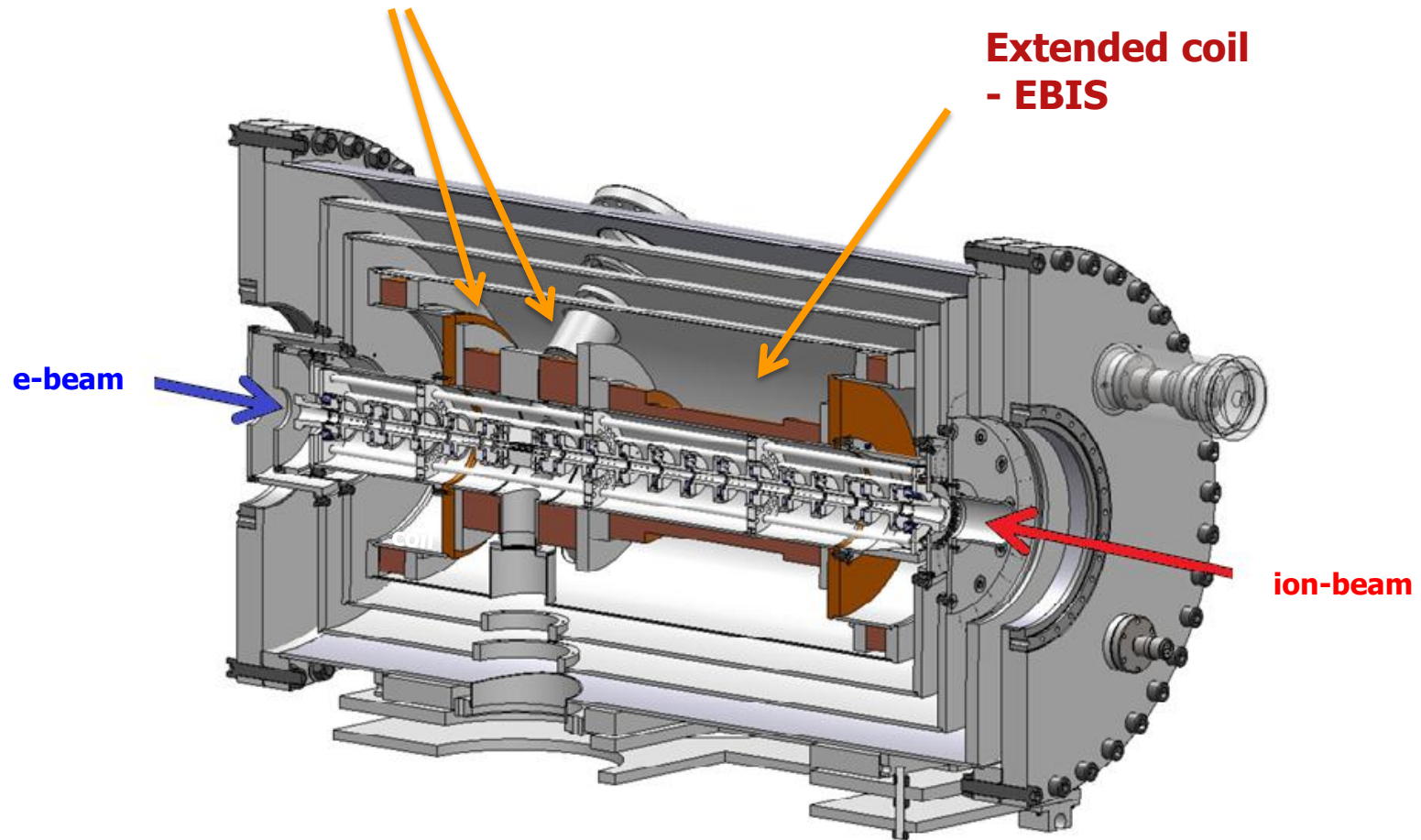
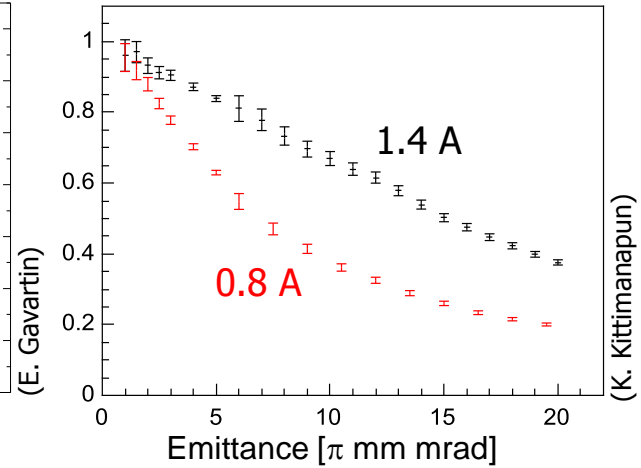
