

# High power adaptive mirror

Development of adaptive mirrors for intra-cavity laser applications

Karsten Schuhmann

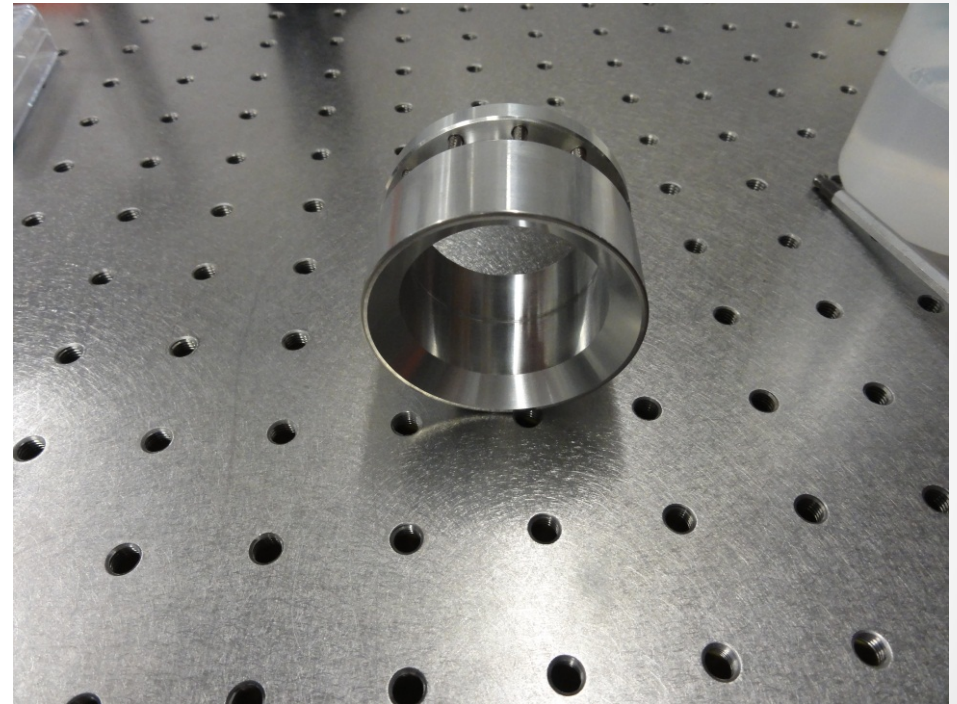
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# Overview

- Motivation (muonic hydrogen Lamb shift)
- Disk laser
- Thermal lens problem
- Adaptive glass mirror
- Results
- Outlook



# Proton radius puzzle



- Spectroscopy of  $\mu p$
- 2S-2P transition frequency depends on the proton radius (R)
- CODATA:  $R=0.8775$  (51) fm
- Our result:  $R=0.84184$  (67) fm
- $7\sigma$  discrepancy

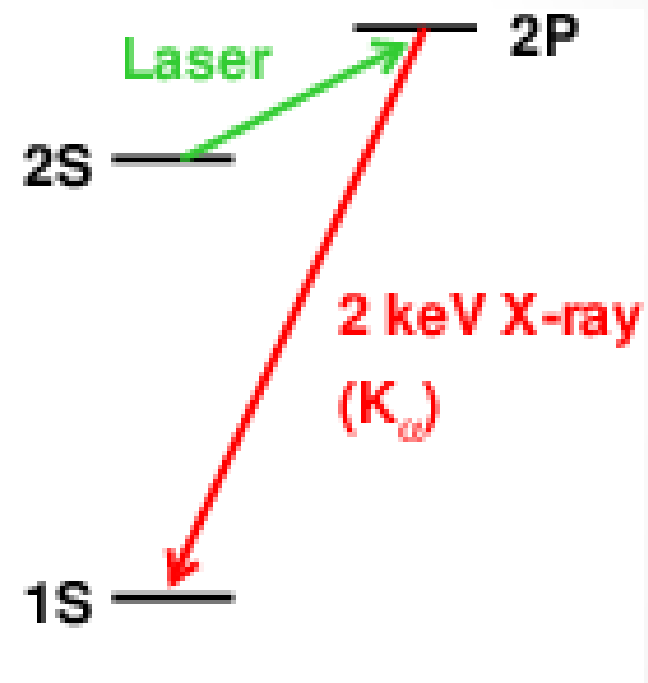
# Laser spectroscopy of $\mu p$

- Measure  $\Delta E^{\text{exp}}(2S-2P)$
- Compare with theoretical prediction:

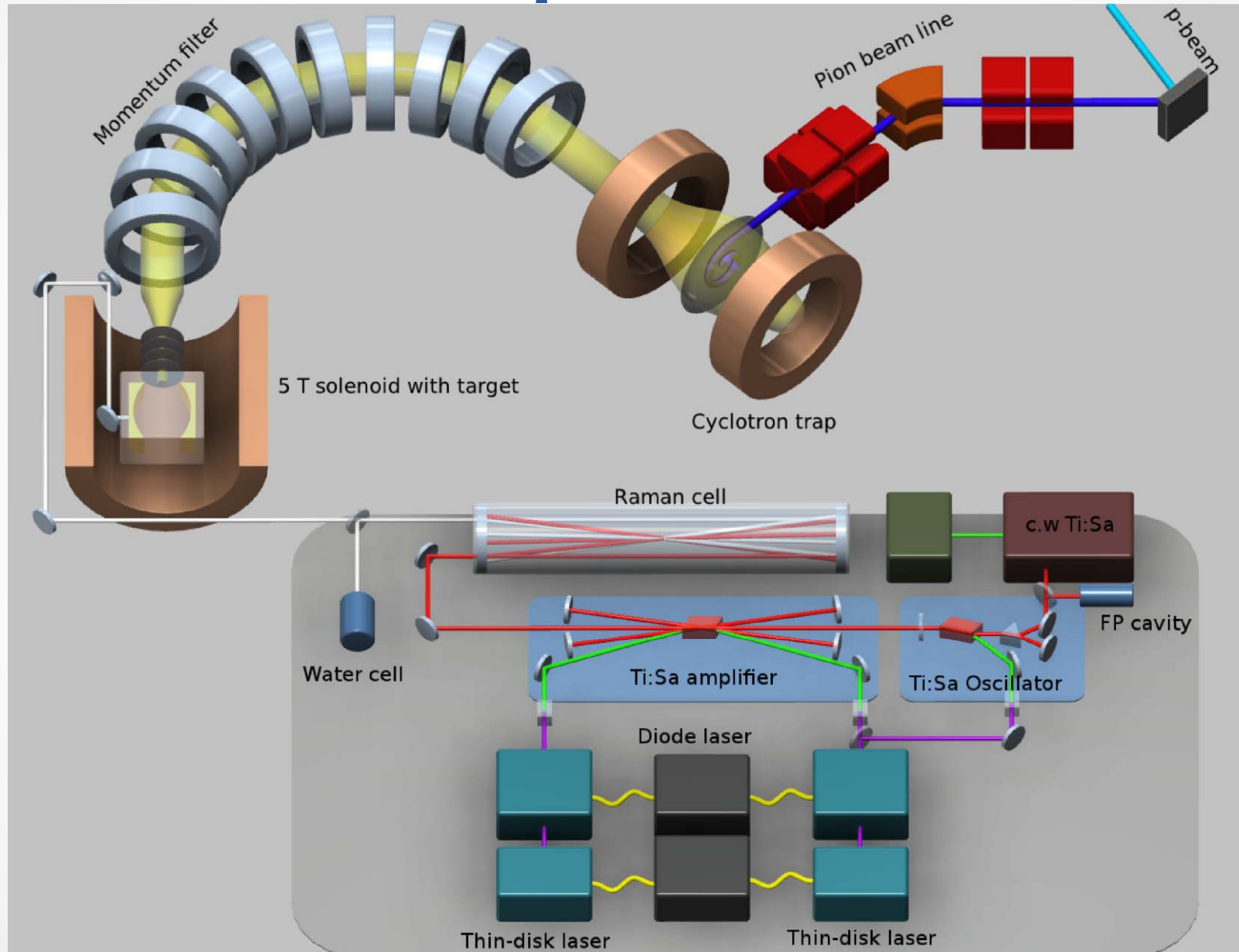
$$\begin{aligned}\Delta E^{\text{th}}(2S-2P) &= 209.9779(49) \\ &+ 5.2262 \cdot R^2 \\ &+ 0.0347 \cdot R^3\end{aligned}$$

- Units are in [meV] and [fm]

