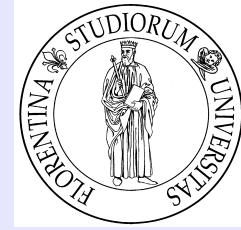


F. Becattini,  
*University of Florence*  
*and University and FIAS Frankfurt*



# A review on global strangeness production

## OUTLINE

- Introduction
- Summary on global strangeness production
- Strangeness production in pp collisions
- Strangeness and p/ $\pi$  “puzzle”
- Conclusions

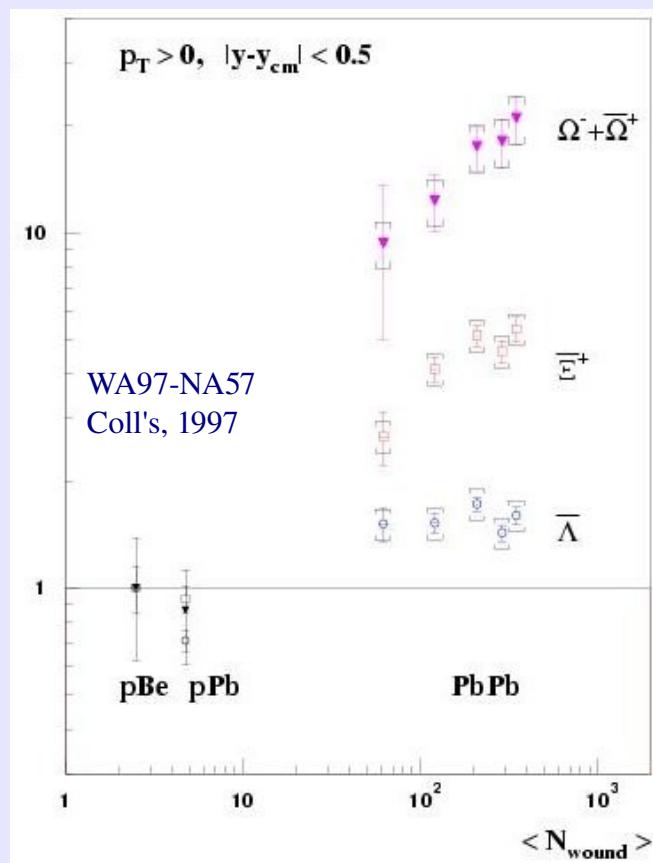
# Strangeness enhancement was predicted as a signature of QGP

J. Rafelski, B. Muller, Phys. Rev. Lett. 48, 1066 (1982)

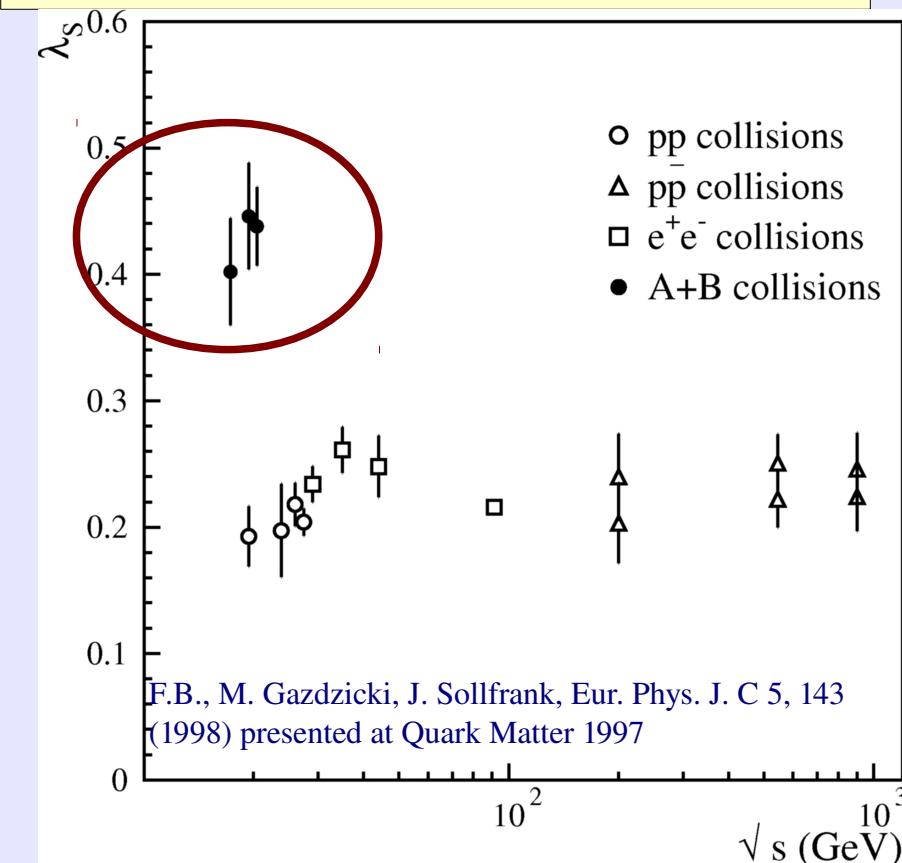
Chiral symmetry restoration favours (relative) strange quark production in a deconfined medium

Strange quark coalescence favours the enhancement of multiple strange hyperons

$$\text{Wroblewski ratio } \lambda_S = \frac{2\langle \bar{s}s \rangle}{\langle \bar{u}u \rangle + \langle \bar{d}d \rangle}$$



NA35-NA49  
data



## What is the origin of the strangeness enhancement?

- ❖ Post-hadronization collisions raising pp-like strange particle abundances (transport model)?
- ❖ Size increase in AA, in other words the relaxation of the canonical suppression in pp collisions (statistical model)?
- ❖ Recombination or coalescence of strange quarks from the plasma (what one would hope for)?

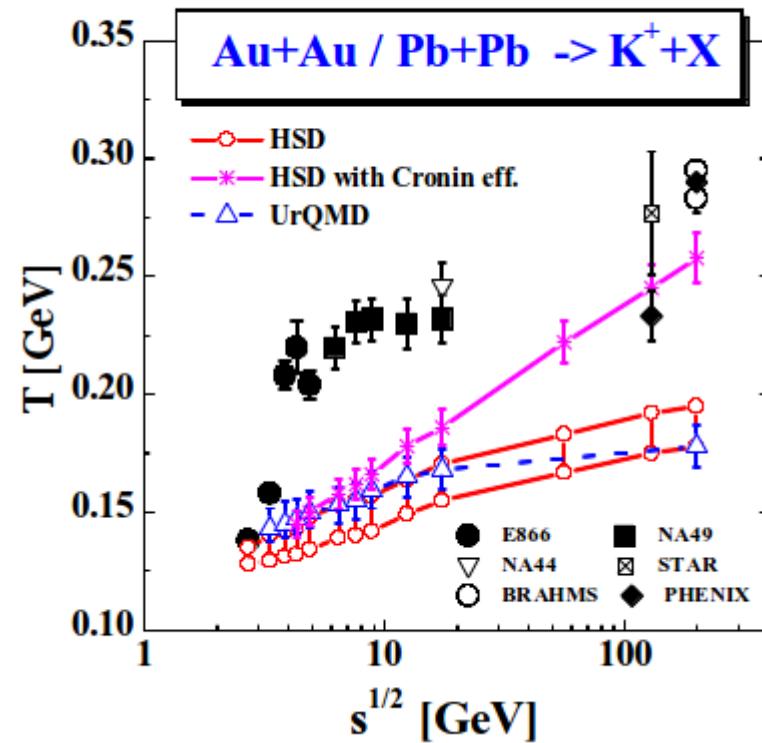
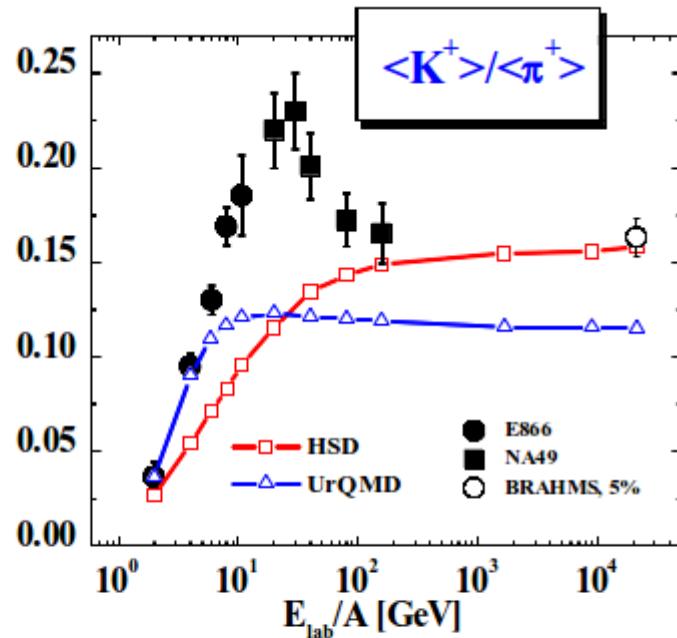
Previous plots show – at least – that AA is not an incoherent superposition of pp collisions

# Transport models (see M. Bleicher's talk)

Hadronization based on:

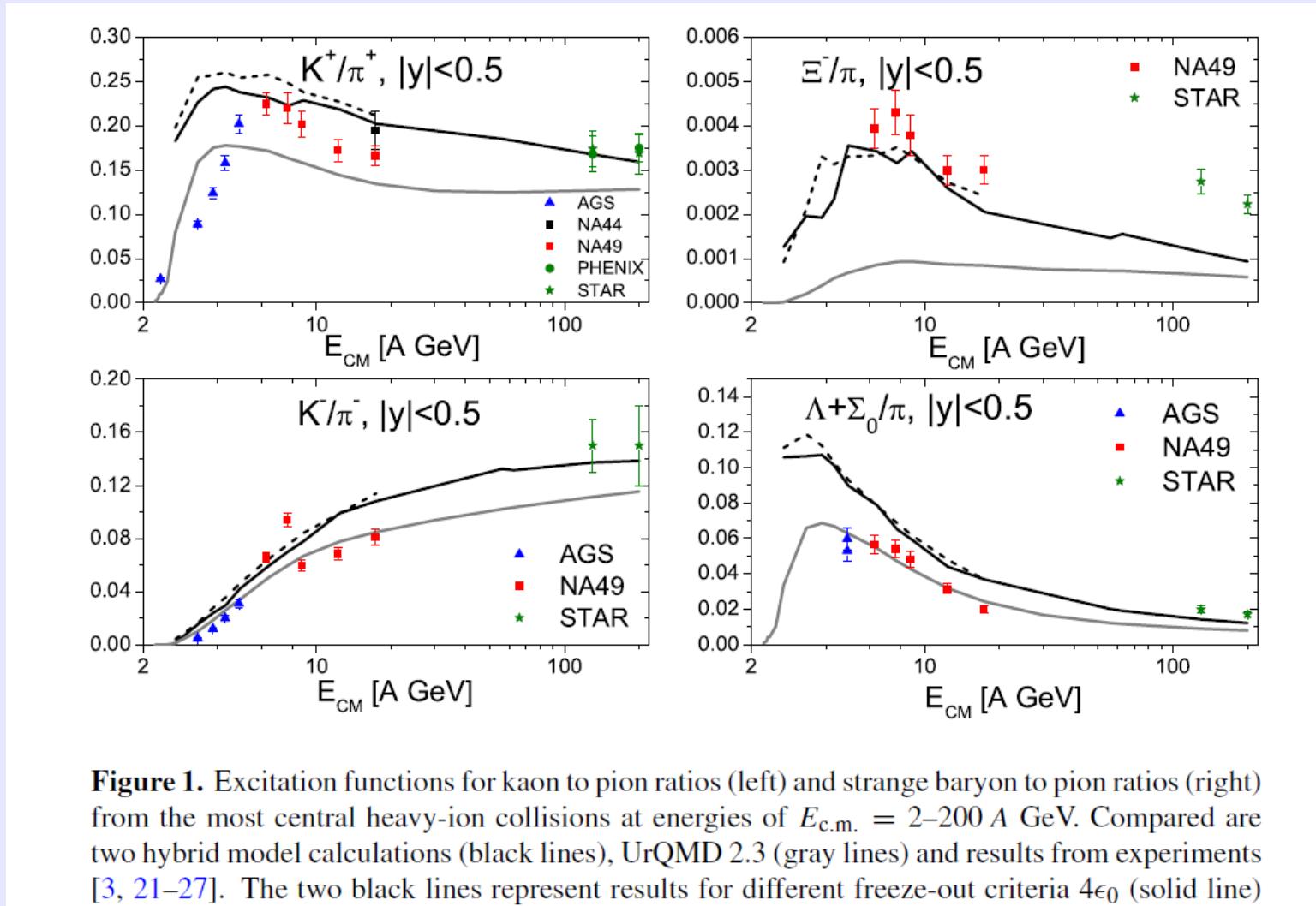
- string model tuned to pp collisions
- statistical hadronization at full chemical equilibrium (hybrid UrQMD)
- different mechanisms where strange quarks produced in the partonic phase are “conserved” (PHSD)

