Floating-point control in the Intel C/C++ compiler and libraries or Why doesn't my application always give the same answer?

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Agenda

- Overview

- Floating-point (FP) Model
 - Comparisons with gcc
- Performance impact
- Runtime math libraries
- Intel[®] Xeon Phi[™] Coprocessors what's different



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Overview

- The finite precision of floating-point operations leads to an inherent uncertainty in the results of a floating-point computation
 - Results may vary within this uncertainty
- Nevertheless, may need reproducibility beyond this uncertainty
 - For reasons of Quality Assurance, e.g. when porting, optimizing, etc
- The right compiler options can deliver consistent, closely reproducible results whilst preserving good performance
 - Across IA-32, Intel[®] 64 and other IEEE-compliant platforms
 - Across optimization levels
 - -fp-model is the recommended high level control for the Intel Compiler



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Floating Point (FP) Programming Objectives

– Accuracy

Produce results that are "close" to the correct value

Measured in relative error, possibly in ulp

Reproducibility

- Produce consistent results
 - From one run to the next
 - From one set of build options to another
 - From one compiler to another
 - From one platform to another

Performance

Produce the most efficient code possible

These options usually conflict! Judicious use of compiler options lets you control the tradeoffs. Different compilers have different defaults.



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Floating Point Semantics

 The –fp-model (/fp:) switch lets you choose the floating point semantics at a coarse granularity. It lets you specify the compiler rules for:

Value safety

- FP expression evaluation
- FPU environment access
- Precise FP exceptions
- FP contractions

(fused multiply-add)

(main focus)

- Also pragmas in C99 standard
 - #pragma STDC FENV_ACCESS etc
- Old switches such as -mp now deprecated
 - Less consistent and incomplete; don't use





The –fp-model switch for icc

-fp-model

- fast [=1] allows value-unsafe optimizations (default)
- fast=2 allows additional approximations
- precise
 value-safe optimizations only
- source | double | extended imply "precise" unless overridden see "FP Expression Evaluation" for more detail
 except enable floating point exception semantics
 strict precise + except + disable fma + don't assume default floating-point environment
- Replaces old switches -mp, -fp-port, etc (don't use!)
- -fp-model precise -fp-model source
 - recommended for ANSI/ IEEE standards compliance, C++ & Fortran
 - "source" is default with "precise" on Intel 64 Linux



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GCC option

- -f[no-]fast-math is high level option
 - It is off by default (different from icc)
 - It is turned on by -Ofast
- Components control similar features:
 - Value safety (-funsafe-math-optimizations)
 - includes reassociation
 - Reproducibility of exceptions
 - Assumptions about floating-point environment
 - Assumptions about exceptional values
- also sets abrupt/gradual underflow (FTZ)
- For more detail, check backup or <u>http://gcc.gnu.org/wiki/FloatingPointMath</u>



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Value Safety

 In SAFE mode, the compiler may not make any transformations that could affect the result, e.g. all the following are prohibited.

x / x ⇔ 1.0	x could be 0.0, ∞ , or NaN
x – y ⇔ - (y – x)	If x equals y, $x - y$ is +0.0 while $-(y - x)$ is - 0.0
x – x ⇔ 0.0	x could be ∞ or NaN
x * 0.0 ⇔ 0.0	x could be -0.0, ∞, or NaN
x + 0.0 ⇔ x	x could be -0.0
$(x + y) + z \Leftrightarrow x + (y + z)$	General reassociation is not value safe
(x == x) ⇔ true	x could be NaN

- UNSAFE (fast) mode is the icc default
- VERY UNSAFE mode enables riskier transformations
 - (-fp-model fast=2)



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Value Safety

Affected Optimizations include:

- Reassociation
- Flush-to-zero
- Expression Evaluation, various mathematical simplifications
- Approximate divide and sqrt
- Math library approximations



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Reassociation

Addition & multiplication are "associative" (& distributive)

- a+b+c = (a+b) + c = a + (b+c)
- a*b + a*c = a * (b+c)
- These transformations are equivalent *mathematically*
 - but <u>not</u> in finite precision arithmetic
- Reassociation can be disabled in its entirety
 - \Rightarrow for standards conformance (C left-to-right)
 - Use -fp-model precise
 - May carry a significant performance penalty (other optimizations also disabled)
- Parentheses are respected only in value-safe mode!
 - -assume protect_parens compromise (Fortran only)
- See exercises for an example derived from a real app



