

# Results on angular correlations with ALICE

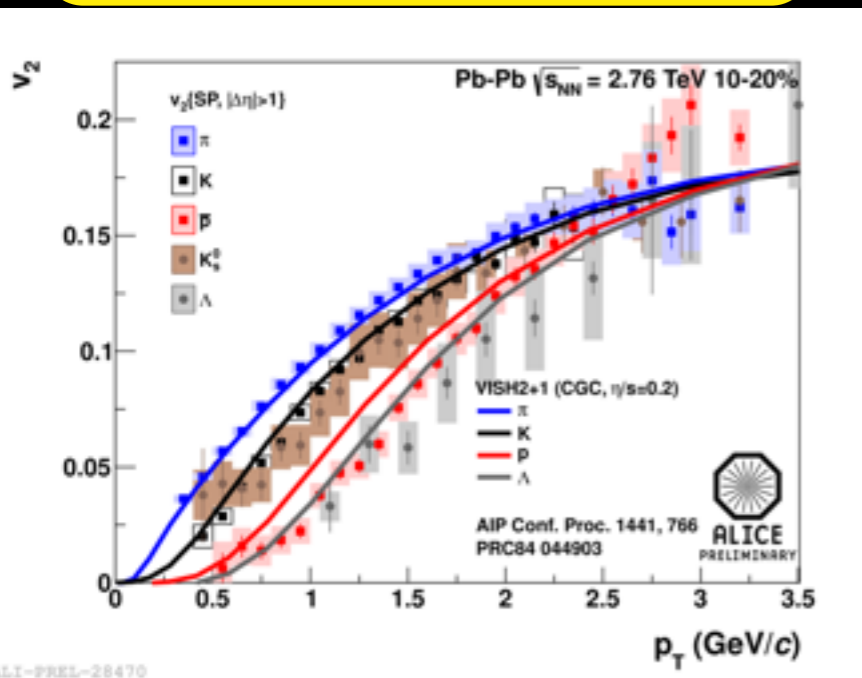
Panos Christakoglou  
Nikhef

for the ALICE Collaboration



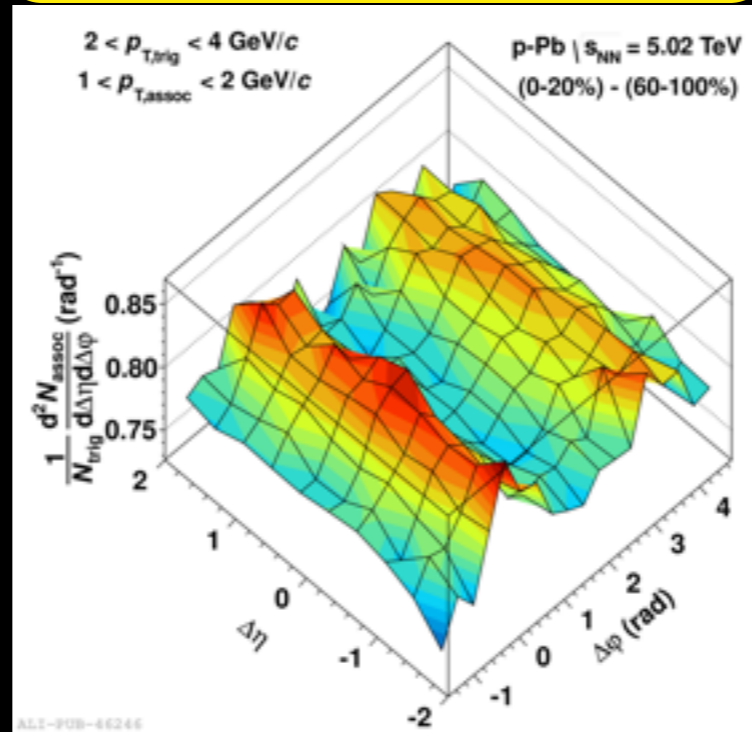
## Flow results in Pb-Pb

- Directed flow measurements
- Flow fluctuations at high  $p_T$  and at forward  $\eta$
- Symmetry plane correlations
- Identified particle  $v_2$  in Pb-Pb



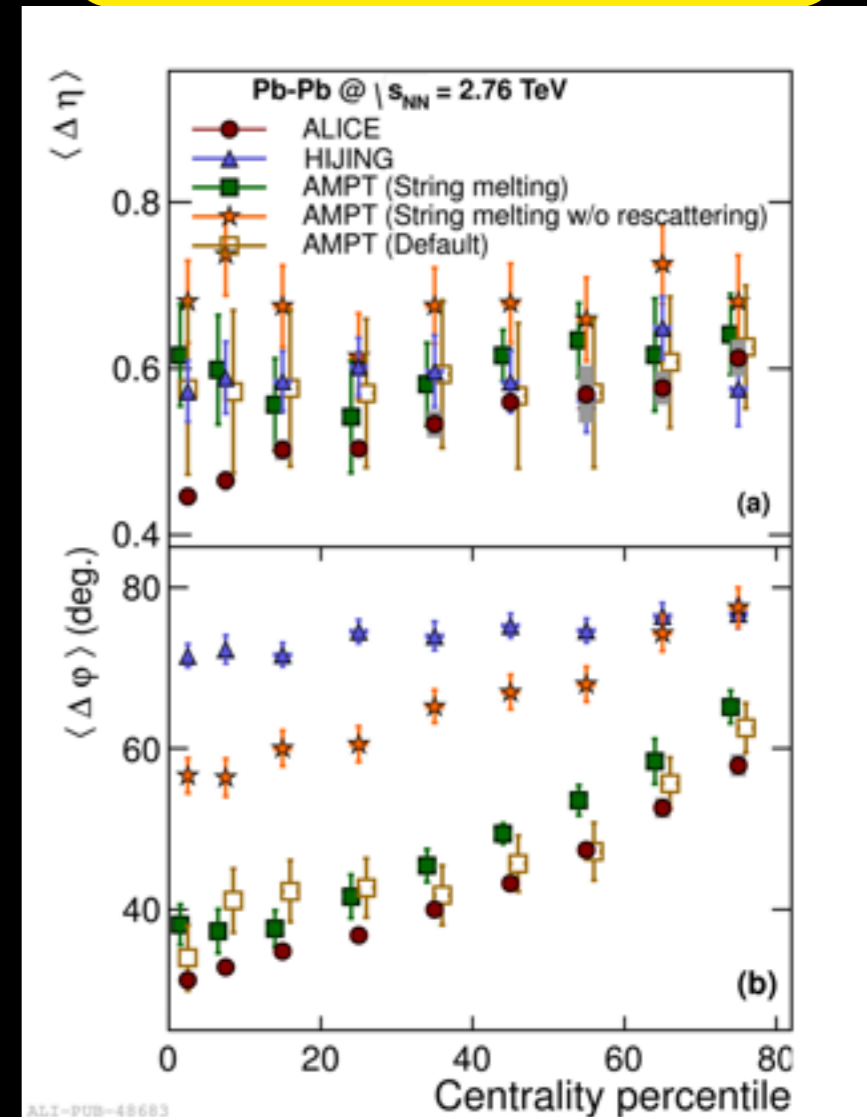
## Particle correlations in p-Pb

- Double ridge
- Identified particle correlations

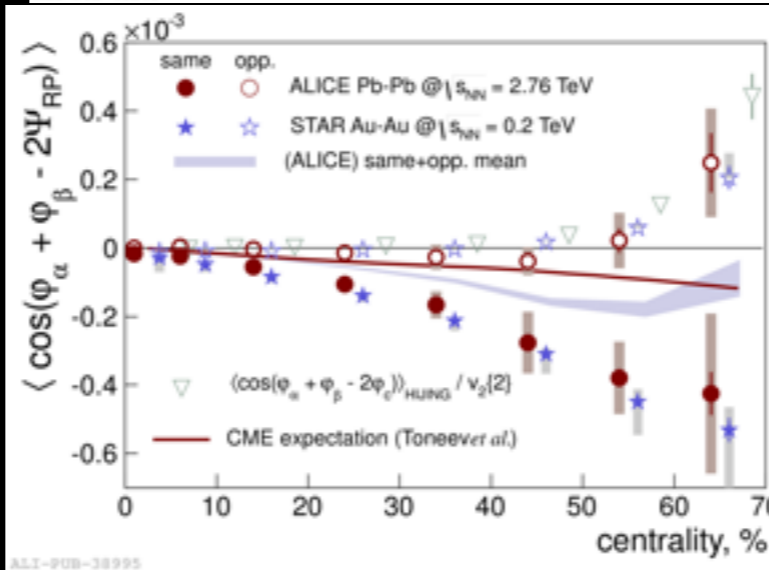


## Two-particle correlations in Pb-Pb

- Jet shape
- Balance functions

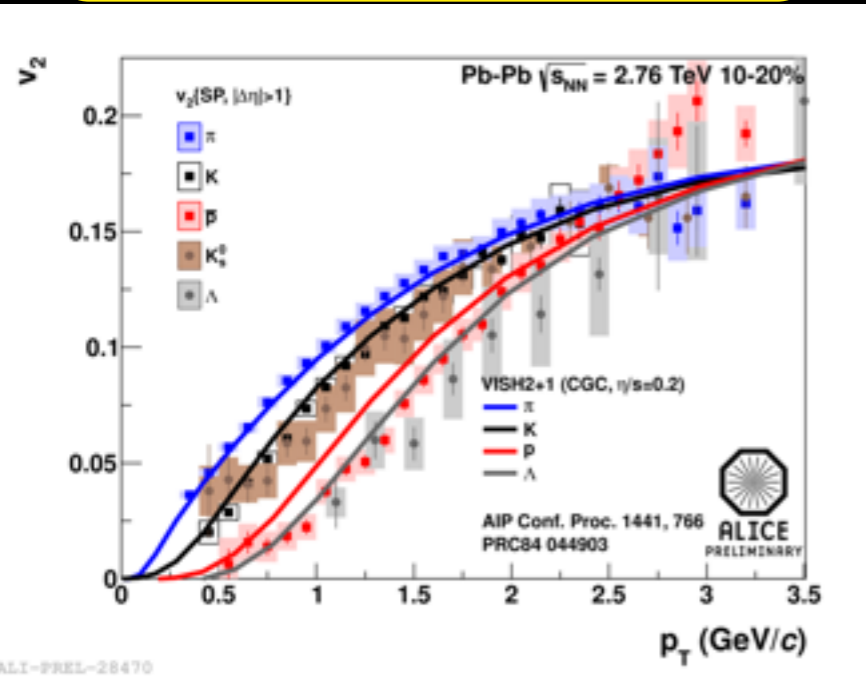


## Testing the Chiral Magnetic Effect



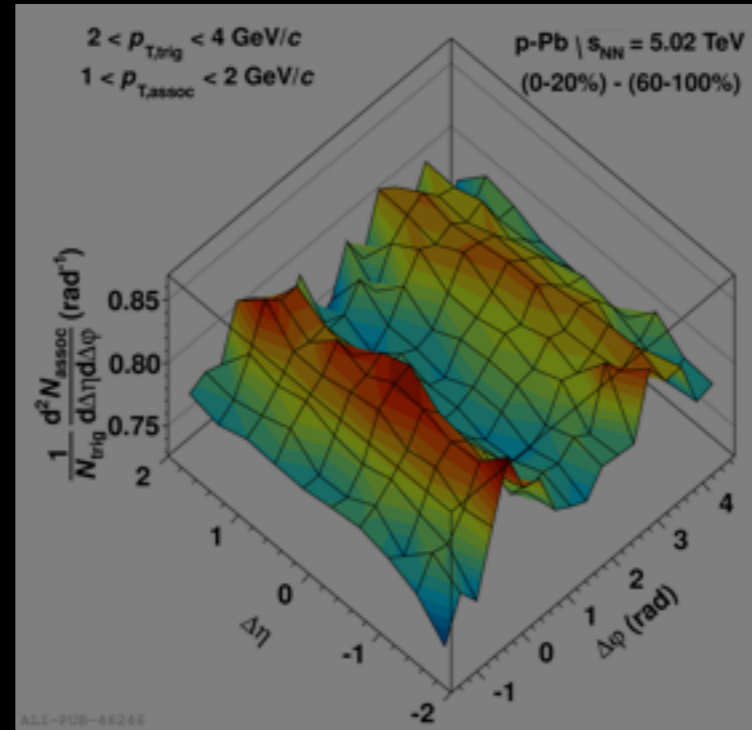
## Flow results in Pb-Pb

- Directed flow measurements
- Flow fluctuations at high  $p_T$  and at forward  $\eta$
- Symmetry plane correlations
- Identified particle  $v_2$  in Pb-Pb



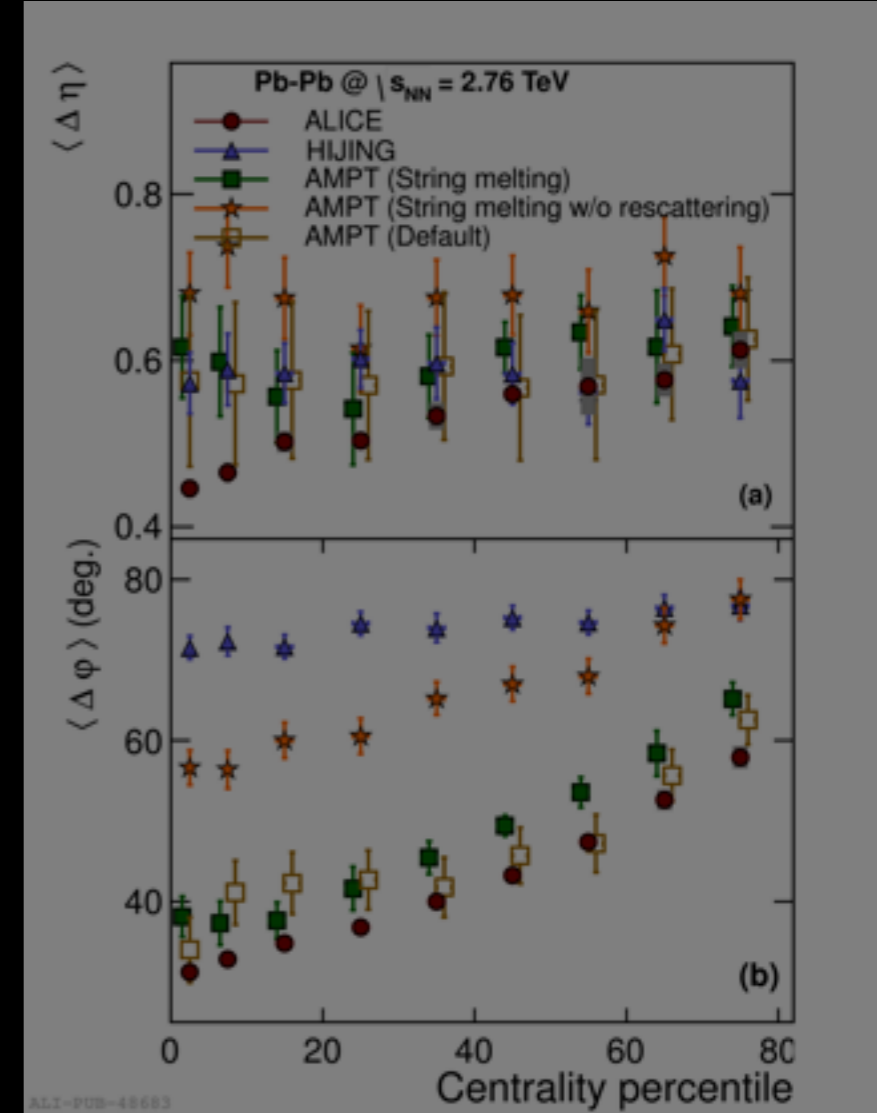
## Particle correlations in p-Pb

- Double ridge
- Identified particle correlations

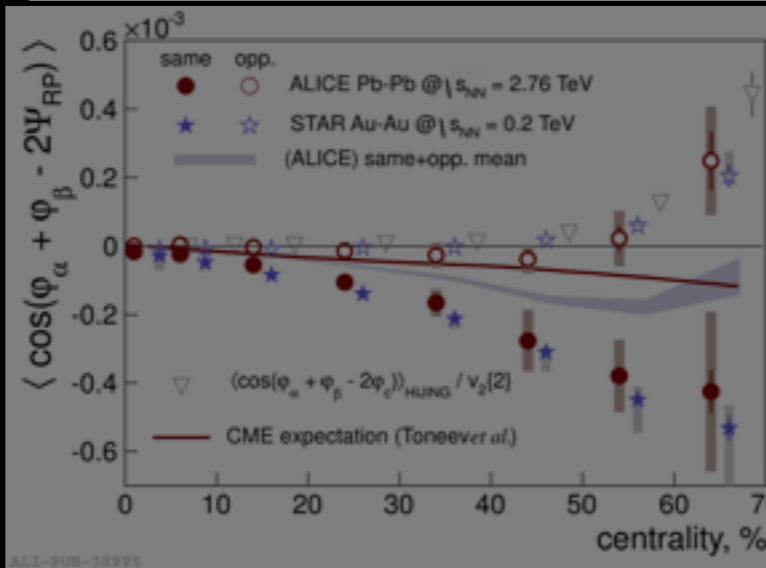


## Two-particle correlations in Pb-Pb

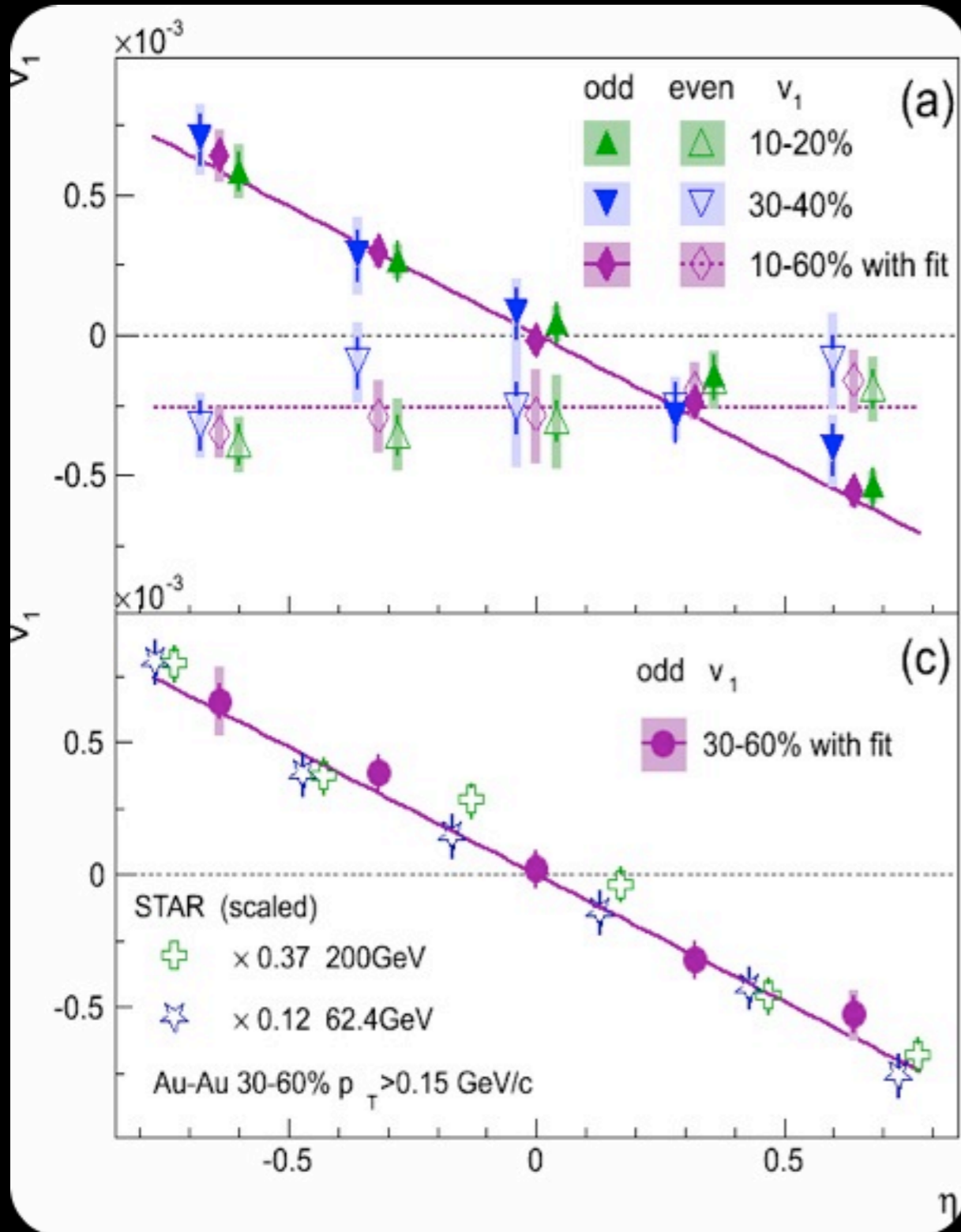
- Jet shape
- Balance functions



## Testing the Chiral Magnetic Effect



(ALICE Collaboration) arXiv:1306.4145



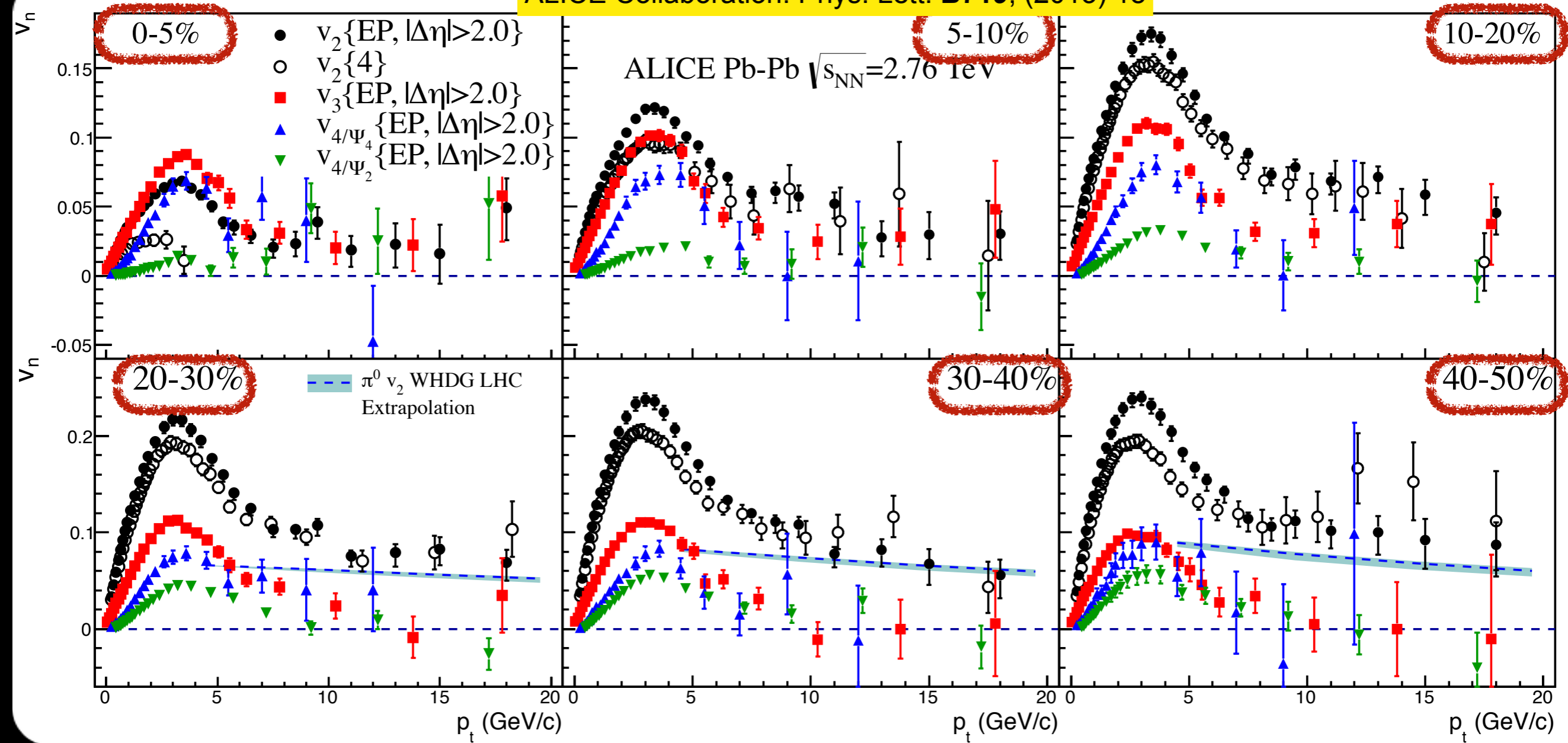
$$v_1 = \langle \cos(\varphi - \Psi) \rangle$$

$$v_1^{odd} \{ \Psi_{SP} \} = \frac{1}{2} [v_1 \{ \Psi_{SP}^p \} + v_1 \{ \Psi_{SP}^t \} ]$$

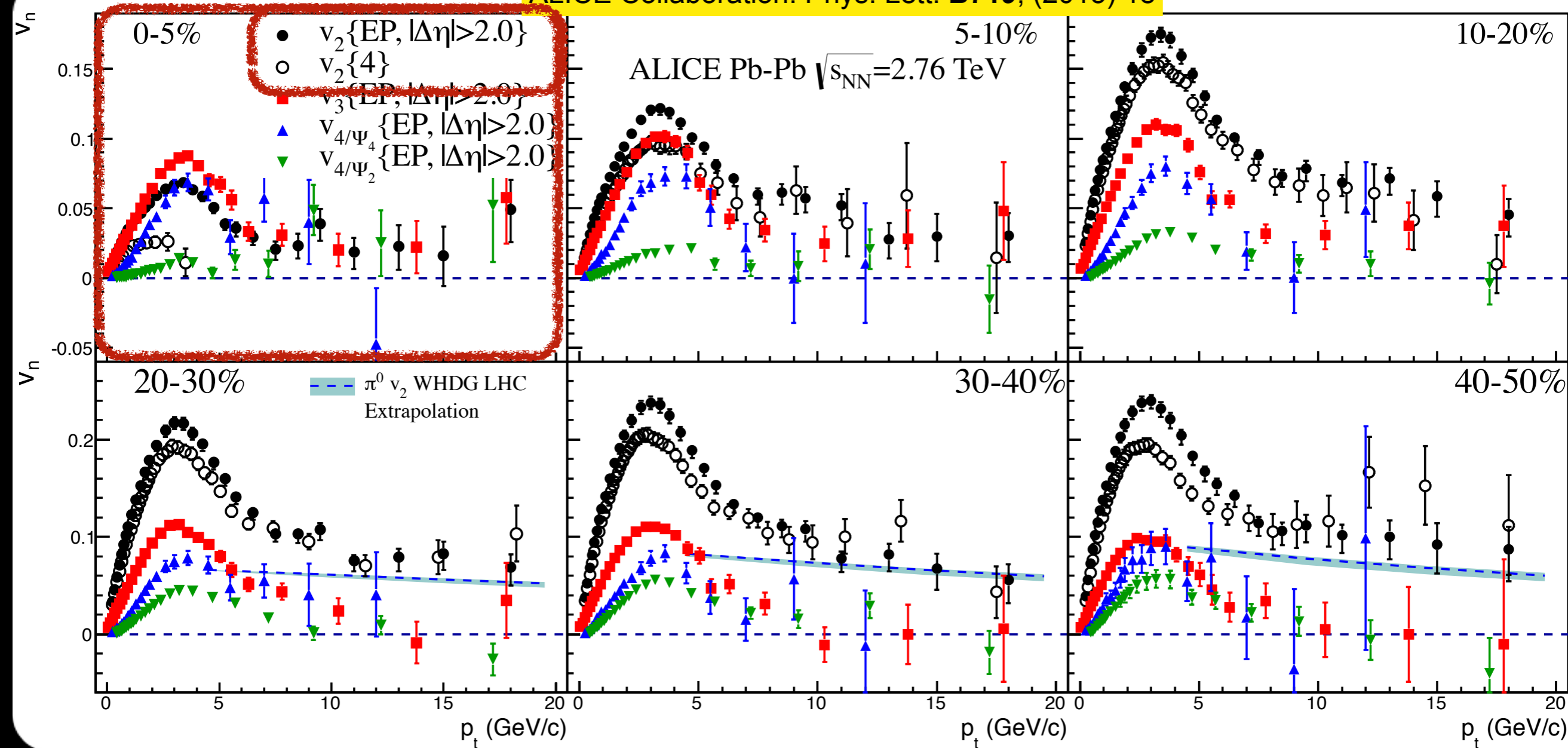
$$v_1^{even} \{ \Psi_{SP} \} = \frac{1}{2} [v_1 \{ \Psi_{SP}^p \} - v_1 \{ \Psi_{SP}^t \} ]$$

- Measured wrt the spectator deflection
- $v_1^{odd}$  negative slope
- ★ similar observation @ RHIC but a factor of  $\sim 3$  smaller magnitude
- ★ consistent with models considering a smaller tilt in x-z @ LHC wrt RHIC
- $v_1^{even}$  negative with no evident  $\eta$  dependence

ALICE Collaboration: Phys. Lett. **B719**, (2013) 18

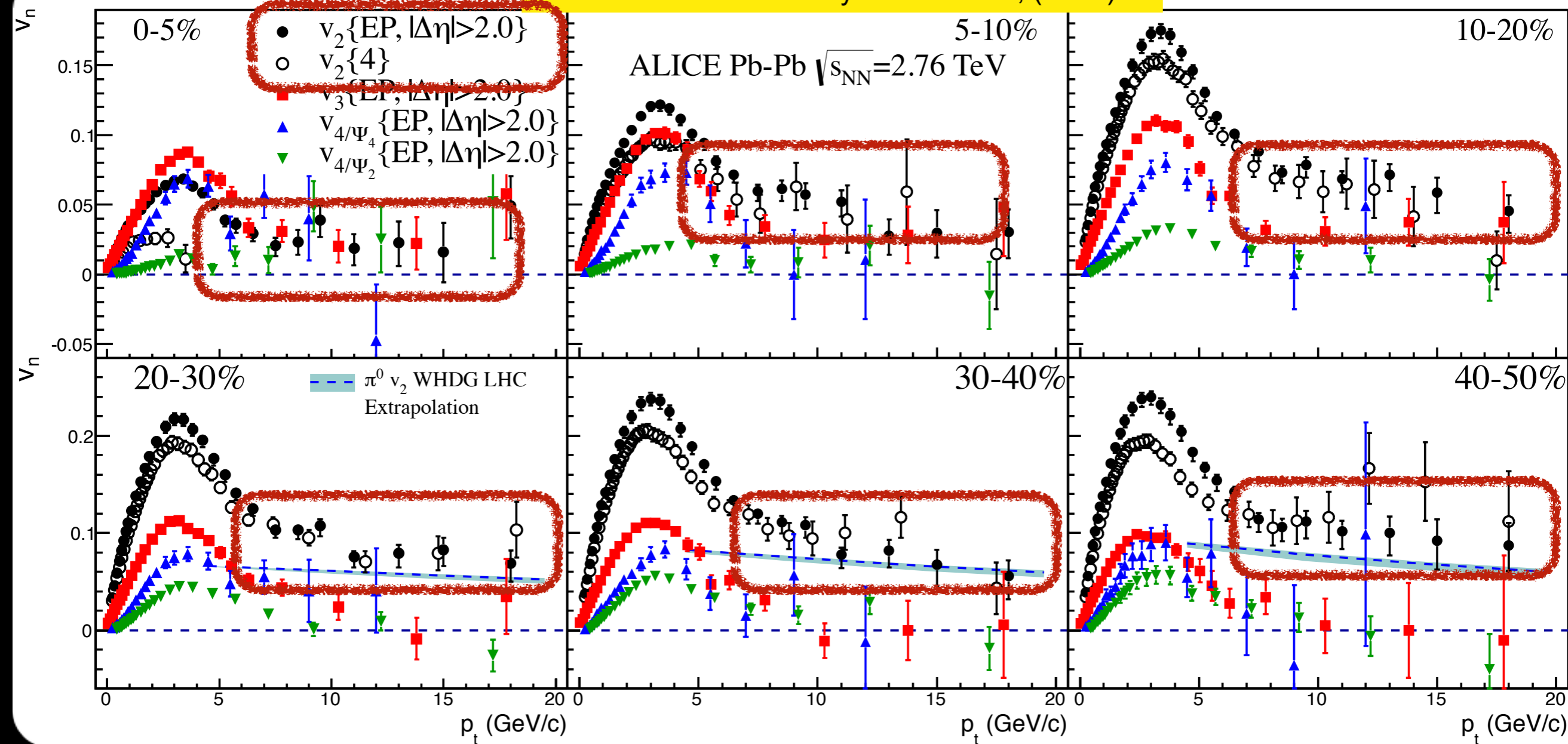


ALICE Collaboration: Phys. Lett. **B719**, (2013) 18



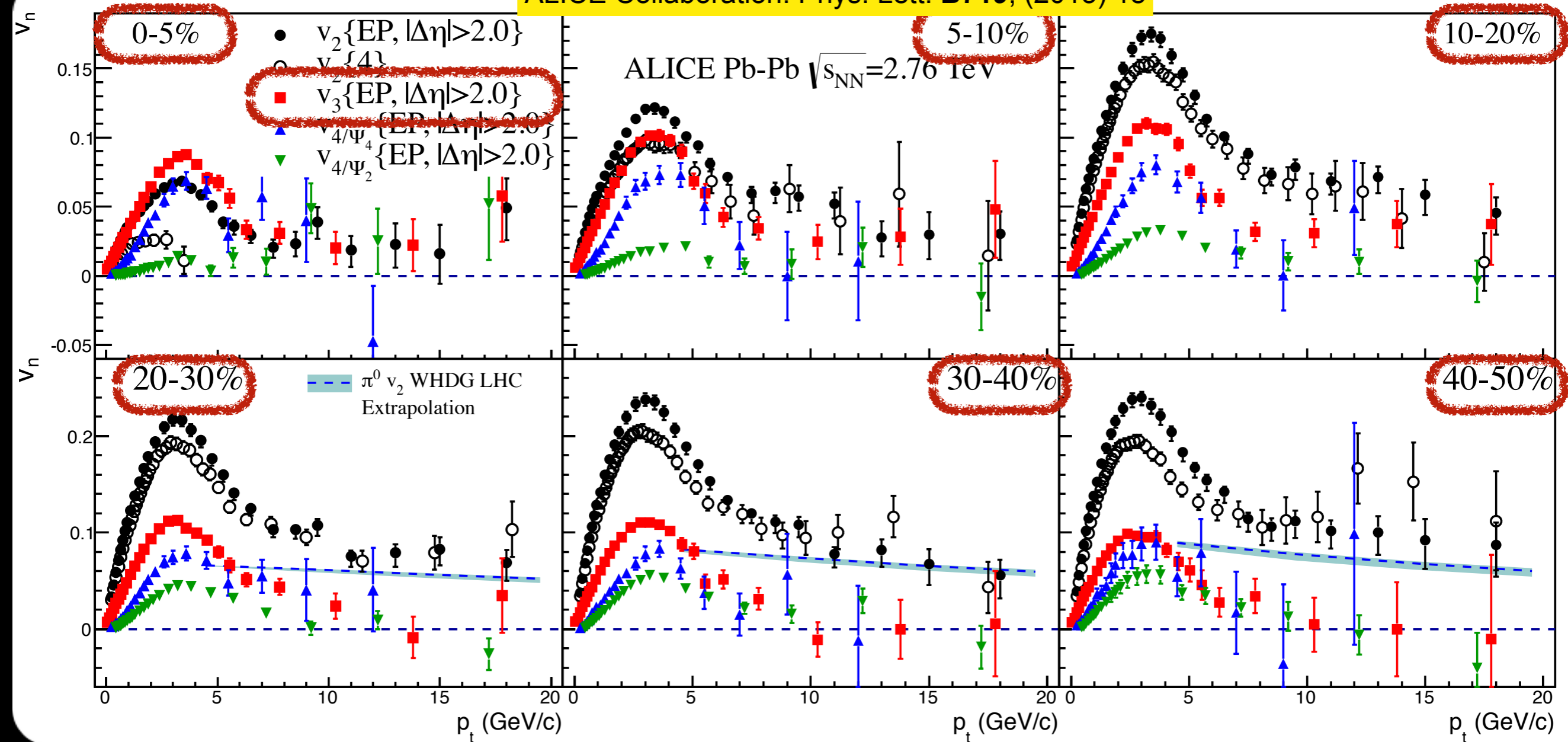
Elliptic flow the dominant harmonic for all centralities except the more central events