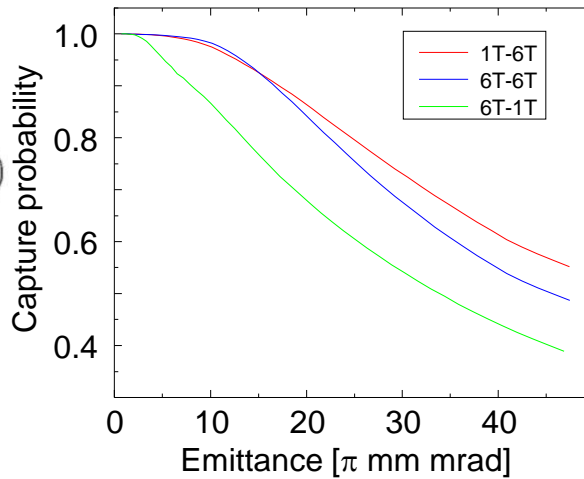
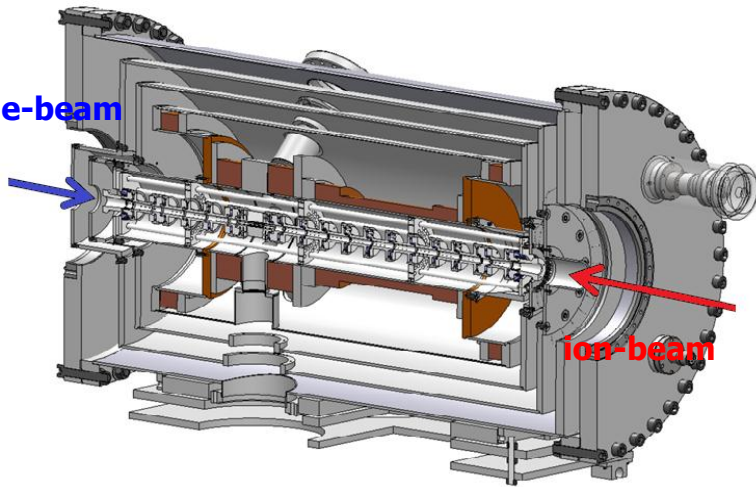


