

# Resummation in processes with jet veto

Xiaohui Liu

partly based on work with Frank Petriello  
arXiv:1210.1906

Chicago 2012 Workshop on LHC Physics



# Outline

- Motivation
- Processes with jet vetoes
- Conclusion and Outlook

# Motivation

- Cross section with jet bins
  - Higgs + 0-j, 1-j, >2-j
  - W+2-j, 3-j
  - BSM searches

Search for dark matter candidates and large extra dimensions in events with a photon and missing transverse momentum in  $pp$  collision data at  $\sqrt{s} = 7$  TeV with the ATLAS detector

The ATLAS Collaboration

Events with more than one jet with  $p_T > 30$  GeV and  $|\eta| < 4.5$  are rejected. Events with one jet are retained to increase the signal acceptance and reduce systematic uncertainties related to the modeling of initial-state radiation. The reconstructed photon,  $E_T^{\text{miss}}$  vector and jets (if found) are required to be well separated in the transverse plane with  $\Delta\phi(\gamma, E_T^{\text{miss}}) > 0.4$ ,  $\Delta R(\gamma, \text{jet}) > 0.4$ , and  $\Delta\phi(\text{jet}, E_T^{\text{miss}}) > 0.4$ . Additional quality criteria [13] are applied to ensure that jets and photons are not pro-

ATLAS [7, 8], the yields corresponding to CTEQ6.6 [31] PDFs are used, as obtained by reweighting these samples. The samples are normalized to NLO predictions [32]. The LO-to-NLO normalization factors decrease from 1.5 to 1.1 as  $n$  increases.

Simulated events corresponding to the  $\chi\bar{\chi} + \gamma$  process with a minimum photon  $p_T$  of 80 GeV are generated using LO matrix elements from MADGRAPH [33] interfaced to PYTHIA 6 using CTEQ6L1 PDFs. Values for  $m_\chi$  be-

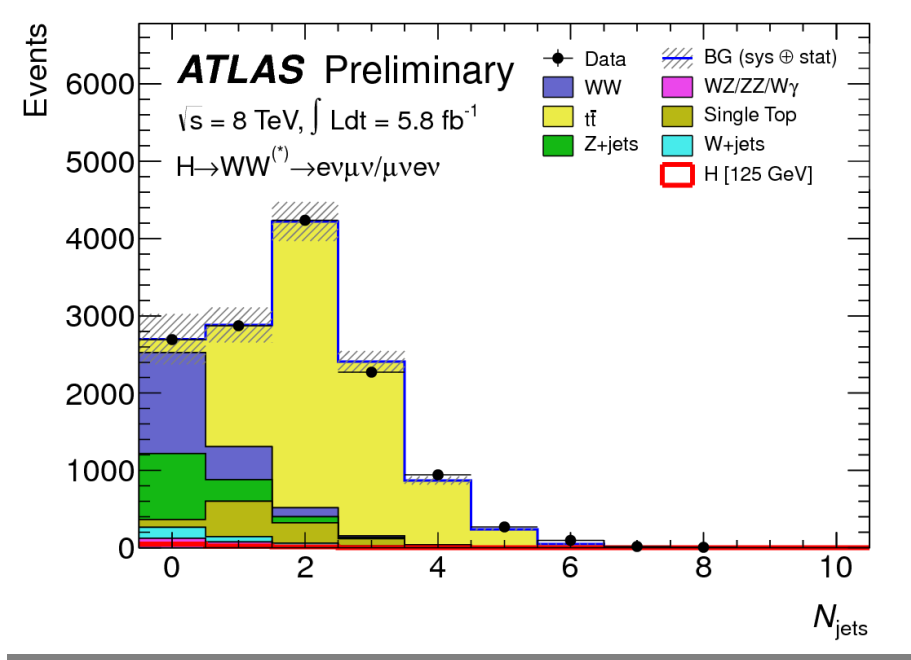
Study of the dijet mass spectrum in  $pp \rightarrow W + \text{jets}$  events at  $\sqrt{s} = 7$  TeV

The CMS Collaboration [7]

Events are selected with one well-identified and isolated lepton (muon or electron), large missing transverse energy  $E_T$ , and exactly two or exactly three high- $p_T$  jets. The selection criteria are similar to those used at the Tevatron [1, 2], but modified to adapt to the higher background rates and different experimental conditions at the LHC. We also place more stringent requirements on the jet kinematics, as suggested in Ref. [3], to enhance any signal compared to the irreducible W plus jets background. We investigate three representative models, a technicolor  $\pi_\tau$  from the decay of a technicolor  $\rho_\tau$  [4], a leptophobic  $Z'$  decaying to two jets [5], and the

# Motivation

- Cross section with jet bins
  - Advantage
    - Beat the backgrounds  $p_T^{veto} \approx 25\text{GeV} - 30\text{GeV}$

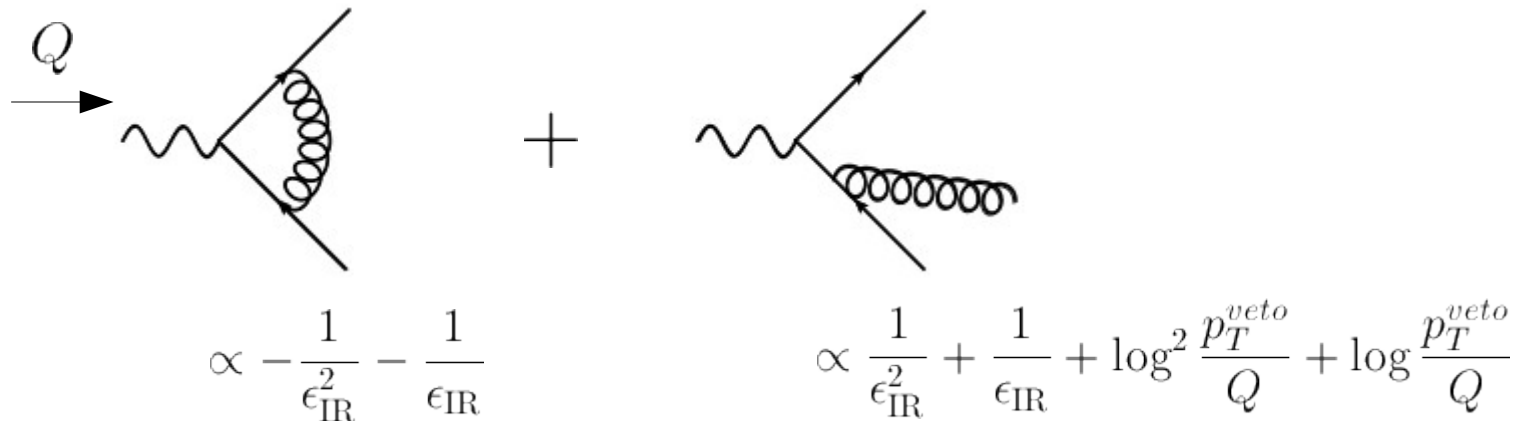


# Motivation

- Cross section with jet bins

- Problems

- Sudakov Logarithms  $\sum_{n,m} C_{n,m} \alpha_s^n L^{2n-m}$ ,  $L = \log \frac{p_T^{veto}}{Q}$



