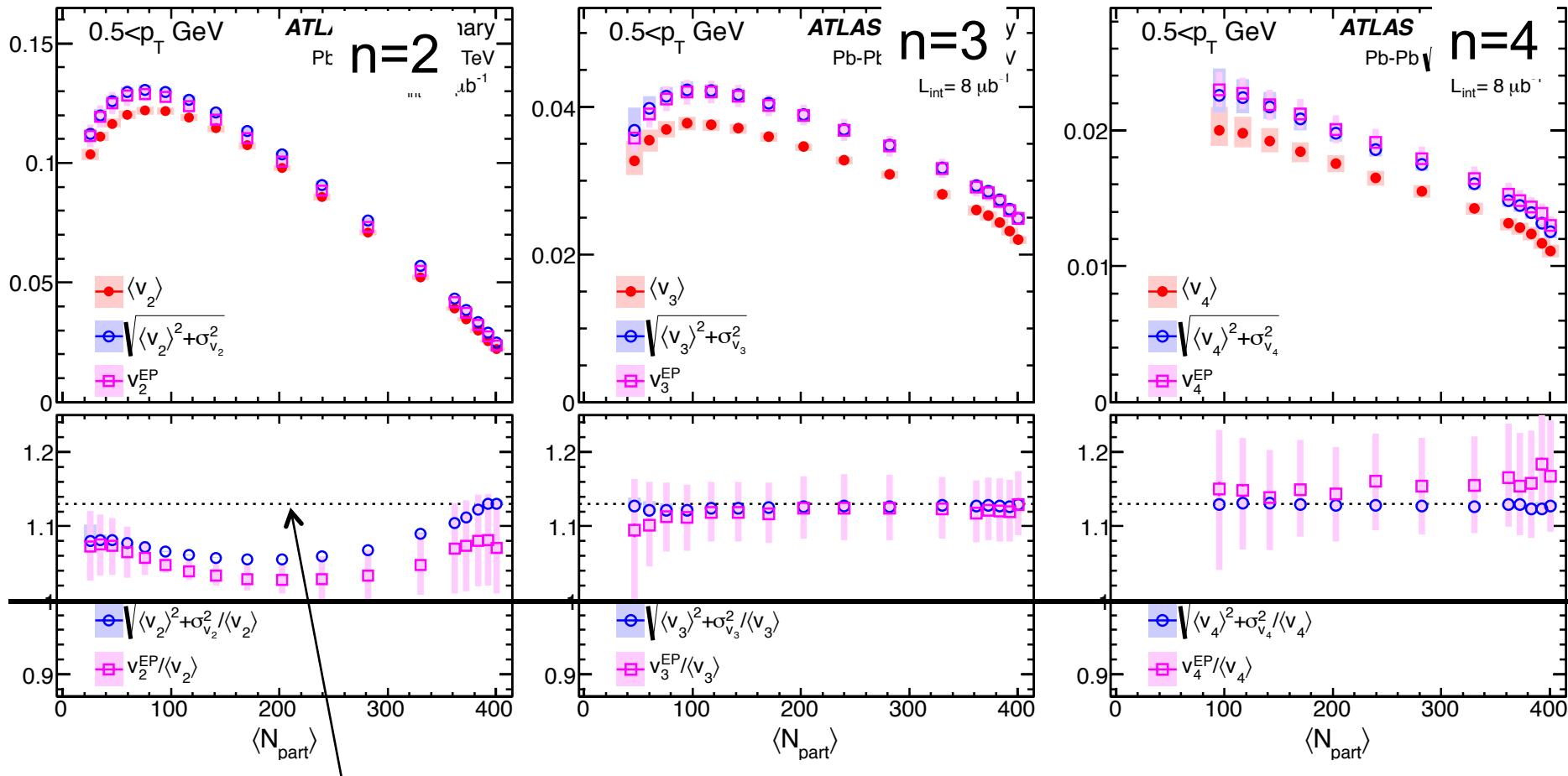
# Glauber or MC-KLN?



- MC-KLN works better in more central collisions
- Glauber better in more peripheral collisions

# Compare to $v_n^{\text{EP}}$ results

- Expectations:  $\langle v_n \rangle \leq v_n^{\text{EP}} \leq \sqrt{\langle v_n^2 \rangle} = \sqrt{\langle v_n \rangle^2 + \sigma_{v_n}^2}$ . Verified!!



