

Modern event generators for LHC physics

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SLAC NAL Theory Group



West Coast ATLAS Forum



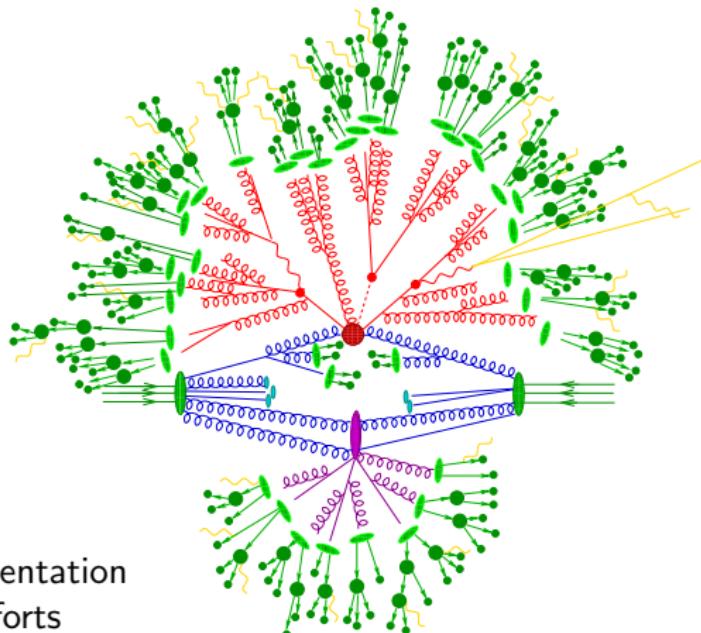
SLAC, 09/15/12

Structure of the simulation

- Hard interaction
- QCD evolution
- Secondary hard interactions
- Jet fragmentation
- Hadron decays
- Higher-order QED corrections

Much recent progress on hard QCD
Benefits from “NLO revolution”

Improved models for MPI and fragmentation
Combined with systematic tuning efforts



Three general-purpose tools with slightly different structure and emphasis

Herwig

- Originated in coherent shower studies → angular ordered PS
- Front-runner in development of Mc@NLO and POWHEG
- Simple in-house ME generator & spin-correlated decay chains
- Original framework for cluster fragmentation

Pythia

- Originated in hadronization studies → Lund string
- Leading in development of multiple interaction models
- Pragmatic attitude to ME generation → external tools
- Extensive PS development and earliest ME \otimes PS matching

Sherpa

- Started with PS generator APACIC++ & ME generator AMEGIC++
- Current MPI model and hadronization pragmatic add-ons
- Leading in development of automated ME \otimes PS merging
- Automated framework for NLO calculations and Mc@NLO

For more information, check out [Buckley et al.] arXiv:1101.2599

For updates and news, go to <http://www.montecarlonet.org>



Rivet [Buckley et al.] arXiv:0103.0694

- LHC-successor to HZTool
Collection of exp. data & matching analysis routines
- Spirit: “Right MC describes everything at the same time”

Professor [Buckley et al.] arXiv:0907.2973

- Tuning in multi-dimensional parameter space of MC
- Generate event samples at random parameter points
Analyse them with Rivet
Parameterize observables
Minimize χ^2 and cross-check

Tune comparisons

Deviation metrics per gen/tune and observable group:

| Gen | Tune | UE | Dijets | Multijets | Jet shapes | W and Z | Fragmentation | B frag |
|----------|------------------------|------|--------|-----------|------------|---------|---------------|--------|
| AlpGen | HERWIG6 | — | 1.83 | 5.36 | 2.48 | 0.91 | — | — |
| | PYTHIA6-AMBT1 | — | 1.55 | 2.80 | 0.61 | 0.53 | — | — |
| | PYTHIA6-D6T | — | 1.38 | 2.67 | 2.31 | 1.67 | — | — |
| | PYTHIA6-P2010 | — | 1.09 | 2.65 | 2.03 | 1.48 | — | — |
| | PYTHIA6-P2011 | — | 1.12 | 2.60 | 0.48 | 0.24 | — | — |
| | PYTHIA6-Z2 | — | 1.48 | 2.63 | 0.55 | 0.48 | — | — |
| | PYTHIA6-profQ2 | — | 1.16 | 2.65 | 1.43 | 1.29 | — | — |
| HERWIG | AUET2-CTEQ6L1 | 0.43 | 0.55 | 0.77 | 0.35 | 0.58 | 22.80 | 2.38 |
| | AUET2-LOxx | 0.25 | 0.71 | 0.60 | 0.39 | 0.88 | 22.13 | 2.29 |
| Herwig++ | 2.5.1-UE-EE-3-CTEQ6L1 | 0.27 | 0.87 | 0.78 | 0.51 | 0.98 | 10.58 | 1.32 |
| | 2.5.1-UE-EE-3-MRSTLOxx | 0.23 | 1.05 | 0.78 | 0.50 | 0.65 | 10.58 | 1.32 |
| PYTHIA6 | AMBT1 | 0.39 | 1.20 | 0.54 | 0.77 | 0.27 | 0.93 | 1.65 |
| | AUET2B-CTEQ6L1 | 0.16 | 0.92 | 0.44 | 0.59 | 0.74 | 0.67 | 1.29 |
| | AUET2B-LOxx | 0.13 | 1.33 | 0.55 | 0.58 | 1.15 | 0.67 | 1.30 |
| | D6T | 0.58 | 0.79 | 0.50 | 0.56 | 1.25 | 0.36 | 2.63 |
| | DW | 0.81 | 0.78 | 0.61 | 0.56 | 1.33 | 0.36 | 2.63 |
| | P2010 | 0.30 | 0.93 | 0.82 | 1.07 | 0.30 | 0.44 | 1.75 |
| | P2011 | 0.12 | 0.89 | 0.67 | 1.02 | 0.53 | 0.43 | 2.13 |
| Pythia8 | ProfQ2 | 0.51 | 0.67 | 0.81 | 0.51 | 0.64 | 0.30 | 1.65 |
| | Z2 | 0.18 | 0.94 | 0.73 | 0.80 | 0.30 | 0.95 | 2.78 |
| Sherpa | 4C | 0.30 | 0.97 | 0.93 | 0.50 | 0.90 | 0.38 | 1.12 |
| Sherpa | 1.3.1 | 0.68 | 0.47 | 0.34 | 0.71 | 0.36 | 0.75 | 2.48 |