$\propto -\frac{1}{\epsilon_{\text{IR}}^2} - \frac{1}{\epsilon_{\text{IR}}}$

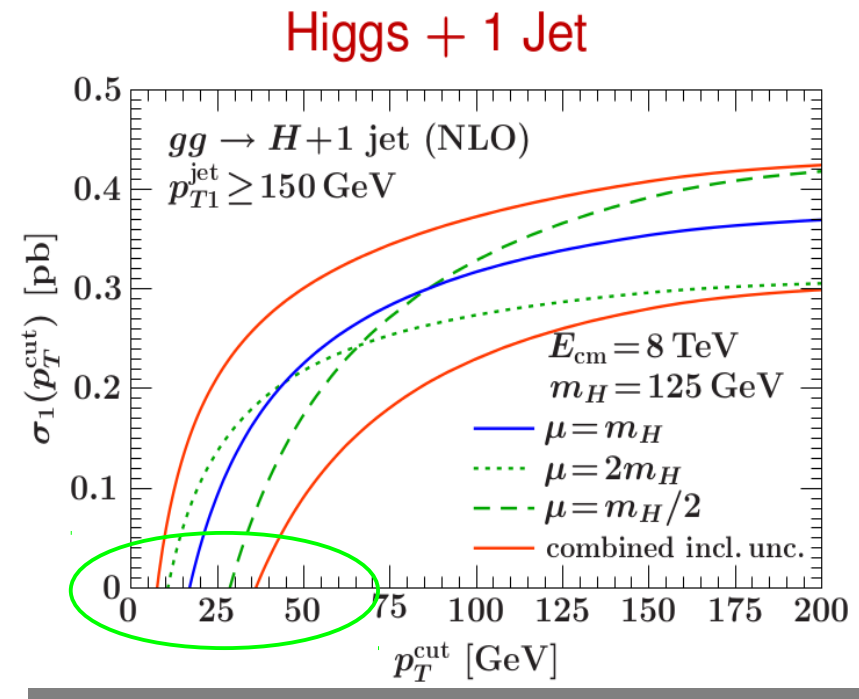
$\propto \frac{1}{\epsilon_{\text{IR}}^2} + \frac{1}{\epsilon_{\text{IR}}} + \log^2 \frac{p_T^{veto}}{Q} + \log \frac{p_T^{veto}}{Q}$

# Motivation

- Cross section with jet bins

- Problems

- Sudakov Logarithms  $\sum_{n,m} C_{n,m} \alpha_s^n L^{2n-m}$ ,  $L = \log \frac{p_T^{\text{veto}}}{Q}$ 
      - Breakdown of fixed-order calculations



# Motivation

- Cross section with jet bins

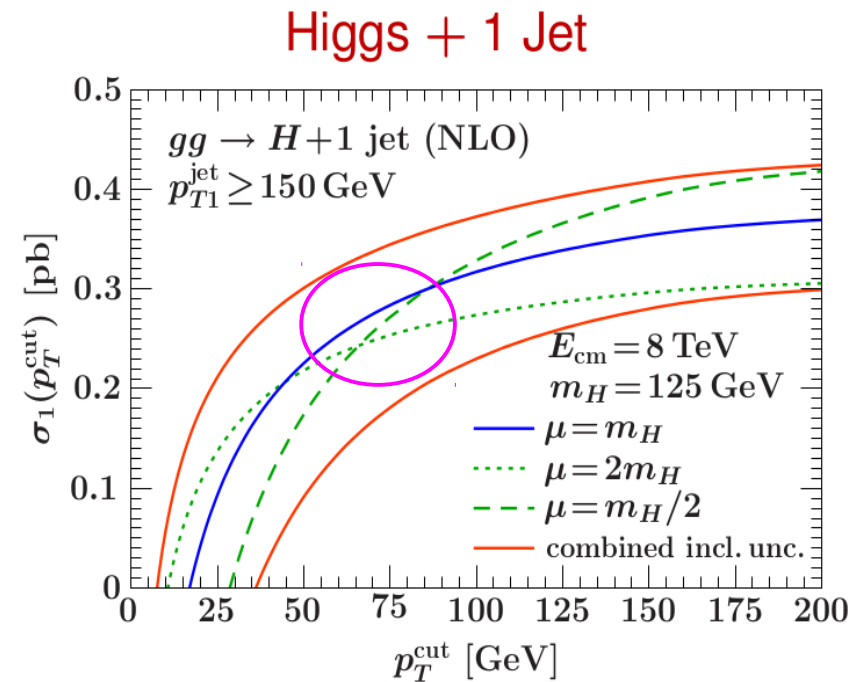
- Problems

- Sudakov Logarithms  $\sum_{n,m} C_{n,m} \alpha_s^n L^{2n-m}$ ,  $L = \log \frac{p_T^{\text{veto}}}{Q}$

- Breakdown of fixed-order calculations

- Unreliable uncertainty estimation (Stewart and Tackmann '11)

Large K Factor – Large Logs



# Motivation

- Cross section with jet bins

- Problems

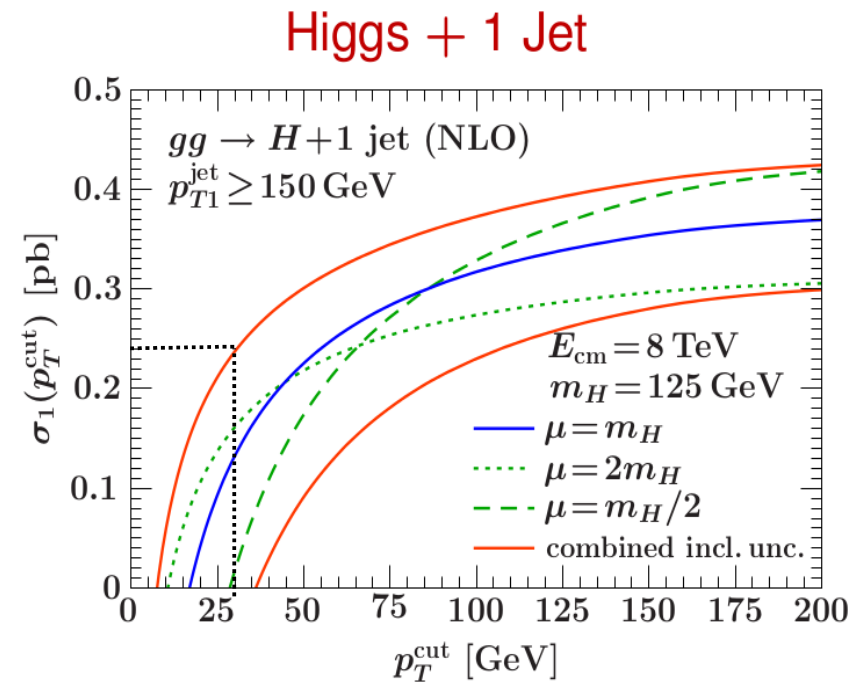
- Sudakov Logarithms  $\sum_{n,m} C_{n,m} \alpha_s^n L^{2n-m}$ ,  $L = \log \frac{p_T^{\text{veto}}}{Q}$