They generally fail to reproduce strangeness enhancement in the first version



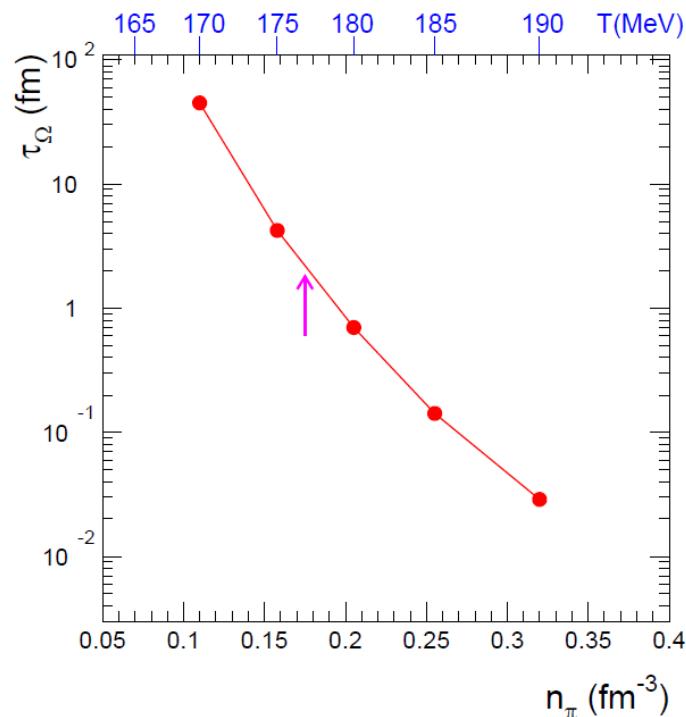
Courtesy of E. Bratkovskaya

# Enhancement is obtained through the local equilibrium assumption



**Figure 1.** Excitation functions for kaon to pion ratios (left) and strange baryon to pion ratios (right) from the most central heavy-ion collisions at energies of  $E_{\text{c.m.}} = 2-200 A \text{ GeV}$ . Compared are two hybrid model calculations (black lines), UrQMD 2.3 (gray lines) and results from experiments [3, 21–27]. The two black lines represent results for different freeze-out criteria  $4\epsilon_0$  (solid line)

# Local equilibrium: a feature of hadronization (hadrons born at equilibrium) or multi-particle collisions?



Further resonant states invoked as possible  
catalyzers of equilibration in the hadronic phase  
("Hagedorn states", C. Greiner et al.)

So far, to my knowledge, no complete  
numerical computation available

# Statistical hadronization model

Besides reproducing the data with few parameters, it provides a common language for elementary (particularly pp) and heavy ion collisions

$$\langle n_j \rangle = \frac{(2S_j + 1)}{2\pi^2} V m_j^2 T K_2\left(\frac{m_j}{T}\right) \frac{Z(\vec{Q} - \vec{q}_j)}{Z(\vec{Q})} \gamma_s^{n_s}$$

pp



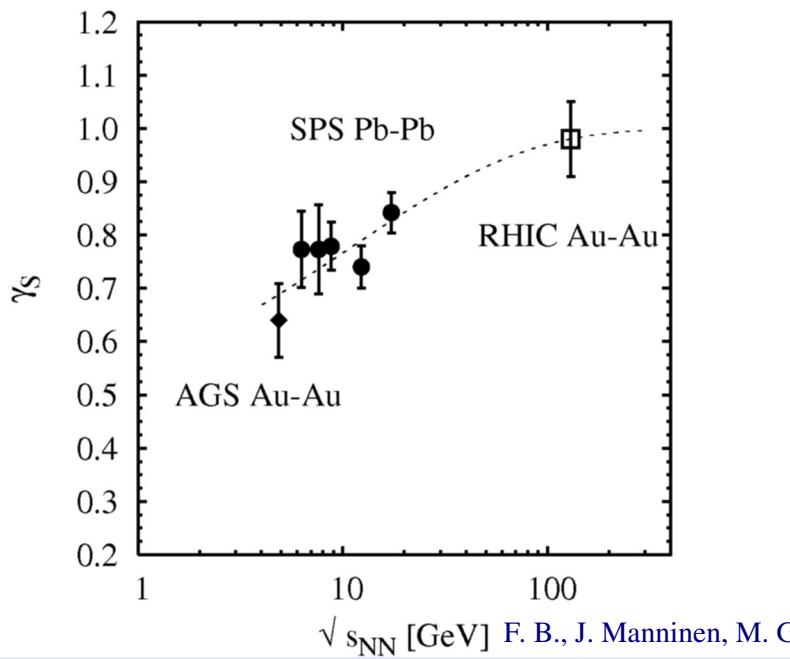
$V \rightarrow \infty$

$$\langle n_j \rangle = \frac{(2S_j + 1)}{2\pi^2} V m_j^2 T K_2\left(\frac{m_j}{T}\right) e^{\vec{\mu} \cdot \vec{q}_j / T} \gamma_s^{n_s}$$

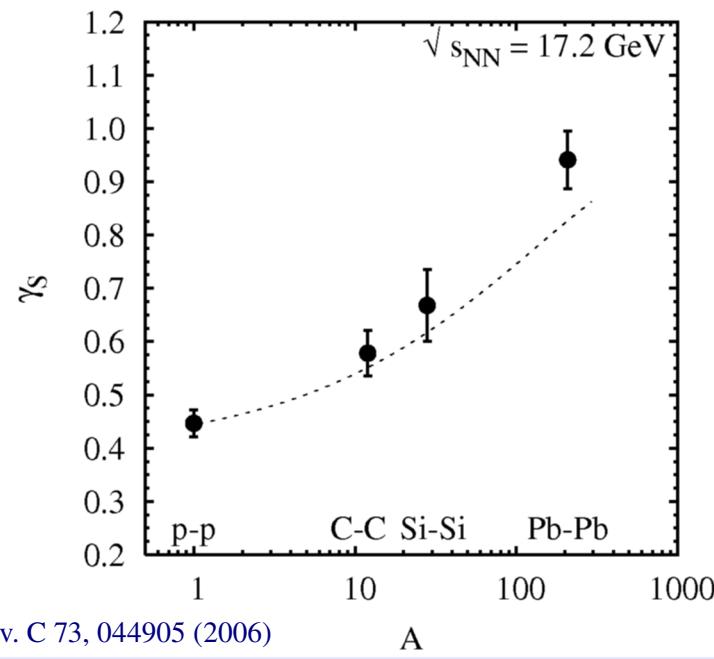
AA

There are some important assumptions about the distribution of charges needed to get to these formulae (see F. B. *An introduction to the statistical hadronization model*, arXiv:0902.3643)

# Relaxation of canonical suppression is not enough

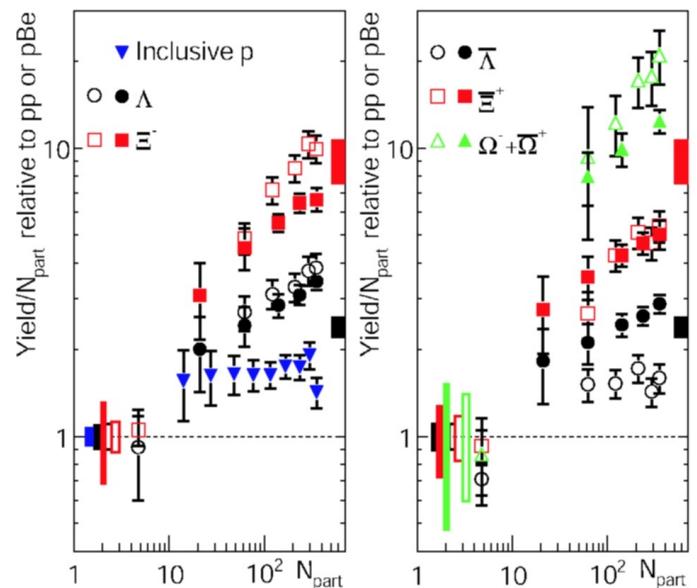
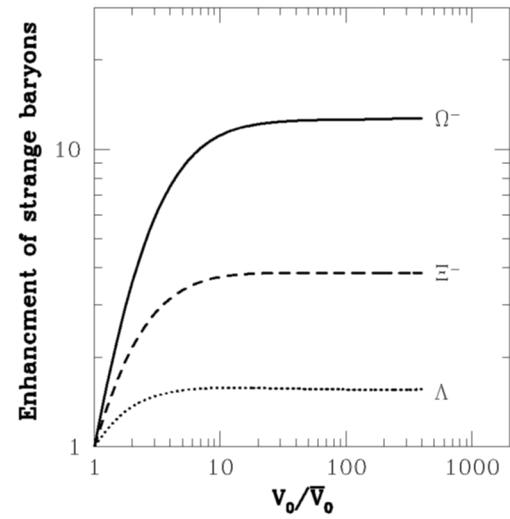


F. B., J. Manninen, M. Gazdzicki, Phys. Rev. C 73, 044905 (2006)

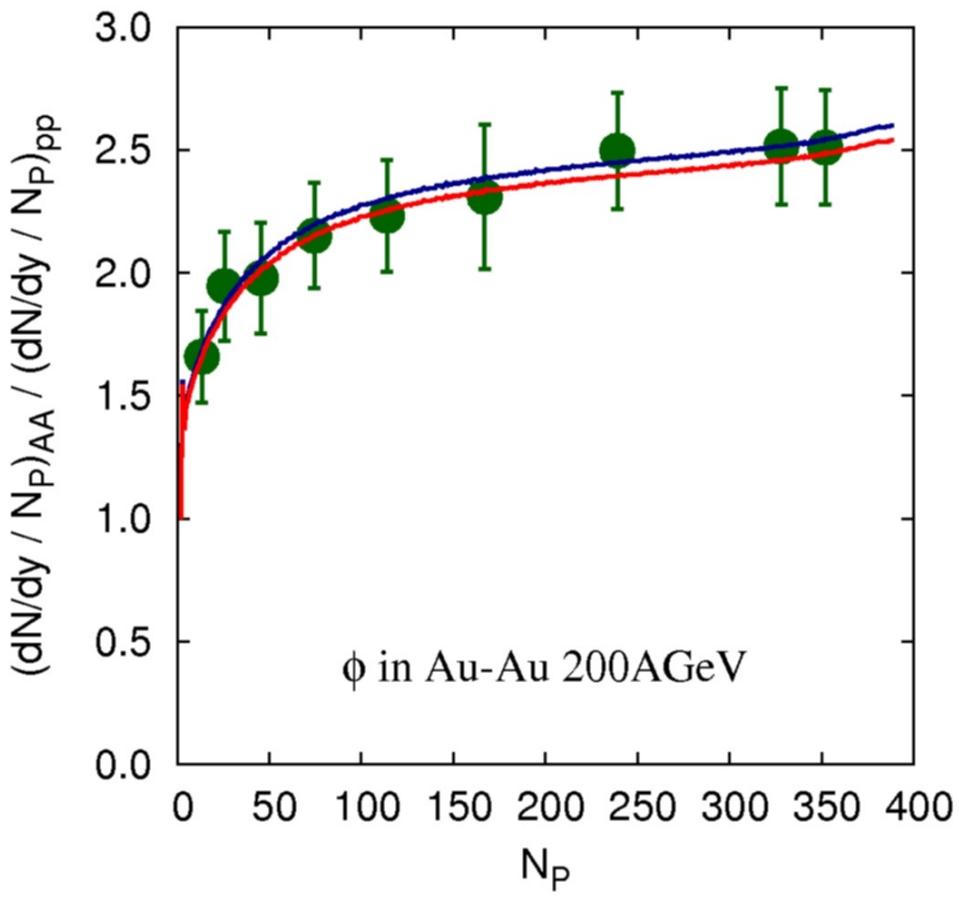


STAR coll., Phys. Rev. C 77 (2008) 044908

S. Hamieh, K. Redlich, A. Tounsi, Phys. Lett. B 486, 61 (2000)



# Discriminating probe: $\phi$ meson

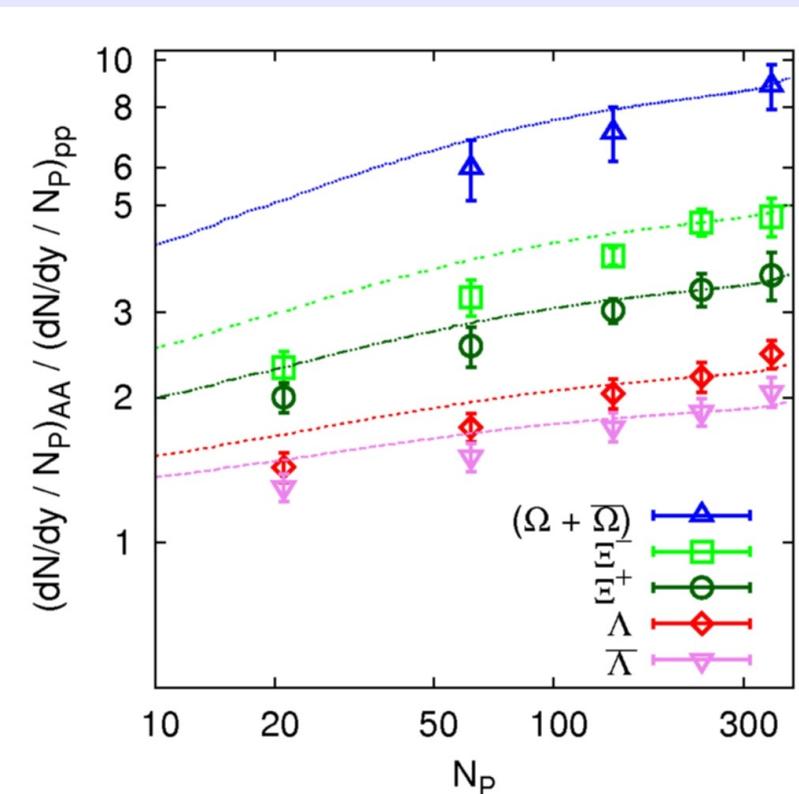


Successfully described by the core-corona model  
(superposition of fully equilibrated core  $\gamma_s=1$  and  
single NN collisions with  $\gamma_s < 1$ )

