

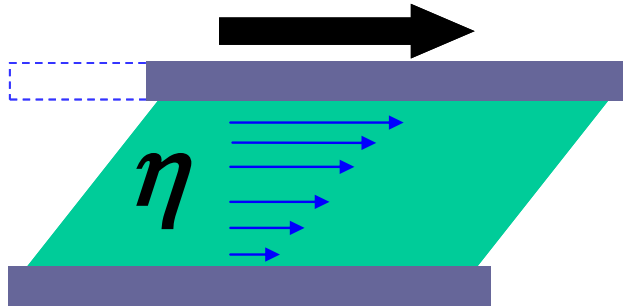
QGP Viscosity & Elliptic Flow for Multi-strange Hadrons

**Huichao Song
Peking University**

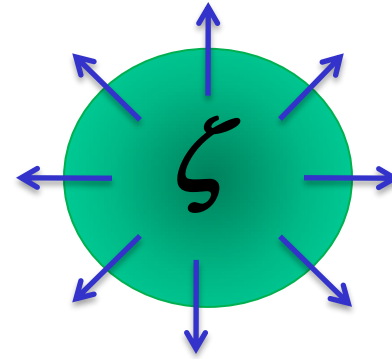
SQM 2013

Birmingham, UK, July 22- 27, 2013

Shear viscosity:



Bulk viscosity:



viscous hydrodynamics

$$\partial_{\mu} T^{\mu\nu}(x) = 0$$

$$T^{\mu\nu} = (e + p + \Pi)u^{\mu}u^{\nu} - (p + \Pi)g^{\mu\nu} + \pi^{\mu\nu}$$

$$\tau_{\pi} \Delta^{\alpha\mu} \Delta^{\beta\nu} \dot{\pi}_{\alpha\beta} + \pi^{\mu\nu} = 2\eta\sigma^{\mu\nu} - \frac{1}{2} \pi^{\mu\nu} \frac{\eta T}{\tau_{\pi}} \partial_{\lambda} \left(\frac{\tau_{\pi}}{\eta T} u^{\lambda} \right)$$

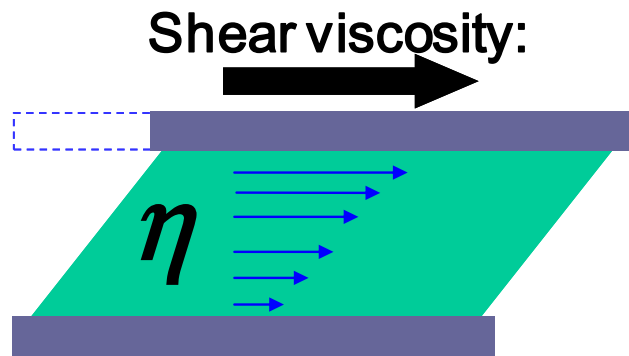
$$\tau_{\Pi} \dot{\Pi} + \Pi = -\zeta(\partial \cdot u) - \frac{1}{2} \Pi \frac{\zeta T}{\tau_{\Pi}} \partial_{\lambda} \left(\frac{\tau_{\Pi}}{\zeta T} u^{\lambda} \right)$$

Input: “EOS”

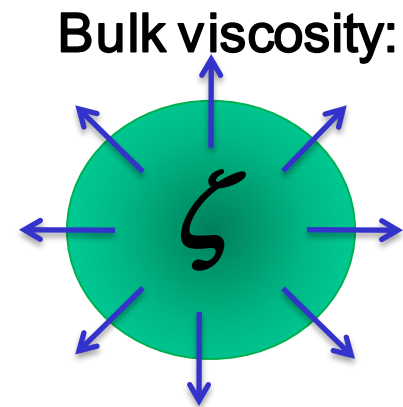
$$\varepsilon = \varepsilon(p)$$

Assume **zero net baryon density & heat conductivity** at RHIC and LHC

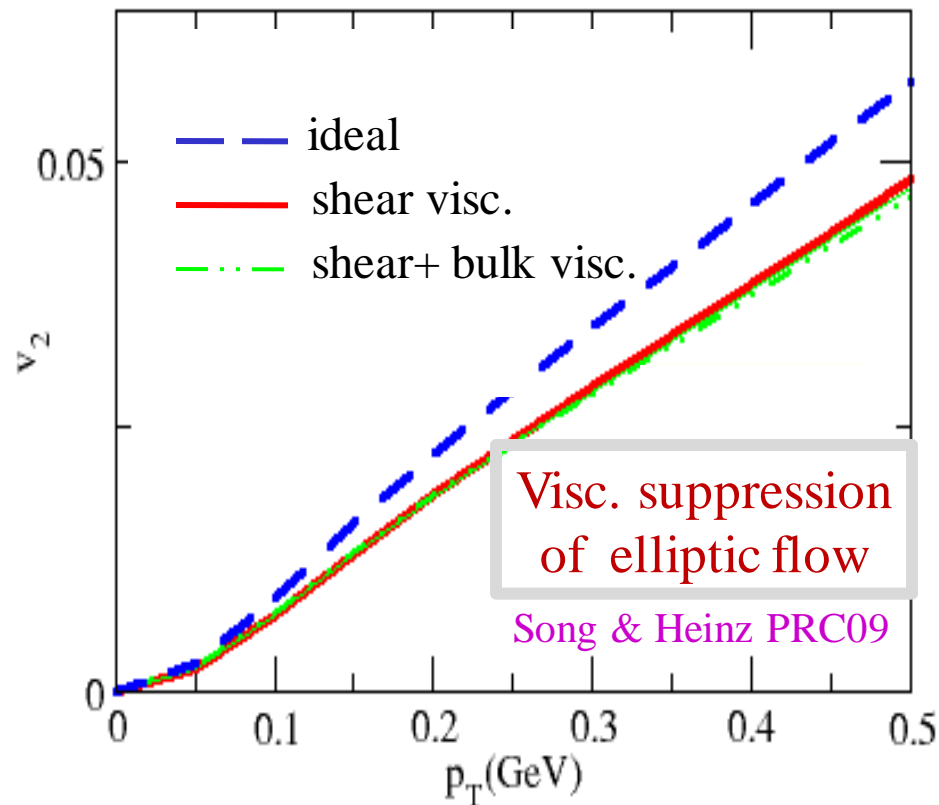
Generic features of shear & bulk viscosities



acts against the buildup
of flow anisotropy



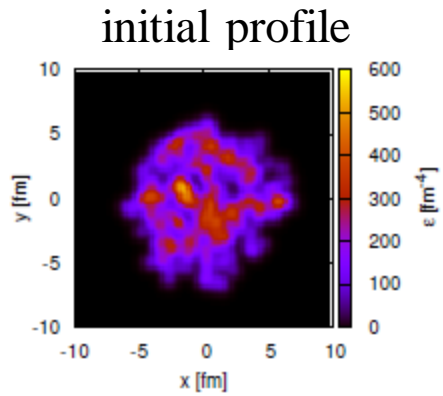
acts against the buildup
of radial flow



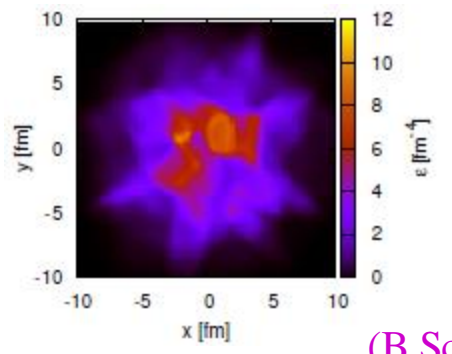
The shear viscosity leads to a significant suppression of v_2 (Romatsche & Romatsche PRL07; song & Heinz PLB08, PRC08; Dusling & Teaney PRC 08; Molnar & Huovinen JPG 08)

Bulk viscous effects are much smaller than shear ones due to the critical slowing down near phase transition (Song & Heinz PRC09)

One can extract the QGP shear viscosity from exp data **without large contaminations from bulk viscosity**

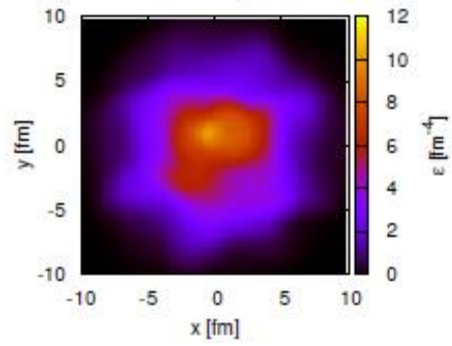


ideal hydro evolution

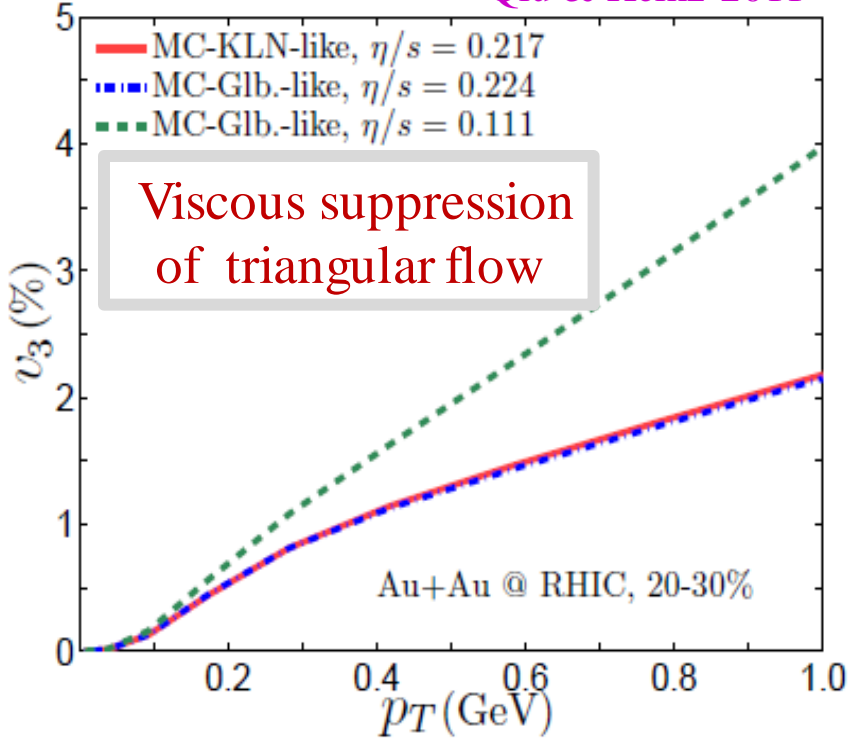


(B.Schenke)

viscous hydro evolution



Qiu & Heinz 2011



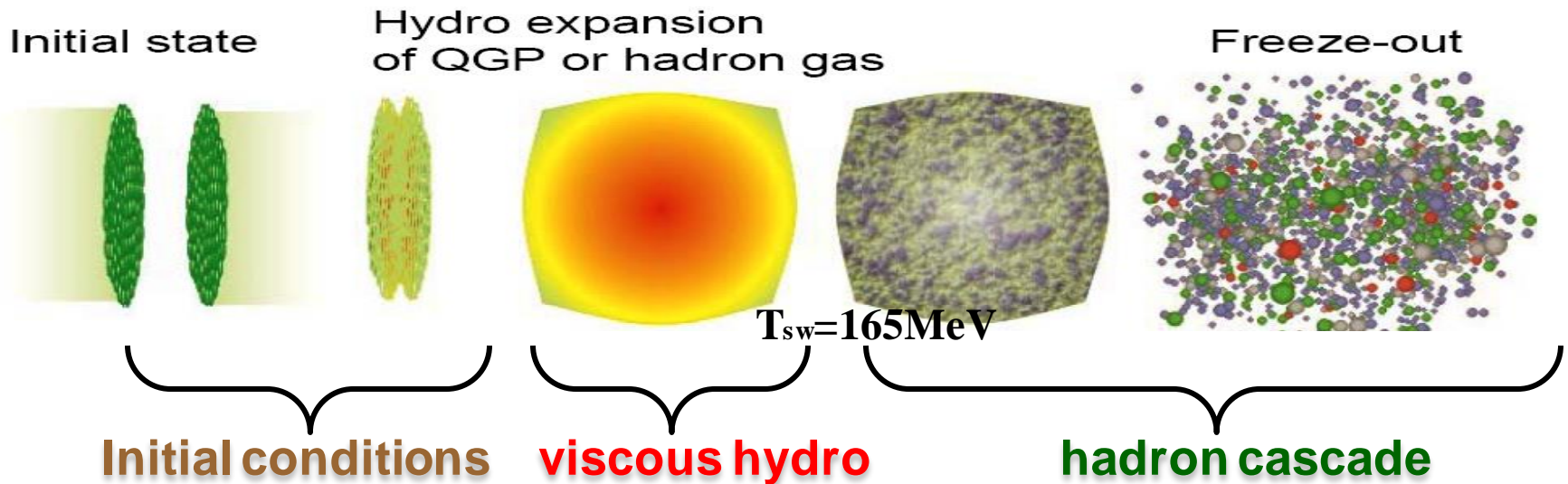
The shear viscosity tends to smear out the inhomogeneous structures, leading to a suppression of v_3 (Schenke, Jeon & Gale PRL2011, PRC2012; Qiu & Heinz PRC2011 ...)

QGP viscosity at RHIC and the LHC

-results from the VISHNU hybrid model

VISHNU hybrid approach

H. Song, S. Bass, U. Heinz, PRC2011



VISHNU:

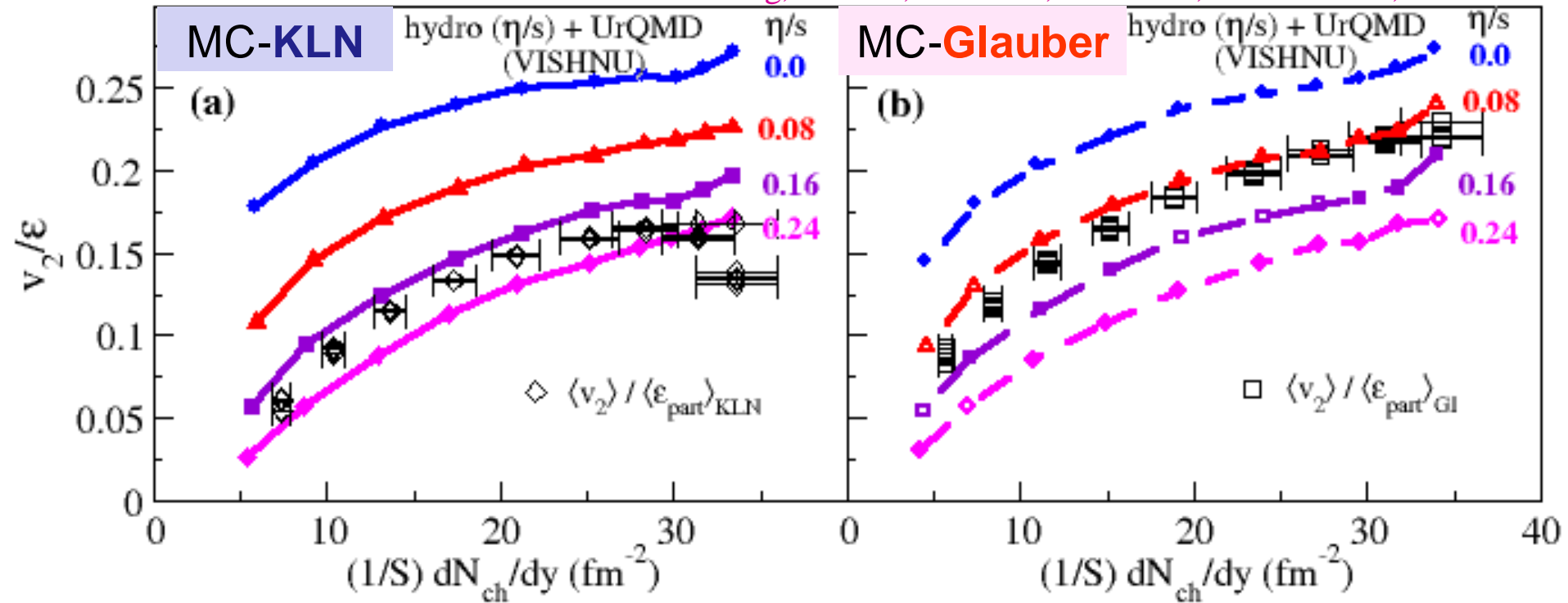
- chemical composition of HRG
 - transport properties of HRG
- } Hadron Cascade
- EoS: (s95p-PCE) (Huovinen & Petreczky10)
 - switching temperature: $T_{sw}=165\text{MeV}$
 - initial conditions

Other related developments

- 3+1 d viscous hydro+ hadron cascade: Ryu et al., arXiv1210.4588 .
- 2+1 d vs 3+1 viscous hydro: Shen, Schenke & Heinz on going work;
- Vredevoogd & Pratt, PRC85,044908(2012)