# The Helmholtz + solenoid magnet configuration for the NSCL EBIS/T

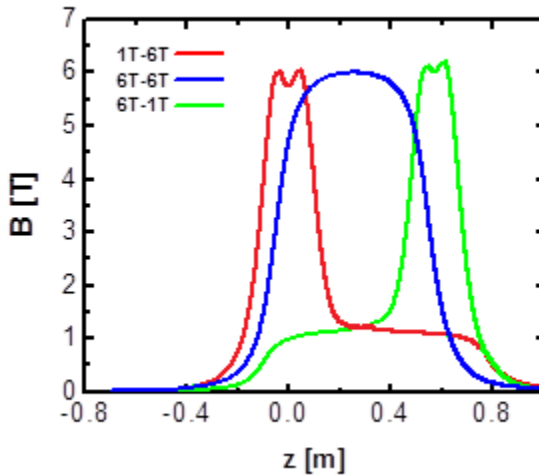
**Split-coil /  
~ Helmholtz configuration  
- EBIT**

**Extended coil  
- EBIS**

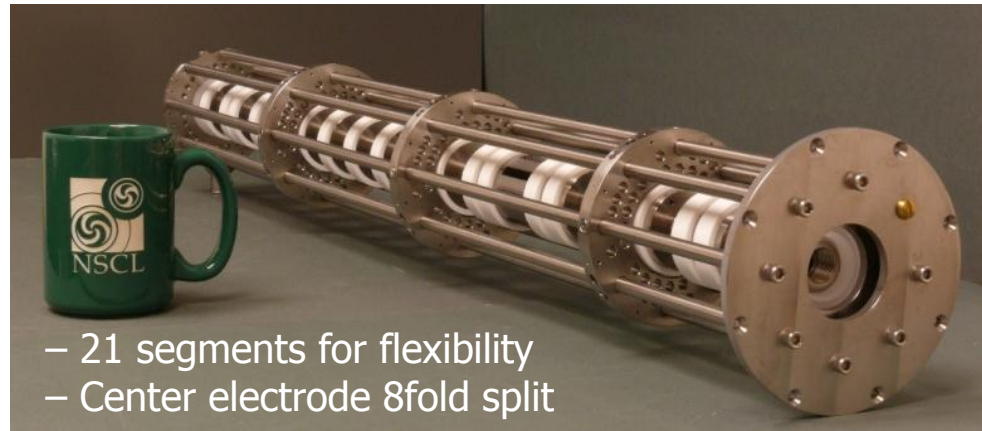




Moderate compression + large e-beam current  
 + longer trap needed = good acceptance  
 → **Two traps for high acceptance and fast breeding**



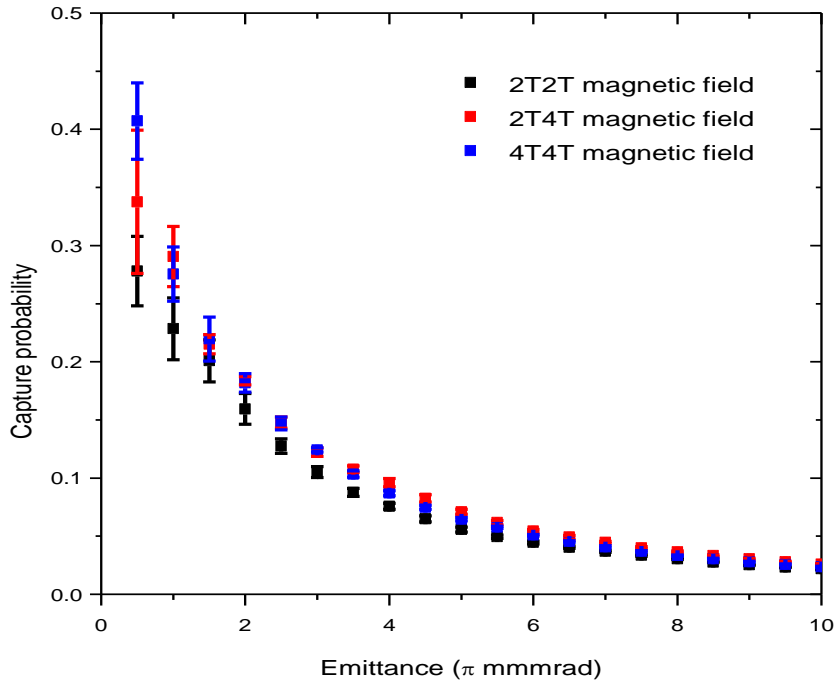
**Trap: ~ 0.8m long**



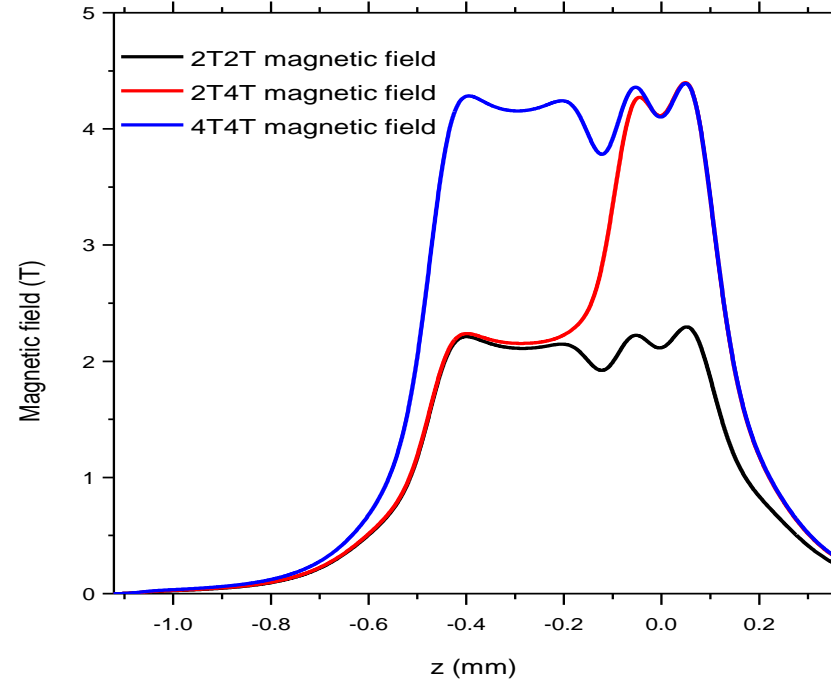
- 21 segments for flexibility
- Center electrode 8fold split