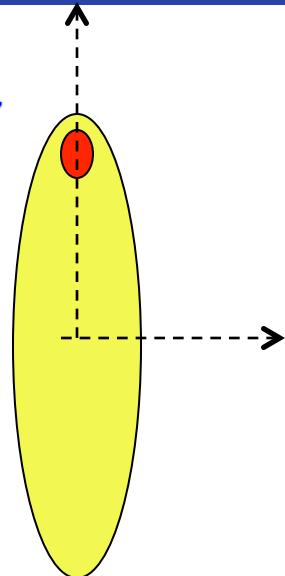
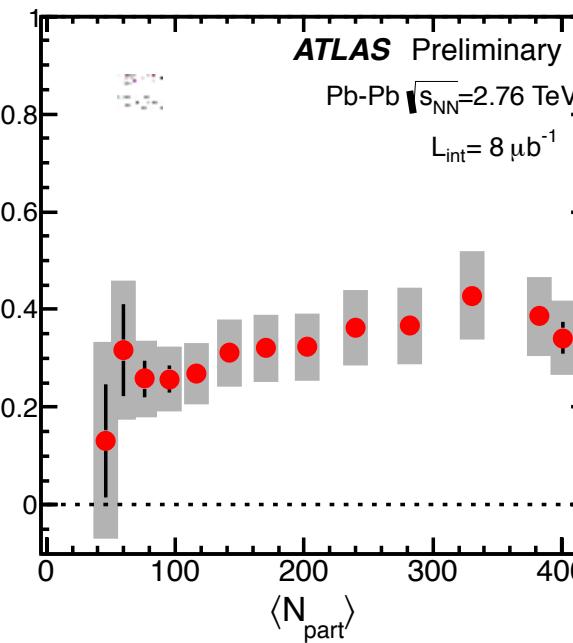
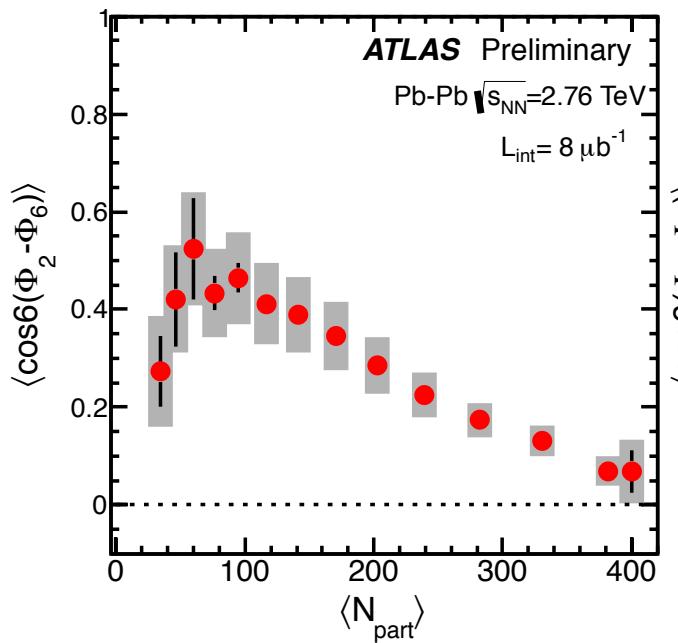
$$\sqrt{\langle v_n^2 \rangle} = \frac{2}{\sqrt{\pi}} \langle v_n \rangle = 1.13 \langle v_n \rangle$$

# Correlations between $\Phi_n$ , $\Phi_m$ etc

Initial correlations  
 Initial state(cumulants) + Flow response = Reaction place correlations  
 Linear & Non-linear Final state