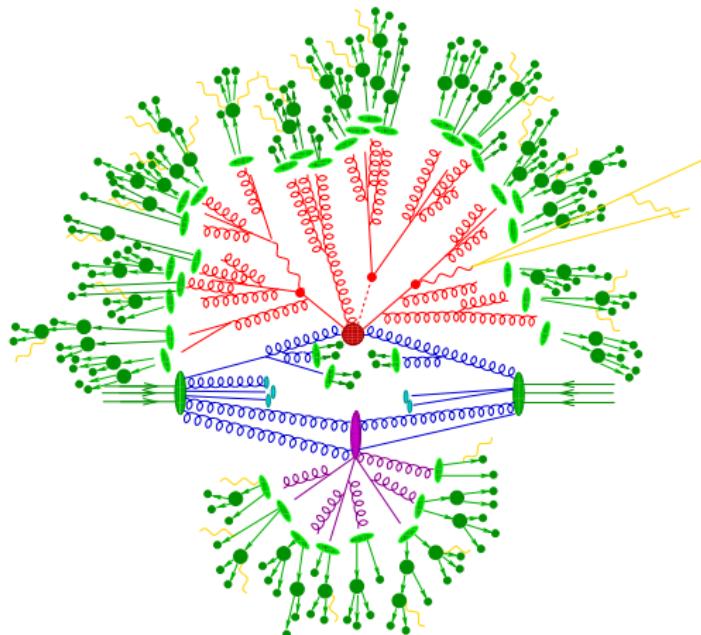
[LH'11 SM WG] arXiv:1203.6803

<http://rivet.hepforge.org/tunecmp/>

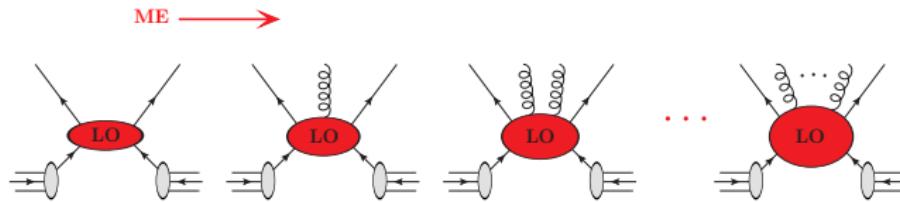


Structure of the simulation

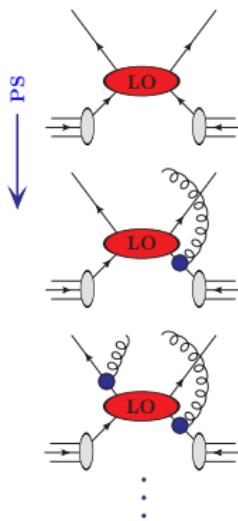
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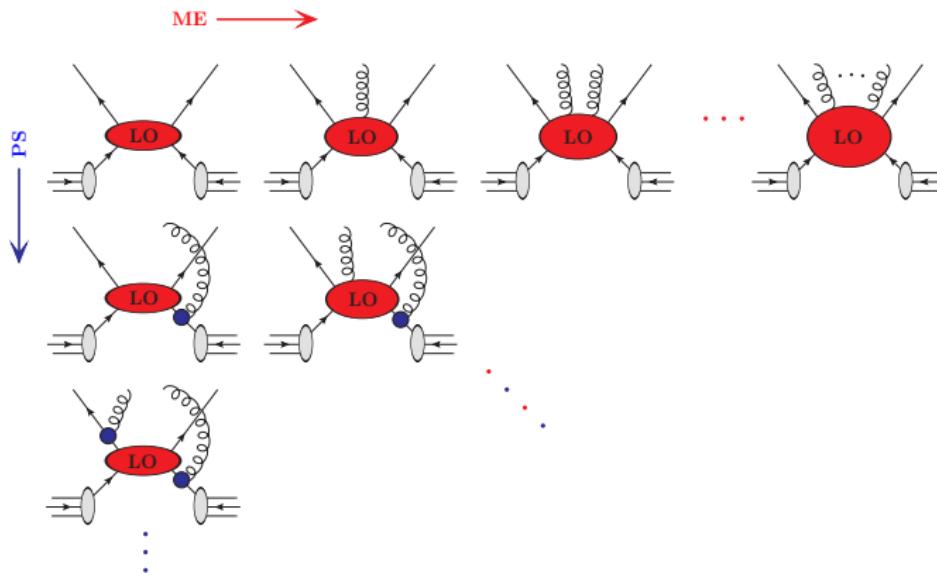
LO matrix elements



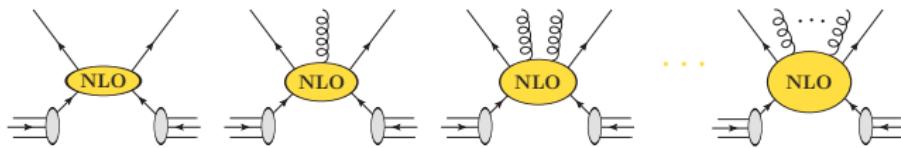
Parton showers

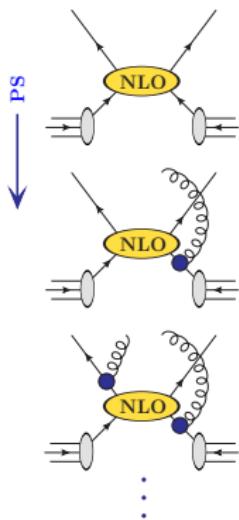


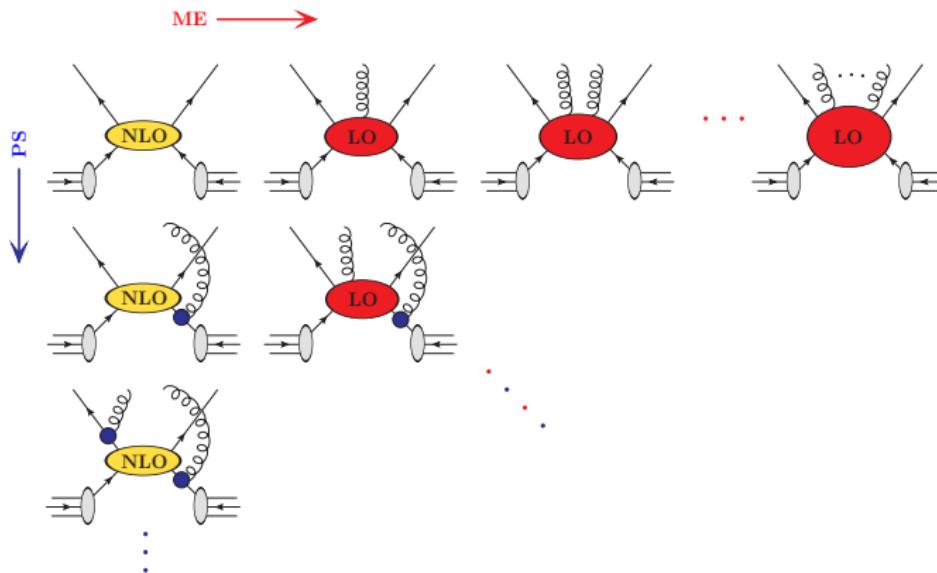
Matrix-element parton-shower merging (ME \otimes PS)