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Example (see exercises)

"tiny" is intended to keep a[i]>0

but... optimizer hoists constant
 expression (c+tiny) out of loop
tiny gets "rounded away" wrt c

```
icc -O1 reassoc.cpp; ./a.out
a = 0 b = inf
icc -fp-model precise reassoc.cpp;./a.out
a = 1e-20 b = 1e+20
```

```
g++ reassoc.cpp; ./a.out

a = 1e-20 b = 1e+20

g++ -O3 -ffast-math reassoc.cpp; ./a.out

a = 0 b = inf
```

```
#include <iostream>
#define N 100
```

```
int main() {
  float a[N], b[N];
  float c = -1., tiny = 1.e-20F;
```

```
for (int i=0; i<N; i++) a[i]=1.0;
```

```
for (int i=0; i<N; i++) {
    a[i] = a[i] + c + tiny;
    b[i] = 1/a[i];
}
std::cout << "a = " << a[0] <<
" b = " << b[0] << "\n";</pre>
```



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}



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Denormalized numbers and Flush-to-Zero (FTZ)

- Denormals extend the (lower) range of IEEE floating-point values, at the cost of:
 - Reduced precision
 - Reduced performance (can be 100 X for ops with denormals)
- If your application creates but does not depend on denormal values, setting these to zero may improve performance ("abrupt underflow", or "flush-to-zero",)
 - Done in SSE or AVX hardware, so fast
 - Happens by default at -O1 or higher (for icc, not gcc)
 - -no-ftz or -fp-model precise will prevent
 - Must compile <u>main</u> with this switch to have an effect
 - fp-model precise –ftz to get "precise" without denormals
 - Not available for x87, denormals always generated
 - (unless trapped and set to zero in software very slow)
- For gcc, -ffast-math sets abrupt underflow (FTZ)
 - But -03 -ffast-math reverts to gradual underflow



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Reductions

- Parallel implementations imply reassociation (partial sums)
 - Not value safe, but can give substantial performance advantage
 - fp-model precise
 - disables vectorization of reductions
 - does not affect OpenMP* or MPI* reductions
 - These remain value-unsafe (programmer's responsibility)
- New features in Intel® Composer XE 2013

```
float Sum(const float A[], int n )
{
    float sum=0;
    for (int i=0; i<n; i++)
        sum = sum + A[i];
    return sum;
}</pre>
```

```
float Sum( const float A[], int n )
{
    int i, n4 = n-n%4;
    float sum=0, sum1=0, sum2=0, sum3=0;
    for (i=0; i<n4; i+=4) {
        sum = sum + A[i];
        sum1 = sum1 + A[i+1];
        sum2 = sum2 + A[i+2];
        sum3 = sum3 + A[i+3];
    }
    sum = sum + sum1 + sum2 + sum3;
    for (; i<n; i++) sum = sum + A[i];
        return sum; }
</pre>
```



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Reproducibility of Reductions in OpenMP*

- Each thread has its own partial sum
 - Breakdown, & hence results, depend on number of threads
 - Partial sums are summed at end of loop
 - Order of partial sums is undefined (OpenMP standard)
 - First come, first served
 - Result may vary from run to run (even for same # of threads)
 - For both gcc and icc
 - Can be more accurate than serial sum
 - For icc & ifort, option to define the order of partial sums (tree algorithm)
 - Makes results reproducible from run to run
 - export KMP_DETERMINISTIC_REDUCTION=yes (in 13.0)
 - May also help accuracy
 - Possible slight performance impact, depends on context
 - Requires static scheduling, fixed number of threads
 - Default for large numbers of threads



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FP Expression Evaluation

In the following expression, what if a, b, c, and d are mixed data types (single and double for example)
 a = (b + c) + d

Four possibilities for intermediate rounding, (corresponding to C99 FLT_EVAL_METHOD)

Indeterminate(-fp-model fast)Use precision specified in source(-fp-model source)Use double precision(C/C++ only)(-fp-model double)Use long double precision (C/C++ only)(-fp-model extended)