ALICE Collaboration: Phys. Lett. **B719**, (2013) 18



- Elliptic flow the dominant harmonic for all centralities except the more central events
- Finite  $v_2$  values at high  $p_T$  (path length dependence)

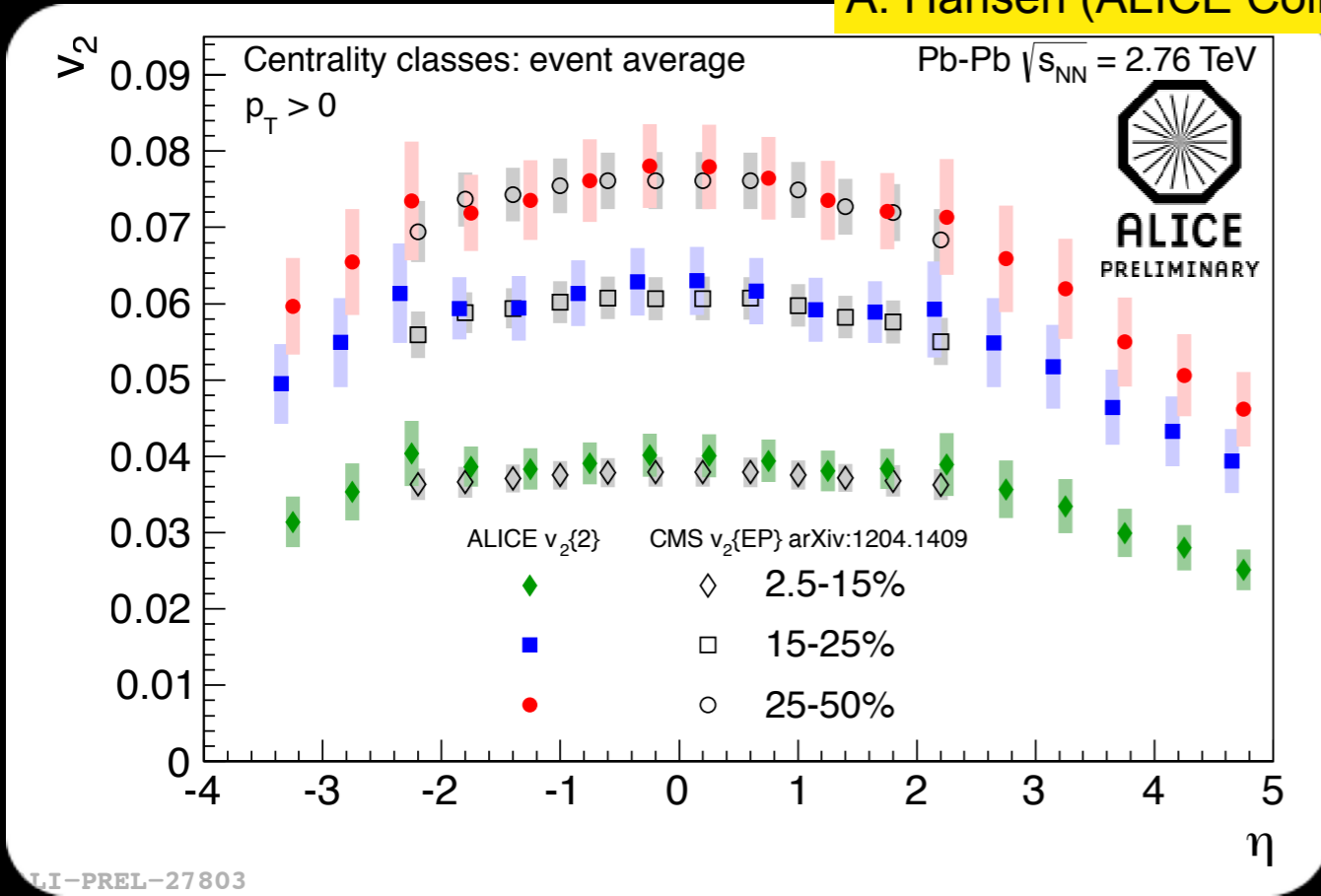
ALICE Collaboration: Phys. Lett. **B719**, (2013) 18



- Elliptic flow the dominant harmonic for all centralities except the more central events
- Finite  $v_2$  values at high  $p_T$  (path length dependence)
- Triangular flow (red points) shows little centrality dependence

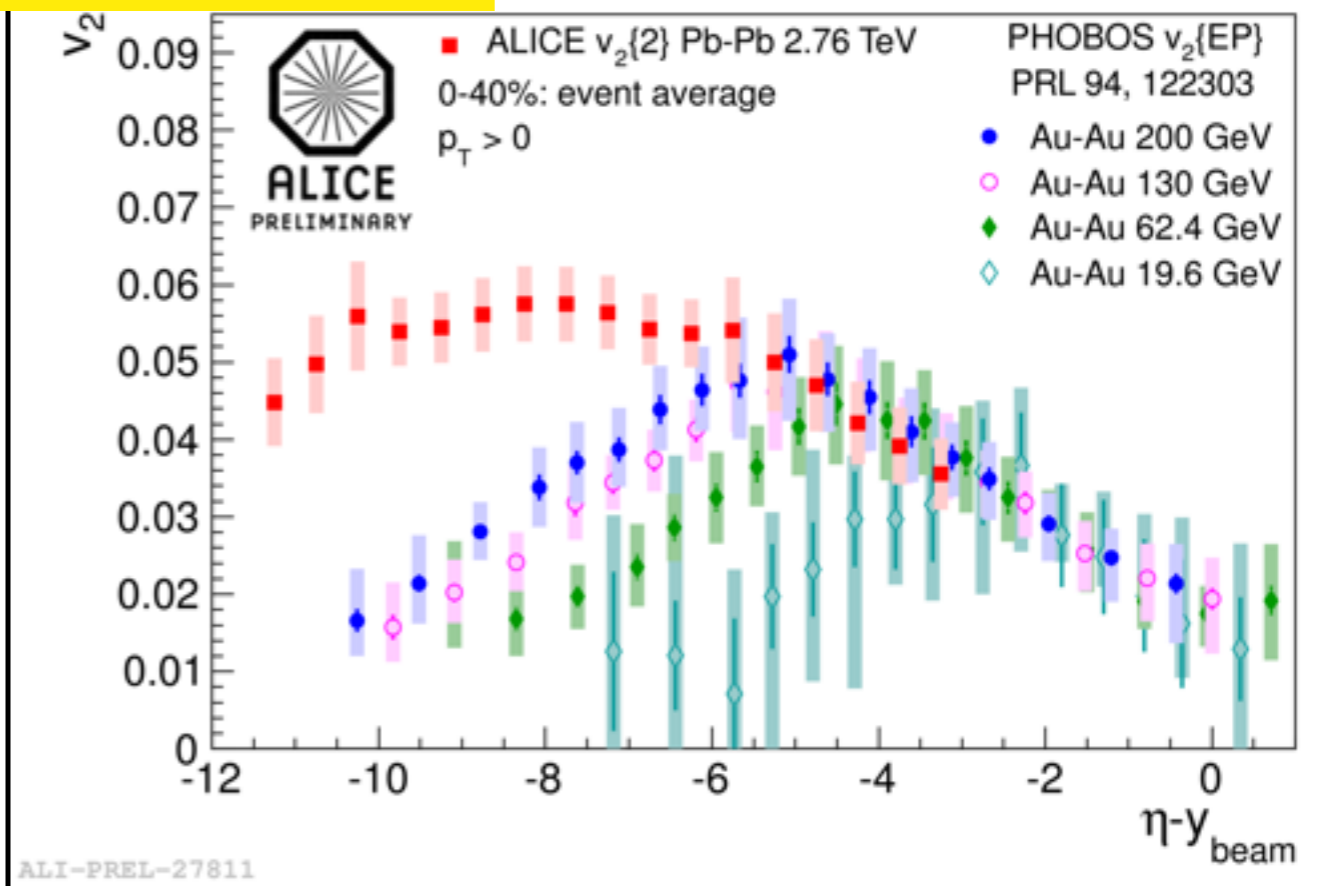
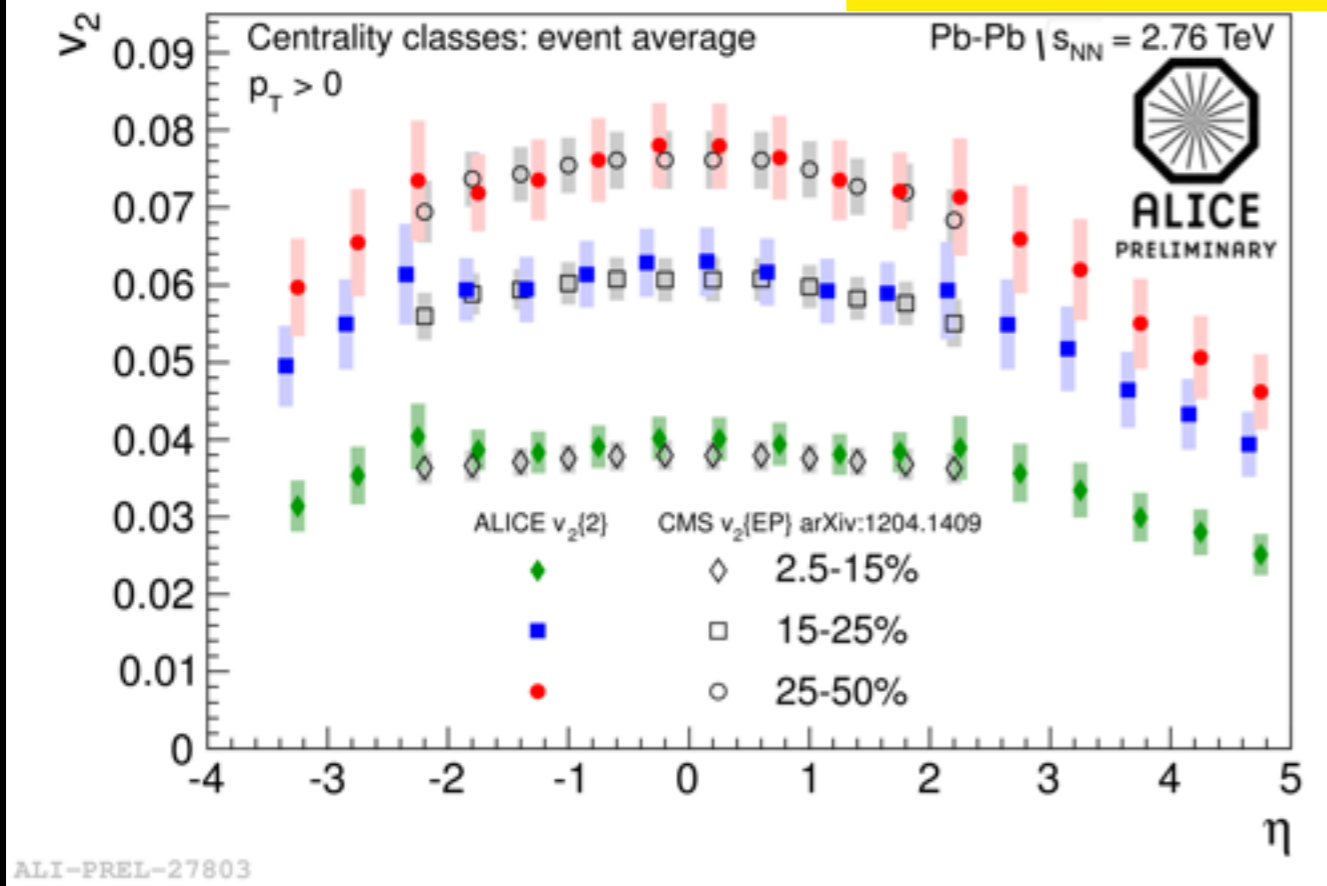


A. Hansen (ALICE Collaboration) @ QM2012



- Extension of the mid-rapidity measurement with the help of the SPD ( $|\eta| < 2$ ) and the FMD ( $-3.4 < \eta < -1.7$  and  $1.7 < \eta < 5.0$ )
- ★ Hit based analysis
- Strong centrality dependence of  $v_2$  (in good agreement with CMS)

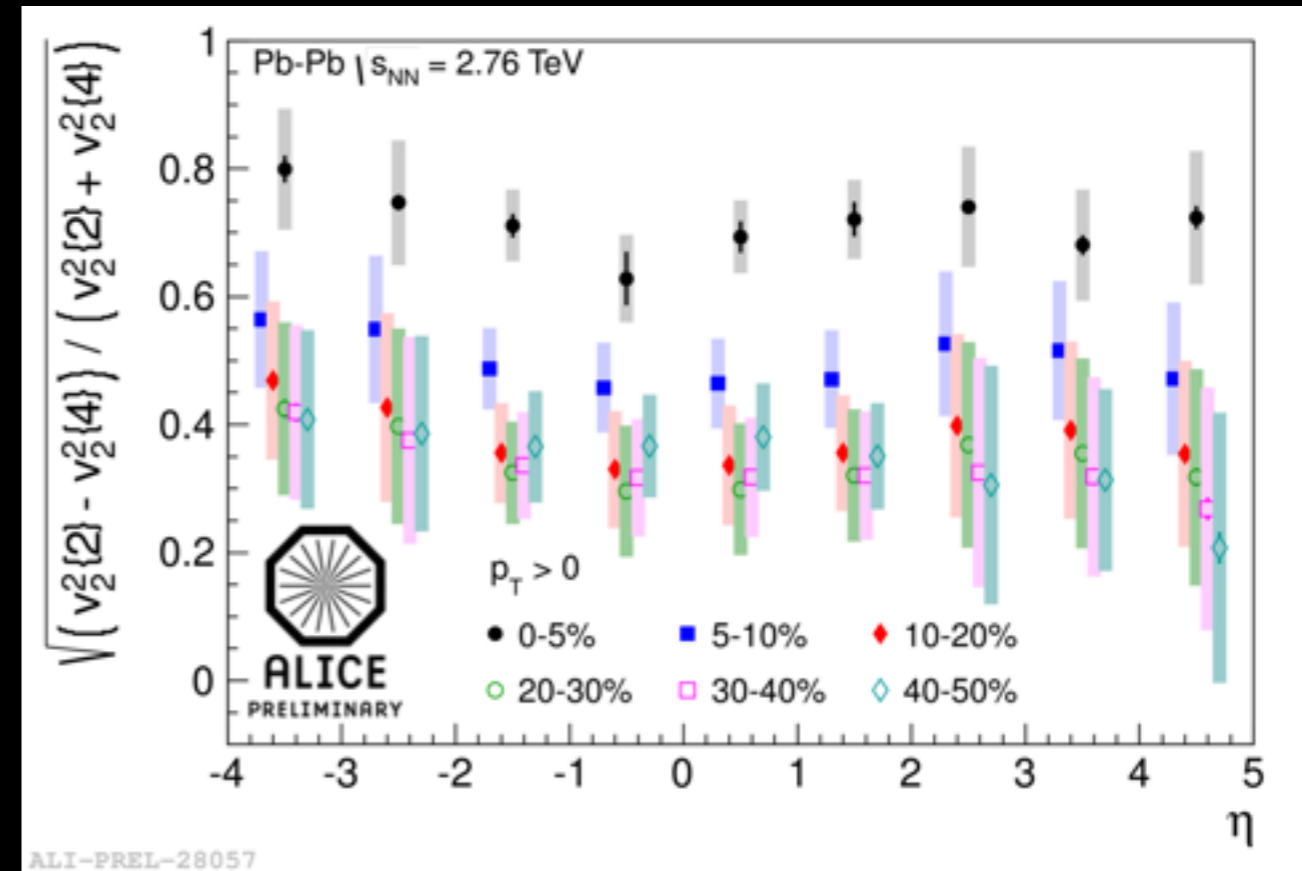
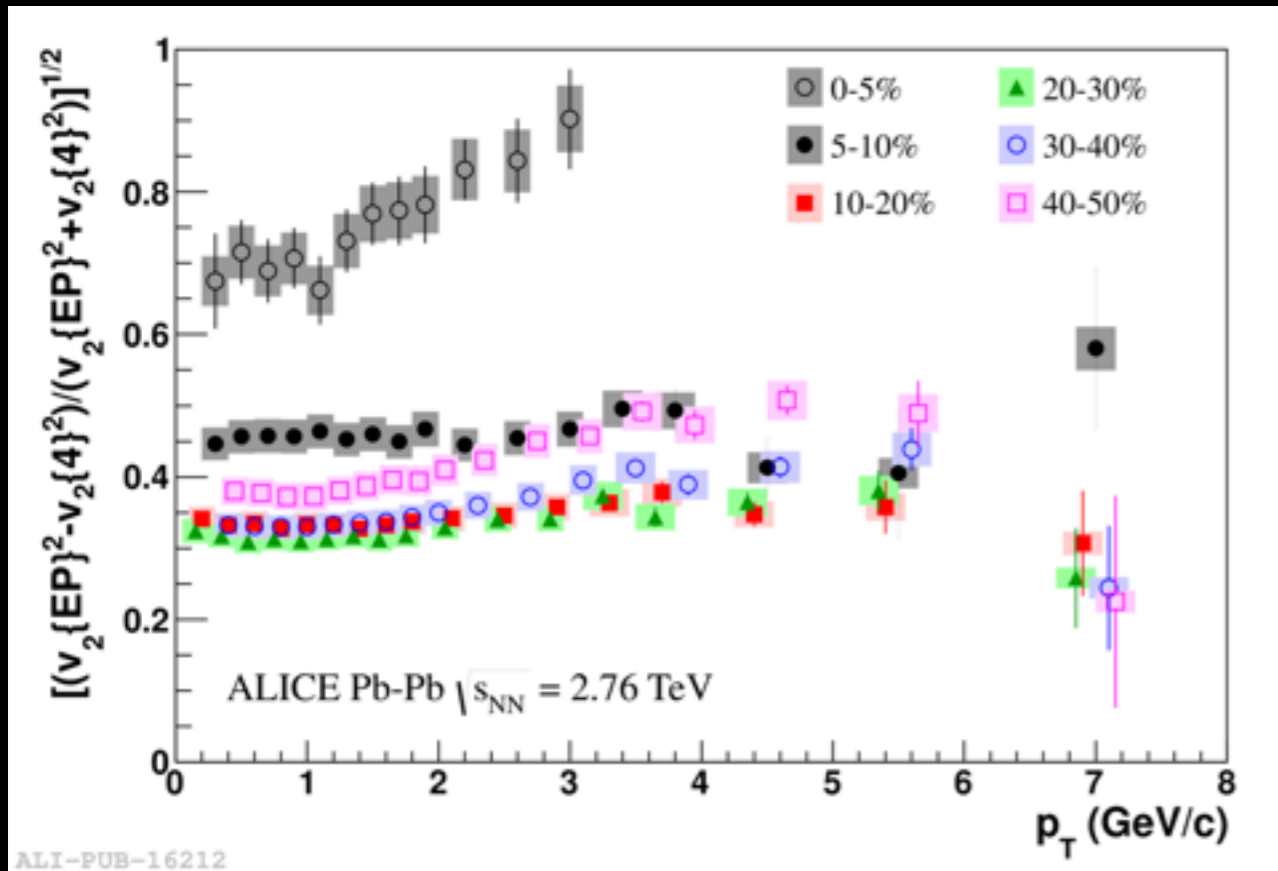
A. Hansen (ALICE Collaboration) @ QM2012



- Extension of the mid-rapidity measurement with the help of the SPD ( $|\eta| < 2$ ) and the FMD ( $-3.4 < \eta < -1.7$  and  $1.7 < \eta < 5.0$ )
- ★ Hit based analysis
- Strong centrality dependence of  $v_2$  (in good agreement with CMS)
- Longitudinal scaling holds between RHIC and LHC

ALICE Collaboration: Phys. Lett. **B719**, (2013) 18

A. Hansen (ALICE Collaboration) @ QM2012



- No strong transverse momentum dependence except
  - ★ the most central events (i.e. 0-5%)
  - ★ the 40-50% class
- Little pseudorapidity dependence

R.S. Bhalerao, M. Luzum, J.-Y. Ollitrault,  
Phys. Rev. **C84** , (2011) 034910

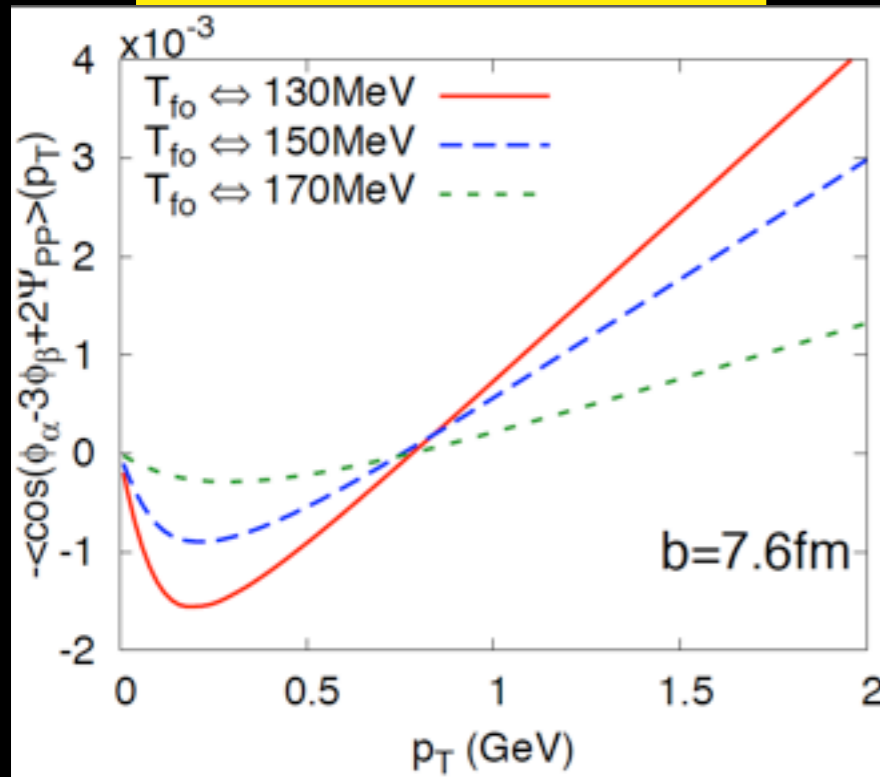
$$\langle \cos(n_1\varphi_1 + n_2\varphi_2 + \dots + n_k\varphi_k) \rangle = v_{n_1} v_{n_2} \dots v_{n_k} \langle \cos(n_1\Psi_1 + n_2\Psi_2 + \dots + n_k\Psi_k) \rangle$$

R.S. Bhalerao, M. Luzum, J.-Y. Ollitrault, Phys. Rev. **C84**, (2011) 034910

$$\langle \cos(n_1\varphi_1+n_2\varphi_2+\dots+n_k\varphi_k) \rangle = v_{n_1}v_{n_2}\dots v_{n_k} \langle \cos(n_1\Psi_1+n_2\Psi_2+\dots+n_k\Psi_k) \rangle$$

$$\langle \cos(\varphi_1-3\varphi_2+2\varphi_3) \rangle = v_1v_2v_3 \langle \cos(\Psi_1-3\Psi_3+2\Psi_2) \rangle$$

D. Teaney and L. Yan, Phys. Rev. **C83**, (2011) 064904



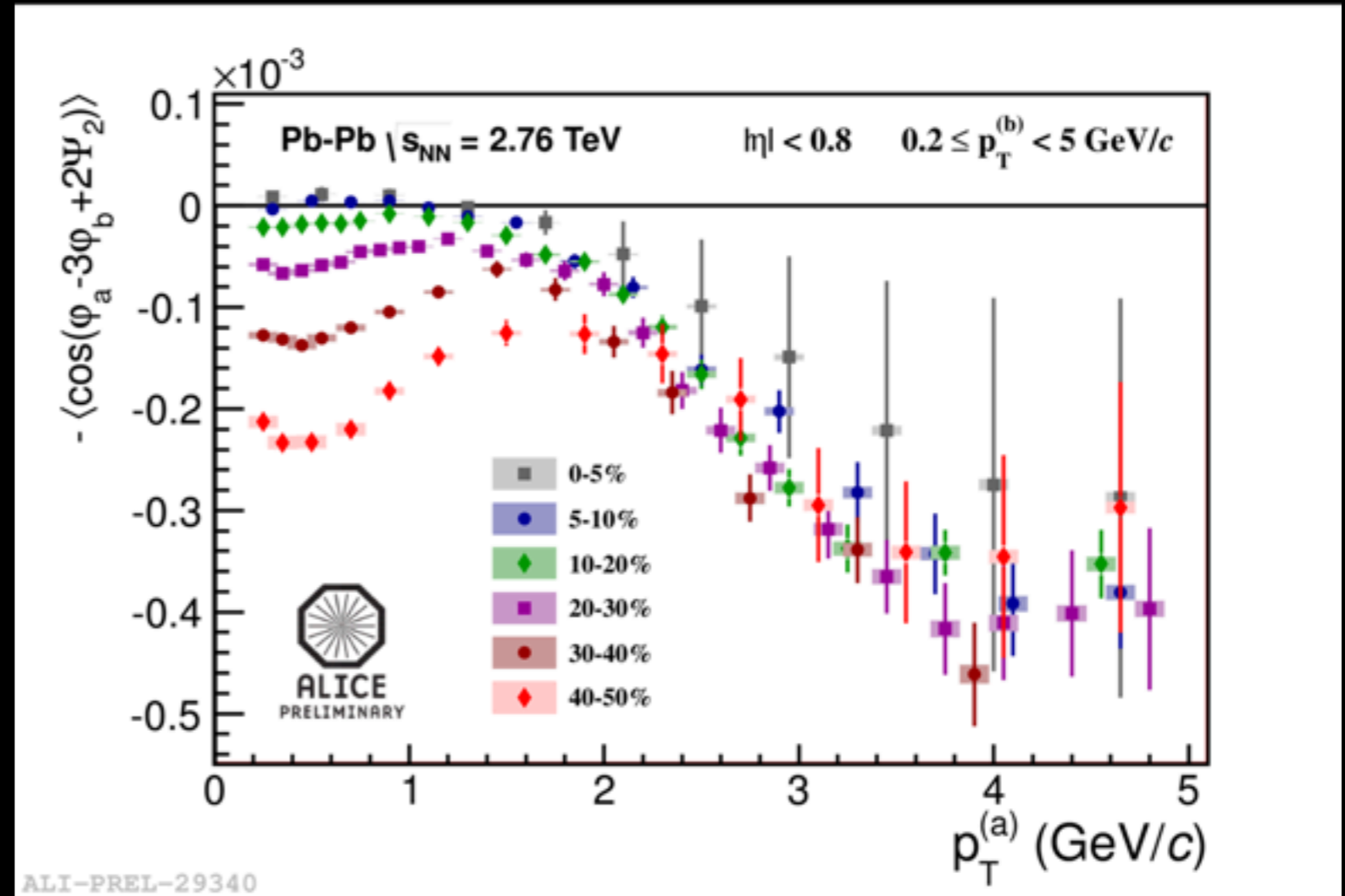
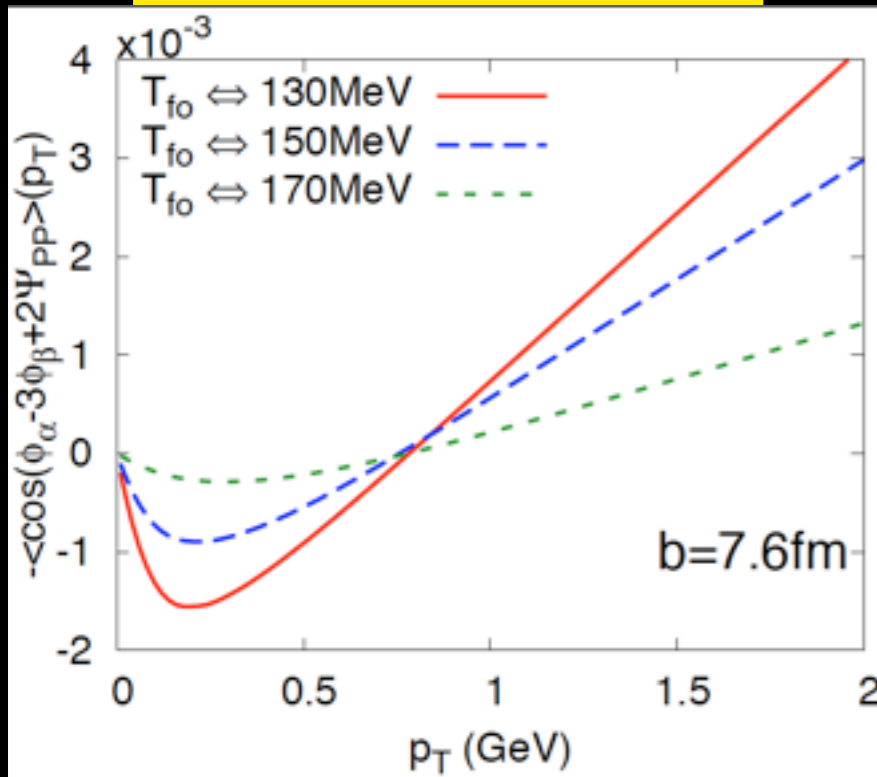
Glauber MC + ideal hydro

R.S. Bhalerao, M. Luzum, J.-Y. Ollitrault, Phys. Rev. **C84**, (2011) 034910

$$\langle \cos(n_1\varphi_1 + n_2\varphi_2 + \dots + n_k\varphi_k) \rangle = v_{n_1}v_{n_2}\dots v_{n_k} \langle \cos(n_1\Psi_1 + n_2\Psi_2 + \dots + n_k\Psi_k) \rangle$$

$$\langle \cos(\varphi_1 - 3\varphi_2 + 2\varphi_3) \rangle = v_1v_2v_3 \langle \cos(\Psi_1 - 3\Psi_3 + 2\Psi_2) \rangle$$

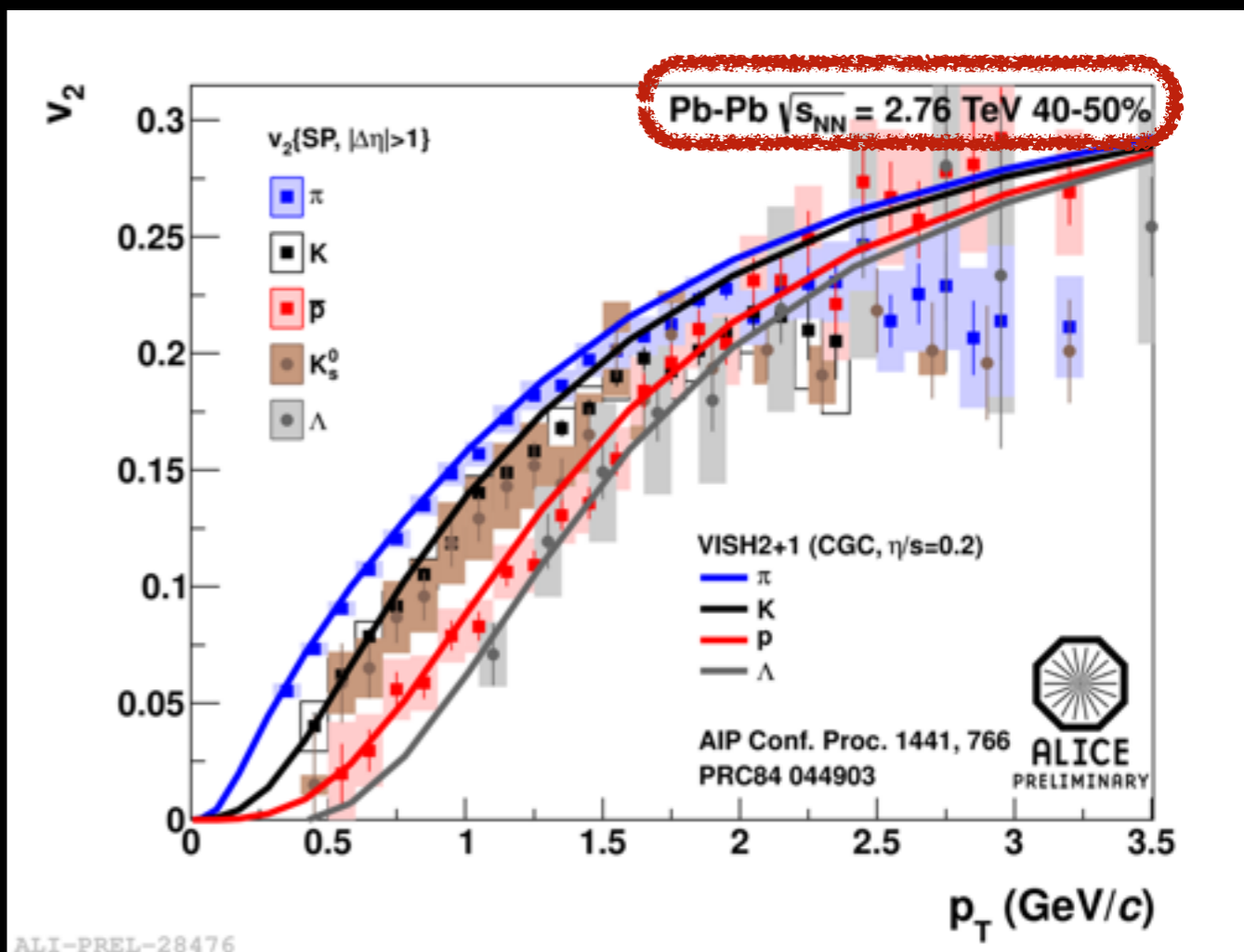
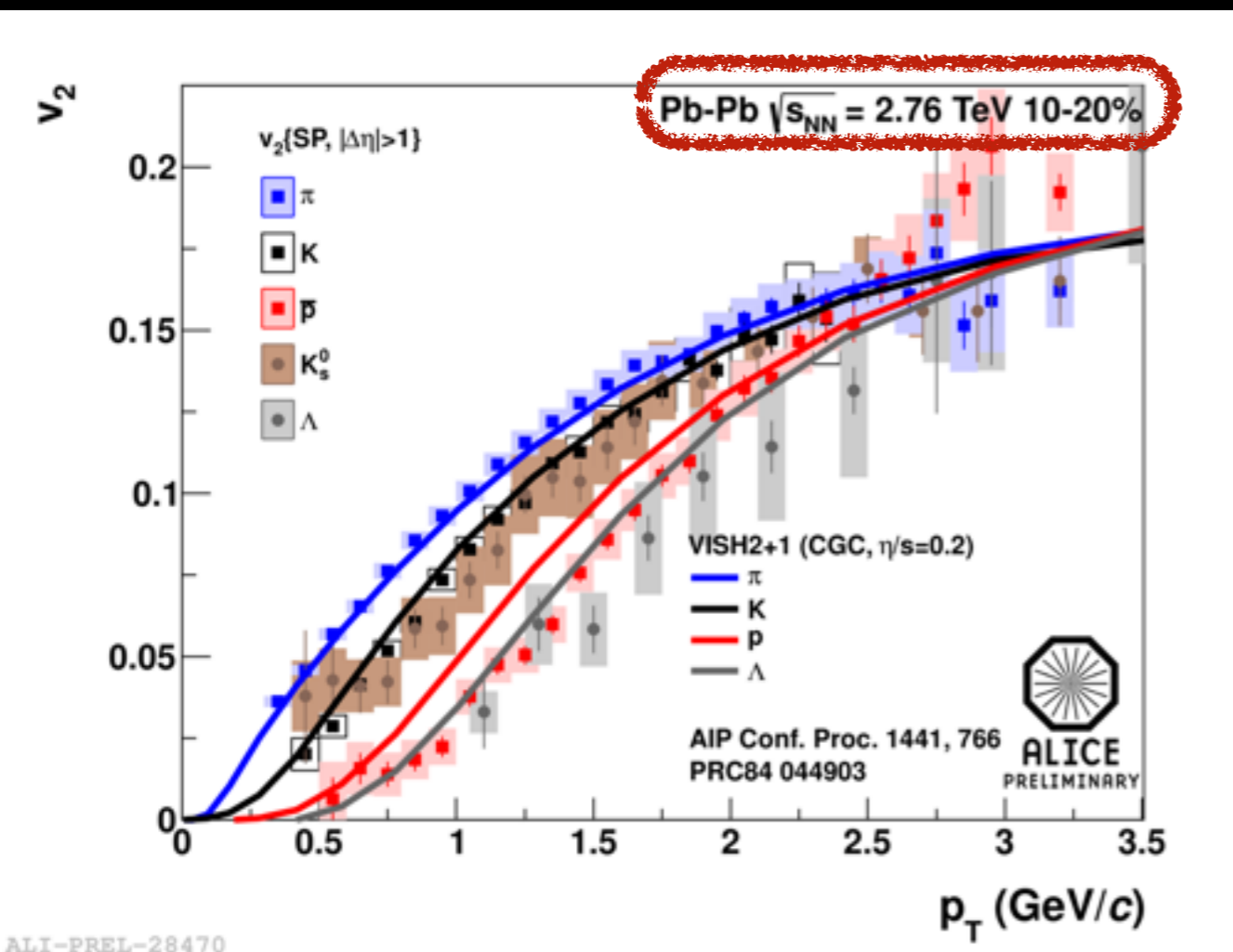
D. Teaney and L. Yan, Phys. Rev. **C83**, (2011) 064904



