



The Universit of Manchest

Monte Carlo Event Generators

Monte

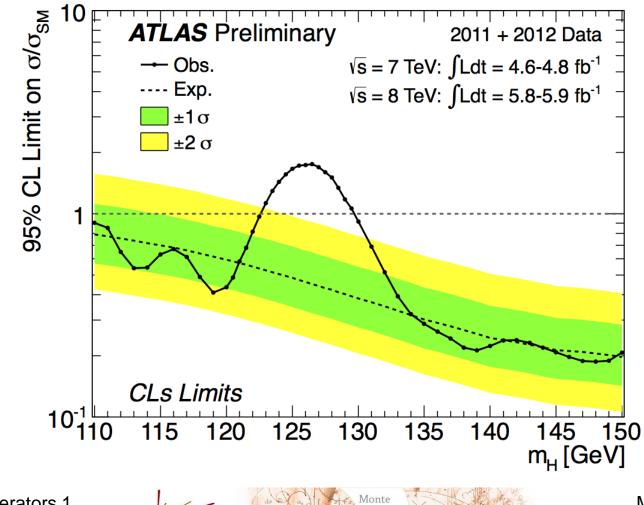
Carlo

net

Mike Seymour University of Manchester



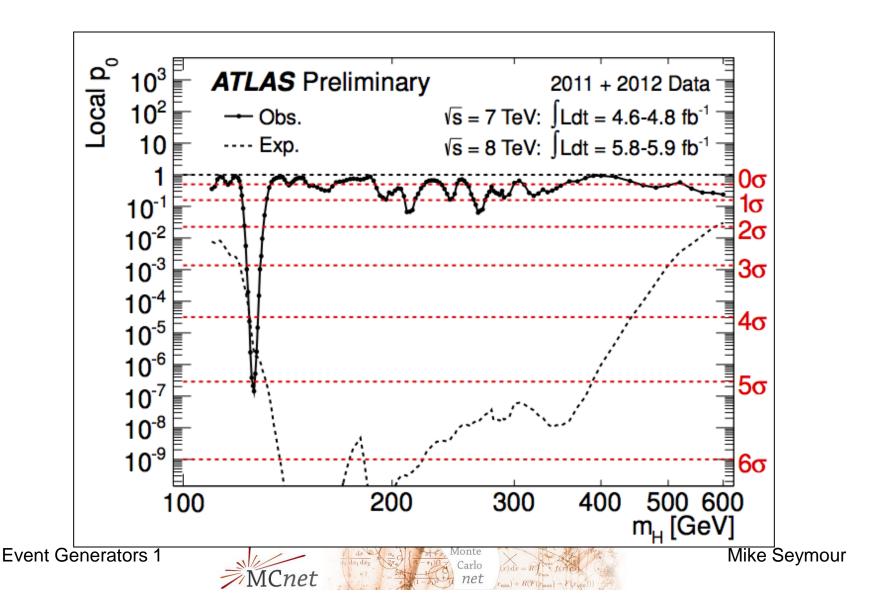
19th August - 1st September 2012

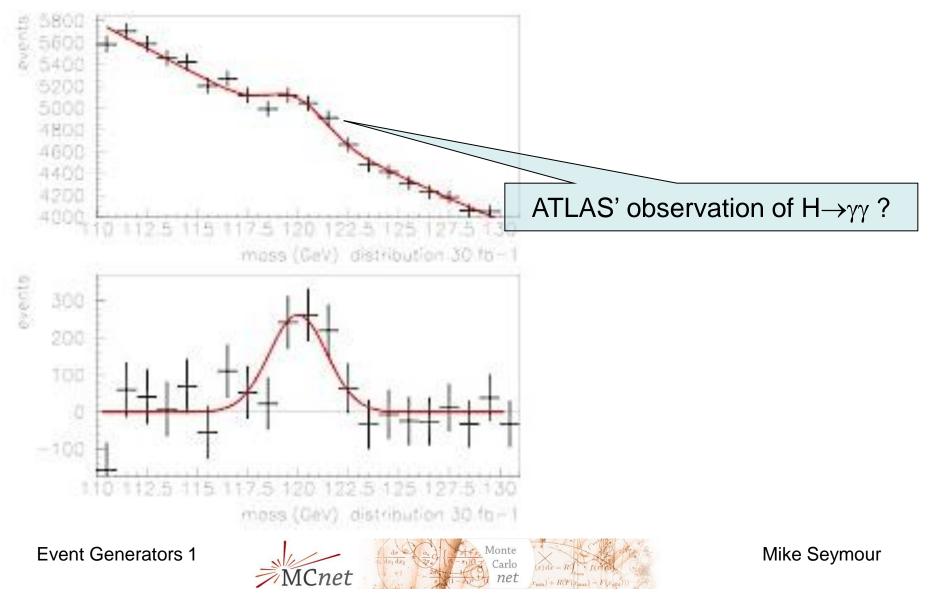


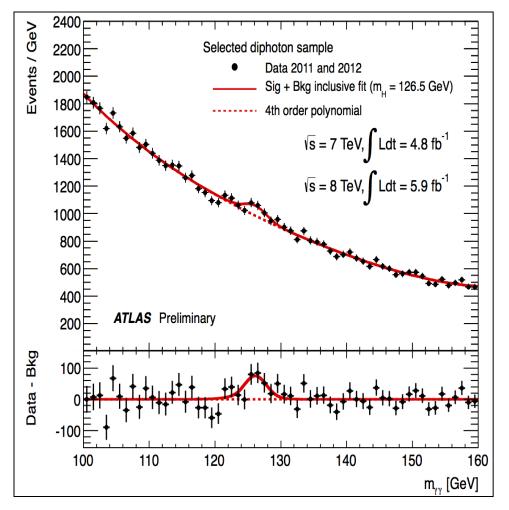
MCnet

Carlo

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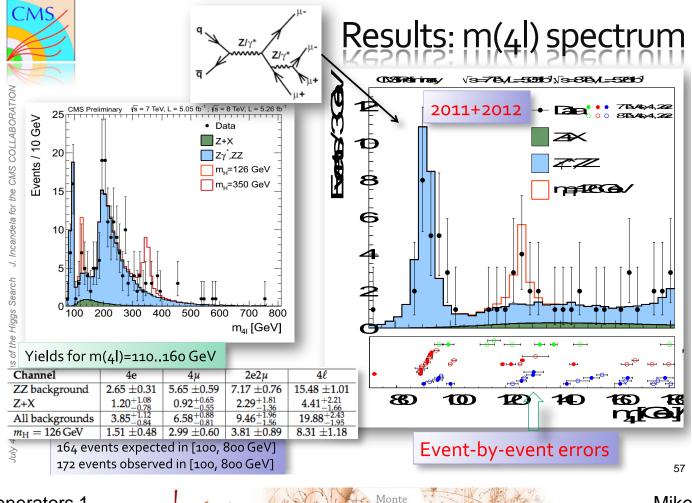






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Carlo

net

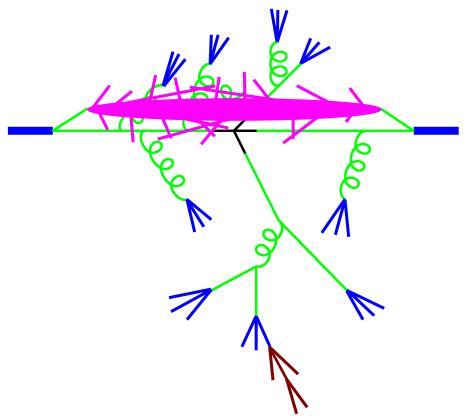
 $(x_{\min}) + R(F(x_{\max}))$

MCnet

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Structure of LHC Events

- 1. Hard process
- 2. Parton shower
- 3. Hadronization
- 4. Underlying event
- 5. Unstable particle decays



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Intro to Monte Carlo Event Generators

- 1. Parton showers
- 2. Hadronization
- 3. Underlying Event / Soft Inclusive Models



