



# Property Measurements of Higgs-like Single Resonance at LHC “The JHU Generator”

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On behalf of

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# Outline

- Review the  $pp \rightarrow X \rightarrow VV$  interactions
  - The JHU Generator is used to simulate the  $pp \rightarrow X \rightarrow VV$  interactions
  - Quick comparison to the VBF@NLO for the spin 2  $X \rightarrow \gamma\gamma$  couplings
- Review the angular analysis and perform generator validations
- Summary

Describe  $pp \rightarrow X \rightarrow VV$   
Interactions

# The JHU Generator

- A MC program developed to simulate production and decay of  $X \rightarrow VV$  with  $X$  spin  $\leq 2$ 
  - $X \rightarrow ZZ \rightarrow 4l, 2l2\tau, 2l2\nu, 2l2q$
  - $X \rightarrow WW \rightarrow 2l2\nu, l\nu\tau\nu, l\nu qq$
  - $X \rightarrow \gamma\gamma$
- Includes all spin correlations and all possible couplings
  - Inputs are general dimensionless couplings - calculates matrix elements
- For the production of  $X$ , both  $gg$  and  $qq$  are considered
- Output in LHE format; e.g. can interface to Pythia for hadronization
- All code publicly available: [www.pha.jhu.edu/spin](http://www.pha.jhu.edu/spin)
  - A dedicated manual is in preparation, aiming to release soon

# X → VV Amplitude for Spin-0

- Model independent amplitude

$$A = v^{-1} \left( g_1^{(0)} m_V^2 \epsilon_1^* \epsilon_2^* + g_2^{(0)} f_{\mu\nu}^{*(1)} f^{*(2),\mu\nu} + g_3^{(0)} f^{*(1),\mu\nu} f_{\mu\alpha}^{*(2)} \frac{q_\nu q^\alpha}{\Lambda^2} + g_4^{(0)} f_{\mu\nu}^{*(1)} \tilde{f}^{*(2),\mu\nu} \right)$$

$$f^{(i),\mu\nu} = \epsilon_i^\mu q_i^\nu - \epsilon_i^\nu q_i^\mu \quad \tilde{f}_{\mu\nu}^{(i)} = 1/2 \epsilon_{\mu\nu\alpha\beta} f^{(i),\alpha\beta} = \epsilon_{\mu\nu\alpha\beta} \epsilon_i^\alpha q_i^\beta$$

- Rewrite it in terms of polarization vectors

$$A = v^{-1} \epsilon_1^{*\mu} \epsilon_2^{*\nu} \left( a_1 g_{\mu\nu} M_X^2 + a_2 q_\mu q_\nu + a_3 \epsilon_{\mu\nu\alpha\beta} q_1^\alpha q_2^\beta \right)$$

- The couplings  $a_1$ - $a_3$  terms are expressed in terms of the couplings  $g_1$ - $g_4$ , see reference paper

- The total amplitude is then expressed as the sum of 3 independent helicity amplitudes, which later can be used in angular analysis

$$A_{00} = -\frac{M_X^2}{v} \left( a_1 x + a_2 \frac{M_{V_1} M_{V_2}}{M_X^2} (x^2 - 1) \right) \quad \Leftarrow \quad x = \frac{M_X^2 - M_{V_1}^2 - M_{V_2}^2}{2M_{V_1} M_{V_2}}$$

$$A_{\pm\pm} = +\frac{M_X^2}{v} \left( a_1 \pm i a_3 \frac{M_{V_1} M_{V_2}}{M_X^2} \sqrt{x^2 - 1} \right)$$

# X → VV Amplitude for Spin-2

- Model independent amplitude including 10 dimensionless couplings with arbitrary parity

$$\begin{aligned}
 A = \Lambda^{-1} & \left[ 2g_1^{(2)} t_{\mu\nu} f^{*1,\mu\alpha} f^{*2,\nu\alpha} + 2g_2^{(2)} t_{\mu\nu} \frac{q_\alpha q_\beta}{\Lambda^2} f^{*1,\mu\alpha} f^{*2,\nu,\beta} \right. \\
 & + g_3^{(2)} \frac{\tilde{q}^\beta \tilde{q}^\alpha}{\Lambda^2} t_{\beta\nu} (f^{*1,\mu\nu} f_{\mu\alpha}^{*2} + f^{*2,\mu\nu} f_{\mu\alpha}^{*1}) + g_4^{(2)} \frac{\tilde{q}^\nu \tilde{q}^\mu}{\Lambda^2} t_{\mu\nu} f^{*1,\alpha\beta} f_{\alpha\beta}^{*(2)} \\
 & + m_V^2 \left( 2g_5^{(2)} t_{\mu\nu} \epsilon_1^{*\mu} \epsilon_2^{*\nu} + 2g_6^{(2)} \frac{\tilde{q}^\mu q_\alpha}{\Lambda^2} t_{\mu\nu} (\epsilon_1^{*\nu} \epsilon_2^{*\alpha} - \epsilon_1^{*\alpha} \epsilon_2^{*\nu}) + g_7^{(2)} \frac{\tilde{q}^\mu \tilde{q}^\nu}{\Lambda^2} t_{\mu\nu} \epsilon_1^* \epsilon_2^* \right) \\
 & + g_8^{(2)} \frac{\tilde{q}_\mu \tilde{q}_\nu}{\Lambda^2} t_{\mu\nu} f^{*1,\alpha\beta} \tilde{f}_{\alpha\beta}^{*(2)} + g_9^{(2)} t_{\mu\alpha} \tilde{q}^\alpha \epsilon_{\mu\nu\rho\sigma} \epsilon_1^{*\nu} \epsilon_2^{*\rho} q^\sigma \left. \right) \\
 & + \frac{g_{10}^{(2)} t_{\mu\alpha} \tilde{q}^\alpha}{\Lambda^2} \epsilon_{\mu\nu\rho\sigma} q^\rho \tilde{q}^\sigma (\epsilon_1^{*\nu} (q\epsilon_2^*) + \epsilon_2^{*\nu} (q\epsilon_1^*)) \left. \right]
 \end{aligned}$$