- Or platform-dependent default (-fp-model precise)
 - Defaults to -fp-model source on Intel64
 - Recommended for most purposes
- The expression evaluation method can significantly impact performance, accuracy, and portability



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The Floating Point Unit (FPU) Environment

– FP Control Word Settings

- Rounding mode (nearest, toward $+\infty$, toward $-\infty$, toward 0)
- Exception masks, status flags (inexact, underflow, overflow, divide by zero, denormal, invalid)
- Flush-to-zero (FTZ), Denormals-are-zero (DAZ)
- x87 precision control (single, double, extended) [don't mess!]
- Affected Optimizations, e.g.
 - Constant folding (evaluation at compile time)
 - FP speculation
 - Partial redundancy elimination
 - Common subexpression elimination
 - Dead code elimination
 - Conditional transform, e.g.

if (c) x = y; else x = z; $\rightarrow x = (c) ? y : z$;



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FPU Environment Access

- When access disabled (default):
 - compiler assumes default FPU environment
 - Round-to-nearest
 - All exceptions masked
 - No FTZ/DAZ
 - Compiler assumes program will NOT read status flags
- If user might change the default FPU environment, inform compiler by setting FPU environment access mode!!

or

- Access may only be enabled in value-safe modes, by:
 - fp-model strict
 - #pragma STDC FENV_ACCESS ON
- Compiler treats control settings as unknown
- Compiler preserves status flags
- Some optimizations are disabled
- If you forget this, you might get **completely** wrong results!
 - Eg from math functions, if you change default rounding mode





Precise FP Exceptions

- When Disabled (default):
 - Code may be reordered by optimization
 - FP exceptions might not occur in the "right" places
- When enabled by
 - -fp-model strict
 - -fp-model except
 - #pragma float_control(except, on)
 - The compiler must account for the possibility that any FP operation might throw an exception
 - Disables optimizations such as FP speculation
 - May only be enabled in value-safe modes
 - (more complicated for x87)
 - Does not unmask exceptions
 - Must do that separately, e.g.
 - -fp-trap=common for C
 - or functions calls such as feenableexcept()
 - -fpe0 or ieee_set_halting_mode() for Fortran





Example

double x., zero = 0.; feenableexcept (FE_DIVBYZERO); for(int i = 0; i < 20; i++) x = zero ? (1./zero) : zero;

Problem: F-P exception from (1./zero) despite explicit protection

- The invariant (1./zero) gets speculatively hoisted out of loop by optimizer, but the "?" alternative does not
- exception occurs before the protection can kick in
- NOTE: may not occur for AVX due to masked vector operations

Solution: Disable optimizations that lead to the premature exception

- icc –fp-model precise –fp-model except (or icc –fp-model strict) disables all optimizations that could affect FP exception semantics
- icc –fp-speculation safe disables just speculation where this could cause an exception
- #pragma float_control around the affected code block (see doc)



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Floating Point Contractions

- affects the generation of FMA instructions on Intel[®] MIC architecture and Intel[®] AVX2 (-xcore-avx2)
 - Enabled by default or -fma, disable with -no-fma
 - Disabled by –fp-model strict or C/C++ #pragma
 - NOT disabled by –fp-model precise
 - -[no-]fma switch overrides -fp-model setting
 - Intel compiler does NOT support 4-operand AMD*-specific fma instruction)
- When enabled:
- The compiler may generate FMA for combined multiply/add
 - Faster, more accurate calculations
 - Results may differ in last bit from separate multiply/add
- When disabled:
 - -fp-model strict, #pragma fp_contract(off) or -no-fma
 - The compiler must generate separate multiply/add with intermediate rounding





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Typical Performance Impact of -fp-model source

- Measured on SPECCPU2006fp benchmark suite:
- -02 or -03
- Geomean reduction due to
 -fp-model precise -fp-model source
 in range 12% 15%
- Intel Compiler XE 2011 (12.0)
- Measured on Intel Xeon[®] 5650 system with dual, 6-core processors at 2.67Ghz, 24GB memory, 12MB cache, SLES* 10 x64 SP2

Use -fp-model source (/fp:source) to improve floating point reproducibility whilst limiting performance impact