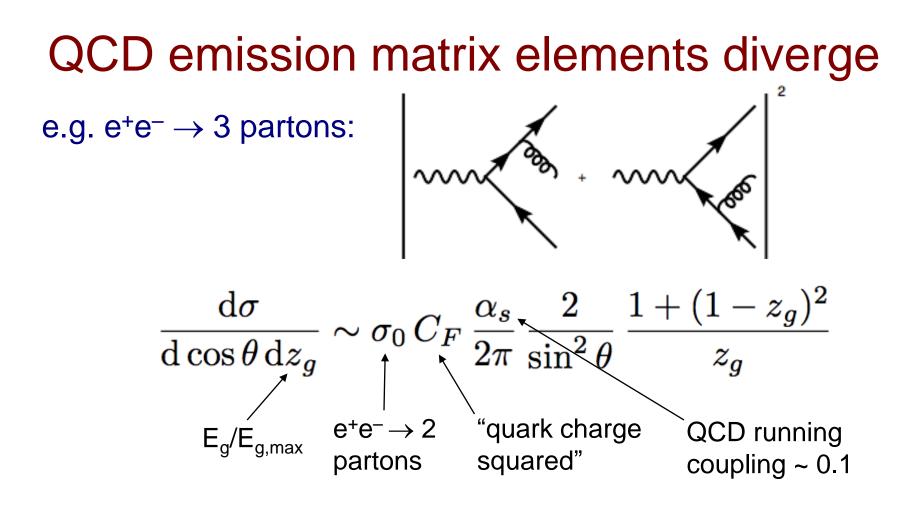
Parton Showers: Introduction

- QED: accelerated charges radiate.
- QCD identical: accelerated colours radiate.
- gluons also charged.
- \rightarrow cascade of partons.
- = parton shower.

- 1. e^+e^- annihilation to jets.
- 2. Universality of collinear emission.
- 3. Sudakov form factors.
- 4. Universality of soft emission.
- 5. Angular ordering.
- 6. Initial-state radiation.
- 7. Hard scattering.
- 8. Heavy quarks.
- 9. Dipole cascades.







Divergent in collinear limit $\theta \rightarrow 0,\pi$ (for massless quarks) and soft limit $z_g \rightarrow 0$

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can separate into two independent jets:

$2 d\cos\theta$	_	$d\cos heta$	$d\cos\theta$
$\sin^2\theta$	_	$\frac{1-\cos\theta}{1-\cos\theta}$	$\frac{1}{1+\cos\theta}$
		$d\cos\theta$ _	$d\cosar{ heta}$
		$\frac{1-\cos\theta}{1-\cos\theta}$	$\overline{1-\cosar{ heta}}$
	\approx	$\frac{d\theta^2}{\theta^2} + \frac{d\bar{\theta}^2}{\bar{\theta}^2}$	

jets evolve independently

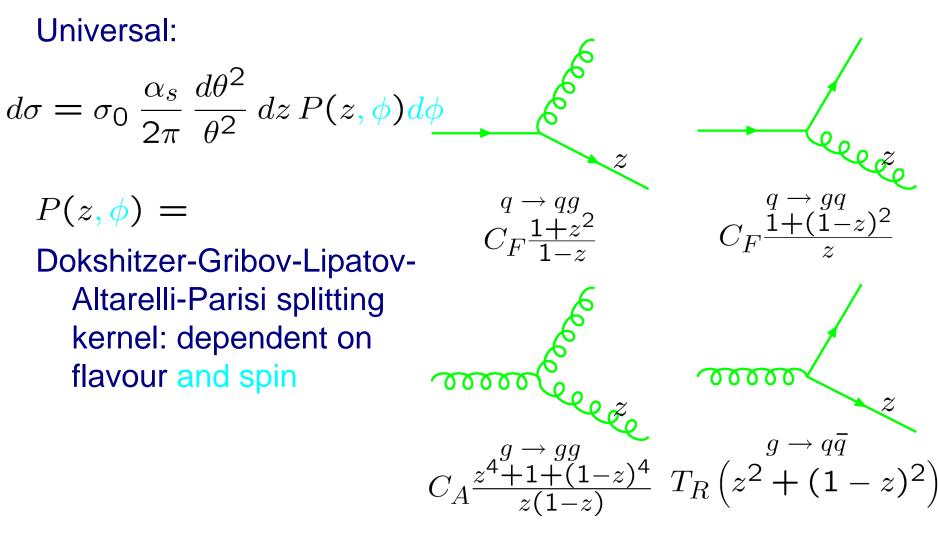
$$d\sigma = \sigma_0 \sum_{\text{jets}} C_F \frac{\alpha_s}{2\pi} \frac{d\theta^2}{\theta^2} dz \frac{1 + (1 - z)^2}{z}$$

Exactly same form for anything $\propto \theta^2$ eg transverse momentum: $k_{\perp}^2 = z^2(1-z)^2 \ \theta^2 \ E^2$ invariant mass: $q^2 = z(1-z) \ \theta^2 \ E^2$

$$\frac{d\theta^{2}}{\theta^{2}} = \frac{dk_{\perp}^{2}}{k_{\perp}^{2}} = \frac{dq^{2}}{k_{\perp}^{2}}$$

$$\frac{dq^{2}}{\frac{dq^$$

Collinear Limit



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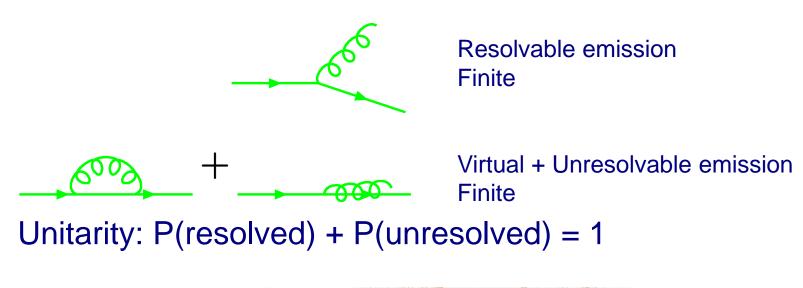


Resolvable partons

What is a parton? Collinear parton pair \longleftrightarrow single parton

Introduce resolution criterion, eg $k_{\perp} > Q_0$.