# X → VV Helicity Amplitudes for Spin-2

- Rewrite the amplitude in terms of polarization amplitudes for the on-shell decay

$$\begin{array}{l}
 2^+ \text{ } CP \\
 2^- \text{ } \overline{CP} \\
 \\
 2^+ \text{ } \overline{CP} \\
 2^- \text{ } CP
 \end{array}
 \quad
 A = \frac{e_1^{*\mu} e_2^{*\nu}}{\Lambda} \left[
 \begin{array}{l}
 c_1 t_{\mu\nu}(q_1 q_2) + c_2 g_{\mu\nu} t_{\alpha\beta} (q_1 - q_2)^\alpha (q_1 - q_2)^\beta \\
 + \frac{c_3 t_{\alpha\beta}}{M_X^2} q_{2\mu} q_{1\nu} (q_1 - q_2)^\alpha (q_1 - q_2)^\beta + 2c_4 (t_{\mu\alpha} q_{1\nu} q_2^\alpha + t_{\nu\alpha} q_{2\mu} q_1^\alpha) \\
 + \frac{c_5 t_{\alpha\beta}}{M_X^2} (q_1 - q_2)^\alpha (q_1 - q_2)^\beta \epsilon_{\mu\nu\rho\sigma} q_1^\rho q_2^\sigma + c_6 t^{\alpha\beta} (q_1 - q_2)_\beta \epsilon_{\mu\nu\alpha\rho} q^\rho \\
 + \frac{c_7 t^{\alpha\beta}}{M_X^2} (q_1 - q_2)_\beta (\epsilon_{\alpha\mu\rho\sigma} q^\rho (q_1 - q_2)^\sigma q_\nu + \epsilon_{\alpha\nu\rho\sigma} q^\rho (q_1 - q_2)^\sigma q_\mu)
 \end{array}
 \right]$$

- The couplings  $c_1$ - $c_7$  terms are expressed in terms of the couplings  $g_1$ - $g_{10}$ , see reference paper

- It is then expressed in terms of 9 helicity amplitudes to be used in angular analysis

$$\begin{array}{l}
 A_{00} = \frac{M_X^4}{M_V^2 \sqrt{6} \Lambda} \left[ (1 + \beta^2) \left( \frac{c_1}{8} - \frac{c_2}{2} \beta^2 \right) - \beta^2 \left( \frac{c_3}{2} \beta^2 - c_4 \right) \right] \\
 A_{\pm\pm} = \frac{M_X^2}{\sqrt{6} \Lambda} \left[ \frac{c_1}{4} (1 + \beta^2) + 2c_2 \beta^2 \pm i\beta (c_5 \beta^2 - 2c_6) \right] \\
 A_{\pm 0} \equiv A_{0\pm} = \frac{M_X^3}{M_V \sqrt{2} \Lambda} \left[ \frac{c_1}{8} (1 + \beta^2) + \frac{c_4}{2} \beta^2 \mp i\beta \frac{(c_6 + c_7 \beta^2)}{2} \right] \\
 A_{+-} \equiv A_{-+} = \frac{M_X^2}{4\Lambda} c_1 (1 + \beta^2)
 \end{array}$$

- The full helicity amplitudes for the off-shell case are in preparation for manuscript

# Connect to VBF@NLO for spin 2

- We compare the equations 1-2 to the VBF@NLO release note
- [http://www-itp.particle.uni-karlsruhe.de/~vbfnlweb/wiki/lib/exe/fetch.php?media=documentation:vbfnlo\\_releasenote26.pdf](http://www-itp.particle.uni-karlsruhe.de/~vbfnlweb/wiki/lib/exe/fetch.php?media=documentation:vbfnlo_releasenote26.pdf)

For the singlet spin-2 field,  $T^{\mu\nu}$ , the effective Lagrangian is

$$\mathcal{L}_{\text{singlet}} = \frac{1}{\Lambda} T_{\mu\nu} \left( \boxed{f_1 B^{\alpha\nu} B_\alpha^\mu + f_2 W_i^{\alpha\nu} W_\alpha^{i,\mu}} + \boxed{f_3 \tilde{B}^{\alpha\nu} B_\alpha^\mu + f_4 \tilde{W}_i^{\alpha\nu} W_\alpha^{i,\mu}} + \boxed{2f_5 (D^\mu \Phi)^\dagger (D^\nu \Phi)} \right), \quad (1)$$

and for the spin-2 triplet field,  $T_j^{\mu\nu}$ , the effective Lagrangian is given by

$$\mathcal{L}_{\text{triplet}} = \frac{1}{\Lambda} T_{\mu\nu j} \left( \boxed{f_6 (D^\mu \Phi)^\dagger \sigma^j (D^\nu \Phi) + f_7 W_\alpha^{j,\mu} B^{\alpha\nu}} \right), \quad (2)$$

- The approximate corresponding couplings in the JHUGen

$$\boxed{g1} \quad \boxed{g5} \quad \boxed{g9}$$

- Technical parameters for generating the 2m+
- JHUGen:  $g1 = g5 = 1$
- VBF@NLO:  $F1 = F2 = F5 = 1$