ALI-PREL-29340

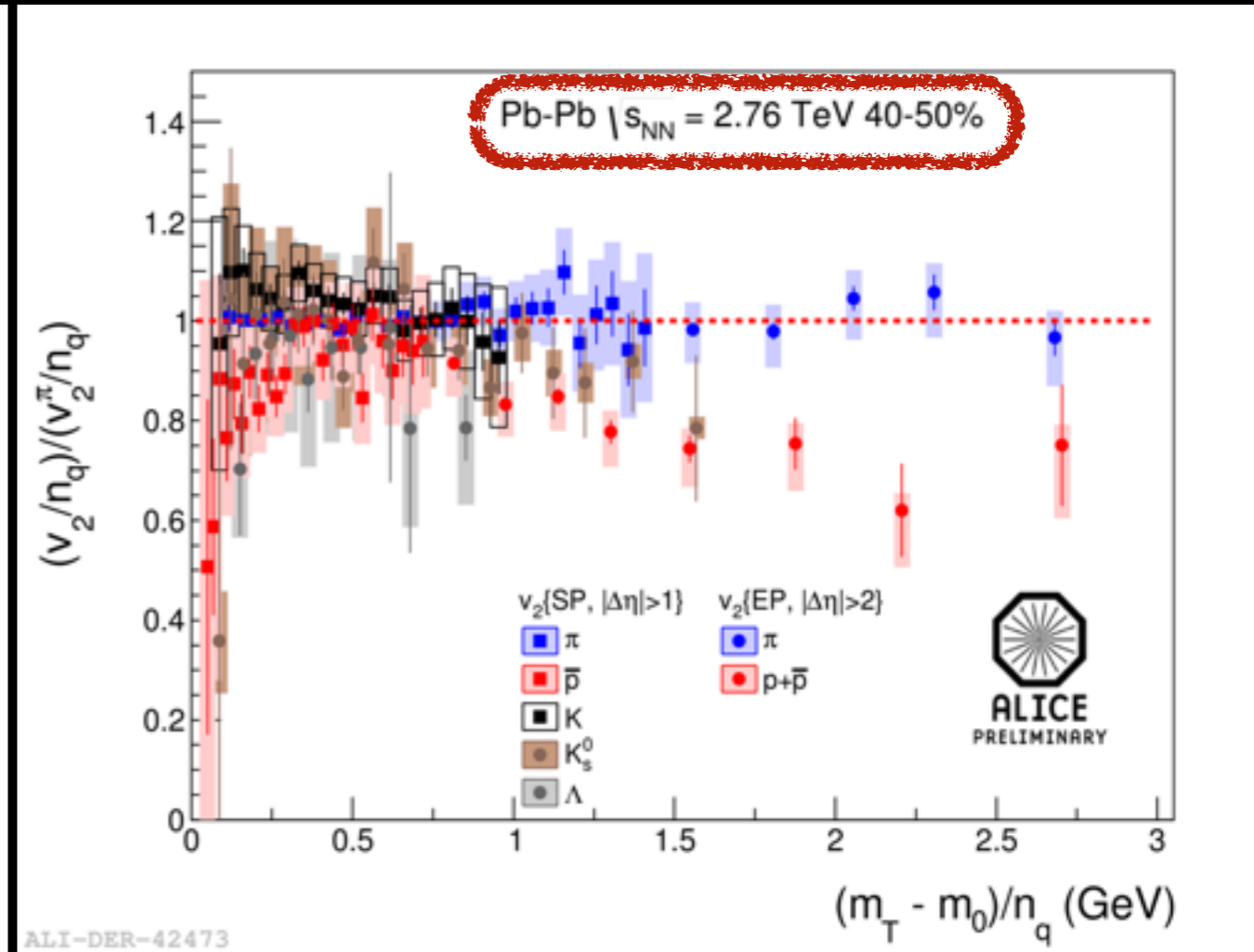
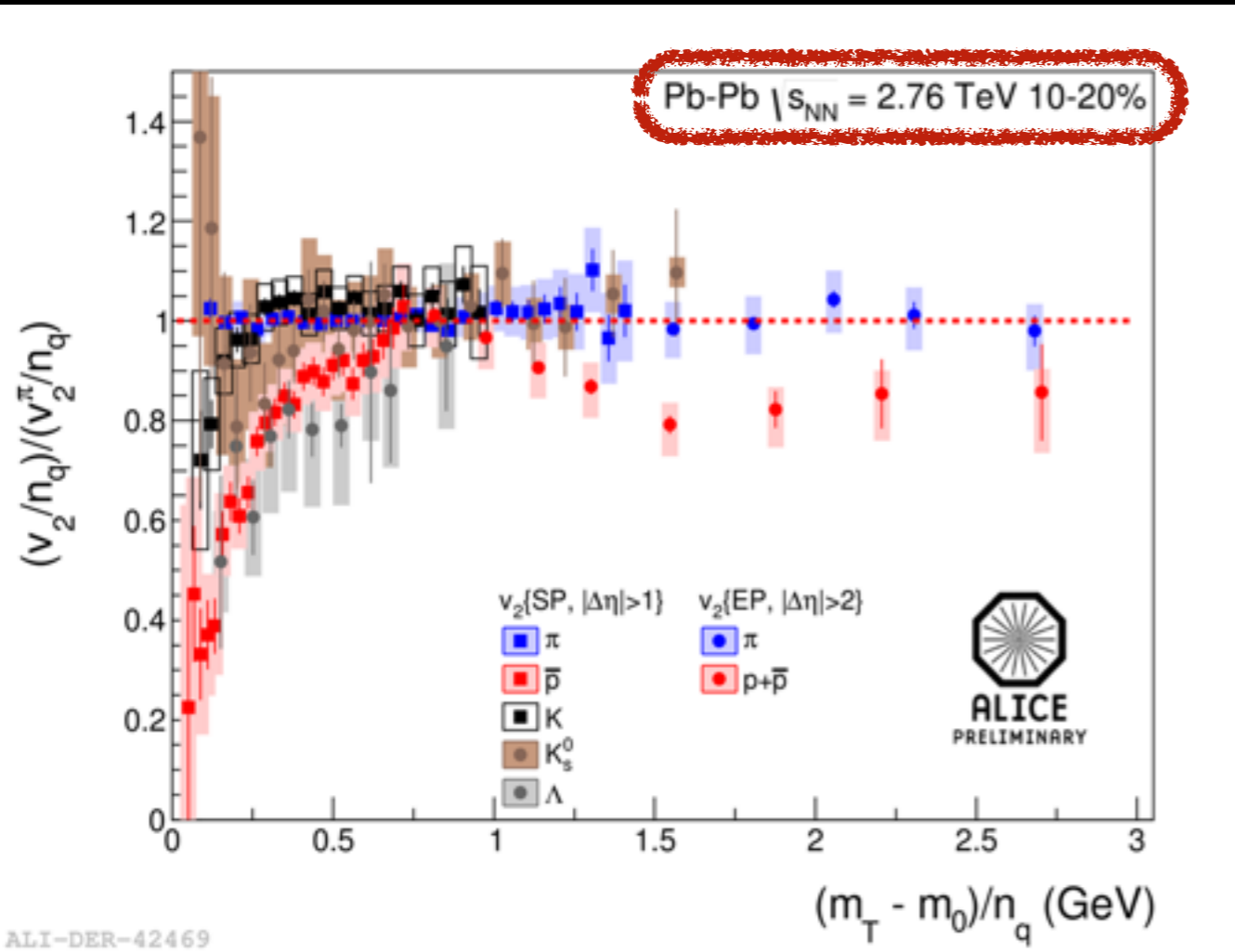
Glauber MC + ideal hydro

- Observation of a 3-plane correlation
- In qualitative agreement with MC Glauber+ideal hydro calculations at low  $p_T$  but hydro curves do not follow data at high  $p_T$



- Observed mass splitting driven by radial flow
- Hydro curves describe data points fairly well
- ★ Better agreement for more central events and for heavier particles when hydro is coupled to a hadronic afterburner

You Zhou (23/7 Parallel session @ 14:00)



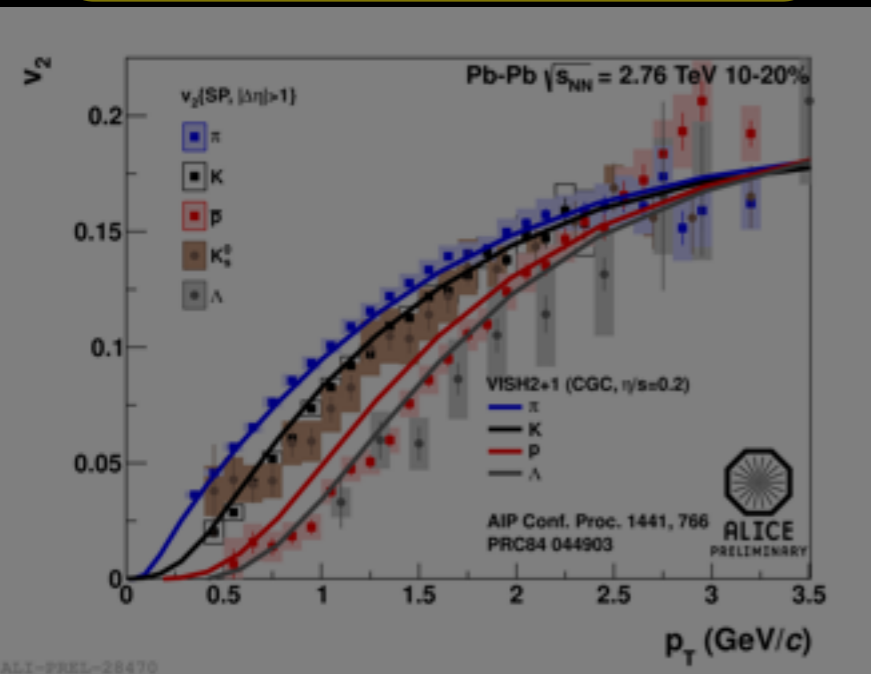
- Low  $(m_T - m_0)/n_q$ : scaling is broken at the LHC
- Intermediate  $(m_T - m_0)/n_q$ : scaling holds at the level of ~20%

You Zhou (23/7 Parallel session @ 14:00)



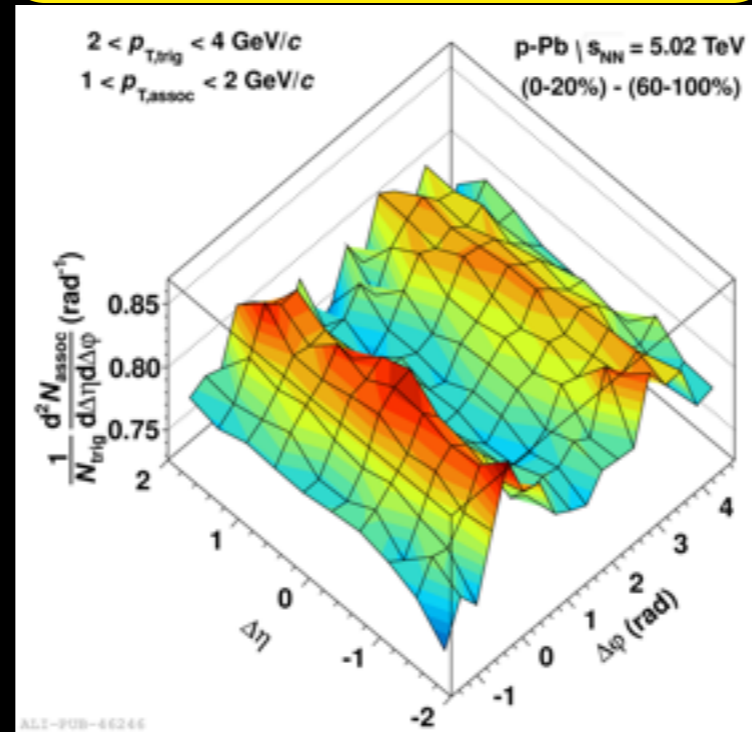
## Flow results in Pb-Pb

- Directed flow measurements
- Flow fluctuations at high  $p_T$  and at forward  $\eta$
- Symmetry plane correlations
- Identified particle  $v_2$  in Pb-Pb



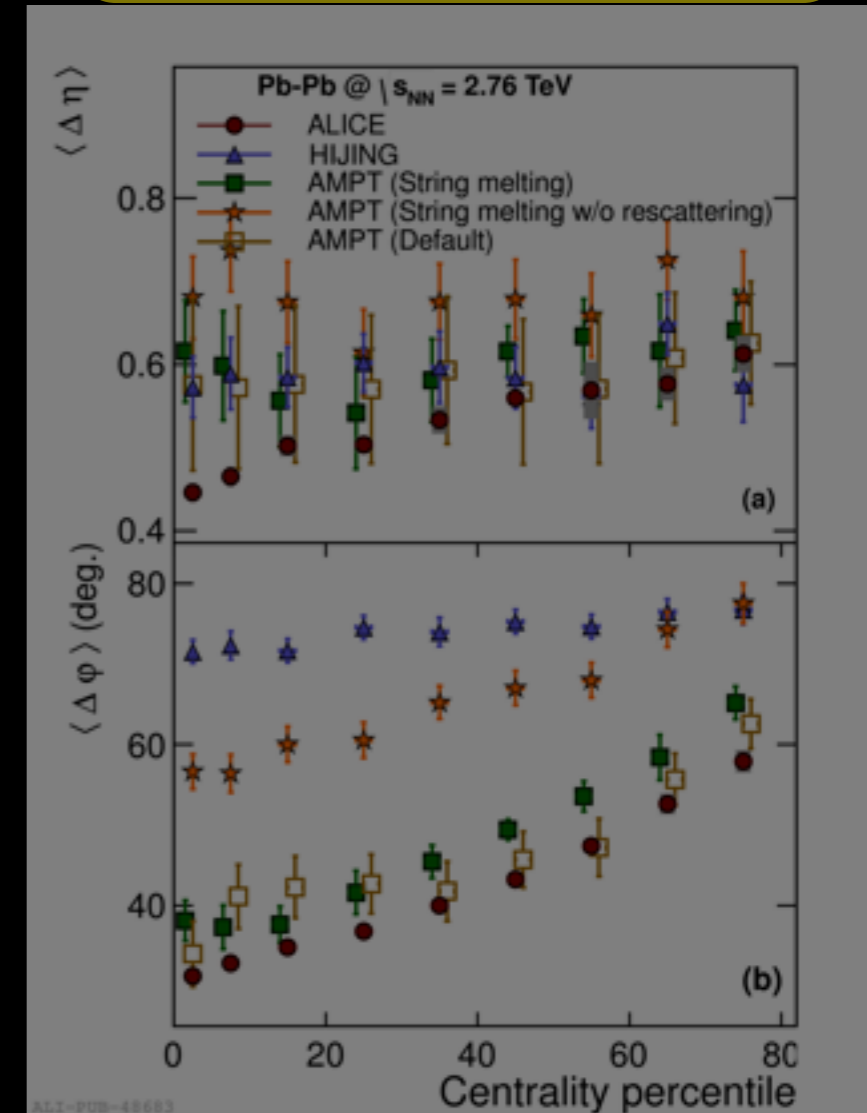
## Particle correlations in p-Pb

- Double ridge
- Identified particle correlations

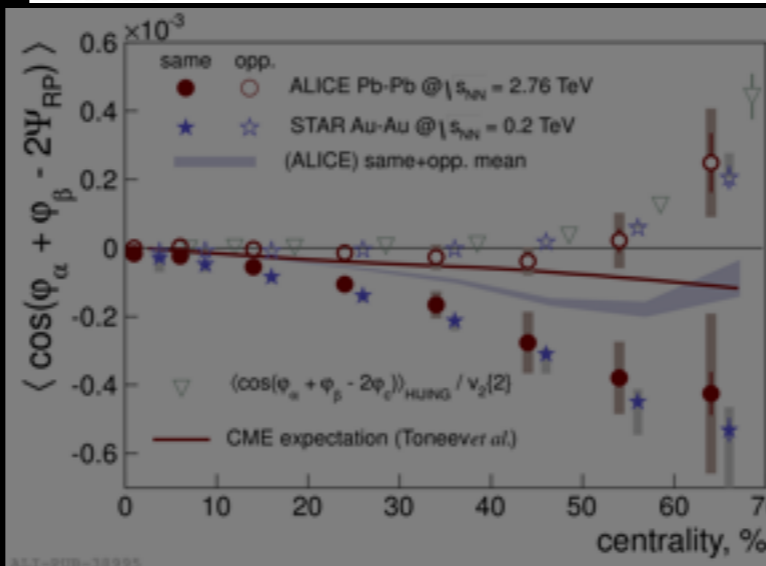


## Two-particle correlations in Pb-Pb

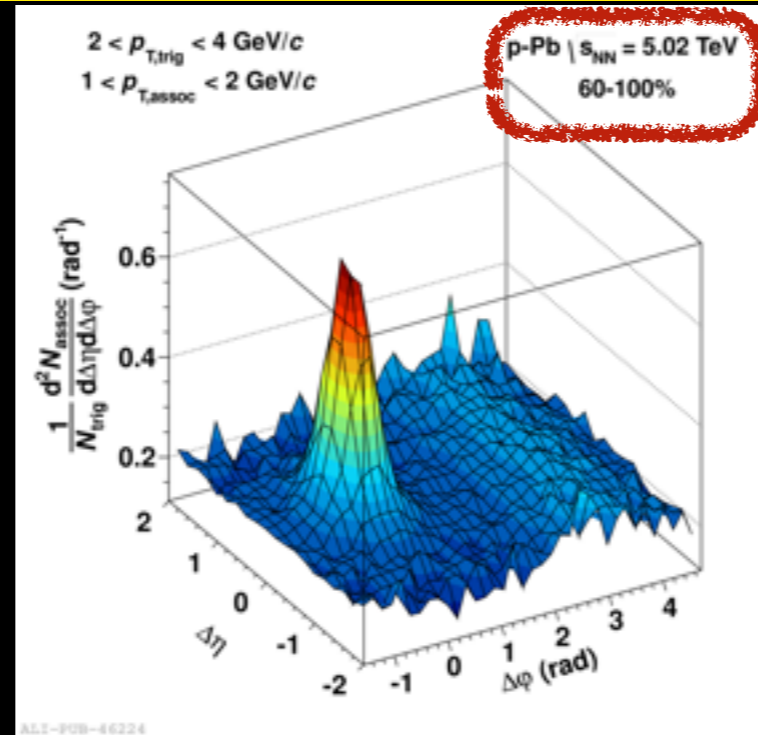
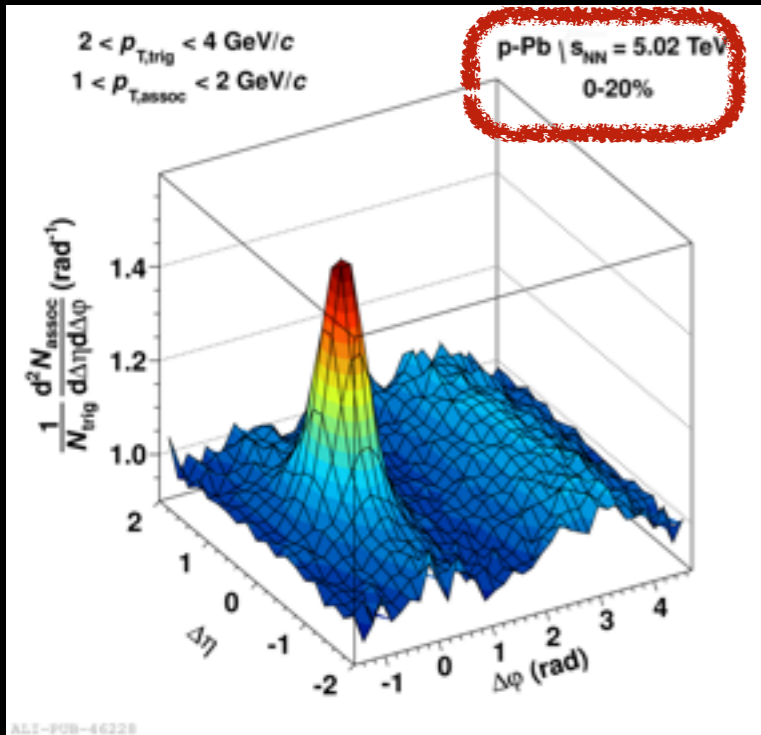
- Jet shape
- Balance functions



## Testing the Chiral Magnetic Effect



ALICE Collaboration: Phys. Lett. **B719**, (2013) 29



$$\frac{1}{N_{\text{trig}}} \frac{d^2 N_{\text{assoc}}}{d\Delta\eta d\Delta\varphi} \frac{S(\Delta\eta, \Delta\varphi)}{B(\Delta\eta, \Delta\varphi)}$$

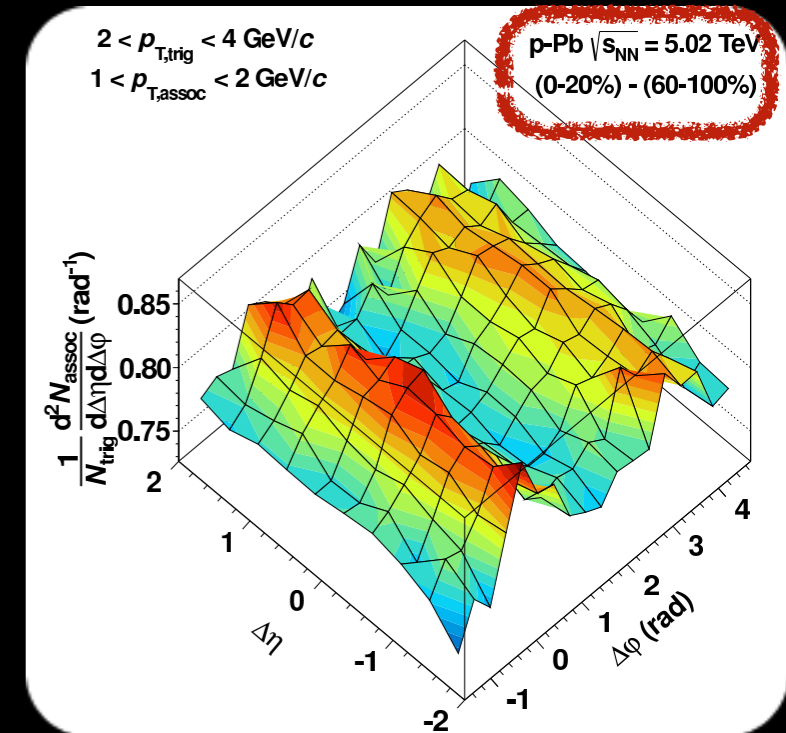
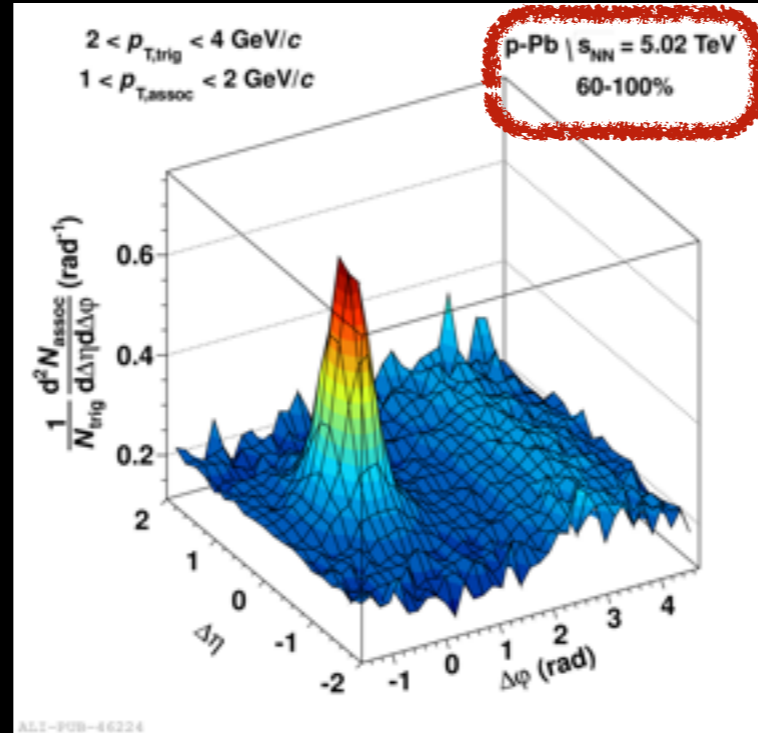
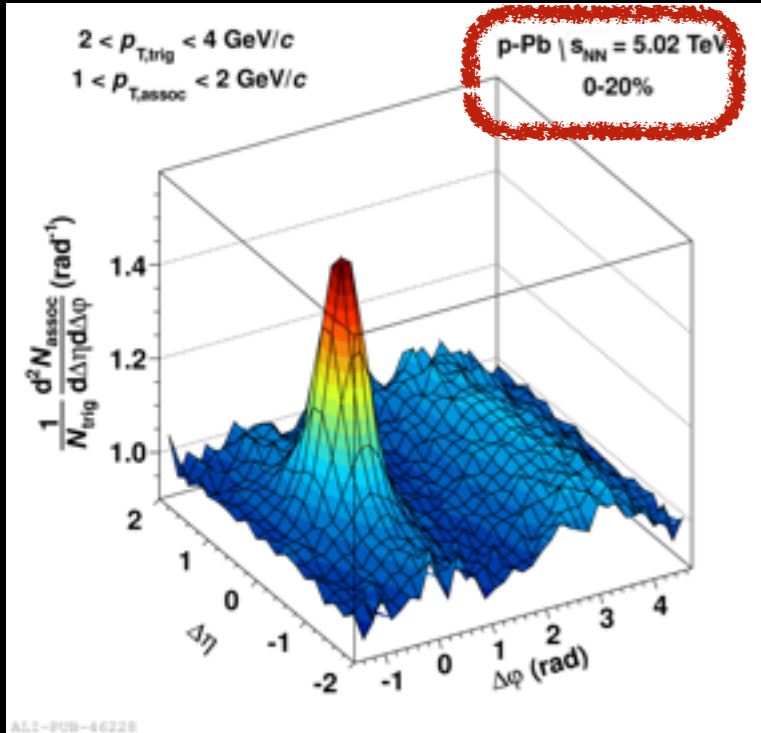
$$S(\Delta\eta, \Delta\varphi) = \left( \frac{1}{N_{\text{trig}}} \frac{d^2 N_{\text{assoc}}}{d\Delta\eta d\Delta\varphi} \right)_{\text{same}}$$

$$B(\Delta\eta, \Delta\varphi) = a \left( \frac{d^2 N_{\text{assoc}}}{d\Delta\eta d\Delta\varphi} \right)_{\text{mixed}}$$

- Near side ridge is observed in central p-Pb collisions

Andreas Morsch (25/7 Plenary session@ 11:30)

ALICE Collaboration: Phys. Lett. **B719**, (2013) 29



$$\frac{1}{N_{trig}} \frac{d^2 N_{assoc}}{d\Delta\eta d\Delta\phi} \frac{S(\Delta\eta, \Delta\phi)}{B(\Delta\eta, \Delta\phi)}$$

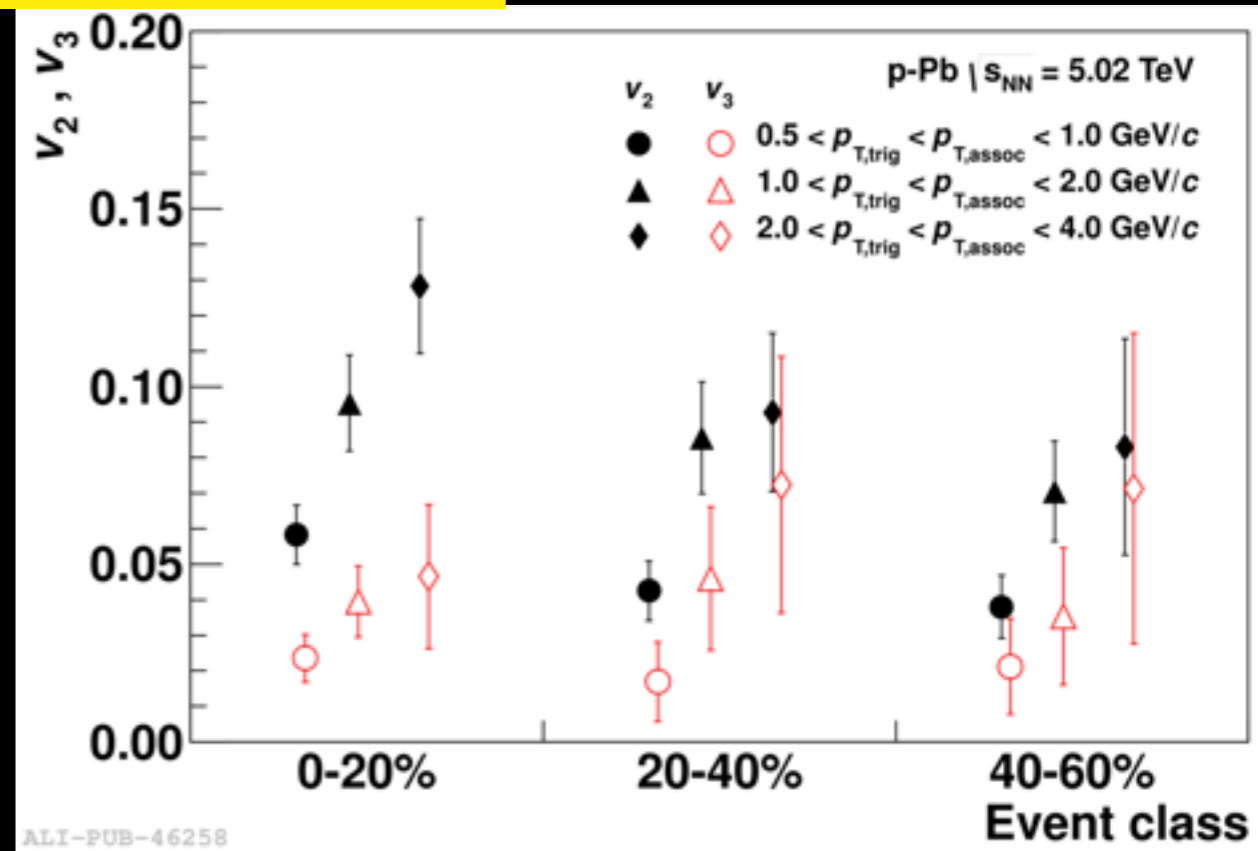
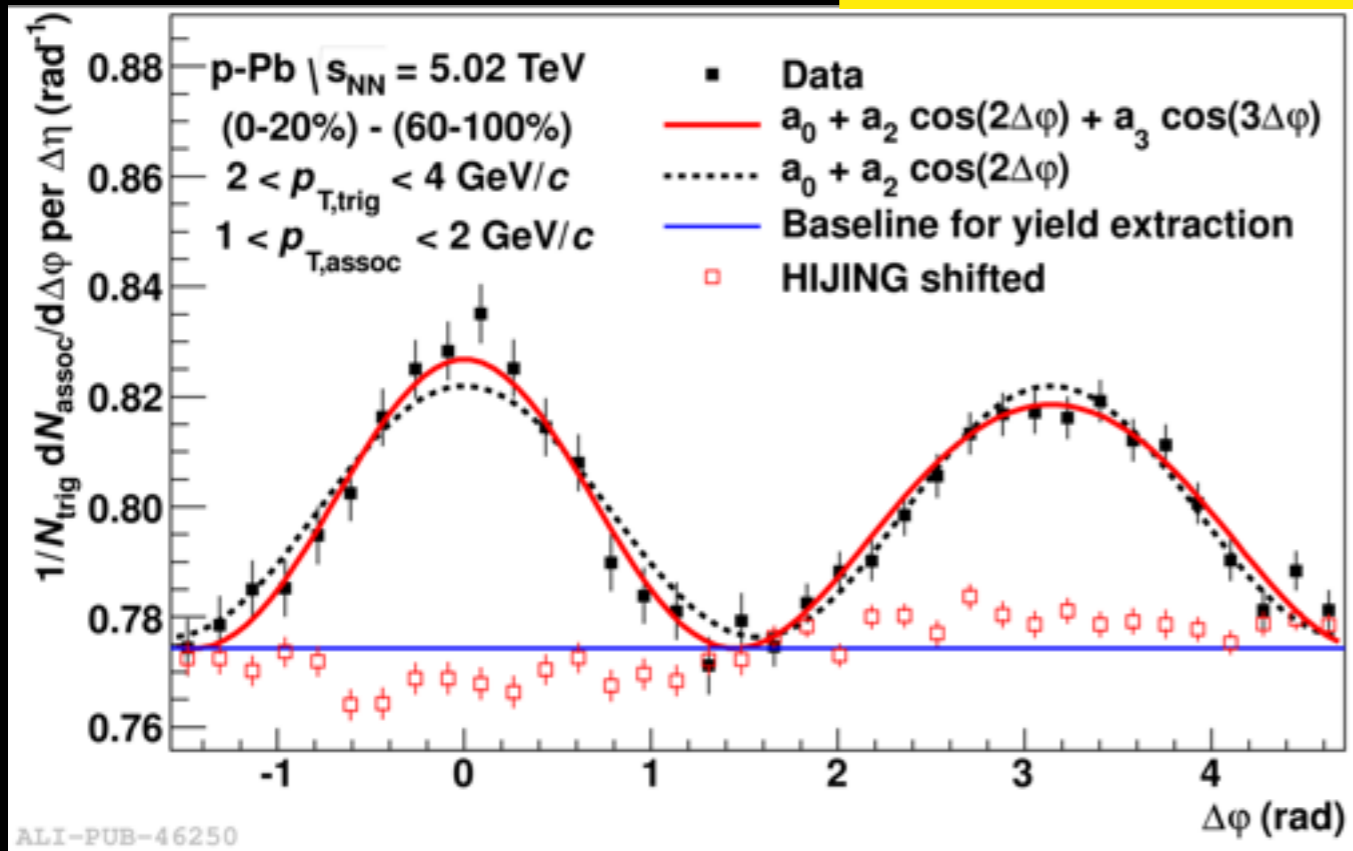
$$S(\Delta\eta, \Delta\phi) = \left( \frac{1}{N_{trig}} \frac{d^2 N_{assoc}}{d\Delta\eta d\Delta\phi} \right)_{same}$$

$$B(\Delta\eta, \Delta\phi) = a \left( \frac{d^2 N_{assoc}}{d\Delta\eta d\Delta\phi} \right)_{mixed}$$

- Near side ridge is observed in central p-Pb collisions
- Subtraction of the jet component i.e. as measured in the 60-100% centrality class reveals
- ★ a double symmetric ridge on the near and the away side!