Virtual corrections must be combined with unresolvable real emission



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Sudakov form factor

Probability(emission between q^2 and $q^2 + dq^2$) $d\mathcal{P} = \frac{\alpha_s}{2\pi} \frac{dq^2}{q^2} \int_{Q_0^2/q^2}^{1-Q_0^2/q^2} dz \ P(z) \equiv \frac{dq^2}{q^2} \bar{P}(q^2).$

Define probability(no emission between Q^2 and q^2) to be $\Delta(Q^2, q^2)$. Gives evolution equation

$$\frac{d\Delta(Q^2, q^2)}{dq^2} = \Delta(Q^2, q^2) \frac{d\mathcal{P}}{dq^2}$$
$$\Rightarrow \Delta(Q^2, q^2) = \exp - \int_{q^2}^{Q^2} \frac{dk^2}{k^2} \bar{P}(k^2).$$

c.f. radioactive decay atom has probability λ per unit time to decay. Probability(no decay after time T) = $\exp - \int^T dt \lambda$

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Sudakov form factor

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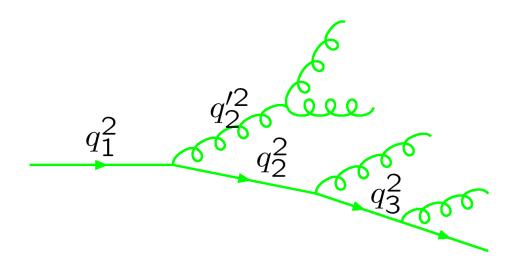
$$\frac{d\Delta(Q^2, q^2)}{dq^2} = \Delta(Q^2, q^2) \frac{d\mathcal{P}}{dq^2}$$
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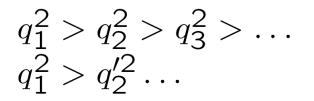
 $\Delta(Q^2, Q_0^2) \equiv \Delta(Q^2)$ Sudakov form factor =Probability(emitting no resolvable radiation)

 $\Delta_q(Q^2) \sim \exp_{Carlo} \frac{\alpha_s}{2\pi} \log^2 \frac{Q^2}{Q^2}$ MCnet

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Multiple emission





But initial condition? $q_1^2 < ???$

Process dependent

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Monte Carlo implementation

Can generate branching according to

$$d\mathcal{P} = \frac{dq^2}{q^2} \bar{P}(q^2) \,\Delta(Q^2, q^2)$$

By choosing $0 < \rho < 1$ uniformly: If $\rho < \Delta(Q^2)$ no resolvable radiation, evolution stops. Otherwise, solve $\rho = \Delta(Q^2, q^2)$ for q^2 =emission scale

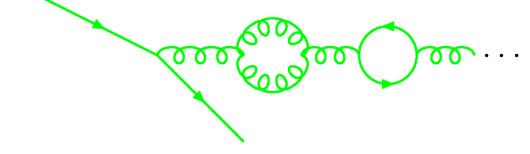
Considerable freedom: Evolution scale: $q^2/k_{\perp}^2/\theta^2$? z: Energy? Light-cone momentum? Massless partons become massive. How? Upper limit for q^2 ?

All formally free choices, but can be very important numerically

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Running coupling

Effect of summing up higher orders:



absorbed by replacing α_s by $\alpha_s(k_{\perp}^2)$.

Much faster parton multiplication – phase space fills with soft gluons.

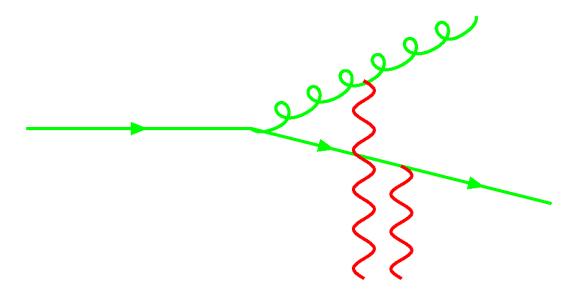
Must then avoid Landau pole: $k_{\perp}^2 \gg \Lambda^2$. Q_0 now becomes physical parameter!