V_2 and QGP viscosity at RHIC

H. Song, S. Bass, U. Heinz, T. Hirano, and C. Shen, PRL2011



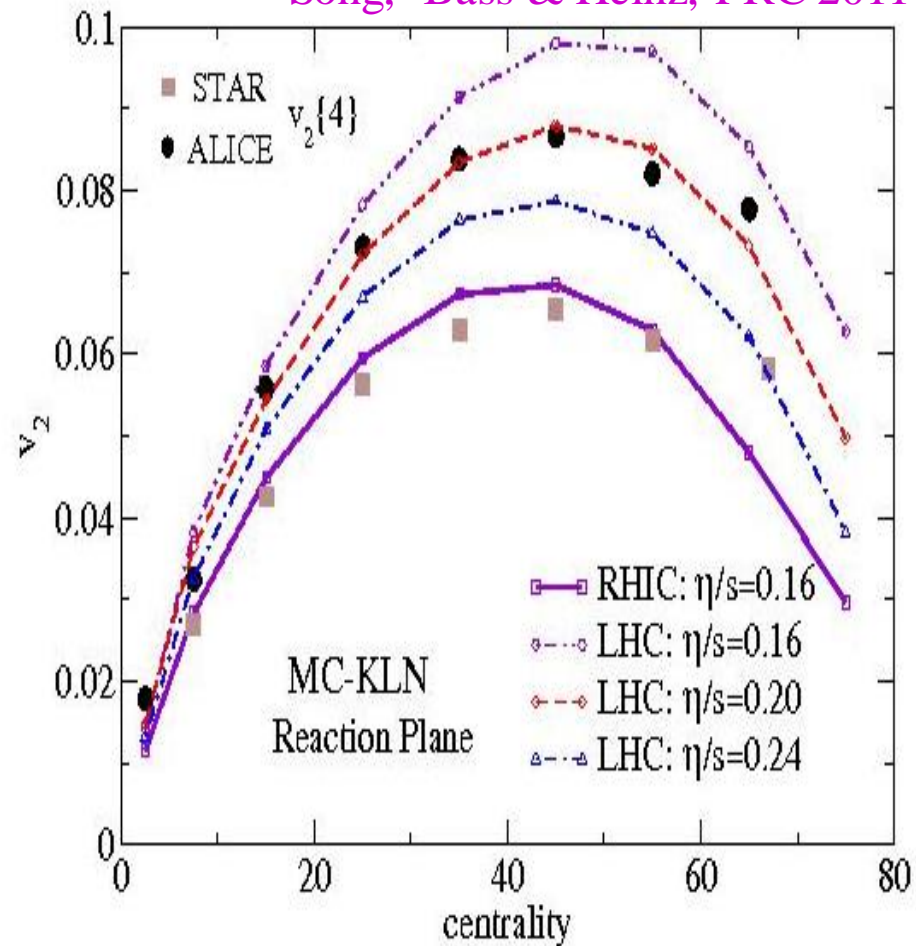
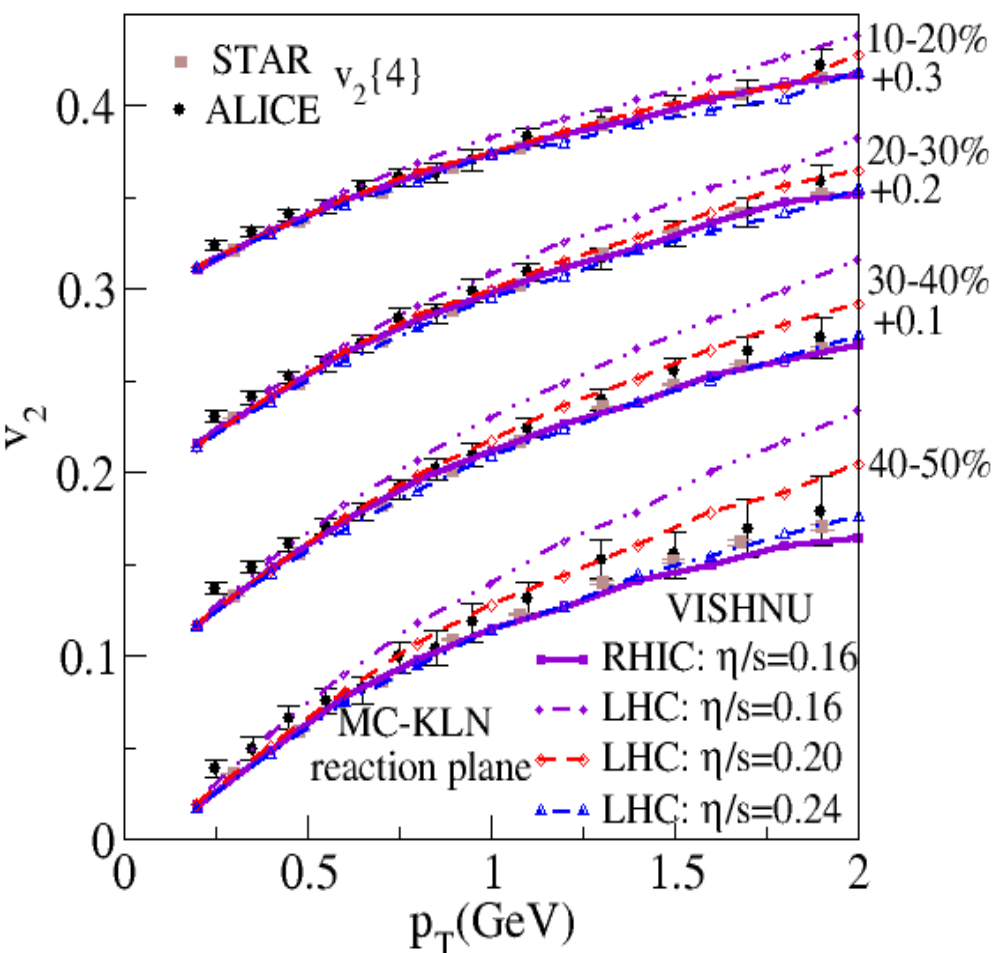
$$1 \times (1/4 \pi) \leq (\eta/s)_{QGP} \leq 2.5 \times (1/4 \pi)$$

The analysis uses:

- integrated V_2 for all charged hadrons: In contrast to $V_2(P_T)$, it is less sensitive to bulk viscosity, δf corrections, radial flow & chemical composition of HRG
- corrected exp. V_2 data that remove non-flow & fluc. effects

V_2 and QGP viscosity at the LHC

Song, Bass & Heinz, PRC 2011



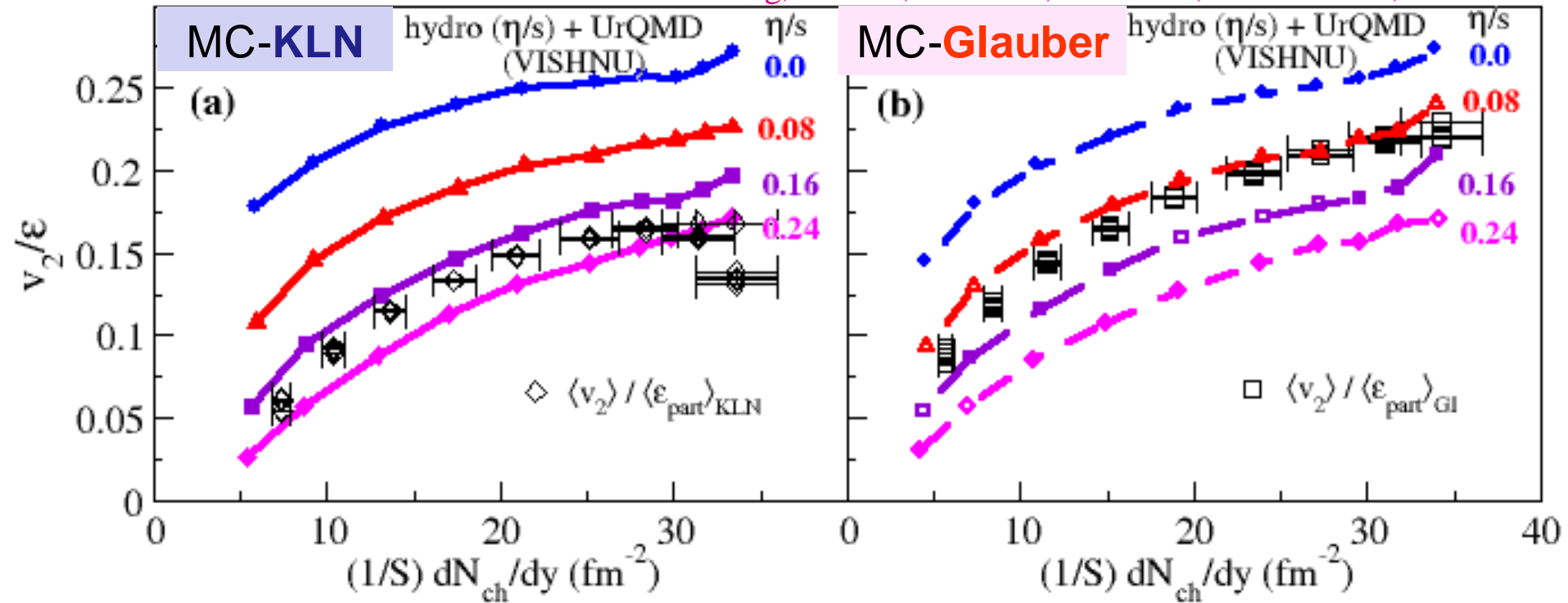
The average QGP viscosity is roughly the same at RHIC and LHC

Please also refer to C. Gale, et al., [ArXiv: 1209.5330 \[nucl-th\]](https://arxiv.org/abs/1209.5330)

Initial state fluctuations, final state correlations & the QGP viscosity

Uncertainties from Initial Conditions

H. Song, S. Bass, U. Heinz, T. Hirano, and C. Shen, PRL2011



$$1 \times (1/4\pi) \leq (\eta/s)_{QGP} \leq 2.5 \times (1/4\pi)$$

Main uncertainties come from initial conditions

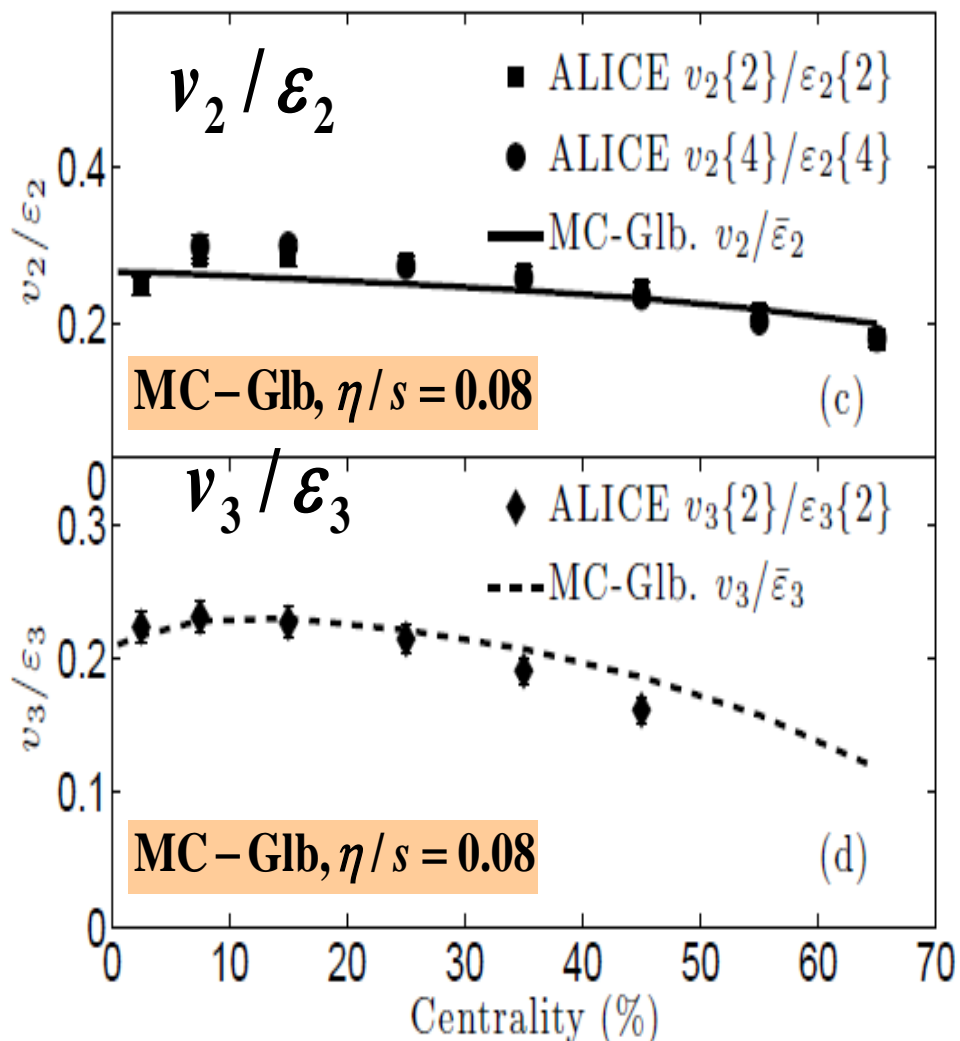
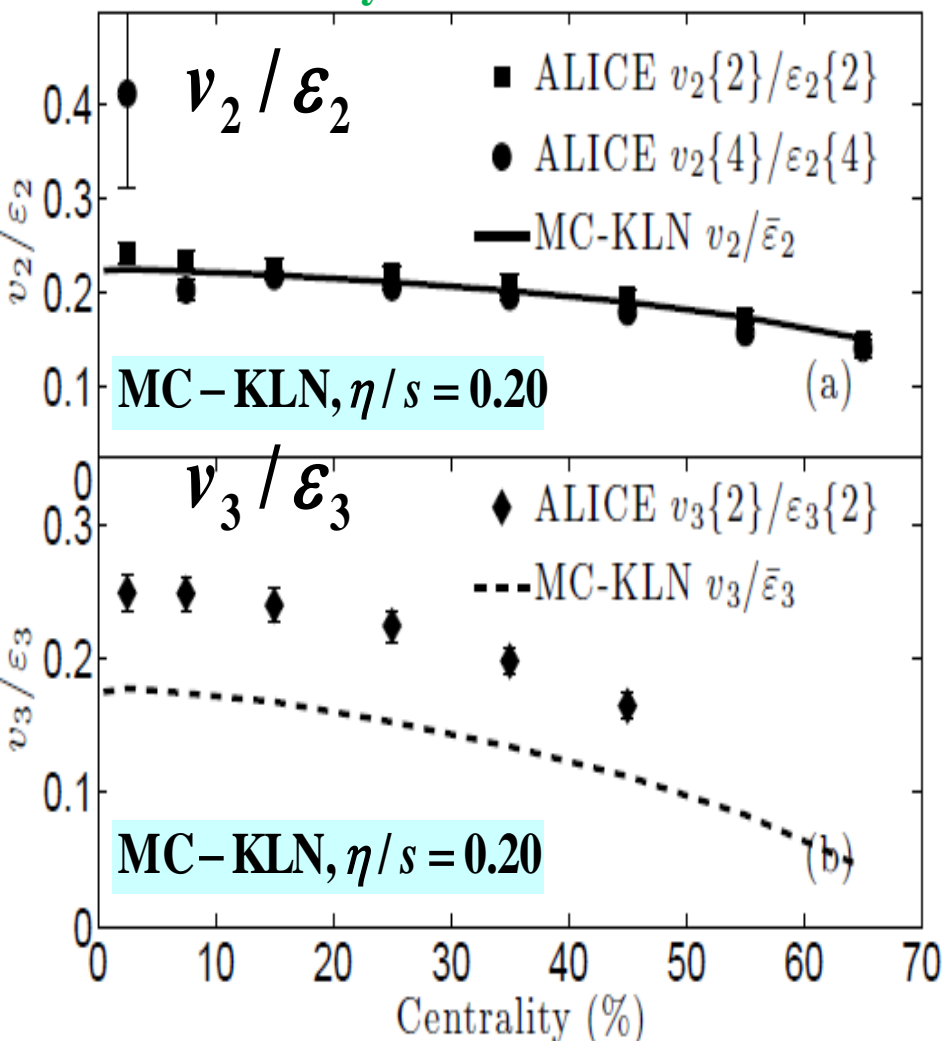
MC-KLN, larger ϵ_2 \longrightarrow HIGHER value of QGP viscosity

MC-Glauber, smaller ϵ_2 \longrightarrow LOWER value of QGP viscosity

MC-KLN & MC-Glauber initializations & V_3

Pure viscous hydro simulations :

Qiu, Shen & Heinz 2011



V_3 prefer lower value of QGP viscosity

MC-Glauber & MC-KLN initializations are based on **fluctuation of nucleon positions**

Theoretical Development on Initialization Models:

- color charge fluctuations** (IP-Glasma, correlated fluctuations)
- multiplicity fluctuations** for local gluon numbers
- transverse/longitudinal flow fluctuations**
- **UrQMD, AMPT, EPOS/NUSES**
-

Related flow Data:

- elliptic flow**
- triangular flow & higher order flow harmonics**
- higher-order event plane correlations**
- Event by event v_n distributions**
- **v_n in ultra-central collisions**
-