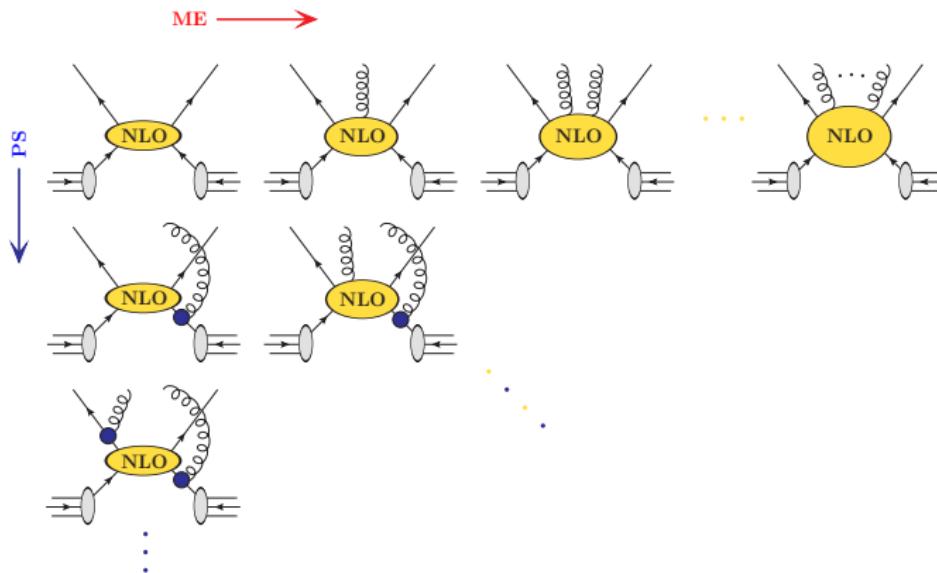
NLO matrix elements

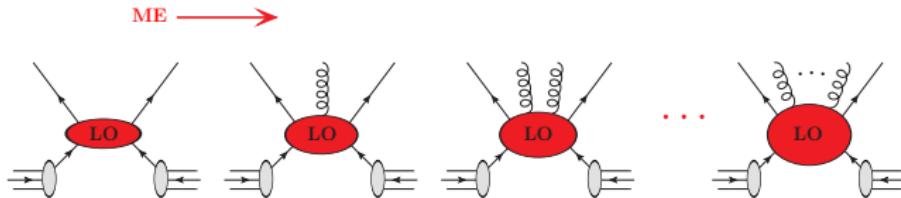


NLO matrix-element parton-shower matching

ME \otimes PS combined with matching (MENLOPS)

Matrix-element parton-shower merging at NLO (ME \otimes PS@NLO)





Plethora of tree-level tools on market
State of the art: Full automation

• Feynman diagrams

- AMEGIC++ [Krauss et al.] hep-ph/0109036
- CompHEP [Boos et al.] hep-ph/0403113
- MADGRAPH [Alwall et al.] arXiv:1106.0522

• Recursive techniques

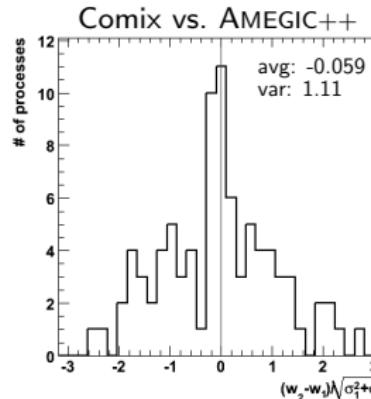
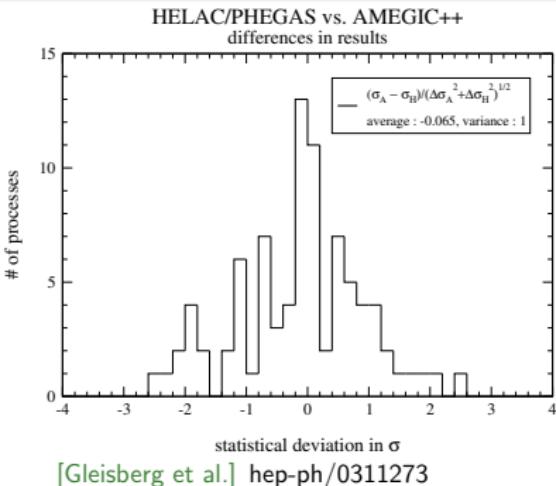
- Comix [Gleisberg,SH] arXiv:0808.3674
- HELAC [Kanaki,Papadopoulos] hep-ph/0002082
- O'Mega [Moretti,Ohl,Reuter] hep-ph/0102195

• α -algorithm

- ALPGEN [Mangano et al.] hep-ph/0206293

LHEF output for passing events
to external MC HERWIG++ & PYTHIA

Useful plugins for NLO calculation
→ Born, real emission & subtraction

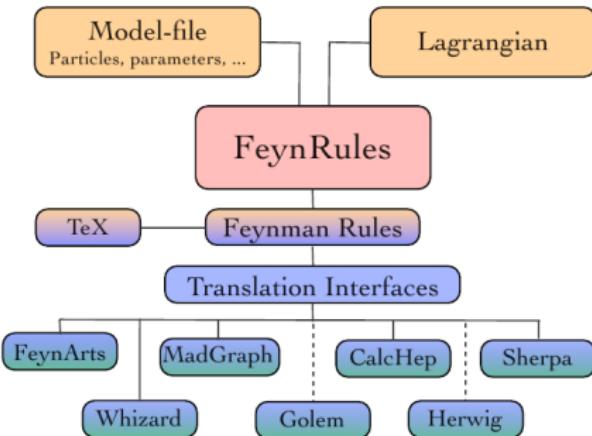


Tree-level ME generators suited for any physics model, but implementing Feynman rules tedious and error-prone

Automated by FeynRules

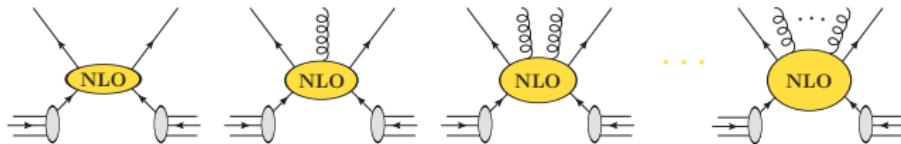
[Christensen,Duhr] arXiv:0806.4194

- Extract vertices from Lagrangian based on minimal information about particle content
- Write ME-generator specific output → universality and cross-checks



Recent developments include:

- UFO** [Degrande,Duhr,Fuks,Grellscheid,Mattelaer,Reiter] arXiv:1108.2040
Model files and Feynman rules → self-contained Python library
- ALOHA** [deAquino,Link,Maltoni,Mattelaer,Stelzer] arXiv:1108.2041 → MADGRAPH
Automated implementation of arbitrary higher-dimensional operators
- Spin-3/2 particles and superfield formalism



$$\text{NLO prediction} \left\{ \begin{array}{l} B = \text{diagram with two external lines and one internal loop} \\ V = \sum 2 \operatorname{Re} \left\{ \text{diagram with two external lines and one internal loop} \right\} \\ R = \sum \text{diagram with two external lines and one internal loop} \end{array} \right.$$