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Soft limit

Also universal. But at amplitude level...

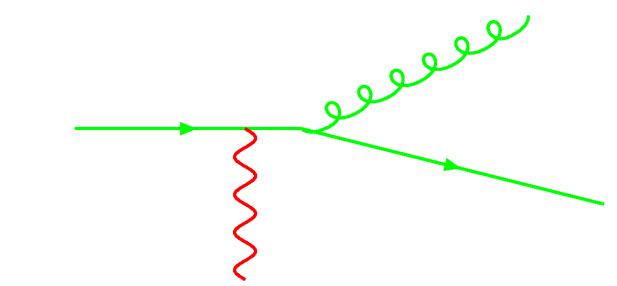


soft gluon comes from everywhere in event. → Quantum interference. Spoils independent evolution picture?

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Angular ordering



outside angular ordered cones, soft gluons sum coherently: only see colour charge of whole jet.

Soft gluon effects fully incorporated by using θ^2 as evolution variable: angular ordering

First gluon not necessarily hardest!

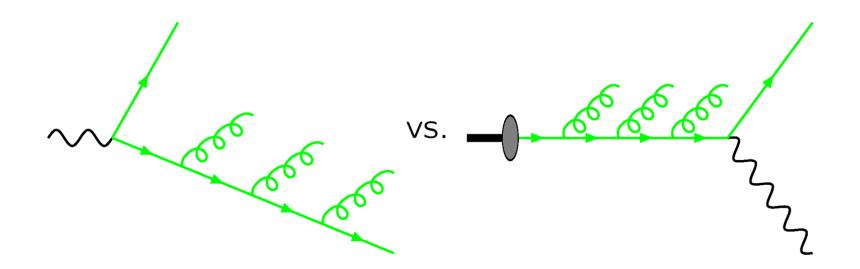
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NO:

Initial state radiation

In principle identical to final state (for not too small x)

In practice different because both ends of evolution fixed:



Use approach based on evolution equations...

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Backward evolution

DGLAP evolution: pdfs at(x, Q^2) as function of pdfs at ($> x, Q_0^2$):

Evolution paths sum over all possible events.

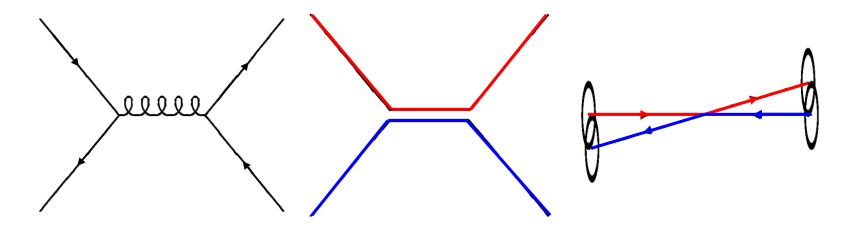
Formulate as backward evolution: start from hard scattering and work down in q^2 , up in x towards incoming hadron.

Algorithm identical to final state with $\Delta_i(Q^2, q^2)$ replaced by $\Delta_i(Q^2, q^2)/f_i(x, q^2)$. **Event Generators 1**



Hard Scattering

Sets up initial conditions for parton showers. Colour coherence important here too.

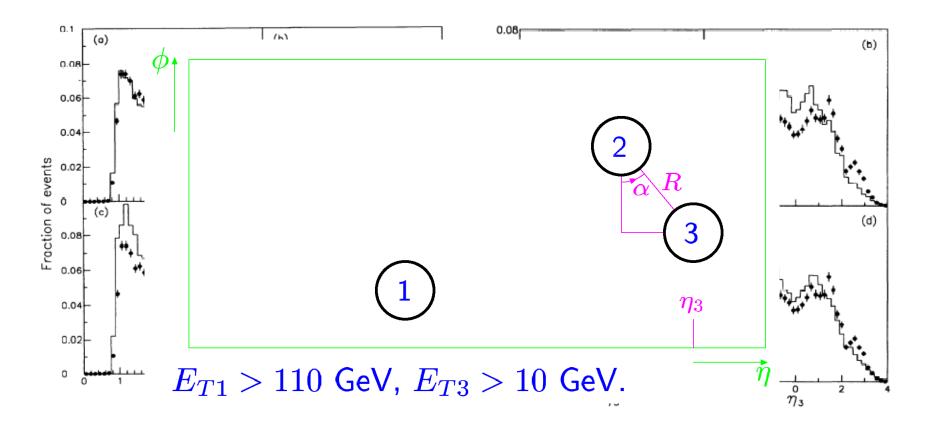


Emission from each parton confined to cone stretching to its colour partner

Essential to fit Tevatron data...