- Extract proton radius



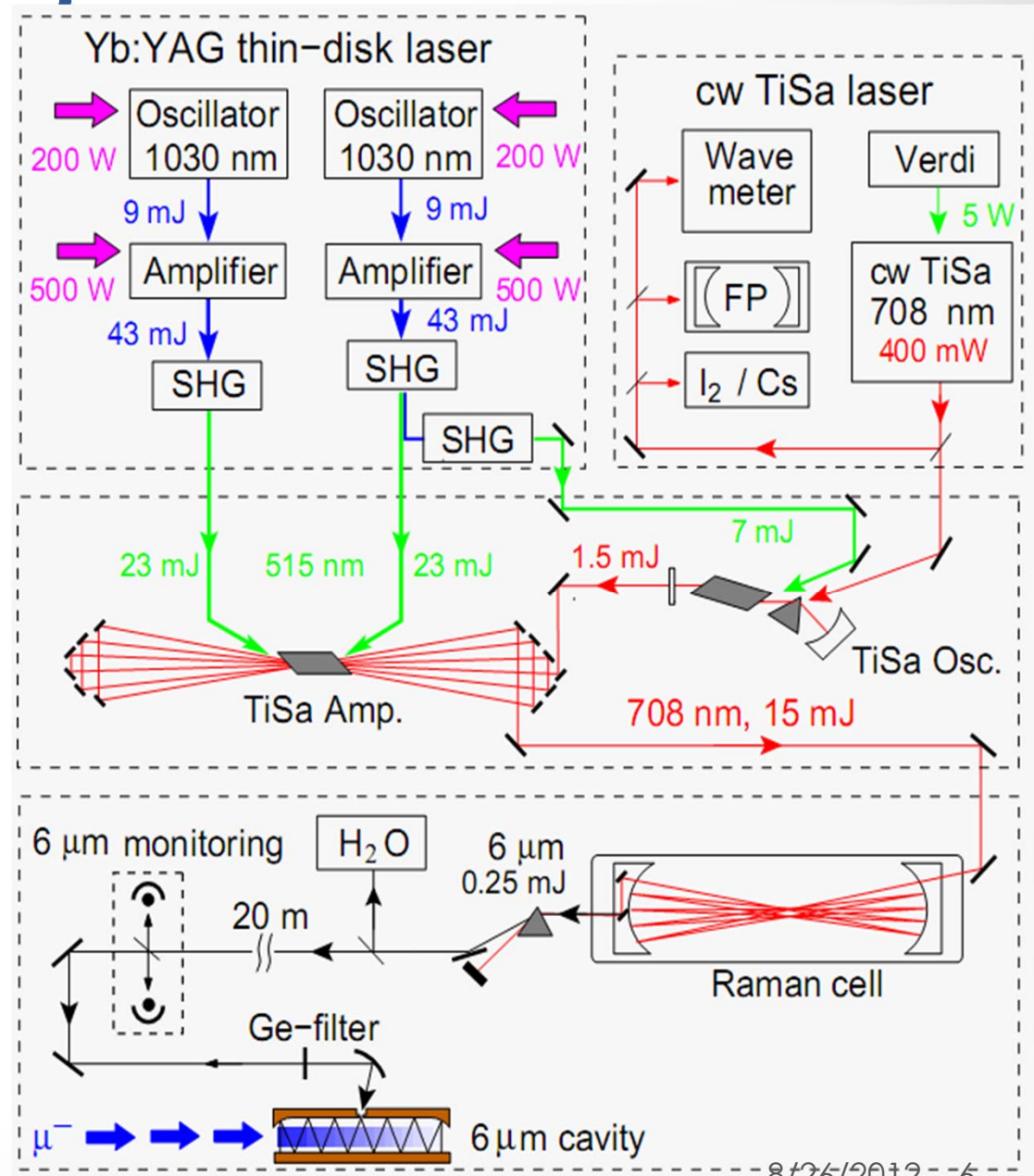
# Setup at PSI



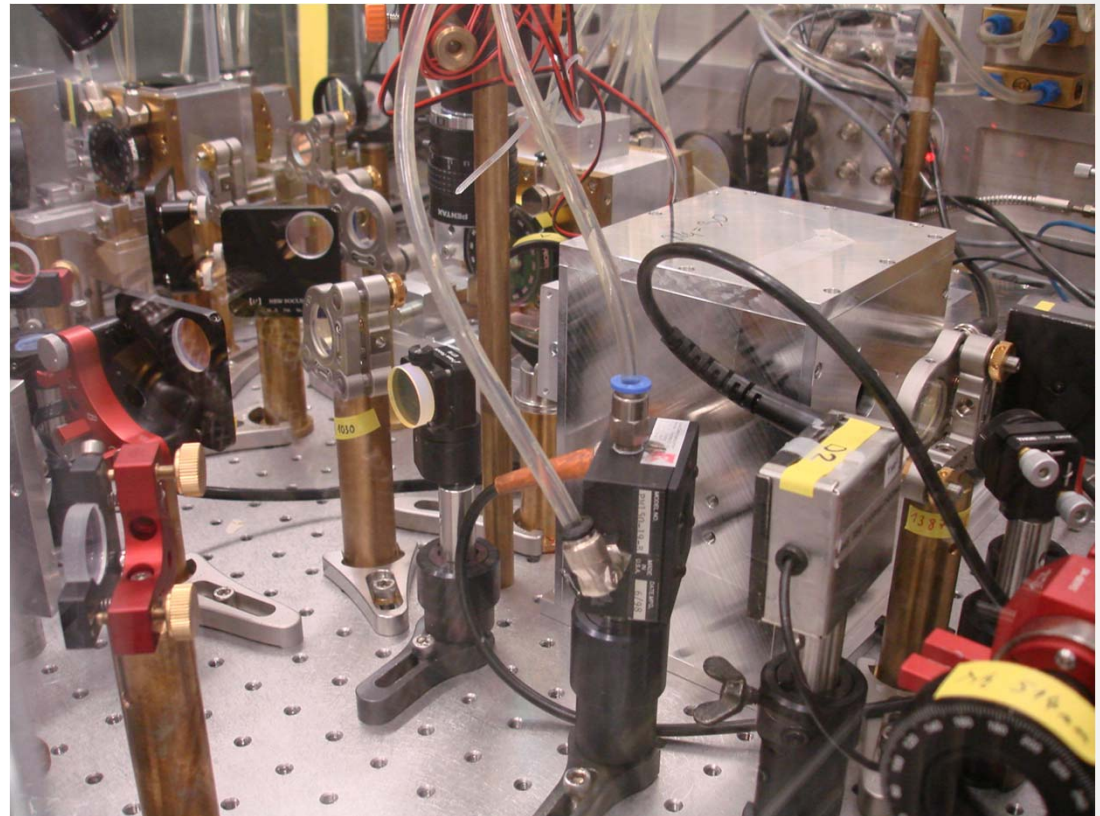
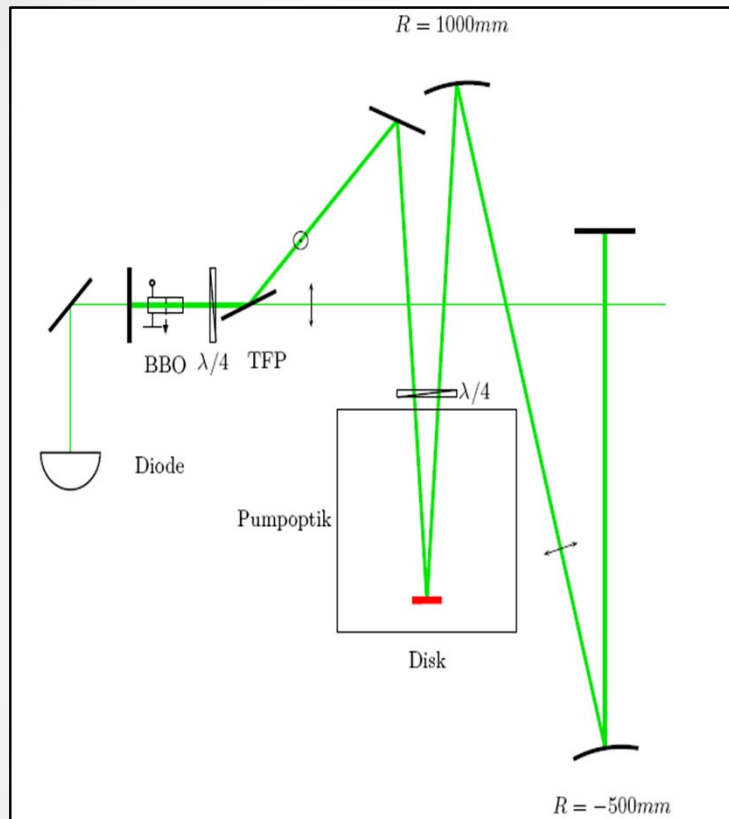


# Laser for $\mu\text{p}$ Lamb shift

- Stochastic trigger
- 0-1200 Hz rep. rate
- 400 ns latency
- 80 mJ @ 1030 nm



# “Old” disk laser oscillator



$E_{\text{max}} = 15 \text{ mJ}$   
Latency = 200 ns

Beside other Improvements we want to use the adaptive mirror to improve this setup.

# Disk laser principle

- Crystal has the form of an extremely short rod
- Large surface
- Efficient cooling
- HR- and AR-coating