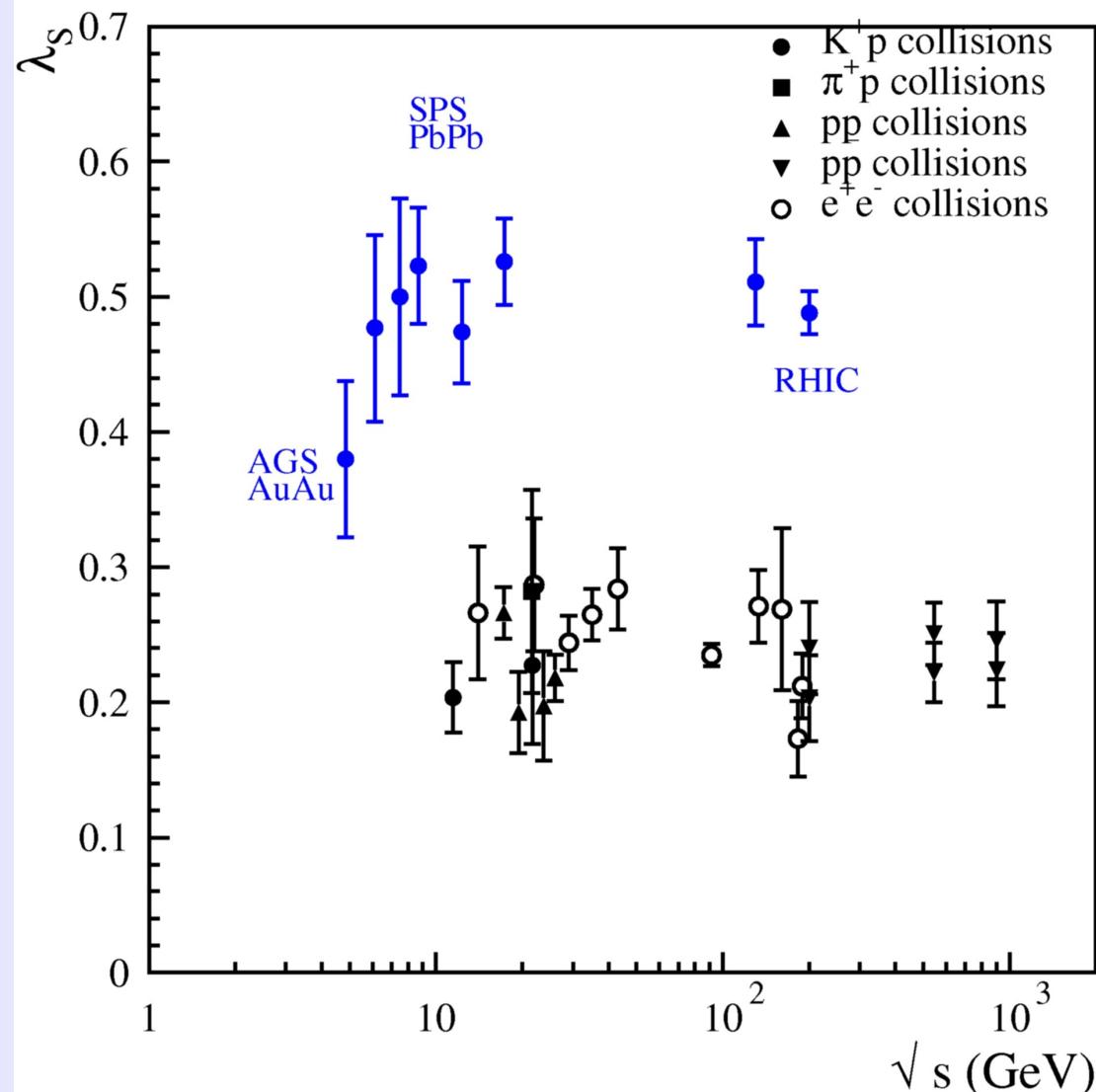
F.B., J. Manninen, J. Phys. G. 35 (2008) 104013;  
Phys. Lett. B 673 (2009) 19  
J. Aichelin, K. Werner, Phys. Rev. C 79 (2009) 064907

$$\langle n_\phi \rangle = \frac{3}{2\pi^2} V m_j^2 T K_2 \left( \frac{m_j}{T} \right) \gamma_s^2$$

in both pp and AA.  
No contribution from heavier resonances

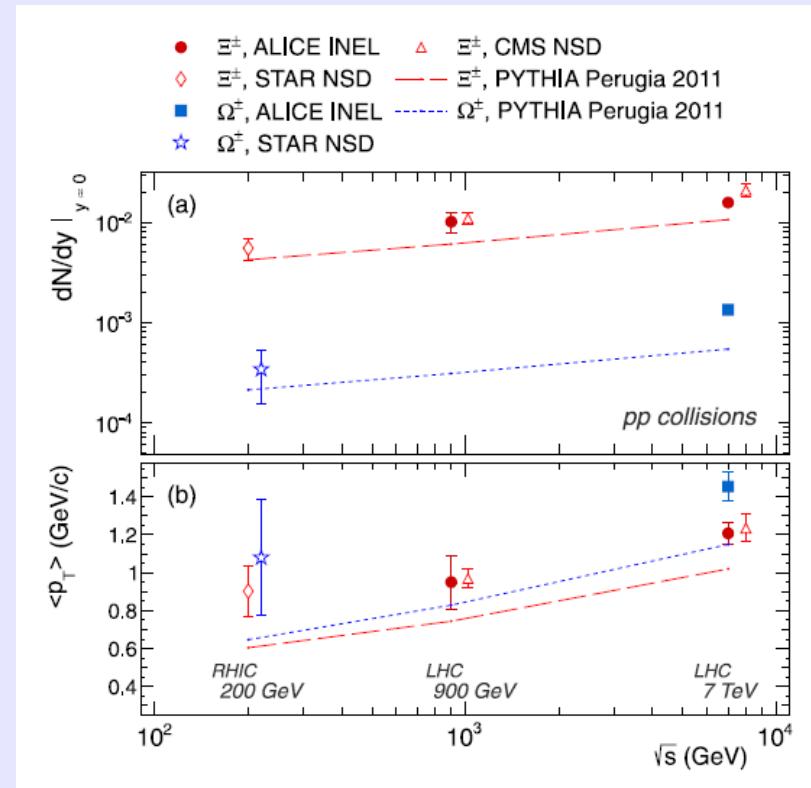
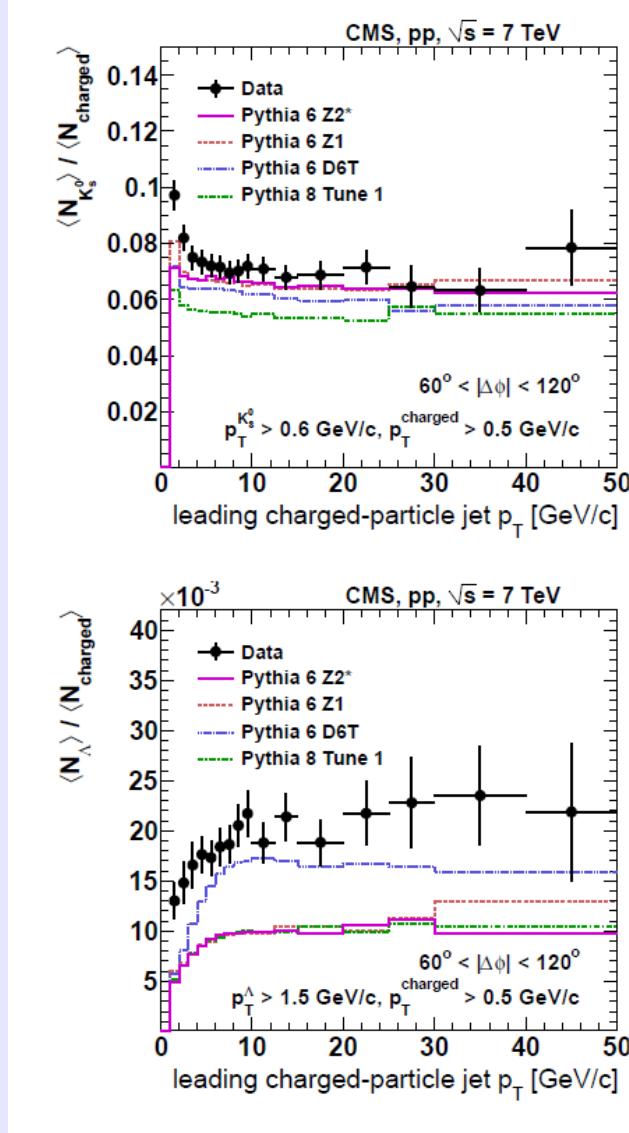


**Conclusion:** this strangeness enhancement cannot be explained within “hadronic” physics

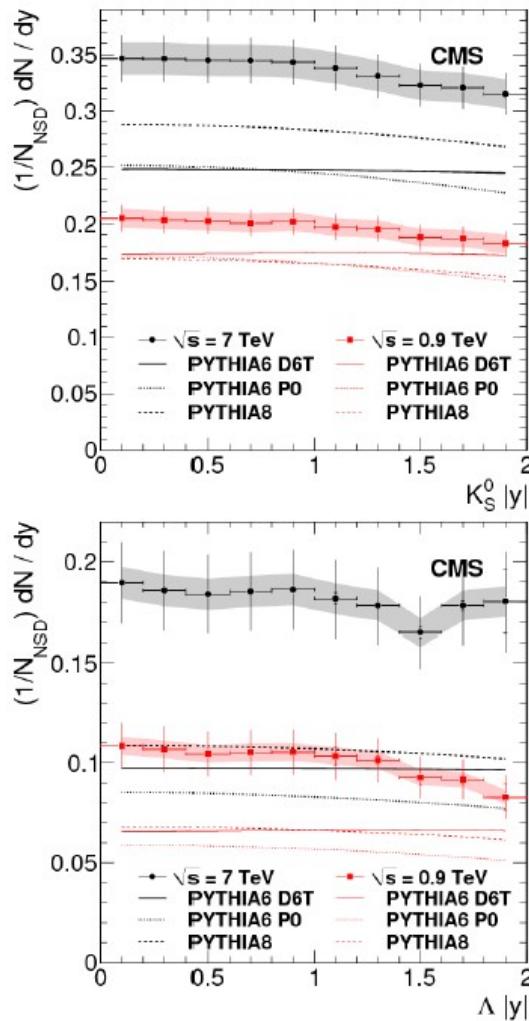


# Strangeness production in pp collisions

It is by now firmly established that the strangeness production in pp collisions increases with energy faster than predicted by PYTHIA (string model).