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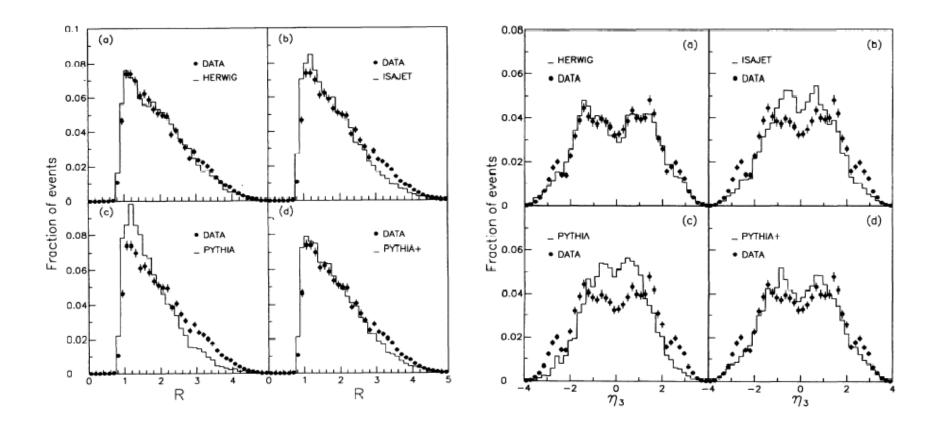




Distributions of third-hardest jet in multi-jet events

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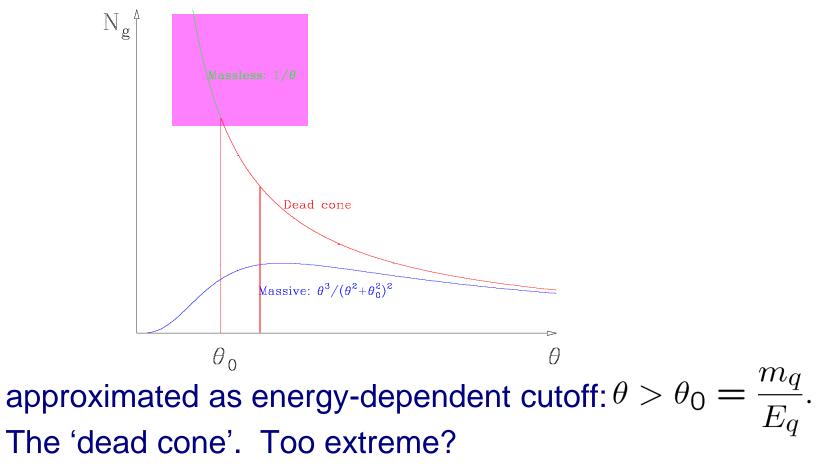
Distributions of third-hardest jet in multi-jet events HERWIG has complete treatment of colour coherence, PYTHIA+ has partial

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Heavy Quarks/Spartons

look like light quarks at large angles, sterile at small angles:



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Heavy Quarks/Spartons

More properly treated using quasi-collinear splitting:

 $\mathrm{d}\mathcal{P}_{\tilde{i}\tilde{j}\to ij} = \frac{\alpha_S}{2\pi} \,\frac{\mathrm{d}\tilde{q}^2}{\tilde{a}^2} \,\mathrm{d}z \,P_{\tilde{i}\tilde{j}\to ij}\left(z,\tilde{q}\right),$ $P_{q \to qg} = \frac{C_F}{1-z} \left| 1 + z^2 - \frac{2m_q^2}{z\tilde{q}^2} \right|,$ $P_{g \to gg} = C_A \left[\frac{z}{1-z} + \frac{1-z}{z} + z (1-z) \right],$ $P_{g \to q \bar{q}} = T_R \left| 1 - 2z \left(1 - z \right) + \frac{2m_q^2}{z \left(1 - z \right) \tilde{q}^2} \right|,$ \rightarrow smooth suppression $P_{\tilde{g}\to\tilde{g}g} = \frac{C_A}{1-z} \left| 1+z^2 - \frac{2m_{\tilde{g}}^2}{z\tilde{q}^2} \right|,$ in forward region $P_{\tilde{q}\to\tilde{q}g} = \frac{2C_F}{1-z} \left[z - \frac{m_{\tilde{q}}}{z\tilde{a}^2} \right],$