Singularities in V & R to be removed before MC-integration

$$\sigma^{NLO} = \int d\Phi_B (B + \tilde{V}) + \int d\Phi_R R = \int d\Phi_B \left[(B + \tilde{V} + I) + \int d\Phi_{R|B} (R - S) \right]$$

Commonly used subtraction techniques:

- **Dipole method** [Catani,Seymour] hep-ph/9605323
[Catani,Dittmaier,Seymour,Trocsanyi] hep-ph/0201036, implemented in

- AMEGIC++ [Gleisberg,Krauss] arXiv:0709.2881, Comix [SH] colorful
- HELAC/PHEGAS [Czakon,Papadopoulos,Worek] arXiv:0905.0883 polarized
- MADDIPOLE [Frederix,Gehrmann,Greiner] arXiv:0808.2128, arXiv:1004.2905

- **FKS method** [Frixione,Kunszt,Signer] hep-ph/9512328, implemented in

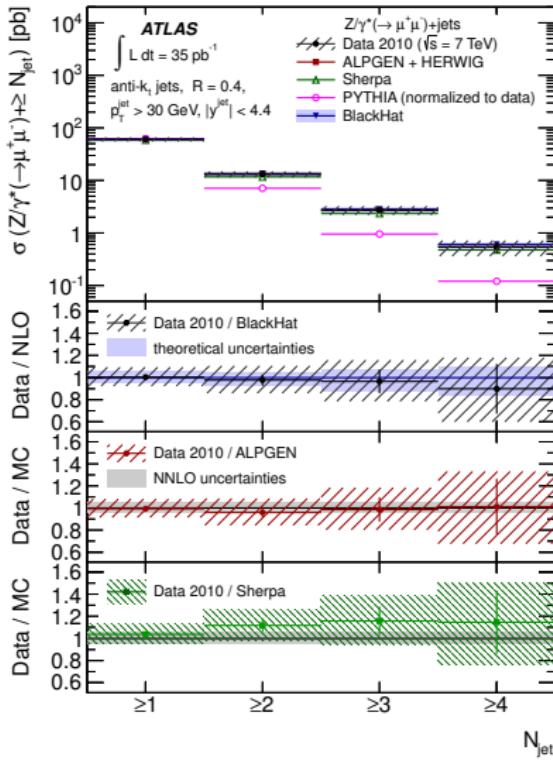
- MADFKS [Frederix,Frixione,Maltoni,Stelzer] arXiv:0908.4272

Several other implementations, which are not part of automated tree-level tools

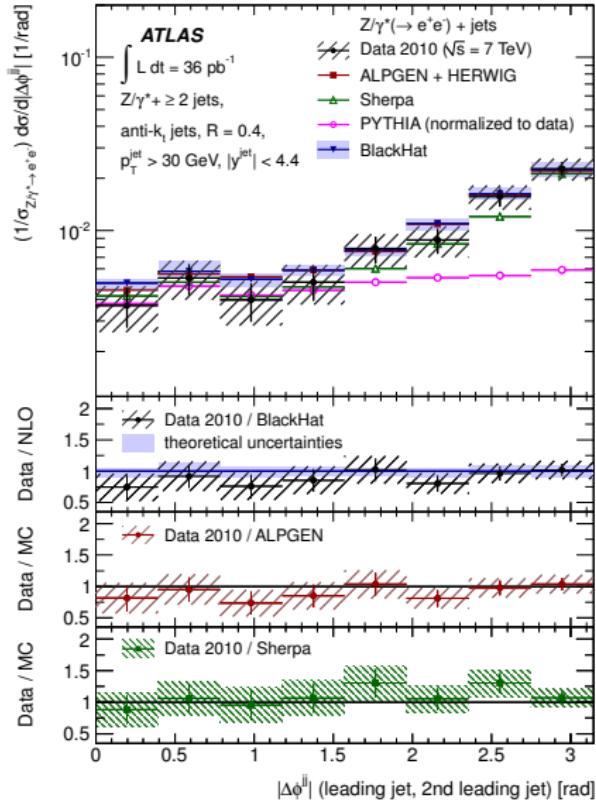
Many (semi-)automated programs to compute virtual
Based on different techniques for loop integration

- **Tensor reduction** [Denner,Dittmaier] hep-ph/0509141
[Binoth,Guillet,Pilon,Heinrich,Schubert] hep-ph/0504267
 - Golem95 [Binoth,Cullen,Greiner,Guffanti,Guillet,Heinrich,Karg,Kauer,Reiter,Reuter]
 - MadGolem [Binoth,Goncalves Netto,Lopez-Val,Mawatari,Plehn,Wigmore]
 - OpenLoops [Cascioli,Maierhöfer,Pozzorini]
- **Generalized unitarity** [Bern,Dixon,Dunbar,Kosower] hep-ph/9409265 hep-ph/9708239
[Ossola,Papadopoulos,Pittau] hep-ph/0609007, [Forde] arXiv:0704.1835
 - BlackHat [Bern,Dixon,Febres-Cordero,Ita,Kosower,Maître,Ozeren,SH]
 - GoSam [Cullen,Greiner,Heinrich,Luisoni,Mastrolia,Ossola,Reiter,Tramontano]
 - HelacNLO [Bevilacqua,Czakon,Garzelli,vanHameren,Kardos,Papadopoulos,Pittau,Worek]
 - MadLoop [Hirschi,Frerix,Frixione,Garzelli,Maltoni,Pittau]
 - NJet [Badger,Biedermann,Uwer,Yundin]
 - OpenLoops [Cascioli,Maierhöfer,Pozzorini]
 - Rocket [Ellis,Giele,Kunszt,Melnikov,Zanderighi]
- **Numerical integration** [Becker,Goetz,Reuschle,Schwan,Weinzierl] arXiv:1111.1733