ALICE Coll., Phys. Lett. B712 (2012) 309



Particle	$\frac{dN}{dy} _{y=0}(\text{PYTHIA D6T})$	
	$0.9 \text{ TeV}$	$7 \text{ TeV}$
$K_S^0$	$0.87 \pm 0.01 \pm 0.07$	$0.72 \pm 0.01 \pm 0.06$
$\Lambda^0$	$0.60 \pm 0.01 \pm 0.07$	$0.54 \pm 0.01 \pm 0.06$
$\Xi^-$	$0.48 \pm 0.05 \pm 0.09$	$0.33 \pm 0.02 \pm 0.05$

### • Strangeness

- Significantly more strangeness is seen in data than in MC
- Factor 3 for  $\Xi$  at 7 TeV
- Discrepancy grows with increasing mass and  $\sqrt{s}$
- $\langle p_T \rangle$  is much better described

**CONCLUSION:** Particles with more strange quarks are more enhanced (w.r.t. PYTHIA) and the more at higher energy

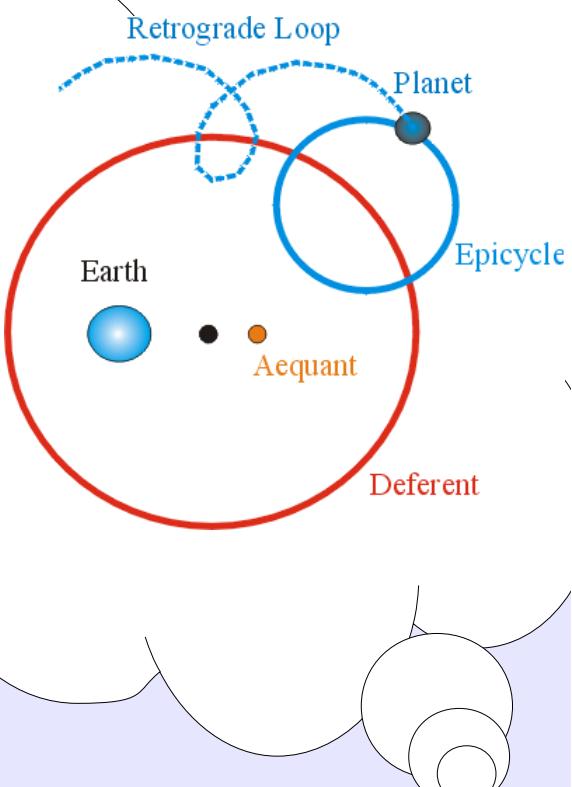
# What is a string-model tuning ?

Parameter	Name	Default	Range gen.	Fit Result		
				Val.	stat.	sys.
$\lambda_{QCD}$	PARJ(81)	0.4	0.25 - 0.35	0.297	$\pm 0.004$	$^{+ 0.007}_{- 0.008}$
$Q_0$	PARJ(82)	1.0	1.0 - 2.0	1.56	$\pm 0.11$	$^{+ 0.21}_{- 0.15}$
$a$	PARJ(41)	0.5	0.1 - 0.5	0.417	$\pm 0.022$	$^{+ 0.011}_{- 0.015}$
$b$	PARJ(42)	0.9	0.850		optimized	
$\sigma_q$	PARJ(21)	0.35	0.36 - 0.44	0.408	$\pm 0.005$	$^{+ 0.004}_{- 0.004}$
$P(^1S_0)_{ud}$	-	0.5	0.3 - 0.5	0.297	$\pm 0.021$	$^{+ 0.102}_{- 0.011}$
$P(^3S_1)_{ud}$	-	0.5	0.2 - 0.4	0.289	$\pm 0.038$	$^{+ 0.004}_{- 0.026}$
$P(^1P_1)_{ud}$	-	0.	see text		0.096	
$P(\text{oth.} P - \text{states})_{ud}$	-	0.	see text		0.318	
$\gamma_s$	PARJ(2)	0.30	0.27 - 0.31	0.308	$\pm 0.007$	$^{+ 0.004}_{- 0.036}$
$P(^1S_0)_s$	-	0.4	0.3 - 0.5	0.410	$\pm 0.038$	$^{+ 0.026}_{- 0.013}$
$P(^3S_1)_s$	-	0.6	0.2 - 0.4	0.297	$\pm 0.021$	$^{+ 0.020}_{- 0.004}$
$P(P - \text{states})_s$	-	0.	see text		0.293	
$\epsilon_c$	PARJ(54)	-	variable	-0.0372	$\pm 0.0007$	$^{+ 0.0011}_{- 0.0012}$
$P(^1S_0)_c$	-	0.25	0.26			
$P(^3S_1)_c$	-	0.75	0.44		adj. to data	
$P(P - \text{states})_c$	-	0.	0.3			
$\epsilon_b$	PARJ(55)	-	variable	-0.00284	$\pm 0.00005$	$^{+ 0.00012}_{- 0.00010}$
$P(^1S_0)_b$	-	0.25	0.175			
$P(^3S_1)_b$	-	0.75	0.525		adj. to data	
$P(P - \text{states})_b$	-	0.	0.3			
$P(q\bar{q})/P(q)$	PARJ(1)	0.1	0.08 - 0.11	0.099	$\pm 0.001$	$^{+ 0.005}_{- 0.002}$
$P(u\bar{s})/P(u\bar{d})/\gamma_s$	PARJ(3)	0.4	0.65		adj. to data	
$P(u\bar{d}1)/P(u\bar{d}0)$	PARJ(4)	0.05	0.07		adj. to data	
extra baryon supp.	PARJ(19)	0.	0.5		adj. to data only uds	
extra $\eta$ supp.	PARJ(25)	1.0	0.65	0.65	$\pm 0.06$	
extra $\eta'$ supp.	PARJ(26)	1.0	0.23	0.23	$\pm 0.05$	

Table 49: Parameter setting and fit results for JETSET 7.4 PS with default decays

Specific  
for  
Light-flav.  
abundances

Specific  
for  
Light-flav.  
abundances

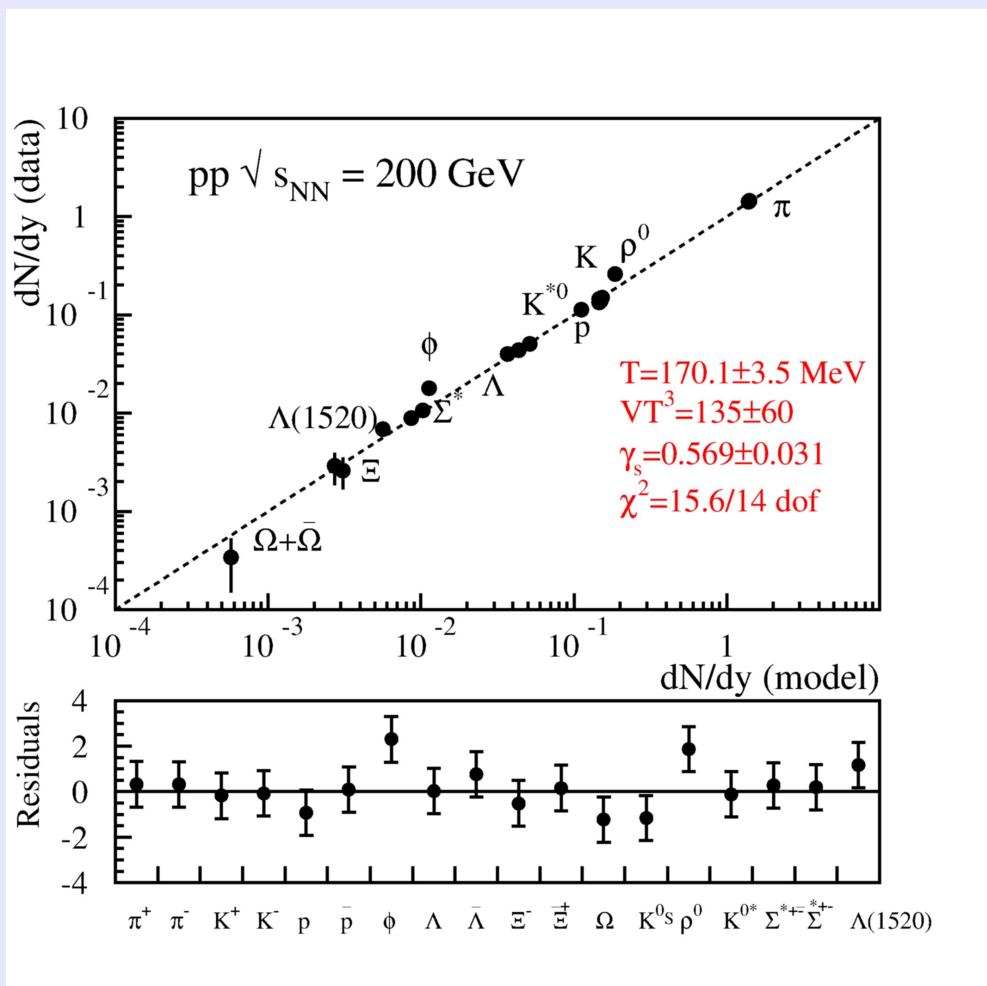


From DELPHI coll., "The next round of...identified particles", hep-ex 9511011

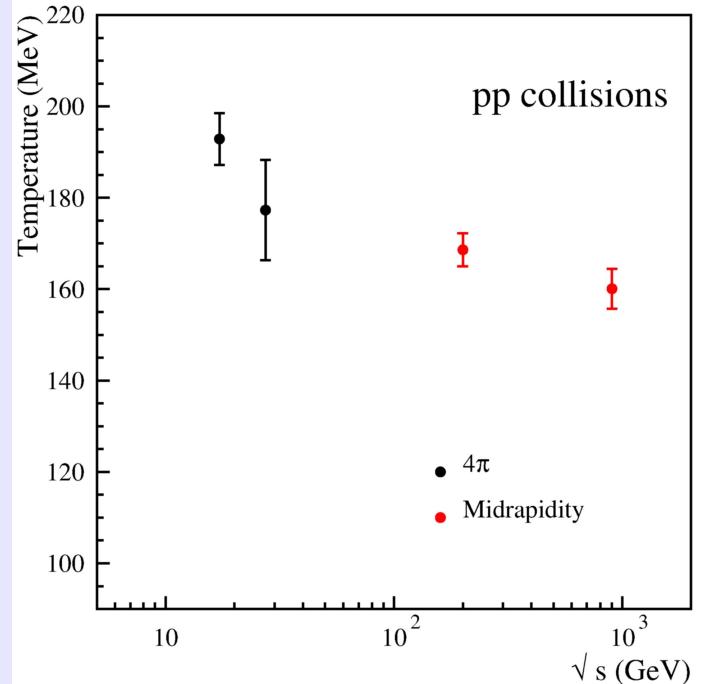
Failure depends on the assumed energy-independence of hadronization parameters

# A re-analysis of pp collisions within the statistical model

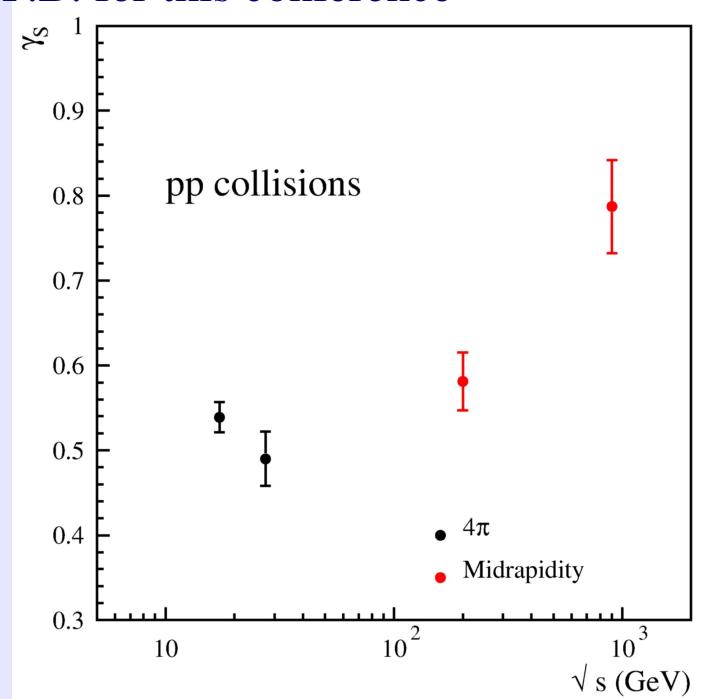
Hadrons are born at equilibrium  
(with undersaturation of strangeness)