Andreas Morsch (25/7 Plenary session@ 11:30)

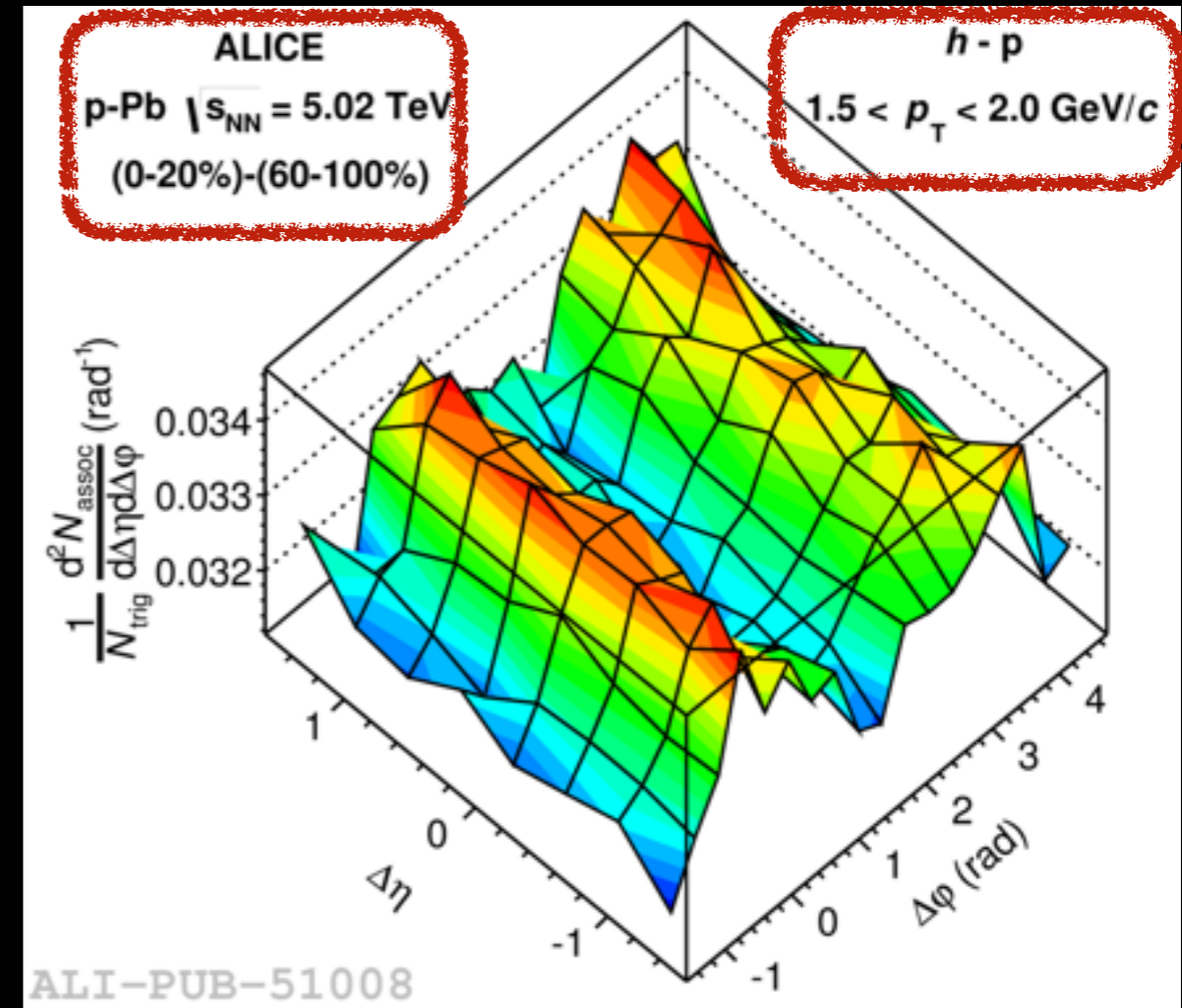
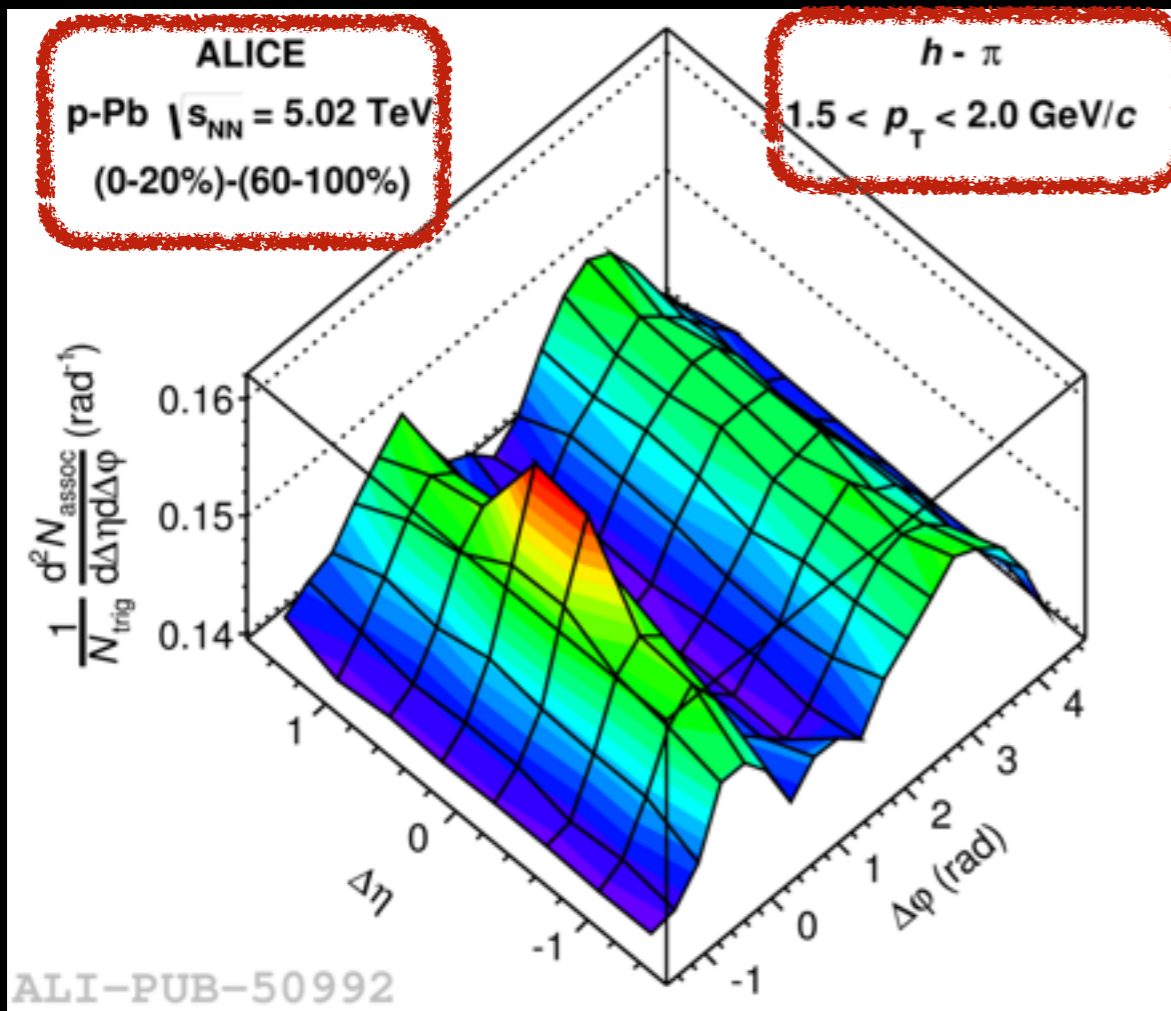
ALICE Collaboration: Phys. Lett. B719, (2013) 29



$$\frac{1}{N_{trig}} \frac{dN_{assoc}}{d\Delta\phi} = a_0 + a_2 \cos(2\Delta\phi) + a_3 \cos(3\Delta\phi)$$

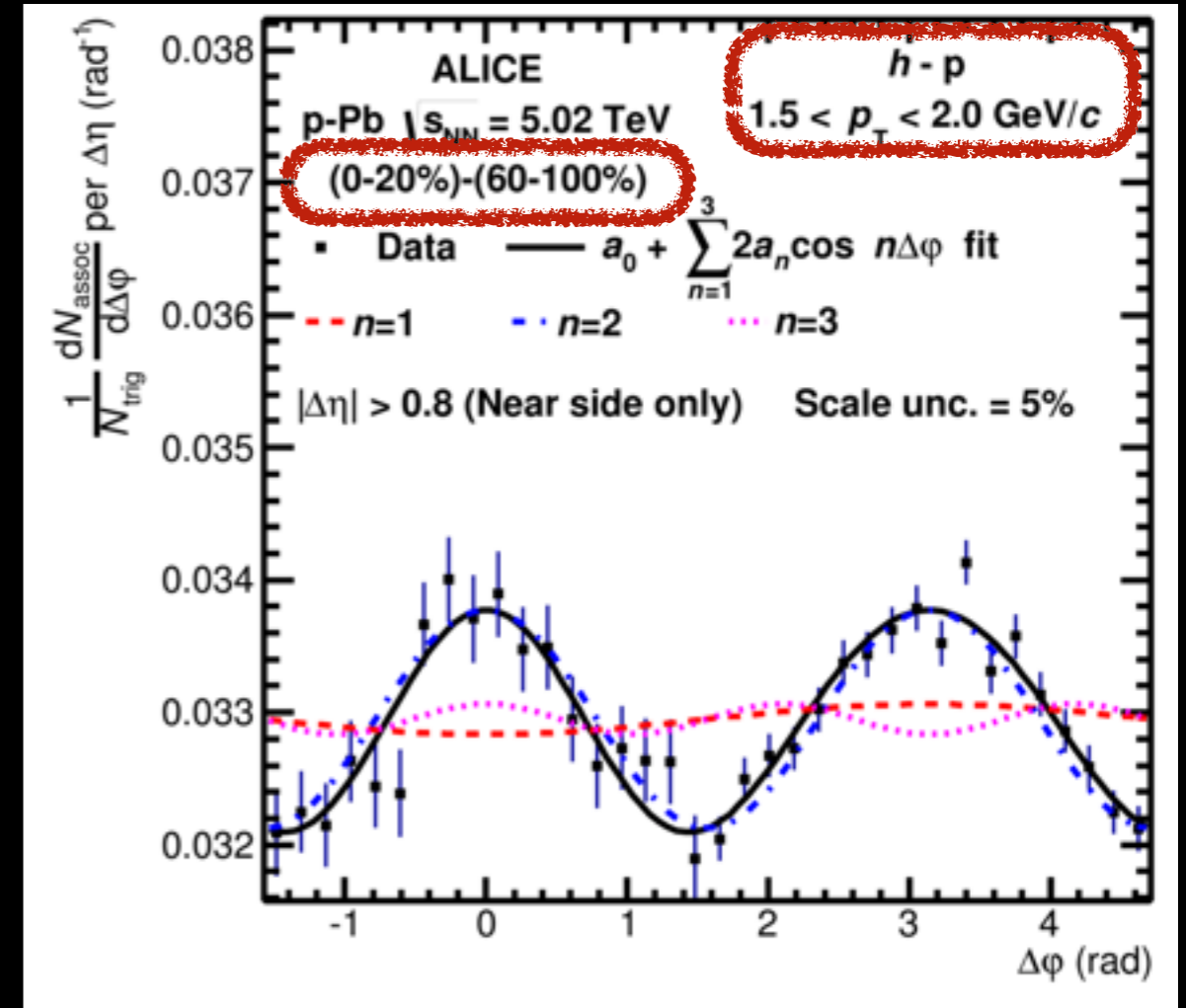
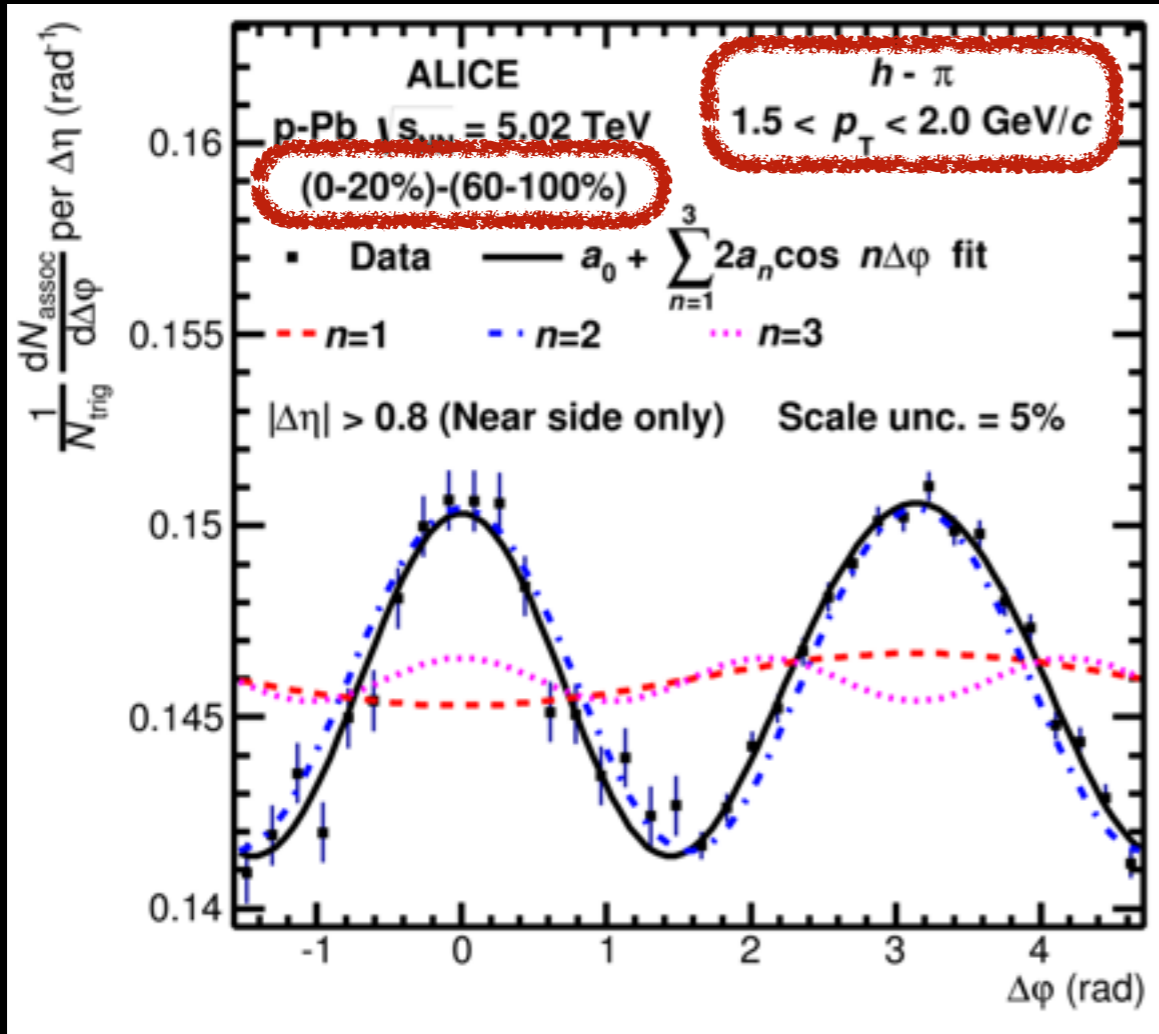
- Fourier decomposition using the 2<sup>nd</sup> and the 3<sup>rd</sup> harmonic
- $v_2$  and  $v_3$  increase with increasing  $p_T$ , while exhibiting a mild multiplicity dependence
- In qualitative agreement with hydro and CGC calculations

K.Dusling and R. Venugopalan, arXiv:1302.7018  
 P. Bozek and W. Broniowski, arXiv:1211.0845



- Similar analysis: charged particle  $\Rightarrow$  “trigger”, ( $\pi, K, p$ )  $\Rightarrow$  “associated”
- Jet component reduction: (0-20)% - (60-100)%
- Symmetric ridges in all cases i.e.  $\pi$ -h, K-h, p-h
- ★ Residual near side jet peak for  $\pi$ -h and to a smaller extent K-h

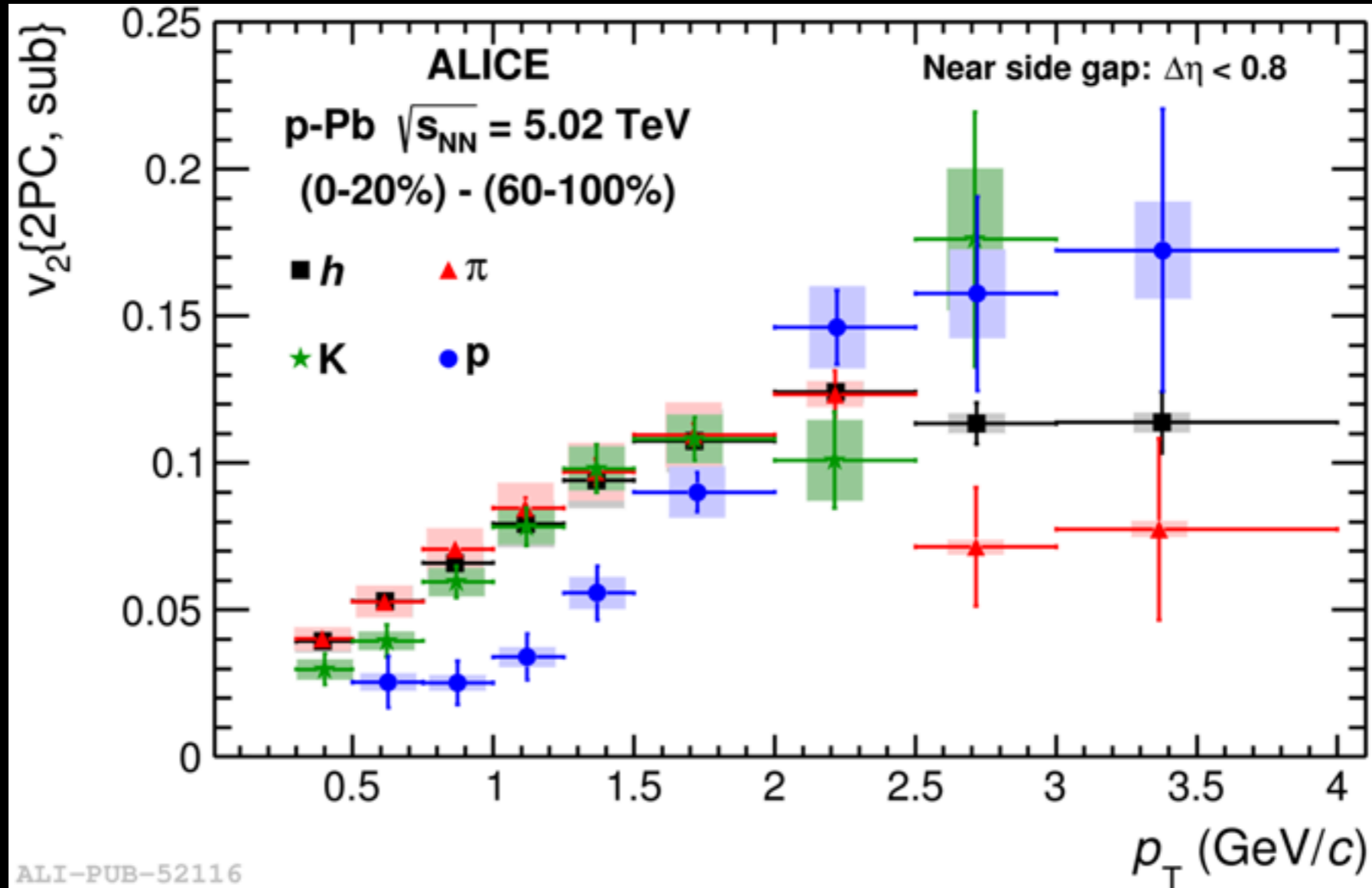
Leonardo Milano (26/7 Parallel session @ 15:20)



$$\frac{1}{N_{trig}} \frac{dN_{assoc}}{d\Delta\phi} = a_0 + a_1 \cos(\Delta\phi) + a_2 \cos(2\Delta\phi) + a_3 \cos(3\Delta\phi)$$

- After subtraction: symmetric double ridges for h- $\pi$ , h-K, h-p
- Small contribution from the odd coefficients

Leonardo Milano (26/7 Parallel session @ 15:20)

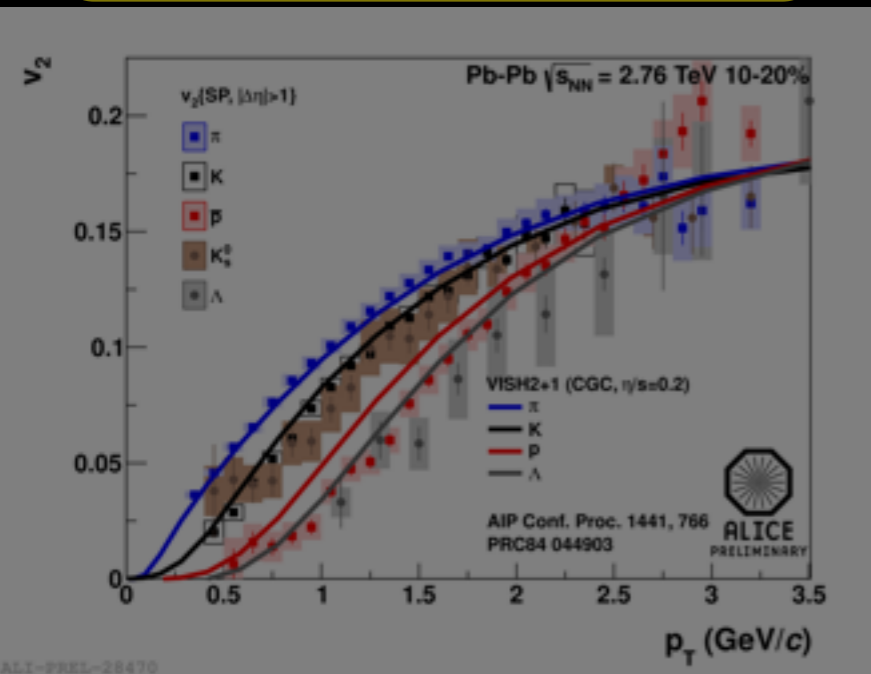


- Mass splitting observed in p-Pb collisions!
- Qualitatively similar picture as in Pb-Pb
- ★ Qualitatively consistent with a system that develops some degree of collective behavior

Leonardo Milano (26/7 Parallel session @ 15:20)

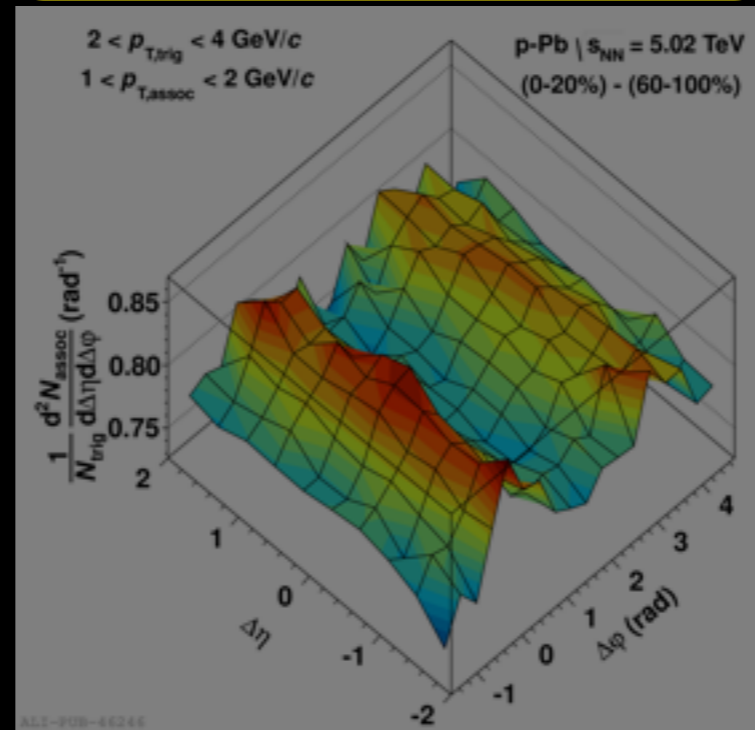
## Flow results in Pb-Pb

- Directed flow measurements
- Flow fluctuations at high  $p_T$  and at forward  $\eta$
- Symmetry plane correlations
- Identified particle  $v_2$  in Pb-Pb



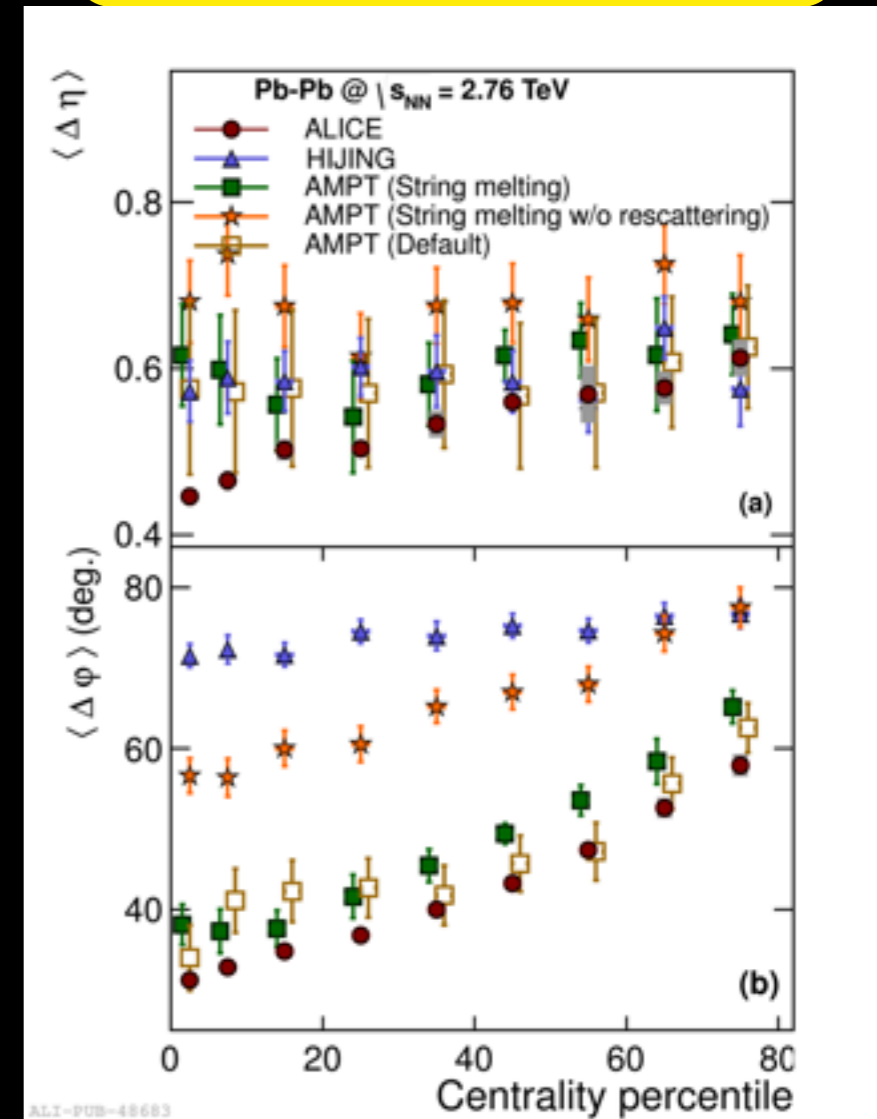
## Particle correlations in p-Pb

- Double ridge
- Identified particle correlations

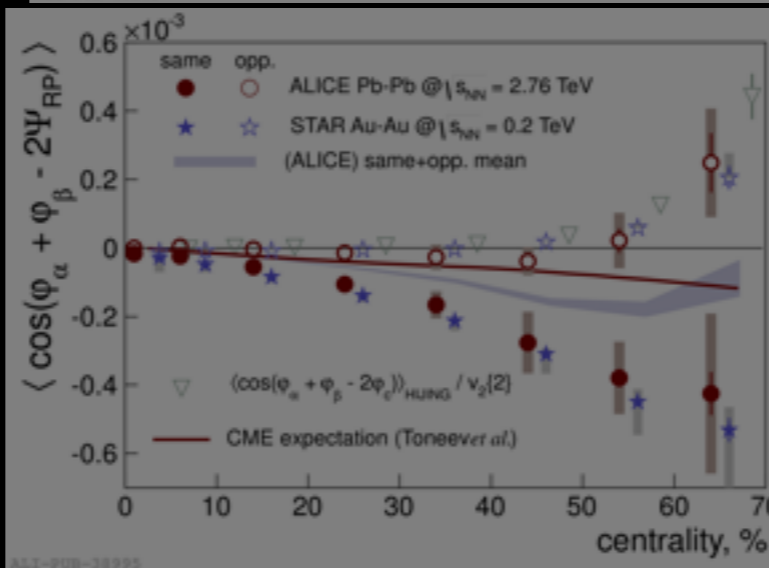


## Two-particle correlations in Pb-Pb

- Jet shape
- Balance functions



## Testing the Chiral Magnetic Effect





N. Armesto *et al.*, Phys. Rev. Lett., **93**, (2004) 242301

- Investigate potential changes in the near-side peak shape
- Probe jet broadening when coupled to the longitudinally flowing medium

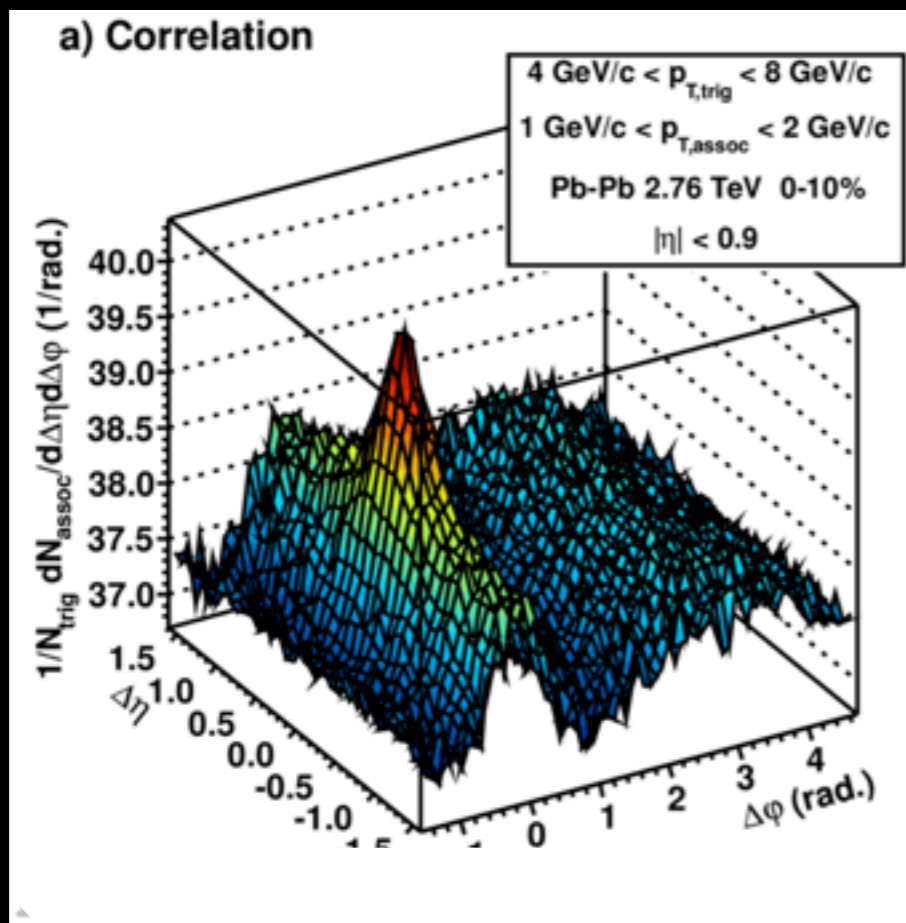
Marek Bombara (23/7 Parallel session@ 15:20)

N. Armesto *et al.*, Phys. Rev. Lett., **93**, (2004) 242301

- Investigate potential changes in the near-side peak shape
- Probe jet broadening when coupled to the longitudinally flowing medium

Associated yield per trigger particle from same and mixed events

$$\frac{1}{N_{trig}} \frac{d^2 N_{assoc}}{d\Delta\eta d\Delta\phi} \frac{S(\Delta\eta, \Delta\phi)}{B(\Delta\eta, \Delta\phi)}$$



Estimate  $\Delta\eta$  independent effects by quantifying the long range correlations ( $|\Delta\eta| > 1$ )

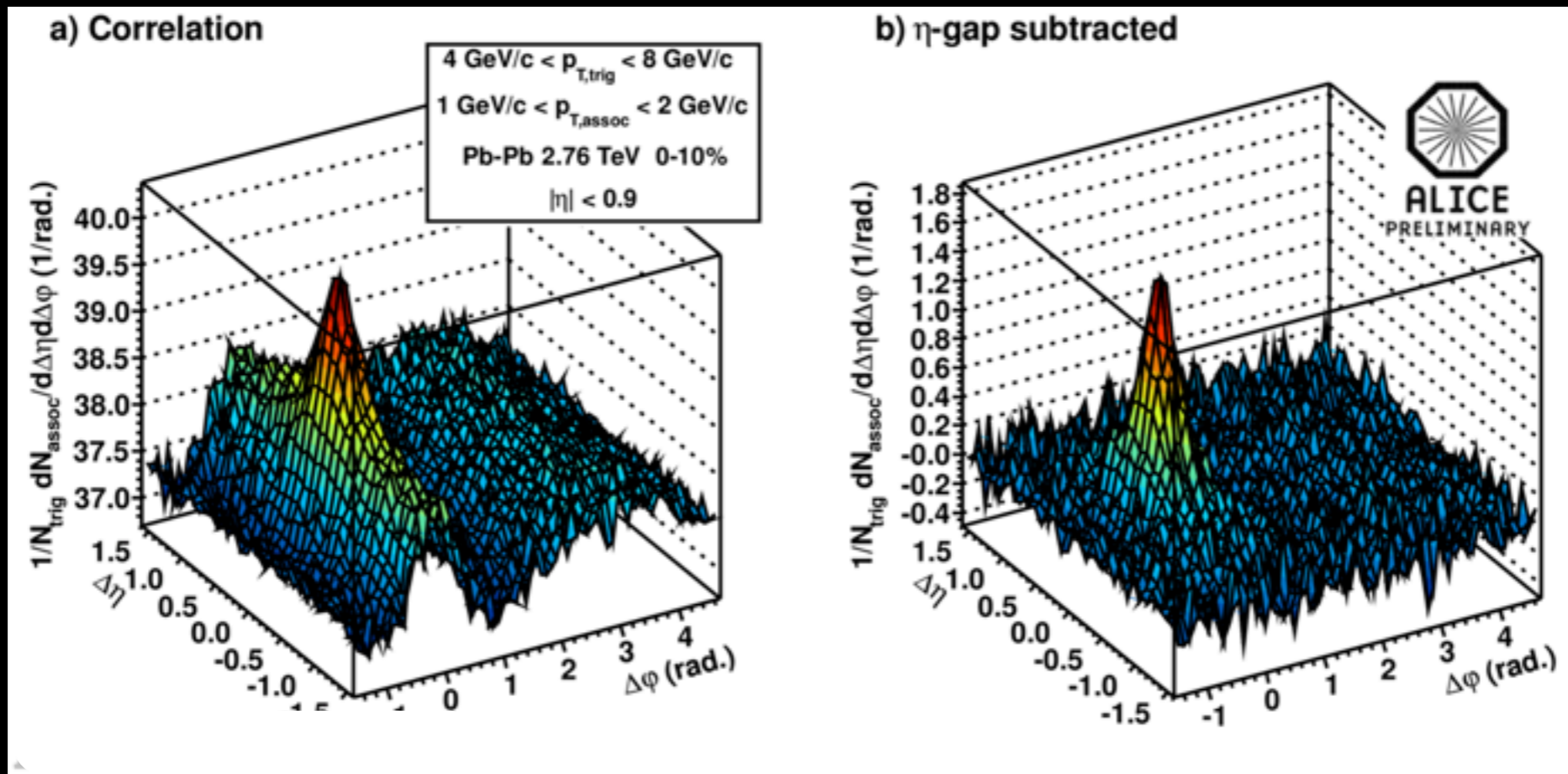
Marek Bombara (23/7 Parallel session@ 15:20)

N. Armesto *et al.*, Phys. Rev. Lett., **93**, (2004) 242301

- Investigate potential changes in the near-side peak shape
- Probe jet broadening when couple to the longitudinally flowing medium