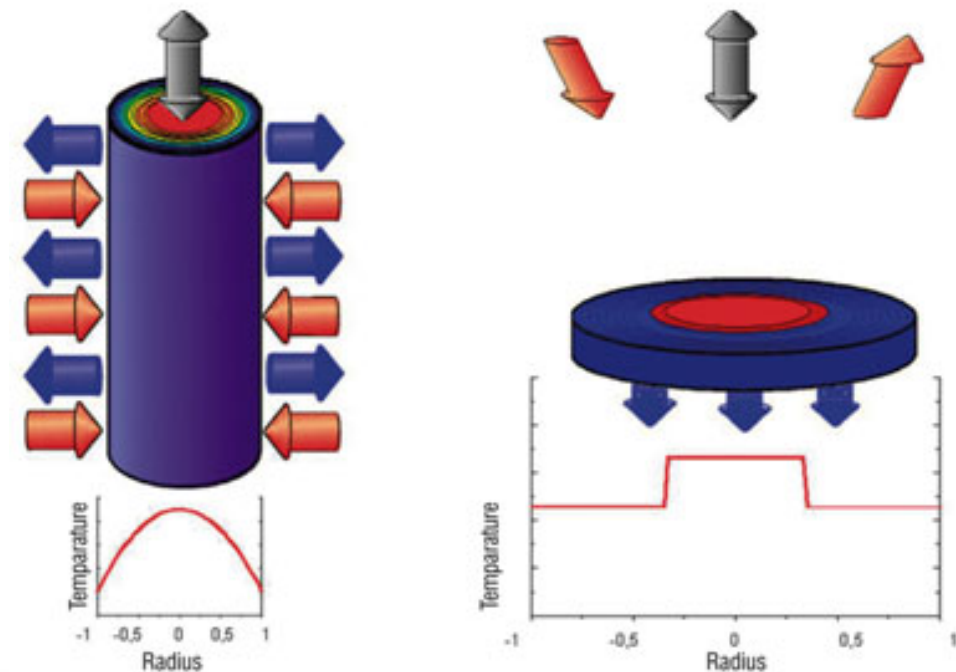
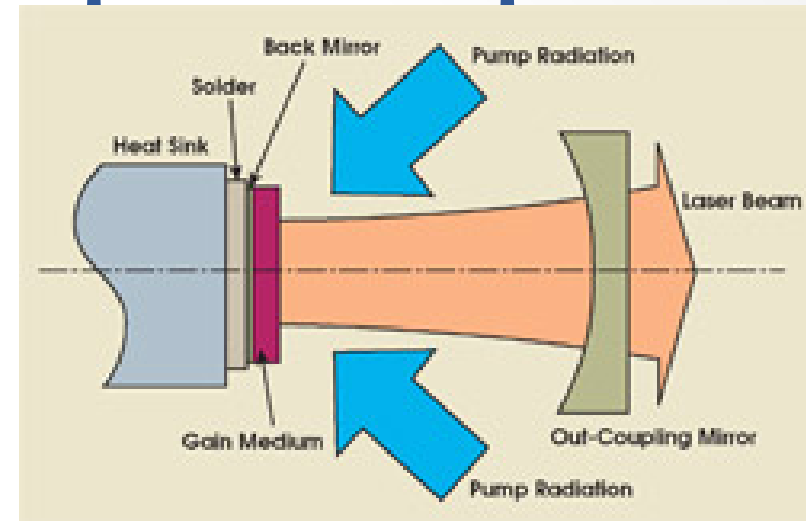
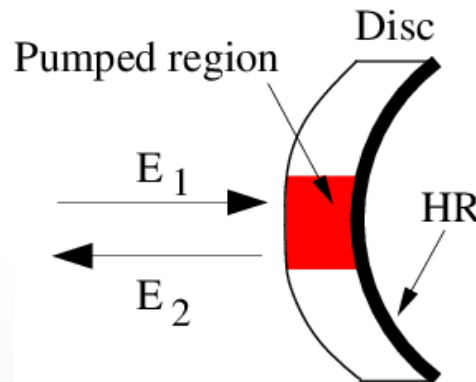
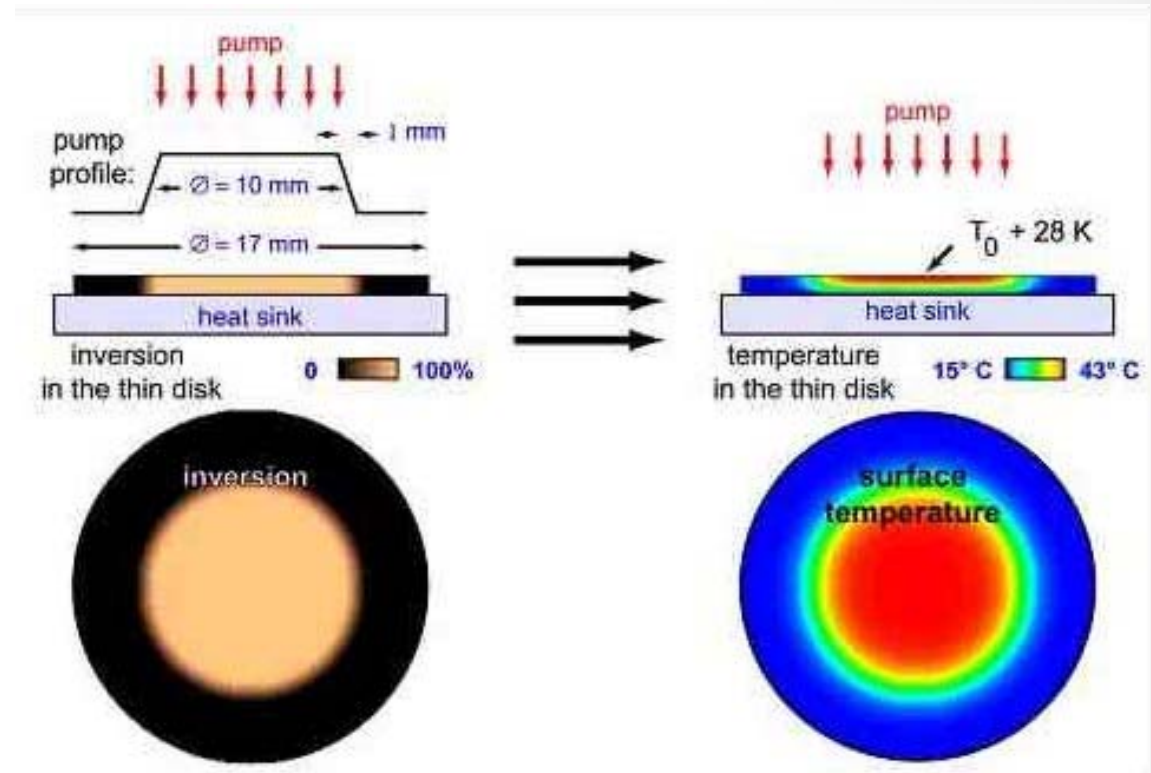


Figure 1



# Thermal lens of disk

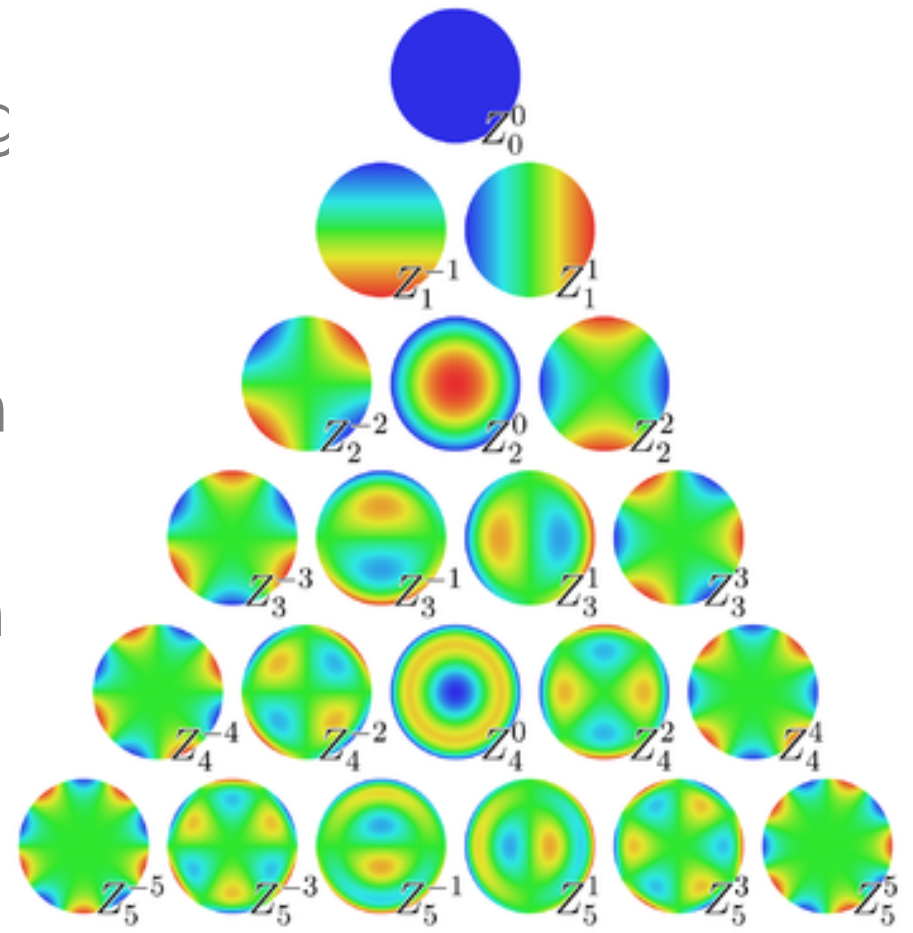
- Thermal expansion
- Thermal change of refractive index  $dn/dT$
- Inversion dependent change of refractive index
- Bending of substrate