- Breakdown of fixed-order calculations

- Unreliable uncertainty estimation (Stewart and Tackmann '11)

Large K Factor – Large Logs

- Large Uncertainties





# Processes with jet vetoes

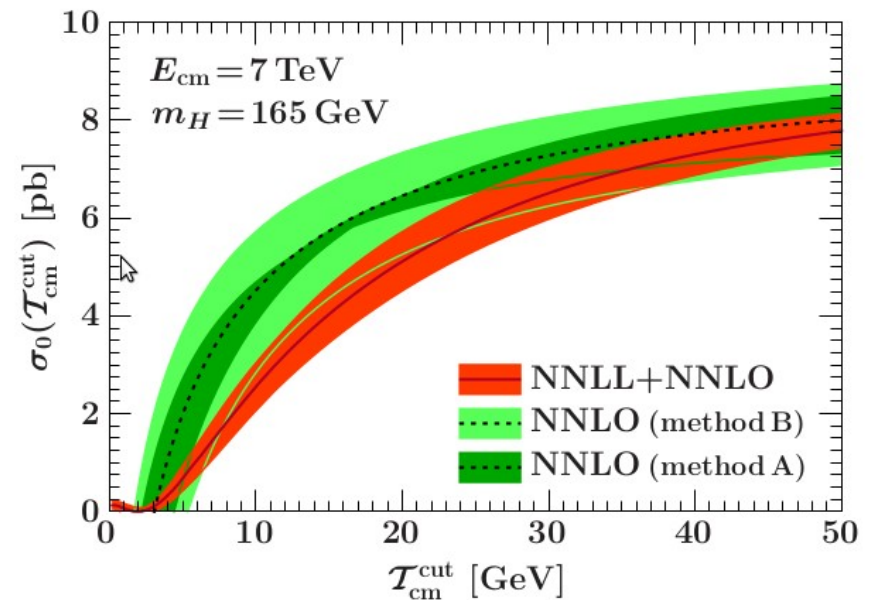
- Previous efforts

- Jettiness (Stewart, Tackmann, Waalewijn '10, Berger and et al, '11)

- Up to NNLL + NNLO accuracy

$$\begin{aligned}
 \sigma \propto & 1 + \alpha_s L^2 + \alpha_s^2 L^4 + \alpha_s^3 L^6 \dots && \text{LL} \\
 & + \alpha_s L + \alpha_s^2 L^3 + \alpha_s^3 L^5 \dots && \text{NLL} \\
 & + \alpha_s n + \alpha_s^2 L^2 + \alpha_s^3 L^4 + \dots && \text{N}^2\text{LL} \\
 & + \alpha_s^2 L + \alpha_s^3 L^3 + \dots \\
 & + \alpha_s^2 n_1 + \alpha_s^3 L^2 \dots
 \end{aligned}$$

Pythia : LL + tuning  
 MC@NLO : NLO + LL

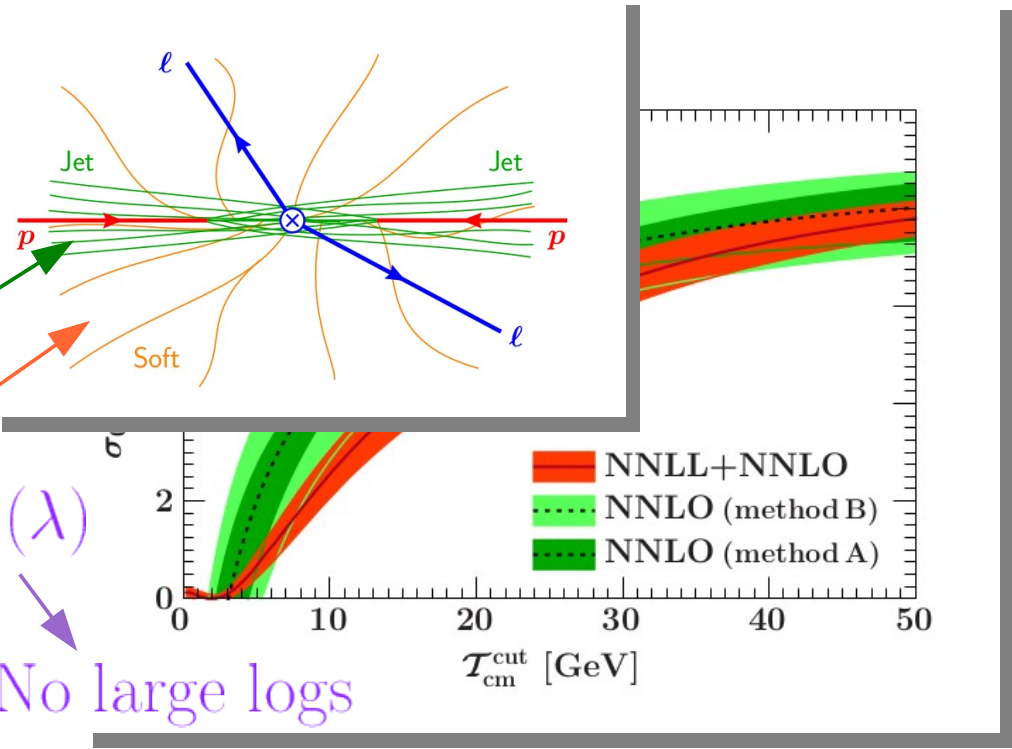


# Processes with jet vetoes

- Previous efforts

- Jettiness (Stewart, Tackmann, Waalewijn '10, Berger and et al, '11)