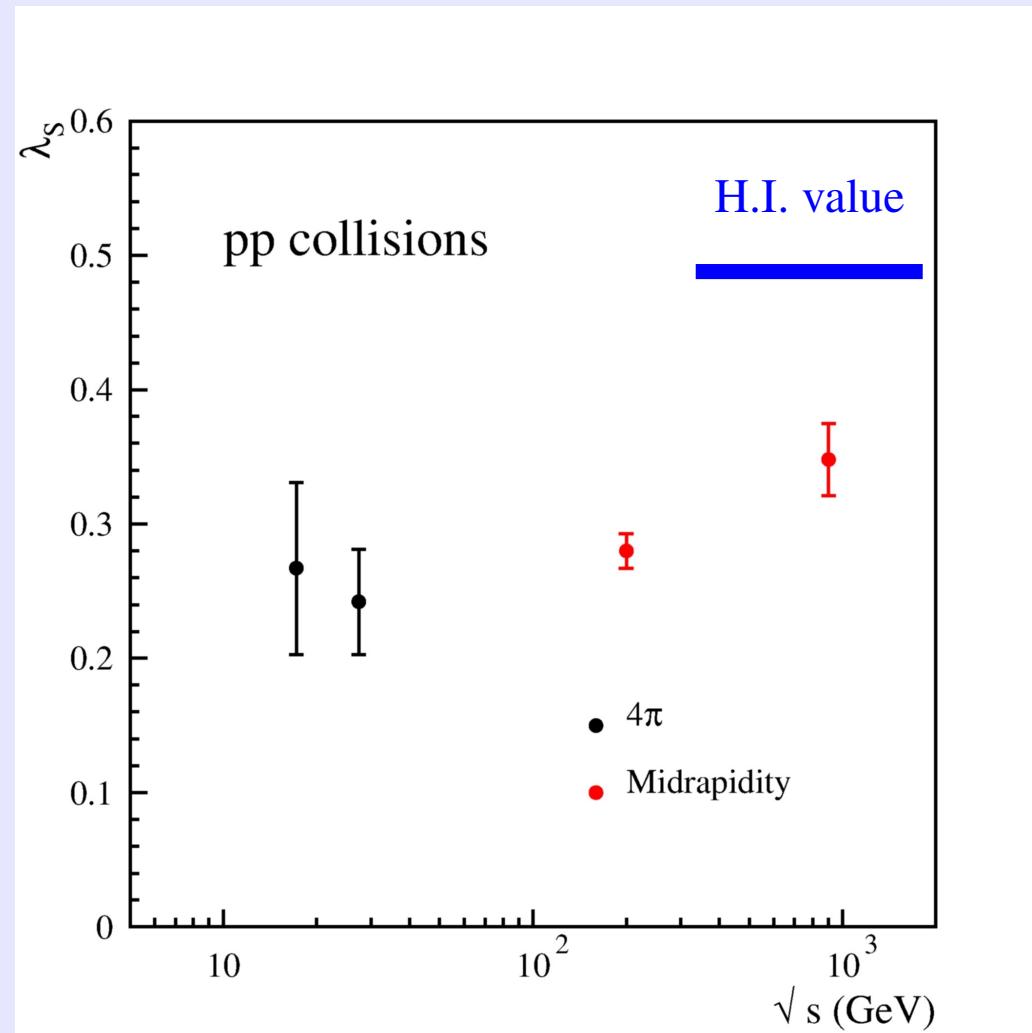
F. B., P. Castorina, A. Milov, H. Satz Eur. Phys. C 66 (2010)



F.B. for this conference

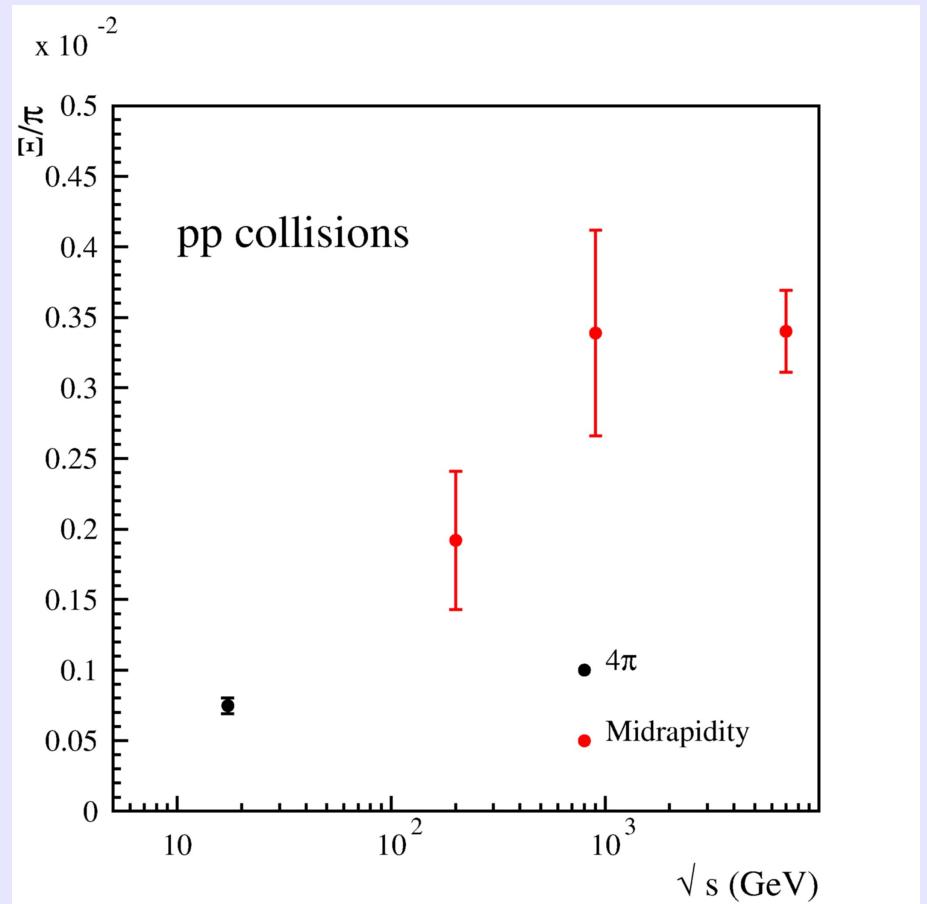
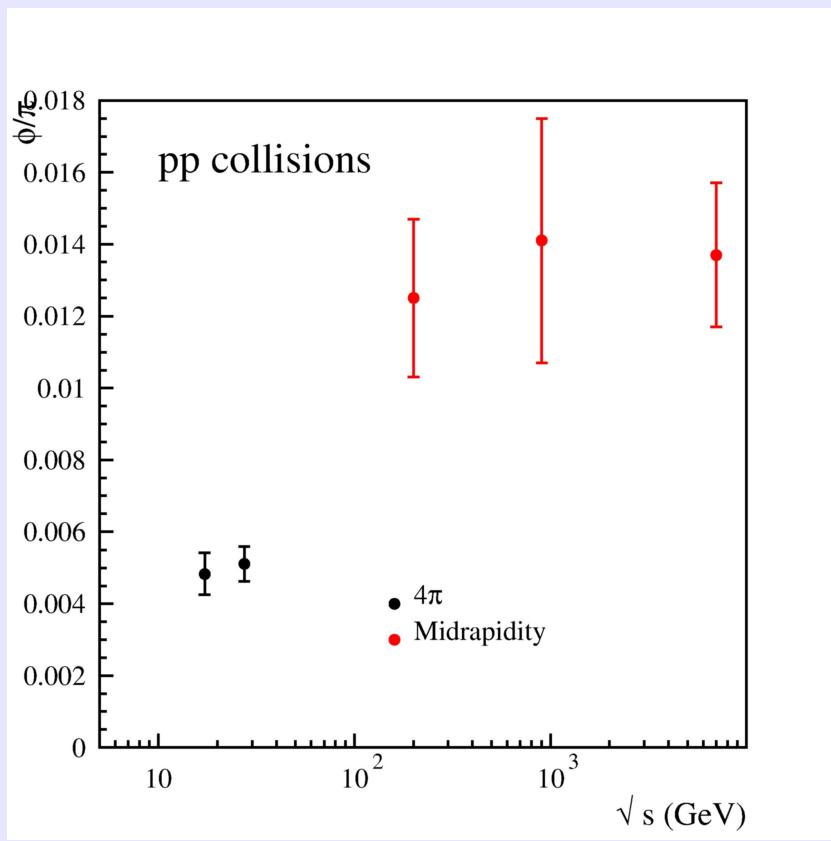


# A genuine strangeness enhancement in pp collisions?



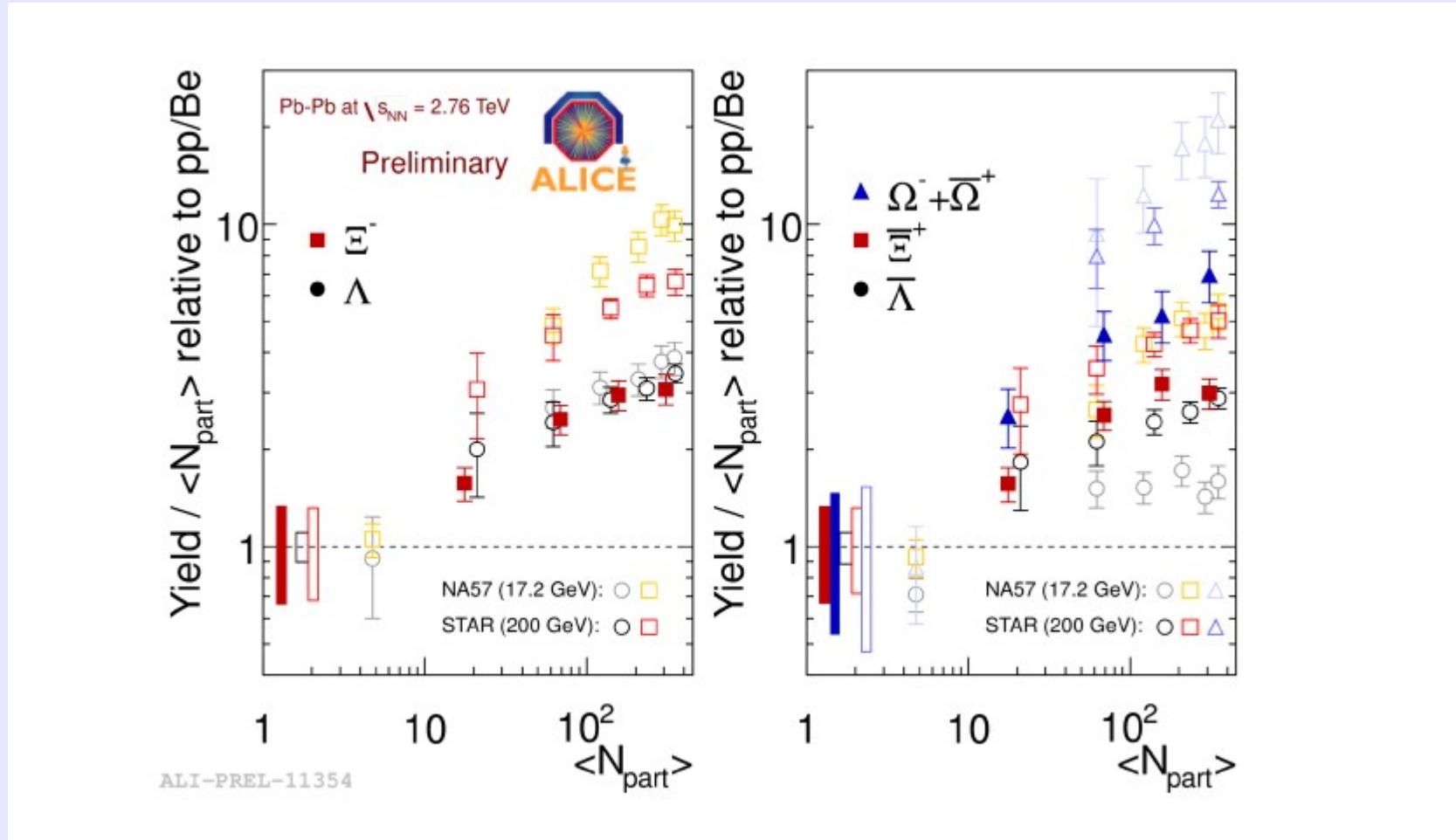
F.B. for this conference

# Mostly a canonical enhancement in pp collisions?



Data points from NA27,NA49,STAR,ALICE

The enhancement in pp at 7 TeV seems to be independent of multiplicity  
(P. R. Petrov, Ph.D. Thesis, University of Birmingham, March 2013)



**CONCLUSION:** Evidence of pp collisions looking more similar to AA collisions at high energy with respect to strangeness production.  
Is it just a midrapidity effect?

# Strangeness production and anti-baryon suppression

Observed low proton yield at LHC w.r.t. to statistical model predictions

A. Andronic et al., J. Phys. G38, 124081 (2011)

Advocated as an effect of post-hadronization rescattering:

F. B., M. Bleicher, T. Kollegger, M. Mitrovski, T. Schuster and R. Stock Phys. Rev. C 85 (2012) 044921 (for SPS)

J. Steinheimer, J. Aichelin and M. Bleicher, Phys. Rev. Lett. 110 (2013) 042501

Y. Pan and S. Pratt, *Baryon Annihilation in Heavy Ion Collisions* arXiv:1210.1577

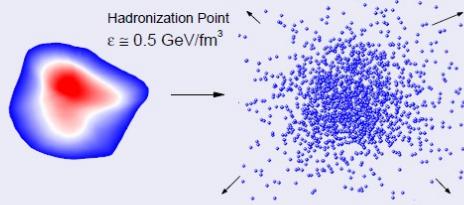
F. B., M. Bleicher, T. Kollegger, T. Schuster, J. Steinheimer and R. Stock, *Hadron Formation in Relativistic Nuclear Collisions*, arXiv:1212.2431

## Elementary Collisions

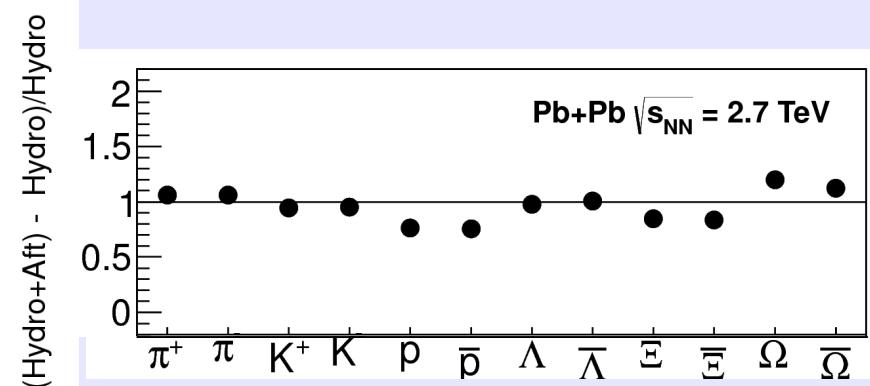


- Hadrons are born into equilibrium.
- They are few and escape the reaction volume immediately.