## Ion trajectory calculations with MC-style ionization – low beam current

Capture probability vs. beam emittance



Axial field distribution



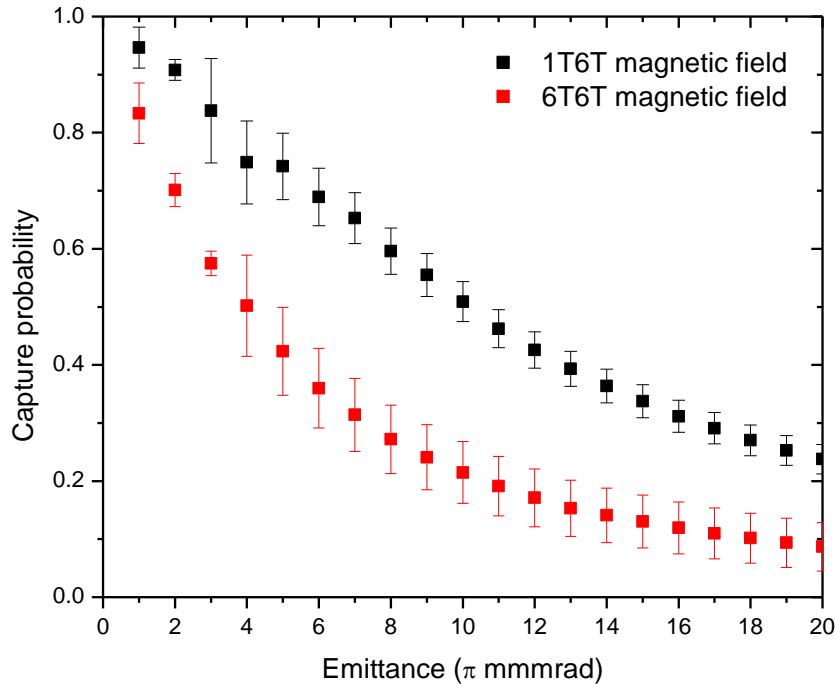
(K. Kittimanapun)

- Ion beam K-39
- Extraction energy 29.306 keV
- Trap length 0.75 m
- Electron beam current 0.1 A
- Electron beam energy 19.545 keV