- Up to NNLL + NNLO accuracy
- Factorization

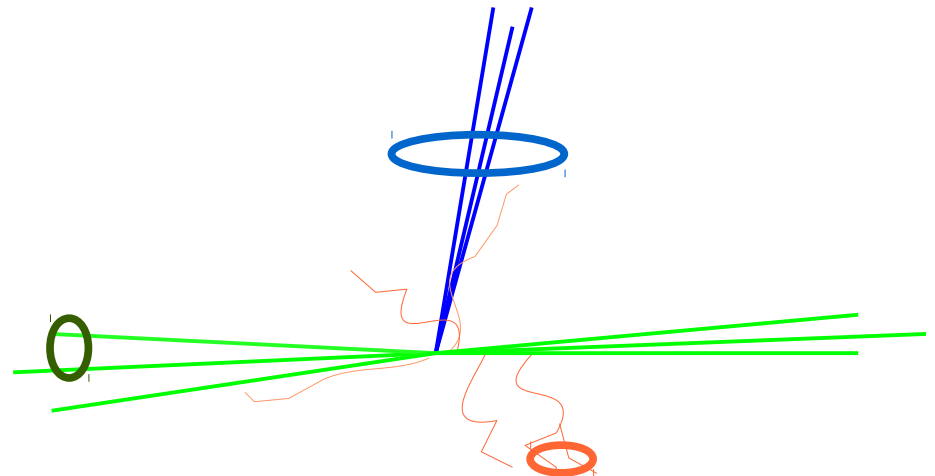


$$d\sigma \sim H \mathcal{B}_a \mathcal{B}_b \otimes S + \mathcal{O}(\lambda)$$

RGE  $\log \frac{Q}{\mu}$   $\log \frac{\sqrt{Q\mathcal{T}}}{\mu}$   $\log \frac{\mathcal{T}}{\mu}$  No large logs

# Processes with jet vetoes

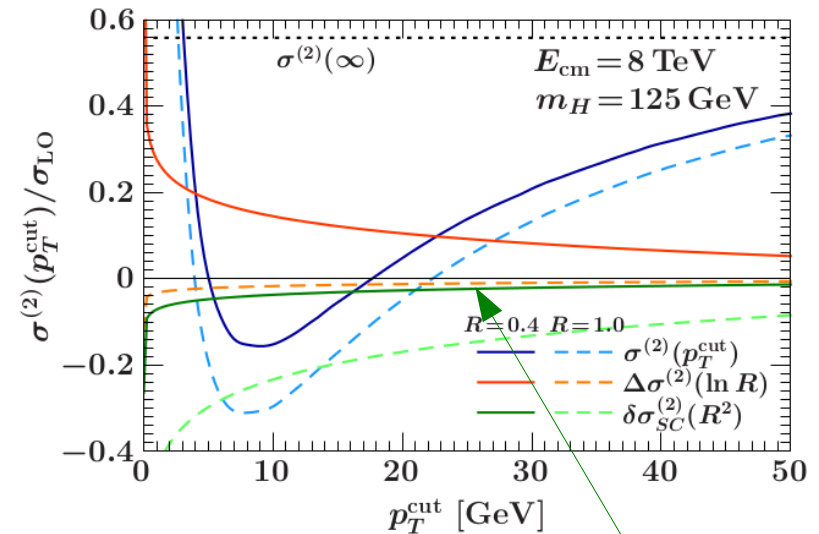
- Real life
  - anti-kT  $R \sim 0.4 - 0.5$
  - pT veto  $p_T^{veto} \sim 25 - 30\text{GeV}$



# Processes with jet vetoes

- Real life

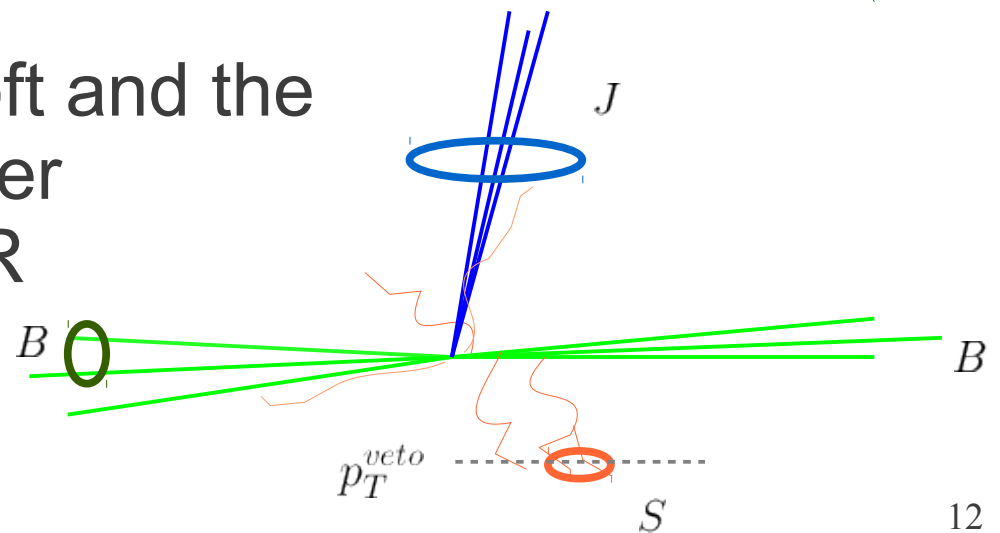
- anti-kT  $R \sim 0.4 - 0.5$
- pT veto  $p_T^{veto} \sim 25 - 30 \text{ GeV}$



- Factorizability

(Becher, Neubert '12, Tackmann, Walsh, Zuberi '12, XL, Petriello '12)

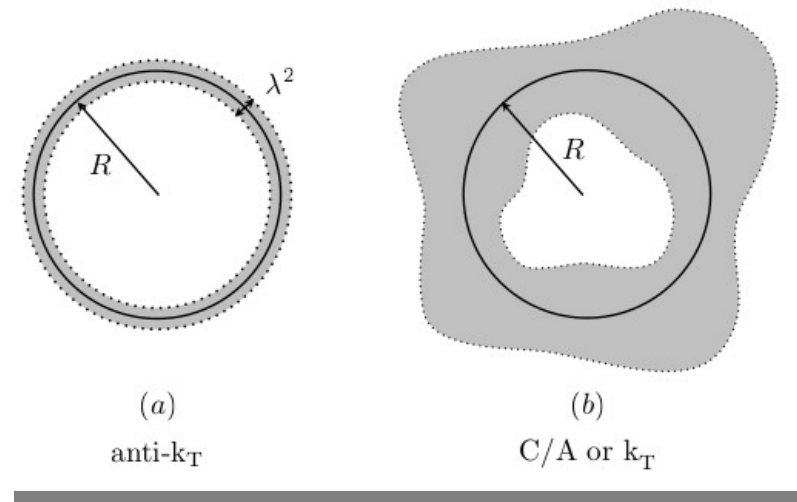
- Mixing between the soft and the beam sectors are power suppressed for small R