$$OPD(x, y) = d(x, y) * n(x, y)$$

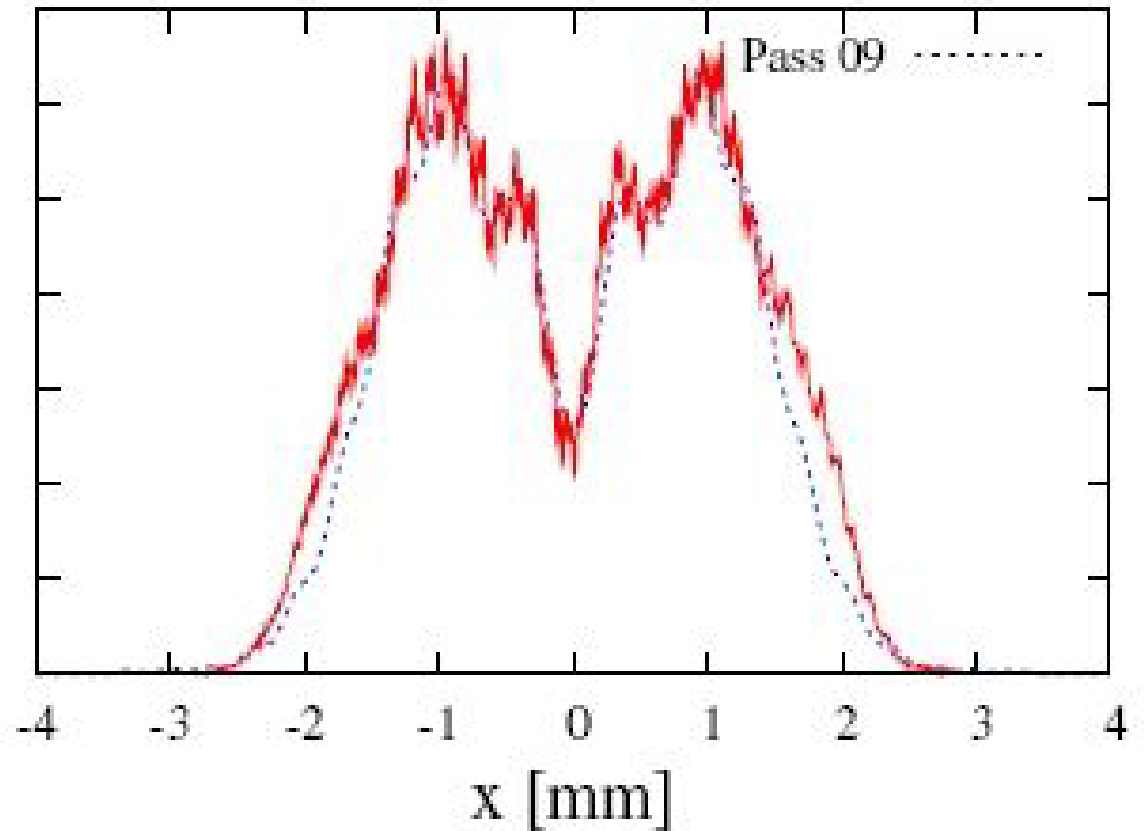
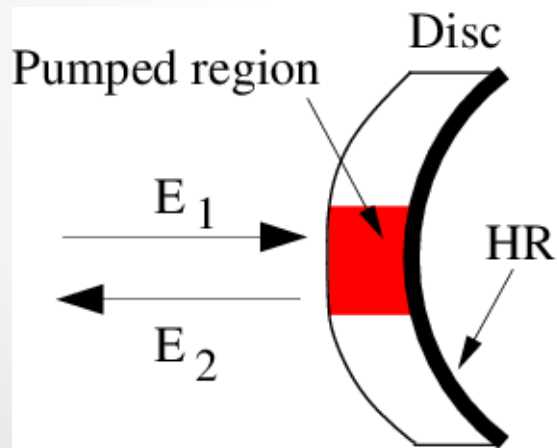
# Description of thermal lenses

- The thermal lens is optical phase difference (OPD)
- It can be described using the Zernike polynomials
- For ideal alignment only symmetrical deformation occur
  - Spherical deformation
  - Higher order deformation

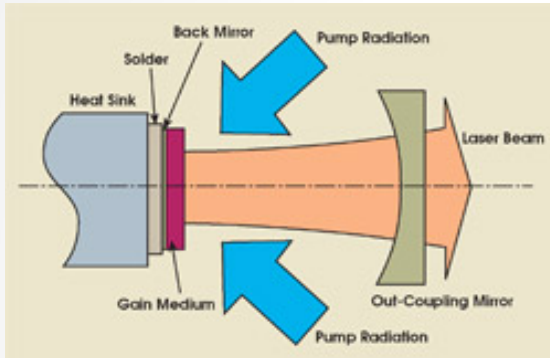


# Aspherical deformation of disk

A Gaussian beam reflected on an aspherical disk acquires high order components

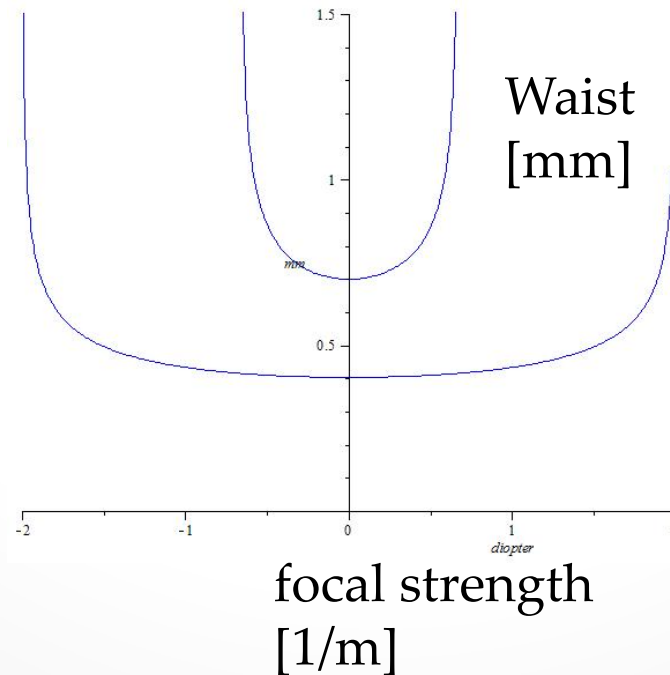
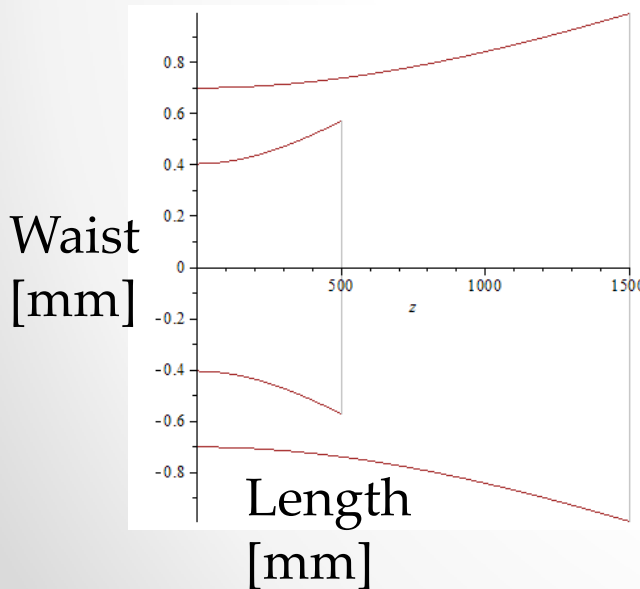


# Resonator stability vs. waist (pulse energy)



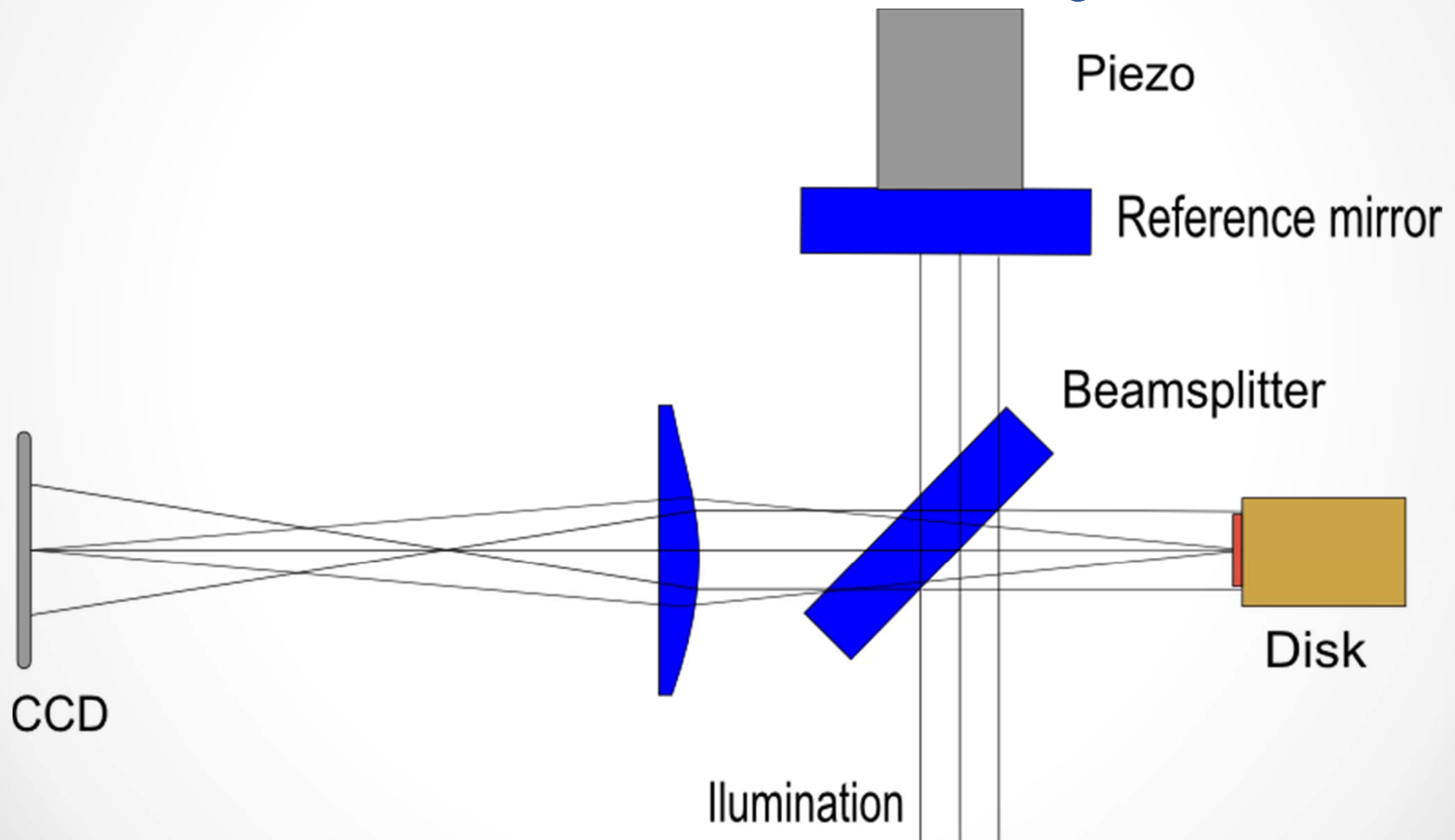
Comparison of two resonators with:  
 $w=0.4$  mm  
 $w=0.7$  mm

$$\Delta V \sim \frac{1}{w^2}$$



- The stability range  $\Delta V$  can be shifted changing laser layout (mirror curvatures and distances).
- But the width of this range depends only on wavelength and waist.