# Technical Details on Generating $0+/0-/2m+$

A more comprehensive manual is in preparation

# Technical Detail on the $0^+ / 0^-$ Decay

- Coupling constants setup for the file `mod_Parameters.F90`

$0^+$

```
!— parameters that define off-shell spin 0 coupling to SM fields, see note
complex(8), public, parameter :: ghg2 = (1.0d0,0d0)
complex(8), public, parameter :: ghg3 = (0.0d0,0d0)
complex(8), public, parameter :: ghg4 = (0.0d0,0d0) ! pseudoscalar
complex(8), public, parameter :: ghz1 = (1.0d0,0d0)
complex(8), public, parameter :: ghz2 = (0.0d0,0d0)
complex(8), public, parameter :: ghz3 = (0.0d0,0d0)
complex(8), public, parameter :: ghz4 = (0.0d0,0d0) ! pseudoscalar
```

$0^-$

```
!— parameters that define off-shell spin 0 coupling to SM fields, see note
complex(8), public, parameter :: ghg2 = (0.0d0,0d0) ! scalar
complex(8), public, parameter :: ghg3 = (0.0d0,0d0)
complex(8), public, parameter :: ghg4 = (1.0d0,0d0) ! pseudoscalar
complex(8), public, parameter :: ghz1 = (0.0d0,0d0) ! scalar
complex(8), public, parameter :: ghz2 = (0.0d0,0d0)
complex(8), public, parameter :: ghz3 = (0.0d0,0d0)
complex(8), public, parameter :: ghz4 = (1.0d0,0d0) ! pseudoscalar
```

- Follow the instructions of the README for the executable command

# Technical Details on the $2m+$ Decay

- Coupling constants setup for the file `mod_Parameters.F90`

```
!-- parameters that define spin 2 coupling to SM fields, see note
! minimal coupling corresponds to a1 = b1 = b5 = 1 everything else 0
complex(8), public, parameter :: a1 = (1.0d0,0d0) ! g1 -- c.f. draft
complex(8), public, parameter :: a2 = (0.0d0,0d0) ! g2
complex(8), public, parameter :: a3 = (0.0d0,0d0) ! g3
complex(8), public, parameter :: a4 = (0.0d0,0d0) ! g4
complex(8), public, parameter :: a5 = (0.0d0,0d0) ! pseudoscalar, g8
complex(8), public, parameter :: graviton_qq_left = (1.0d0,0d0)! graviton coupling to quarks
complex(8), public, parameter :: graviton_qq_right = (1.0d0,0d0)

!-- see mod_Graviton
logical, public, parameter :: generate_bis = .true.
logical, public, parameter :: use_dynamic_MG = .true.

complex(8), public, parameter :: b1 = (1.0d0,0d0) ! all b' below are g's in the draft
complex(8), public, parameter :: b2 = (0.0d0,0d0)
complex(8), public, parameter :: b3 = (0.0d0,0d0)
complex(8), public, parameter :: b4 = (0.0d0,0d0)
complex(8), public, parameter :: b5 = (1.0d0,0d0)
complex(8), public, parameter :: b6 = (0.0d0,0d0)
complex(8), public, parameter :: b7 = (0.0d0,0d0)
complex(8), public, parameter :: b8 = (0.0d0,0d0)
complex(8), public, parameter :: b9 = (0.0d0,0d0)
complex(8), public, parameter :: b10 = (0.0d0,0d0) ! this coupling does not contribute for gamma+gamma final states
```

# Review Angular Analysis and Perform JHUGen Validation

# Angular Analysis

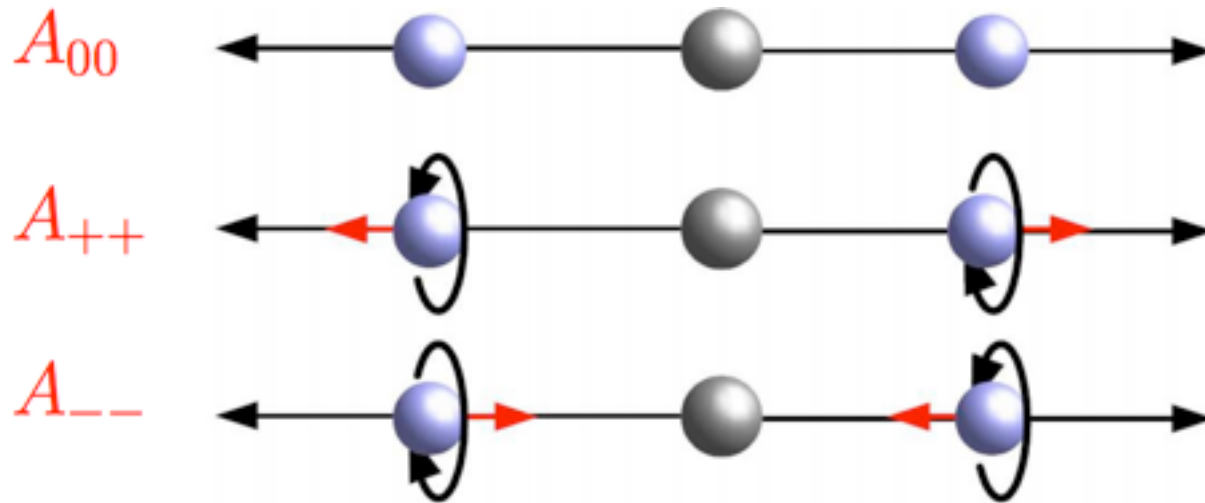
- The helicity amplitudes can be measured from angular analysis

$$d\sigma \propto \sum_{\chi, \mu, \tau} \left| \sum_{\lambda, m} A_{ab}(\{\Omega\}) \right|^2$$