# Processes with jet vetoes

- Real life

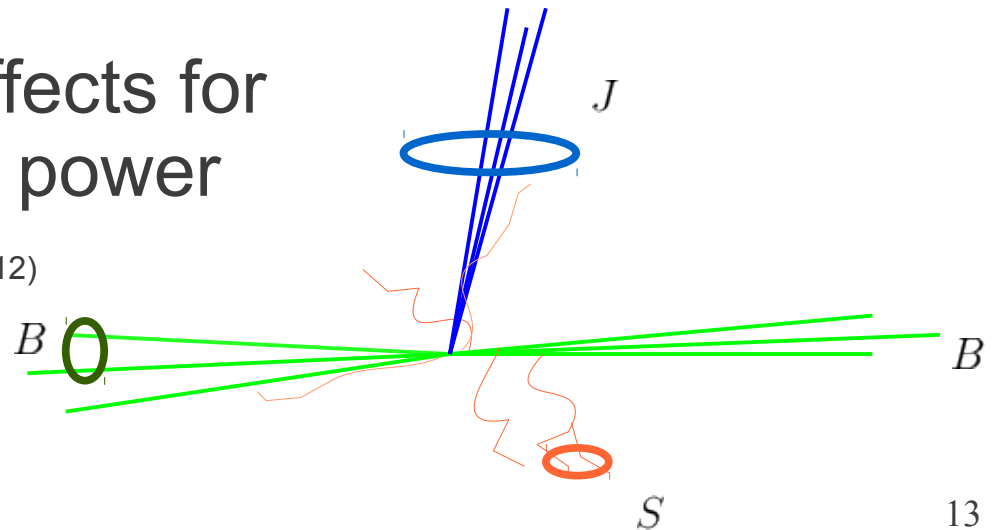
- anti-kT  $R \sim 0.4 - 0.5$
- pT veto  $p_T^{veto} \sim 25 - 30 \text{ GeV}$



- Factorizability (Becher, Neubert '12, Tackmann, Walsh, Zuberi '12, XL, Petriello '12)

- Boundary clustering effects for anti-kT central jets are power suppressed (Kelley, Walsh, Zuberi '12)

$$\rho_{ij} = \min(p_{T,i}^{-1}, p_{T,j}^{-1}) \frac{\Delta R_{ij}}{R}, \quad \rho_i = p_{T,i}^{-1}$$



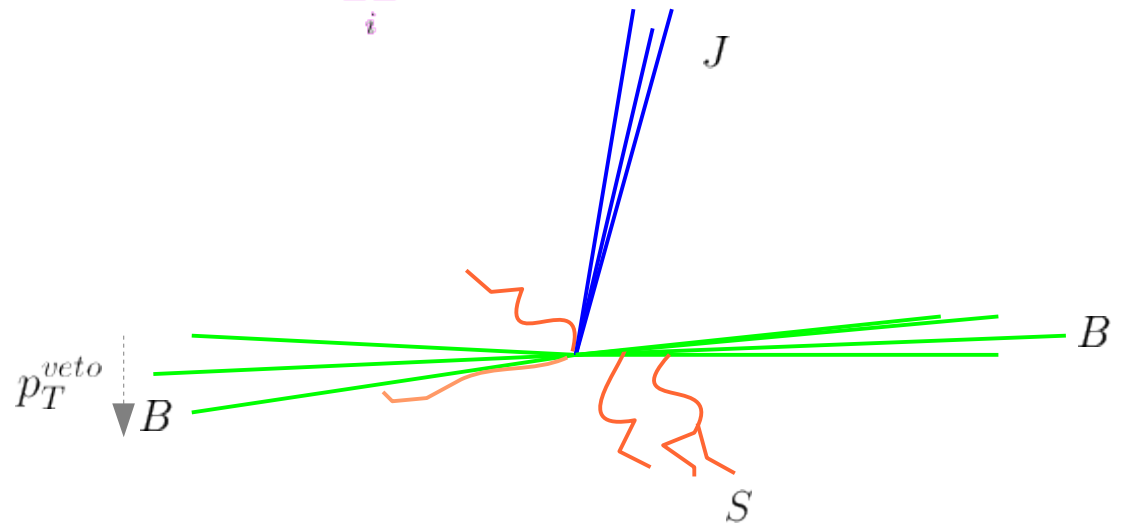
# Processes with jet vetoes

- $N(H/W/Z) + n\text{-j}$

(XL and Petriello, '12, Becher and Neubert, '12 for 0-jet bin)

- Factorization

$$d\sigma = d\Phi_N d\Phi_{J_i} \mathcal{F}(\Phi_N, \Phi_{J_i}) \sum_{a,b} \int dx_a dx_b \frac{1}{2\hat{s}} (2\pi)^4 \delta^4 \left( q_a + q_b - \sum_i^n q_{J_i} - q_N \right) \\ \times \sum_{\text{spin}} \sum_{\text{color}} \text{Tr}(H \cdot S) \mathcal{I}_{a,i_a j_a} \otimes f_{j_a}(x_a) \mathcal{I}_{b,i_b j_b} \otimes f_{j_b}(x_b) \prod_i^n J_{J_i}(R)$$



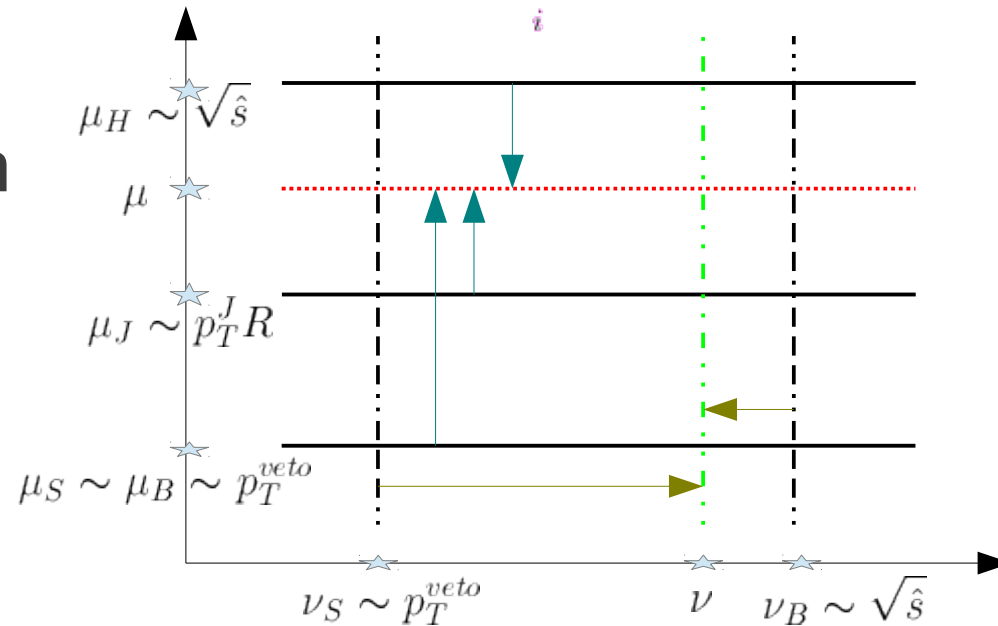
# Processes with jet vetoes

- N(H/W/Z) + n-j (XL and Petriello, '12)

