Update on resummation for γ , W- and Z-boson production at large p_T



FOR FUNDAMENTAL PHYSICS

Xavier Garcia i Tormo



Introduction: $W/Z/\gamma$ production

Inclusive production of $W/Z/\gamma$ at hadron colliders

 $H_1 + H_2 \rightarrow W/Z/\gamma + X$

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2 channels at Born level:



Current work toward obtaining N²LO QCD corrections to the p_T spectrum NLO is well known, and implemented in numerical integration programs: FEWZ (Melnikov, Petriello'06; Gavin, Li, Petriello, Quackenbush'10), DYNNLO (Catani, Cieri, Ferrera, de Florian, Grazzini'09), QT (Gonsalves), MCFM (Campbell, Ellis, Williams)

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To improve fixed order predictions: include resummation of terms enhanced in a certain limit

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We focus on the large- p_T region of the spectrum. Close to the maximum kinematically-allowed value, p_T^{\max} , terms like $\ln(1 - p_T/p_T^{\max})$ appear in the fixed order result

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Expand around $p_T = p_T^{\max}$ and resum enhanced terms Laenen, Oderda, Sterman'98

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 $p_T = p_T^{\text{max}}$ limit not relevant phenomenologically: tiny cross section in this region; but threshold-enhanced terms expected to be important away from it: *dynamical threshold enhancement* (effect of rapid falloff of PDFs at large x)

Becher, Neubert, Xu'07; Catani, Mangano, Nason'98; Appell, Sterman, Mackenzie'88

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Real radiation simplifies considerably at the partonic threshold limit: only soft or collinear radiation

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SCET factorization formula ($q\bar{q}$ channel)

$$d\hat{\sigma} \propto H \int \mathrm{d}k \, J_g(m_X^2 - (2E_J)k) S_{q\bar{q}}(k)$$

 $m_X^2 = (p_a + p_b - p_Z)^2$, E_J is the energy of the jet

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Hadronic cross section is given by convolution with PDFs

$$d\sigma \propto \sum_{ab} \int dx_1 dx_2 f_a(x_1) f_b(x_2) \left[d\hat{\sigma}_{ab} \right]$$

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■ Complete results for N²LL accuracy

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■ Two-loop soft (and jet) functions known (needed for N³LL)

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Partial results at N³LL (not including two-loop non-logarithmic pieces for the hard, soft, and jet functions)

(resummation using traditional approach has now been computed at N²LL $_{Kidonakis, Gonsalves'12}$)

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Becher, XGT

Electroweak effects

Becher, XGT

Extracting the two-loop hard function (from results in the literature)

Becher, Bell, Lorentzen, Marti

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• (Public) code for N^3LL resummation

Lorentzen

(Padé approximation $\Gamma_4=\Gamma_3/(\Gamma_2)^2$ is always used for the four-loop cusp anomalous dimension)

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ew corrections cannot be omitted to have precise prediction for $p_T \gg M_V$



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 $\mathsf{Strategy:} \\ \mathsf{SM} \stackrel{(\mu_h \sim p_T)}{\to} \mathsf{SCET}_{\mathrm{EW}(\mathsf{dynamical}\ Z,\ W)} \stackrel{(\mu_l \sim M_V)}{\to} \mathsf{SCET}_{\gamma(\mathsf{photons}\ \mathsf{-and\ gluons-})} \\$

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W, Z bosons in SCET_{γ} in terms of (boosted) HQET-like fields.

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W, Z bosons in SCET_{γ} in terms of (boosted) HQET-like fields. J and S are defined in SCET_{γ} and contain only photons and gluons

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$$\alpha_s \sim a \quad ; \quad L := \log \frac{p_T^2}{M_V^2} \sim \frac{1}{a} \quad ; \quad \alpha_i \sim a^2$$

$$(\alpha_i = \alpha_1, \alpha_2, \alpha_{\rm em})$$

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$$\log \mathcal{M} \sim \begin{pmatrix} \alpha_{s}L^{2} + \alpha_{i}L^{2} & \alpha_{s}L + \alpha_{i}L & \alpha_{s} + \alpha_{i} \\ \sim \frac{1}{a} + 1 & \sim 1 + a & \sim a + a^{2} \\ \alpha_{s}^{2}L^{3} + \alpha_{i}^{2}L^{3} & \alpha_{s}^{2}L^{2} + \alpha_{i}^{2}L^{2} & \alpha_{s}^{2}L + \alpha_{s}\alpha_{i}L + \alpha_{i}^{2}L^{2} & \alpha_{s}^{2} + \alpha_{s}\alpha_{i} + \alpha_{i}^{2} \\ \sim \frac{1}{a} + a & \sim 1 + a^{2} & \alpha_{s}^{2}L + \alpha_{s}\alpha_{i}L + \alpha_{i}^{2}L^{2} & \alpha_{s}^{2} + \alpha_{s}\alpha_{i} + \alpha_{i}^{2} \\ \alpha_{s}^{3}L^{4} + \alpha_{i}^{3}L^{4} & \alpha_{s}^{3}L^{3} + \alpha_{s}^{2}\alpha_{i}L^{3} + \alpha_{s}\alpha_{i}^{2}L^{3} + \alpha_{i}^{3}L^{3} & \vdots & \ddots \\ \sim \frac{1}{a} + a^{2} & \sim 1 + a + a^{2} + a^{3} & \vdots & \ddots \\ \vdots & \vdots & \vdots & & & \end{pmatrix}$$

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Pure-QCD terms: $N^{k-1}LL$ accuracy corresponds to terms in the first k columns

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We will consider also the rest of the terms, which involve at least one α_i

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Some care is needed to define the observable, since we can have both photon and gluon real radiation.