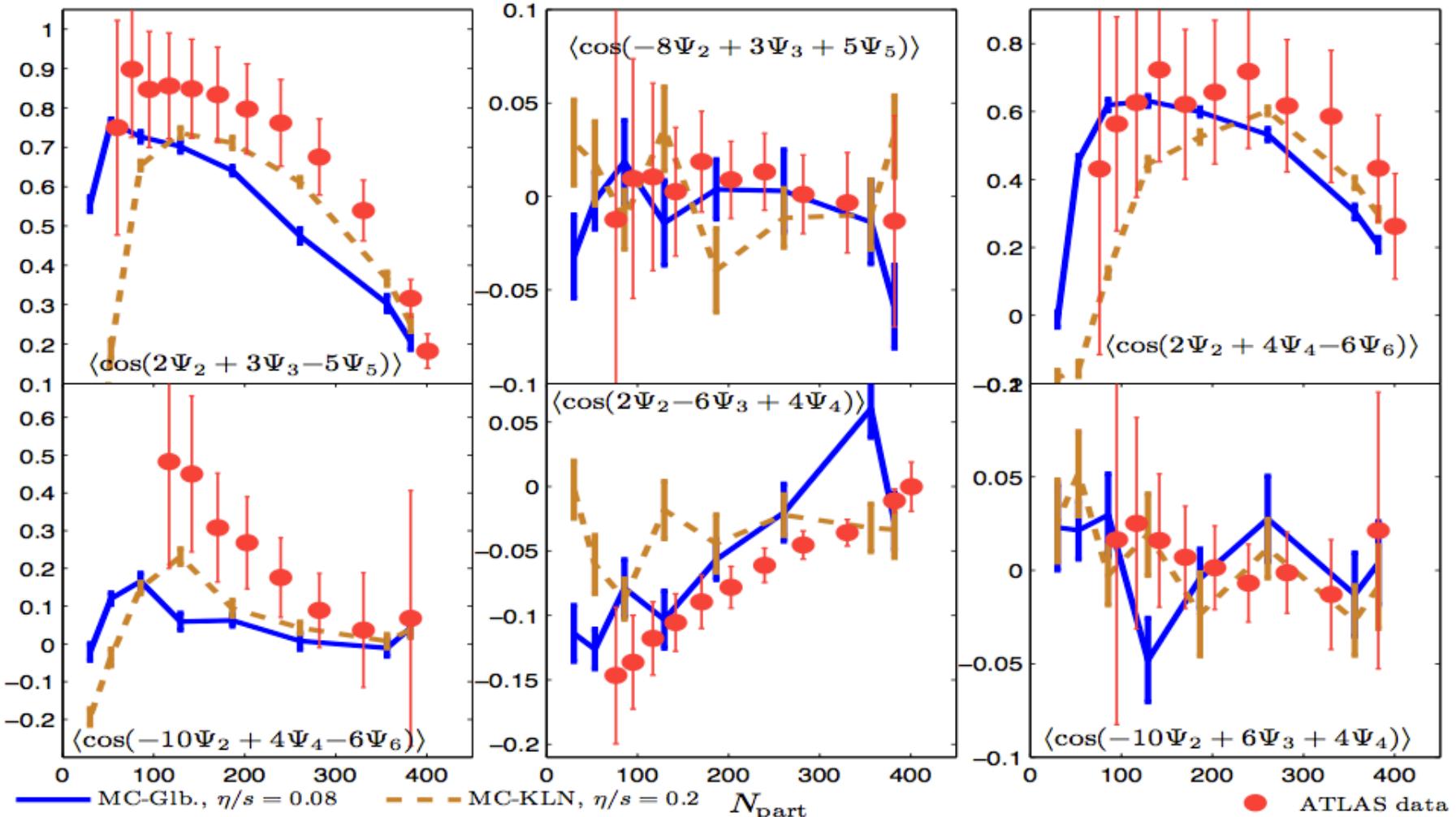
$$\frac{dN_{\text{evts}}}{d(k(\Phi_n - \Phi_m))} \propto 1 + 2 \sum_{j=1}^{\infty} V_{n,m}^j \cos jk(\Phi_n - \Phi_m)$$

$$V_{n,m}^j = \langle \cos jk(\Phi_n - \Phi_m) \rangle$$



$$\nu_6 e^{-i6\Psi_6} = \text{geometry} + \nu_2 \nu_2 \nu_2 e^{-i6\Psi_2} + \nu_3 \nu_3 e^{-i6\Psi_3} + \nu_2 \nu_4 e^{-i2\Psi_2 - i4\Psi_4} + \dots$$