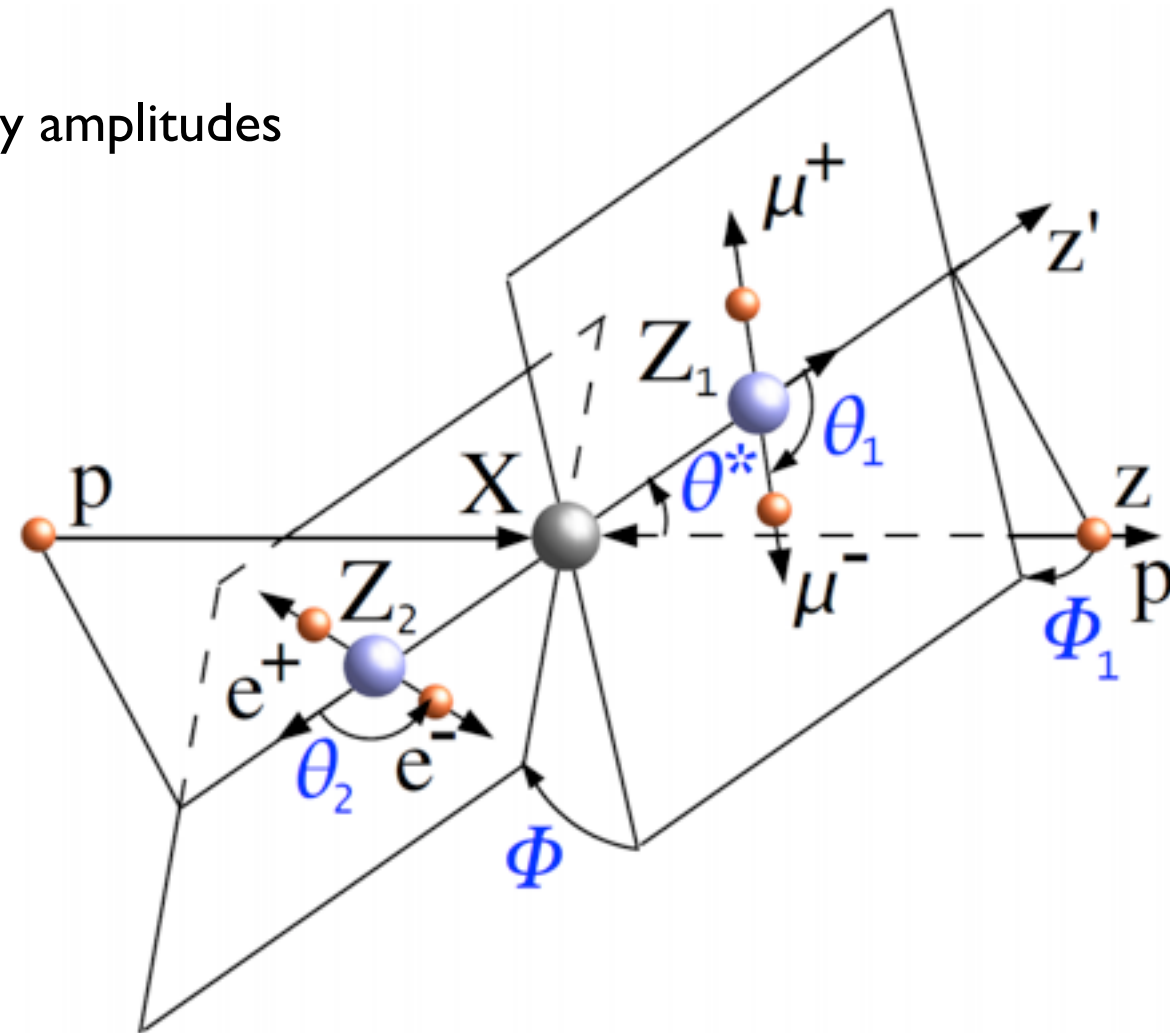
$$A_{ab} \propto D_{\chi_1 - \chi_2, m}^{J^*}(\Omega^*) B_{\chi_1 \chi_2} \times D_{m, \lambda_1 - \lambda_2}^{J^*}(\Omega) A_{\lambda_1 \lambda_2}$$

$$\times D_{\lambda_1, \mu_1 - \mu_2}^{S_1^*}(\Omega_1) T(\mu_1, \mu_2) \times D_{\lambda_2, \tau_1 - \tau_2}^{S_2^*}(\Omega_2) W(\tau_1, \tau_2)$$