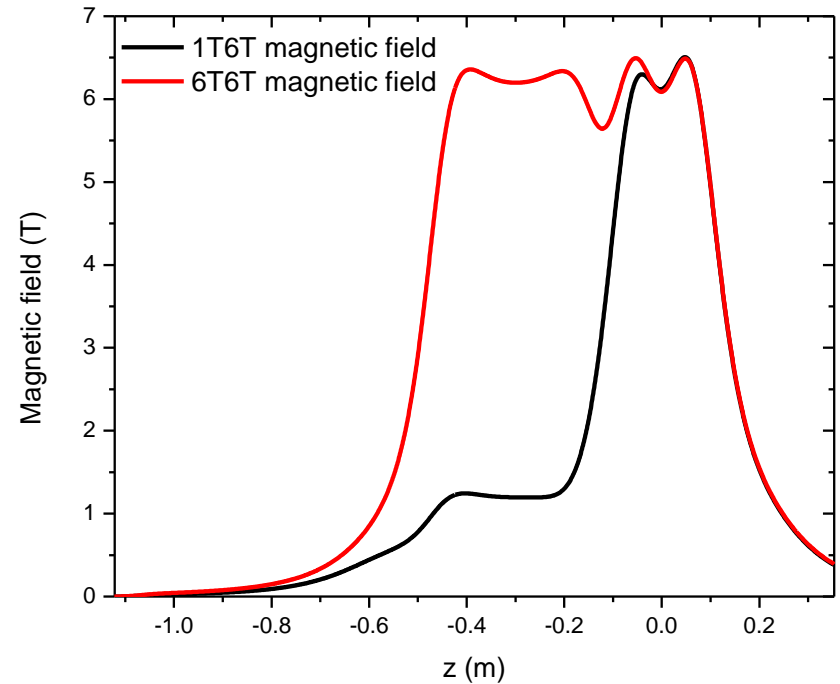
→ At low beam current: Not so much

## Ion trajectory calculations with MC-style ionization – **high beam current**

Capture probability vs. beam emittance



Axial field distribution



(K. Kittimanapun)

- Ion beam  $^{56}\text{Fe}$
- Extraction energy 60 keV
- Trap length 0.75 m
- **Electron beam current 1 A**
- Electron beam energy 12.5 keV
- Electron beam current density
  - $1.6 \times 10^3 \text{ A/cm}^2$  at 1T region
  - $1.2 \times 10^4 \text{ A/cm}^2$  at 6T region

→ **At high beam current: Yes**

**Try something less time-consuming instead:**

**1: Use: 'Geometrical acceptance'** ( see F. Wenander, CERN report)  
**= maximum emittance of ion beam caught inside e-beam**

$$\alpha_{\max} = \pi \frac{r_{ebeam}}{\sqrt{2U_{ext}}} \cdot \left( Br_{ebeam} \sqrt{\frac{q}{m}} + \sqrt{\frac{qB^2 r_{ebeam}^2}{4m} + \frac{\rho_l}{2\pi\epsilon_0}} \right)$$

= f( e-radius  $r_{ebeam}$ , acceleration voltage  $U_{ext}$ , magnetic field strength  $B$ , longitudinal SC density  $\rho_l$ )

**With Herrmann-formula for e-beam radius**

$$r_h = r_b \sqrt{\frac{1}{2} + \frac{1}{2} \sqrt{1 + 4 \left( \frac{8kT_c r_c^2 m}{e^2 r_b^4 B^2} + \frac{B_c^2 r_c^4}{B^2 r_b^4} \right)}}$$

→ **Partial efficiency given by  $\epsilon_{beam}$  in relation to  $\alpha_{\max}$**

**2: Calculate  $t_{12}$  from  $1^+ \rightarrow 2^+$  x-section. E.g. use  $f(E) \sim E^{-0.75}$**

→ **Partial efficiency given by time-in-trap compared to  $t_{12}$ :  $\sim 1 - \exp(-t_{trap} / t_{12})$**

**→ Easy analytical estimate for capture probability of DC beam!**

**Depends on :**

- **ion beam emittance, trap magnetic field, e-current, trap length**
- E-energy, mean ion energy in trap, ion extraction energy,
- e-gun parameters:  $B_c$ ,  $T_c$ ,  $r_c$

→ **Even Excel can do it!**

# F. Wenander's emittance formula → acceptance

Capture probability = f(trap length, electron energy, B-field, emittance)  
using F. Wenander's formula + Lotz' X-section

cathode radius	rc	mm	3.18
e-energy	Ee	keV	20
mean energy in trap	Eion	eV	100
Ionization x-section	$\sigma_{1 \rightarrow 2}$	A <sup>2</sup>	0.03340
mean velocity in trap	$\langle v_t \rangle$	m/s	22232.5