Associated yield per trigger particle from same and mixed events

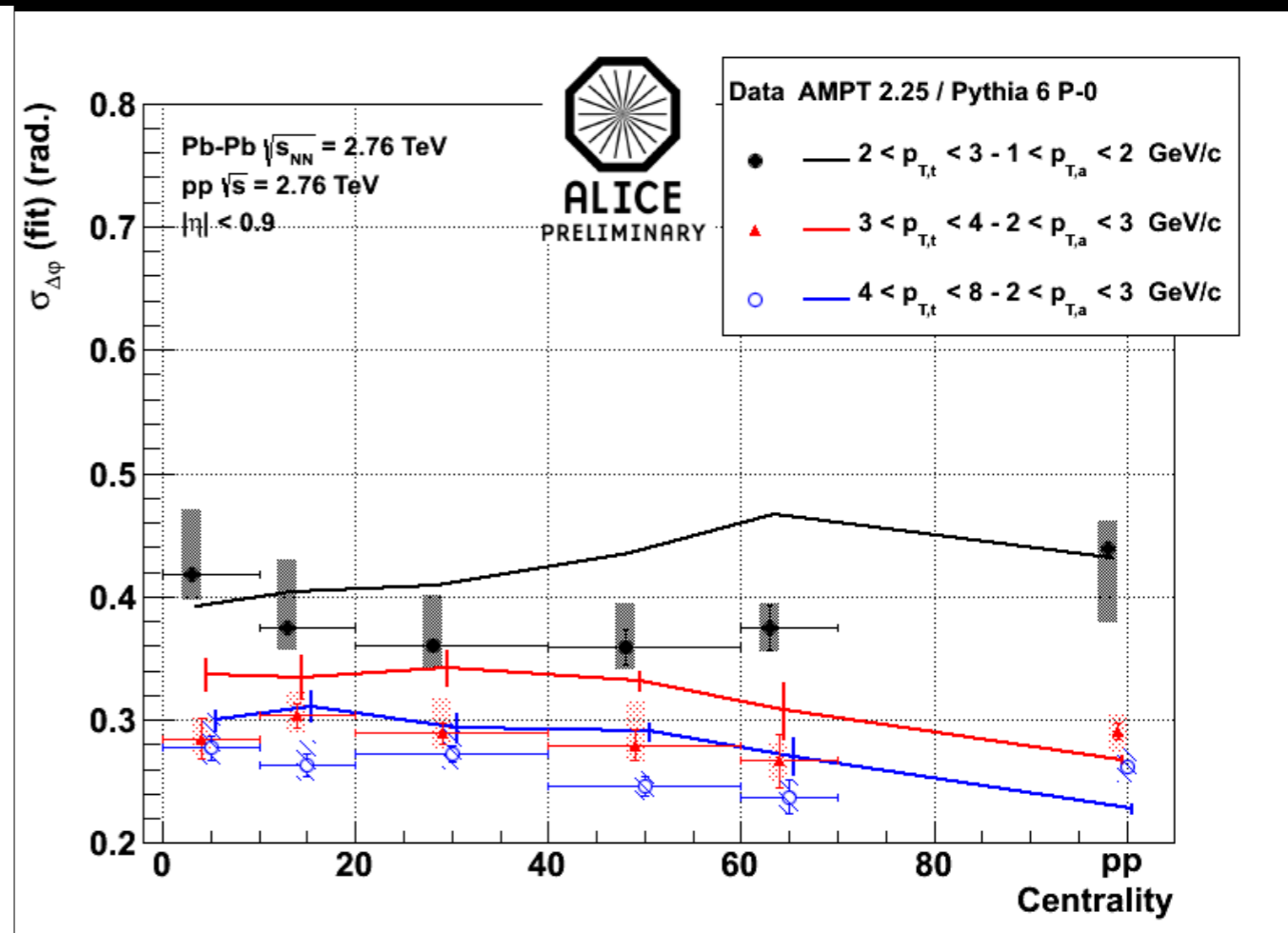
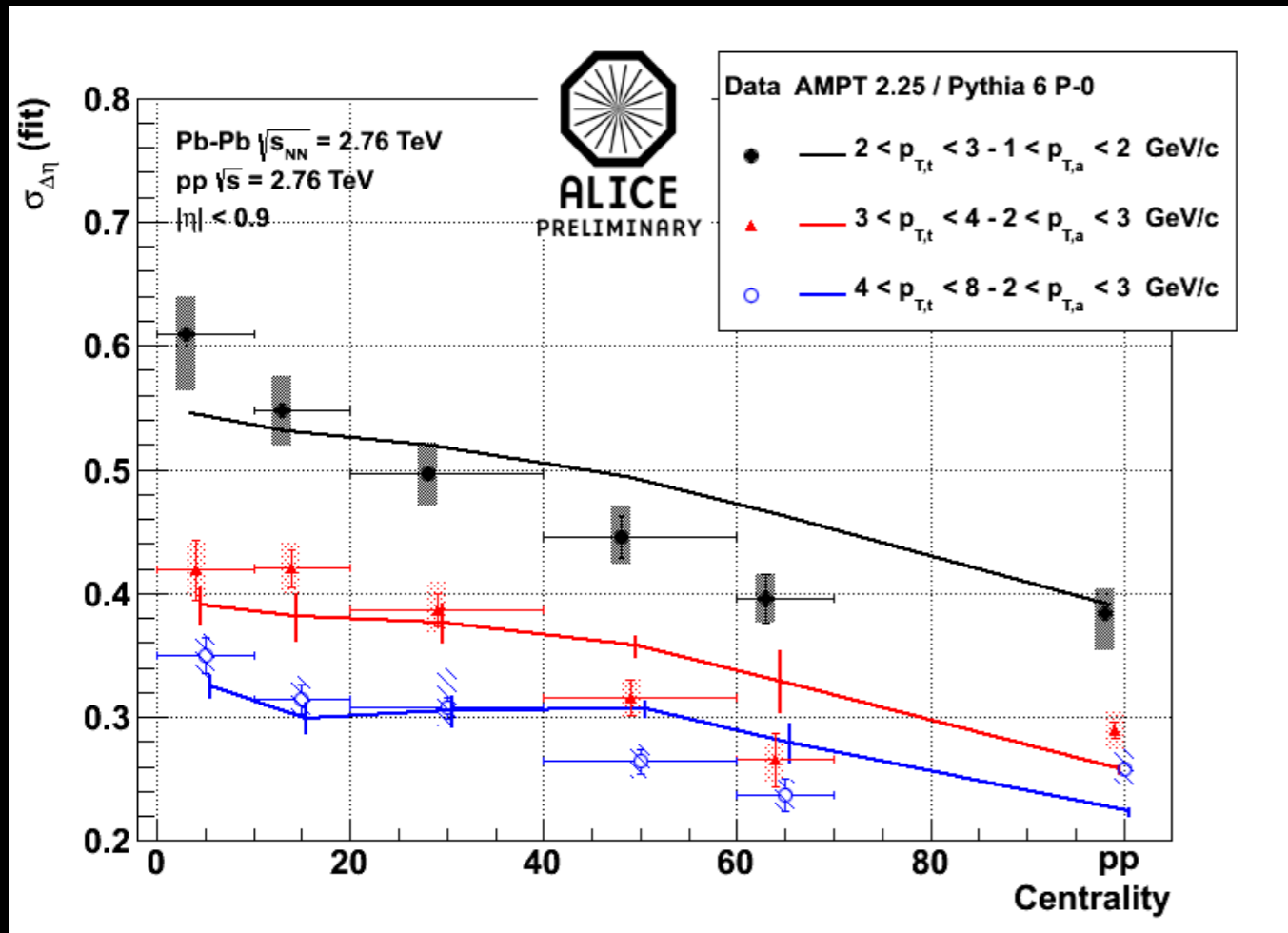
$$\frac{1}{N_{trig}} \frac{d^2 N_{assoc}}{d\Delta\eta d\Delta\phi} \frac{S(\Delta\eta, \Delta\phi)}{B(\Delta\eta, \Delta\phi)}$$



Estimate  $\Delta\eta$  independent effects by quantifying the long range correlations ( $|\Delta\eta| > 1$ )

Subtract from short range region ( $|\Delta\eta| < 1$ )

Marek Bombara (23/7 Parallel session@ 15:20)



- Significant centrality dependence for  $\sigma_{\Delta\eta}$  but mild effect for  $\sigma_{\Delta\phi}$
- AMPT describes fairly well the data points
- Interplay of jets with flow?

Marek Bombara (23/7 Parallel session@ 15:20)

S. Bass, P. Danielewicz and S. Pratt ,  
Phys. Rev. Lett. **85**, (2000) 2689

$$B_{+-}(\Delta\eta, \Delta\phi, p_{T, trig}, p_{T, assoc}) = \frac{1}{2} (C_{US} - C_{LS})$$

$$C_{US}: C_{+-}, C_{-+}$$

$$C_{LS}: C_{++}, C_{--}$$

$$C_{+-} = \left( \frac{N_{+-}}{N_{+}} \right) / f_{+-}$$

Detector acceptance and inefficiencies (mixed events or from convolution of single particle distributions)

particle pair density normalized to the number of trigger particles

S. Bass, P. Danielewicz and S. Pratt, Phys. Rev. Lett. **85**, (2000) 2689

$$B_{+-}(\Delta\eta, \Delta\phi, p_{T, trig}, p_{T, assoc}) = \frac{1}{2} (C_{US} - C_{LS})$$

$$C_{US}: C_{+-}, C_{-+}$$

$$C_{LS}: C_{++}, C_{--}$$

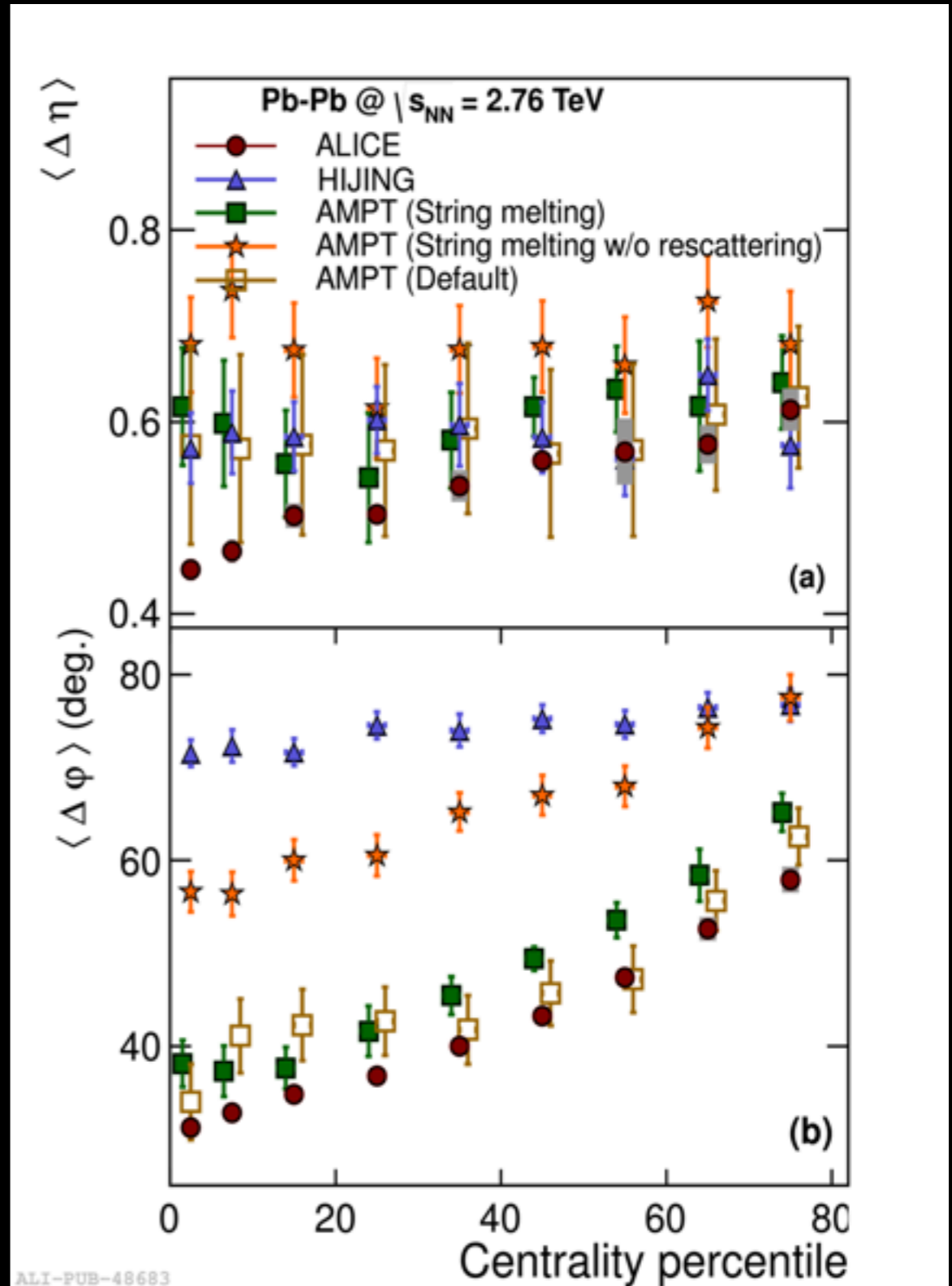
$$C_{+-} = \left( \frac{N_{+-}}{N_+} \right) / f_{+-}$$

Detector acceptance and inefficiencies (mixed events or from convolution of single particle distributions)

particle pair density normalized to the number of trigger particles

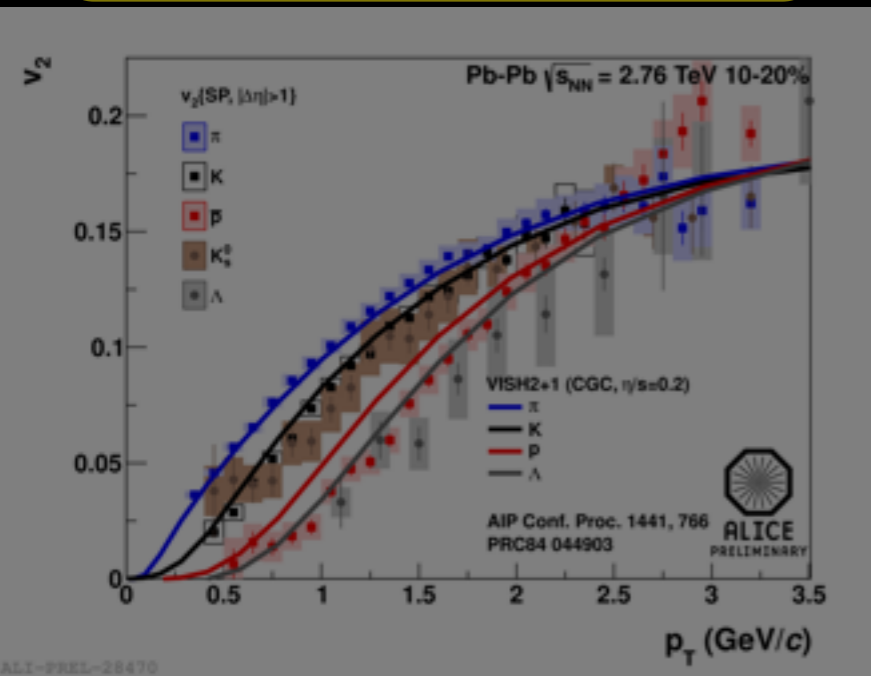
- Width probes the formation time of balancing charges (affected also by radial flow)
- Data: strong centrality dependence
- ★ Consistent with the idea of late stage creation of charges focused by radial flow
- Models that incorporate collective effects (e.g. AMPT) in quantitative agreement with data (for  $\Delta\phi$ )

ALICE Collaboration: Phys. Lett. **B723**, (2013) 267



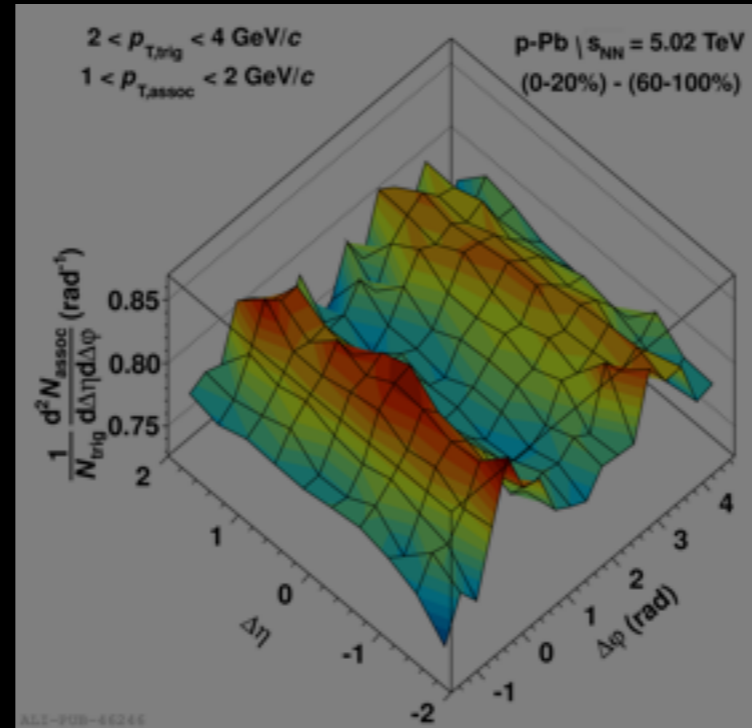
## Flow results in Pb-Pb

- Directed flow measurements
- Flow fluctuations at high  $p_T$  and at forward  $\eta$
- Symmetry plane correlations
- Identified particle  $v_2$  in Pb-Pb



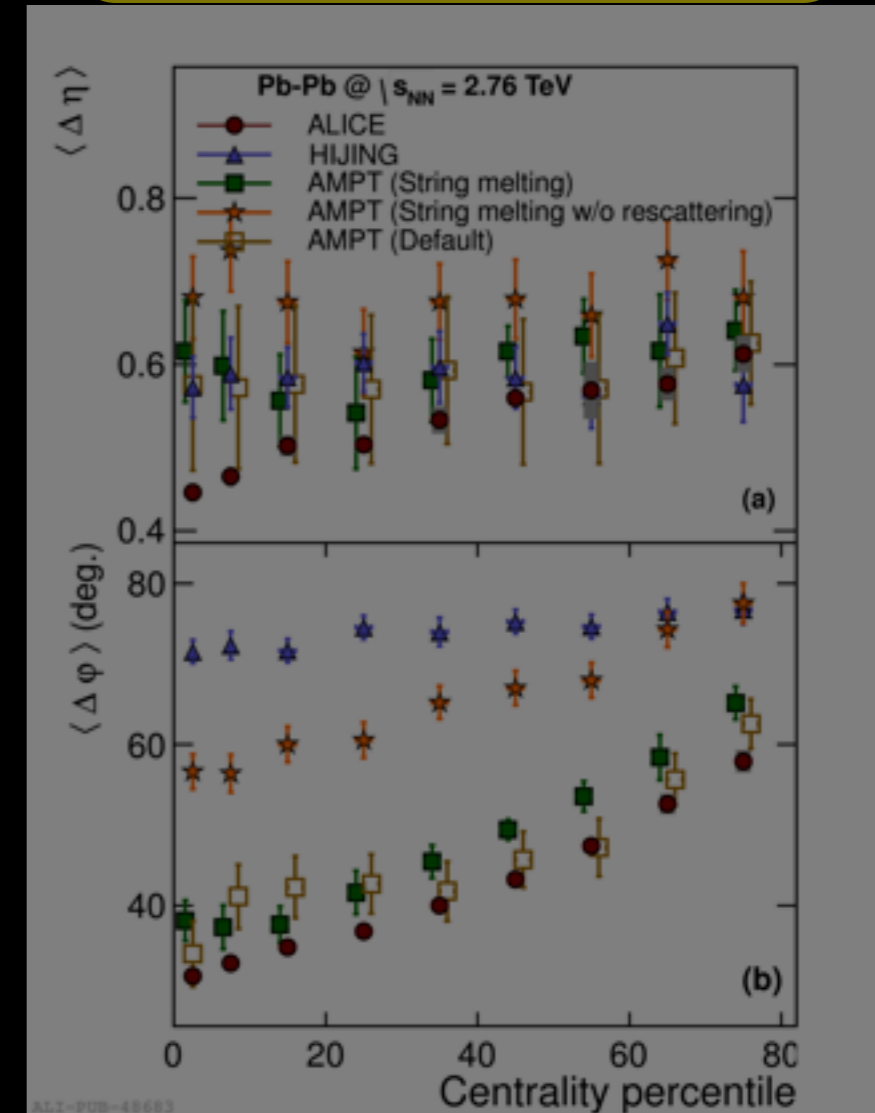
## Particle correlations in p-Pb

- Double ridge
- Identified particle correlations

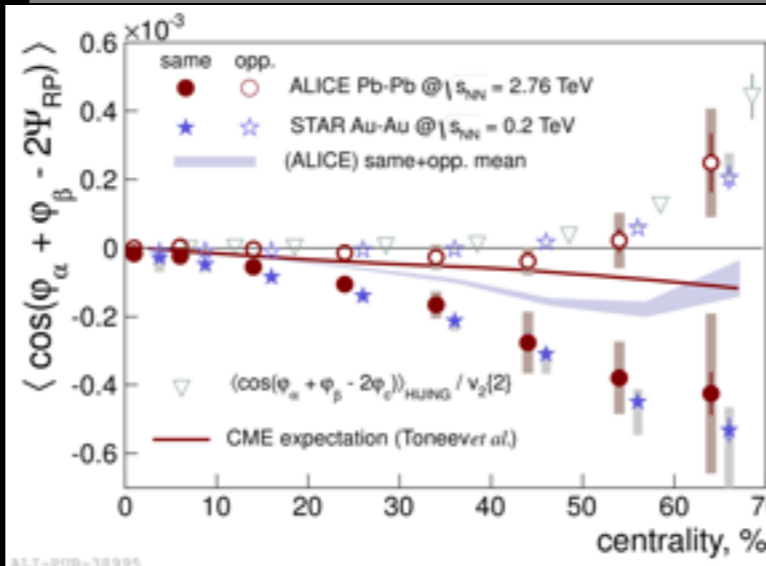


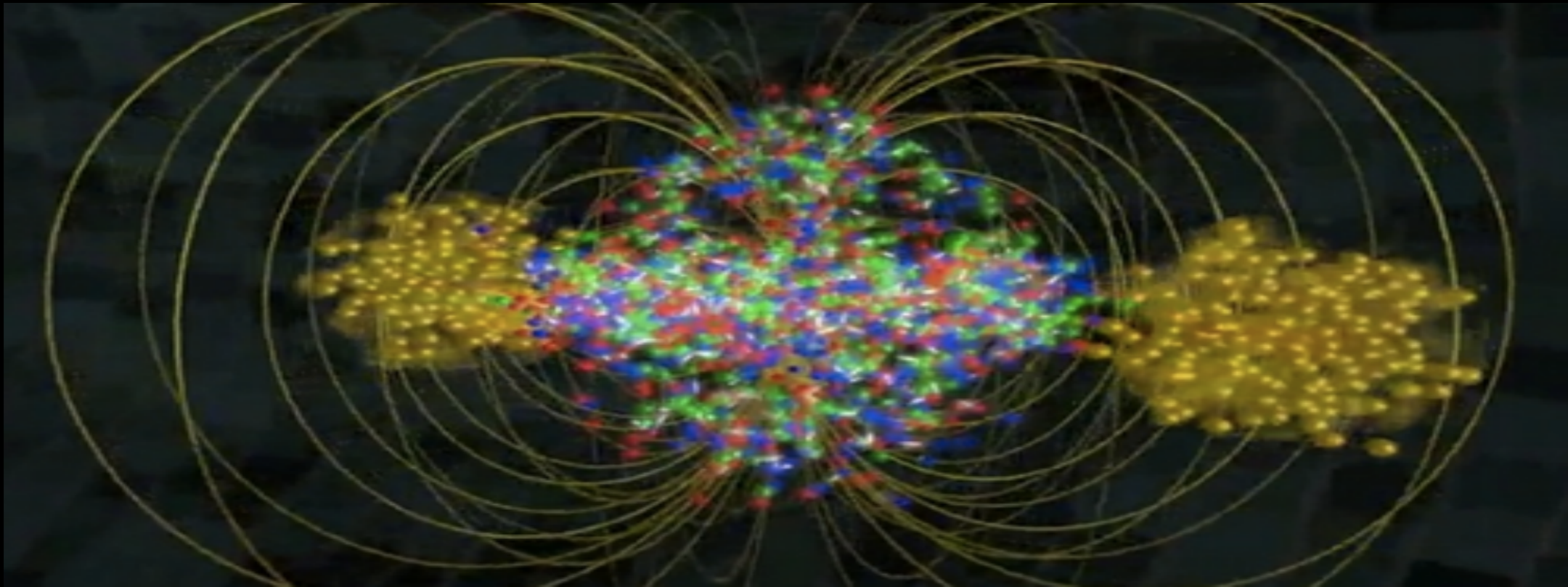
## Two-particle correlations in Pb-Pb

- Jet shape
- Balance functions



## Testing the Chiral Magnetic Effect

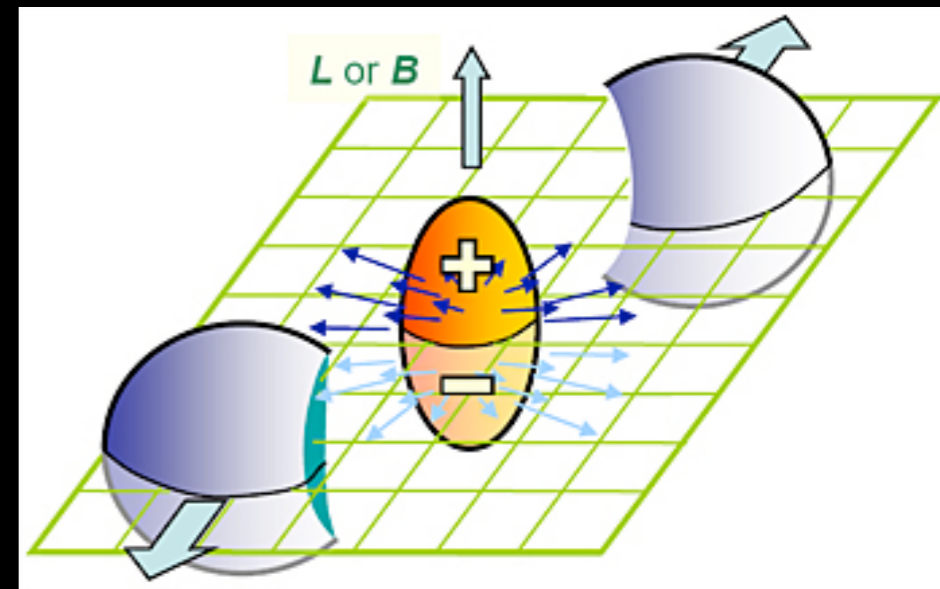




- Ions collide  $\Rightarrow$  strong magnetic field ( $\sim 10^{17} - 10^{19}$  G!!!)
- Deconfined phase (if conditions are satisfied)
- Theory: excited QCD vacuum states (domains)  $\Rightarrow$  P and CP invariance locally broken
- Interaction of quarks with these domains and with the magnetic field  $\Rightarrow$  spin alignment and development of an E/M current

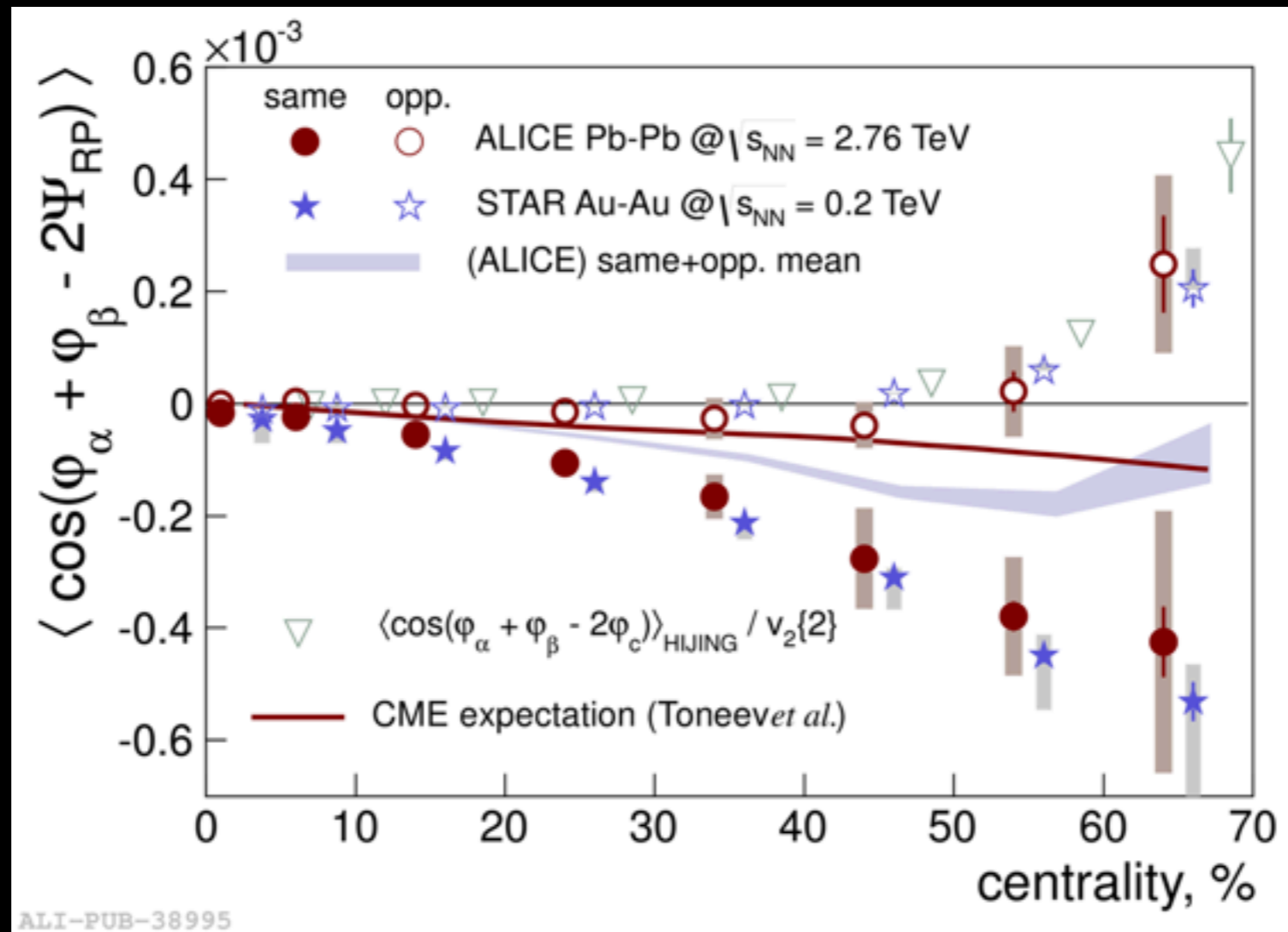
EDM of QCD matter

Experimental consequence: charge asymmetry wrt to  $\Psi_2$



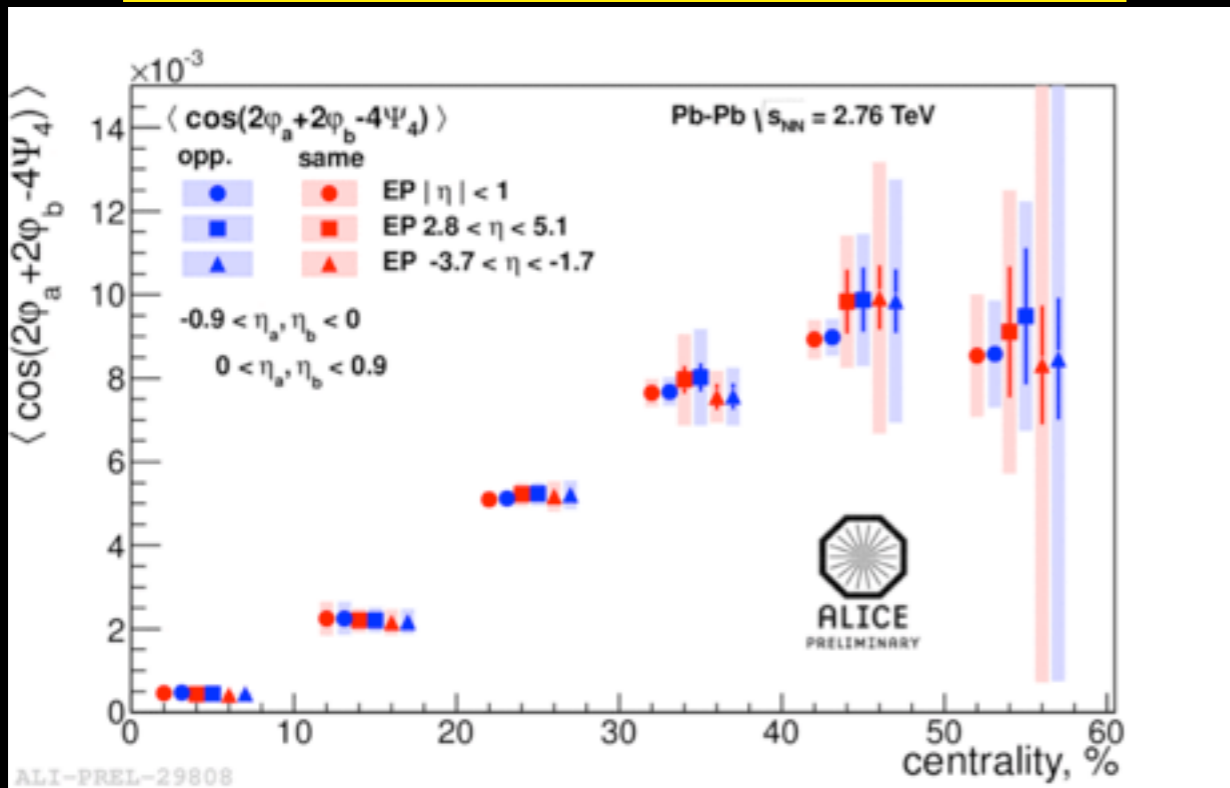


(ALICE Collaboration), Phys. Rev. Lett. **110**, (2013) 012301



- Results in qualitative agreement with the CME expectations
- Homework: disentangle background effects from potential CME signal
- ★ Background: local charge conservation (balance functions) +  $v_n$  modulations