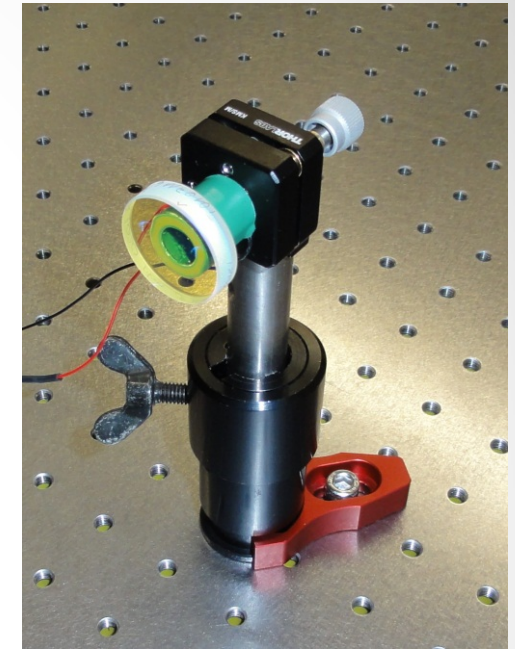
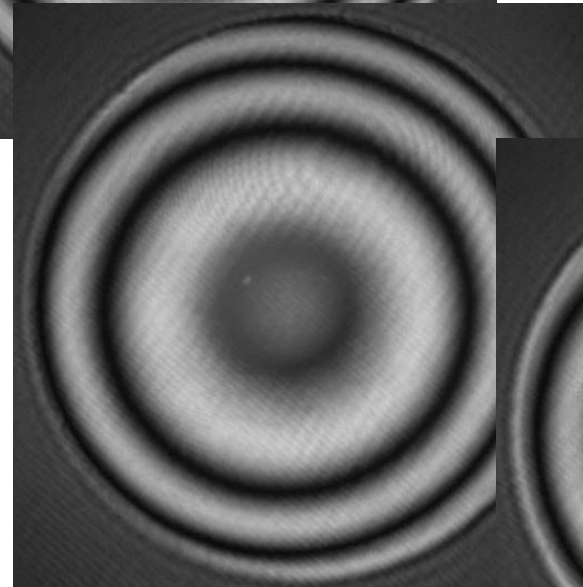
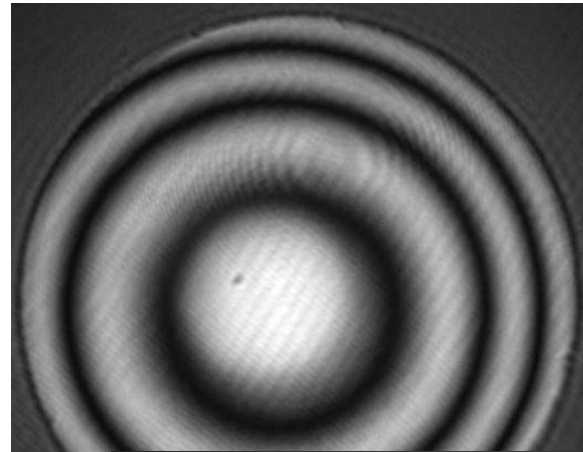
# Interferometry





# In situ measurement

- Measurement of optical phase deformation (OPD) of laser disk during operation
- We developed an interferometer for in situ measurements
- Record multiple pictures with shifted reference mirror (phase shift measurement)



# Unfolded OPD

- We developed a software to evaluate interferograms
- Phase shift analysis of N pictures
- Phase unwrapping

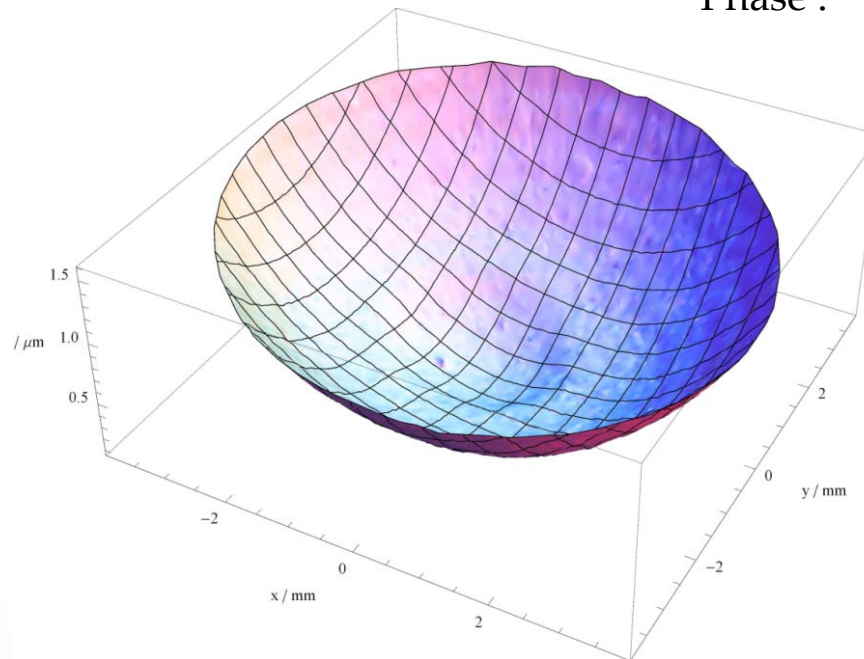
Example for N=3

$$Phase = \arctan \left( \frac{\begin{pmatrix} \sin(\alpha_1) \\ \sin(\alpha_2) \\ \sin(\alpha_3) \end{pmatrix} \times \begin{pmatrix} A_1 \\ A_2 \\ A_3 \end{pmatrix}}{\begin{pmatrix} \cos(\alpha_1) \\ \cos(\alpha_2) \\ \cos(\alpha_3) \end{pmatrix} \times \begin{pmatrix} A_1 \\ A_2 \\ A_3 \end{pmatrix}} \right)$$


$\alpha_{1..N}$ : Global phases of the various pictures

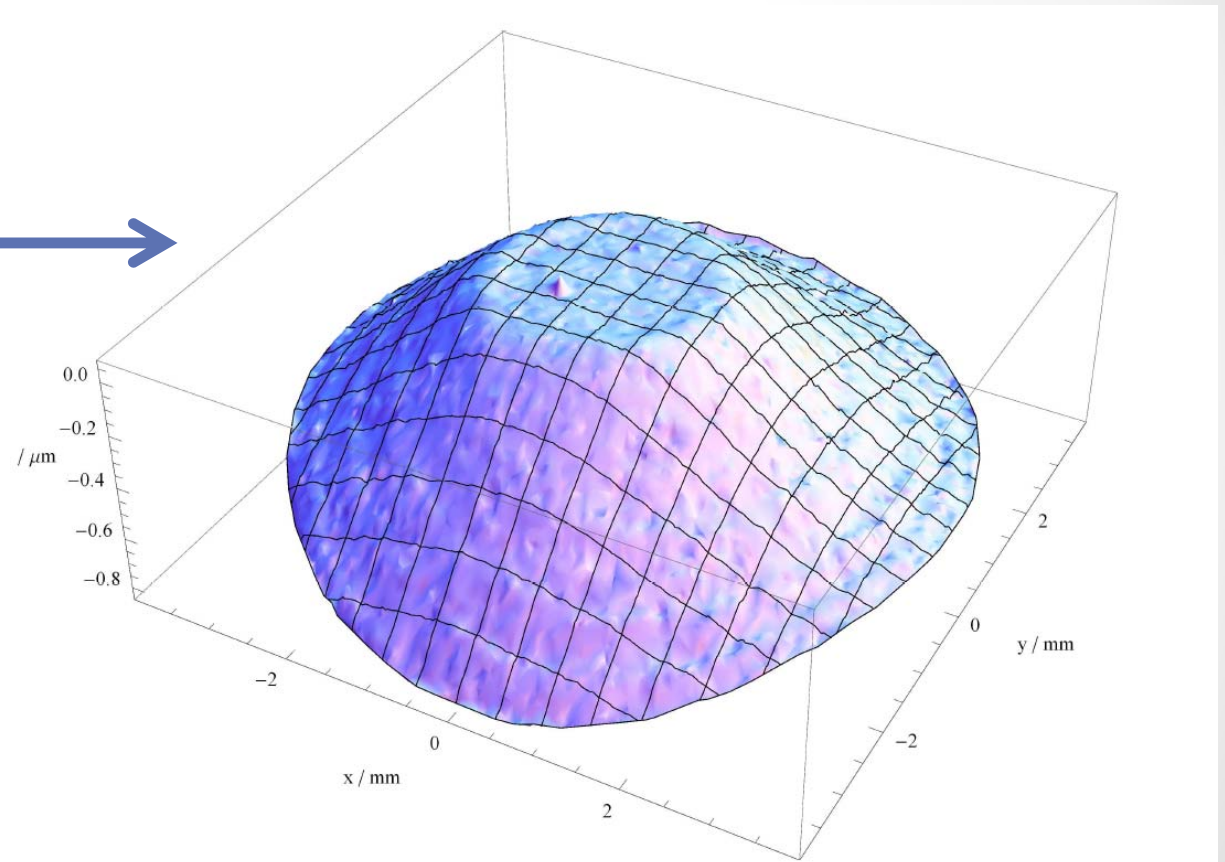
$A_{1..N}$ : Intensity of a pixel of the various pictures