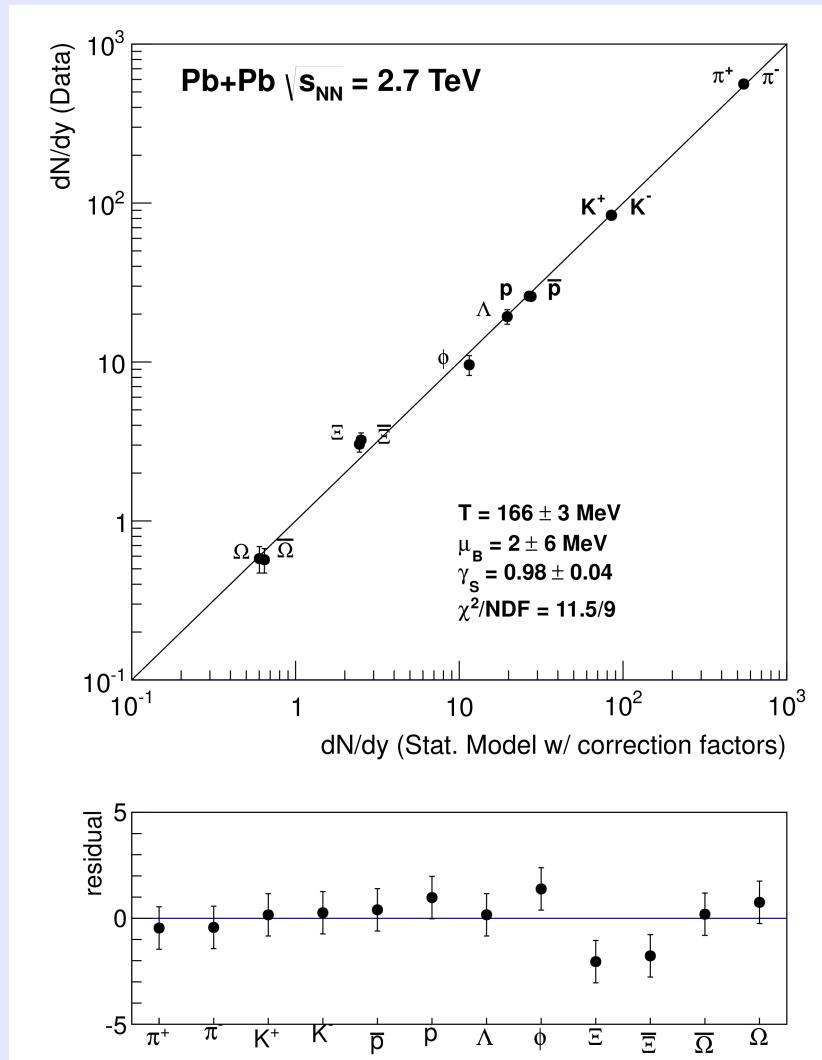
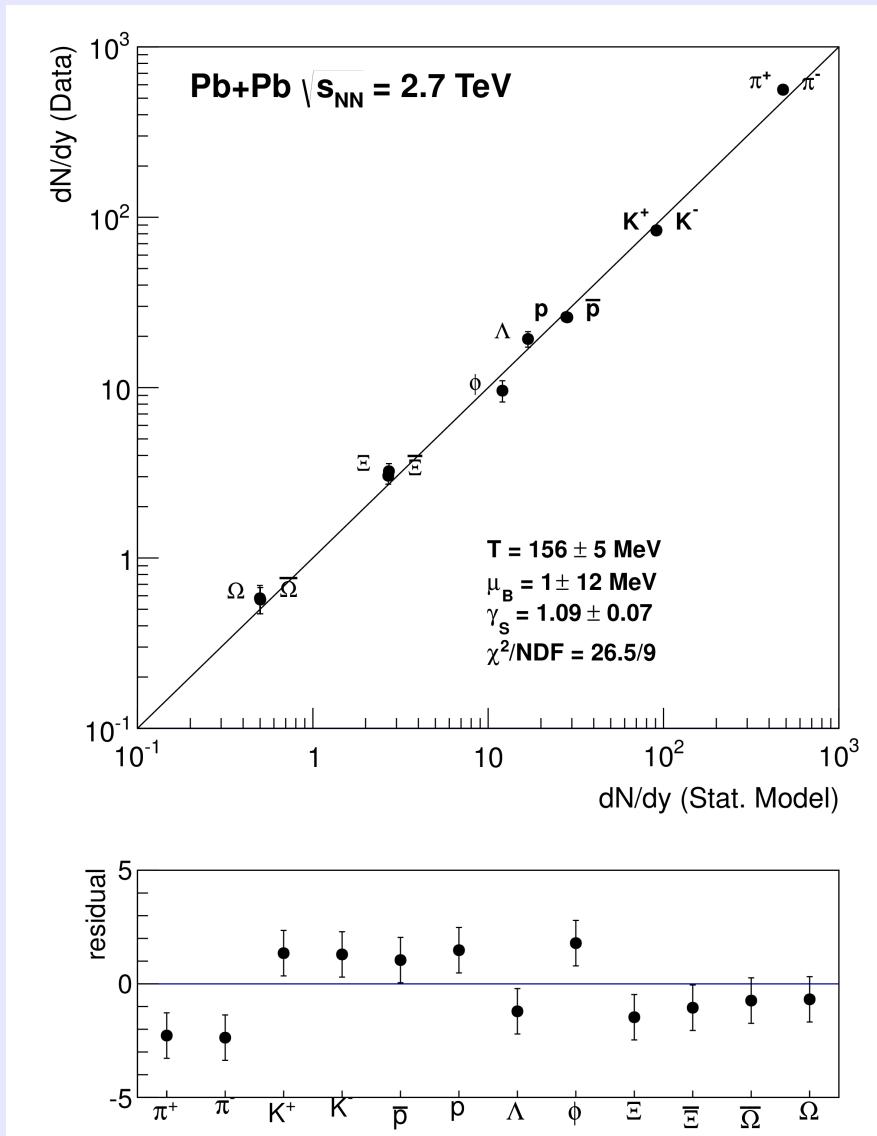
## Heavy Ion Collisions



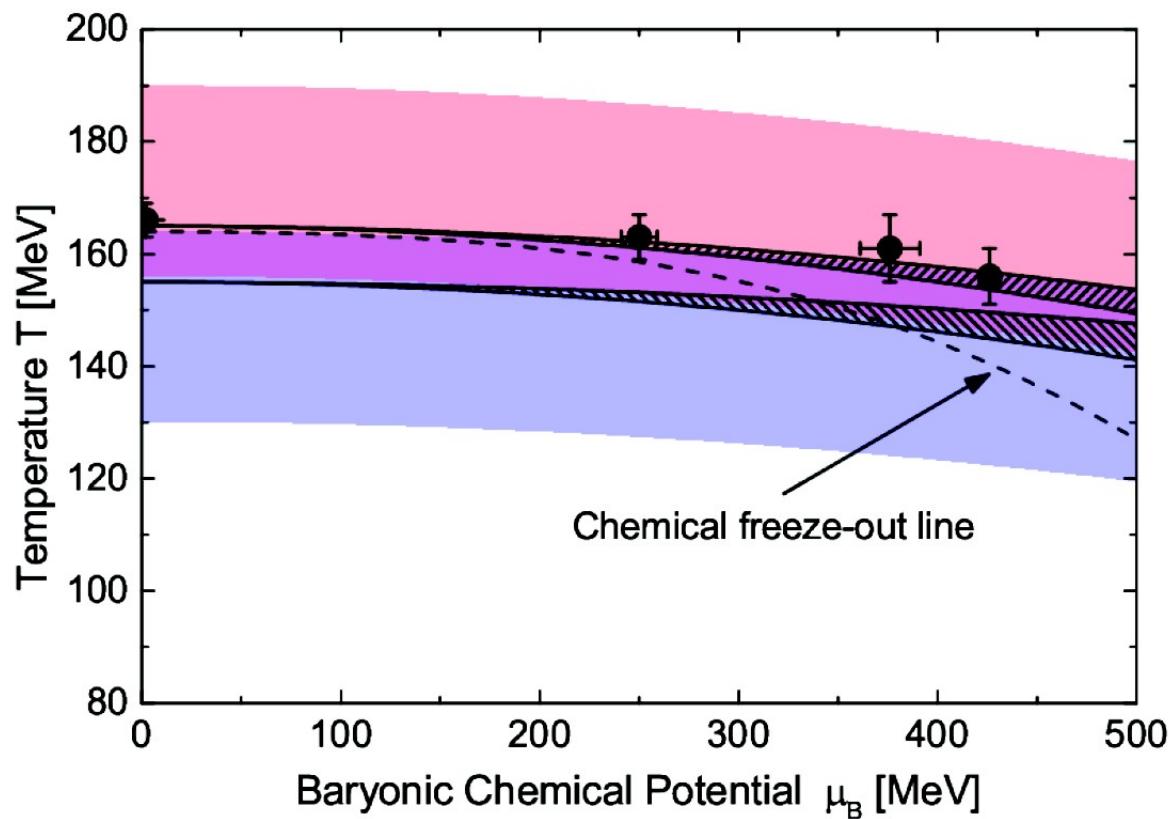
- Hadrons are born into equilibrium.
- They need more time to escape the reaction volume.
- They can undergo inelastic collisions.



The use of (hybrid) UrQMD transport model correction factors leads to an improved agreement with statistical hadronization model fit



# Comparing reconstructed equilibrium point with lattice QCD



	$ T(\text{ MeV}) $	$ \mu_B(\text{ MeV}) $	$\gamma_S$	$ \chi^2/NDF $
Pb-Pb 20% central $\sqrt{s_{NN}} = 2.7 \text{ TeV}$				
Std. fit	$156 \pm 5$	$1 \pm 12$	$1.09 \pm 0.07$	26.5/9
Mod. fit	$166 \pm 3$	$2 \pm 6$	$0.98 \pm 0.04$	11.5/9
Pb-Pb 5% central $\sqrt{s_{NN}} = 17.3 \text{ GeV}$				
Std. fit	$151 \pm 4$	$266 \pm 9$	$0.91 \pm 0.05$	26.9/11
Mod. fit	$163 \pm 4$	$250 \pm 9$	$0.83 \pm 0.04$	20.4/11
Pb-Pb 5% central $\sqrt{s_{NN}} = 8.7 \text{ GeV}$				
Std. fit	$148 \pm 4$	$385 \pm 11$	$0.78 \pm 0.06$	17.9/9
Mod. fit	$161 \pm 6$	$376 \pm 15$	$0.72 \pm 0.06$	25.9/9
Pb-Pb 5% central $\sqrt{s_{NN}} = 7.6 \text{ GeV}$				
Std. fit	$140 \pm 1$	$437 \pm 5$	$0.91 \pm 0.01$	22.4/7
Mod. fit	$156 \pm 5$	$426 \pm 4$	$0.81 \pm 0.00$	14.7/7

Lattice calculations from

F. Karsch, J. Phys. G 38, 124098 (2011); S. Borsanyi et al., ibidem 124101  
G. Endrodi, Z. Fodor, S. D. Katz and K. K. Szabo, JHEP 1104, 001 (2011)

See also: *The critical line of two-flavor QCD at finite isospin or baryon densities from imaginary chemical potentials.* P. Cea, L. Cosmai, M. D'Elia, A. Papa, F. Sanfilippo, Phys.Rev. D85 (2012) 094512