Combination of BlackHat and SHERPA is pushing limits



[ATLAS] arXiv:1111.2690

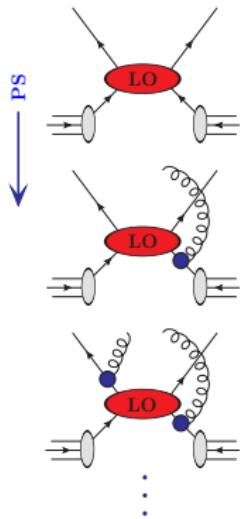


Fully automated NLO predictions with **MadLoop**

[Hirschi et al.] arXiv:1103.0621

| Process | μ | n_{lf} | LO | NLO |
|--|--------------|----------|---------------------------|-------------------------|
| a.1 $pp \rightarrow t\bar{t}$ | m_t | 5 | 123.76 ± 0.05 | 162.08 ± 0.12 |
| a.2 $pp \rightarrow tj$ | m_t | 5 | 34.78 ± 0.03 | 41.03 ± 0.07 |
| a.3 $pp \rightarrow t\bar{j}j$ | m_t | 5 | 11.851 ± 0.006 | 13.71 ± 0.02 |
| a.4 $pp \rightarrow t\bar{b}j$ | $m_t/4$ | 4 | 25.62 ± 0.01 | 30.96 ± 0.06 |
| a.5 $pp \rightarrow t\bar{b}jj$ | $m_t/4$ | 4 | 8.195 ± 0.002 | 8.91 ± 0.01 |
| b.1 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e$ | m_W | 5 | 5072.5 ± 2.9 | 6146.2 ± 9.8 |
| b.2 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e j$ | m_W | 5 | 828.4 ± 0.8 | 1065.3 ± 1.8 |
| b.3 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e jj$ | m_W | 5 | 298.8 ± 0.4 | 300.3 ± 0.6 |
| b.4 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^-$ | m_Z | 5 | 1007.0 ± 0.1 | 1170.0 ± 2.4 |
| b.5 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- j$ | m_Z | 5 | 156.11 ± 0.03 | 203.0 ± 0.2 |
| b.6 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- jj$ | m_Z | 5 | 54.24 ± 0.02 | 56.69 ± 0.07 |
| c.1 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e b\bar{b}$ | $m_W + 2m_b$ | 4 | 11.557 ± 0.005 | 22.95 ± 0.07 |
| c.2 $pp \rightarrow (W^+ \rightarrow) e^+ \nu_e t\bar{t}$ | $m_W + 2m_t$ | 5 | 0.009415 ± 0.000003 | 0.01159 ± 0.00001 |
| c.3 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- b\bar{b}$ | $m_Z + 2m_b$ | 4 | 9.459 ± 0.004 | 15.31 ± 0.03 |
| c.4 $pp \rightarrow (\gamma^*/Z \rightarrow) e^+ e^- t\bar{t}$ | $m_Z + 2m_t$ | 5 | 0.0035131 ± 0.0000004 | 0.004876 ± 0.000002 |
| c.5 $pp \rightarrow \gamma t\bar{t}$ | $2m_t$ | 5 | 0.2906 ± 0.0001 | 0.4169 ± 0.0003 |
| d.1 $pp \rightarrow W^+ W^-$ | $2m_W$ | 4 | 29.976 ± 0.004 | 43.92 ± 0.03 |
| d.2 $pp \rightarrow W^+ W^- j$ | $2m_W$ | 4 | 11.613 ± 0.002 | 15.174 ± 0.008 |
| d.3 $pp \rightarrow W^+ W^+ jj$ | $2m_W$ | 4 | 0.07048 ± 0.00004 | 0.1377 ± 0.0005 |
| e.1 $pp \rightarrow HW^+$ | $m_W + m_H$ | 5 | 0.3428 ± 0.0003 | 0.4455 ± 0.0003 |
| e.2 $pp \rightarrow HW^+ j$ | $m_W + m_H$ | 5 | 0.1223 ± 0.0001 | 0.1501 ± 0.0002 |
| e.3 $pp \rightarrow HZ$ | $m_Z + m_H$ | 5 | 0.2781 ± 0.0001 | 0.3659 ± 0.0002 |
| e.4 $pp \rightarrow HZ j$ | $m_Z + m_H$ | 5 | 0.0988 ± 0.0001 | 0.1237 ± 0.0001 |
| e.5 $pp \rightarrow Ht\bar{t}$ | $m_t + m_H$ | 5 | 0.08896 ± 0.00001 | 0.09869 ± 0.00003 |
| e.6 $pp \rightarrow Hb\bar{b}$ | $m_b + m_H$ | 4 | 0.16510 ± 0.00009 | 0.2099 ± 0.0006 |
| e.7 $pp \rightarrow Hjj$ | m_H | 5 | 1.104 ± 0.002 | 1.036 ± 0.002 |

Parton showers



Parton showers are defined by

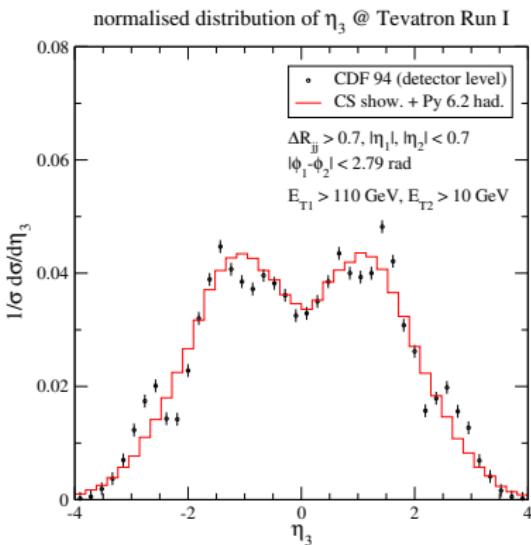
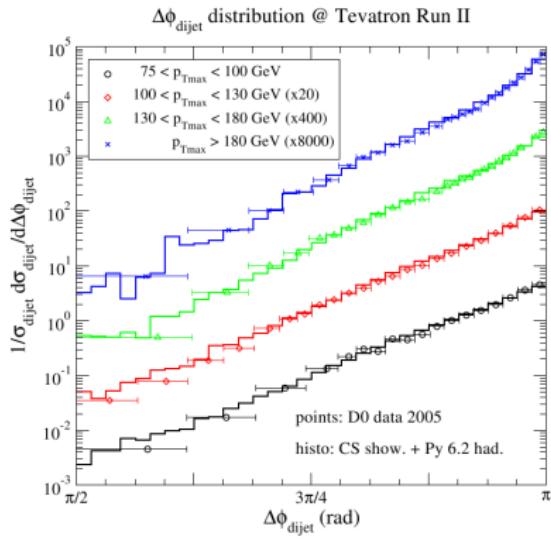
- Evolution & splitting variable
- Momentum mapping (recoil scheme)
- Splitting kernels

Publicly available programs and their characteristics:

| | Evolution variable | Splitting variable | Coherence |
|--------------------------|-----------------------|--------------------|--------------------------|
| Ariadne | dipole- k_{\perp}^2 | Rapidity | $2 \rightarrow 3$ kernel |
| Herwig | $E^2 \theta^2$ | Energy fraction | AO |
| Herwig++ | $(t - m^2)/z(1 - z)$ | LC mom fraction | AO |
| Pythia 6.x | t | Energy fraction | Enforced |
| Pythia 8 | k_{\perp}^2 | LC mom fraction | Enforced |
| Sherpa 1.1.x | t | Energy fraction | Enforced |
| Sherpa 1.2.x (Vincia) | dipole- k_{\perp}^2 | LC mom fraction | $2 \rightarrow 3$ kernel |
| | dipole- k_{\perp}^2 | LC mom fraction | $2 \rightarrow 3$ kernel |