Phase: Phase of pixel



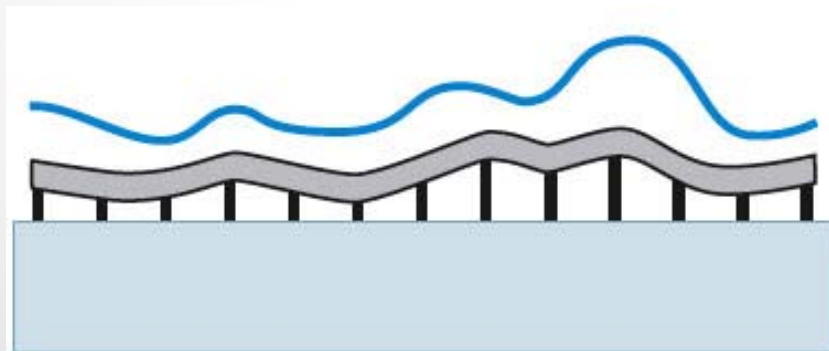
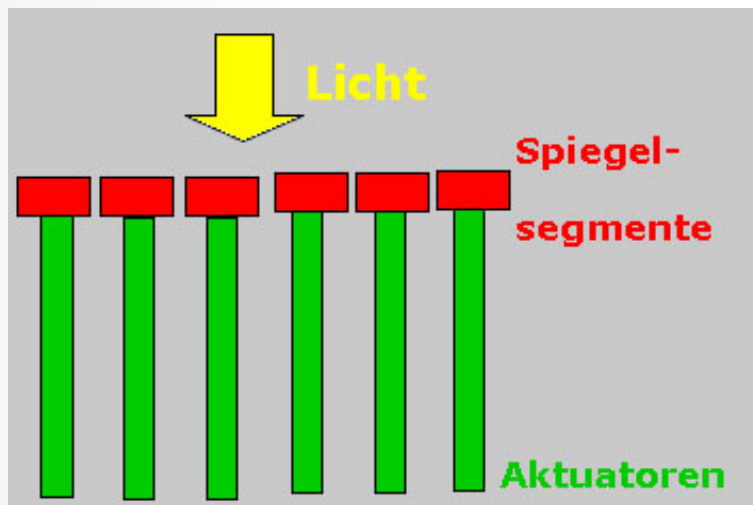
# OPD with subtracted spherical lens

- Fit parabola to OPD within the pump spot
- Get the remnant 
- Mainly bending of substrate
- Within the pump spot the aspherical deformations are negligible

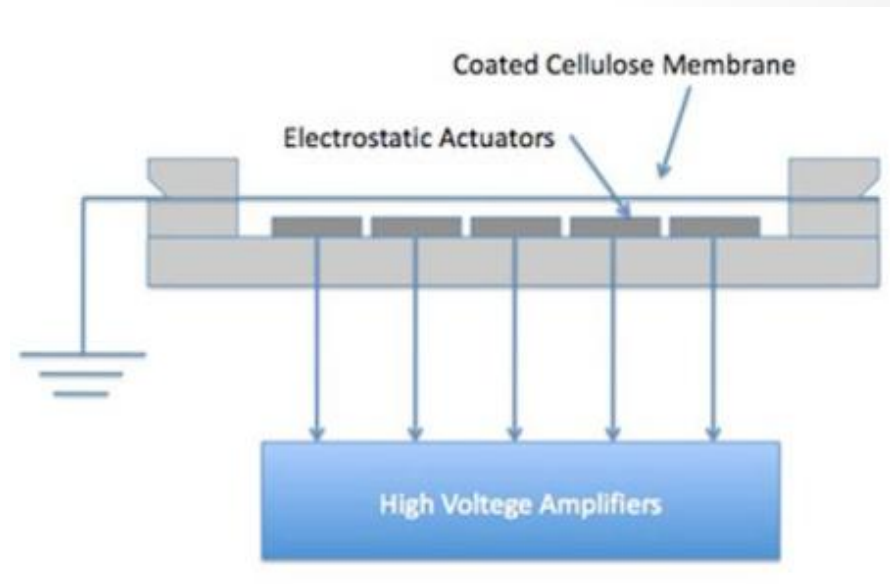
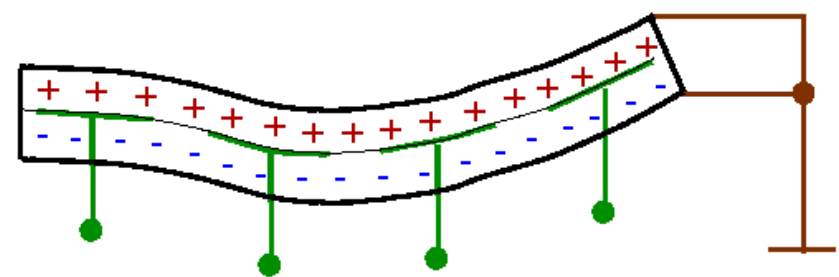


# Bending mirrors in astronomy

Mirror with discrete actuators



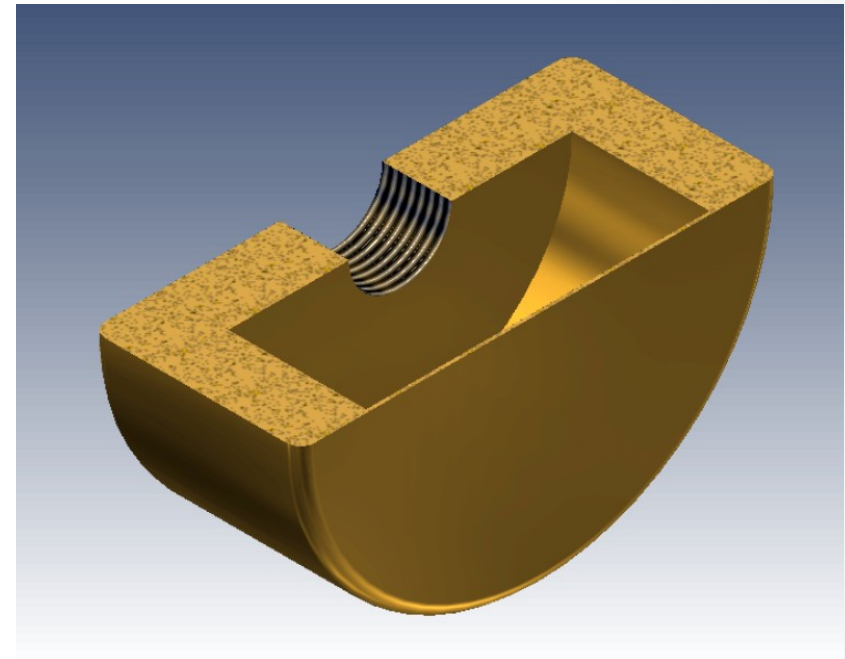
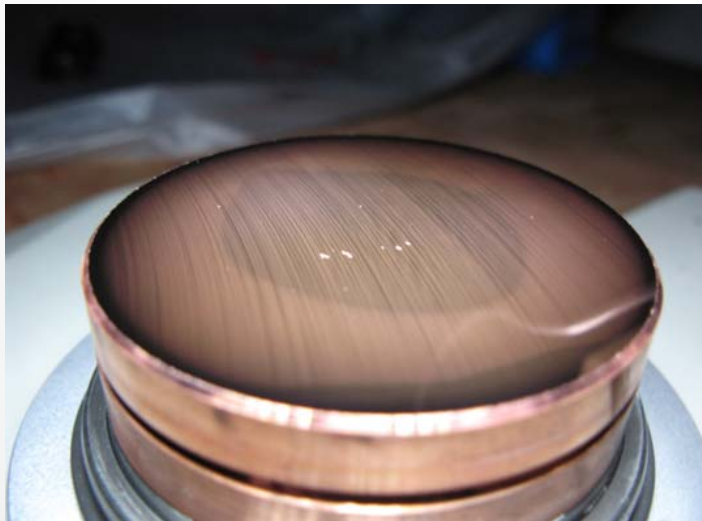
Full surface electrostatic adaptive mirrors





# Pressure driven metallic membrane

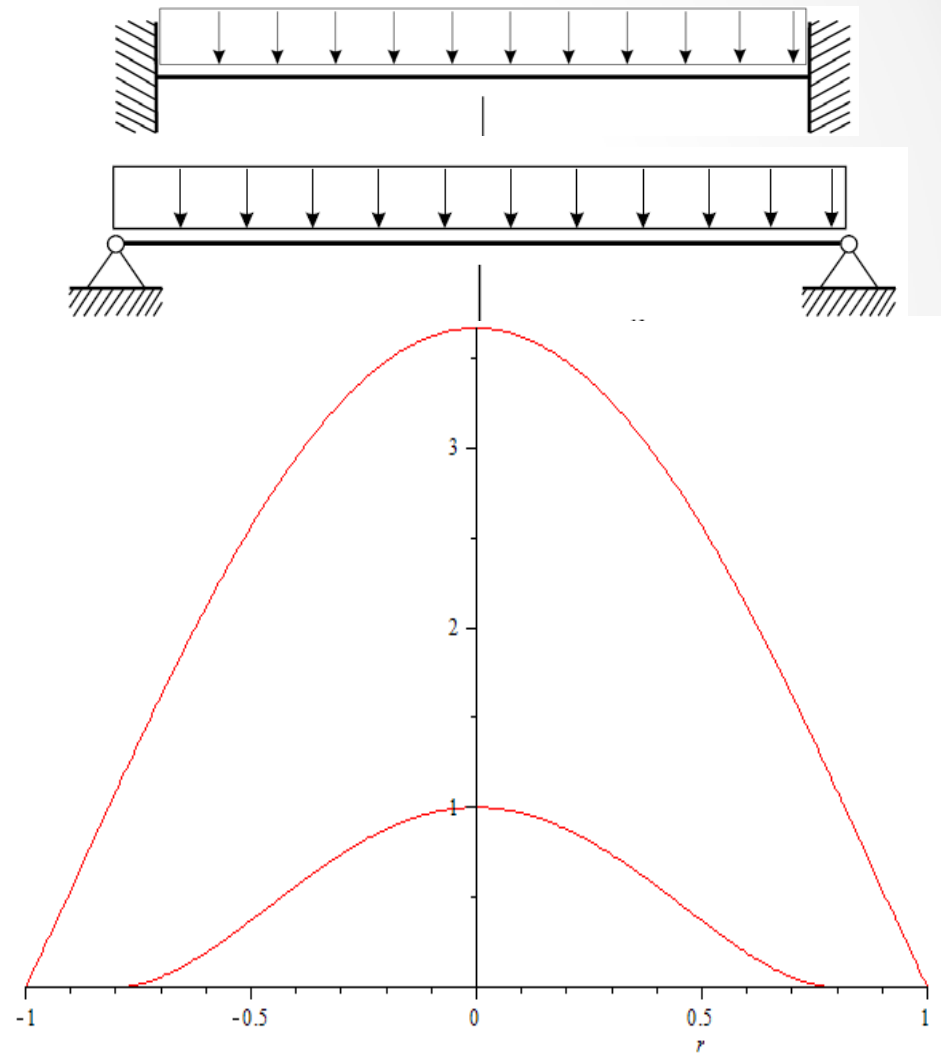
- 0.25 % scattering loss
- 80 kW/cm<sup>2</sup> damage threshold



