

Flavor hierarchy in the confinement transition of QCD

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in collaboration with

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Strangeness in Quark Matter 2013
Birmingham, UK, July 23, 2013



Motivation

- ▶ confinement transition of $N_f = 2 + 1$ QCD at $\mu_B = 0$ is an **analytic crossover**
- ▶ pseudo-critical temperature:
 $T_C = (154 \pm 9) \text{ MeV}$ A. Bazavov et al., Phys. Rev. D 85 (2012) 054503
 $T_C = (147 \pm 5) - (155 \pm 6) \text{ MeV}$ S. Borsányi et al., JHEP 1009 (2010) 073
from a rapid change in different order parameters
- ▶ fluctuations of conserved charges (in heavy-ion collisions B , Q and S ; in QCD net u -, d - and s -quark numbers) are sensitive to the **microscopic structure** of the matter
Jeon and Koch, Phys. Rev. Lett. 85 (2000) 2076; Asakawa, Heinz and Müller, Phys. Rev. Lett. 85 (2000) 2072
- ▶ a rapid change in these observables provides a signal for a phase transition
- ▶ measurable experimentally and calculable (as susceptibilities) in lattice QCD:

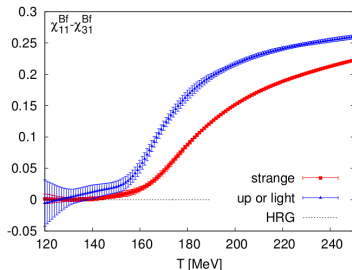
$$\chi_{lmn}^{uds} = \frac{\partial^{l+m+n}(\rho/T^4)}{\partial(\mu_u/T)^l \partial(\mu_d/T)^m \partial(\mu_s/T)^n}$$

Lattice QCD results

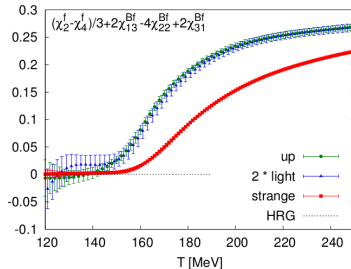
- ▶ continuum-extrapolated lattice QCD data of χ_2^u and χ_2^s at physical u - and s -quark masses show a clear separation in the behavior between up and strange quarks
 - interpreted as an indication for a **flavor hierarchy** in the crossover transition C. Ratti et al., Phys. Rev. D 85 (2012) 014004
- ▶ quark mass effect

Lattice QCD results

- ▶ model-dependent approach via comparison of Hadron Resonance Gas (HRG) model with IQCD data:
 - ▶ combinations of higher-order susceptibilities suggested which are zero in the hadronic phase and become non-zero with the onset of s-quark liberation (deconfinement) [A. Bazavov et al., arXiv:1304.7220 \[hep-lat\]](#)
→ see talk by [C. Schmidt](#) (Friday)
 - ▶ generalized to any flavor in order to study a possible flavor-specific behavior [R. Bellwied et al., arXiv:1305.6297 \[hep-lat\]](#)



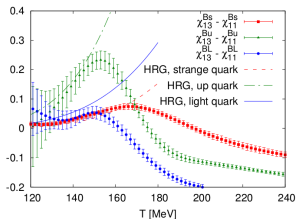
from [R. Bellwied et al., arXiv:1305.6297 \[hep-lat\]](#)



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Lattice QCD results

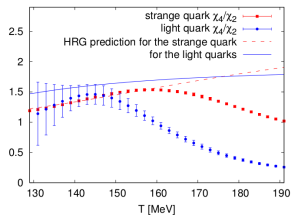
- ▶ a different susceptibility combination: in hadronic phase **sensitive** to baryons containing **more than one** quark of flavor f



from R. Bellwied et al., arXiv:1305.6297 [hep-lat]

- shows a pronounced separation of flavors

- ▶ investigate fluctuations of net light-quark number and net strange-quark number χ_4^f / χ_2^f (π do **not** carry net light-quark number)

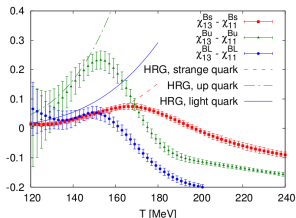


from R. Bellwied et al., arXiv:1305.6297 [hep-lat]

- flavor-dependence of the **liberation temperature** (T at which HRG model starts to deviate from IQCD)
- flat curves

Lattice QCD results

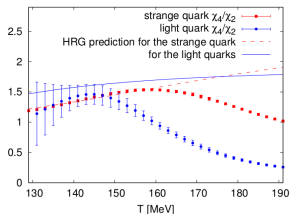
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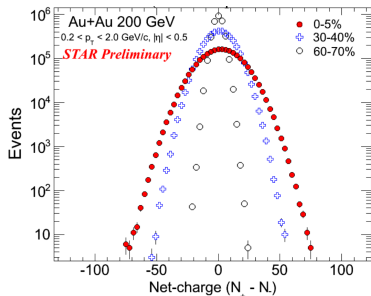


from R. Bellwied et al., arXiv:1305.6297 [hep-lat]

Idea: fingerprint of a **flavor hierarchy** measurable in **higher-order moments** of particle-identified multiplicity distributions?