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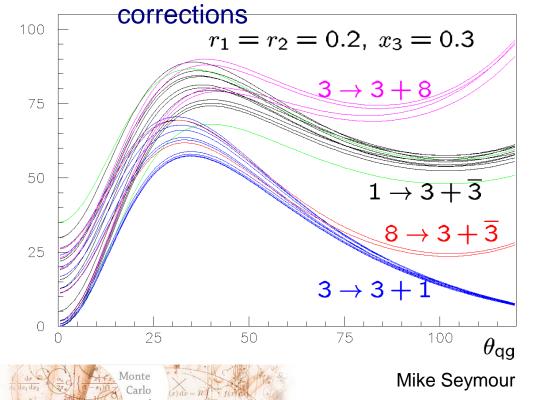


Heavy Quarks/Spartons

- Dead cone only exact for
- emission from spin-0 particle, or
- infinitely soft emitted gluon

colour	spin	γ_5	example
$1 \rightarrow 3 + \overline{3}$			(eikonal)
$1 \rightarrow 3 + \overline{3}$	$1 \rightarrow \frac{1}{2} + \frac{1}{2}$	$1,\gamma_5,1\pm\gamma_5$	$Z^0 \to q \overline{q}$
$3 \rightarrow 3 + 1$	$\frac{1}{2} \rightarrow \frac{1}{2} + 1$	$1,\gamma_5,1\pm\gamma_5$	$t \to bW^+$
$1 \rightarrow 3 + \overline{3}$	$0 \rightarrow \frac{1}{2} + \frac{1}{2}$	$1,\gamma_5,1\pm\gamma_5$	$H^0 \to q \overline{q}$
$3 \rightarrow 3 + 1$	$\frac{1}{2} \rightarrow \frac{1}{2} + 0$	$1,\gamma_5,1\pm\gamma_5$	$t\tobH^+$
$1 \rightarrow 3 + \overline{3}$	$1 \rightarrow 0 + 0$	1	$Z^0 \to \tilde{q} \overline{\tilde{q}}$
$3 \rightarrow 3 + 1$	$0 \rightarrow 0 + 1$	1	$\tilde{q}\to \tilde{q}'W^+$
$1 \rightarrow 3 + \overline{3}$	$0 \rightarrow 0 + 0$	1	$H^0 \to \tilde{q}\overline{\tilde{q}}$
$3 \rightarrow 3 + 1$	$0 \rightarrow 0 + 0$	1	$\tilde{q} \to \tilde{q}' H^+$
$1 \rightarrow 3 + \overline{3}$	$\frac{1}{2} \rightarrow \frac{1}{2} + 0$	$1,\gamma_5,1\pm\gamma_5$	$\chi ightarrow q \overline{\tilde{q}}$
$3 \rightarrow 3 + 1$	$0 \rightarrow \frac{1}{2} + \frac{1}{2}$	$1,\gamma_5,1\pm\gamma_5$	$\mathbf{\tilde{q}} ightarrow \mathbf{q} \chi$
$3 \rightarrow 3 + 1$	$\frac{1}{2} \rightarrow 0 + \frac{1}{2}$	$1,\gamma_5,1\pm\gamma_5$	$t \to \tilde{t} \chi$
$8 \rightarrow 3 + \overline{3}$	$\frac{1}{2} \rightarrow \frac{1}{2} + 0$	$1,\gamma_5,1\pm\gamma_5$	$\tilde{g} \to q \overline{\tilde{q}}$
$3 \rightarrow 3 + 8$	$0 \rightarrow \frac{1}{2} + \frac{1}{2}$	$1,\gamma_5,1\pm\gamma_5$	$\tilde{q} \to q \tilde{g}$
$3 \rightarrow 3 + 8$	$\frac{1}{2} \rightarrow 0 + \frac{1}{2}$	$1,\gamma_5,1\pm\gamma_5$	$t\to \tilde{t}\tilde{g}$