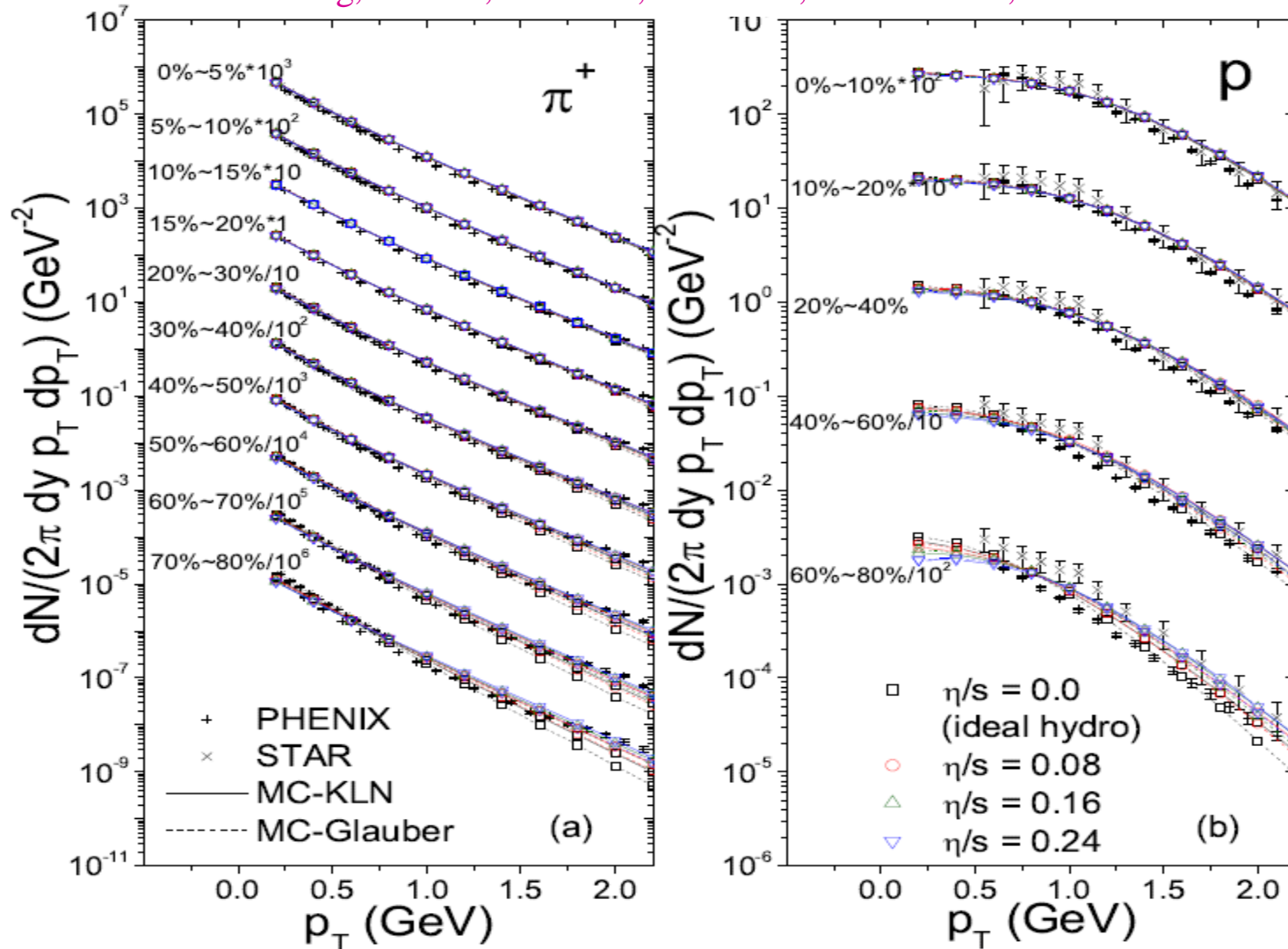
A further study of flow data in different aspects, using e-b-e VISHNU will constrain initialization models, tightening the limit on $(\eta/s)_{QGP}$

--Please also refer the work from B. Schenke and OSU group for recent developments

Multiplicity, Spectra and elliptic flow for identified hadrons

RHIC: spectra for identified hadrons

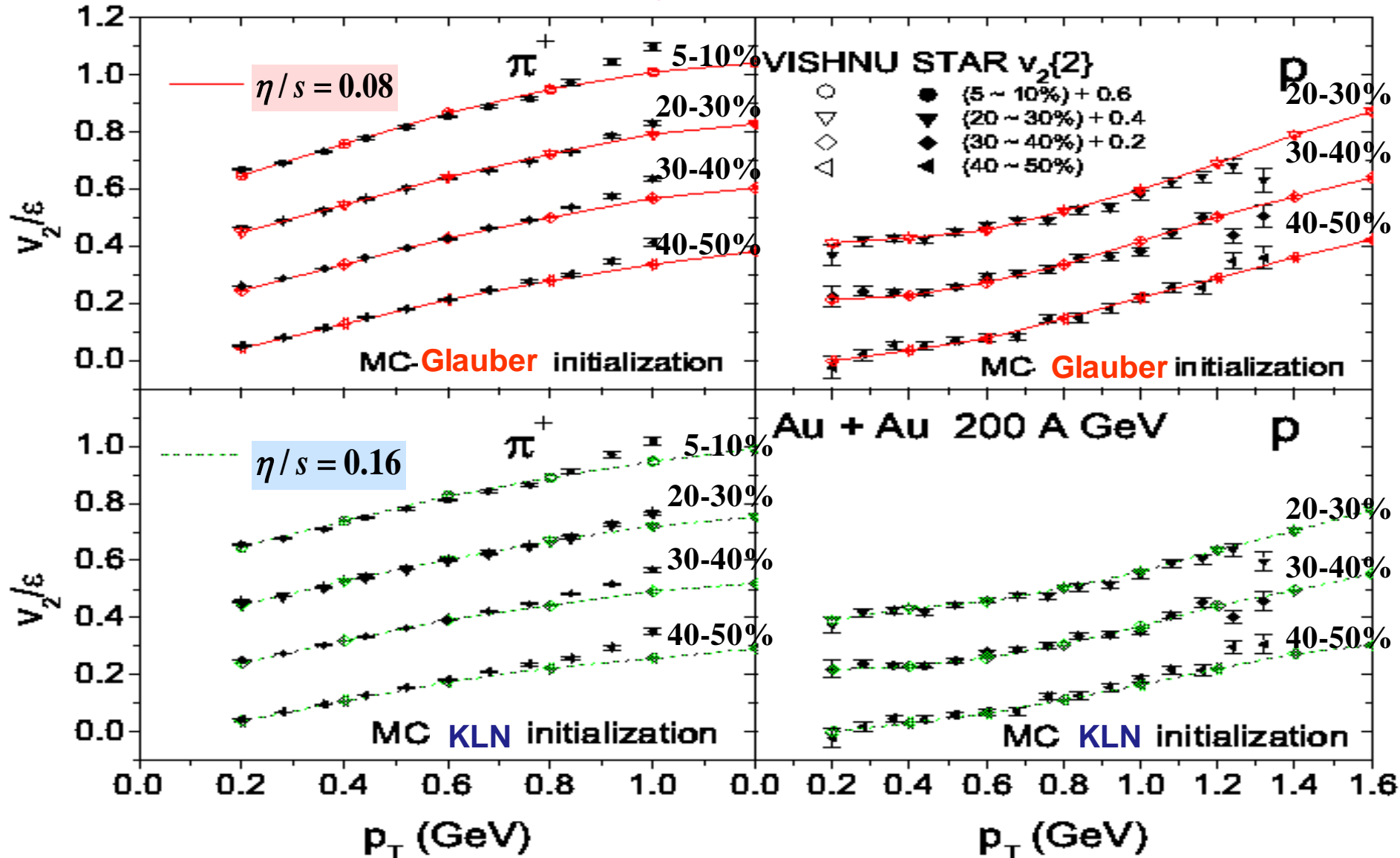
H. Song, S. Bass, U. Heinz, T. Hirano, and C. Shen, PRC2011



-a nice fit for both pion and proton spectra, insensitive to QGP viscosity

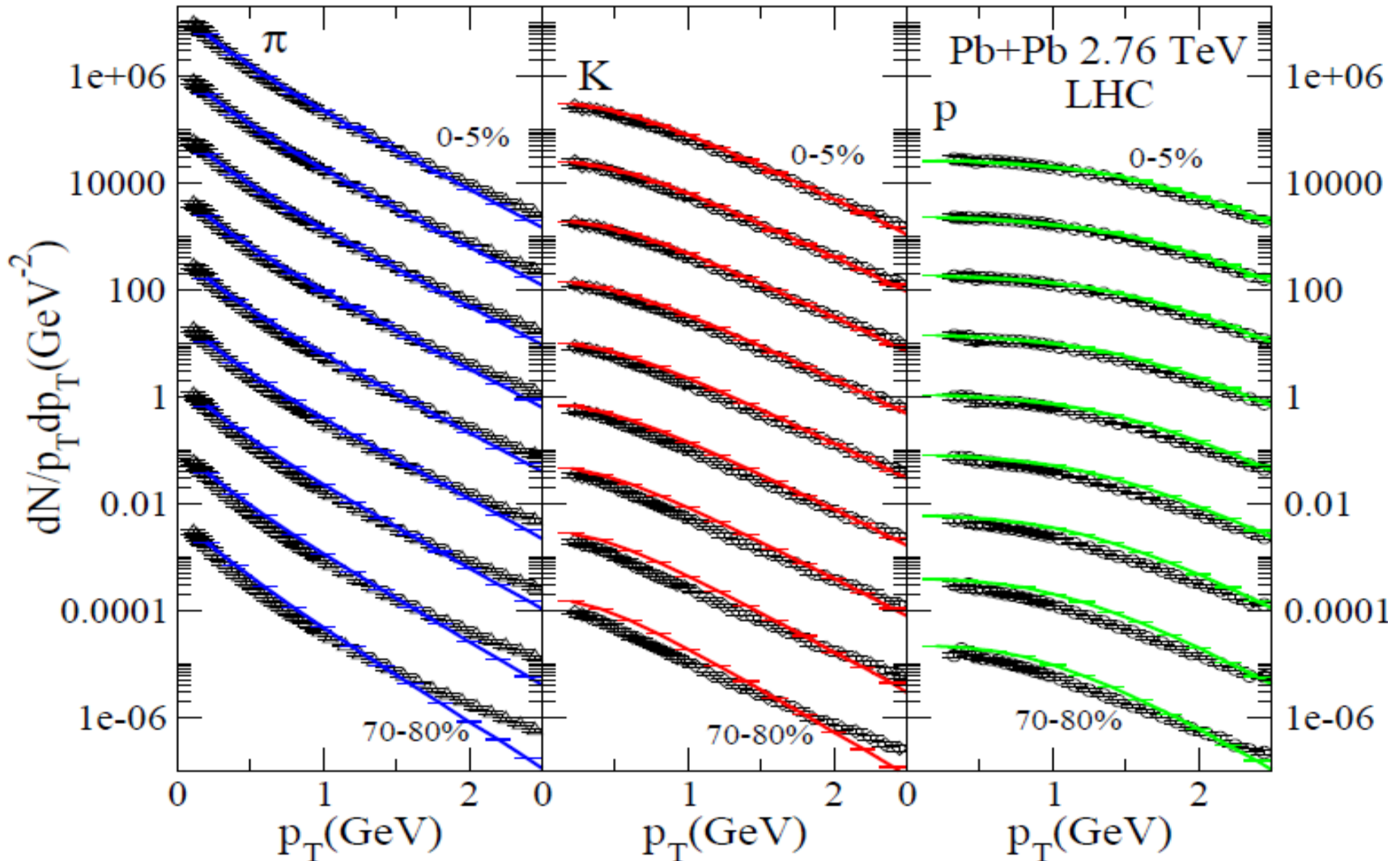
RHIC: $V_2(p_T)$ for identified hadrons

H.Song, S. Bass, U. Heinz, T. Hirano, and C. Shen, PRC2011



LHC: spectra for identified hadrons

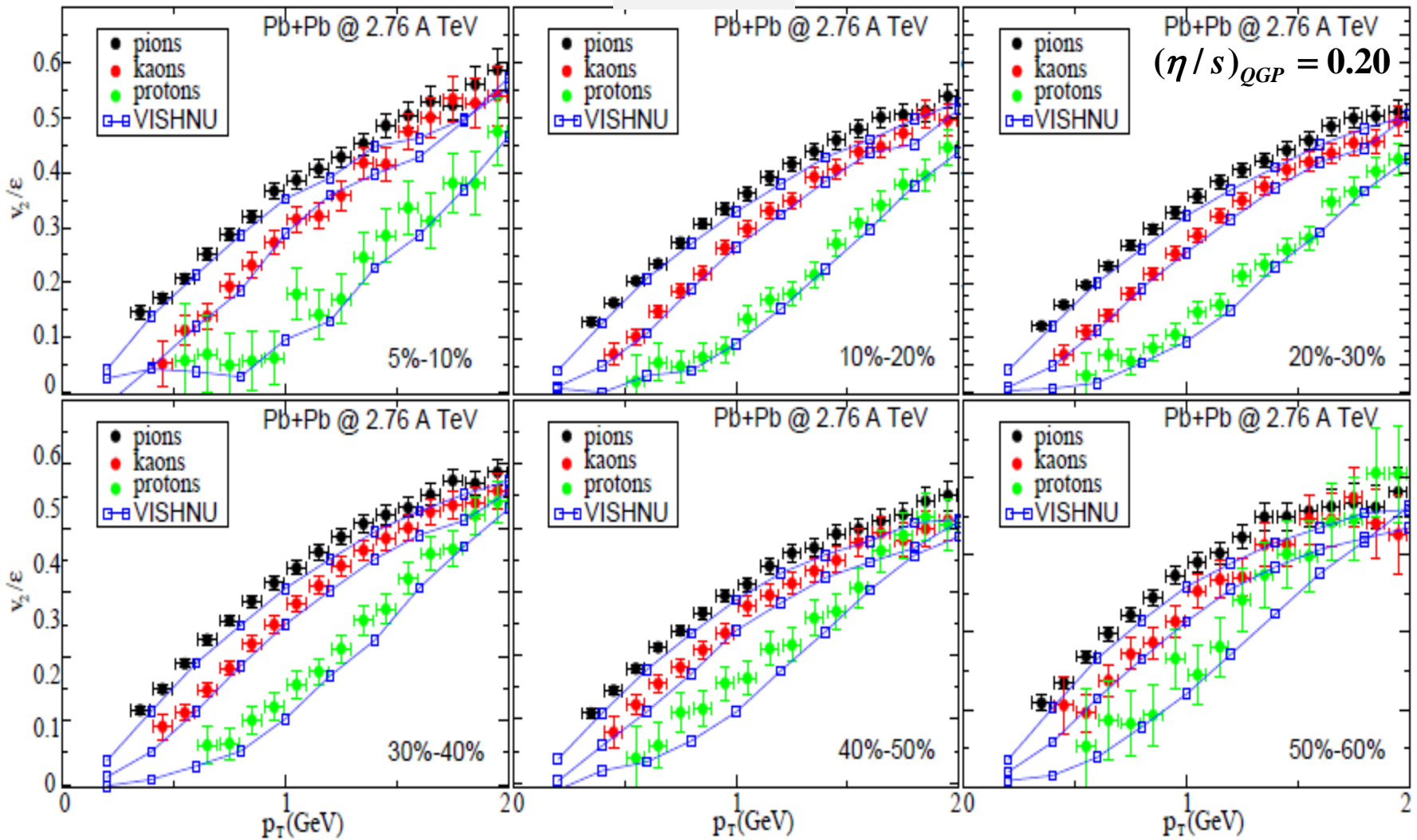
H. Song, S. Bass, U. Heinz, in preparations



-a nice fit for pions, kaons and proton spectra

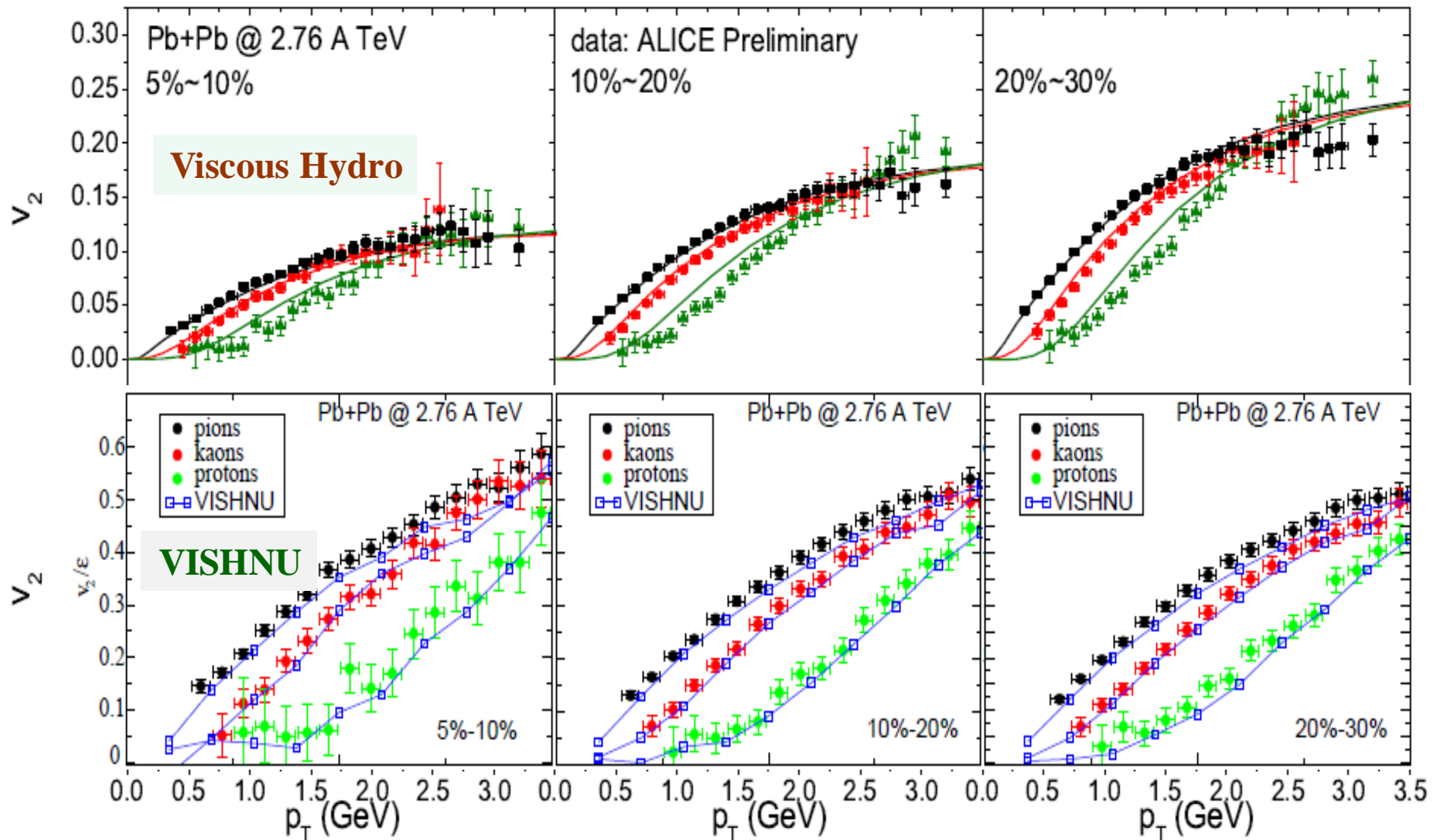
LHC: $v_2(p_T)$ for identified hadrons

VISHNU



A very nice fit of $V_2(P_T)$ for all centrality bins at LHC from VISHNU hybrid model