– Factorization

$$d\sigma = d\Phi_N d\Phi_{J_i} \mathcal{F}(\Phi_N, \Phi_{J_i}) \sum_{a,b} \int dx_a dx_b \frac{1}{2\hat{s}} (2\pi)^4 \delta^4 \left( q_a + q_b - \sum_i^n q_{J_i} - q_N \right) \\ \times \sum_{\text{spin}} \sum_{\text{color}} \text{Tr}(H \cdot S) \mathcal{I}_{a,i_a j_a} \otimes f_{j_a}(x_a) \mathcal{I}_{b,i_b j_b} \otimes f_{j_b}(x_b) \prod_i^n J_{J_i}(R)$$

– Resummation



# Processes with jet vetoes

- $N(H/W/Z) + n-j$  (XL and Petriello, '12)

– NLL

$$d\sigma_{\text{NLL}} = \sum_{ab} \int dx_a dx_b \text{Tr} \left[ H_{\text{LO}}^{ab \rightarrow N\{J_i\}}(\mu_H) S U_{H,\{J_i\}}(\mu, \mu_H) U_{S,\{J_i\}}(\mu, \nu, \mu_S, \nu_S) \right] \\ \times f_a(\mu_B, x_a) f_b(\mu_B, x_b) \mathcal{I}_{B,a,b}(\mu, \nu, \mu_B, \nu_B, x_a, x_b) \prod_i \mathcal{R}_{J_i}(\mu, \mu_J, R).$$

- Resummation at the fully differential cross section level
- Very compact analytic expressions (examples in the backup slides)
- Easy to supplement MCFM with these corrections
- Can improve the accuracy systematically



# Processes with jet vetoes

- Other Approach

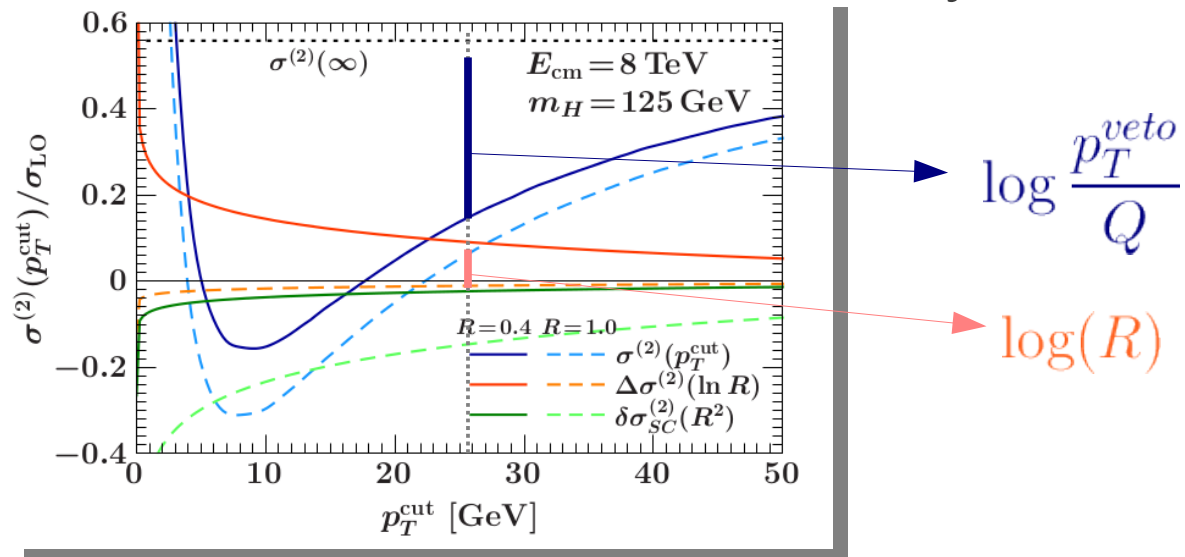
- NNLL+NNLO formula (not fact. thm.) for 0-jet bin

(Banfi, Monni, Salam, Zanderighi, '12)

- Potential Issue

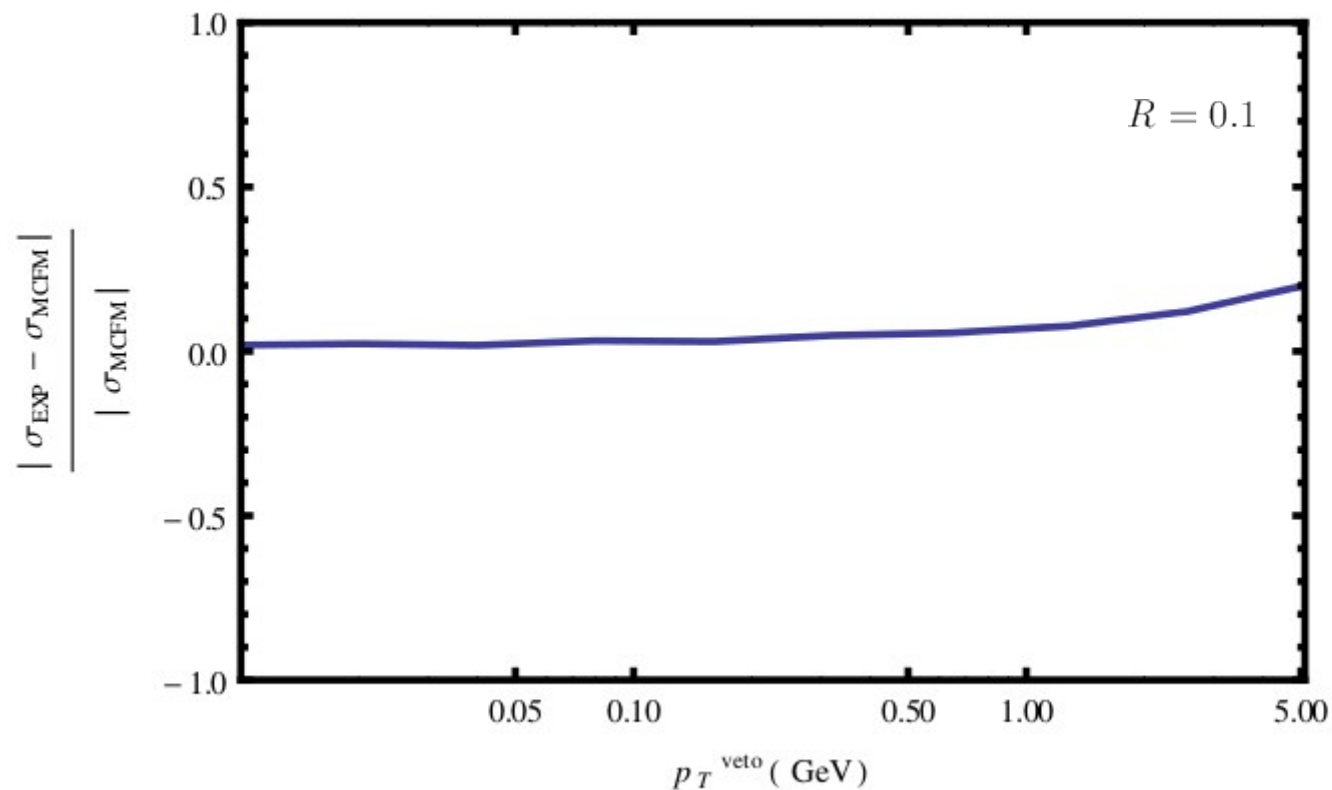
- Clustering Log(R) (Tackmann, Walsh, Zuberi, '12)