- For example, a Higgs like spin 0 resonance has 3 helicity amplitudes



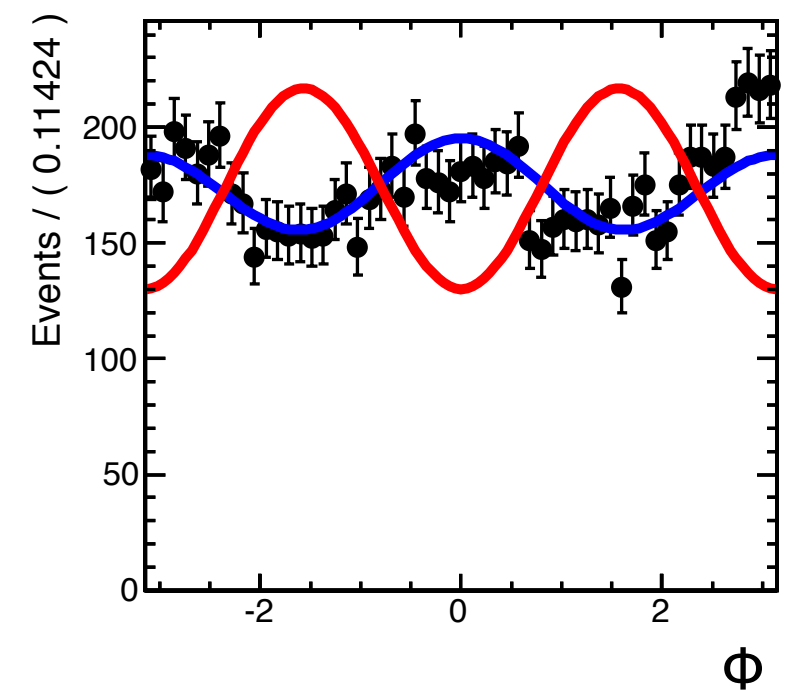
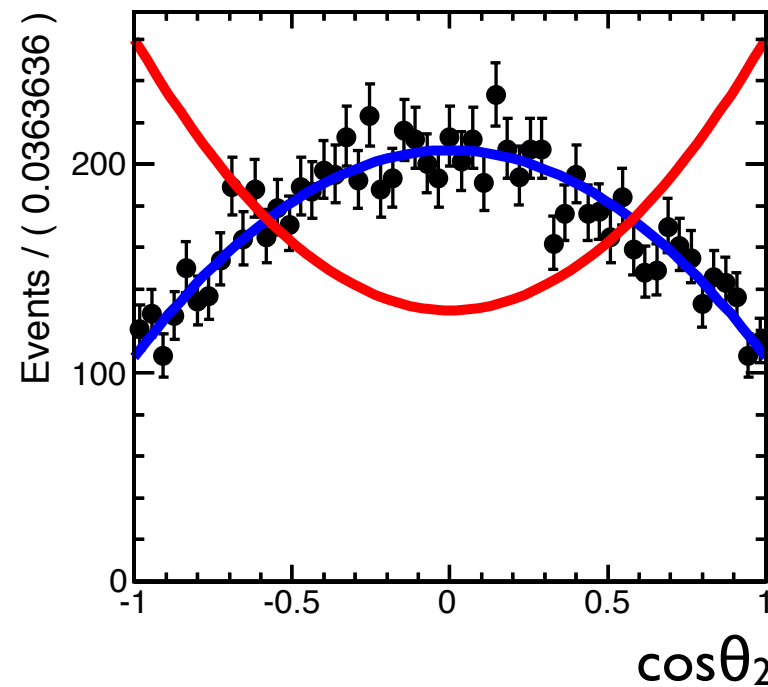
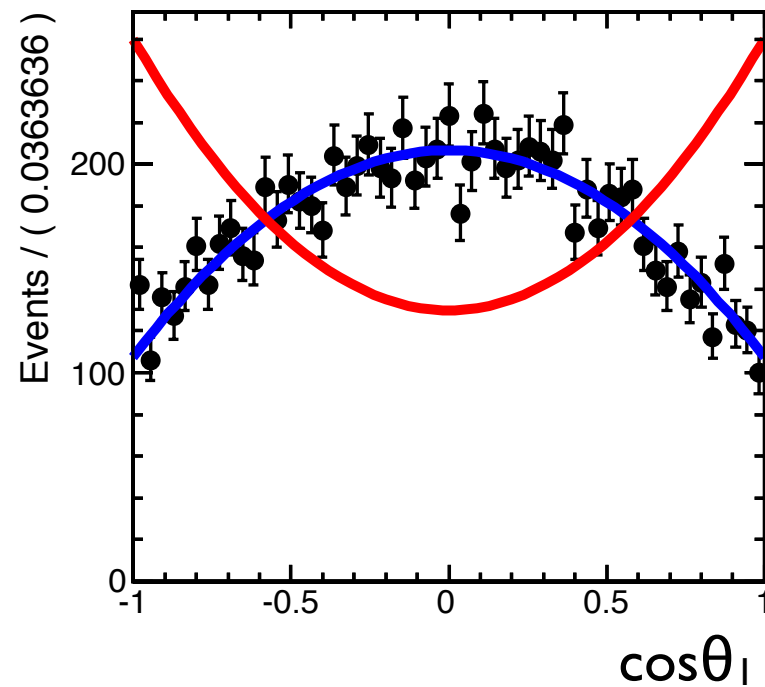