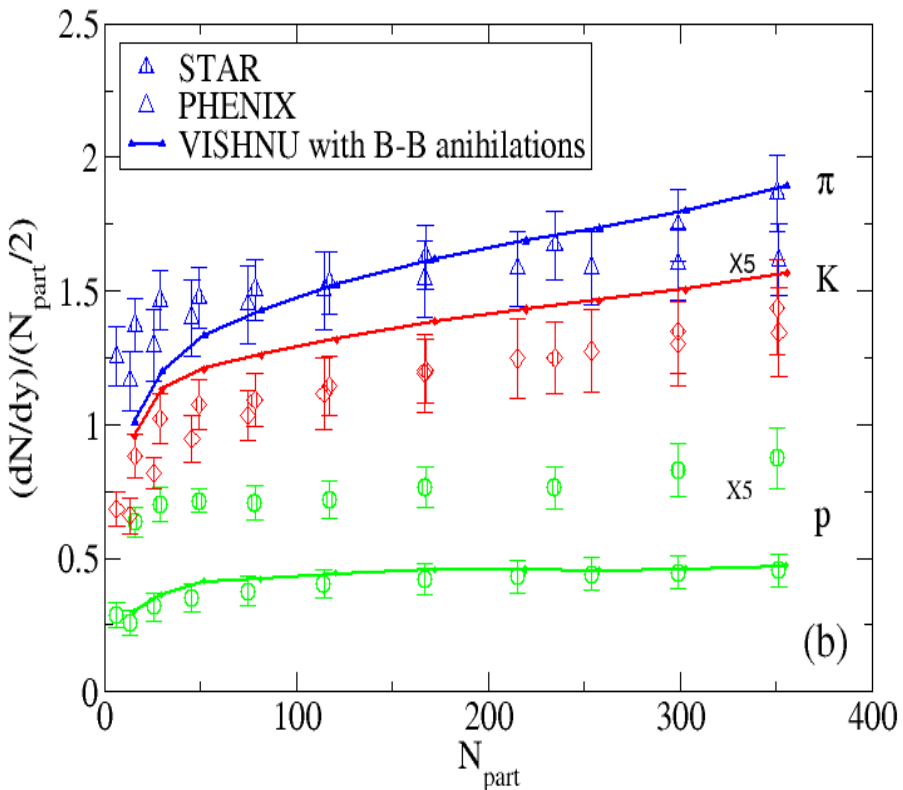
LHC: $V_2(p_T)$ for identified hadrons



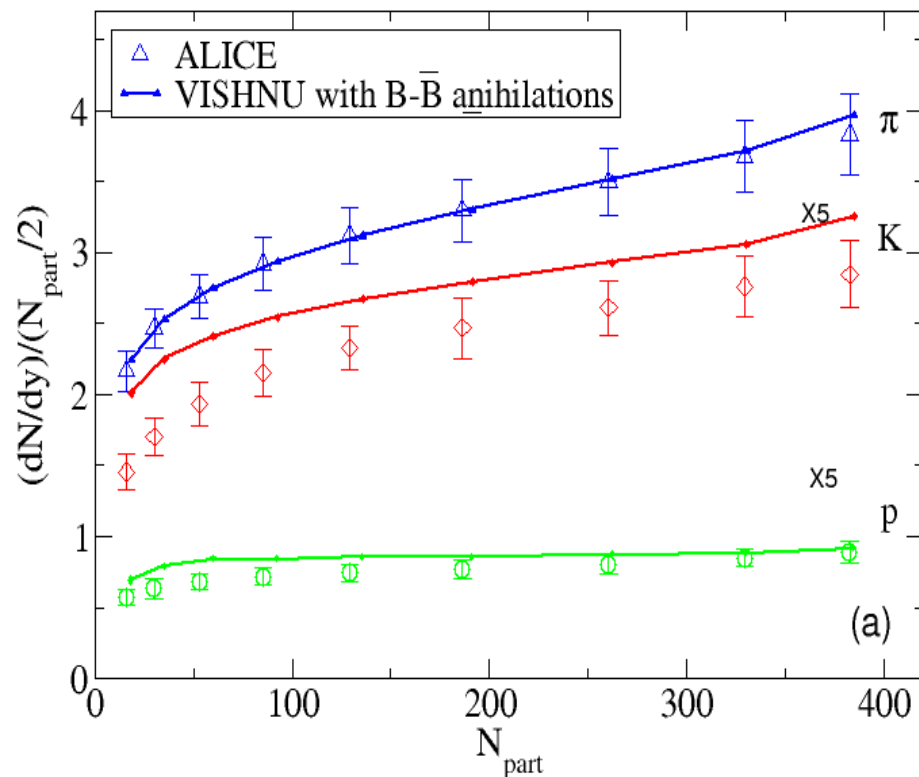
A comparison between viscous hydrodynamics and VISHNU

dN/dy for identified hadrons (RHIC & LHC)

RHIC : 200 A GeV Au+Au



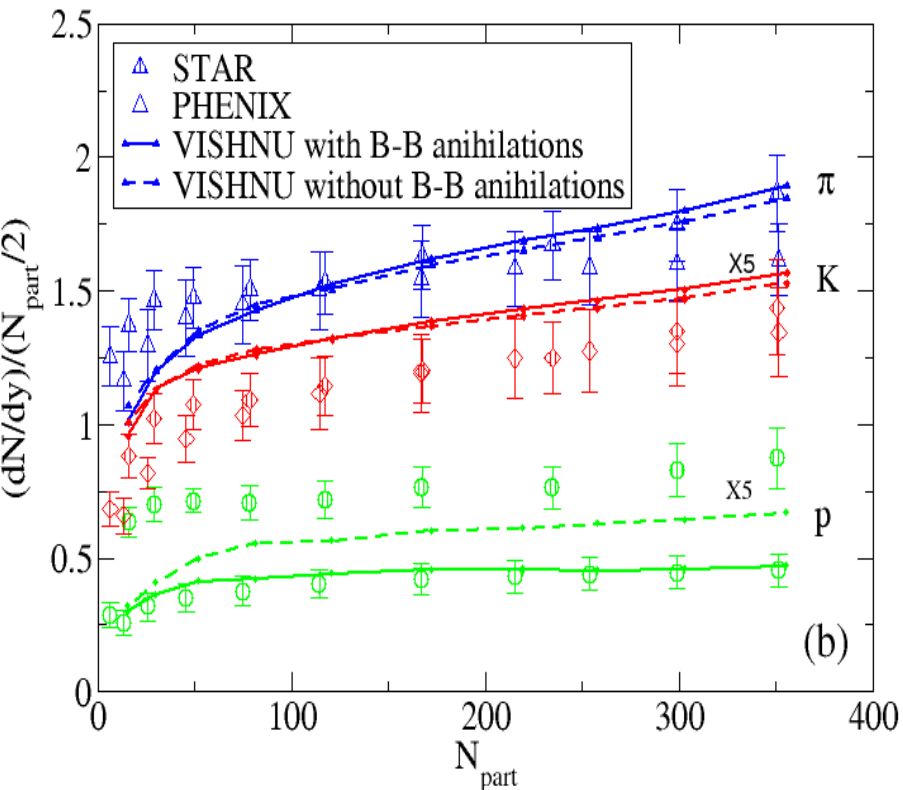
LHC : 2.76 A TeV Pb+Pb



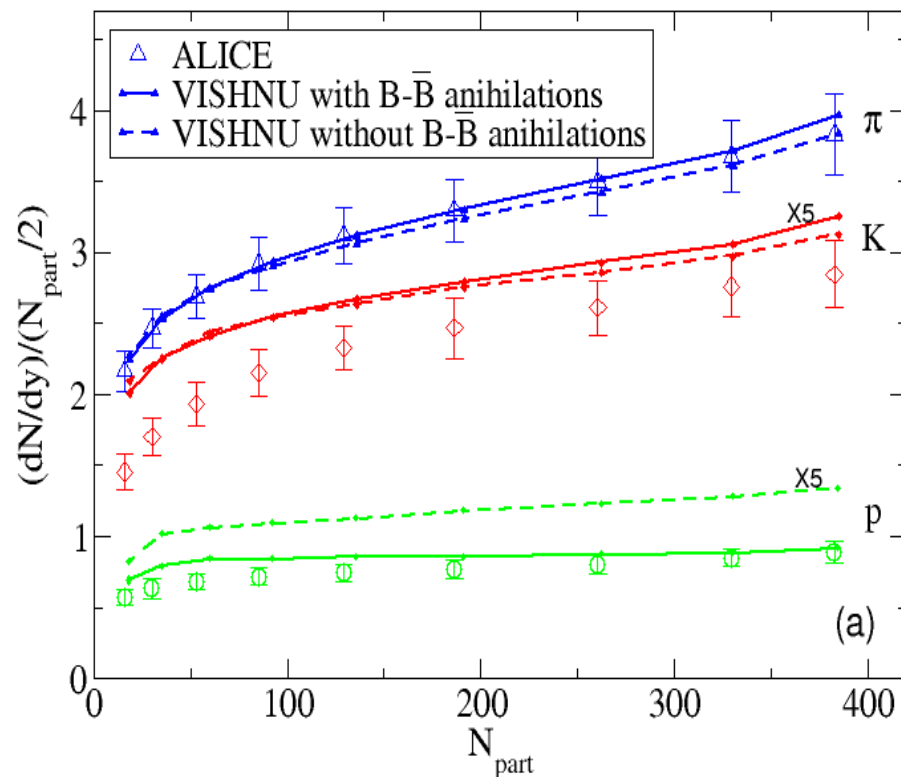
-VISHNU nicely describes the multiplicity for pions, kaons & protons

dN/dy for identified hadrons (RHIC & LHC)

RHIC : 200 A GeV Au+Au



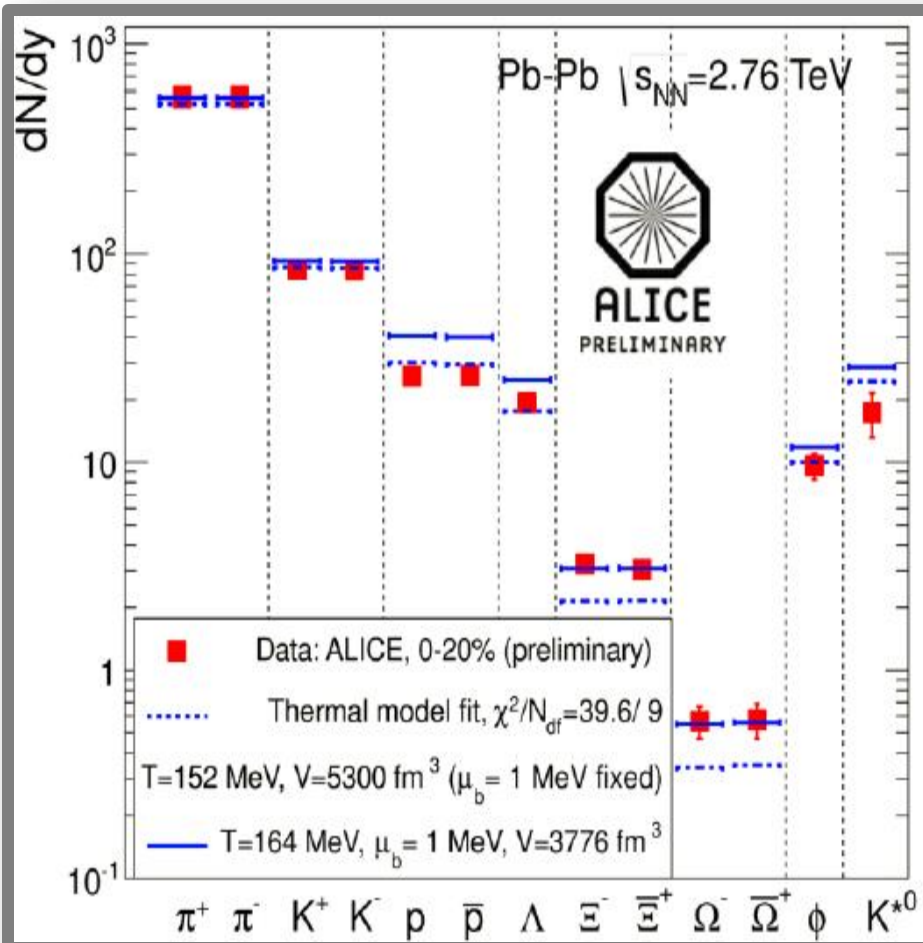
LHC : 2.76 A TeV Pb+Pb



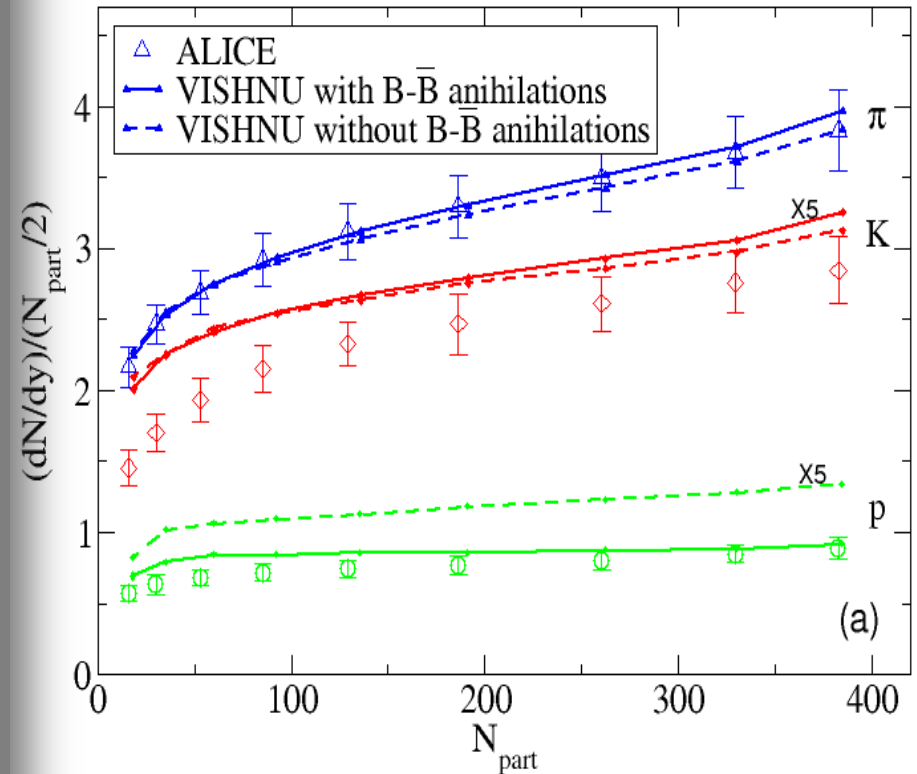
- VISHNU nicely describes the multiplicity for pions, kaons & protons
- B-Bbar annihilations plays an important role for a nice fit of the proton data

VISHNU : $T_{ch} = 165 \text{ MeV}$

dN/dy for identified hadrons (RHIC & LHC)



LHC : 2.76 A TeV Pb+Pb



-VISHNU nicely describes the multiplicity for pions, kaons & protons

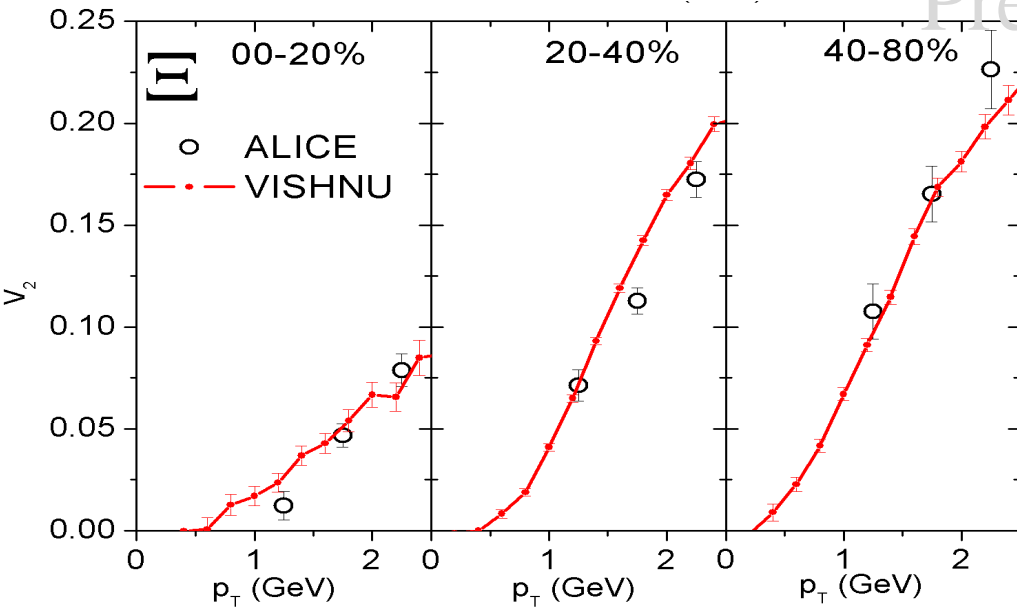
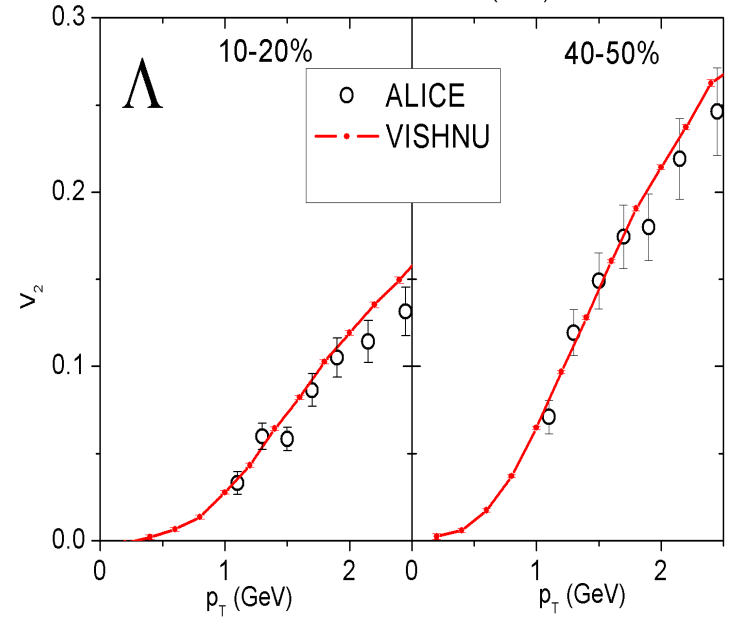
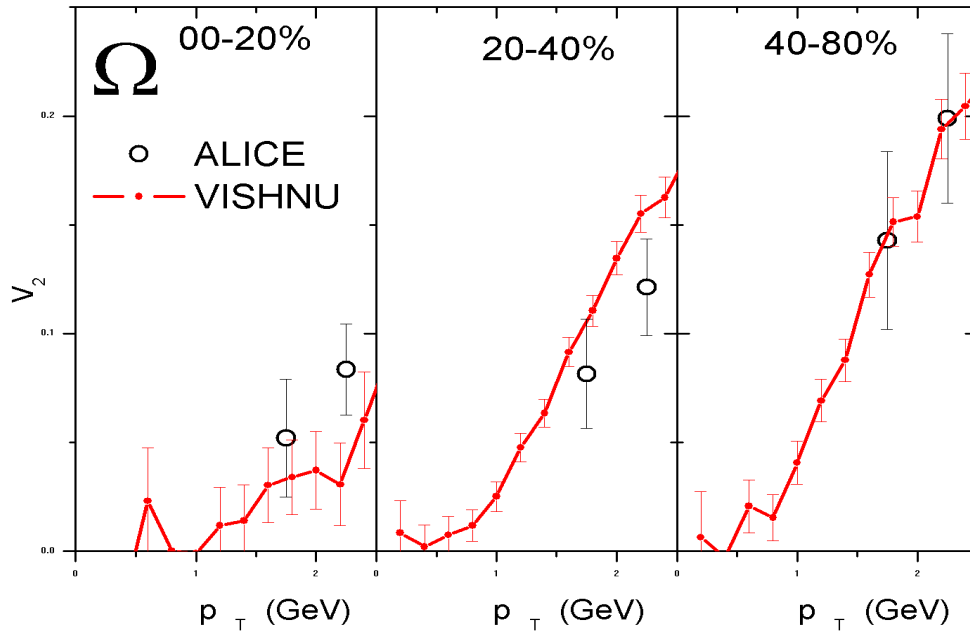
-B-Bbar annihilations plays an important role for a nice fit of the proton data

Statistical Model : $T_{ch} \sim 150$ MeV ?
(no B-Bbar annihilations!)