# A different explanation

Strange particles may be formed at a larger temperature than non-strange

R. Bellwied, S. Borsanyi, Z. Fodor, S. Katz and C. Ratti, arXiv:1305.6297 [hep-lat].

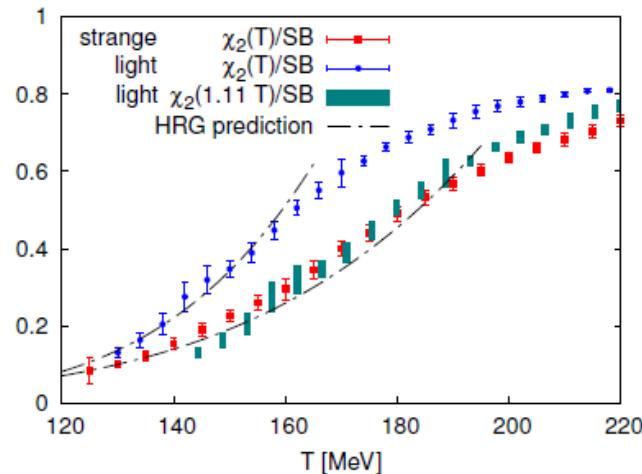
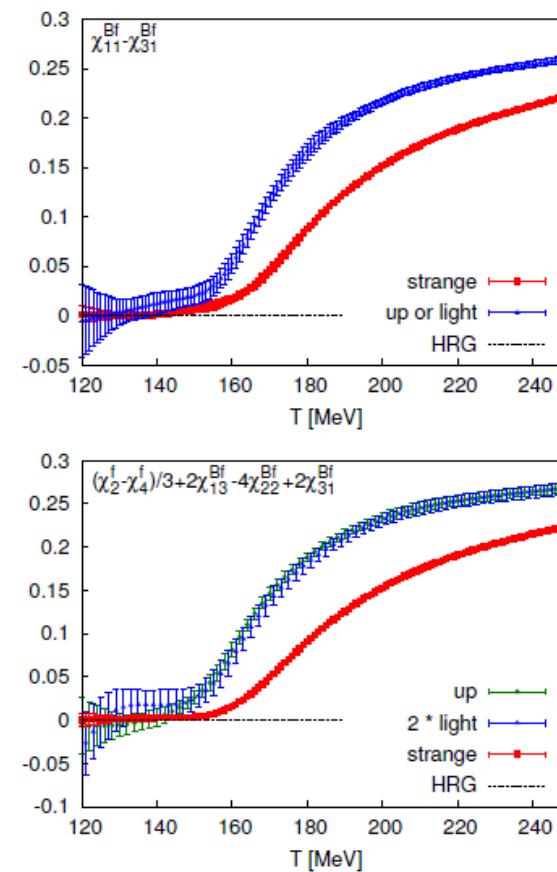


FIG. 1. Light and strange quark susceptibilities in the continuum limit (plotted as blue circles and red squares, respectively). The transition temperatures defined by the inflection points for  $\chi_2^L$  (150 MeV) and for  $\chi_2^s$  (165 MeV) differ by  $\approx 15$  MeV. A rescaling transformation is shown with bars.



In principle, it could be tested with multiplicities. Best in pp collisions!

See also the extended discussion of F. Karsch,  
arXiv:1307.3978

$$\chi_{mn}^{XY} = \frac{\partial^{(m+n)} [p(\hat{\mu}_X, \hat{\mu}_Y)/T^4]}{\partial \hat{\mu}_X^m \partial \hat{\mu}_Y^n} \Big|_{\hat{\mu}=0},$$

$$\begin{aligned} M(c_1, c_2) &= \chi_2^S - \chi_{22}^{BS} + c_1 v_1 + c_2 v_2, \\ B_1(c_1, c_2) &= \frac{1}{2} (\chi_4^S - \chi_2^S + 5\chi_{13}^{BS} + 7\chi_{22}^{BS}) \\ &\quad + c_1 v_1 + c_2 v_2, \\ B_2(c_1, c_2) &= -\frac{1}{4} (\chi_4^S - \chi_2^S + 4\chi_{13}^{BS} + 4\chi_{22}^{BS}) \\ &\quad + c_1 v_1 + c_2 v_2, \\ B_3(c_1, c_2) &= \frac{1}{18} (\chi_4^S - \chi_2^S + 3\chi_{13}^{BS} + 3\chi_{22}^{BS}) \\ &\quad + c_1 v_1 + c_2 v_2. \end{aligned}$$

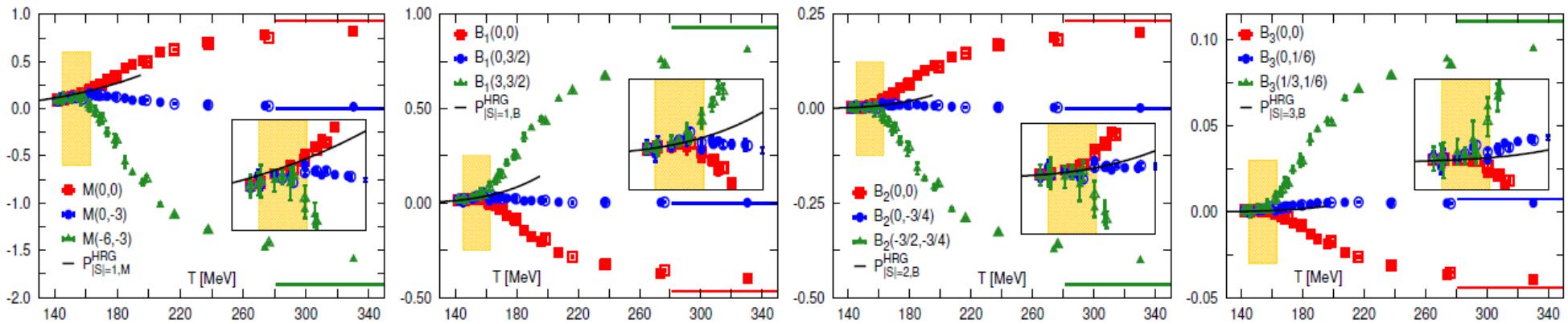


FIG. 2. Four combinations [see Eqs. (3-6)] of net strangeness fluctuations and baryon-strangeness correlations  $M(c_1, c_2)$ ,  $B_1(c_1, c_2)$ ,  $B_2(c_1, c_2)$  and  $B_3(c_1, c_2)$  (from left to right), each for three different sets of  $(c_1, c_2)$ . Up to the chiral crossover temperature  $T_c = 154(9)$  MeV [13] (shown by the shaded regions), independent of  $(c_1, c_2)$ , these combinations give the partial pressures of  $|S| = 1$  mesons ( $P_{|S|=1,M}^{HRG}$ ) and  $|S| = 1, 2, 3$  baryons ( $P_{|S|=1,B}^{HRG}$ ,  $P_{|S|=2,B}^{HRG}$ ,  $P_{|S|=3,B}^{HRG}$ ) in an uncorrelated gas of hadrons having masses equal to their vacuum masses, i.e. in the HRG model. Above the  $T_c$  region such a hadronic description breaks down (shown in the insets) and all the combinations smoothly approach towards their respective,  $(c_1, c_2)$  dependent, high temperature limits (indicated by the lines at the high temperatures) described by the non-interacting massless strange quarks. The LQCD results for the  $N_\tau = 6$  and 8 lattices are shown by the open and filled symbols respectively.

$\sqrt{S_{NN}}$ (GeV)	Ref	$10^4 V_S$ (MeV $^{-3}$ )	$10^4 V_{NS}$ (MeV $^{-3}$ )	$T_S$ (MeV)	$T_{NS}$ (MeV)	$\mu_S$ (MeV)	$\mu_{NS}$ (MeV)	$\chi^2/N_{df}$
6.27	[8–11]	1.1 (0.2)	1.6 (0.3)	139 (4)	131 (4)	435 (11)	446 (10)	1.6/4
7.62	[8–11]	1.2 (0.2)	1.4 (0.3)	144 (3)	139 (3)	399 (13)	395 (10)	3.0/5
7.7	[15]	1.0 (0.2)	1.5 (0.6)	147 (3)	138 (8)	424 (18)	368 (28)	8.0/4
8.76	[9–12]	0.8 (0.1)	1.3 (0.4)	152 (3)	145 (5)	393 (15)	358 (18)	4.4/5
11.5	[15]	1.0 (0.1)	1.9 (0.7)	157 (3)	142 (7)	310 (15)	278 (28)	0.8/4
17.3	[10–14]	1.1 (0.2)	2.8 (0.4)	157 (3)	142 (3)	214 (14)	208 (8)	15/7
39.	[15]	1.0 (0.2)	2.4 (0.8)	168 (4)	148 (8)	115 (13)	98 (24)	1.2/4
62.4	[16–18]	1.3 (0.3)	2.3 (0.7)	169 (5)	155 (8)	70 (20)	65 (25)	8.0/7
130.	[19–22]	1.6 (0.5)	2.5 (1.0)	169 (6)	157 (8)	35 (23)	25 (20)	4.4/5
200.	[23–25]	2.2 (0.4)	2.8 (0.8)	164 (3)	155 (6)	31 (11)	22 (16)	23/6
2700.	[26]	4.1 (0.6)	8.8 (0.8)	162 (3)	146 (3)	14 (12)	-2 (7)	4.4/6

Some years ago, we suggested precisely the opposite (for e+e-)  
F. B., P. Castorina, J. Manninen, H. Satz, Eur. Phys. J. C56 (2008) 493

$T$	$m_s = 0.075$	$m_s = 0.100$	$m_s = 0.125$
$T(00)$	0.178	0.178	0.178
$T(0s)$	0.172	0.167	0.162
$T(ss)$	0.166	0.157	0.148
$T(000)$	0.178	0.178	0.178
$T(00s)$	0.174	0.171	0.167
$T(0ss)$	0.170	0.164	0.157
$T(sss)$	0.166	0.157	0.148

$\sigma = 0.2 \text{ GeV}^2$

Our goal was to  
explain  $\gamma_s$

# Final reflection

How to compare a N parameter fit with close-to-reasonable  $\chi^2$  with an N+x with a “perfect”  $\chi^2$ ?

**SIMPLICITY** and **ECONOMY** of the description shall discriminate  
(Occam's razor principle)

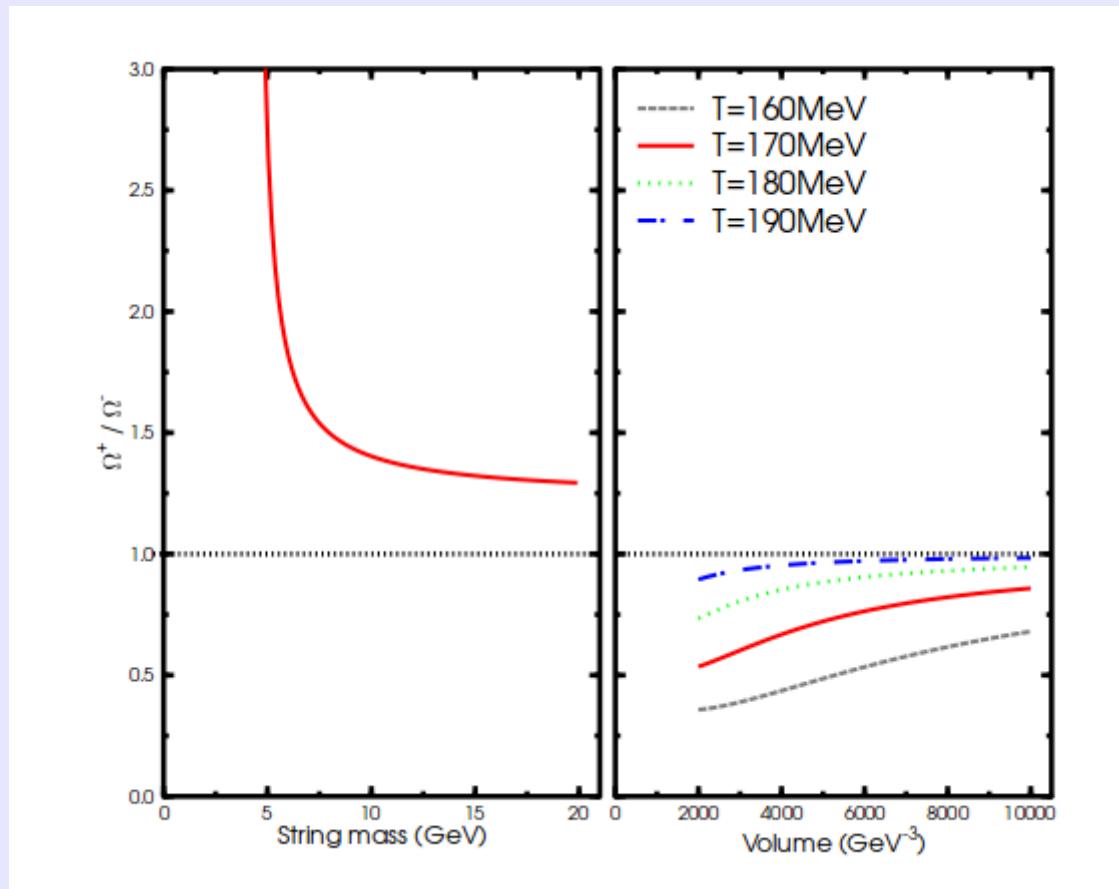
- Free parameters are sometimes needed and useful to understand the data,  
But they should be always waiting for an explanation (connection with some known phenomenon).
- Free parameters of a theory have a natural hierarchy ( $T > \gamma_s$ ) and also a numerical hierarchy.
- Once a fairly good description is achieved, it would be desirable to describe the deviations without introducing new parameters.