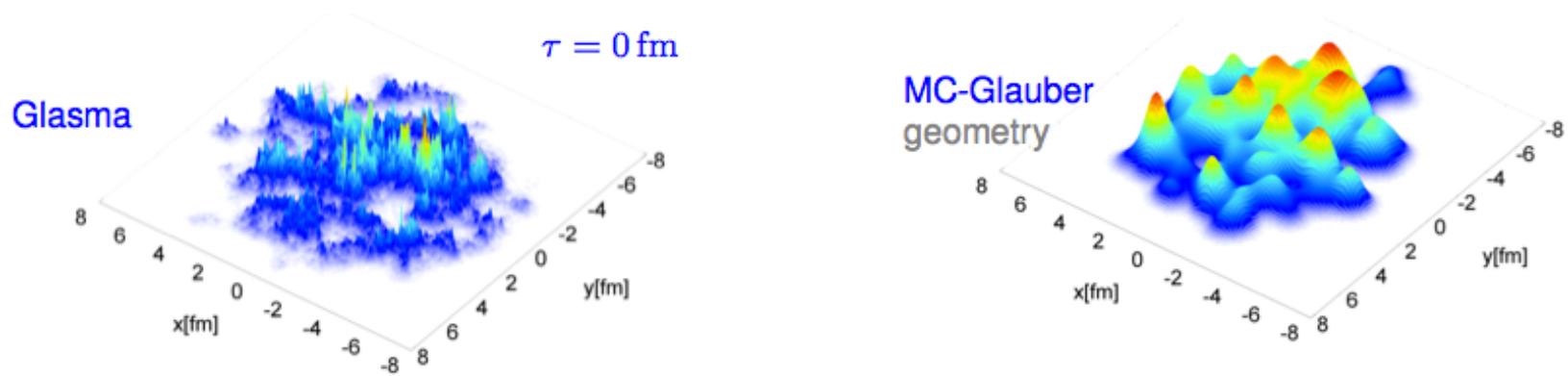
# Correlations between three EP



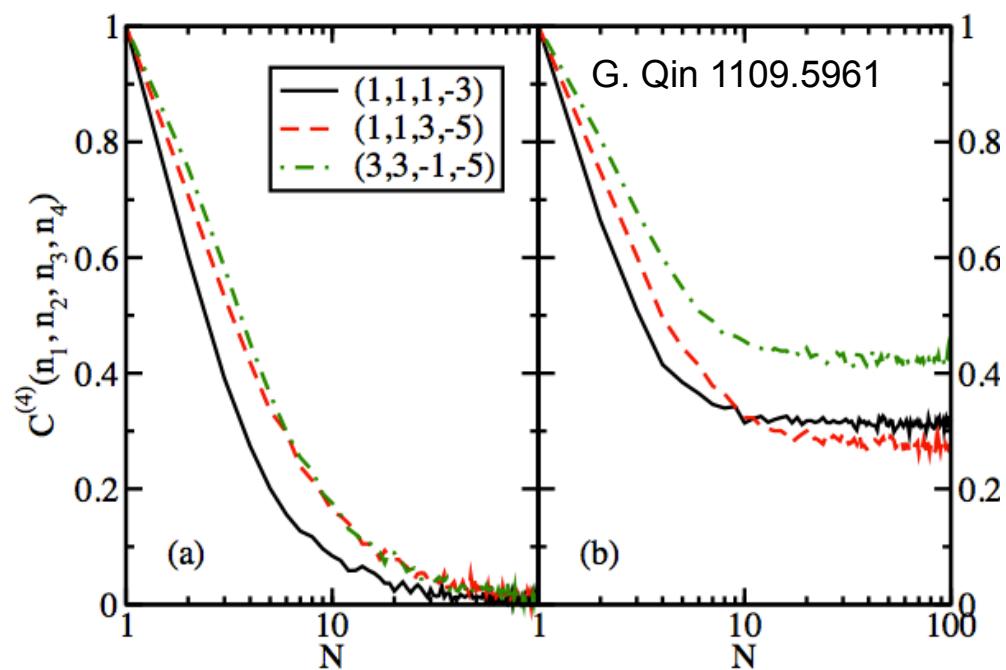
- Dynamic mixing in hydrodynamics Not only  $v_n$ , but also  $v_{n,m}$ ,  $v_{n,m,k}$  etc

$$v_5 e^{-i5\Psi_5} = \text{geometry} + v_2 v_3 e^{-i2\Psi_2 - i3\Psi_3} + \dots$$