VISHNU : $T_{ch} = 165$ MeV

Elliptic flow for multi-strange hadrons

V_2 for multi-strange hadrons (LHC)

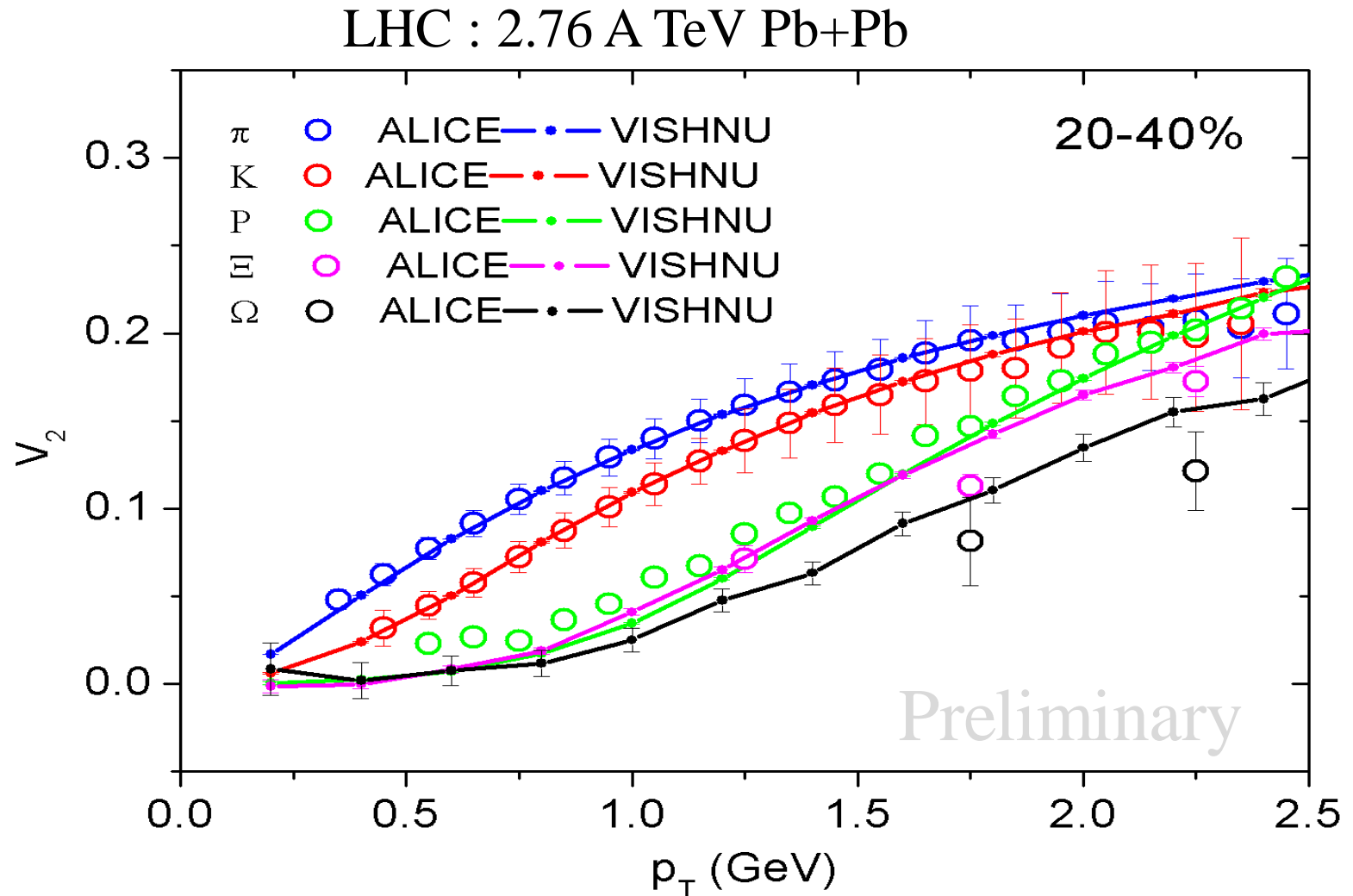


Preliminary

2.76 A TeV Pb +Pb collisions

-a nice description for the elliptic flow for Lambda, Xi and Omega up to 2.5 GeV !

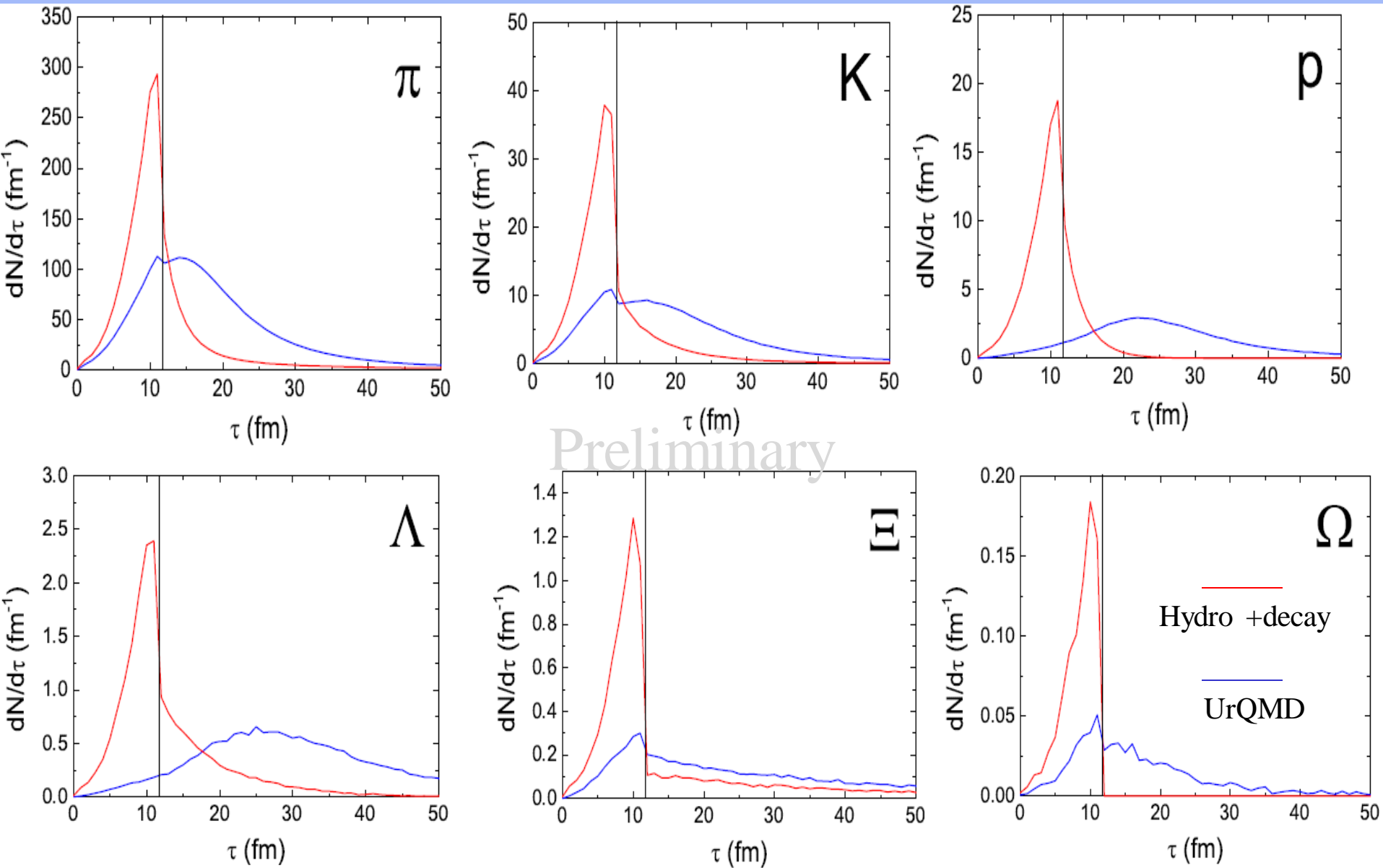
Mass ordering of elliptic flow (LHC)



-Roughly reproduce the mass-ordering!

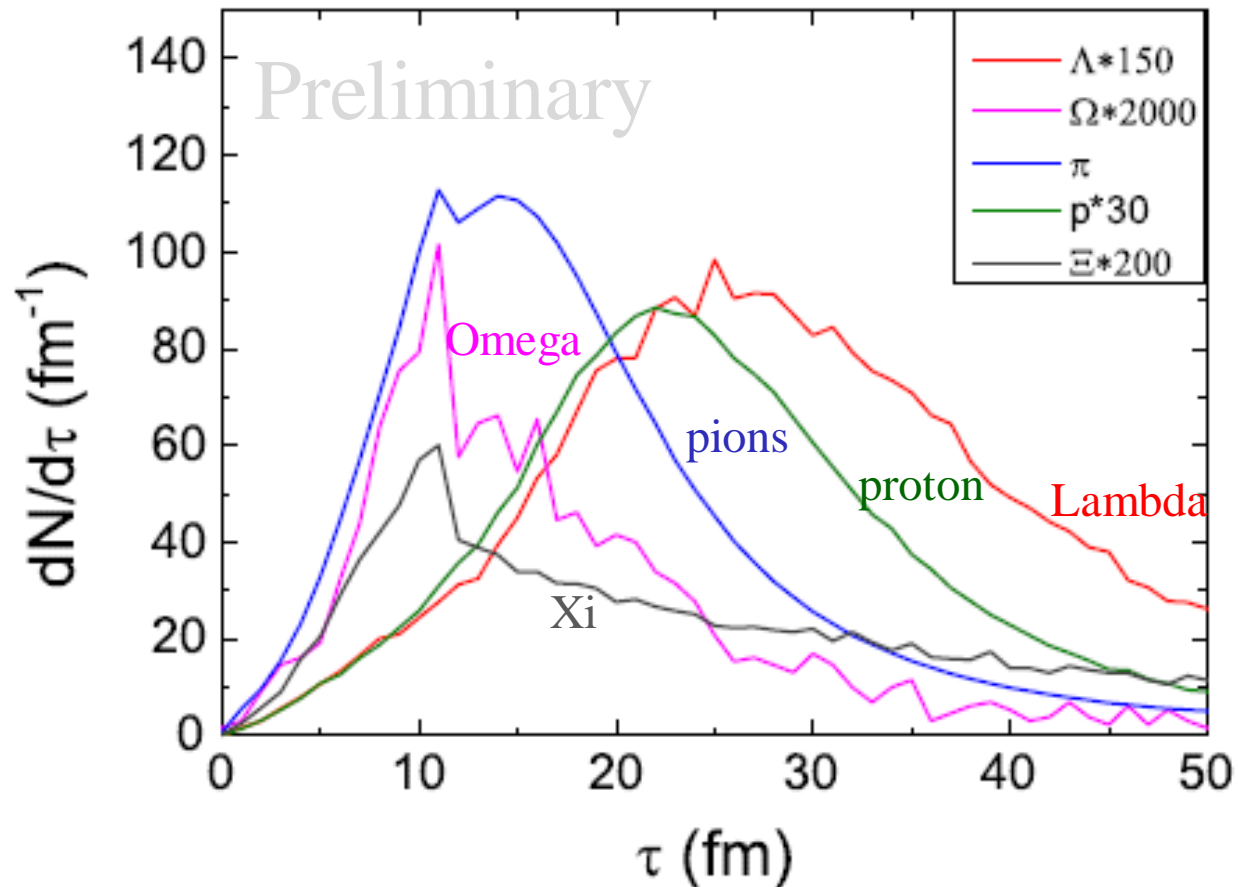
Do these multi-strange hadrons
decouple from the system near T_c ?

UrQMD/decay freeze-out time distributions



-These multi-strange hadrons are NOT that weakly coupled with the medium!

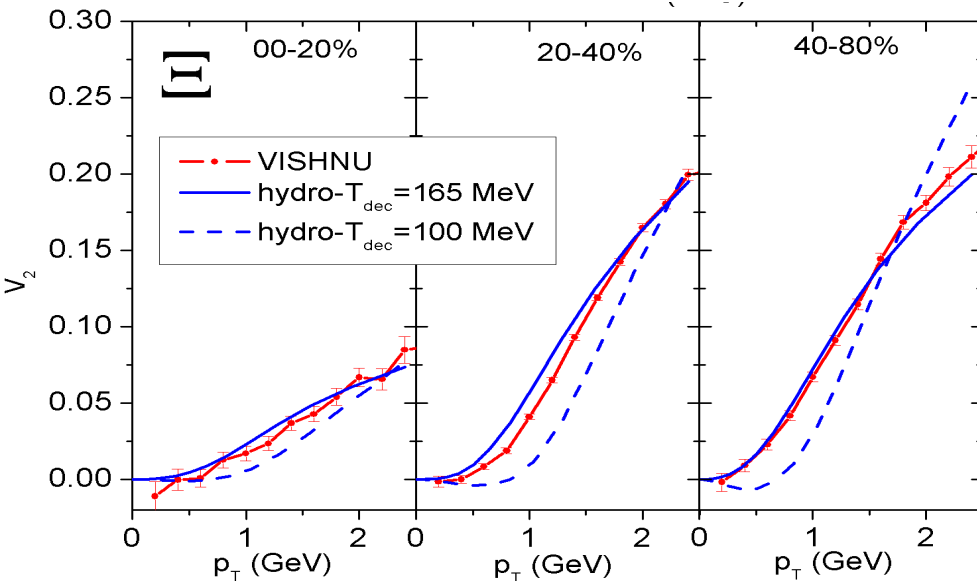
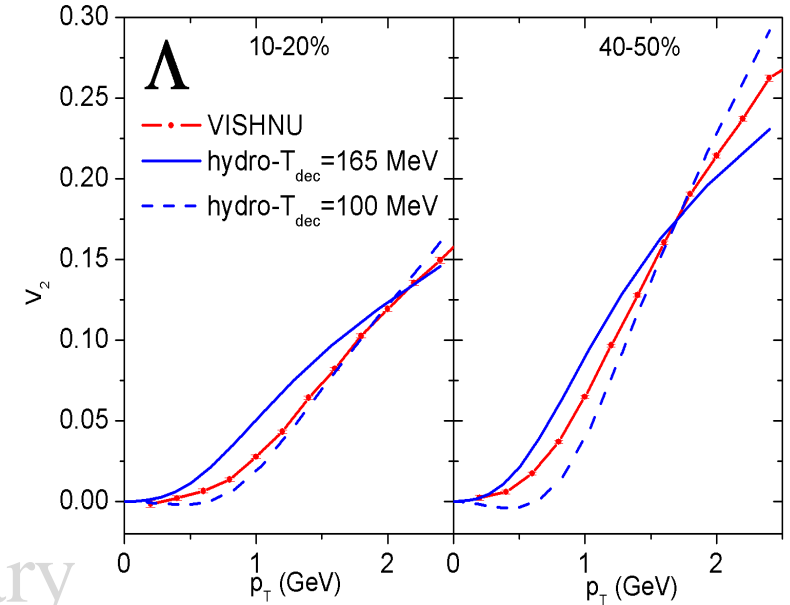
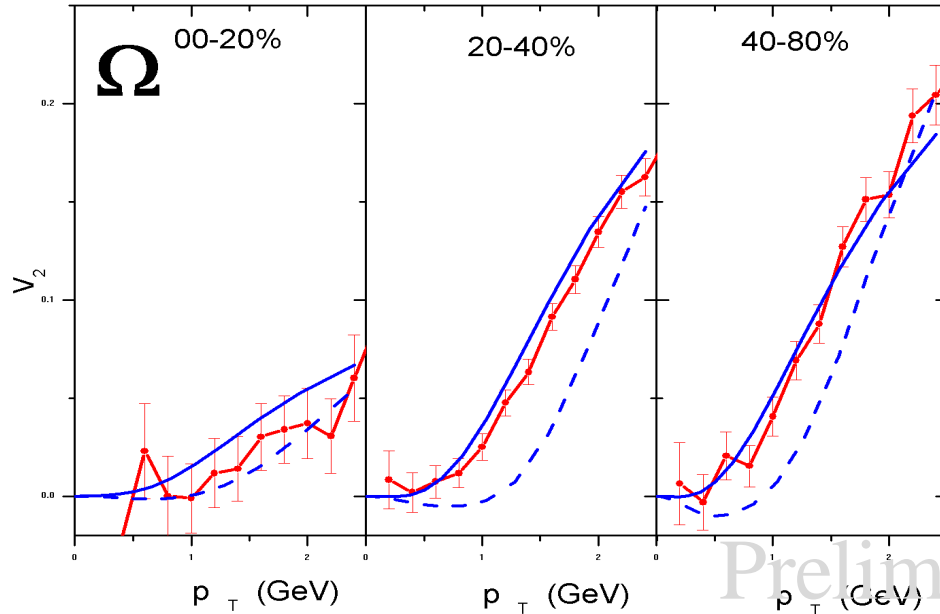
UrQMD freezeout time distributions



-Lamba freeze-out even later than pion and protons !