[Krauss,Schumann] arXiv:0709.1027

New PS developments based on Catani-Seymour subtraction formalism
 Few model ambiguities, excellent approximation of higher-order real ME

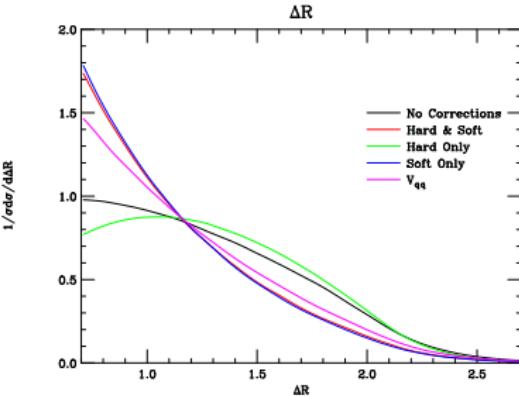
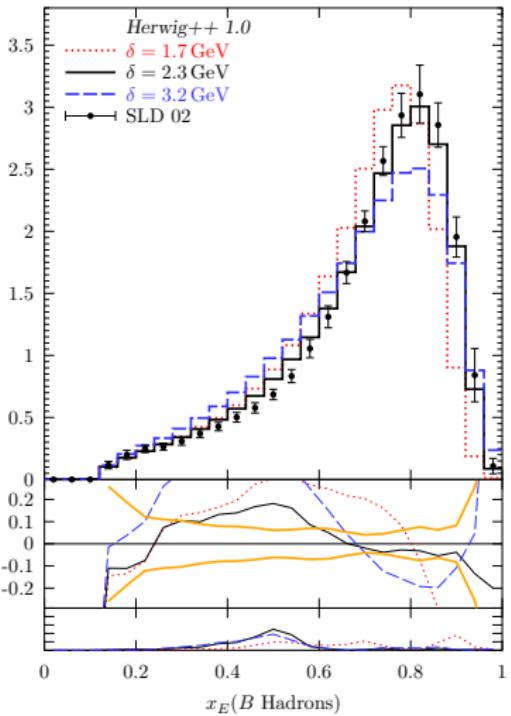


[Gieseke et al.] hep-ph/0311208

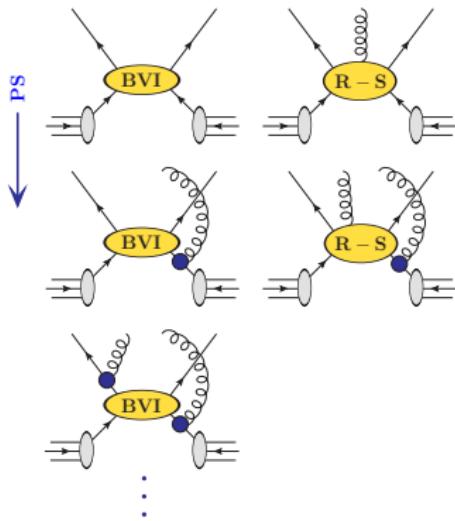
[Hamilton,Richardson] hep-ph/0612236

Many (not so recent) improvements on heavy flavor treatment in HERWIG++

- Reduction of dead region
- ME correction in $t \rightarrow Wb$ decays
- Extended quasi-collinear splitting functions



Matching NLO and PS



[Frixione,Webber] hep-ph/0204244

Differential event rate to $\mathcal{O}(\alpha_s)$ in PS

$$\frac{d\sigma_{\text{PS}}}{d\Phi_n} = B_n \left[\Delta_n^{(K)}(t_c, \mu_Q^2) + \int_{t_c}^{\mu_Q^2} d\Phi_1 K_n \Delta_n^{(K)}(t(\Phi_1), \mu_Q^2) \right]$$

 K_n - sum of PS kernels for n -parton final state**Make this NLO-correct:**

- Radiation pattern from ME corrected PS
Correction weight $w_n = D_n^{(A)} / B_n K_n$, where $D_n^{(A)} \rightarrow$ dipole term
- Replace $B \rightarrow \bar{B}^{(A)} = B + \tilde{V} + I + \int d\Phi_1 (D^{(A)} - S)$
- Add hard remainder function $\int d\Phi_R H^{(A)}$, where $H^{(A)} = [R - D^{(A)}]$

Differential event rate to $\mathcal{O}(\alpha_s)$ in matched calculation

$$\frac{d\sigma_{\text{NLOPS}}}{d\Phi_n} = \bar{B}_n^{(A)} \left[\Delta_n^{(A)}(t_c) + \int_{t_c}^{\mu_Q^2} d\Phi_1 \frac{D_n^{(A)}}{B_n} \Delta_n^{(A)}(t(\Phi_1)) \right] + \int d\Phi_1 H_n^{(A)}$$

MC@NLO and POWHEG differ only in choice of $D^{(A)}$

Method 1

[Frixione,Webber] hep-ph/0204244

- Original algorithm formulated such that $D_n^{(A)} \rightarrow D_n^{(K)} = B_n K_n$,
i.e. modified subtraction carried out with parton-shower approximation
- Exact only in collinear region
Missing subleading colour terms in single-logarithmic divergences
- Solved by smoothly fading out real-emission correction in singly-soft region
Need to correct for mismatch, but only affects unresolved gluons anyhow

Method 2

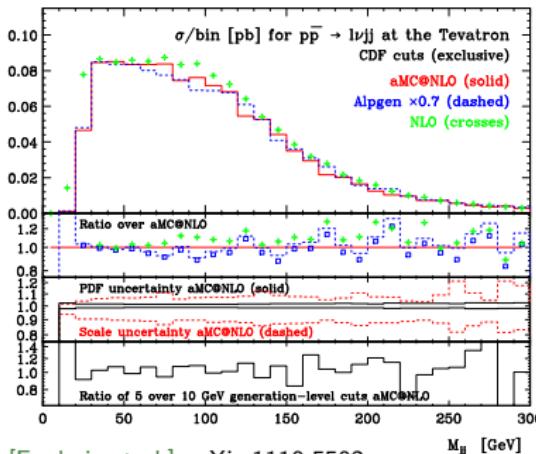
[SH,Krauss,Schönherr,Siegert] arXiv:1111.1220

- Alternative solution employs $D_n^{(A)} \rightarrow D_n^{(S)} = S_n$
i.e. parton-shower evolution performed with NLO subtraction terms
- Leads to non-probabilistic Sudakov factor $\Delta_n^{(S)}$
Requires modification of veto algorithm
- Exact cancellation of all divergences without additional smoothing
Equivalent to one-step full colour parton shower algorithm