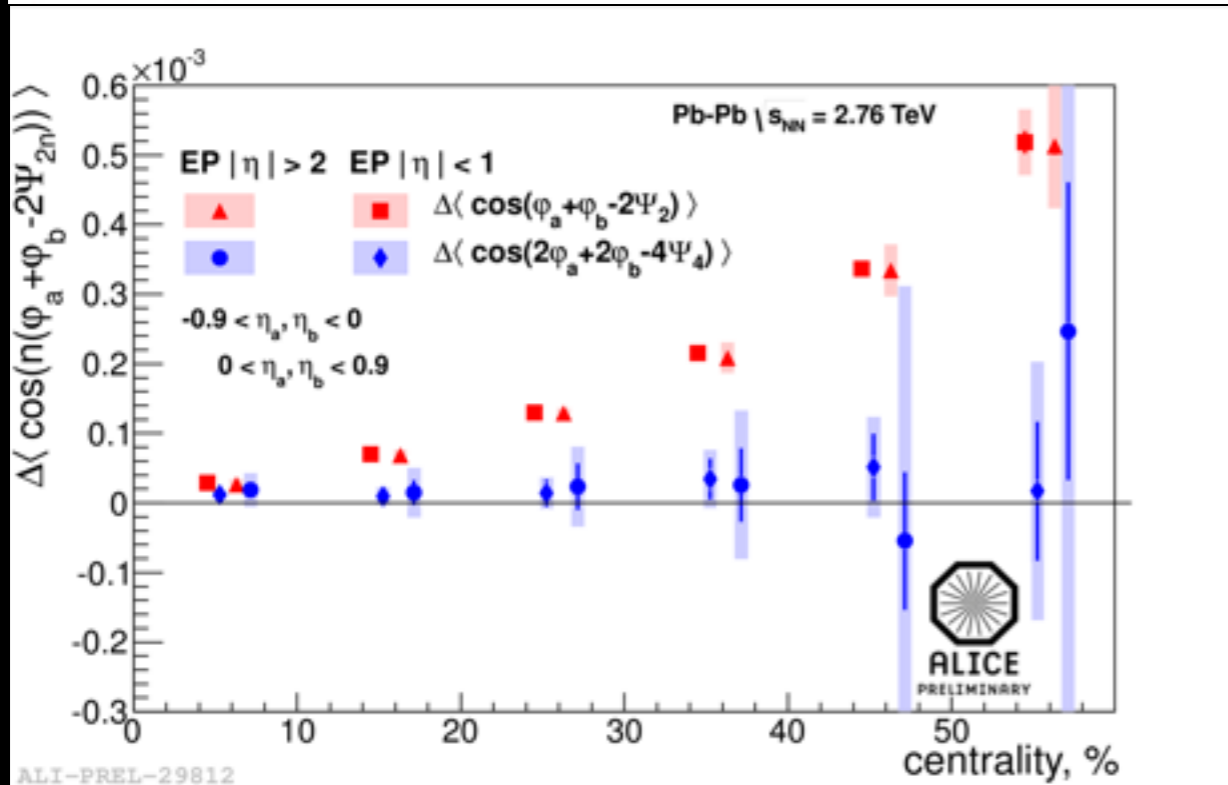
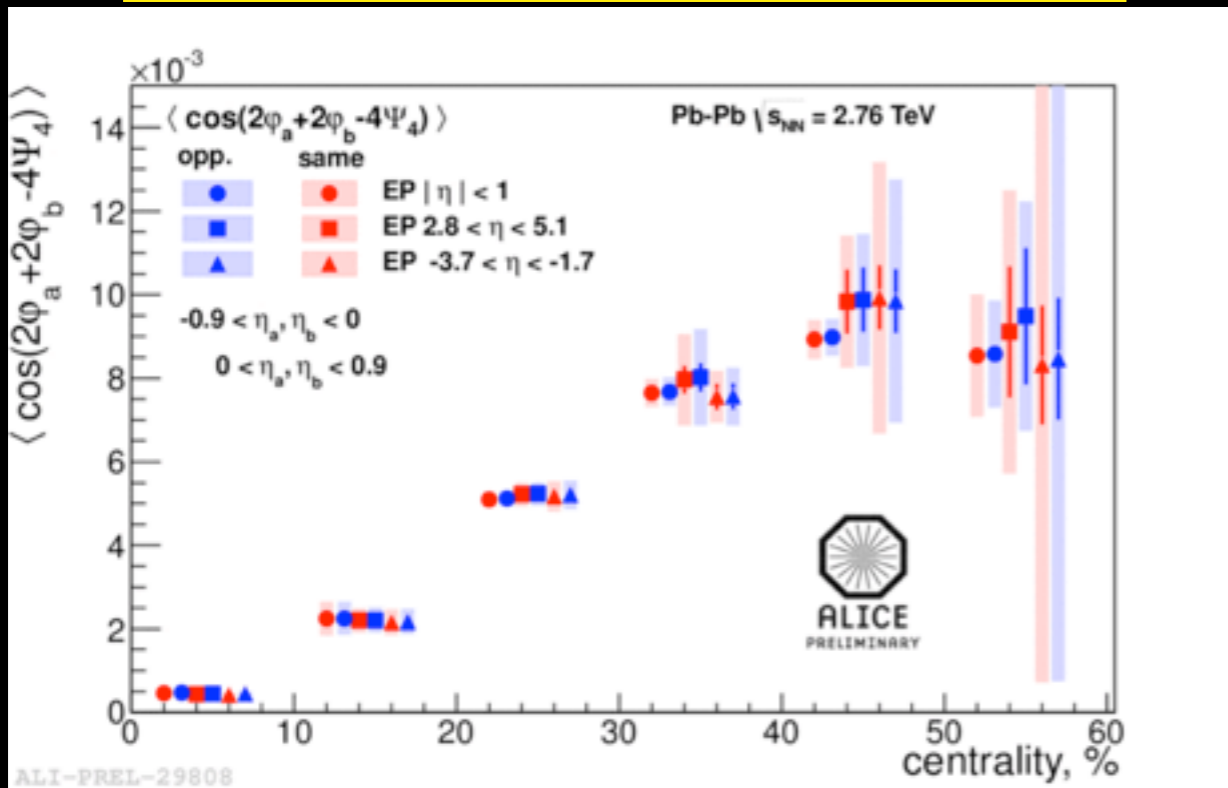
J. Mlynarz (ALICE Collaboration) @ QM2012



$$\langle \cos(2\varphi_\alpha + 2\varphi_\beta - 4\Psi_4) \rangle$$

- Charge independent correlations:
  - ★ elliptic flow fluctuations relative to the 4<sup>th</sup> order symmetry plane
- Charge dependent correlations:
  - ★ no contribution from CME
  - ★ contribution from local charge conservation +  $v_4$

J. Mlynarz (ALICE Collaboration) @ QM2012

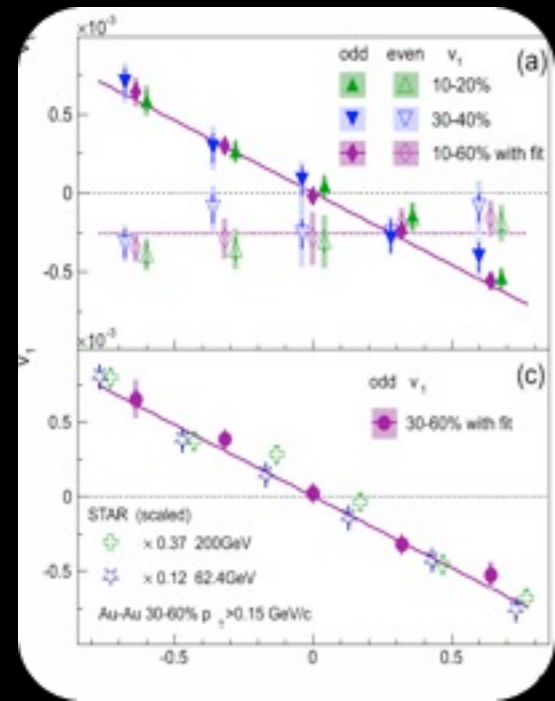


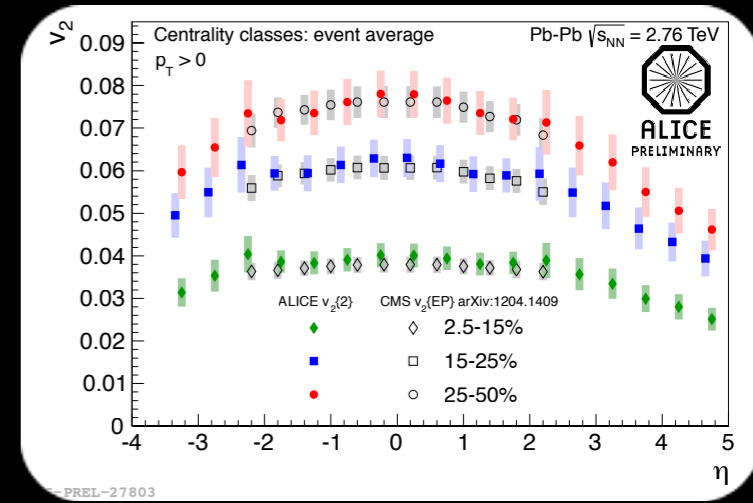
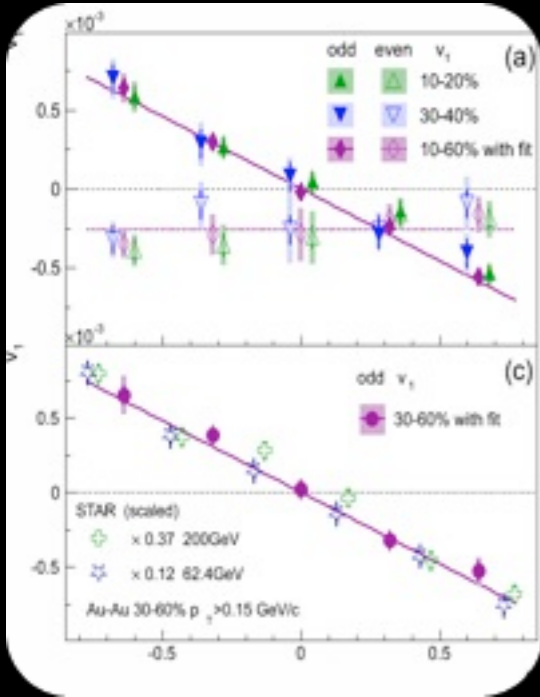
$$\langle \cos(2\varphi_\alpha + 2\varphi_\beta - 4\Psi_4) \rangle$$

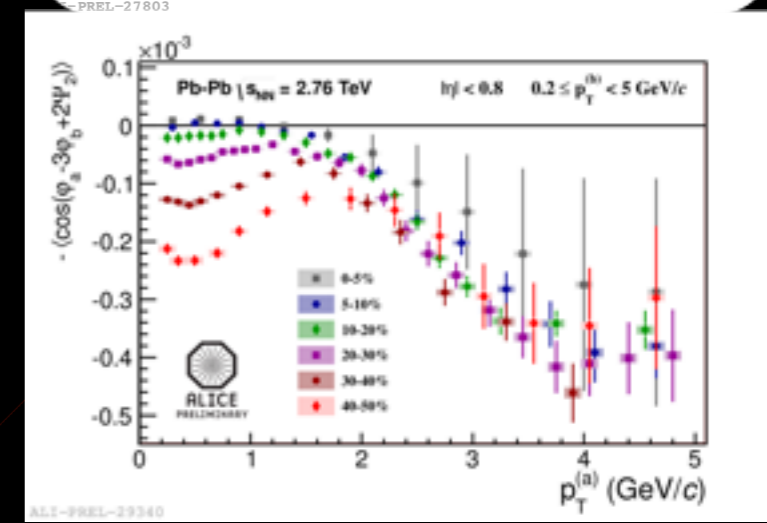
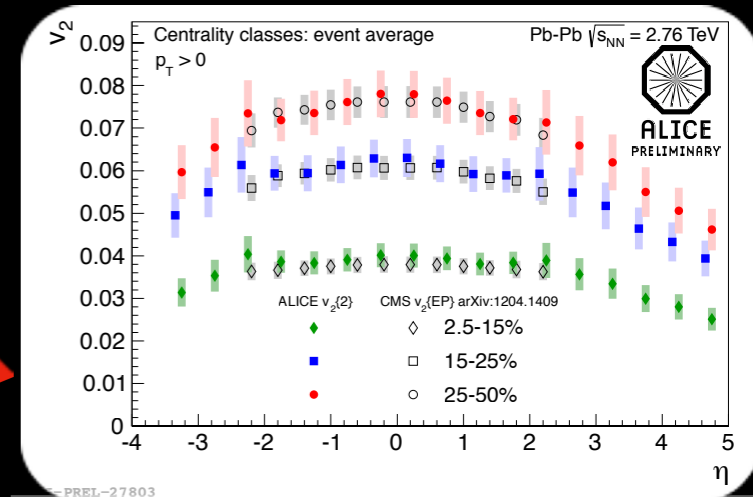
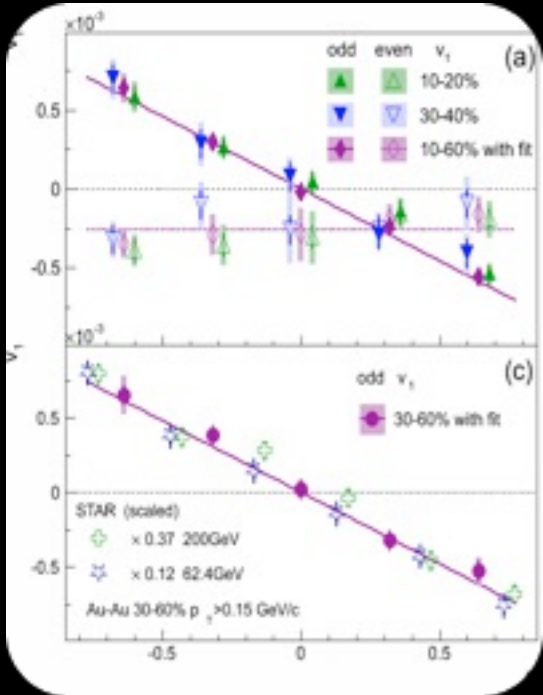
- Charge independent correlations:
  - ★ elliptic flow fluctuations relative to the 4<sup>th</sup> order symmetry plane
- Charge dependent correlations:
  - ★ no contribution from CME
  - ★ contribution from local charge conservation +  $v_4$

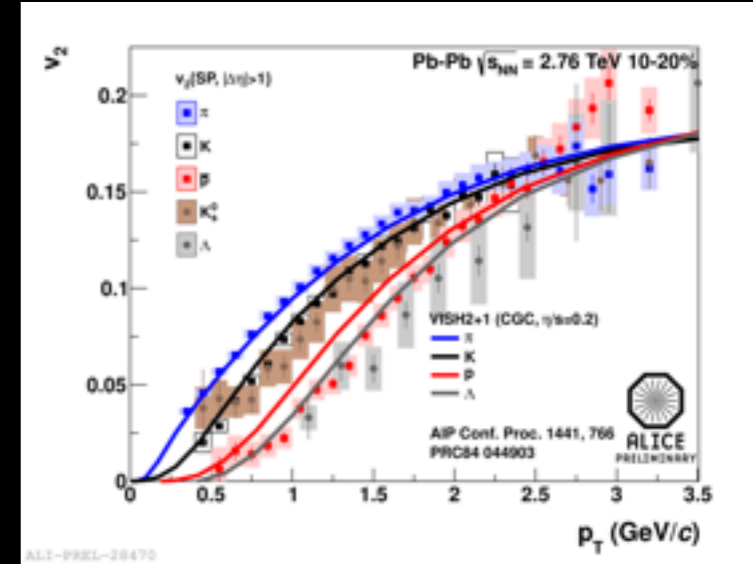
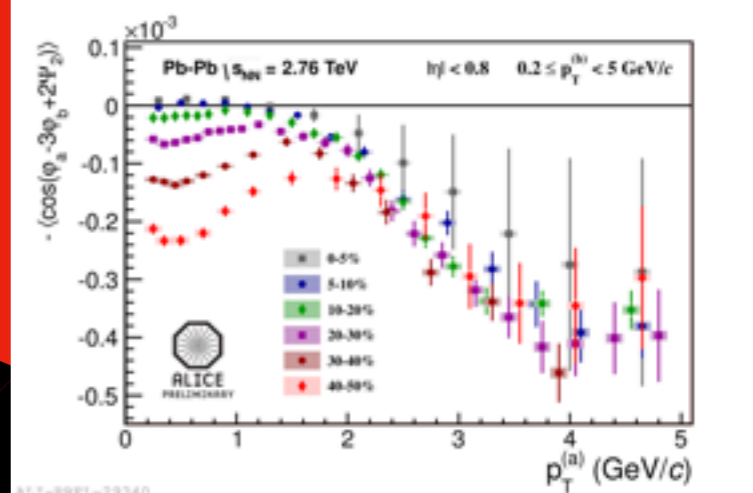
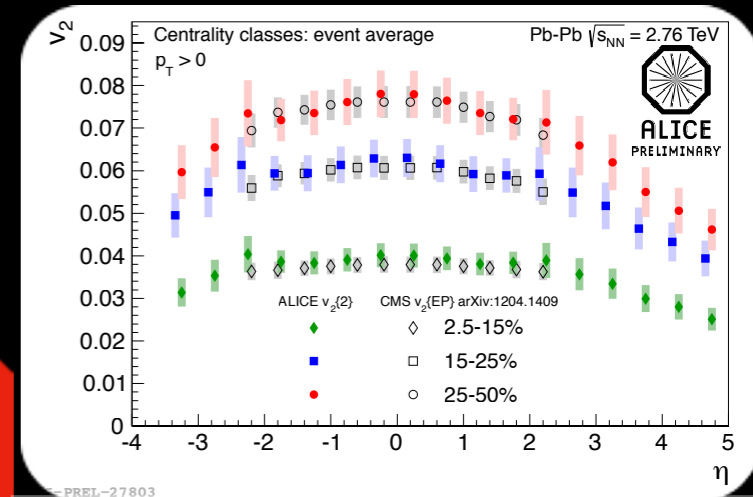
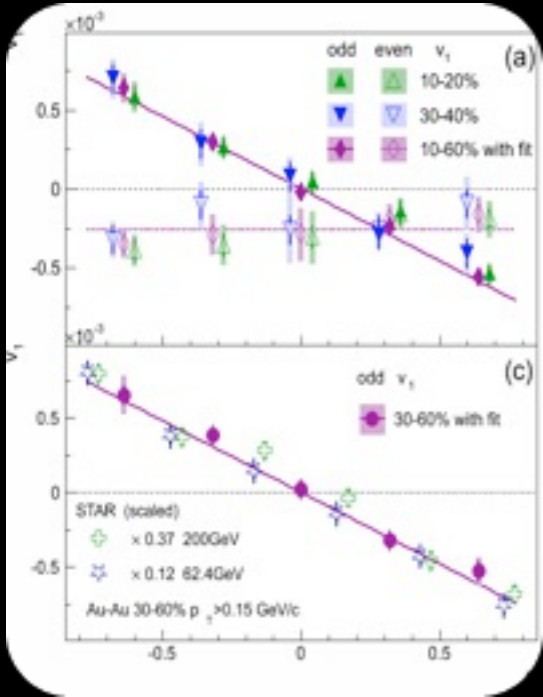
Results show no significant charge dependence within the current (large) statistical and systematic uncertainty  $\Rightarrow$  not significant contribution from background?



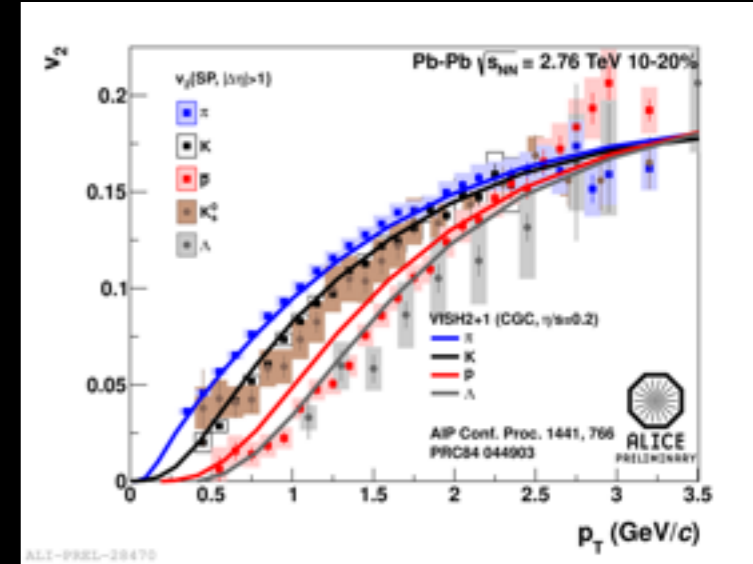
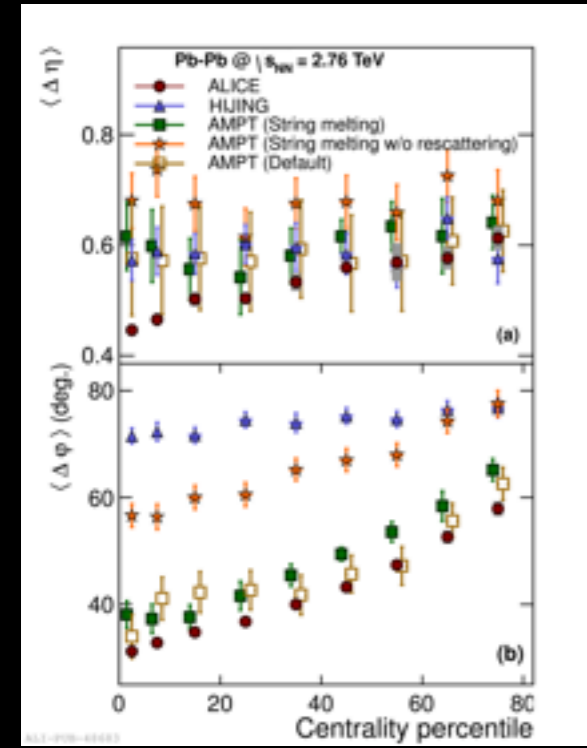
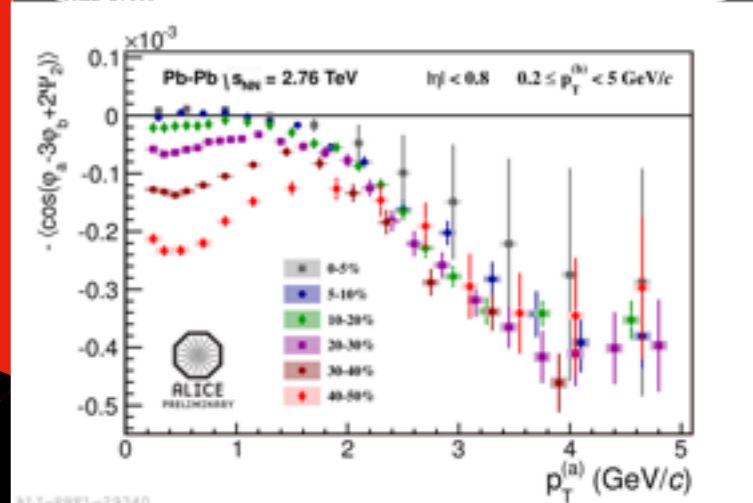
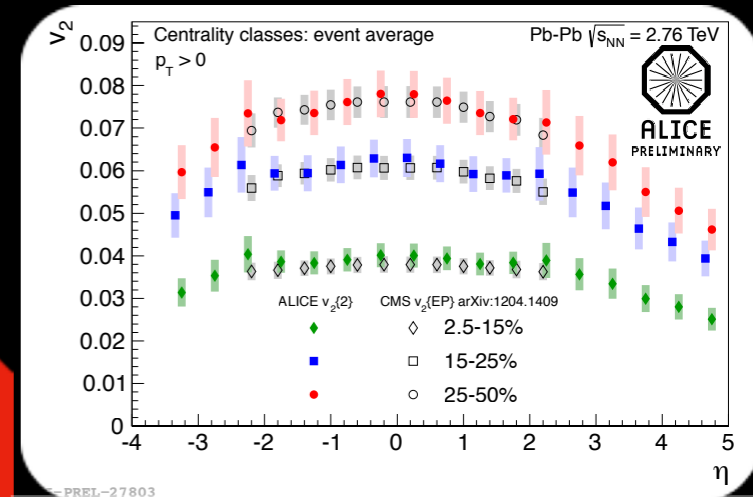
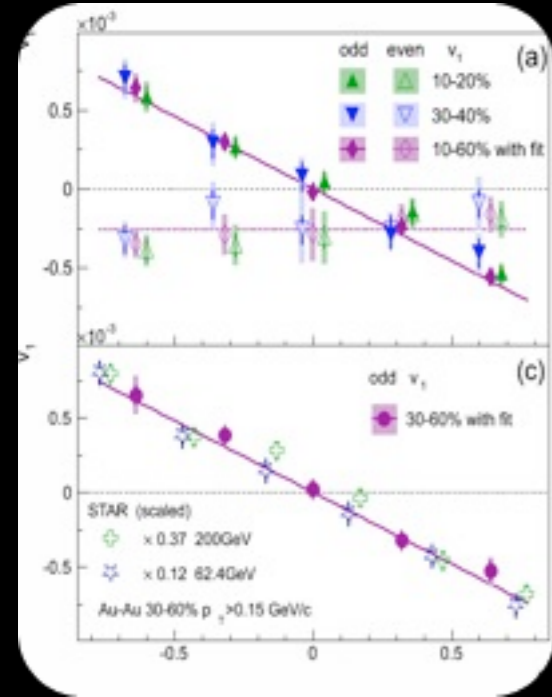


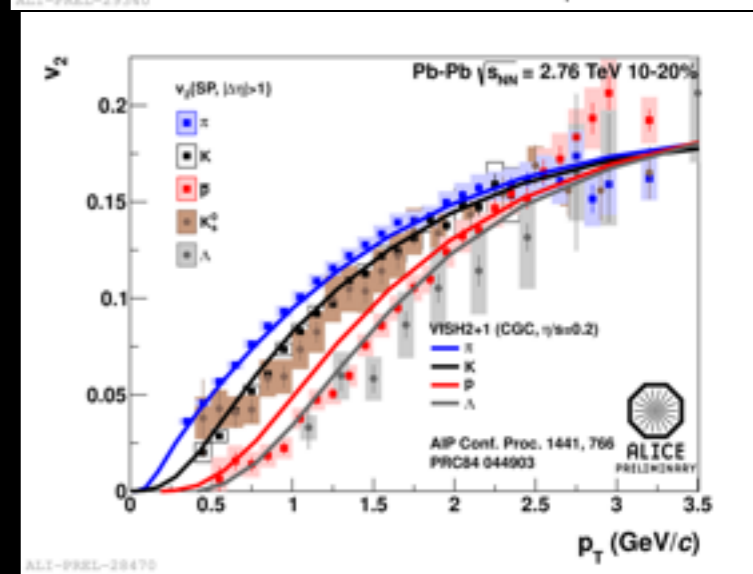
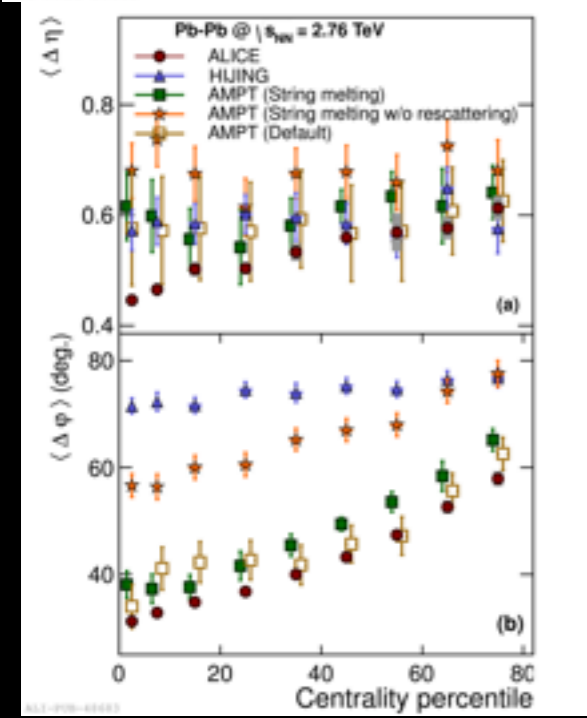
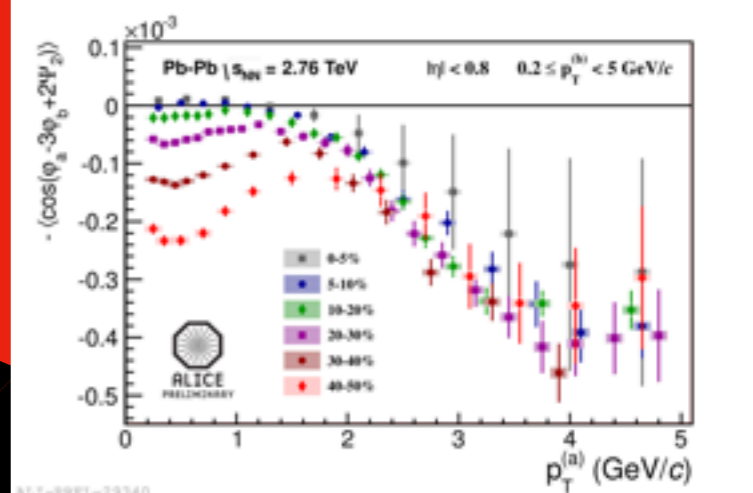
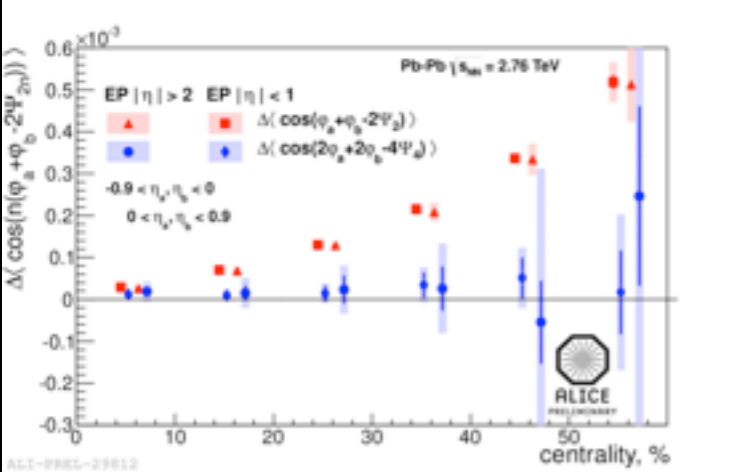
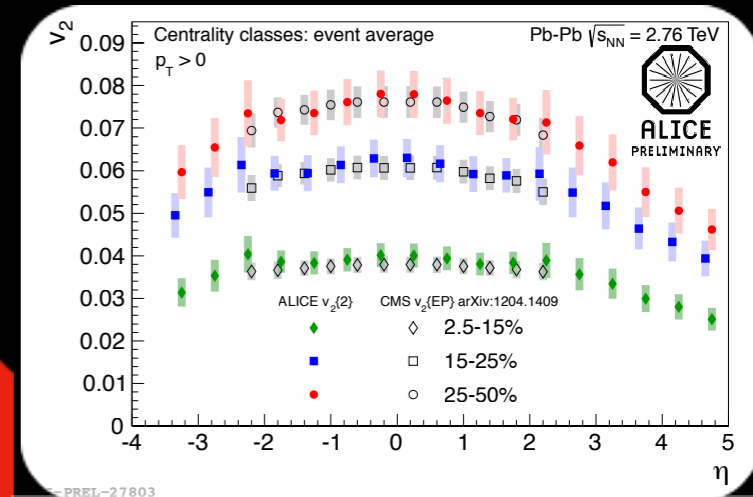
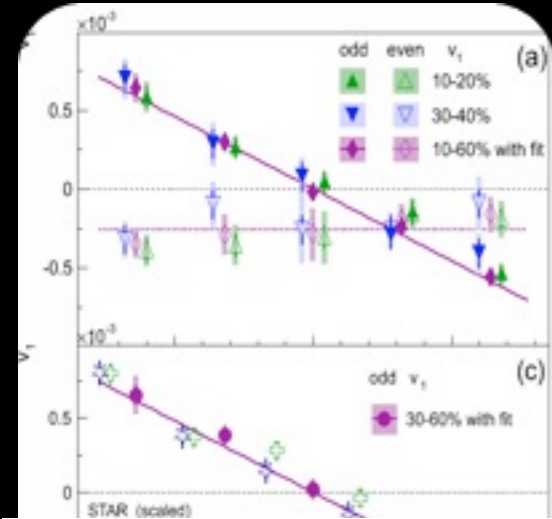


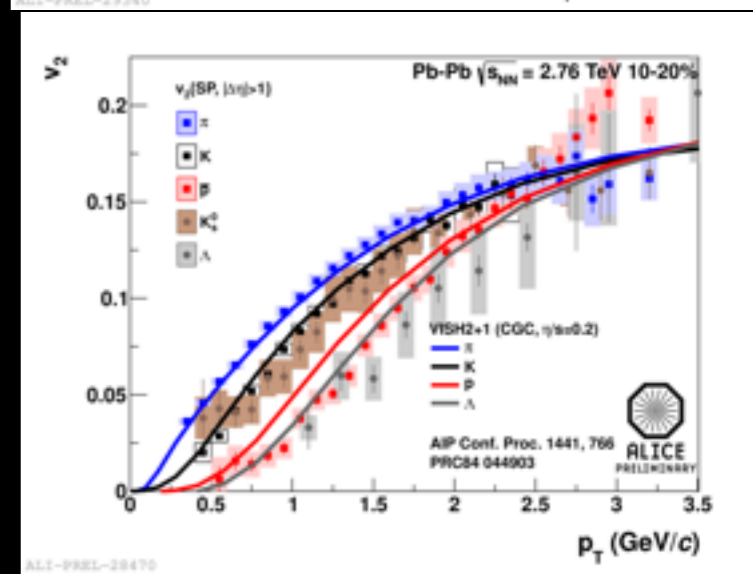
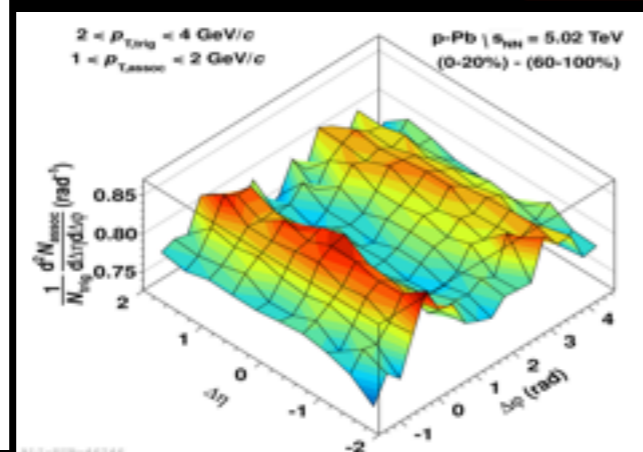
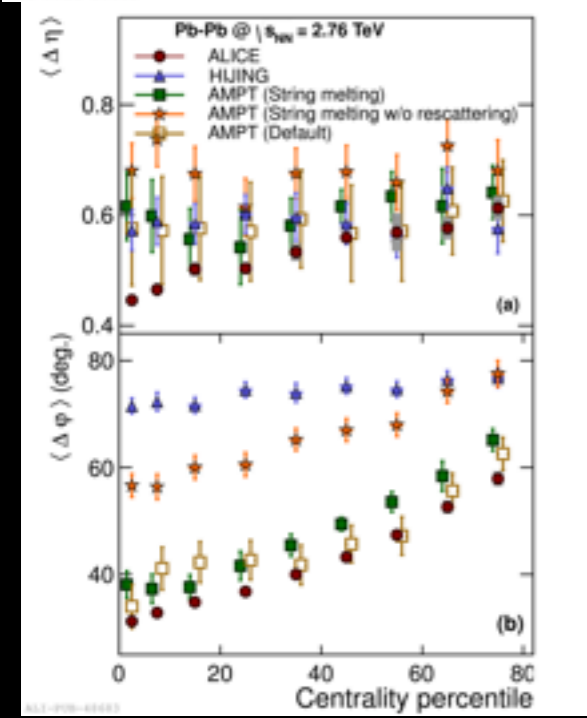
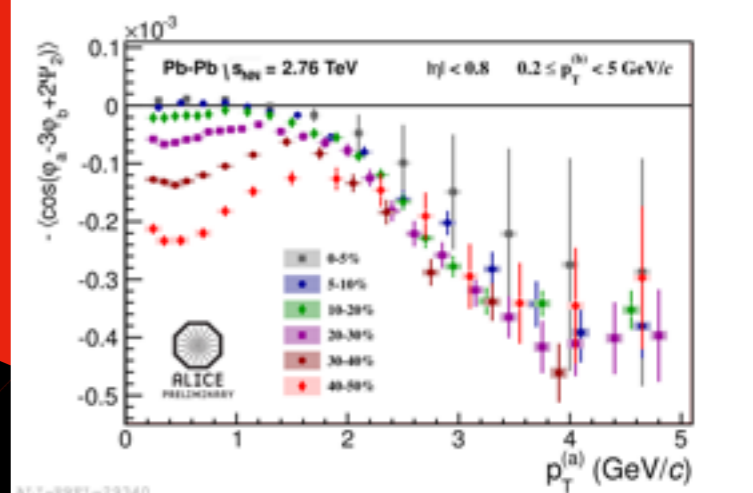
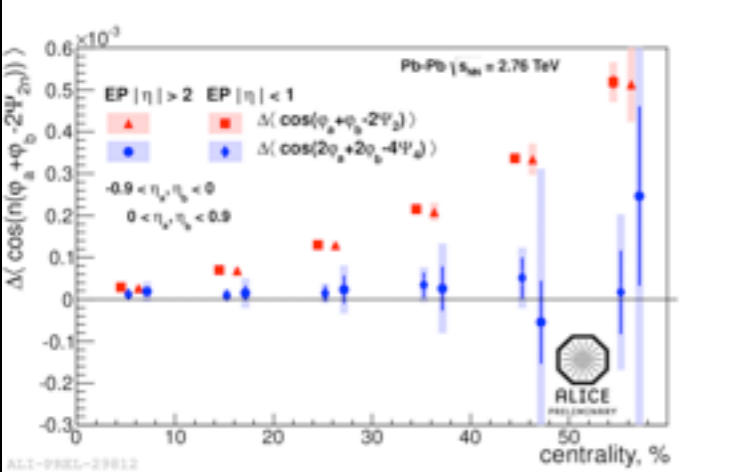
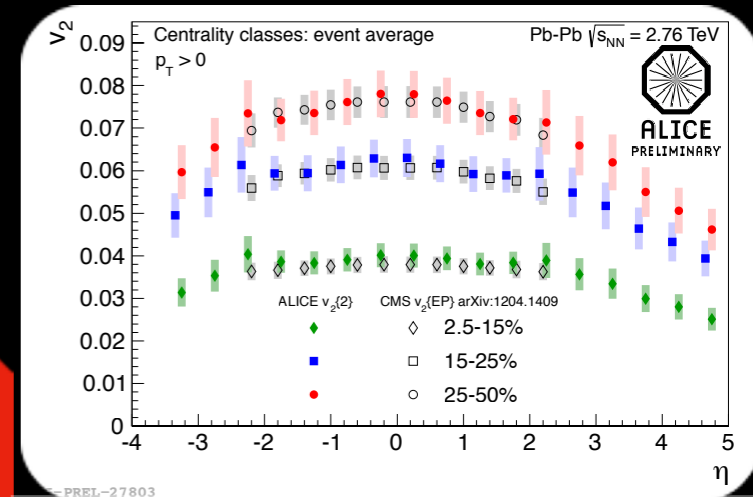
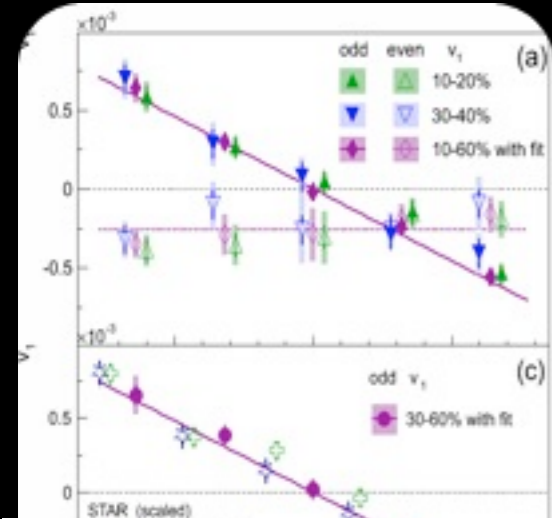