# How to measure number/size of the hot spots? <sup>24</sup>



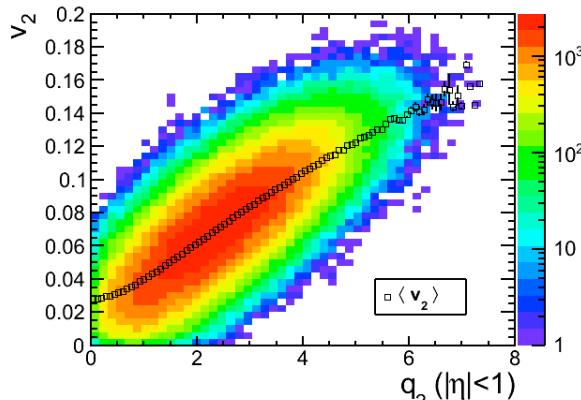
Not so easy due to  
non-linear effects



# EVENT SHAPE ENGINEERING

Talk of S.Voloshin: Plenary IC

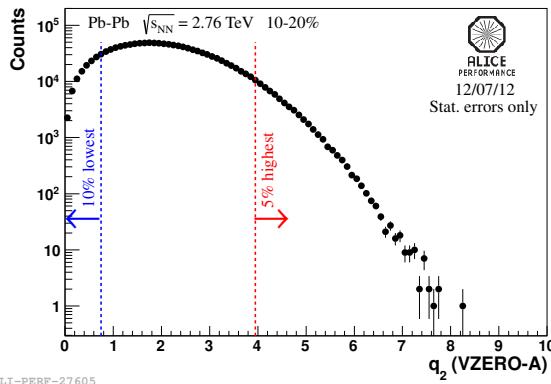
- Selection of azimuthally anisotropic events: length of flow vector,  $q_2$



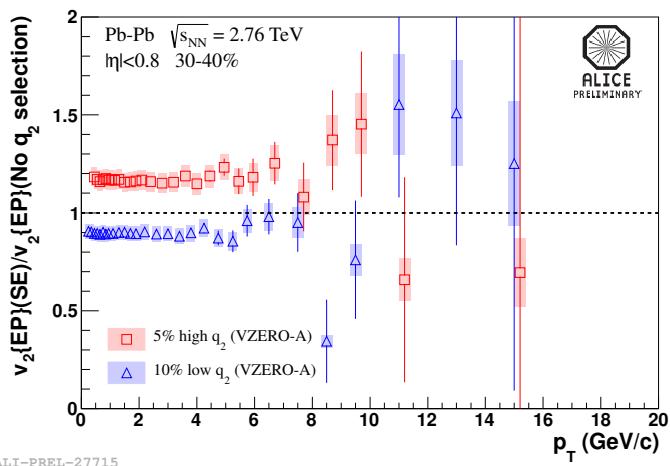
$$Q_{n,X} = \sum_{i=1}^M \cos(n\phi_i)$$