- Moderate and well controlled for experimentally interesting R



# Processes with jet vetoes

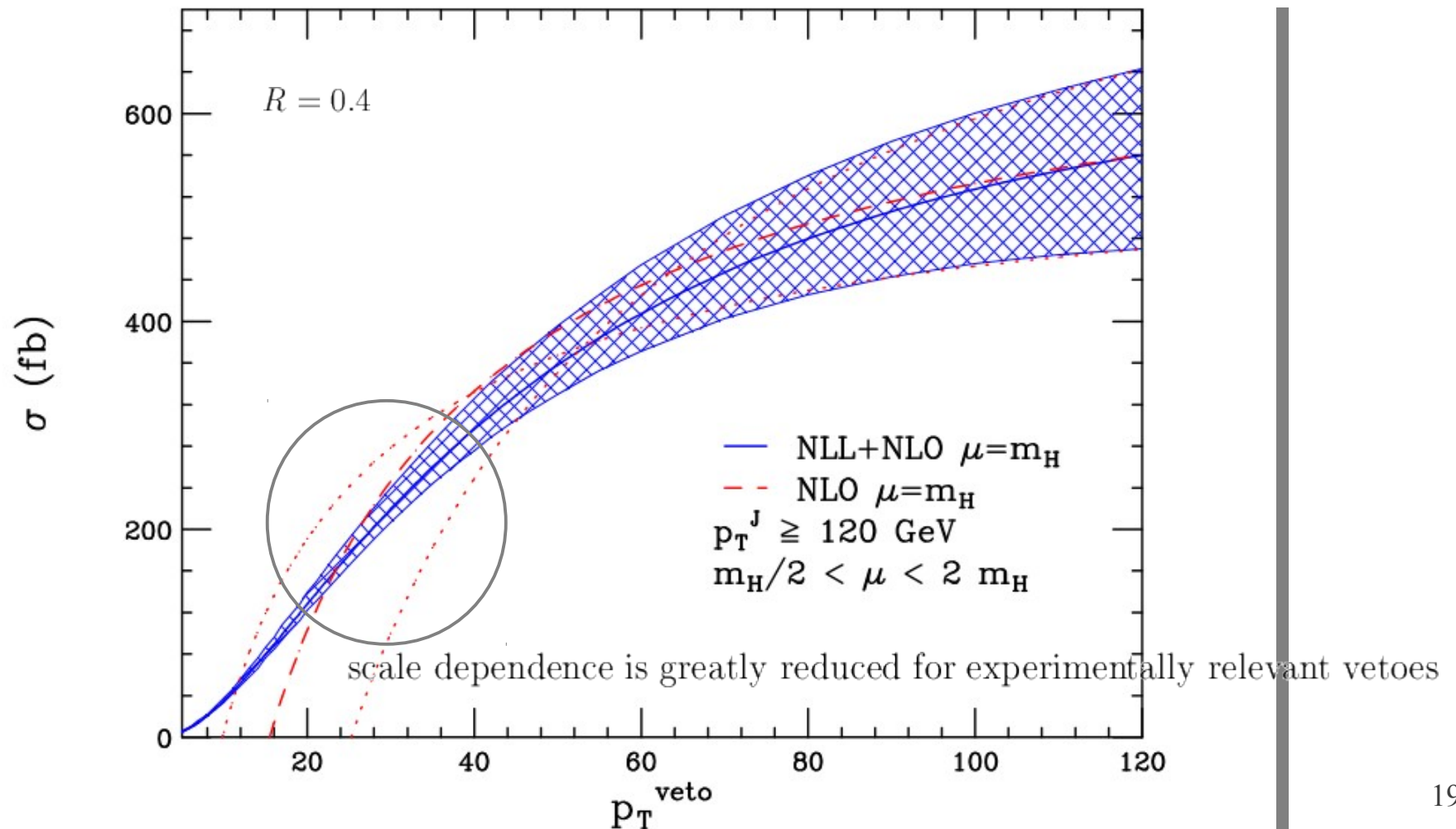
- Higgs + 1-j (XL and Petriello, '12)
  - Catches the NLL structures