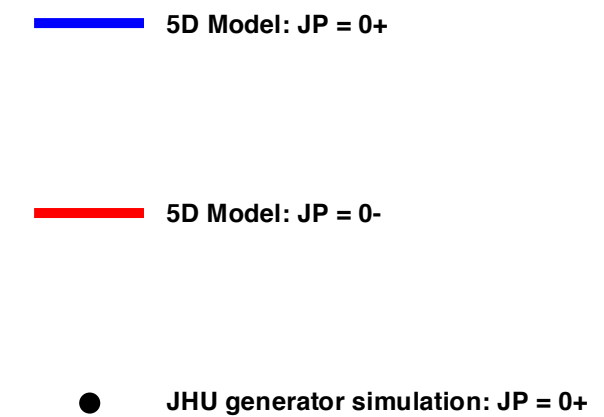
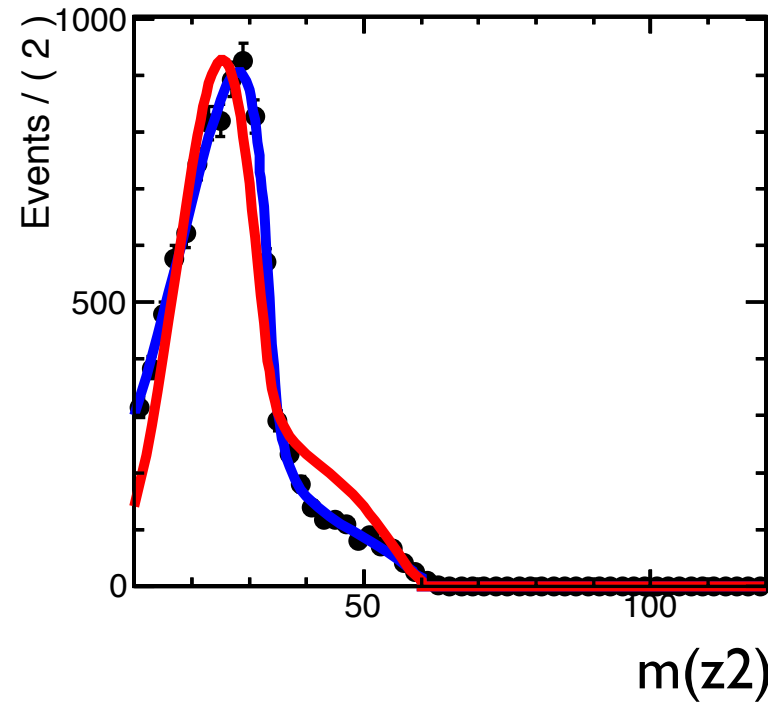
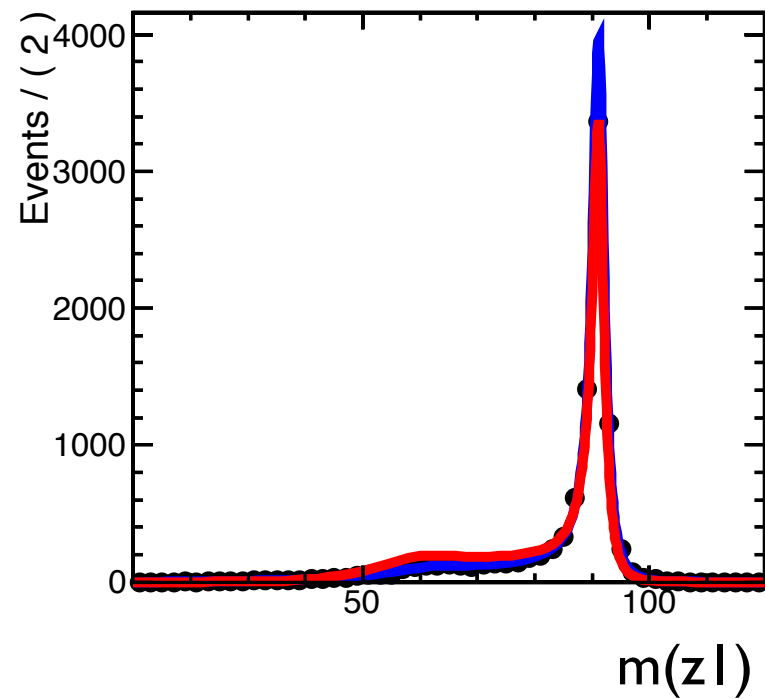
Need only 5 angles  $\{\theta_1, \theta_2, \theta^*, \Phi, \Phi_1\}$   
to fully describe the production/decay