# CONCLUSIONS

- Strangeness enhancement in AA from energies  $O(10)$  GeV is genuine
- Relative strangeness production in pp collisions increases with energy and faster than predicted by any tuned version of the string-model.  
Is it a size effect?
- Consequently, pp collisions seem to asymptotically look like AA collisions also with regard to strangeness production
- Anti-baryon suppression indicates that hadrons rescatter after hadronization
- Do strange quarks hadronize at higher T?

# How to discriminate statistical and string model in pp collisions

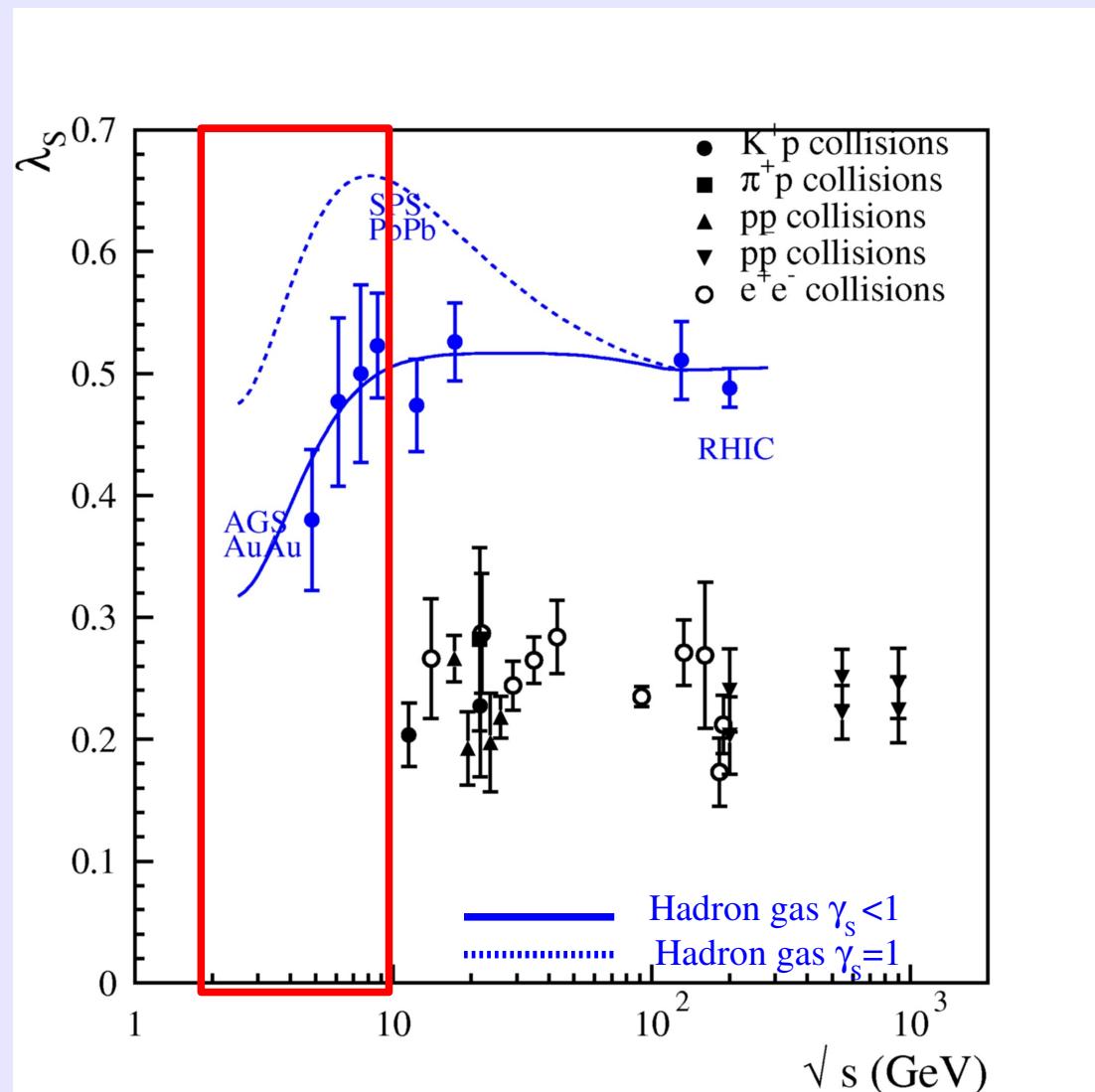
(M. Bleicher et al., Phys. Rev. Lett. 88, 202501 (2002))



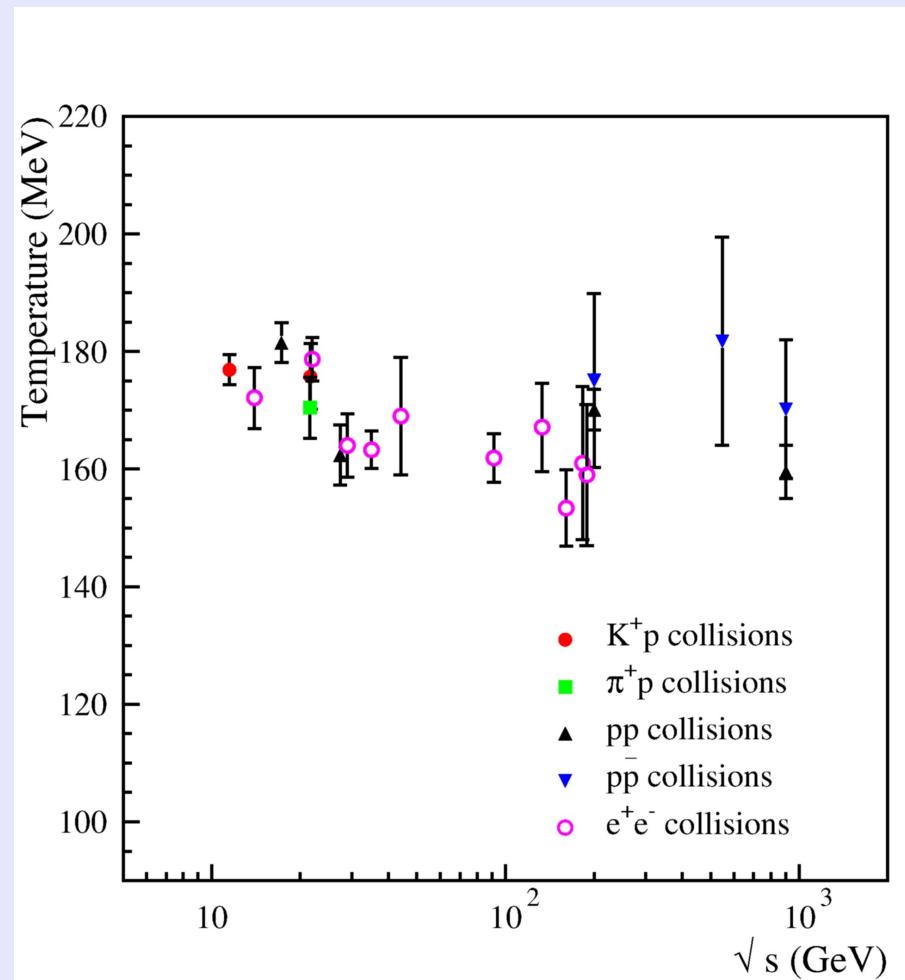
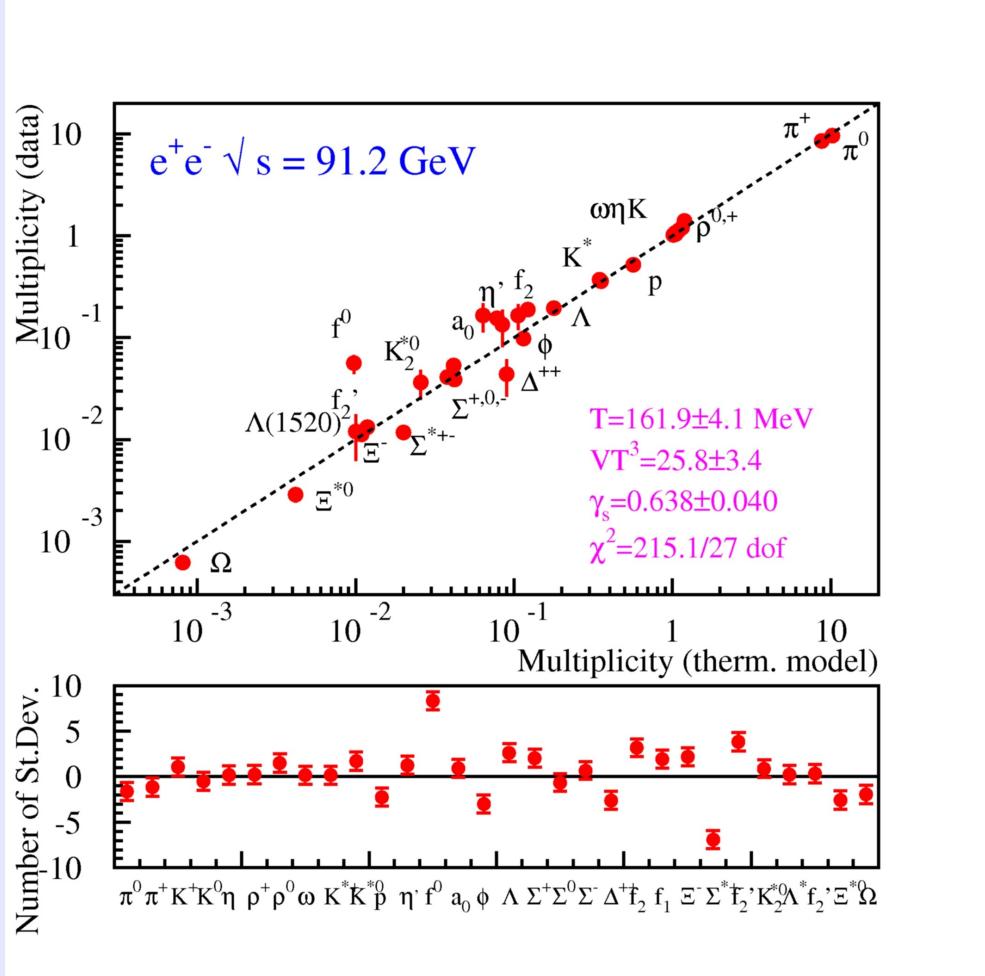
# What at SPS? Where is the onset of full chemical equilibrium?

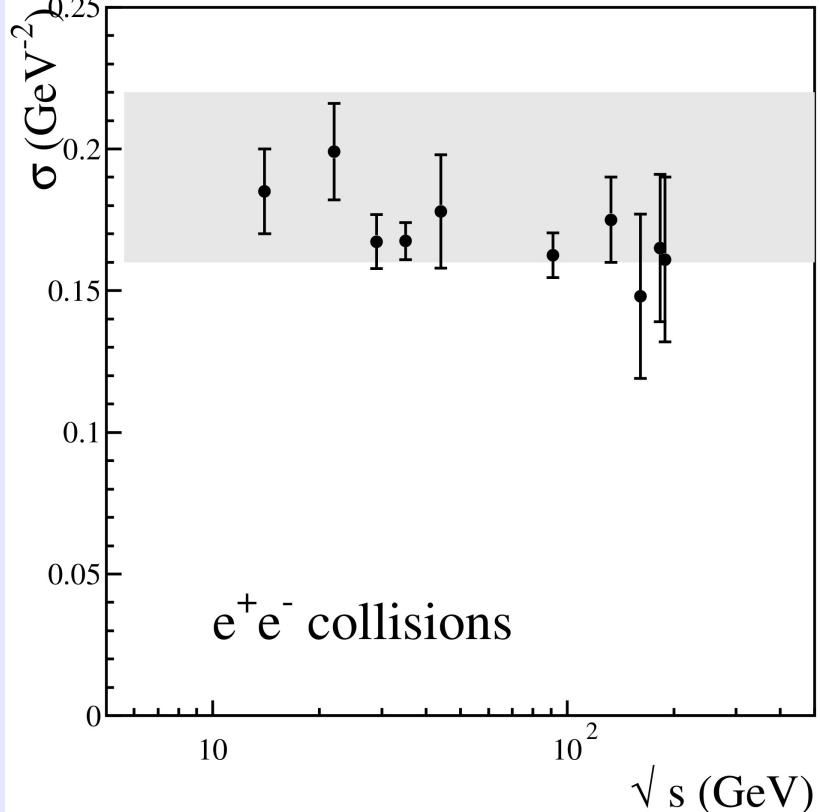
Can core-corona effect account for  $\gamma_s$  also at SPS?

Need to re-analyze carefully SPS and AGS data as a function of centrality and system size



# Where do we start from?





The parameter values fall within the expected region