-earlier freeze-out for Xi and Omega!

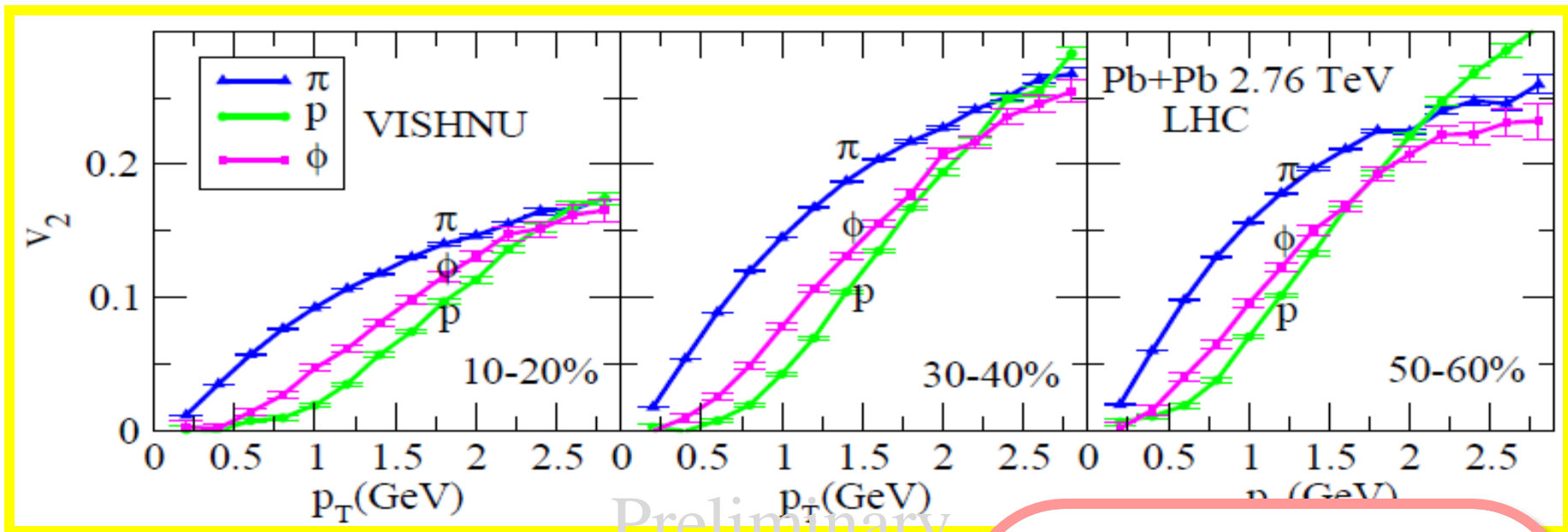
VISHNU vs Hydro with $T_{\text{dec}}=165$ & 100 MeV



- freeze-out temperature for Lambda is much below T_c !
- freeze-out temperatures for Omega and xi are closer to T_c !
- need more studies for firm conclusions

phi-meson

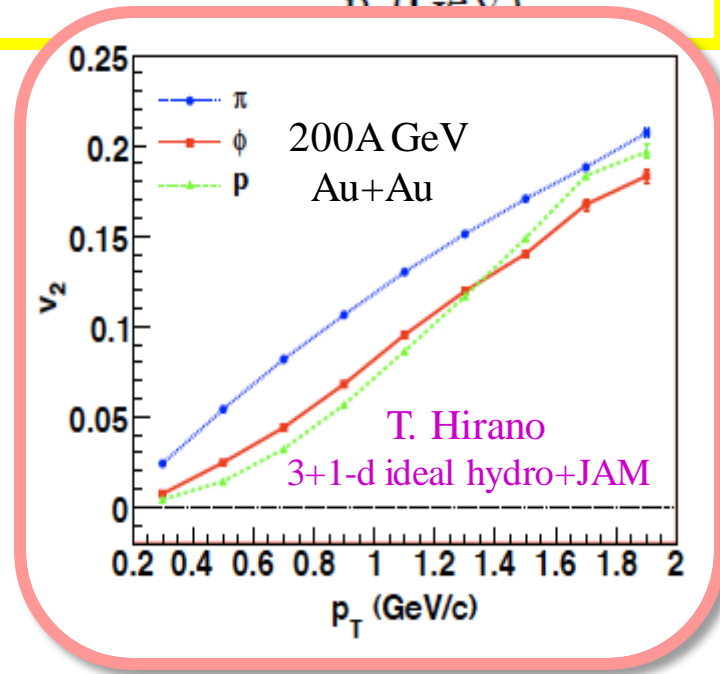
Elliptic flow for phi at the LHC



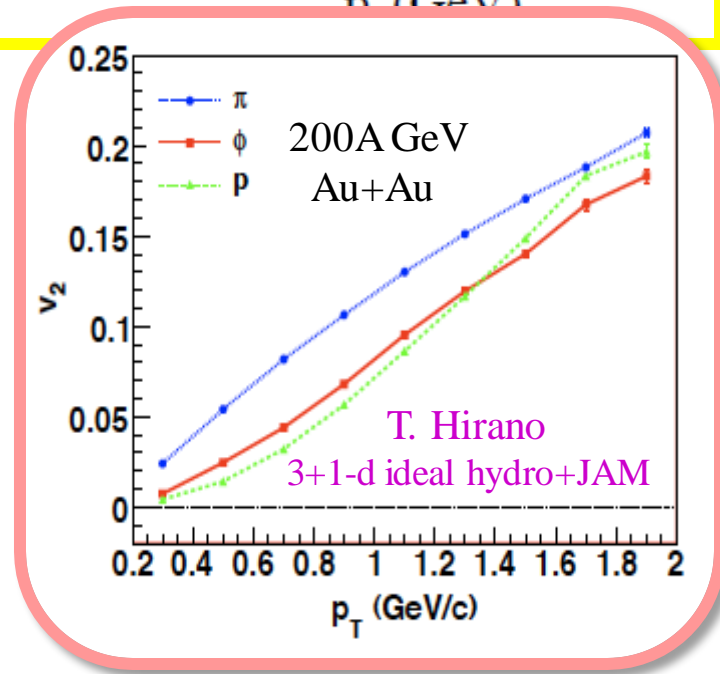
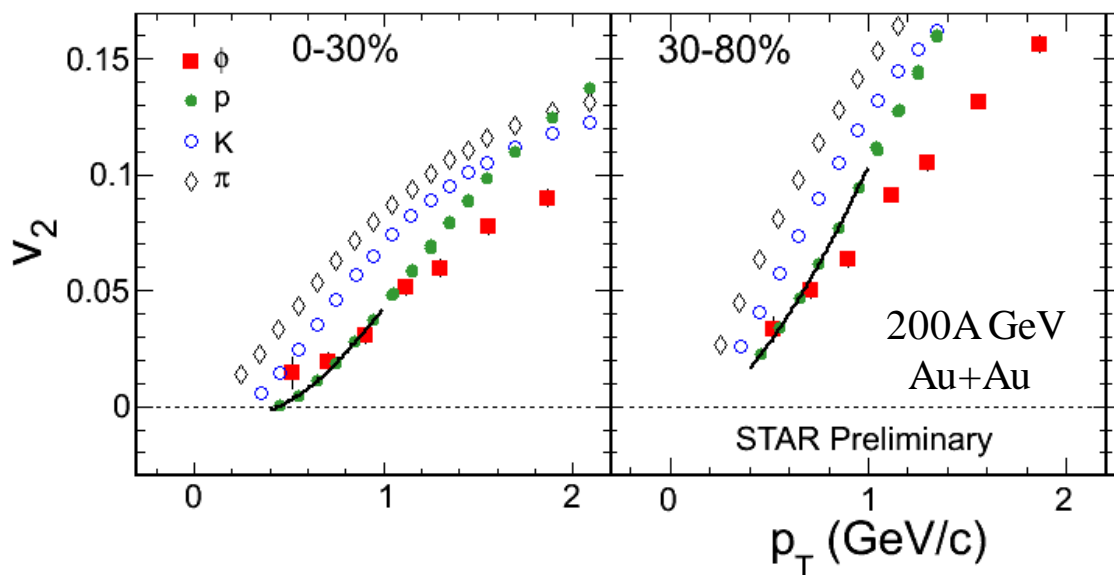
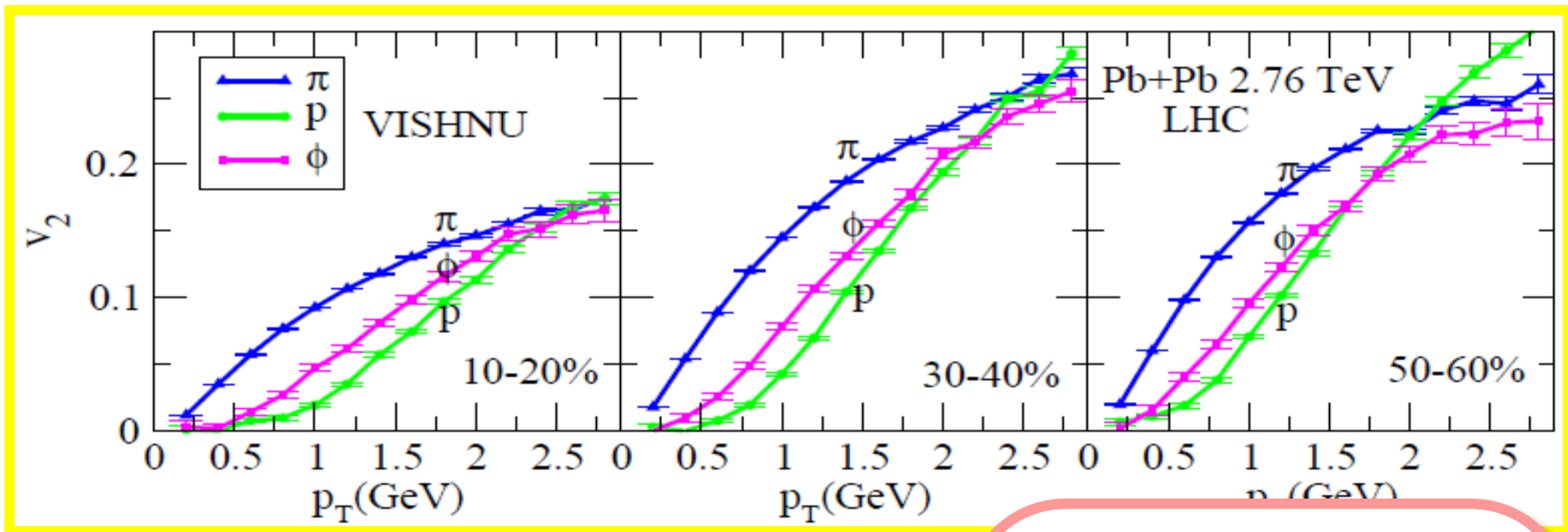
Preliminary

-Hadron cascade: small cross sections for phi

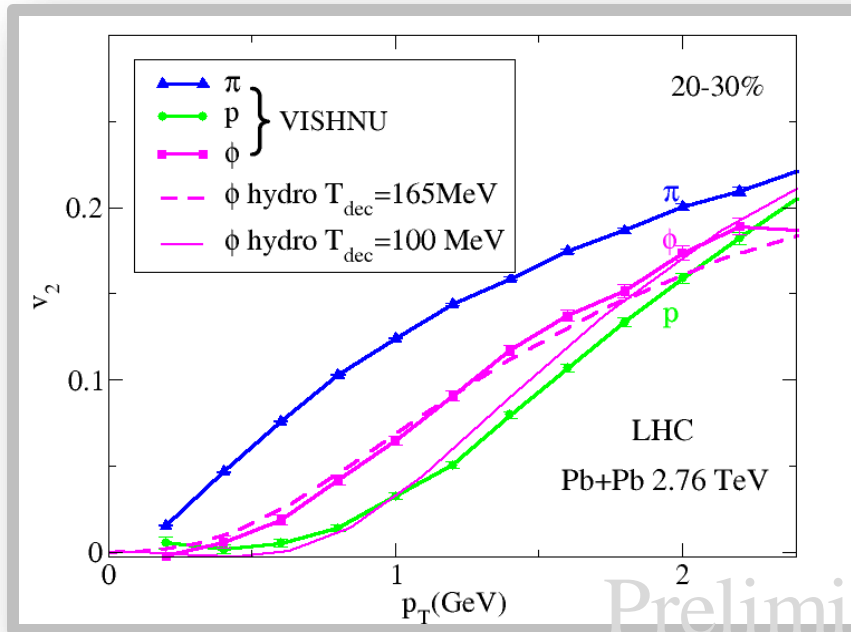
-mass ordering between phi and proton are independent of collision energies, centralities & theoretical details



Elliptic flow for phi at the LHC



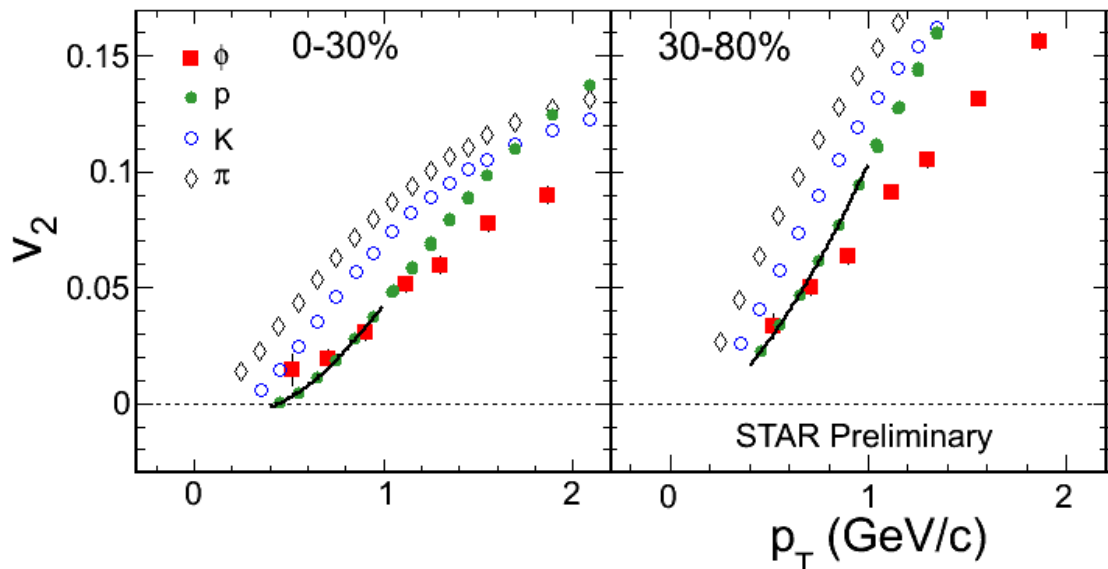
ϕ V_2 in strong & weakly coupling limit



-hydro + $T_{\text{dec}} = 165$ MeV
weakly coupling limit

-hydro + $T_{\text{dec}} = 100$ MeV
strong coupling limit

VISHNU:
small cross sections for ϕ



Neither the strongly nor the weakly coupling limit nor the cases in between (VISHNU) could explain the mass-ordering between proton & ϕ shown in experiment

ϕ -meson puzzle !