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Math Library Functions

- Different implementations may not have the same accuracy
 - On Intel 64:
 - libsvml for vectorized loops
 - libimf (libm) elsewhere
 - Processor-dependent code within libraries, selected at runtime
 - Inlining was important for Itanium, to get software pipelining, but less important for Intel 64 since can vectorize with libsvml
 - Used for some division and square root implementations
- No official standard (yet) dictates accuracy or how results should be rounded (except for division & sqrt)
- -fp-model precise helps generate consistent math calls
 - eg within loops, between kernel & prolog/epilog
 - Remove or reduce dependency on alignment
 - May prevent vectorization unless use -fast-transcendentals
 - When may differ from non-vectorized loop



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New math library features (12.x compiler)

- Select minimum precision
 - Currently for libsvml (vector); scalar libimf normally "high"
 - -fimf-precision=<high|medium|low>
 - Default is off (compiler chooses)
 - Typically high for scalar code, medium for vector code
 - "low" typically halves the number of mantissa bits
 - Potential performance improvement
 - "high" ~0.55 ulp; "medium" < 4 ulp (typically 2)</p>
- -fimf-arch-consistency=<true | false>
 - Will produce consistent results on all microarchitectures or processors within the same architecture
 - Run-time performance may decrease
 - Default is false (even with -fp-model precise !)



Math Libraries – potential issues

- Differences could potentially arise between:
 - Different compiler releases, due to algorithm improvements
 - Use -fimf-precision
 - another workaround, use later RTL with both compilers
 - Different platforms, due to different algorithms or different code paths at runtime
 - Libraries detect run-time processor internally
 - Independent of compiler switches
 - use -fimf-arch-consistency=true
 - Expected accuracy is maintained
 - 0.55 ulp for libimf
 - < 4 ulp for libsvml (default for vectorized loops)</p>
- Adherence to an eventual standard for math functions would improve consistency but at a cost in performance.



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Intel® Math Kernel Library

- Linear algebra, FFTs, sparse solvers, statistical, ...
 - Highly optimized, vectorized
 - Threaded internally using OpenMP*
 - By default, repeated runs may not give identical results
- Conditional BitWise Reproducibility (new)
 - Repeated runs give identical results under certain conditions:
 - Same number of threads
 - OMP_SCHEDULE=static (the default)
 - Same OS and architecture (e.g. Intel 64)
 - Same microarchitecture, or specify a minimum microarchitecture
 - Consistent data alignment
 - Call mkl_cbwr_set(MKL_CBWR_COMPATIBLE)
 - Or set environment variable MKL_CBWR_BRANCH="COMPATIBLE"
 - In Intel® Composer XE 2013





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Intel® Threading Building Blocks

- A C++ template library for parallelism
 - Dynamic scheduling of user-defined tasks
 - Supports parallel_reduce() pattern
 - Repeated runs may not give identical results
- "Community preview" feature for reproducibility:
 - parallel_deterministic_reduce()
 - In Intel® Composer XE 2013
 - Repeated runs give identical results provided the usersupplied body yields consistent results
 - Independent of the number of threads
 - Simple partitioner always breaks up work in the same way
 - But results may differ from a serial reduction
 - May be some impact on performance



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Floating-Point Behavior on the Intel[®] Xeon Phi[™] Coprocessor

- Floating-point exception flags are set by KCi vector instructions
 - the flags can be read
 - unmasking and trapping is not supported.
 - attempts to unmask will result in seg fault
 - -fpe0 (Fortran) and -fp-trap (C) are disabled
 - fp-model except or strict will yield (slow!) x87 code that supports unmasking and trapping of floating-point exceptions
- Denormals are supported by KCi (but slow, like host)
 - Needs -no-ftz or -fp-model precise (like host)
- 512 bit vector transcendental math functions available (SVML)
 - Division and square root implementations still settling down
 - Both SVML and fast inlined divide and sqrt sequences available
 - Many options to select different implementations
 - See <u>Differences in floating-point arithmetic between Intel(R) Xeon</u> processors and the Intel Xeon Phi(TM) coprocessor for details and status





Comparing Floating-Point Results between Intel[®] Xeon processors and the Intel[®] Xeon Phi[™] Coprocessor

- Different architectures expect some differences
 - Different optimizations
 - Use of fused multiply-add (FMA)
 - Different implementations of math functions
- To minimize differences (e.g. for debugging)
 - Build with -fp-model precise (both architectures)
 - Build with -no-fma (Intel® MIC architecture)
 - Select high accuracy math functions
 - (e.g. -fimf-precision=high; default with -fp-model precise)
 - Choose reproducible parallel reductions (slides 15 & 28)
 - Or run sequentially, if you have the patience...
 - Remember, the true uncertainty of your result is probably much greater!