$$Q_{n,Y} = \sum_{i=1}^M \sin(n\phi_i)$$

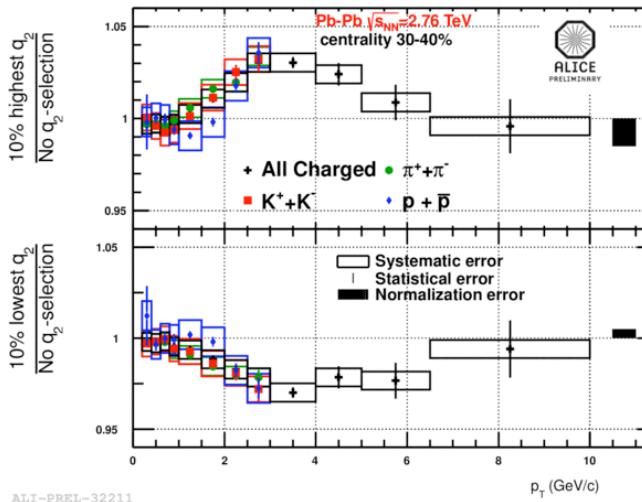
$$q_n = Q_n / \sqrt{M}$$



Talk of A.Dobrin: 1C



ALI-PREL-27715



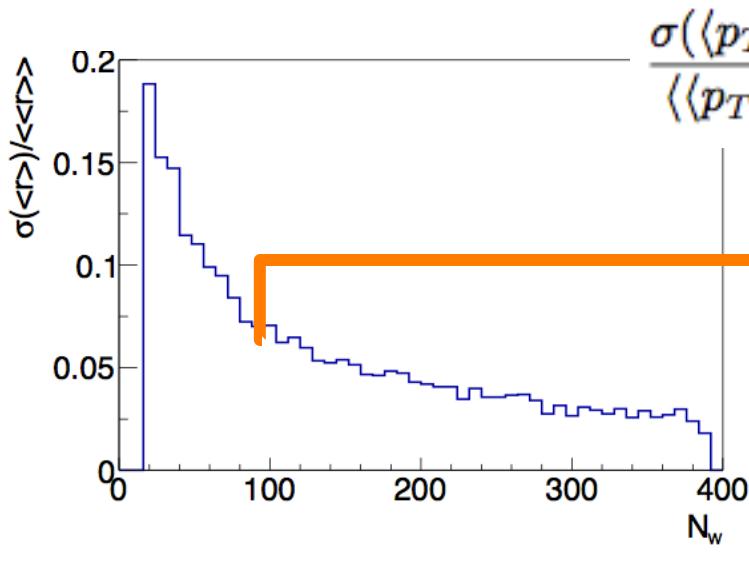
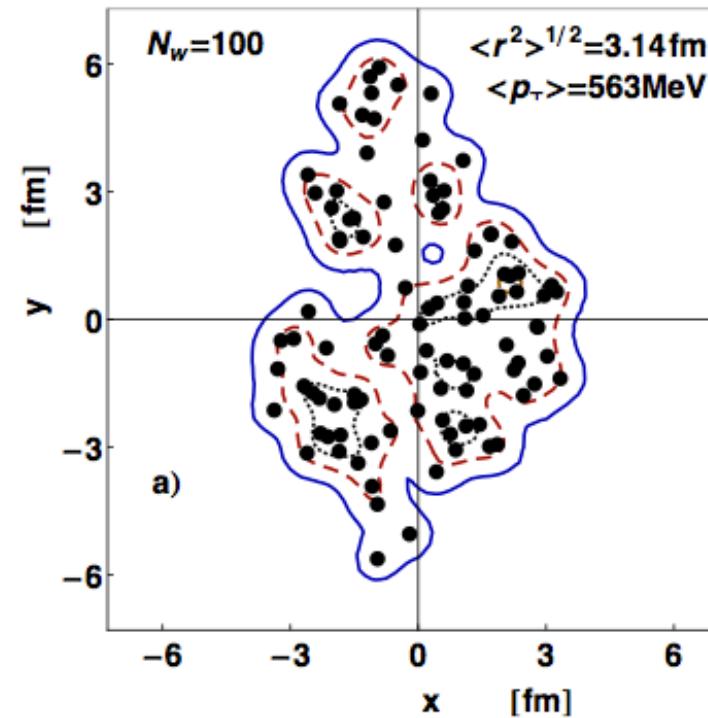
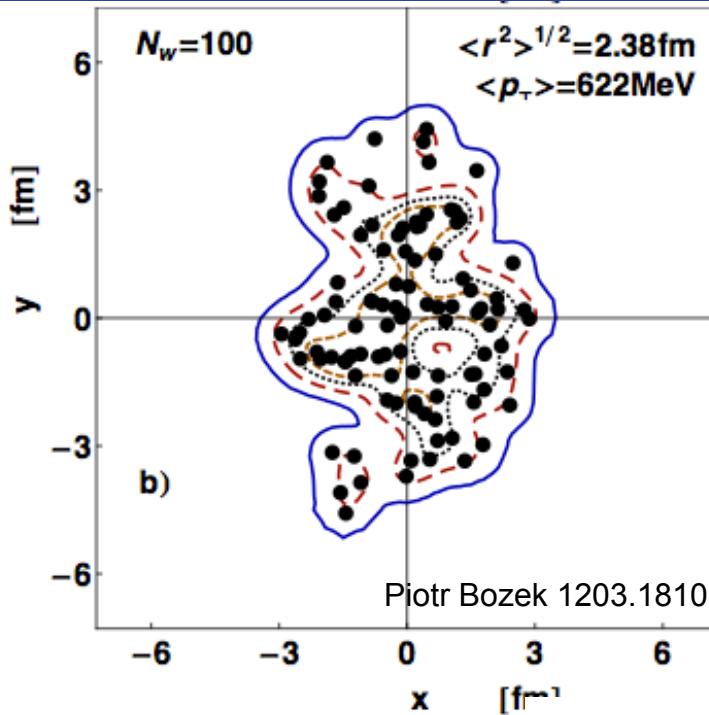
Talk of L.Milano: 5A

expected effect on  $v_2$  and consequence on PID'ed transverse momentum spectra

Largely expected since  $v_2 \sim \varepsilon_2$ .

More useful as a tool for jet tomography?

# Transverse size fluctuation



$$\frac{\sigma(\langle p_T \rangle)}{\langle \langle p_T \rangle \rangle} \simeq 0.3 \frac{\sigma(\langle r \rangle)}{\langle \langle r \rangle \rangle}$$