Summary

QGP viscosity at RHIC and the LHC

Extraction η/s from elliptic flow data using VISHNU indicates:

$$1 \times (1/4\pi) \leq \eta/s \leq 2.5 \times (1/4\pi) \quad (\text{MC-Glauber; MC-KLN})$$

Approximately similar averaged QGP viscosity at RHIC and LHC energies

Recent developments on initialization models:

color charge fluctuations; multiplicity fluctuations; initial flow fluctuations

to implement e-b-e VISHNU to further study: triangular flow & higher order flow harmonics, higher-order event plane correlations e-b-e v_n

will help us to constrain initialization models, tightening the limit on $(\eta/s)_{QGP}$

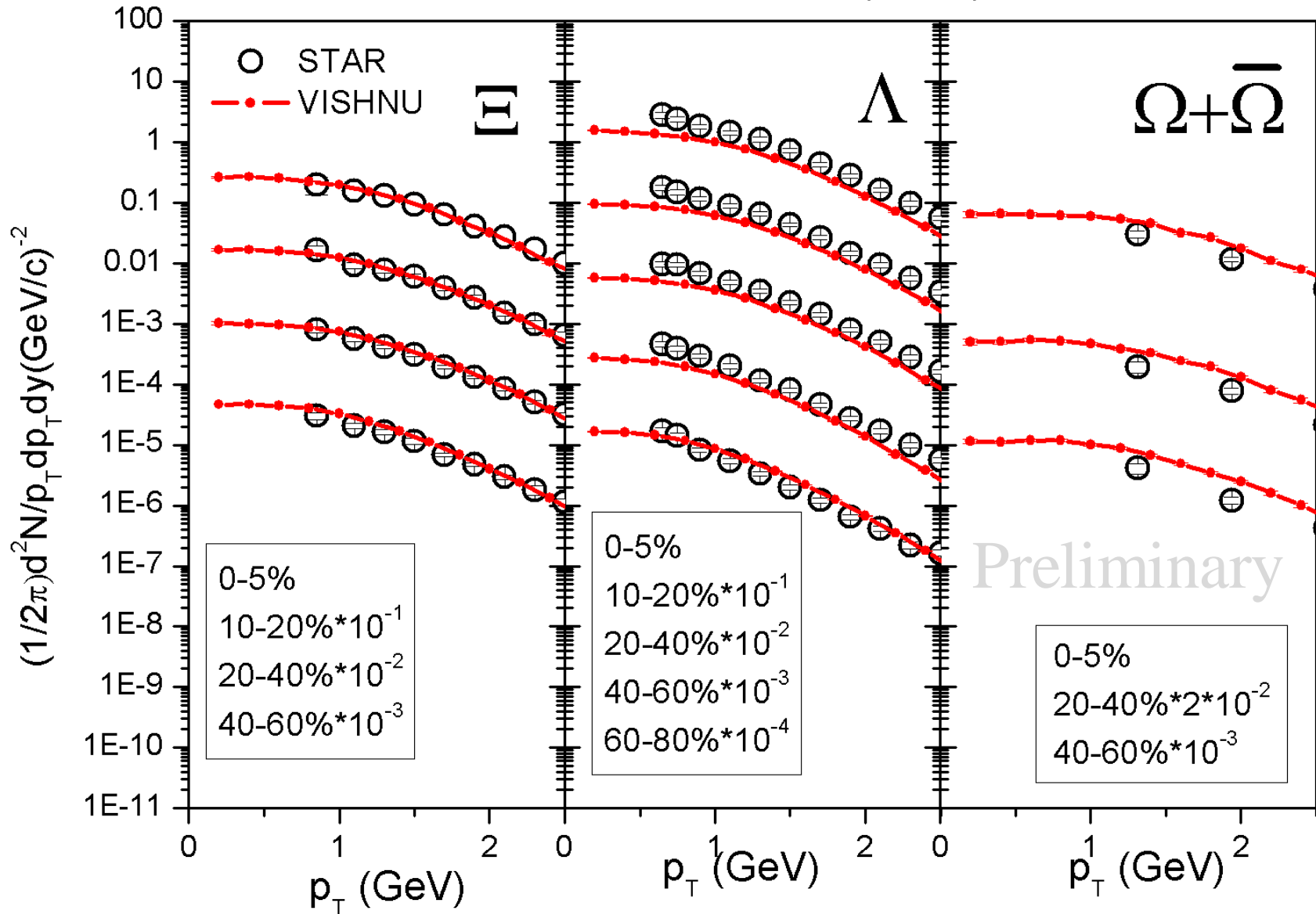
Spectra & V_2 for identified hadrons (& multi-strange hadrons)

- A nice description of the p_T spectra and v_2 for pions, kaons and protons
- **VISHNU with B-Bbar annihilations prefer $T_{ch}=165$ MeV**
- A nice description for $v_2(p_T)$ for multi-strangeness at the LHC for various of centrality.
- **Fails to describe the ϕ - v_2 (RHIC) within the strongly, weakly coupling limit or VISHNU**

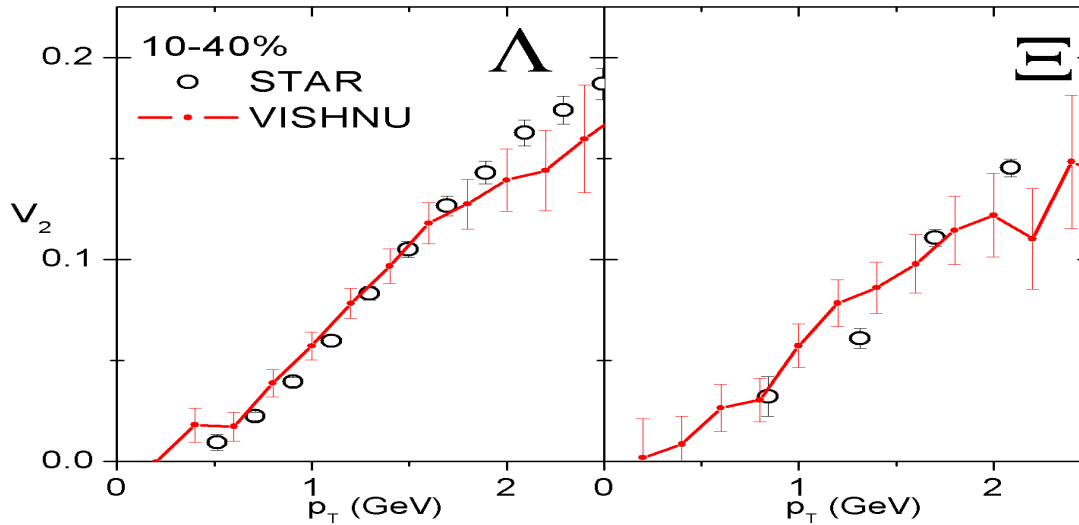
Thank you

Spectra for multi-strange hadrons (RHIC)

Au + Au 200 A GeV (RHIC)



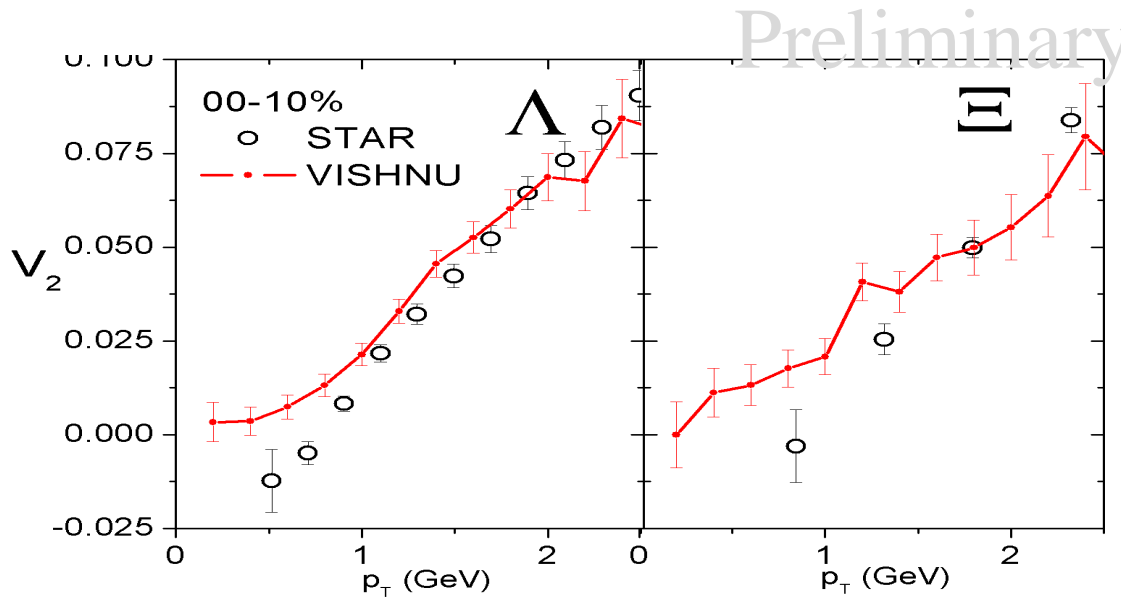
V_2 for multi-strange hadrons (RHIC)



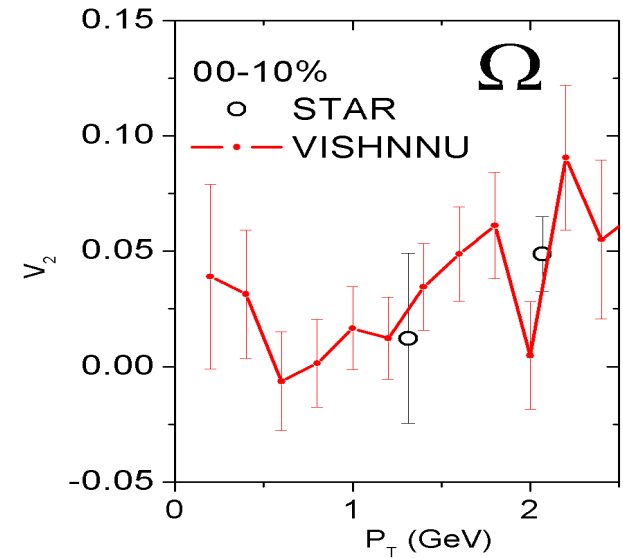
-10-40% : nice description of the experimental data

-High statistic runs are needed in the near future !

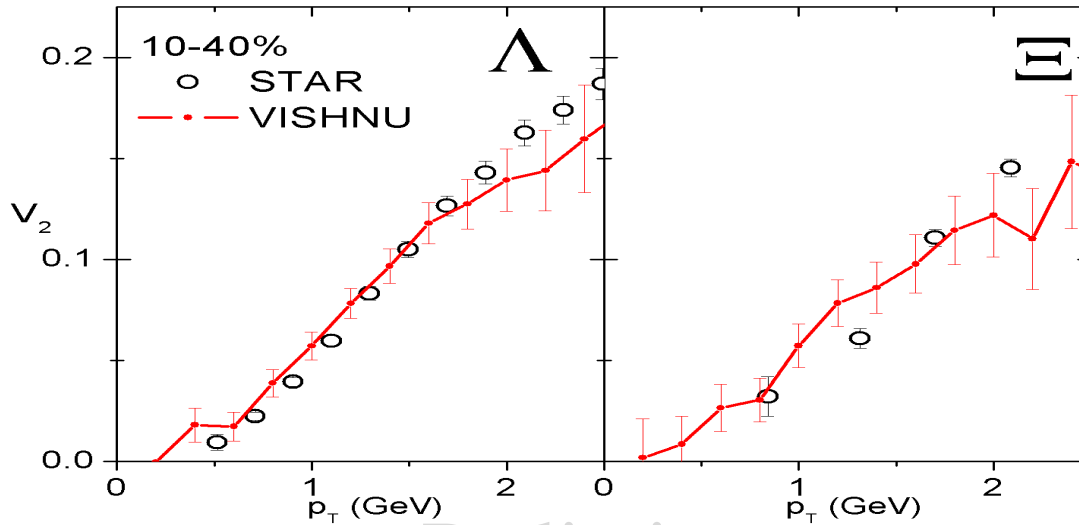
-0-10% : non-flow & fluctuation effects



Preliminary



V_2 for multi-strange hadrons (RHIC)

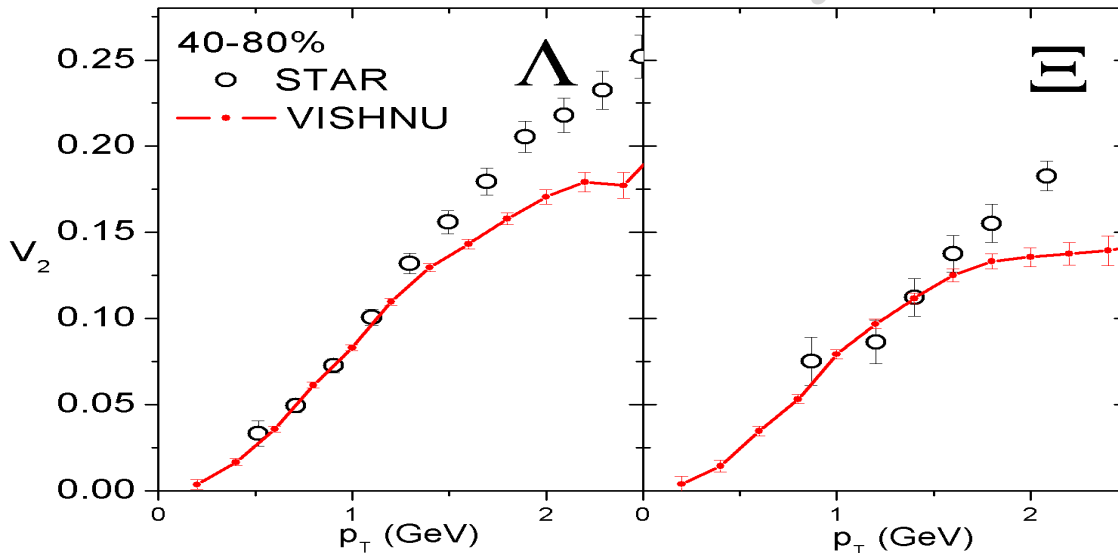


-10-40% : nice description of the experimental data

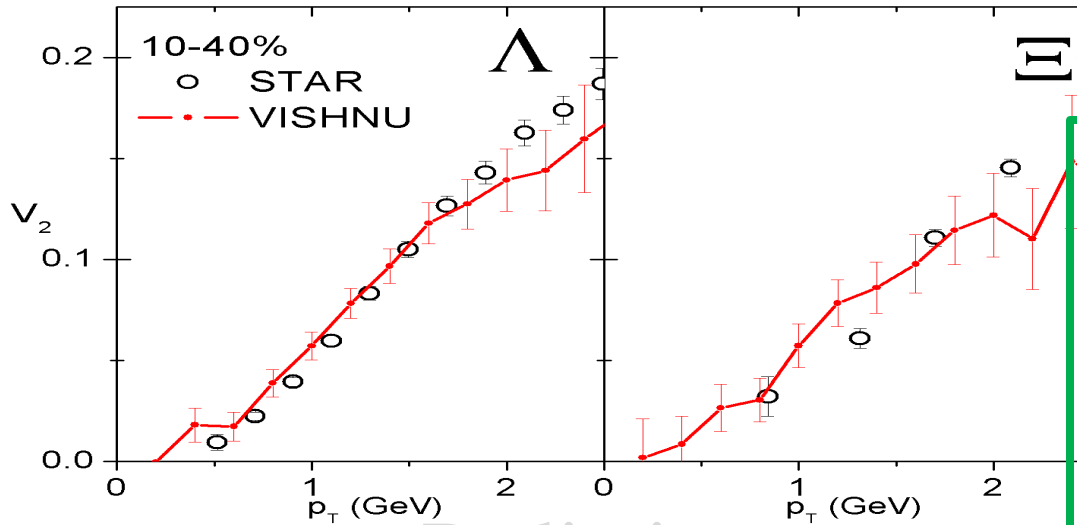
-High statistic runs are needed in the near future !

-40-80%: non-flow & fluctuation effects

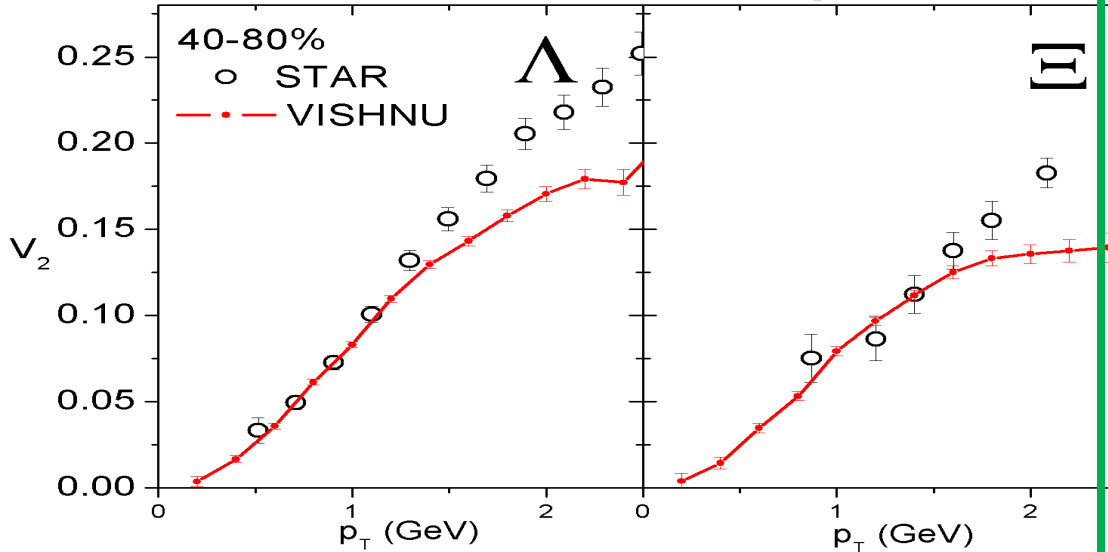
Preliminary



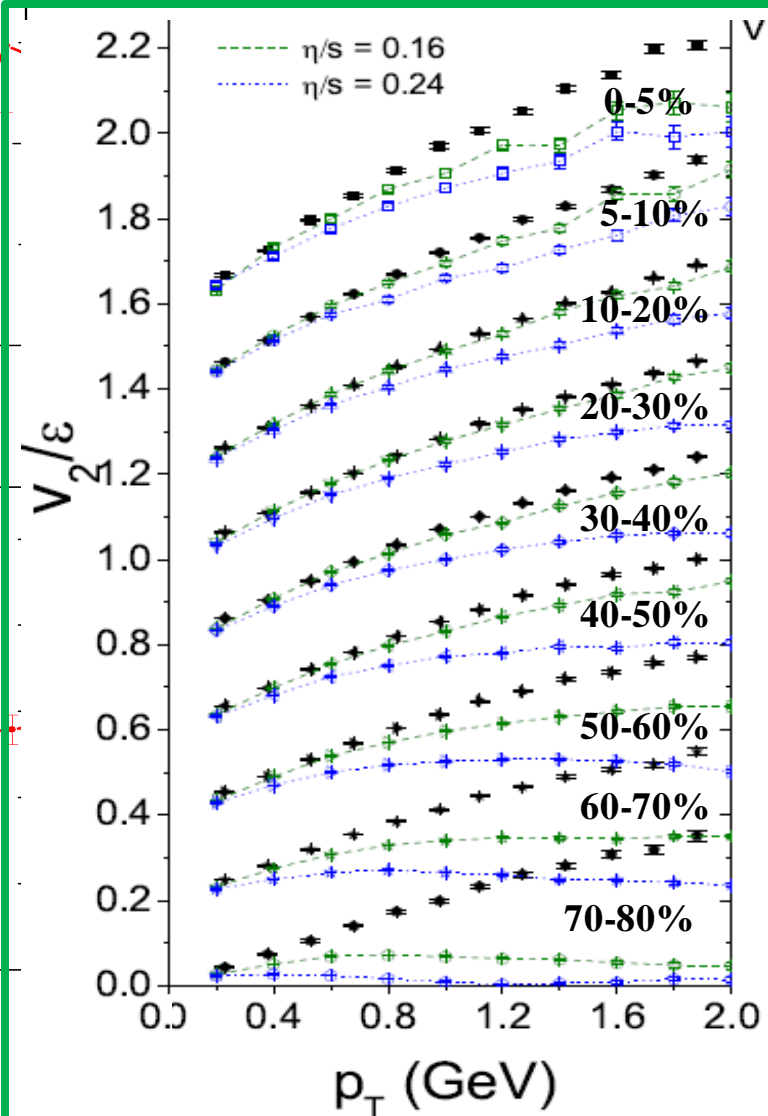
v_2 for multi-strange hadrons (RHIC)