Further Information

- Microsoft Visual C++* Floating-Point Optimization http://msdn2.microsoft.com/enus/library/aa289157(vs.71).aspx
- The Intel® C++ and Fortran Compiler Documentation, "Floating Point Operations"
- "Consistency of Floating-Point Results using the Intel® Compiler" <u>http://software.intel.com/en-</u> <u>us/articles/consistency-of-floating-point-results-using-the-</u> <u>intel-compiler/</u>
- "Differences in Floating-Point Arithmetic between Intel® Xeon® Processors and the Intel® Xeon Phi[™] Coprocessor" <u>http://software.intel.com/sites/default/files/article/326703/flo</u> <u>ating-point-differences-sept11.pdf</u>
- Goldberg, David: "What Every Computer Scientist Should Know About Floating-Point Arithmetic" Computing Surveys, March 1991, pg. 203



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Quick Overview of Primary Switches

Primary Switches	Description	
/fp:keyword	<pre>fast[=1 2], precise, source, double, extended,</pre>	
-fp-model <i>keyword</i>	except, strict Controls floating point semantics	
/Qftz[-] -[no-]ftz	Flushes denormal results to Zero	
Some Other switches		
/Qfp-speculation keyword -fp-speculation keyword	<i>fast,</i> safe, strict, off floating point speculation control	
/Qprec-div[-] -[no-]prec-div	Improves precision of floating point divides	
/Qprec-sqrt[-] -[no-]prec-sqrt	Improves precision of square root calculations	
/Qfma[-] -[no-]fma	Enable[Disable] use of fma instructions	
/Qfp-trap:fp-trap=common	Unmask floating point exceptions (C/C++ only)	
/fpe:0 -fpe0	Unmask floating point exceptions (Fortran only)	
/Qfp-port -fp-port	Round floating point results to user precision	
/Qprec -mp1	More consistent comparisons & transcendentals	
/Op[-] -mp [-nofltconsistency]	Deprecated; use /fp:source etc instead	





Floating-point representations

Parameter	Single	Double	Quad or Extended Precision (IEEE_X)*
Format width in bits	32	64	128
Sign width in bits	1	1	1
mantissa	23 (24 implied)	52 (53 implied)	112 (113 implied)
Exponent width in bits	8	11	15
Max binary exponent	+127	+1023	+16383
Min binary exponent	- 126	- 1022	-16382
Exponent bias	+127	+1023	+16383
Max value	~3.4 x 10 ³⁸	~1.8 x 10 ⁻³⁰⁸	~1.2 x 10 ⁻⁴⁹³²
Value (Min normalized)	~1.2 x 10 ⁻³⁸	~2.2 x 10 ⁻³⁰⁸	~3.4 x 10 ⁻⁴⁹³²
Value (Min denormalized)	~1.4 x 10 ⁻⁴⁵	~4.9 x 10 ⁻³²⁴	~6.5 x 10 ⁻⁴⁹⁶⁶



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Special FP number representations

Single precision representations

	1 Sign bit	8 Exponent bits	(1)+23 Significand bits
zero	0 or 1	0	0
denormalized	0 or 1	0	(0.)xxxxx
normalized	0 or 1	1-254	(1.)xxxxx
infinity	0 or 1	255	0
Signalling NaN (SNaN)	No meaning	255	(1.)0xxxx
Quiet Nan (QNaN)	No Meaning	255	(1.)1xxxx



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Flush-To-Zero and Denormal FP Values

- A *normalized* FP number has leading binary bit and an exponent in the range accommodated by number of bits in the exponent.
- example:

```
0.171865_{10} = 1/8 + 1/32 + 1/64= 0.001011_2
```

normalized = $1.011_2 \times 2^{-3}$

- Exponent is stored in 8 bits single or 11 bits double: mantissa in 23 bits single, 52 bits double
- exponent biased by 127 (single precision)
- leading sign bit normalized "1." bit implied, not physically stored (1.011 stored as 011)