Statistical moments of multiplicity distributions

- ▶ measurement of fluctuations in a conserved charge X



from D. McDonald, talk at QM2012

(observable X : net electric charge)

statistical moments:

- ▶ mean $\langle X \rangle$
- ▶ deviation $\langle \delta X \rangle = \langle X - \langle X \rangle \rangle$
- ▶ variance (width) $\sigma_X^2 = \langle (\delta X)^2 \rangle$
- ▶ skewness (\sim asymmetry)
 $S_X = \langle (\delta X)^3 \rangle / \sigma_X^3$
- ▶ kurtosis (\sim center peakedness)
 $\kappa_X = \langle (\delta X)^4 \rangle / \sigma_X^4 - 3$
- ▶ ...

Relation to ratios of susceptibilities

- ▶ ratios of susceptibilities of a conserved charge can be directly related to the statistical moments: e.g. net electric charge

$$\kappa_Q \sigma_Q^2 = \frac{\chi_4^Q(T, \mu_B)}{\chi_2^Q(T, \mu_B)} = \frac{\chi_4^Q(T)}{\chi_2^Q(T)} + \mathcal{O}(\mu_B^2)$$

- ▶ provide a model-independent measure of freeze-out conditions from lattice QCD [F. Karsch, Central Eur. J. Phys. 10 \(2012\) 1234](#); [A. Bazavov et al., Phys. Rev. Lett. 109 \(2012\) 192302](#); [S. Borsanyi et al., arXiv:1305.5161\[hep-lat\]](#)
- ▶ advantage of susceptibility ratios: volume-dependence cancels out

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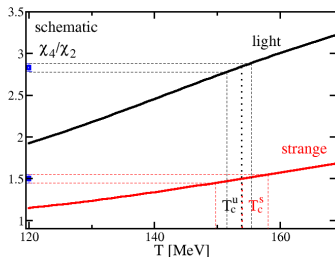
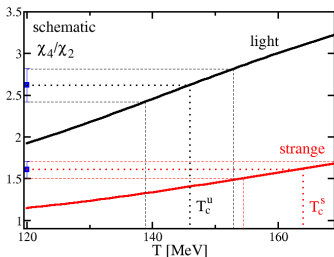
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Goal: define a measurement of flavor-specific fluctuation observables being related to ratios of quark number susceptibilities

⇒ ongoing project

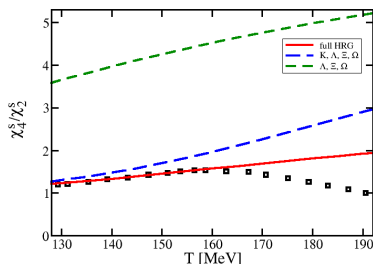
Defining a suitable measurement

- ▶ ALICE has measurements of $\pi, \rho, K, \Lambda, \Xi, \Omega$
- ▶ higher-order moment analysis of particle-identified multiplicity distributions
- ▶ have to be sensitive to the flavor-composition of the individual hadrons (\rightarrow optimal measurement: ρ vs. Ω but flat χ_4^f/χ_2^f)
- ▶ task: find **optimal final state combinations** that allow a discrimination of light from strange quarks by providing steep χ_4^f/χ_2^f -curves



Defining a suitable measurement

- ▶ strange-quark number fluctuations:



IQCD data from R. Bellwied et al., arXiv:1305.6297 [hep-lat]

- optimal final state subset: Λ^0 , Ξ^- and Ω^- plus their antiparticles
- ▶ light-quark number fluctuations: consider as subset K^+ and p plus their antiparticles (π do not contribute to the net light-quark number)

How to relate measurement with HRG model?

- ▶ non-trivial issue M. Kitazawa and M. Asakawa, Phys. Rev. C 86 (2012) 024904; A. Bzdak and V. Koch, Phys. Rev. C 86 (2012) 044904 ...