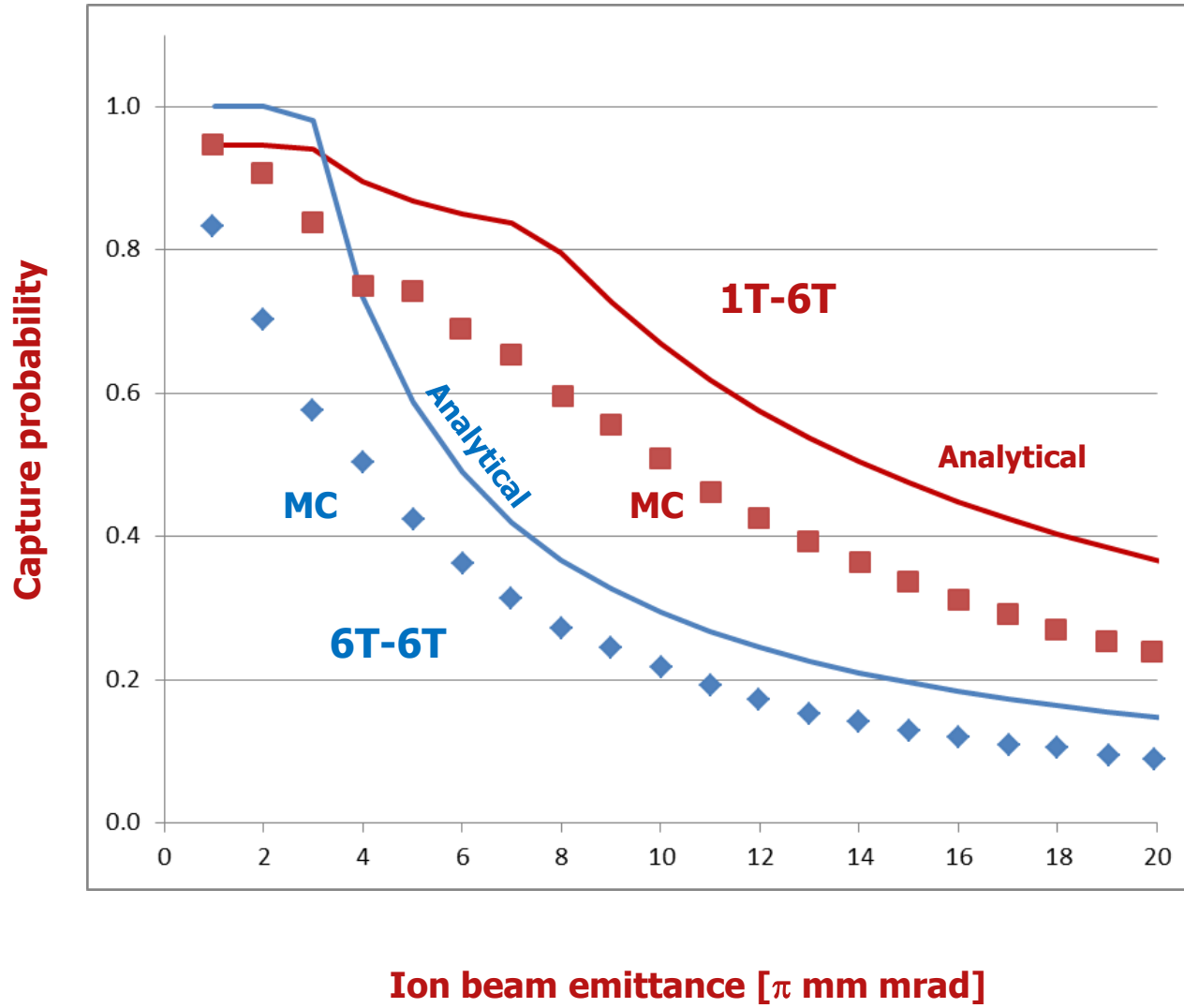
Color code:

affected by acceptance
affected by time in trap / j
affected by both
>99%

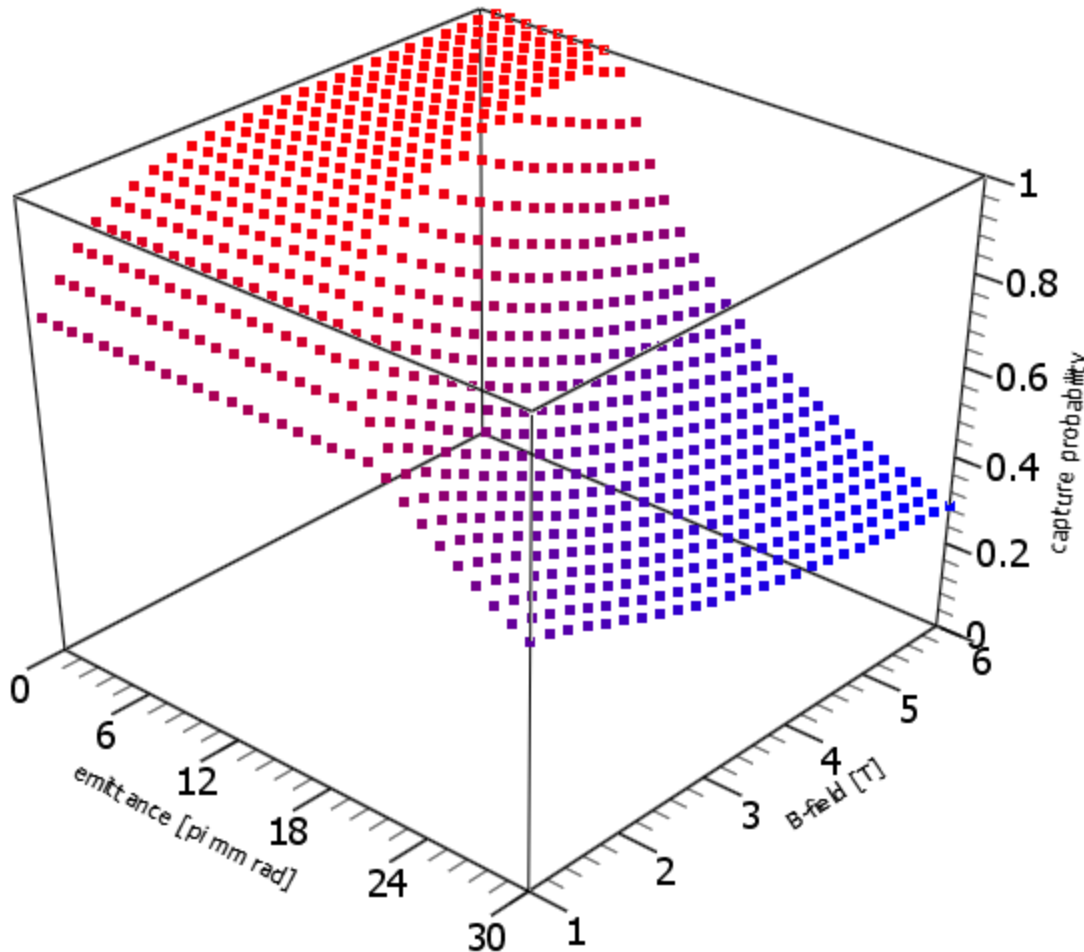
## Capture probability [%]

↓ current / trap length →

	dz [m]	π mm mrad			
	<b>0.16</b>				
I [A]	<b>0.1</b>				
	↓ ε/B →	1	2	4	6
	3	2.2	4.3	6.2	7.6
	10	0.9	1.3	1.9	2.3
	30	0.3	0.4	0.6	0.8
	50	0.2	0.3	0.4	0.5
	<b>0.4</b>				
I [A]	<b>1.5</b>				
	↓ ε/B →	1	2	4	6
	3	24.7	46.3	72.7	86.2
	10	24.7	46.3	57.4	55.5
	30	13.8	17.5	19.1	18.5
	50	8.3	10.5	11.5	11.1
	<b>1.2</b>				
I [A]	<b>2.4</b>				
	↓ ε/B →	1	2	4	6
	3	33.6	61.0	86.8	95.5
	10	33.6	61.0	86.8	78.0
	30	24.9	29.9	29.1	26.0
	50	14.9	17.9	17.5	15.6
	<b>5</b>				
I [A]	<b>5</b>				
	↓ ε/B →	1	2	4	6
	3	47.4	81.5	98.0	99.8
	10	47.4	81.5	98.0	99.8
	30	47.4	61.8	49.1	39.9
	50	34.9	37.1	29.4	24.0



Again:  
 At low emittance:  
 B does not matter so much,  
 if you have sufficient I !!



$^{56}\text{Fe}$  , mass 56 u  
 e current [A] 2.5  
 trap length [m] 1

e energy [keV]: 15  
 mean ion E in trap [eV]: 300  
 ion extraction E [keV]: 60  
 Bc [G]: 20  
 Tc [T]: 1000  
 rc [mm]: 6.3