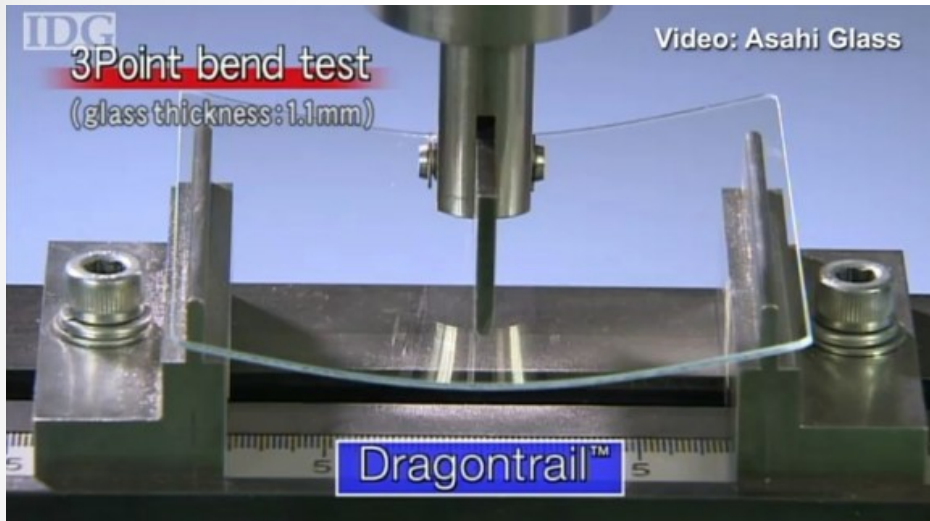


# Deformation

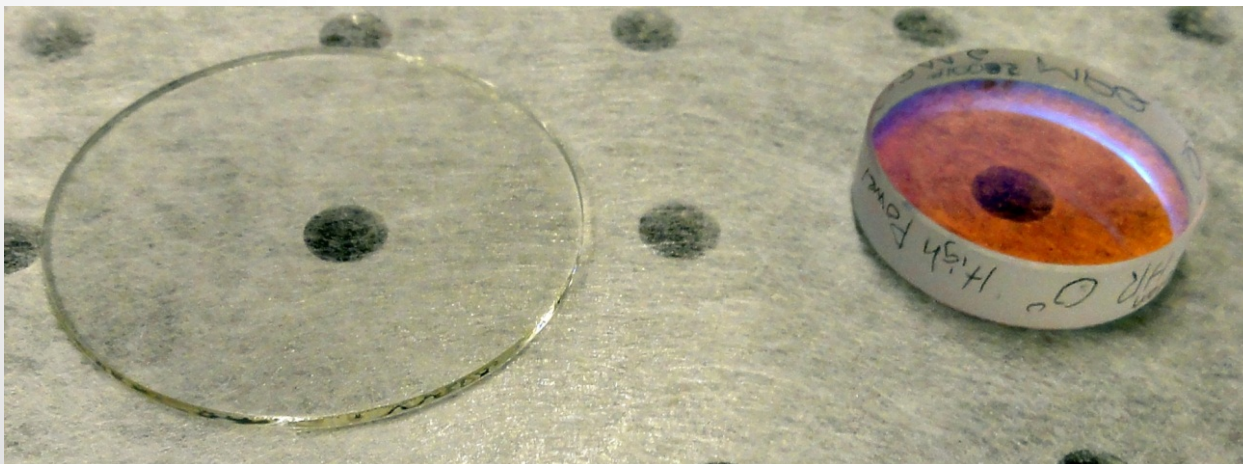
- Solutions of dgl. are well known
  - Clamped substrate  
 $w \sim 1 - 2 \cdot r^2 + r^4$
  - Flexible mounting  
 $w \sim 5 - 6 \cdot r^2 + r^4$
- Thick substrate with homogeneous properties
- Homogeneous pressure



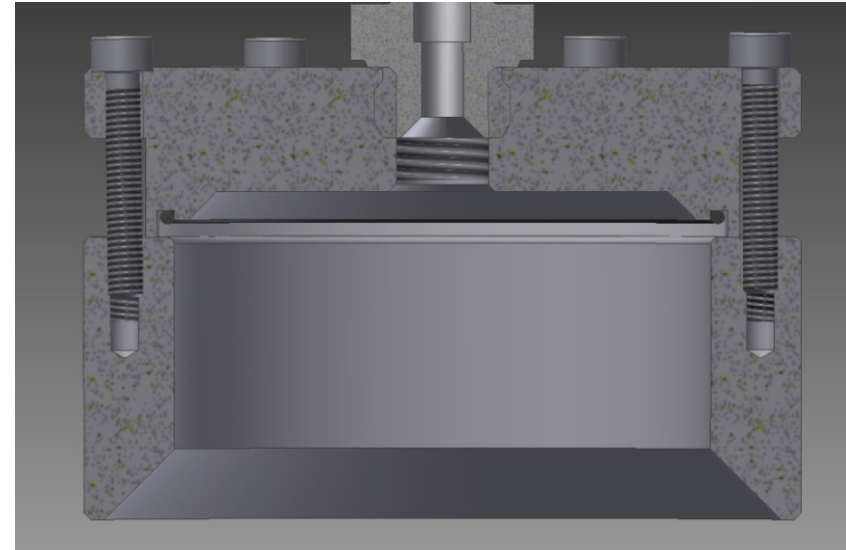
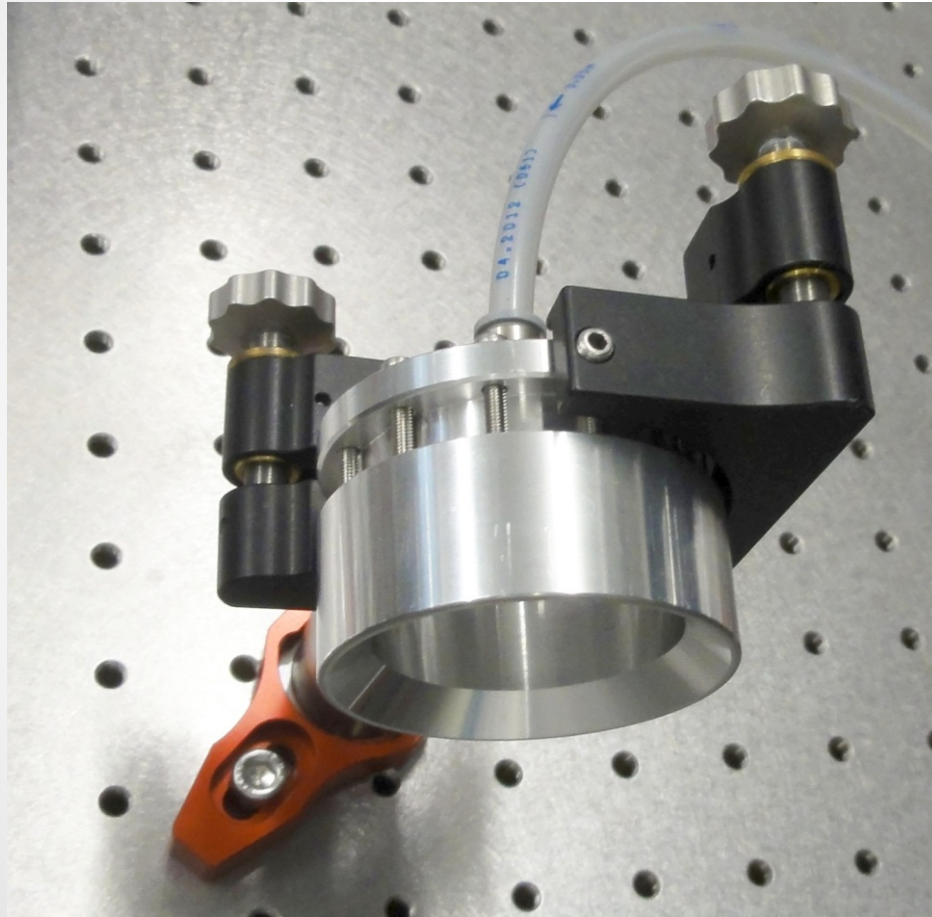
# Benefit of glass membrane



- Very low surface roughness (scattering loss  $\leq 0,01 \%$ )
- Damage thresholds up to  $100 \text{ MW/cm}^2$  (1000 times larger than on a metallic substrate)