- ▶ detector acceptance:

for identified particles express HRG model momentum-integrals in terms of transverse momentum p_T and rapidity $y \rightarrow$

$$E_i = \sqrt{p_T^2 + m_i^2} \cosh y ; d^3p = p_T \sqrt{p_T^2 + m_i^2} \cosh y dp_T dy d\phi$$

- ▶ influence of strong resonance decays: H. Bebie et al., Nucl. Phys. B 378 (1992) 95
 - ▶ assumption: ground state excitations inherit the fluctuations of the decaying resonances
 - ▶ effective number of ground state excitation i

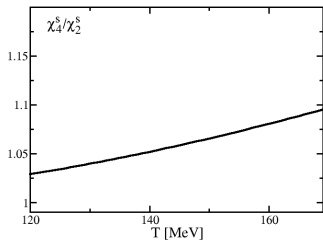
$$\bar{N}_i(T, \mu_i) = N_i(T, \mu_i) + \sum_r d_{r \rightarrow i} N_r(T, \mu_r)$$

is the sum of the actual number of i plus resonance decay contributions with $d_{r \rightarrow i}$ the average number of i produced from r (modulo efficiency corrections due to acceptance cuts)

- ▶ feed-down correction for weak decay contributions (experiment)

Example: $K^+ - K^-$ measurement

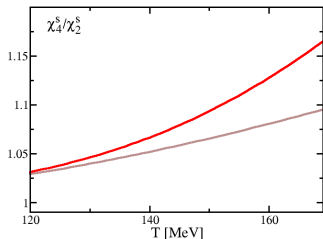
- ▶ net-Kaon multiplicity distribution measures net-strangeness distribution in the (K^+, K^-) – subsystem
- ▶ $\kappa\sigma^2(N_{K^+} - N_{K^-}) = \chi_4^S/\chi_2^S$



- ▶ HRG model result

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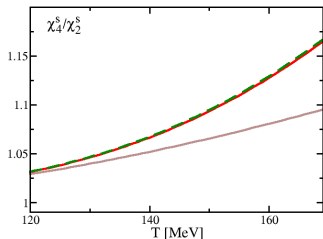
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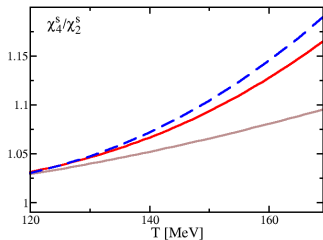
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- ▶ HRG model result
- ▶ influence of resonance decays is **sizeable**
- ▶ exhibits negligible **chemical potential dependence** for small μ_X ($\mu_B = 20$ MeV, $\mu_S = 4$ MeV)

Example: $K^+ - K^-$ measurement

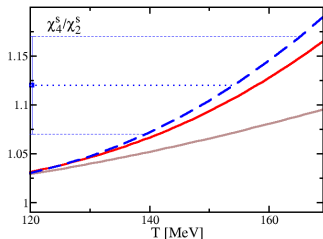
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(GeV/c) ≤ 2.0 , $|y| \leq 0.5$

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data from D. McDonald (for STAR), arXiv:1210.7023 [nucl-ex]

$\kappa\sigma^2$ of net-Kaons, 0 - 5% centrality, Au+Au at $\sqrt{s} = 200$ GeV

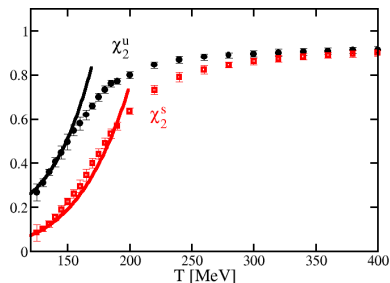
- ▶ HRG model result
- ▶ influence of resonance decays is **sizeable**
- ▶ **acceptance cuts**: $0.2 \leq p_T$ (GeV/c) ≤ 2.0 , $|y| \leq 0.5$
- ▶ fluctuations in net-strangeness fixed at $T_{f.o.} \simeq 153$ MeV

Conclusions

- ▶ continuum-extrapolated lattice QCD results for suitably chosen combinations of susceptibilities of conserved charges show a clear separation in the behavior of different quark flavors in the crossover region
- ▶ might be an indication for a flavor hierarchy
- ▶ idea: look for evidences of a flavor hierarchy in higher moments of particle-identified multiplicity distributions
- ▶ proposed a possible experimental measurement and discussed how to deduce from it information about details in the transition region (in a model-dependent way)
 - ▶ highlighted importance of resonance decays and detector acceptance cuts for (K^+ , K^-) subsystem

Backup-Slides

First indications for a flavor-separation

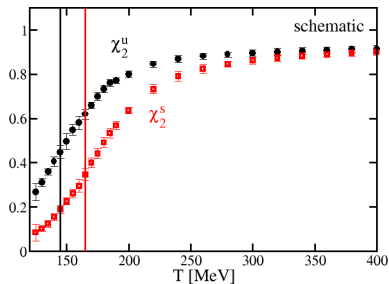


data taken from [S. Borsányi et al., JHEP 1201 \(2012\) 138](#)

diagonal quark number
susceptibilities for up and strange
quark flavors:

- ▶ fairly well described by a HRG model for lower T

First indications for a flavor-separation



data taken from [S. Borsányi et al., JHEP 1201 \(2012\) 138](#)

- ▶ quantitatively similar observation from the combination of (B, Q, S) -susceptibilities from [A. Bazavov et al., Phys. Rev. D 86 \(2012\)](#)

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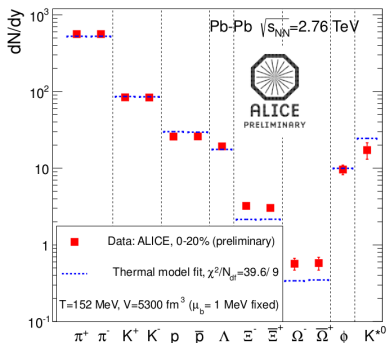
diagonal quark number susceptibilities for up and strange quark flavors:

- ▶ clear difference between light (up) and strange quarks: rapid change happens for strange quarks at a larger T than for light quarks (about $(15 - 20)$ MeV difference), i.e. fluctuations in strange quark number density cease at a larger T
- ▶ indication for a **flavor hierarchy in the QCD crossover transition**

Experimental indications: Charged hadron production

- ▶ **integrated yields** provide higher **flavor-sensitivity** than e.g. hadron/pion ratios

feed-down corrected dN/dy at midrapidity in central (0-20%) Pb-Pb



ALI-PREL-32248

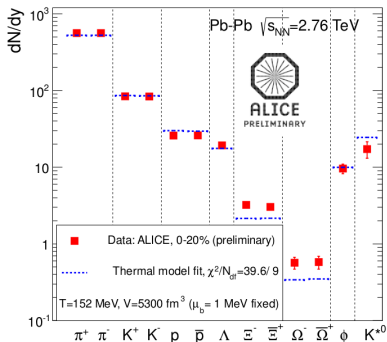
L. Milano (for ALICE), arXiv:1302.6624 [hep-ex] and QM2012

- ▶ standard Statistical Hadronization Model (SHM) fit with $T_{ch} = 164$ MeV gives poor overall description
- ▶ global fit: $T_{ch} = (152 \pm 3)$ MeV but yields of **(multi)strange baryons** underestimated
- ▶ fit to individual yields would be better if T_{ch} for strange hadrons was **higher** than for non-strange hadrons (**sequential progression**)

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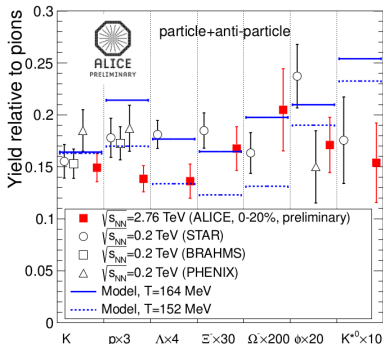
ALI-PREL-32248

- ▶ possible explanation: **flavor hierarchy** in the chemical freeze-out
- ▶ **caveat**: for SHM-fits of yields knowledge of a (T -dependent) **volume V** is needed

Experimental indications: Charged hadron production

▶ particle-yield ratios

yields relative to pions



ALI-PREL-32253

- ▶ similar observations can be made in particle/pion ratios
- ▶ **caveat:** (multi)strange baryon/pion ratios mix quark-flavor sectors (less flavor-specific)

L. Milano (for ALICE), arXiv:1302.6624 [hep-ex] and QM2012

R. Preghenella (for ALICE), Acta Phys. Polon. B43 (2012) 555

Possible explanations for yield measurements

- ▶ anti-baryon–baryon annihilation in the hadronic phase:

- ▶ non-equilibrium, final state effect as consequence of in-medium enhanced annihilation cross section

F. Becattini et al., Phys. Rev. C 85 (2012) 044921; arXiv:1212.2431 [nucl-th];

J. Steinheimer et al., Phys. Rev. Lett. 110 (2013) 042501; Y. Karpenko et al., Phys.

Rev. C 87 (2013) 024914

- ▶ regeneration processes important

Y. Pan and S. Pratt, arXiv:1210.1577 [nucl-th]

- ▶ effect more pronounced in central than in peripheral collisions

- ▶ viscous-hydro approach with species-dependent (dynamically generated) T_{ch}

P. Bozek and I. Wyskiel-Piekarska, Phys. Rev. C 85 (2012) 064915

- ▶ chemical non-equilibrium SHM

M. Petrán et al., arXiv:1303.2098 [hep-ph]

- ▶ **flavor hierarchy**