From the full-SM point of view, p_T of V can be balanced by both recoiling parton and photon.

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Inclusive production: consider V+jet (with ew corr.) and $V + \gamma$ (with QCD corr.) Hollik, Kasprzik, Kniehl'07

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- Put a cut on parton transverse momentum Kühn, Kulesza, Pozzorini, Schulze'07

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(the two different approaches only induce small numerical differences on the size of the corrections)

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We consider the threshold limit. Operators in SCET will contain (i) collinear quark or gluon field, or (ii) collinear photon



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Can consider them separately at leading power in SCET -in practice we will just ignore operator (ii)-

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- pure-QCD corrections are also significant. Hard, jet and soft scales appropriate for QCD resummation are (Becher, Lorentzen, Schwartz'11):

$$\mu_h = \frac{13p_T + 2M_V}{12} - \frac{p_T^2}{\sqrt{s}} \quad ; \quad \mu_j = \frac{7p_T + 2M_V}{12} \left(1 - 2\frac{p_T}{\sqrt{s}}\right) \quad ; \quad \mu_s = \frac{\mu_j^2}{\mu_h}$$



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- μ_j (and μ_s) for p_T values LHC measures are above M_V
- main part of the ew corrections contained in the hard function
- ew corrections to jet and soft functions are small \rightarrow Consider only leading ew terms in J and S, then ew and strong corrections do not mix. Can set $\mu_j = M_V$ just in ew part



(scales varied by factor of 2; terms up to order a in the exponent for ew part)

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Z production



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W production



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Relative importance of ew corrections does not depend much on the order used for the QCD resummation 6 UNIVERSITÄT BERN ALBERT EINSTEIN CENTER FOR FUNDAMENTAL PHYSIC

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- Relative importance of ew corrections does not depend much on the order used for the QCD resummation
- Including electroweak terms up to order a in the exponent is enough for $\sim 1-2\%$ precision



- Including electroweak terms up to order a in the exponent is enough for $\sim 1-2\%$ precision
- Photon effects on the PDFs not included in the numerical evaluation. Some PDF sets have QED effects, but lower orders for QCD part

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Complete N³LL: two-loop hard function

Becher, Bell, Lorentzen, Marti

Two-loop QCD computations needed to extract the hard function H for $\rm N^3LL$ accuracy are known

Garland, Gehrmann, Glover, Koukoutsakis, Remiddi'02; Gehrmann, Tancredi'11



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Analytic result for two-loop QCD corrections to helicity amplitudes. Given in terms of one- and two-dimensional harmonic polylogarithms (very long expressions!)



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Analytic result for two-loop QCD corrections to helicity amplitudes. Given in terms of one- and two-dimensional harmonic polylogarithms (very long expressions!)

Finite amplitudes: UV renormalized. IR divergences subtracted according to Catani's formula.

Need to add IR div. back and subtract in \overline{MS} (as needed for H in SCET factorization formula)



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Complete N³LL: new (public) code

Lorentzen

New C++ code to compute the p_T spectrum up to N³LL accuracy.



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New C++ code to compute the p_T spectrum up to N³LL accuracy.

Much faster than previous Mathematica code. Speed increase specially important when including 2-loop hard function (for $N^{3}LL$).



Lorentzen

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Much faster than previous Mathematica code. Speed increase specially important when including 2-loop hard function (for N³LL). It takes about 30 min. to compute one p_T point at N³LL accuracy with per mill precision



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Numerical integrations done with Cuba libraries. Can take advantage of multicore processors



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Numerical integrations done with Cuba libraries. Can take advantage of multicore processors

Fully documented, easily configurable input parameters, to be made publicly available in the future



Impact of the 2-loop constant term



(gg
ightarrow gV channel not implemented yet)

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Conclusions and outlook



■ N³LL resummation (with Padé approx. for Γ_4) for $\gamma/W/Z$ production at large p_T is now achieved

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Electroweak-Sudakov effects included

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- Complete phenomenological analysis, at N³LL and with ew effects, and comparisons with LHC data will be presented in the future

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- Electroweak-Sudakov effects included
- Complete phenomenological analysis, at N³LL and with ew effects, and comparisons with LHC data will be presented in the future
 - ♦ Higgs production at large p_T will also be presented
 Becher, Schwarz