Preliminary

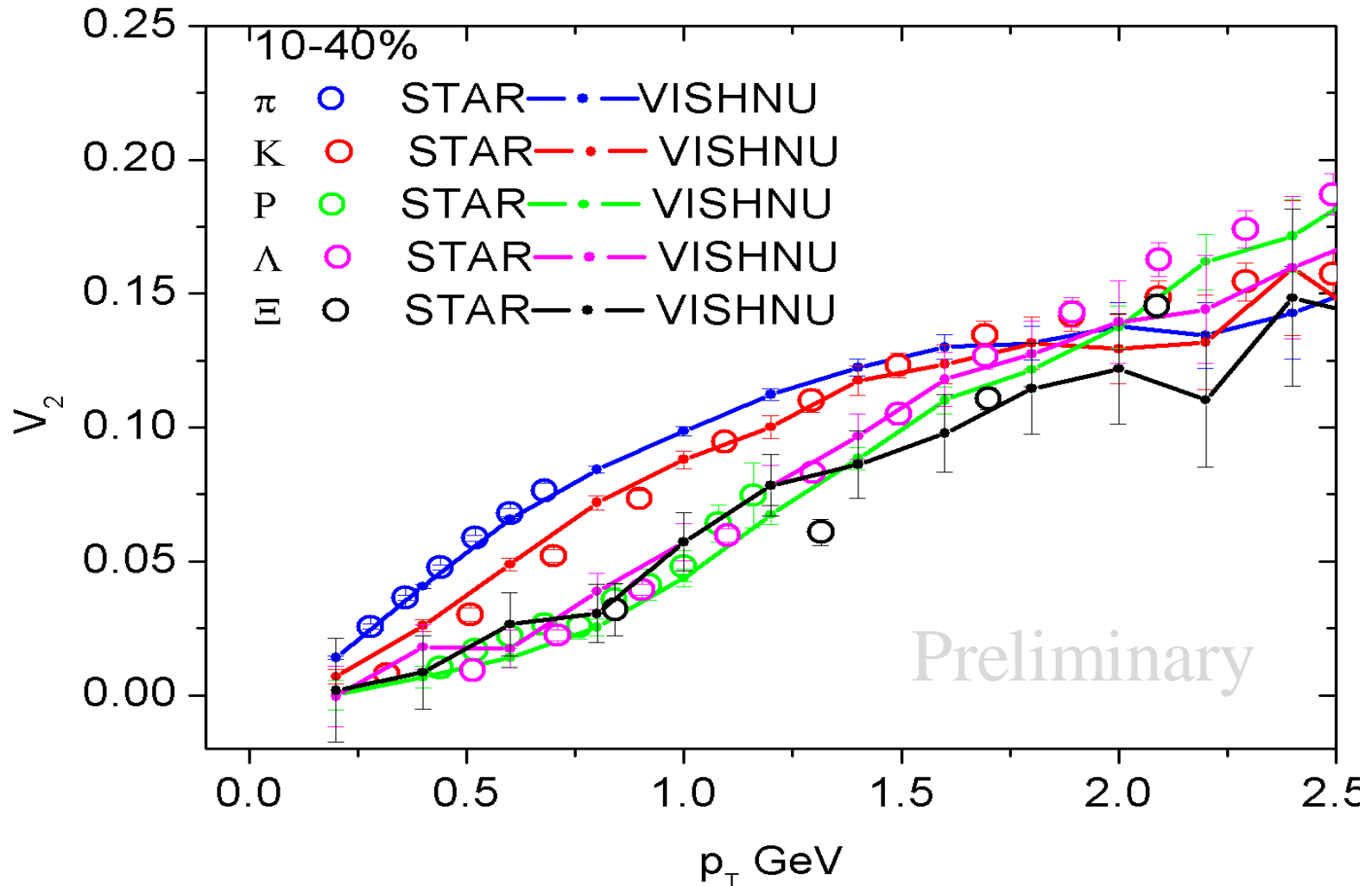


v_2 {EP} for all charged Hadrons
Non-flow & fluctuations



Mass ordering of elliptic flow (RHIC)

RHIC: 200 A GeV Au + Au

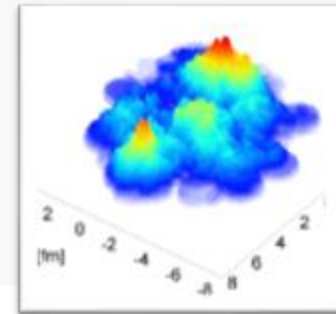


-High statistic runs are needed in the near future !

Initialization Models

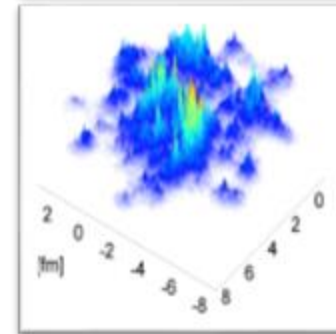
-fluctuations of nucleon positions:

MC-Glauber: } T. Hirano & Y. Nara, Phys. Rev. C 79 064904 (2009)
MC-KLN: } (used in the **VISHNU hybrid model**)



-fluctuations of color charges (in the framework of CGC):

IP-Glasma: B. Schenke et al., arXiv:1202.6646; 1206.6805 [nucl-th]
C. Gale, et al., arXiv: 1210.5144, 1209.5330 [nucl-th].



Correlated Fluctuation: B. Muller & A. Schafer, arXiv:1111.3347 [hep-ph]
S. Moreland, Z. Qiu and U. Heinz, arXiv:1210.5508

-fluctuations of local gluon numbers (in the framework of MC-KLN):

Multiplicity fluctuations: A. Dumitru and Y. Nara, Phys. Rev. C 85, (2012) 034907
A. Dumitru, arXiv:1210.7864 [hep-ph].

Pre-equilibrium dynamics

Free Streaming limit: G. Qin, et. al., Phys. Rev. C82 064903 (2010); OSU, on-going work

Hydro limit: OSU group, on-going work

Pre-equilibrium dynamics smoothes out fluctuations, reducing $\varepsilon_2, \varepsilon_3$, but building radial flow

-early flow & fluctuations from dynamical models:

URQMD initialization: H.Petersen & M. Bleicher, Phys. Rev. C81, 044906,2010

AMPT initialization: L. Pang, Q.Wang & X.N.Wang, arXiv:1205.5019 [nucl-th]

L. Pang, Q.Wang & X.N.Wang, arXiv: 1211.1579[nucl-th]

EPOS/NEXUS initialization: K. Werner et al., Phys. Rev. C83:044915,2011;

H. J. Drescher et, al., Phys.Rev. C65 , 054902 (2002).

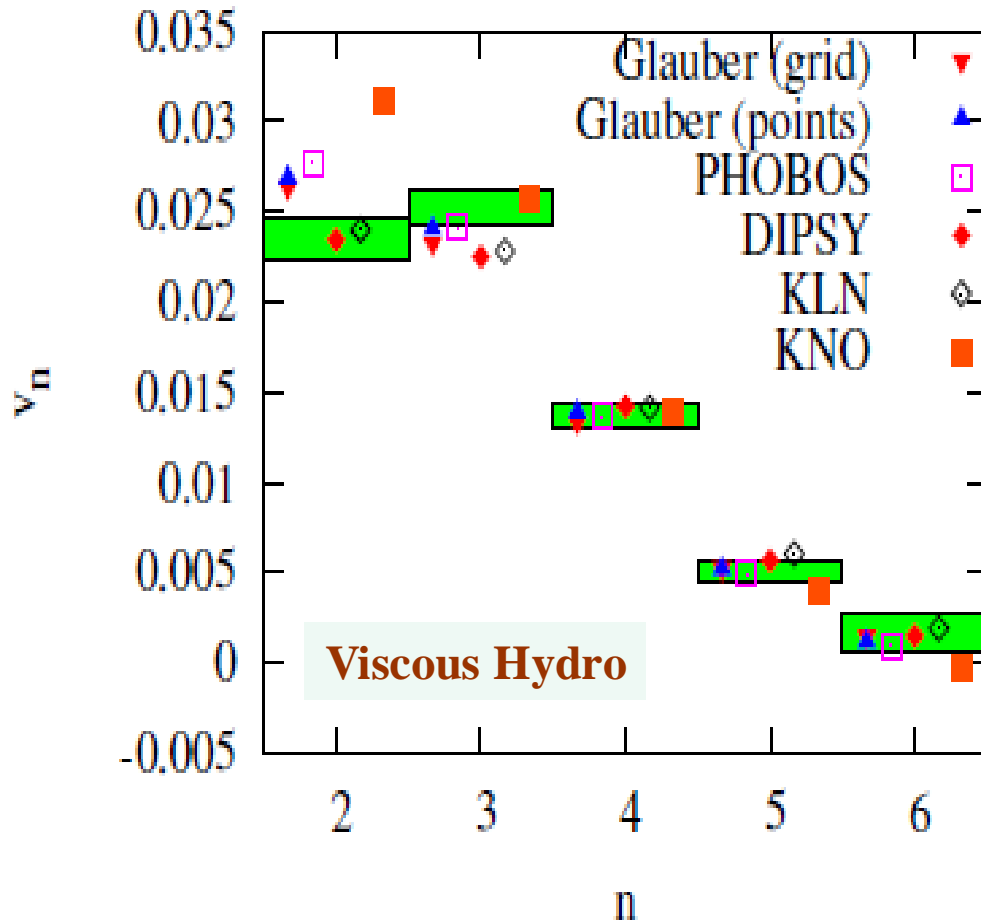
IP-Glasma: B. Schenke, et.al, arXiv:1202.6646; 1206.6805 [nucl-th]

C. Gale, et al., arXiv:1210.5144, 1209.5330 [nucl-th].

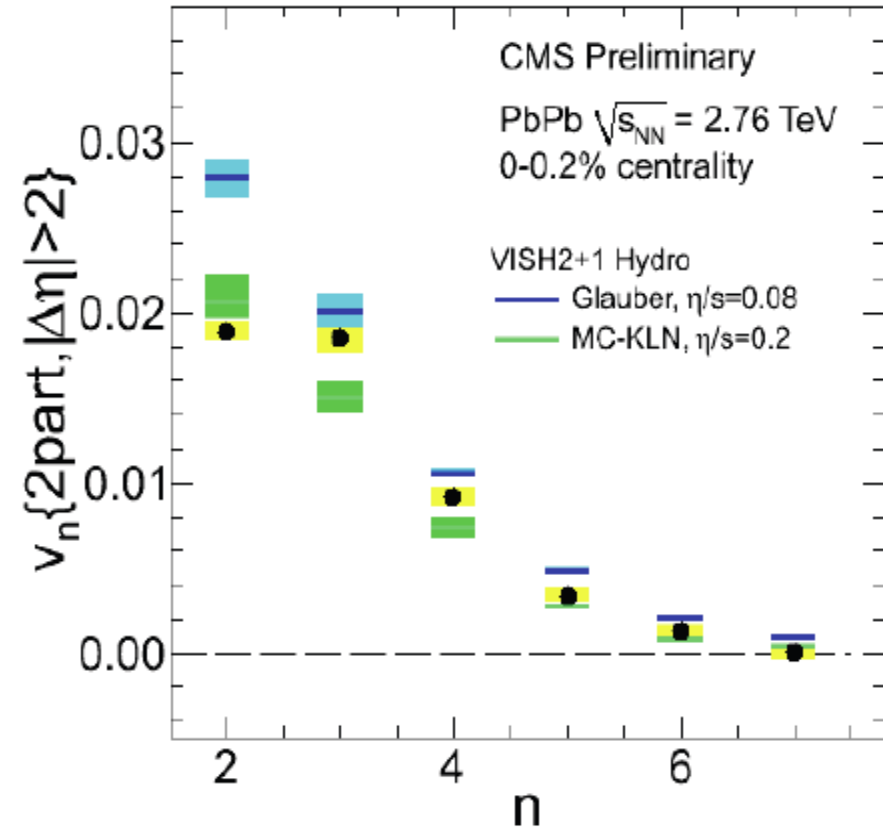
Except IP-Glasma, most pre-equilibrium dynamics was studied within the ideal hydro framework. Their quantitative influences on $(\eta/s)_{QGP}$ are still unknown.

Extracting η/s from V_n in ultra-central collisions

Luzum & Ollitrault, arXiv: 1210.8422



C. Shen, Z. Qiu, and U. Heinz.

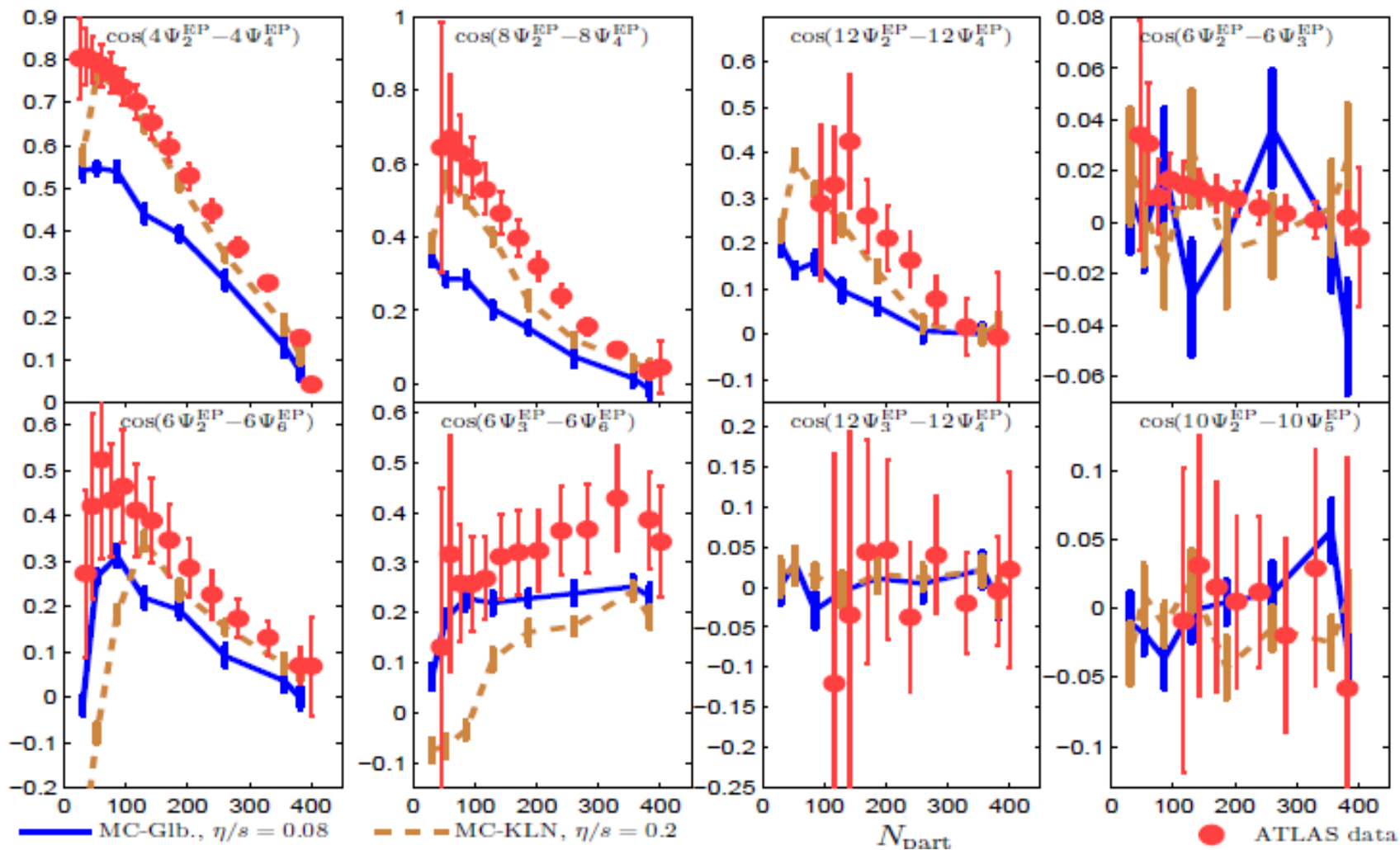


-In most central collisions, fluctuation effects are dominant (Geometry effects are suppressed)

-can not simultaneously fit V_2 and V_3 with single η/s (MC-Glauber & MC-KLN)

Higher Order Event Plane Correlations

Qiu & Heinz, arXiv:1208.1200[nucl-th]



EXP. data:[ATLAS Collaboration],
CERN preprint ATLAS-CONF-2012-049

Pure e-b-e viscous hydro simulations :
qualitatively reproduce the measured event plane correlations

V_n & E-b-E V_n distributions

C. Gale et al., arXiv:1209.4330[nucl-th]