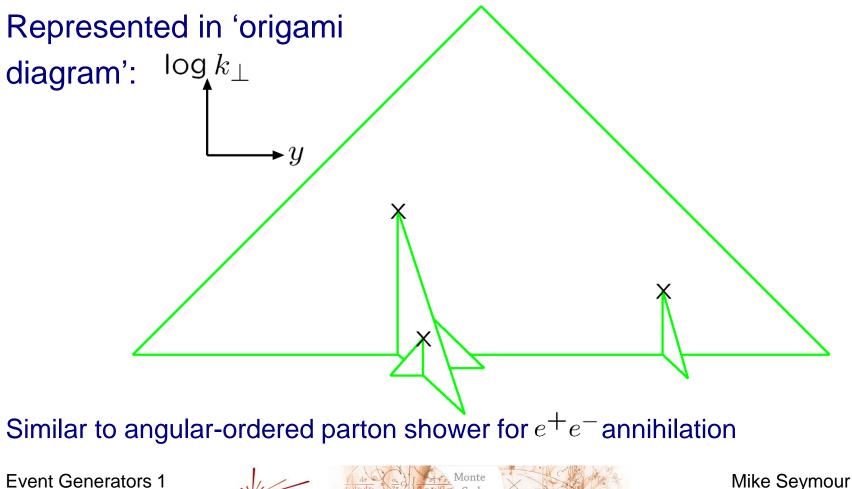
- In general, depends on
- energy of gluon
- colours and spins of emitting particle and colour partner
- → process-dependent mass



The Colour Dipole Model

Conventional parton showers: start from collinear limit, modify to incorporate soft gluon coherence Colour Dipole Model: start from soft limit Emission of soft gluons from colour-anticolour dipole universal (and classical): $d\sigma \approx \sigma_0 \frac{1}{2} C_A \frac{\alpha_s(k_\perp)}{2\pi} \frac{dk_\perp^2}{k_\perp^2} dy, \quad y = \text{rapidity} = \log \tan \theta/2$ After emitting a gluon, colour dipole is split: Event Generators 1 Mike Seymour

Subsequent dipoles continue to cascade c.f. parton shower: one parton \rightarrow two CDM: one dipole \rightarrow two = two partons \rightarrow three



Initial-state radiation in the CDM

There is none!

- Hadron remnant forms colour dipole with scattered quark.
- Treated like any other dipole.
- Except remnant is an extended object: suppression

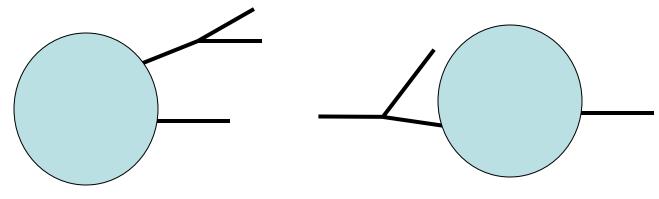
Biggest difference relative to angular-ordered \rightarrow more radiation at small x

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Dipole Cascades

- Most new implementations based on dipole picture:
 - Catani & MHS (1997)
 - Kosower (1998)
 - Nagy & Soper (May 2007)
 - Giele, Kosower & Skands (July 2007) VINCIA
 - Dinsdale, Ternick & Weinzierl (Sept 2007)
 - Schumann & Krauss (Sept 2007) SHERPA
 - Winter & Krauss (Dec 2007) SHERPA



Matrix Element Matching

Parton shower built on approximations to QCD matrix elements valid in **collinear** and **soft** approximations

 \rightarrow describe bulk of radiation well \rightarrow hadronic final state

 \rightarrow but ...

- searches for new physics
- top mass measurement
- *n* jet cross sections

• ...

- \rightarrow hard, well-separated jets
- described better by fixed ("leading") order matrix element
- would also like next-to-leading order normalization

→ need matrix element matching Event Generators 1

Older Programs, still sometimes seen

- PYTHIA 6.2: traditional q^2 ordering; veto of non-ordered final state emission; partial implementation of angular ordering in initial state; big range of hard processes.
- HERWIG 6: complete implementation of colour coherence; NLO evolution for large x; smaller range of hard processes.
- ARIADNE: complete implementation of colour dipole model; best fit to HERA data; interfaced to PYTHIA for hard processes.



Supported Programs

- PYTHIA 6.3: p_T-ordered parton showers, interleaved with multi-parton interactions; dipole-style recoil; matrix element for first emission in many processes.
- PYTHIA 8: new program with many of the same features as PYTHIA 6.3, many 'obsolete' features removed.
- SHERPA: new program built from scratch; p_T-ordered dipole showers; multi-jet matching scheme (CKKW) to AMAGIC++ built in.
- Herwig++: new program with similar parton shower to HERWIG (angular ordered) plus quasi-collinear limit and recoil strategy based on colour flow; spin correlations.

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Summary

- Accelerated colour charges radiate gluons.
 Gluons are also charged → cascade.
- Probabilistic language derived from factorization theorems of full gauge theory.
 Colour coherence is a fact of life: do not trust those who ignore it!
- Modern parton shower models are very sophisticated implementations of perturbative QCD, but would be useless without hadronization models...