# Processes with jet vetoes

- Higgs + 1-j

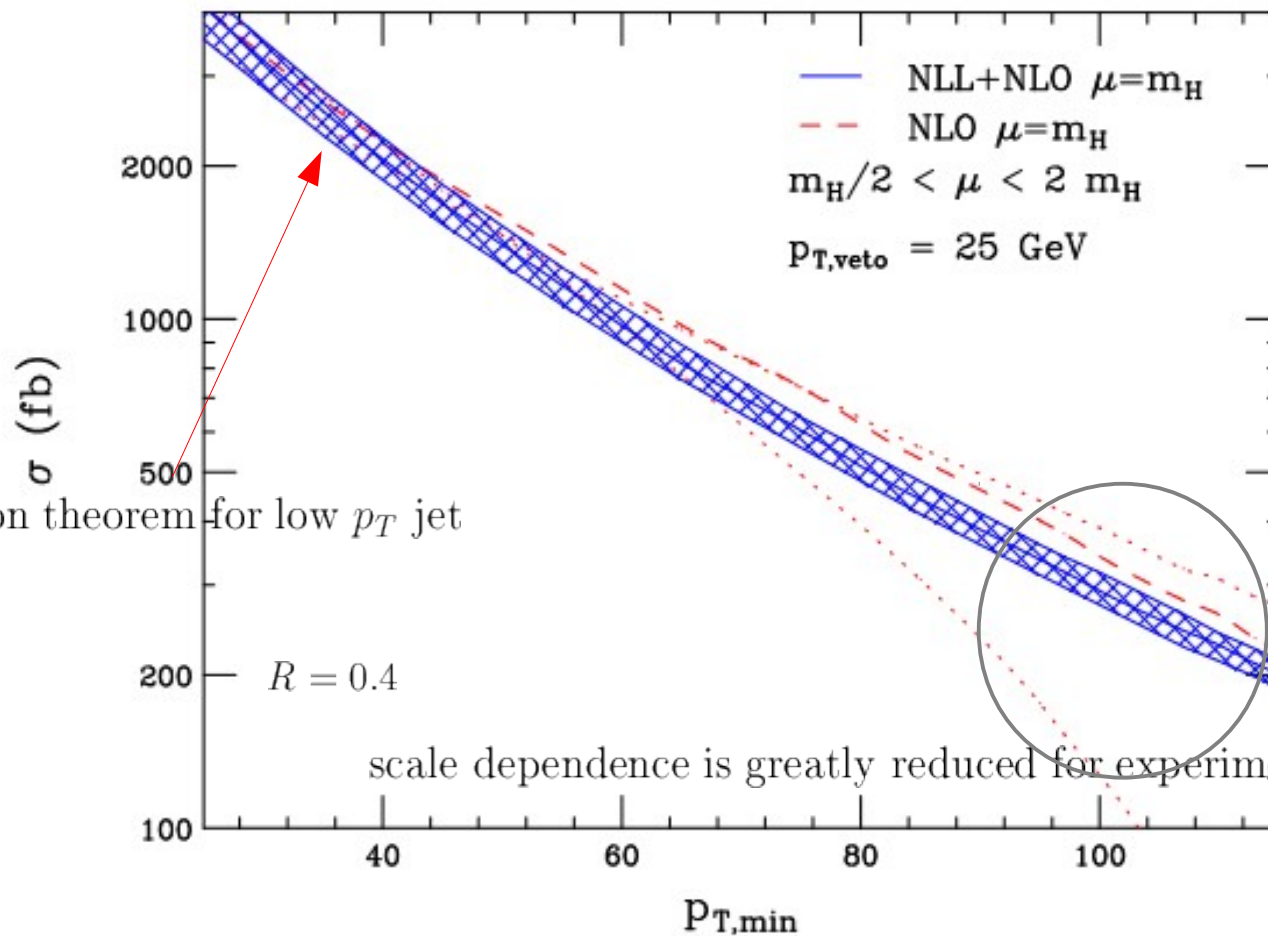
(XL and Petriello, '12)



# Processes with jet vetoes

- Higgs + 1-j

(XL and Petriello, '12)



new factorization theorem for low  $p_T$  jet

$R = 0.4$

scale dependence is greatly reduced for experimentally relevant vetoes

# Conclusion and Outlook

- Resum NLL for exclusive multi-jet events
  - Neat analytic expressions
  - Reliable prediction
  - Reduced scale dependence
- Things to do
  - NLL' (within reach) and beyond
  - Entire spectrum (low jet  $p_T$ )
  - Matching schemes and uncertainties
  - Compare with parton shower

Thanks

# Backup

- Neat expressions

arXiv:1210.1906

$$\mathcal{R}_{J_i} = \exp \left[ -2T_i^2 S(\mu_J, \mu) - A_{J_i}(\mu_J, \mu) \right] \left( \frac{\mu_J}{p_T^{J_i} R} \right)^{-2T_J^2 A_\Gamma(\mu_J, \mu)},$$

For the NLL resummation, we need

$$A_\Gamma(\mu_i, \mu_f) = \frac{\Gamma_0}{2\beta_0} \left\{ \log r + \frac{\alpha_s(\mu_i)}{4\pi} \left( \frac{\Gamma_1}{\Gamma_0} - \frac{\beta_1}{\beta_0} \right) (r - 1) \right\}, \quad (38)$$

and

$$S(\mu_i, \mu_f) = \frac{\Gamma_0}{4\beta_0^2} \left\{ \frac{4\pi}{\alpha_s(\mu_i)} \left( 1 - \frac{1}{r} - \log r \right) + \left( \frac{\Gamma_1}{\Gamma_0} - \frac{\beta_1}{\beta_0} \right) (1 - r + \log r) + \frac{\beta_1}{2\beta_0} \log^2 r \right\}, \quad (39)$$

# Backup

- Log counting

	matching (singular)	nonsingular	$\gamma_x$	$\Gamma_{\text{cusp}}$	$\beta$	PDF
LO	LO	LO	-	-	1-loop	LO
NLO	NLO	NLO	-	-	2-loop	NLO
NNLO	NNLO	NNLO	-	-	3-loop	NNLO
LL	LO	-	-	1-loop	1-loop	LO
NLL	LO	-	1-loop	2-loop	2-loop	LO
NNLL	NLO	-	2-loop	3-loop	3-loop	NLO
NLL'+NLO	NLO	NLO	1-loop	2-loop	2-loop	NLO
NNLL+NNLO	(N)NLO	NNLO	2-loop	3-loop	3-loop	NNLO
NNLL'+NNLO	NNLO	NNLO	2-loop	3-loop	3-loop	NNLO
N <sup>3</sup> LL+NNLO	NNLO	NNLO	3-loop	4-loop	4-loop	NNLO

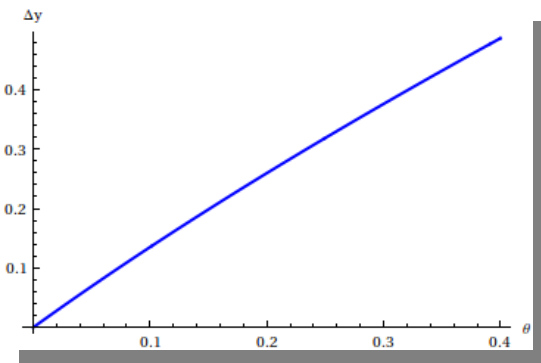
Table from Berger, Marcantonini, Stewart, Tackmann and Waalewijn '11



# Backup

- Q
  - Why the clustering between the soft and the central collinear radiations is not a problem?

- A
  - The clustering does NOT depend on how the collinear mode splits



small  $\theta \rightarrow$  small  $\Delta y$

$$d_{SC_i} \sim d_{SC_j} \sim d_{SJ}$$

# Backup

- Q
  - Why the clustering between the soft and the beam collinear radiations is a problem?
- A
  - The clustering DOES depend on how the beam mode splits