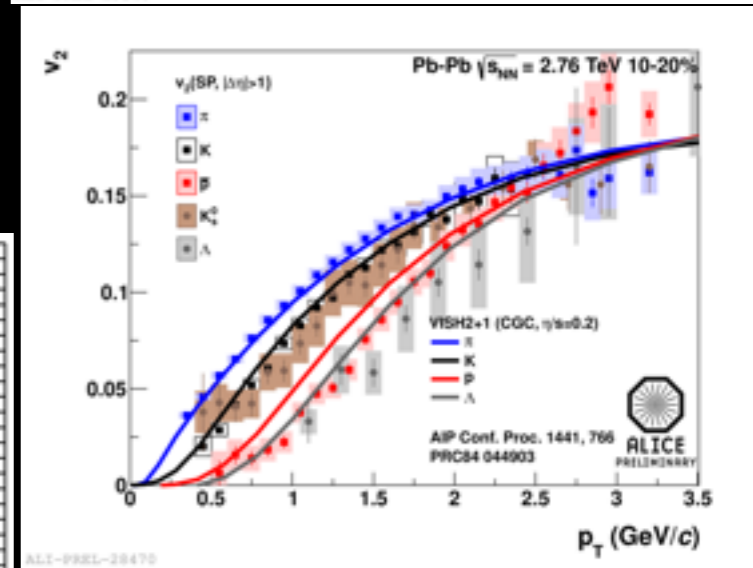
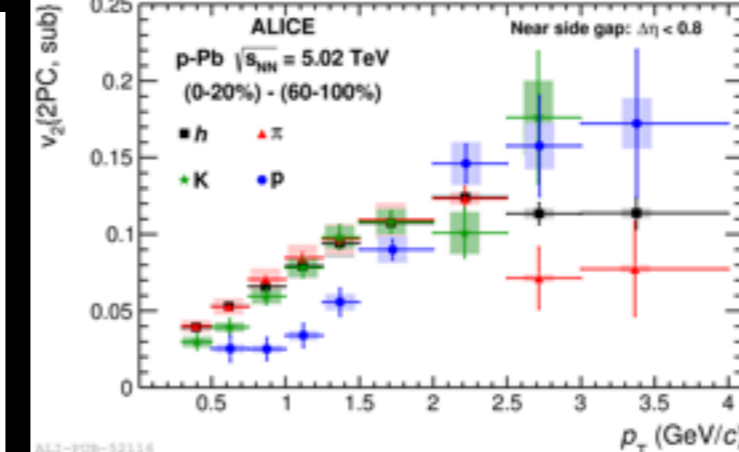
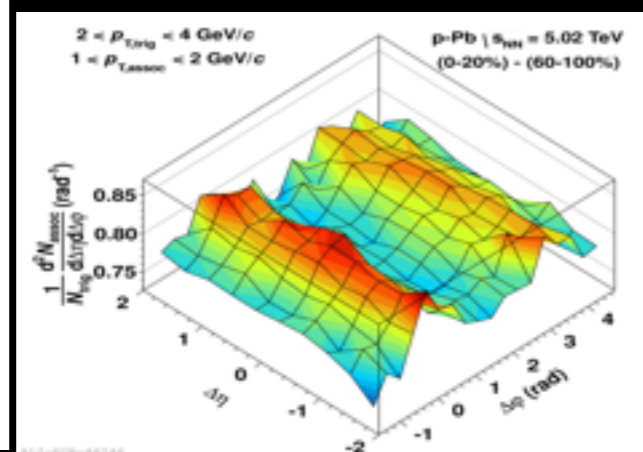
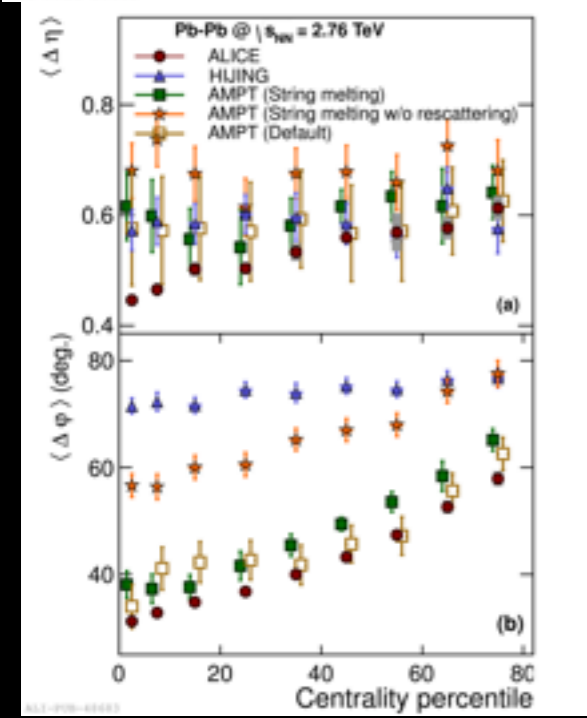
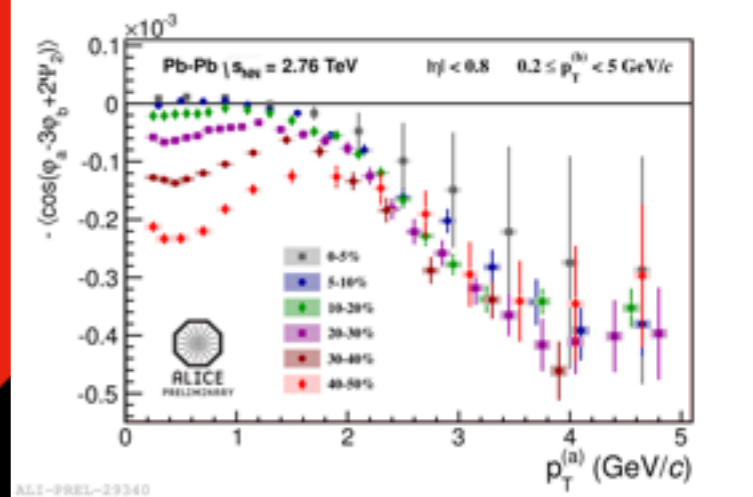
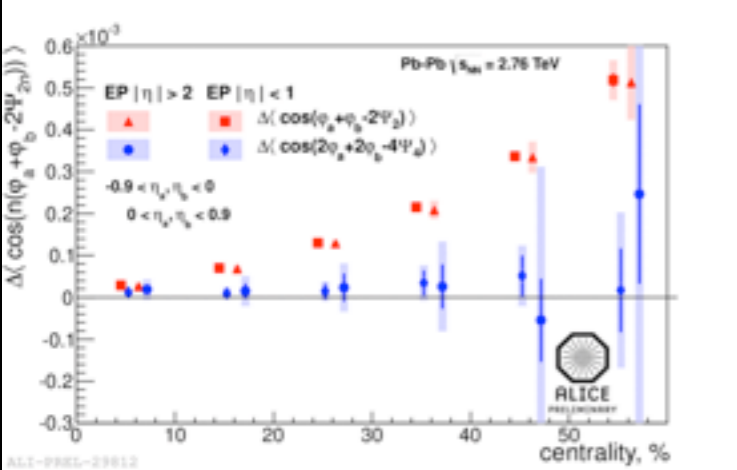
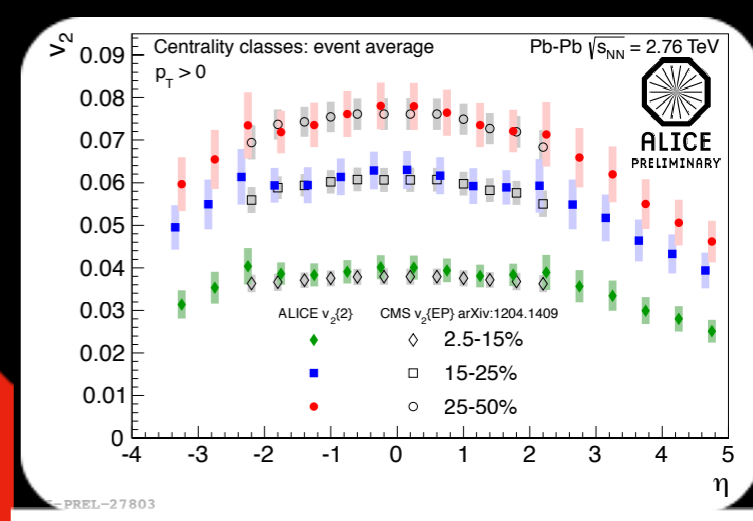
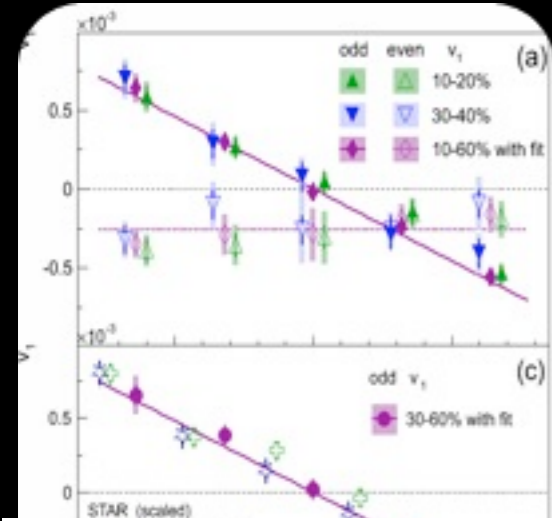








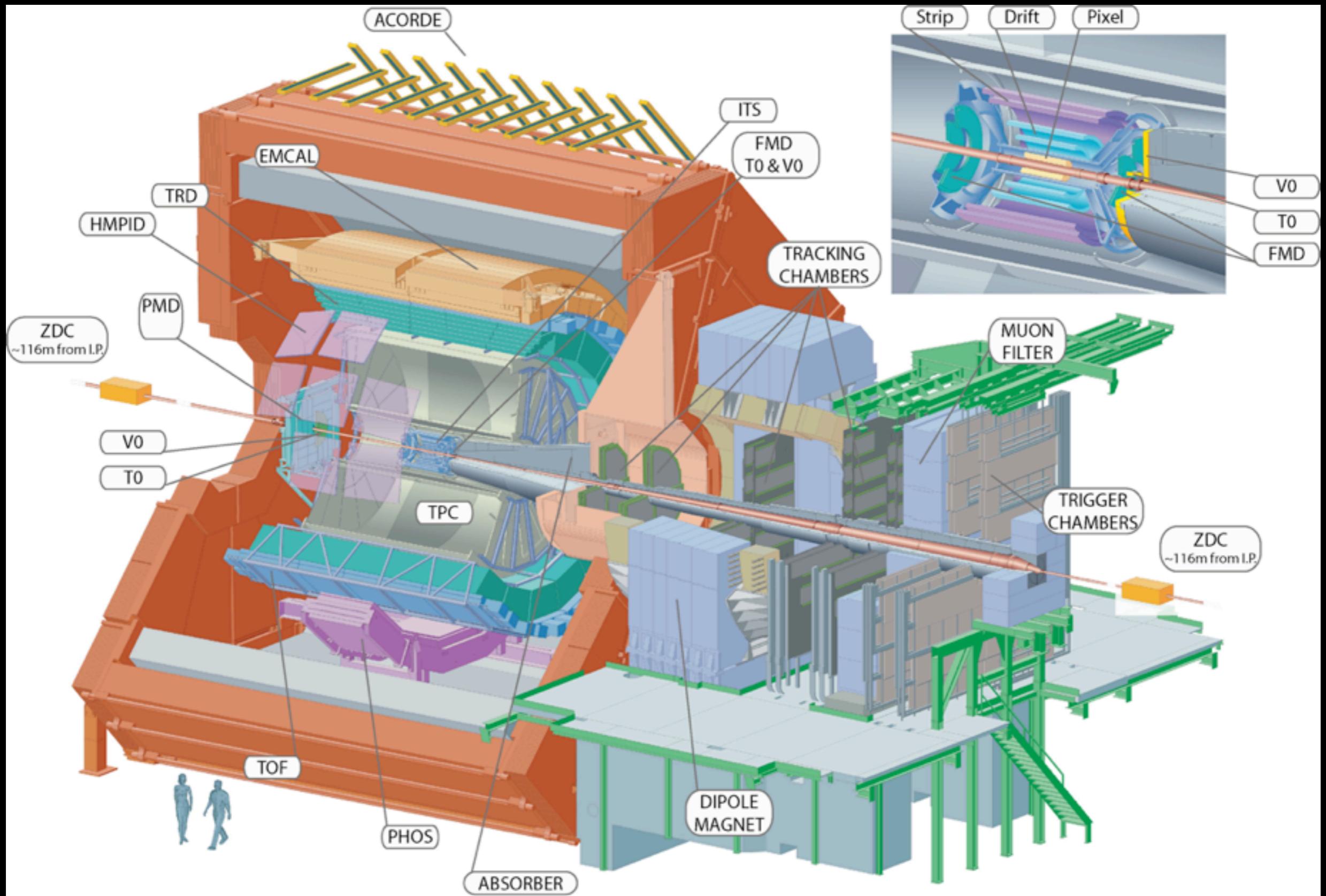




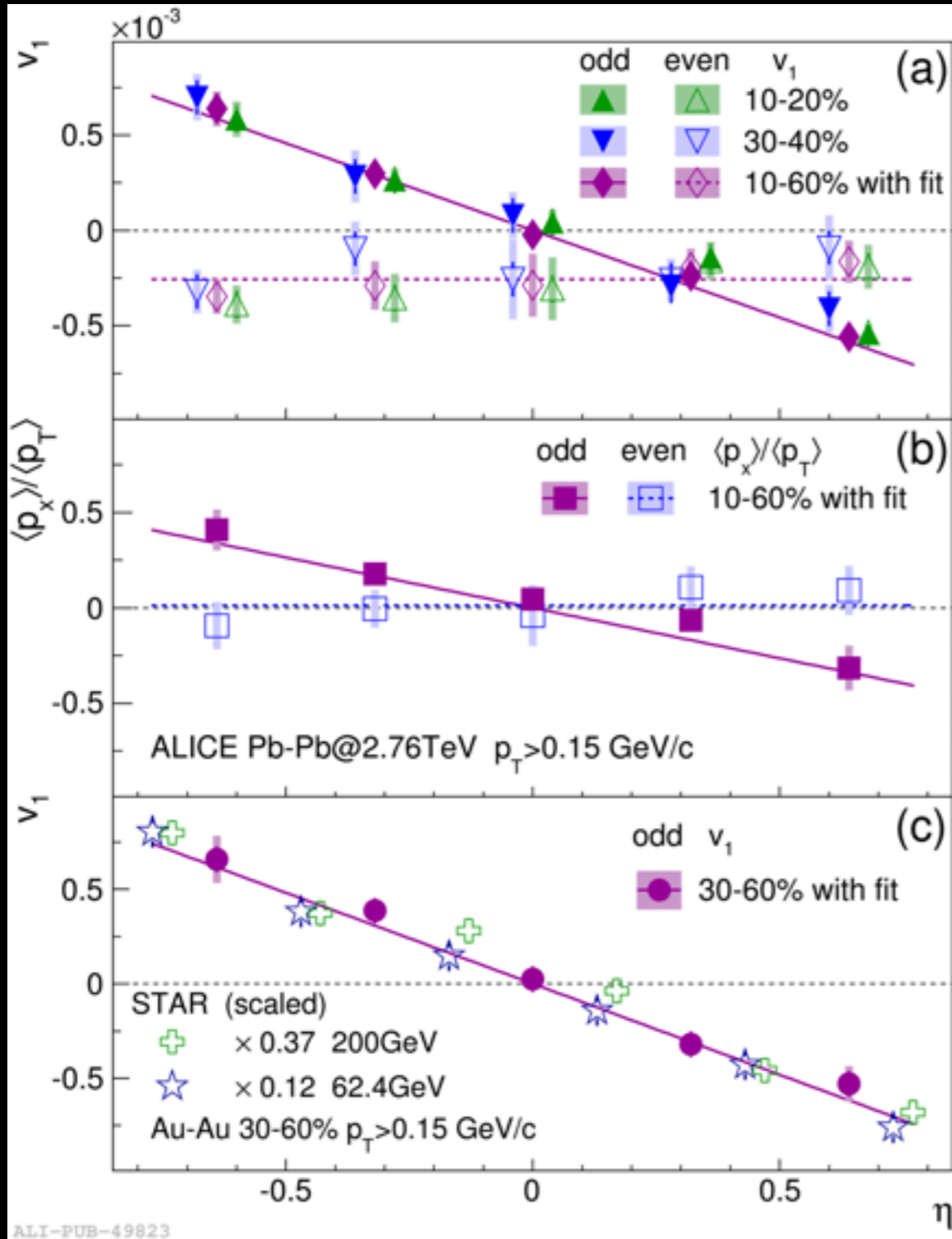


ALICE

# BACKUP



(ALICE Collaboration) arXiv:1306.4145



$$v_1 = \langle \cos(\varphi - \Psi) \rangle$$

$$v_1^{odd} \{ \Psi_{SP} \} = \frac{1}{2} [ v_1 \{ \Psi_{SP}^p \} + v_1 \{ \Psi_{SP}^t \} ]$$

$$v_1^{even} \{ \Psi_{SP} \} = \frac{1}{2} [ v_1 \{ \Psi_{SP}^p \} - v_1 \{ \Psi_{SP}^t \} ]$$

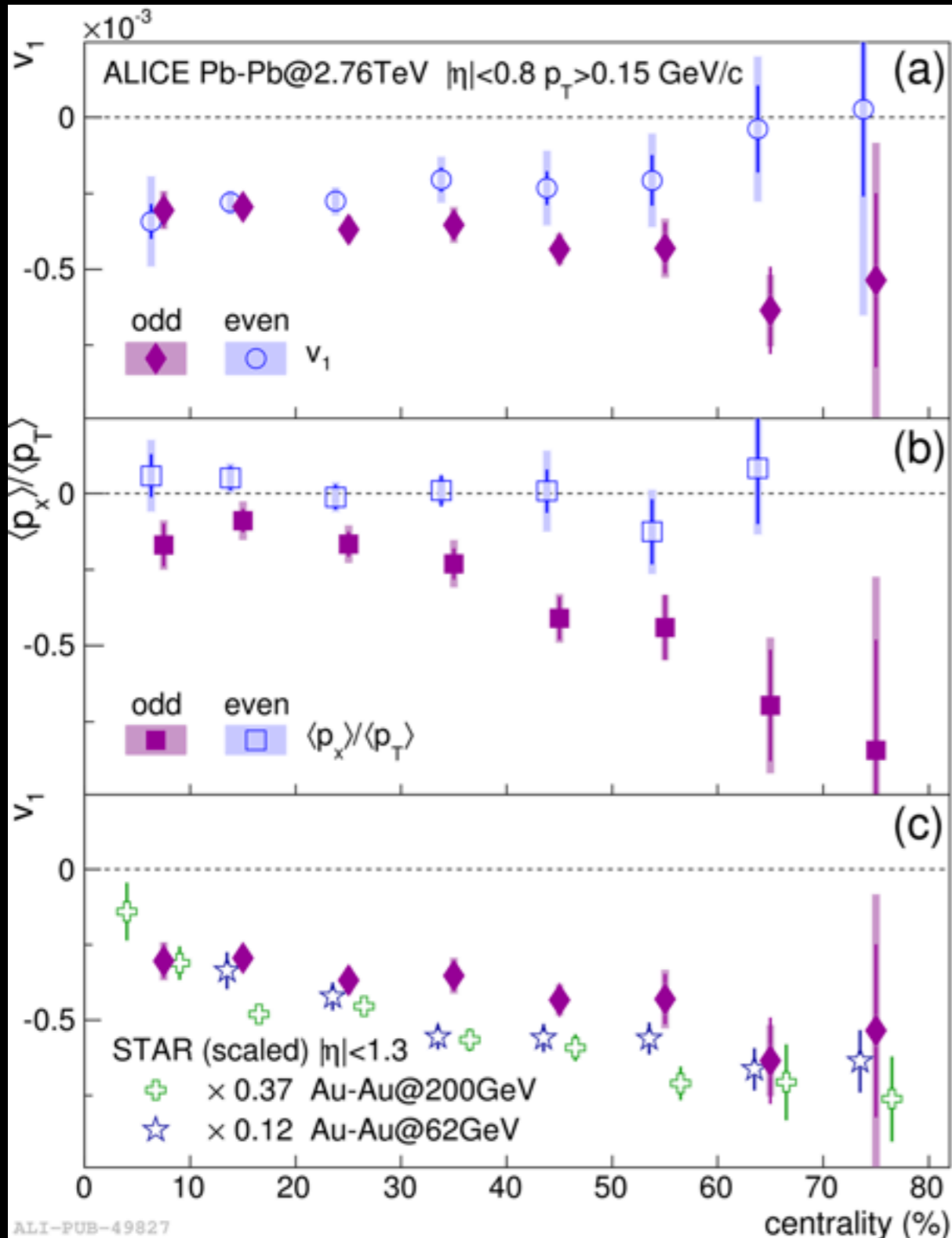
- Measured wrt the spectator deflection
- $v_1^{odd}$  negative slope
- ★ similar observation @ RHIC but a factor of ~3 smaller magnitude
- $v_1^{even}$  negative with no evident  $\eta$  dependence
- Relative momentum shift:
  - ★ Odd component smaller slope than the  $v_1^{odd}$ ,
  - ★ even component compatible with 0

$$\frac{\langle p_x \rangle}{\langle p_T \rangle} = \frac{\langle p_T \cos(\varphi - \Psi_{SP}) \rangle}{\langle p_T \rangle}$$



$$v_1 = \langle \cos(\varphi - \Psi) \rangle$$

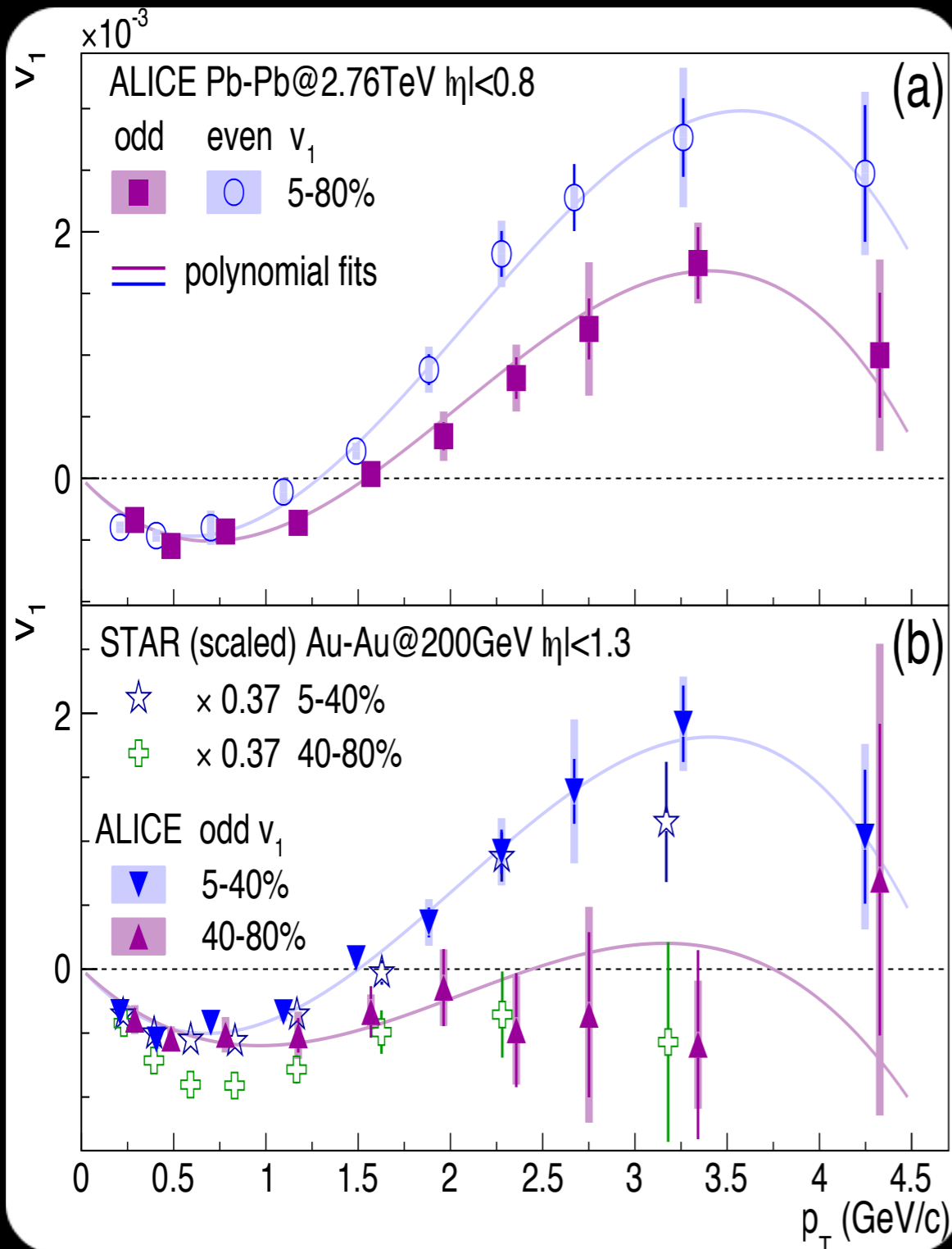
(ALICE Collaboration) arXiv:1306.4145



- Odd parts multiplied with -1 for  $\eta < 0$
- Mild centrality dependence for both  $v_1^{\text{odd}}$  and  $v_1^{\text{even}}$
- Significantly smaller magnitude of  $v_1^{\text{odd}}$  compared to RHIC

$$v_1 = \langle \cos(\varphi - \Psi) \rangle$$

(ALICE Collaboration) arXiv:1306.4145

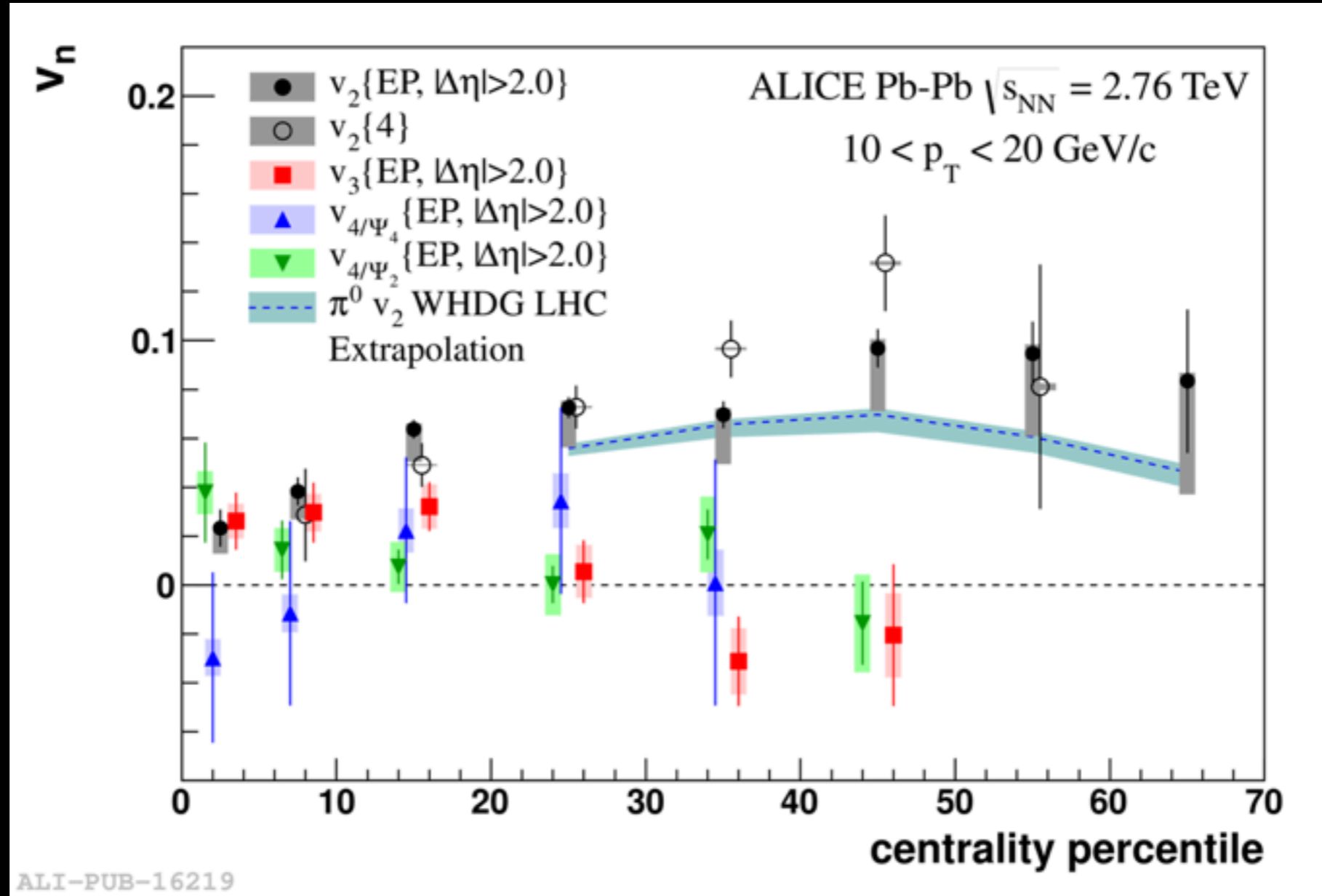


● Change of sign around 1.2-1.7 GeV/c

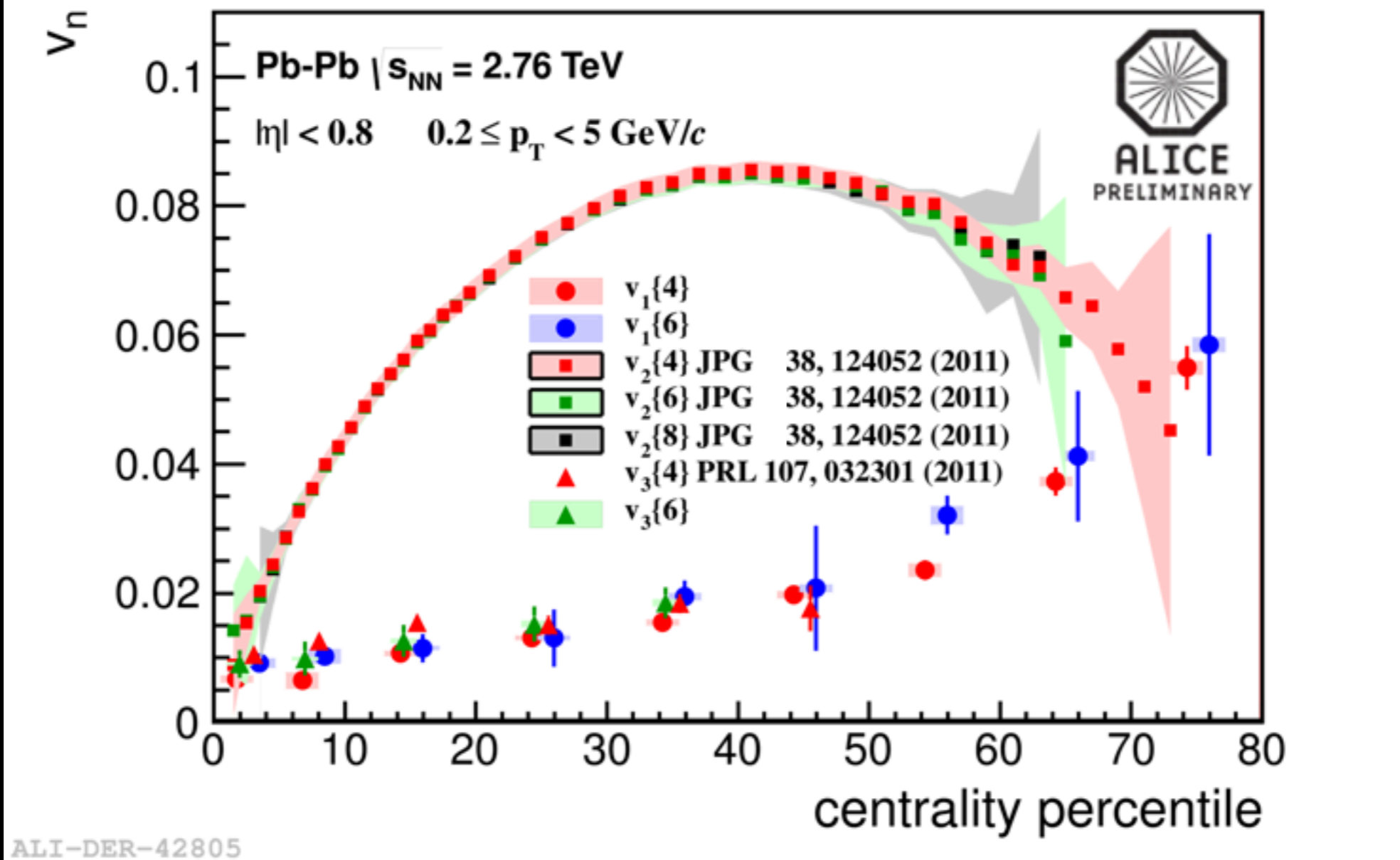
● Similar trends compared to RHIC

★ Note the scaling for the RHIC data

ALICE Collaboration: Phys. Lett. **B719**, (2013) 18



A. Bilandzic (ALICE Collaboration) @ QM2012

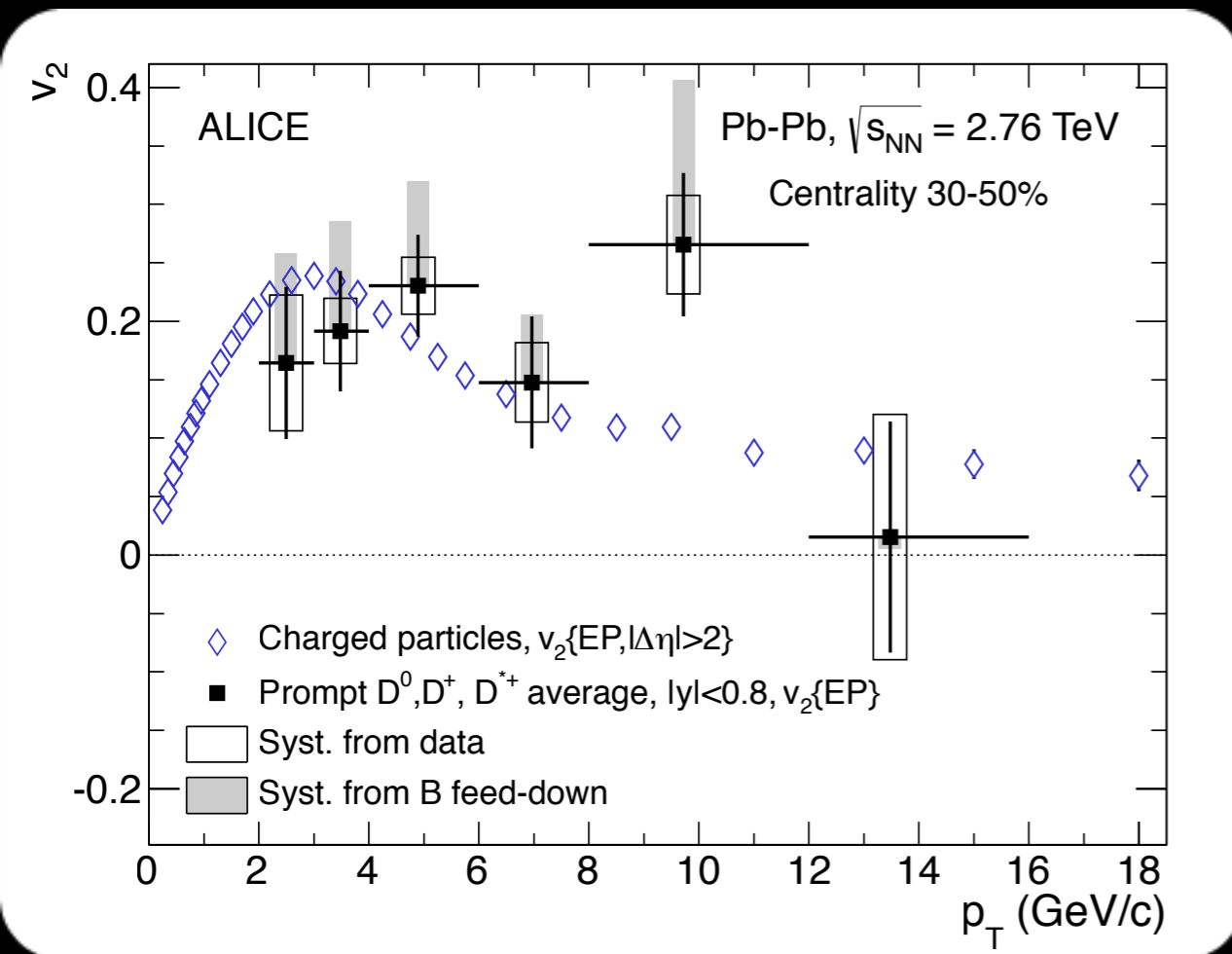


●  $V_n\{4\} \approx V_n\{6\} \approx V_n\{8\}$

● Bessel-Gaussian can be considered as a candidate for the p.d.f.