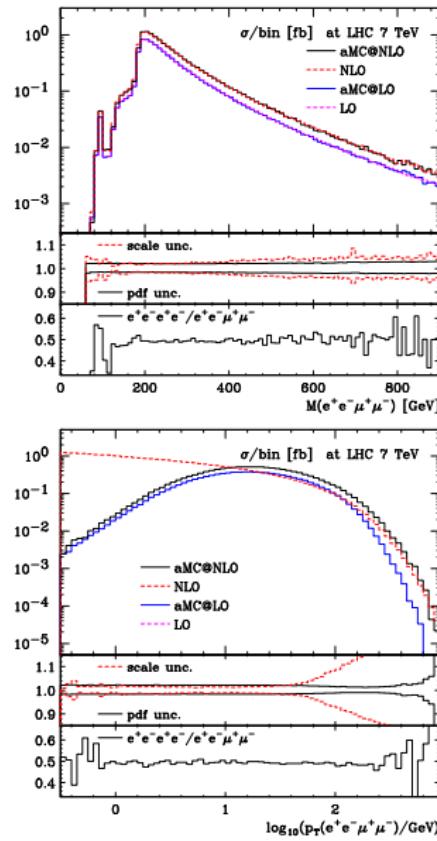
Method 1 automated in aMc@NLO

Using MADFKS subtraction and fHERWIG PS
Framework for convenient uncertainty estimate

- $t\bar{t}h$ arXiv:1104.5613
- 4 leptons arXiv:1110.4738
- $W^\pm + 2$ jets arXiv:1110.5502



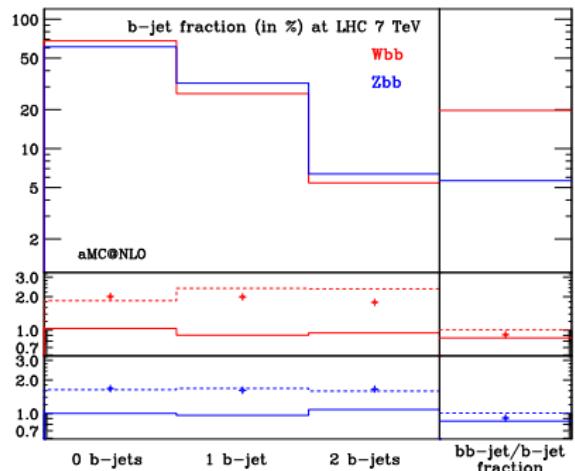
[Frederix et al.] arXiv:1110.5502



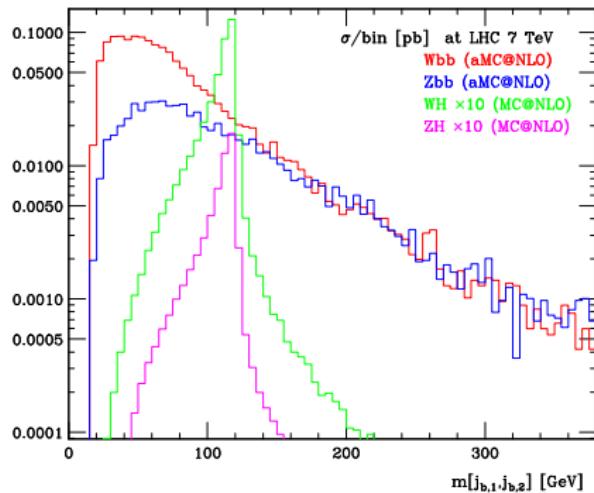
[Frederix et al.] arXiv:1110.4738

Method 1 automated in aMc@NLO

Applied to Vbb in 4-flavor scheme

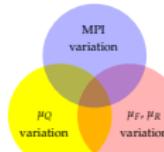
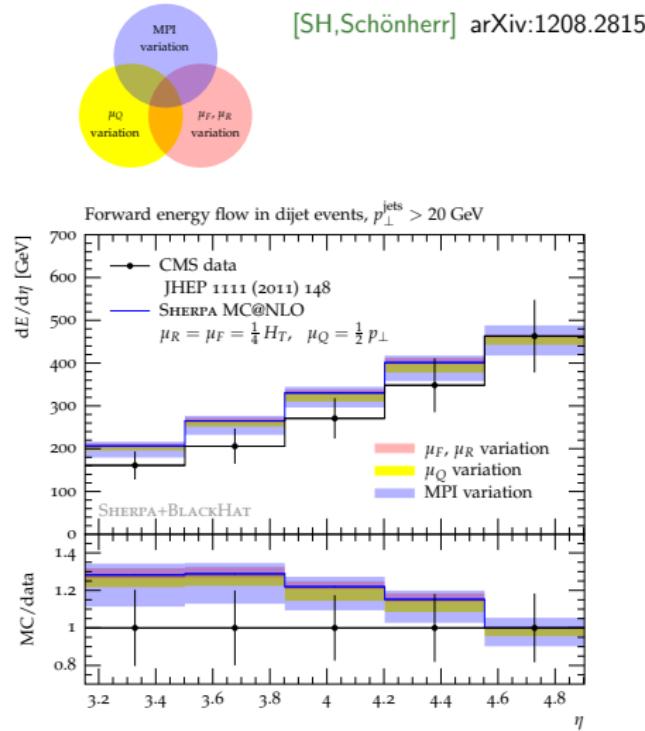
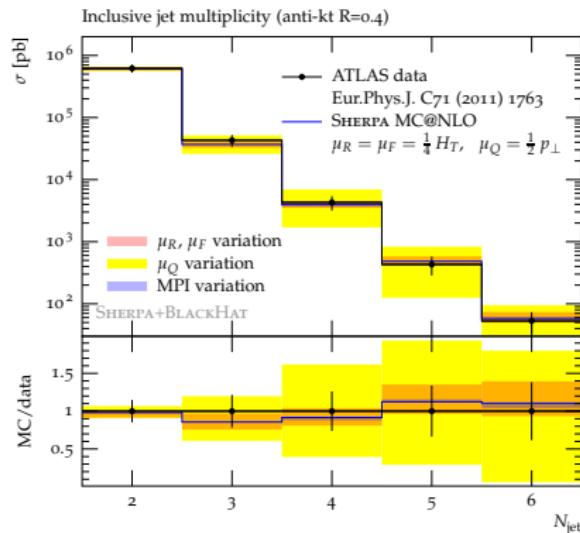