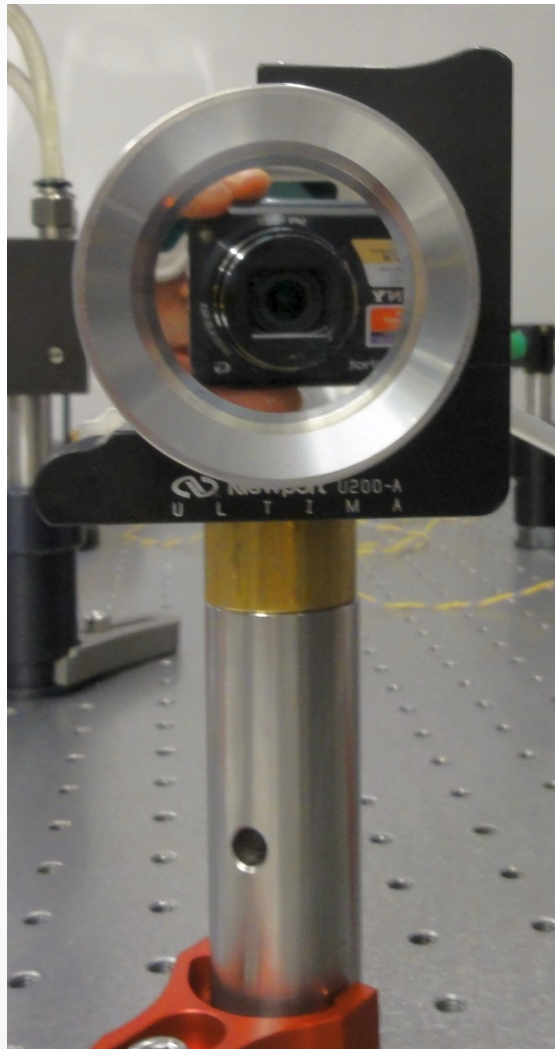
# Our deformable mirror



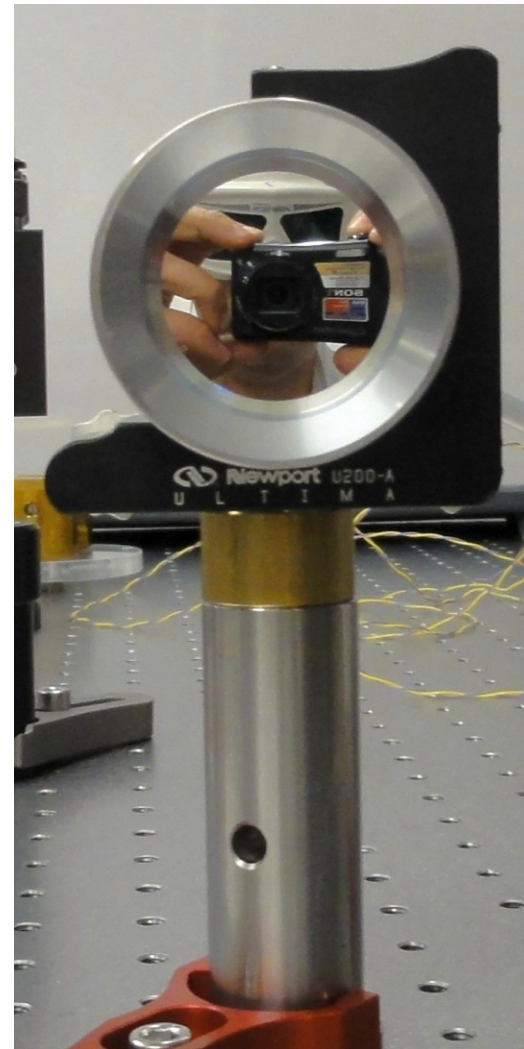
- Driven with pressurized air
- Glass substrate



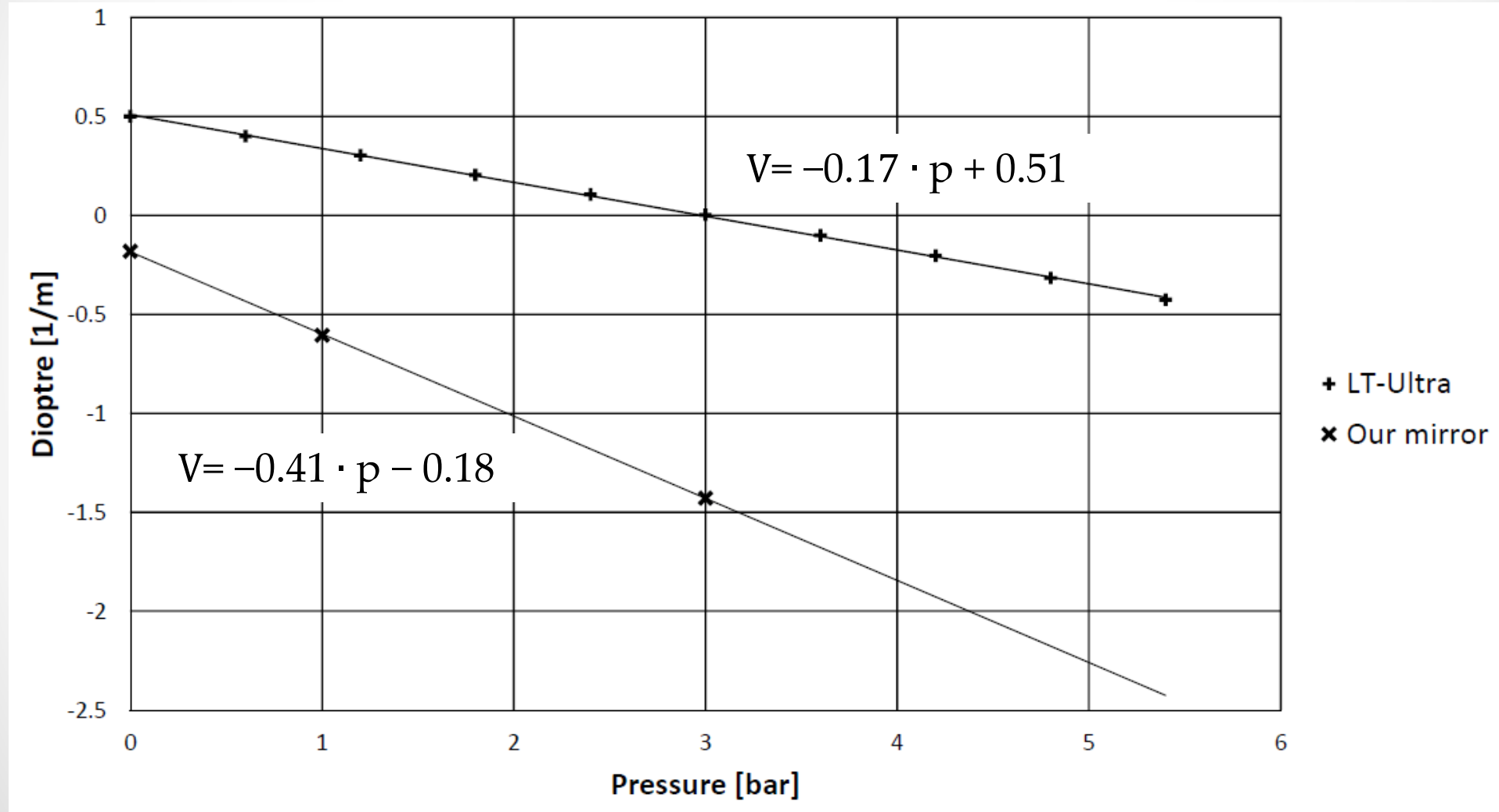
0 bar



6 bar



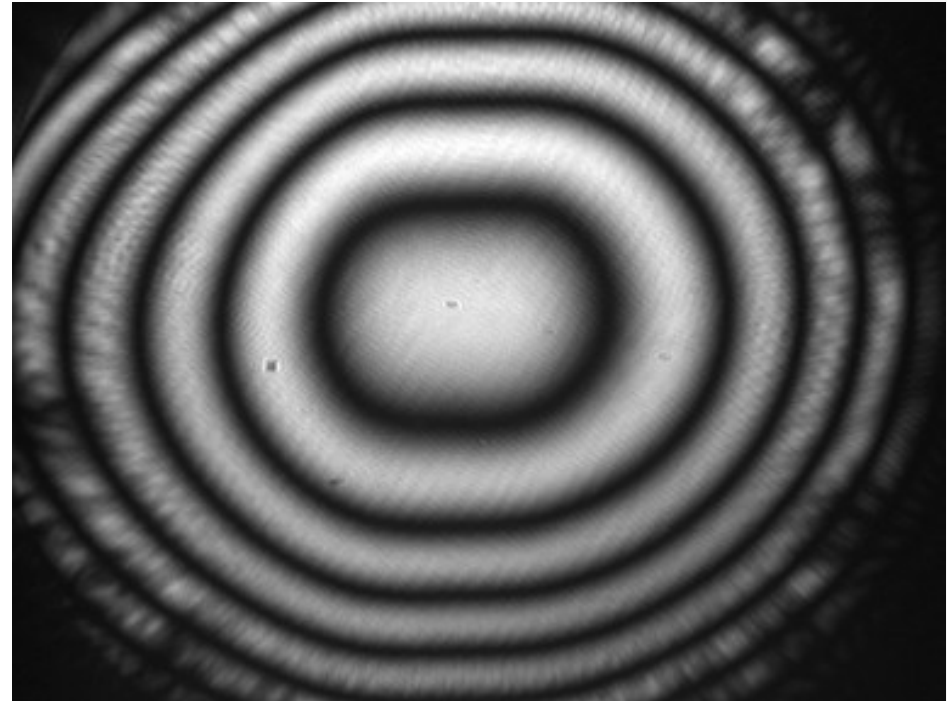
# Measured adaptive range





# Future improvements

- Improve surface quality
- Apply HR-coating
- Intra-cavity test
- Measurement of adaptive mirror OPD in laser operation



# Outlook

- Implement adaptive mirror in disk laser oscillator for upcoming Lamb shift measurement in muonic helium ion.
- Improve laser stability.
- Increase pulse energy from a single oscillator to 100 mJ.

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