- Detailed expressions for the spin 1 and spin 2 can be found in the reference [PhysRevD.81.075022](#)

# Generator Validation ( $X \rightarrow ZZ 0+ / 0-$ )

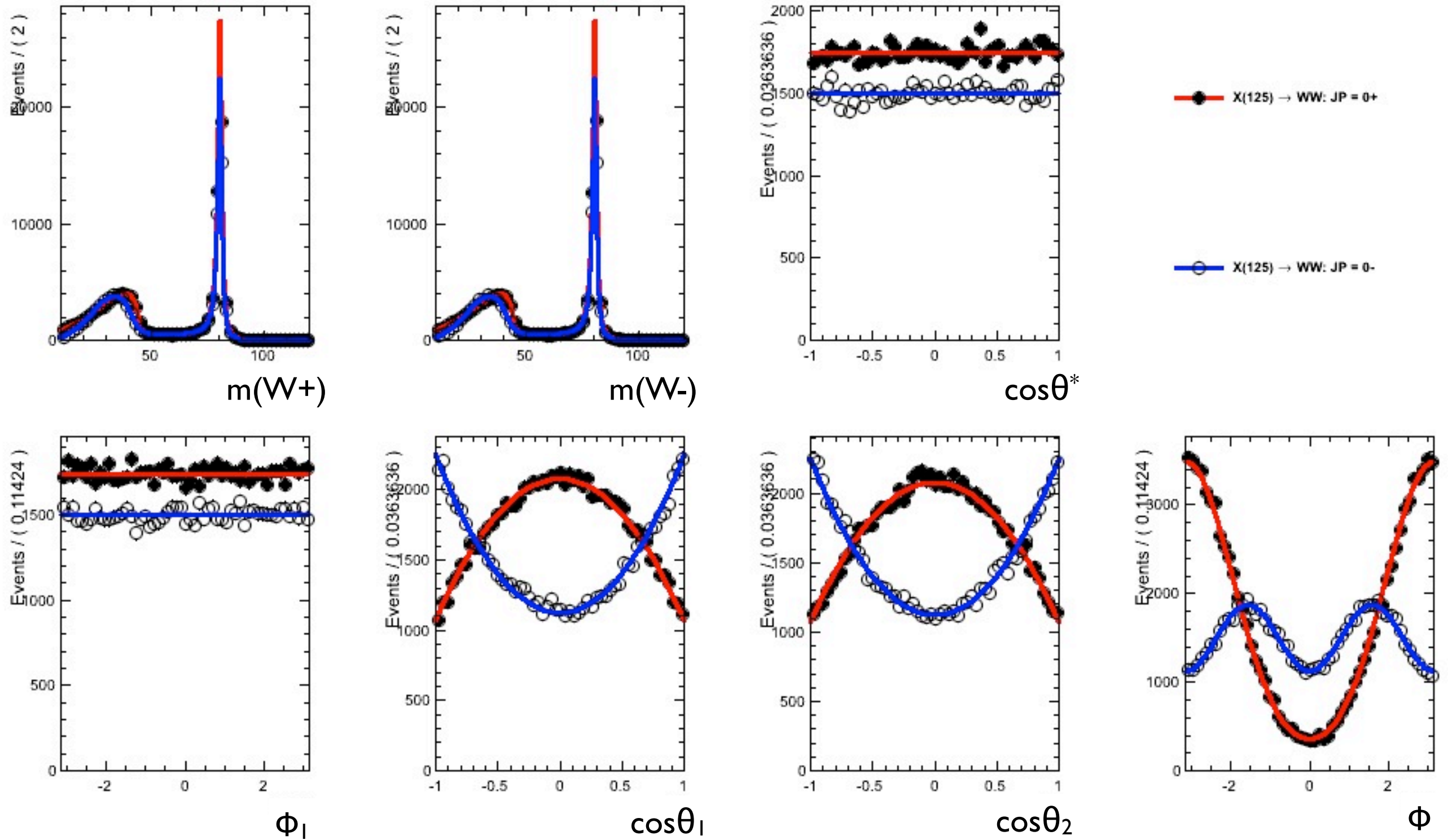
- In this test  $m_X = 125$  GeV



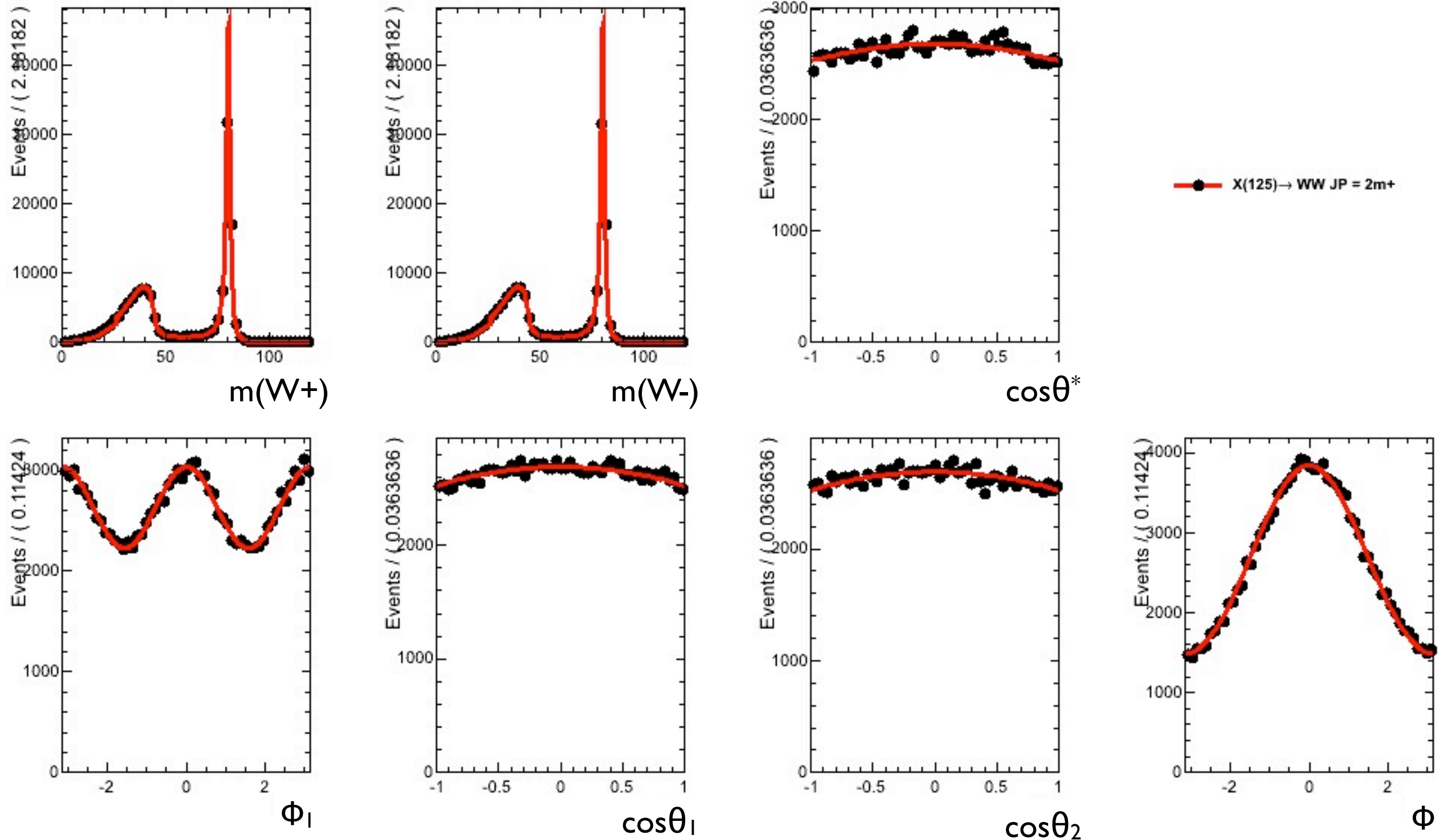


# Generator Validation ( $X \rightarrow WW$ 0+/0-)

- In this test  $m_X = 125$  GeV

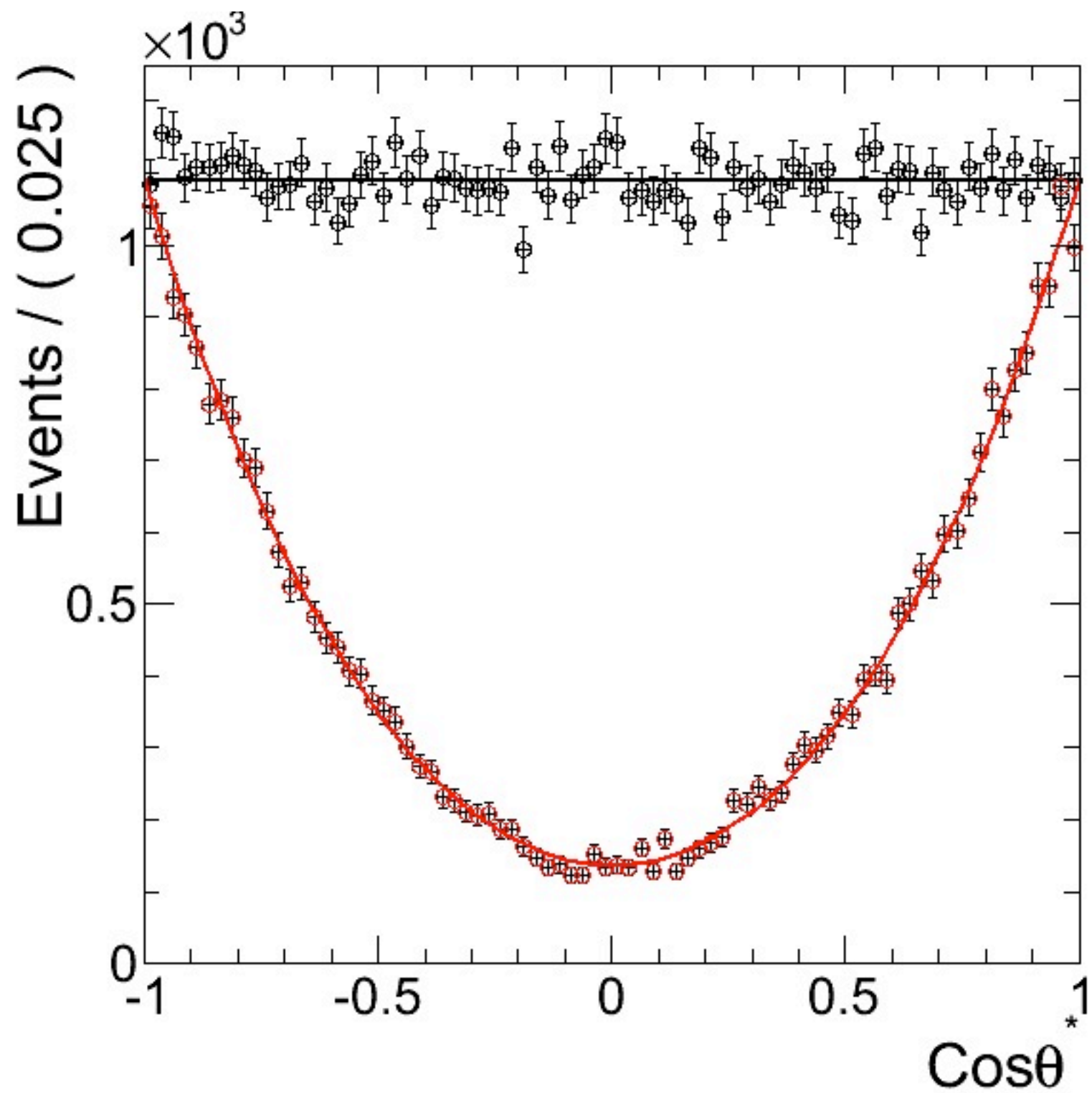


# Generator Validation ( $X \rightarrow WW 2m+$ )





# Generator Validation ( $X \rightarrow \gamma\gamma$ )



$0^+$   
 $2m^+$

# Summary

- We reviewed the model-independent amplitude for  $X \rightarrow VV \rightarrow 4$  fermions interaction
- We reviewed the JHU generator for production and decay of  $X \rightarrow VV$  with  $X$  spin  $\leq 2$ 
  - $X \rightarrow ZZ \rightarrow 4l, 2l2\tau, 2l2\nu, 2l2q$
  - $X \rightarrow WW \rightarrow 2l2\nu, lv\tau\nu, lvqq$
  - $X \rightarrow \gamma\gamma$
- Make a quick comparison to the VBF@NLO for the spin 2 model
  - JHUGen considers more general couplings
  - Both generators can generate the minimal couplings  $2m+$  models