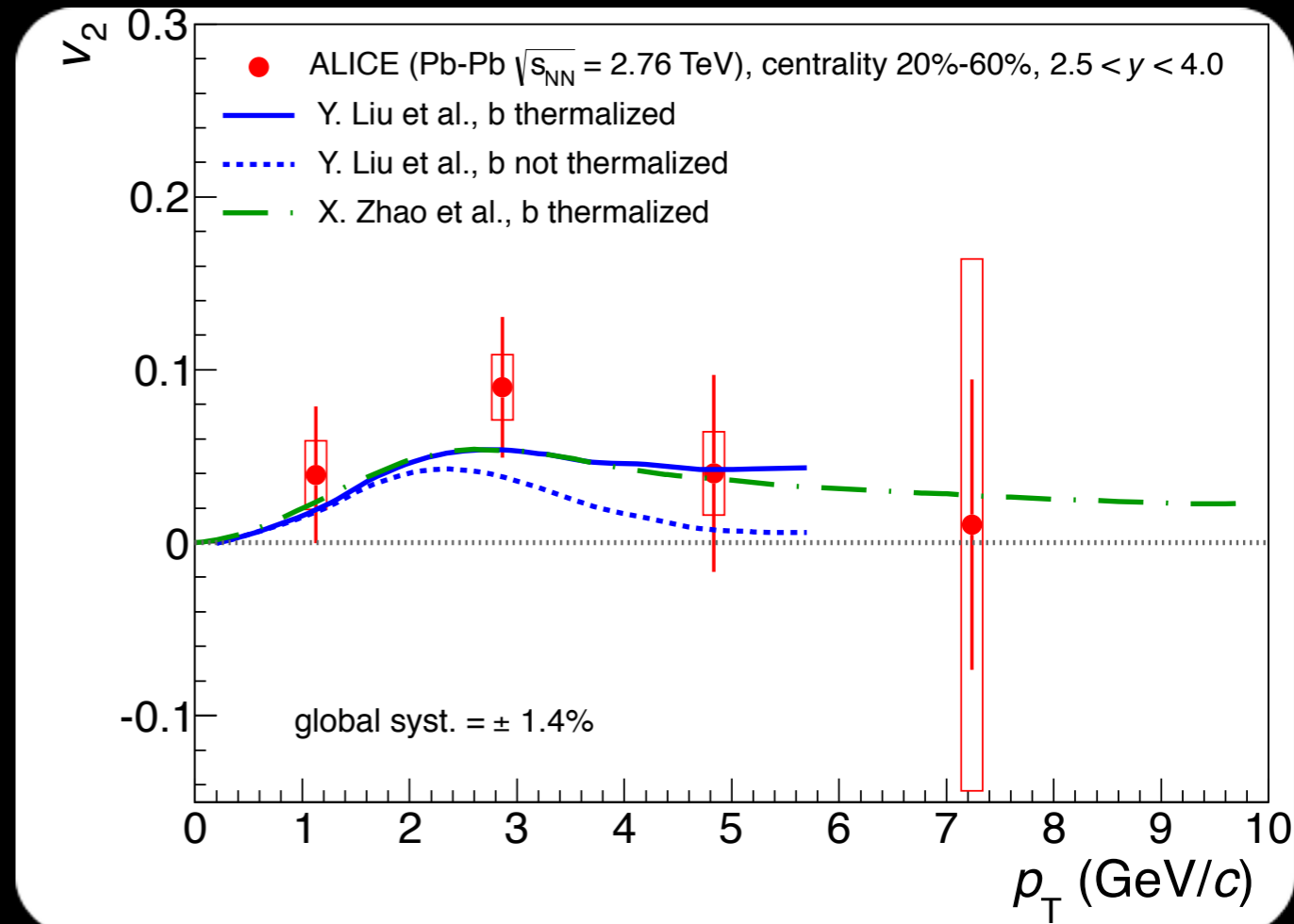
S. Voloshin, Phys. Lett. **B659**, 537 (2008)

ALICE Collaboration: arXiv:1305.2707



- Measured elliptic flow with the event plane, scalar product and the q-cumulant methods
- Results for  $D^0, D^+$  and  $D^{*+}$ , are in agreement and thus averaged in the plot
- Observed non-zero  $v_2$  for 30-50% and for  $2 < p_T < 6$  GeV/c ( $\sim 5.7\sigma$ )

ALICE Collaboration: arXiv:1303.5880



- Inclusive  $J/\Psi$   $v_2$  measured in the  $\mu^+\mu^-$  channel using the event plane method
- Indication of a non-zero  $v_2$  for 20-60% for  $2 < p_T < 4$  GeV/c at a level of  $\sim 2\sigma$  ( $2.7\sigma$  for  $2 < p_T < 6$  GeV/c for 20-40%)

Elena Bruna (25/7 Parallel session @ 15:20)



- Let's start from the Fourier series describing the azimuthal distribution of particles
- ★  $a_1$ : quantifies the charge separation perpendicular to the reaction plane
- ★  $a_n$  ( $n > 1$ ): higher order coefficients describe the shape in azimuth of the CME

$$\frac{dN}{d\varphi} \sim 1 + 2 \sum_{n=1}^{\infty} \{ v_n \cos[n(\varphi - \Psi_n)] + a_n \sin[n(\varphi - \Psi_n)] \}$$

- The experimental tool proposed to probe the signal was the two-particle correlator relative to the second order symmetry plane  $\Psi_2$ :

$$C_{11}^{a\beta}\{\Psi_2\} = \langle \cos[\varphi_\alpha - \varphi_\beta - 2\Psi_2] \rangle$$

- This correlator can be extended to higher orders:

$$C_{nm}^{a\beta}\{\Psi_k\} = \langle \cos[n\varphi_\alpha - m\varphi_\beta - (n-m)\Psi_k] \rangle$$

- In case of  $n=m$  the correlator transforms to the one with no explicit dependence on the symmetry plane:

$$C_n^{a\beta} = \langle \cos[n(\varphi_\alpha - \varphi_\beta)] \rangle$$

- For the case where  $m=0$  and  $n > 0$  the correlator gives the well known flow coefficients relative to the  $k^{\text{th}}$  order symmetry plane:

$$v_n^a\{\Psi_k\} = \langle \cos[n(\varphi_\alpha - \Psi_k)] \rangle$$

$$C_{nm}^{a\beta} \{ \Psi_k \} = \langle \cos [ n\varphi_\alpha - m\varphi_\beta - (n-m)\Psi_k ] \rangle$$

• Sensitivity to the CME:  $C_{nm}^{a\beta} \{ \Psi_k \} \sim (-1)^{n-m} \langle a_n^\alpha a_n^\beta \rangle$

Note: No solid quantitative expectations of the an terms at the LHC from theory; some qualitative expectations for a1 but higher orders are a completely new territory!!!



• Sensitivity to local charge conservation:  $\Delta C_{nm}^{a\beta} \{ \Psi_k \} = \frac{2C_{nm}^{+-} - C_{nm}^{++} - C_{nm}^{--}}{2}$

$$\begin{aligned} \Delta C_{nm}^{a\beta} \{ \Psi_k \} = & \Delta \langle \cos [ n(\varphi_\alpha - \varphi_\beta) ] \cos [ (n+m)(\varphi_\beta - \Psi_k) ] \rangle - \\ & \Delta \langle \cos [ n(\varphi_\alpha - \varphi_\beta) ] \rangle v_{|n+m|} \{ \Psi_k \} + \\ & \Delta \langle \cos [ n(\varphi_\alpha - \varphi_\beta) ] \rangle v_{|n+m|} \{ \Psi_k \} - \\ & \Delta \langle \sin [ n(\varphi_\alpha - \varphi_\beta) ] \sin [ (n+m)(\varphi_\beta - \Psi_k) ] \rangle \end{aligned}$$

$$\begin{aligned} \Delta C_{nm}^{a\beta} \{ \Psi_k \} = & v_{|n+m|}^{symm.} \{ \Psi_k \} + \\ & \Delta C_n^{a\beta} v_{|n+m|} \{ \Psi_k \} - \\ & v_{|n+m|}^{asymm.} \{ \Psi_k \} \end{aligned}$$



$$C_{nm}^{a\beta} \{ \Psi_k \} = \langle \cos [ n\varphi_\alpha - m\varphi_\beta - (n-m)\Psi_k ] \rangle$$

• Sensitivity to the CME:  $C_{nm}^{a\beta} \{ \Psi_k \} \sim (-1)^{n-m} \langle a_n^\alpha a_n^\beta \rangle$

Note: No solid quantitative expectations of the an terms at the LHC from theory; some qualitative expectations for a1 but higher orders are a completely new territory!!!

• Sensitivity to local charge conservation:

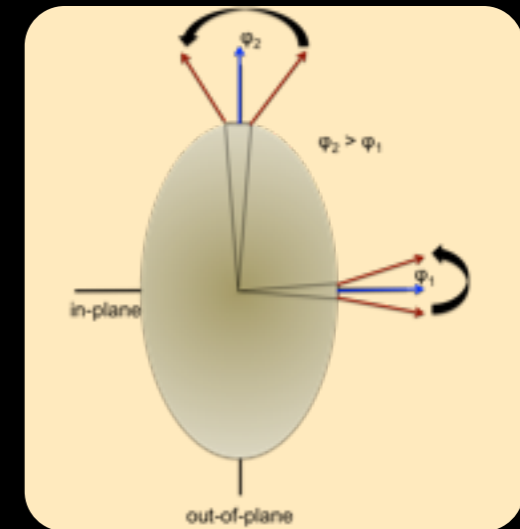
$$\Delta C_{nm}^{a\beta} \{ \Psi_k \} = \frac{2C_{nm}^{+-} - C_{nm}^{++} - C_{nm}^{--}}{2}$$

$$\Delta C_{nm}^{a\beta} \{ \Psi_k \} = \Delta \langle \cos [ n(\varphi_\alpha - \varphi_\beta) ] \cos [ (n+m)(\varphi_\beta - \Psi_k) ] \rangle - \Delta \langle \cos [ n(\varphi_\alpha - \varphi_\beta) ] \rangle v_{|n+m|} \{ \Psi_k \} + \Delta \langle \cos [ n(\varphi_\alpha - \varphi_\beta) ] \rangle v_{|n+m|} \{ \Psi_k \} - \Delta \langle \sin [ n(\varphi_\alpha - \varphi_\beta) ] \sin [ (n+m)(\varphi_\beta - \Psi_k) ] \rangle$$

$$\Delta C_{nm}^{a\beta} \{ \Psi_k \} = v_{|n+m|}^{symm.} \{ \Psi_k \} +$$

$$\Delta C_n^{a\beta} v_{|n+m|} \{ \Psi_k \} - v_{|n+m|}^{asymm.} \{ \Psi_k \}$$

This term quantifies how more tightly correlated the in-plane pairs are wrt the out-of-plane ones





$$C_{nm}^{a\beta} \{ \Psi_k \} = \langle \cos [ n\varphi_\alpha - m\varphi_\beta - (n-m)\Psi_k ] \rangle$$

• Sensitivity to the CME:  $C_{nm}^{a\beta} \{ \Psi_k \} \sim (-1)^{n-m} \langle a_n^\alpha a_n^\beta \rangle$

Note: No solid quantitative expectations of the an terms at the LHC from theory; some qualitative expectations for a1 but higher orders are a completely new territory!!!



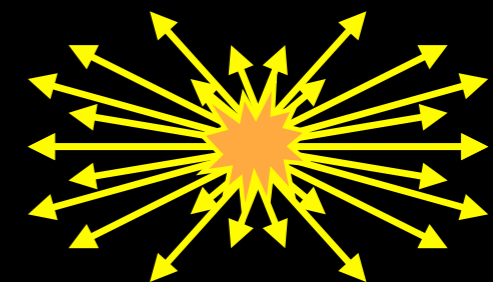
• Sensitivity to local charge conservation:

$$\Delta C_{nm}^{a\beta} \{ \Psi_k \} = \frac{2C_{nm}^{+-} - C_{nm}^{++} - C_{nm}^{--}}{2}$$

$$\begin{aligned} \Delta C_{nm}^{a\beta} \{ \Psi_k \} = & \Delta \langle \cos [ n(\varphi_\alpha - \varphi_\beta) ] \cos [ (n+m)(\varphi_\beta - \Psi_k) ] \rangle - \\ & \Delta \langle \cos [ n(\varphi_\alpha - \varphi_\beta) ] \rangle v_{|n+m|} \{ \Psi_k \} + \\ & \Delta \langle \cos [ n(\varphi_\alpha - \varphi_\beta) ] \rangle v_{|n+m|} \{ \Psi_k \} - \\ & \Delta \langle \sin [ n(\varphi_\alpha - \varphi_\beta) ] \sin [ (n+m)(\varphi_\beta - \Psi_k) ] \rangle \end{aligned}$$

$$\begin{aligned} \Delta C_{nm}^{a\beta} \{ \Psi_k \} = & v_{|n+m|}^{symm.} \{ \Psi_k \} + \\ & \Delta C_n^{a\beta} v_{|n+m|} \{ \Psi_k \} - \\ & v_{|n+m|}^{asymm.} \{ \Psi_k \} \end{aligned}$$

This term quantifies how many more balancing pairs there are in-plane wrt the out-of-plane





$$C_{nm}^{\alpha\beta}\{\Psi_k\} = \langle \cos[n\varphi_\alpha - m\varphi_\beta - (n-m)\Psi_k] \rangle$$

• Sensitivity to the CME:  $C_{nm}^{\alpha\beta}\{\Psi_k\} \sim (-1)^{n-m} \langle a_n^\alpha a_n^\beta \rangle$

Note: No solid quantitative expectations of the an terms at the LHC from theory; some qualitative expectations for a1 but higher orders are a completely new territory!!!

• Sensitivity to local charge conservation:

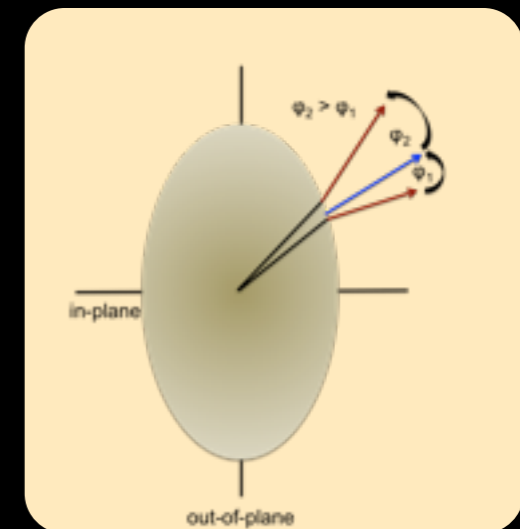
$$\Delta C_{nm}^{\alpha\beta}\{\Psi_k\} = \frac{2C_{nm}^{+-} - C_{nm}^{++} - C_{nm}^{--}}{2}$$

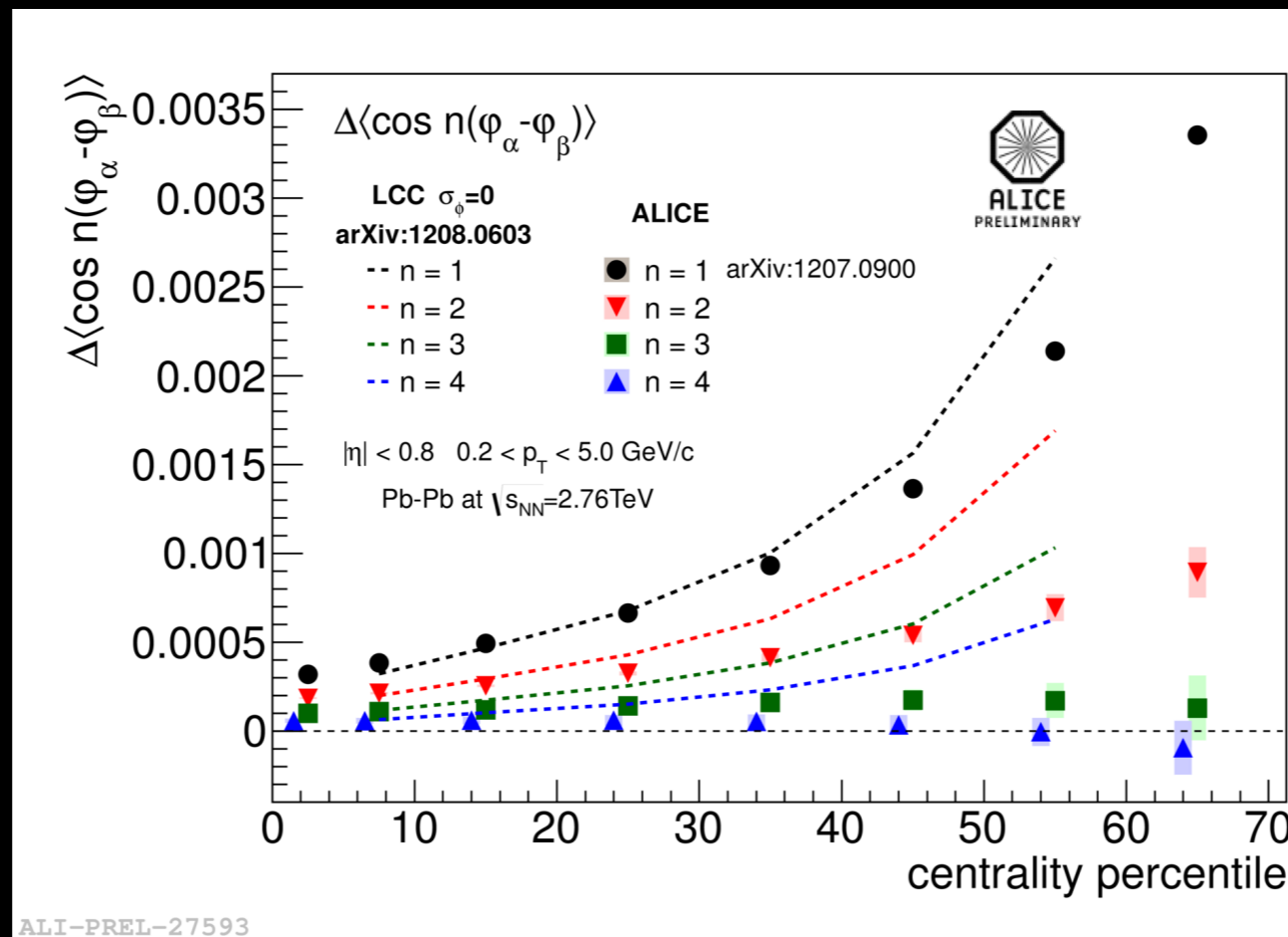
$$\begin{aligned} \Delta C_{nm}^{\alpha\beta}\{\Psi_k\} = & \Delta \langle \cos[n(\varphi_\alpha - \varphi_\beta)] \cos[(n+m)(\varphi_\beta - \Psi_k)] \rangle - \\ & \Delta \langle \cos[n(\varphi_\alpha - \varphi_\beta)] \rangle v_{|n+m|}\{\Psi_k\} + \\ & \Delta \langle \cos[n(\varphi_\alpha - \varphi_\beta)] \rangle v_{|n-m|}\{\Psi_k\} - \\ & \Delta \langle \sin[n(\varphi_\alpha - \varphi_\beta)] \sin[(n+m)(\varphi_\beta - \Psi_k)] \rangle \end{aligned}$$

$$\Delta C_{nm}^{\alpha\beta}\{\Psi_k\} = v_{|n+m|}^{symm.}\{\Psi_k\} +$$

$$\Delta C_{nm}^{\alpha\beta} v_{|n+m|}\{\Psi_k\} - v_{|n+m|}^{asymm.}\{\Psi_k\}$$

This term quantifies how more likely it is for the balancing charge to be emitted towards the symmetry plane wrt the trigger (leading) particle





- Results are compared to a blast wave model tuned to match the published charged particle  $v_2$  values at the LHC and the identified particle spectra as reported by ALICE
- The model generates particle pairs (balanced) at the surface based on an initial separation parameter  $\sigma$  that can be adjusted accordingly (e.g.  $\sigma = 0$  point-like unlike-sign particle emission)
- Model describes the data for the first harmonic reasonably well (besides the most peripheral classes) but systematically overestimates the centrality dependence for the higher moments.

For further details: Yasuto Hori (for the ALICE Collaboration), "Mixed harmonic charge dependent correlations measured with ALICE" shown @ Quark Matter 2012, Washington DC



$$C_{nm}^{\alpha\beta}\{\Psi_k\} = \langle \cos[n\varphi_\alpha - m\varphi_\beta - (n-m)\Psi_k] \rangle$$

The second harmonic modulation of the balance function wrt  $\Psi_2$

$$\Delta C_{1,1}\{\Psi_2\} = \Delta \langle \cos(\varphi_\alpha + \varphi_\beta - 2\Psi_2) \rangle$$

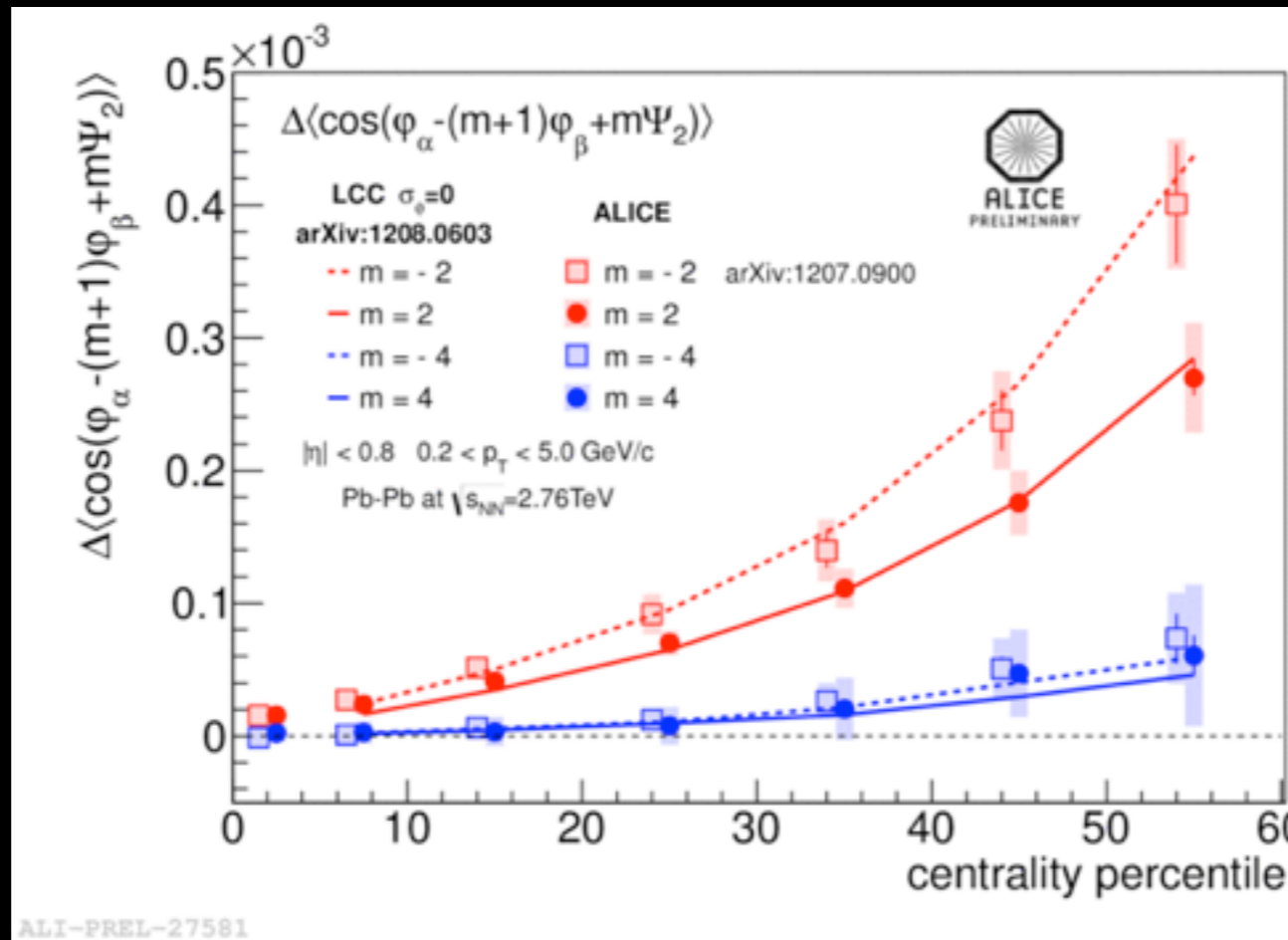
$$\Delta C_{1,3}\{\Psi_2\} = \Delta \langle \cos(\varphi_\alpha - 3\varphi_\beta + 2\Psi_2) \rangle$$

The fourth harmonic modulation of the balance function wrt  $\Psi_2$

$$\Delta C_{1,-3}\{\Psi_2\} = \Delta \langle \cos(\varphi_\alpha + 3\varphi_\beta - 4\Psi_2) \rangle$$

$$\Delta C_{1,5}\{\Psi_2\} = \Delta \langle \cos(\varphi_\alpha - 5\varphi_\beta + 4\Psi_2) \rangle$$

The model reproduces successfully the main features for a set of correlators with different harmonics



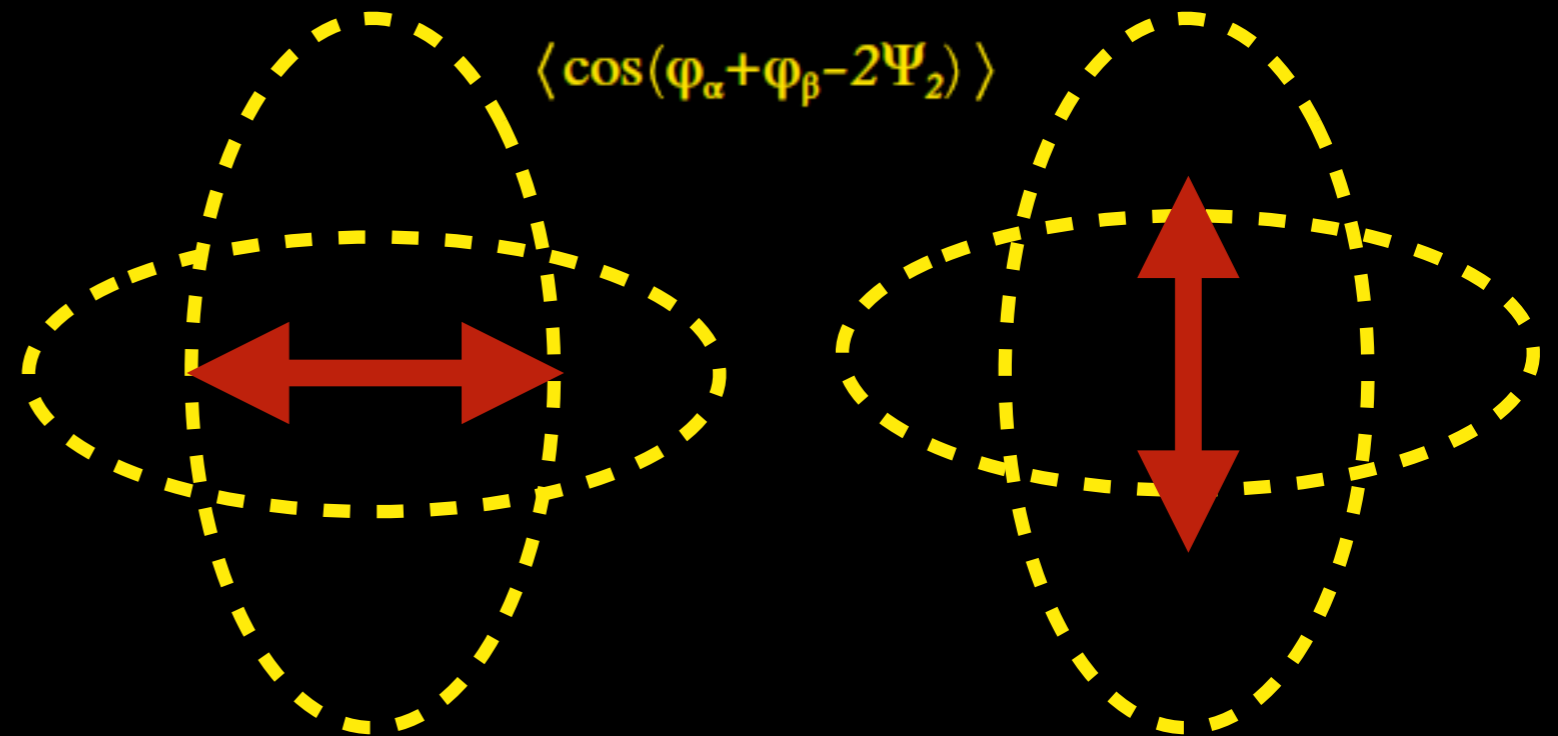
Y. Hori (ALICE Collaboration) @ QM2012

**Charge independent correlations:**

- ★ directed flow fluctuations relative to the 2<sup>nd</sup> order symmetry plane

**Charge dependent correlations:**

- ★ contribution from CME
- ★ contribution from local charge conservation +  $v_2$

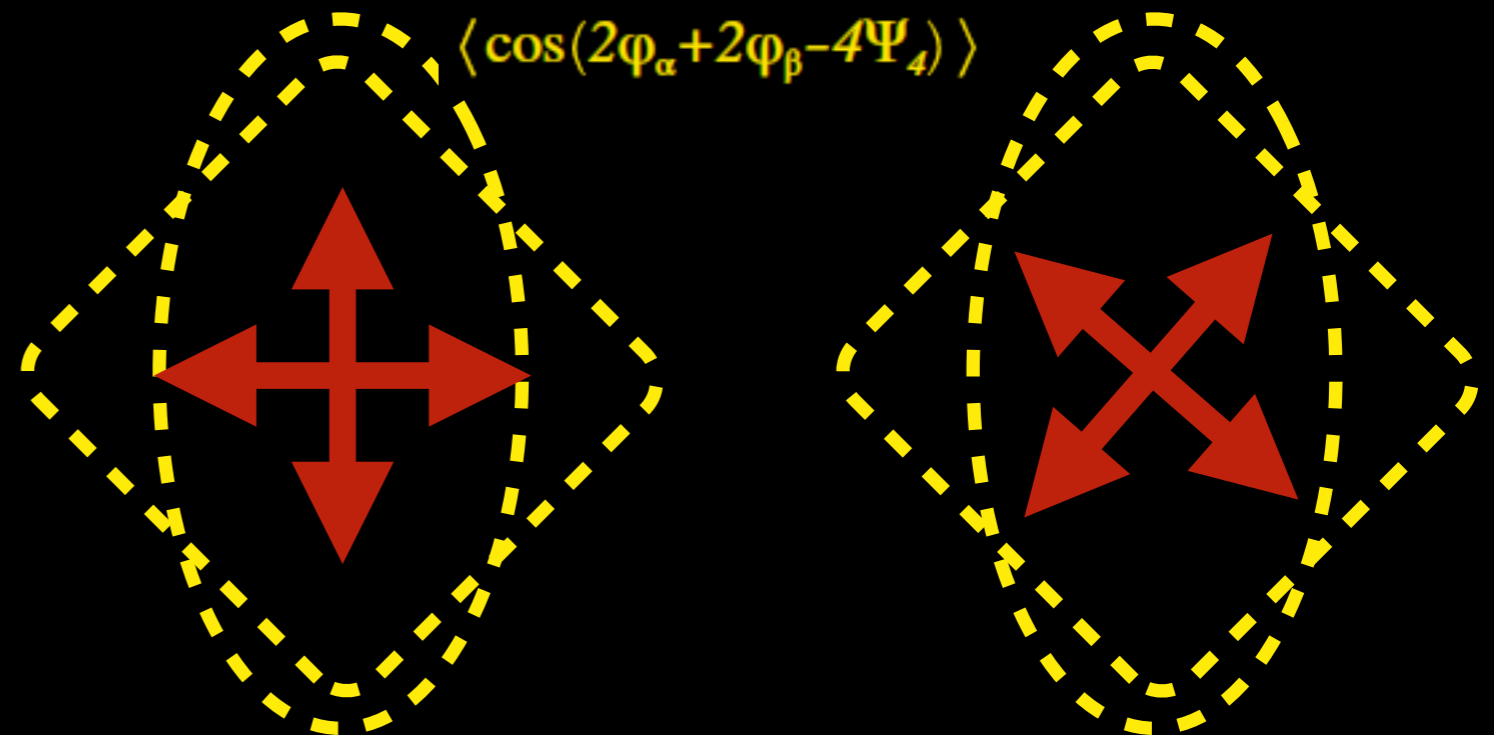


**Charge independent correlations:**

- ★ elliptic flow fluctuations relative to the 4<sup>th</sup> order symmetry plane

**Charge dependent correlations:**

- ★ no contribution from CME
- ★ contribution from local charge conservation +  $v_4$



For further details: Jocelyn Mlynarz (for the ALICE Collaboration), “Charged dependent correlations relative to the 4th harmonic” shown @ Quark Matter 2012, Washington DC