0 01111100 0110000000000000000000000



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Flush-To-Zero and Denormal FP Values

- What happens if the number is close to zero BUT exponent X in the 2^{-x} won't fit in 8 or 11 bits?
- 2⁻¹²⁸ for example in single precision
- Cannot represent in a NORMALIZED fashion:
- 1/2¹²⁷ = 0.00...001₂ (126 zeros after the binary point and a binary 1)
- = $1.0_2 \times 2^{-128}$
- But -128 won't fit in a 127 biased 8-bit exponent value!
- Solution: DENORMAL representation
- Exponent is -126 (all zeros), NO implied leading 1.
- 0 0000000 10000000000000000000000



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Flush-To-Zero and Denormal FP Values

- "Underflow" is when a very small number is created that cannot be represented. "gradual underflow" is when values are created that can be represented as denormal
- Denormals do not include as many significant digits
- Gradual loss of precision as denormal values get closer to zero
- OK, fine, I like these denormal numbers, they carry some precision why are denormals an issue?
 - UNFORTUNATELY denormals can cause 100x loss of performance
- Solution: set any denormal to zero: FLUSH TO ZERO
 - Keeps performance up, tradeoff is some loss of precision and dynamic range



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-prec-div and -prec-sqrt Options

- Both override the –fp-model settings
- Default is -no-prec-sqrt, and somewhere between -prec-div and -no-prec-div

[-no]-prec-div /Qprec-div[-]

- Enables[disables] various divide optimizations
 - x / y ⇔ x * (1.0 / y)
 - Approximate divide and reciprocal

[-no]-prec-sqrt /Qprec-sqrt[-]

Enables[disables] approximate sqrt and reciprocal sqrt



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-[no-]fast-transcendentals

- The compiler frequently optimizes calls of math library functions (like exp, sinf) in loops
- Uses SVML (short vector math library) to vectorize loops
- Uses the XMM direct call routines,

e.g. exp \rightarrow ____libm_sse2_exp (IA-32 only)

May sometimes use fast in-lined implementations

This switch "-[no]fast-transcendental can be used to override default behavior

 Behavior related to settings of fp-model and other switches – see reference manual !!



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gcc options

- -ffast-math implies
 - -fno-math-errno
 - -funsafe-math-optimizations
 - ffinite-math-only
 - fno-rounding-math
 - fno-signaling-nans
 - fcx-limited-range
 - & sets ___FAST_MATH___
- -funsafe-math-optimizations implies
 - fno-signed-zeros
 - -fassociative-math
 - fno-trapping-math
 - freciprocal-math
 - & sets abrupt underflow





Math Functions on the Intel[®] Xeon Phi[™] Coprocessor

- Faster, more approximate versions of math functions can still be obtained with –fp-model precise by adding
 - -fast-transcendentals -no-prec-div -no-prec-sqrt
 - See <u>Differences in floating-point arithmetic between Intel(R) Xeon</u> processors and the Intel Xeon Phi(TM) coprocessor for details and status
- Switches for finer control of math function accuracy:
 - -fimf-precision=<high|medium|low> [:func1,func2,...]
 - fimf-max-error
 - fimf-accuracy-bits
 - fimf-absolute-error
 - -fimf-domain-exclusion



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Math Functions on the Intel[®] Xeon Phi[™] Coprocessor

- Math functions have special branches and code to handle "exceptional" arguments
 - Faster versions possible if this can be skipped
- -fimf-domain-exclusion= <value>; the bits of <value> indicate domains for which the compiler need not generate special code
 - 1 extreme values (close to singularities or infinities; denormals)
 - 2 NaNs
 - 4 infinities
 - 8 denormals
 - 16 zeros
 - E.g. -fimf-domain-exclusion=31 excludes all of these for all functions
- Can be restricted to specific functions, e.g.
 - fimf-domain-exclusion=15:/sqrt,sqrtf gives fast, inlined versions of single & double precision square root
- -fp-model-fast=2 implies -fimf-domain-exclusion=15