[Fredrix et al.] arXiv:1106.6019



Method 2 automated in SHERPA

Allows to determine fixed-order
and resummation scale uncertainty



[SH,Schönherr] arXiv:1208.2815

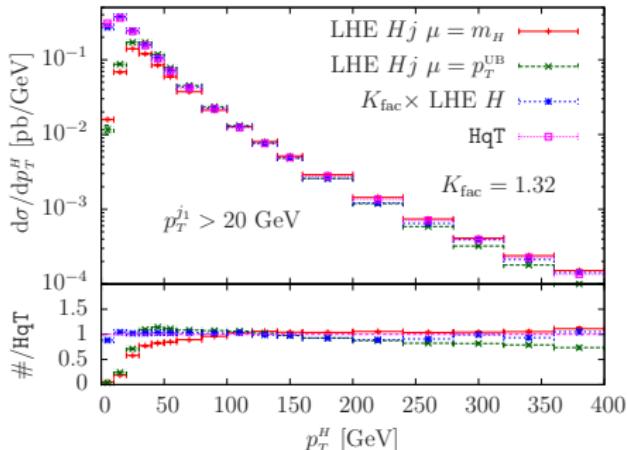
- Jet multiplicity → uncertainty due to choice of μ_Q^2
- Forward energy flow → major uncertainty from underlying event

$D^{(A)} \rightarrow R \Rightarrow MC@NLO \rightarrow POWHEG$
 [Frixione,Nason,Oleari] arXiv:0709.2092

Partially automated in POWHEGBox
 [Alioli,Oleari,Nason,Re] arXiv:1002.2581

- FKS subtraction
- PYTHIA/fHERWIG PS

Extensive list of processes implemented
 Recent example: $h+2$ jets in GF



[Campbell,Ellis,Frederix,Nason,Oleari,Williams]
 arXiv:1202.5475

POWHEGBOX originally aimed at providing framework only
 → many contributors and rapid development

[Barzè,Bernaciak,Bagnaschi,Campbell,Ellis,Frederix,deGrassi,Jäger,Klasen,Kovarik,Melia,Moch,Montagna,Nicrosini,Piccinini,Reina,Ridolfi,Rontsch,Slavich,Uwer,Vicini,Wackerlo,Weydert,Williams,Zanderighi]

Heading towards full automation using MADGRAPH & GO SAM

Some in-house implementations of POWHEG in HERWIG++

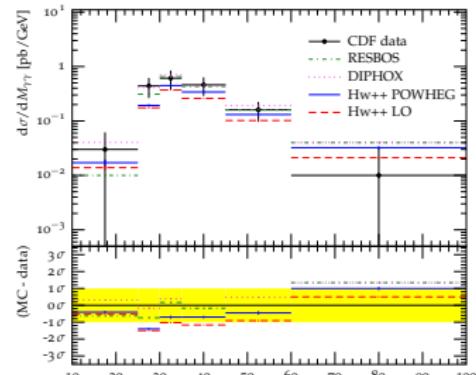
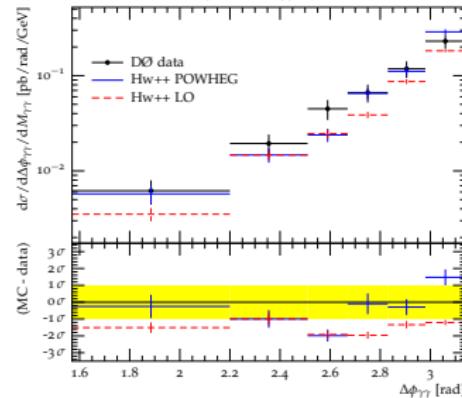
- Drell-Yan arXiv:0806.0290
- $W/Z + \text{Higgs}$ arXiv:0903.4135
- Higgs in GF arXiv:0903.4345
- DIS & VBF arXiv:1106.2983
- Diphoton arXiv:1106.3939

Truncated PS always included!

While argued that necessary in principle truncated PS is **neglected** in POWHEGBox

Elegant solution for diphoton production:
Split real-emission ME into QCD & QED
parts using respective subtraction terms

$$R_{\text{QCD}}^{(A)} = R \frac{\sum D_{\text{QCD}}^{(A)}}{\sum D_{\text{QCD}}^{(A)} + \sum D_{\text{QED}}^{(A)}}$$

(a) $50 \leq M_{\gamma\gamma} < 80 \text{ GeV}$ 

[d'Errico, Richardson] arXiv:1106.3939

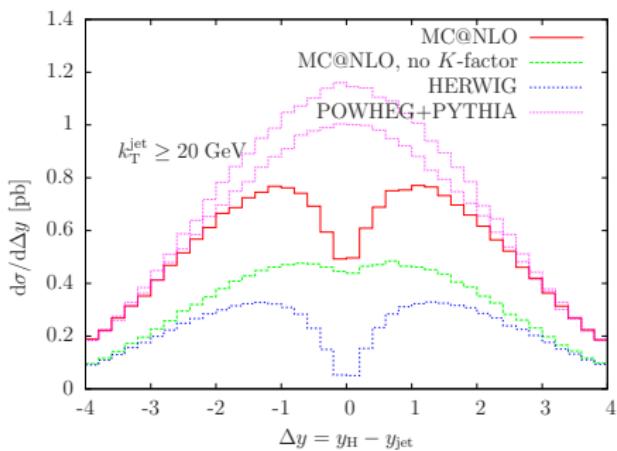
Controversial issue: What is resummed in POWHEG / Mc@NLO?

$D^{(A)}/H^{(A)}$ can be adjusted in functional form & active phase space

Mc@NLO → a-priori choice / POWHEG → tuneable damping parameter h

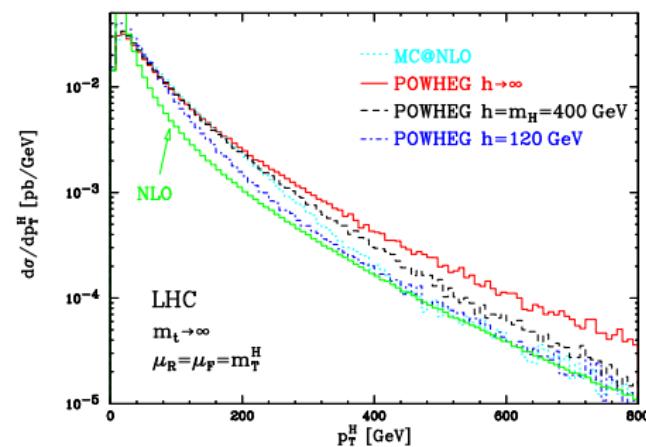
Why important? Two examples:

Limited phase-space coverage of PS
→ dead zones appear as “Mc@NLO dip”



[Nason,Webber] arXiv:1202.1251

h not defined by resummation scale → disagreement with NLO in high- p_T tails



[Nason,Webber] arXiv:1202.1251

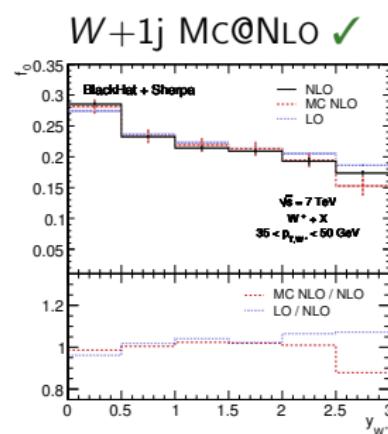
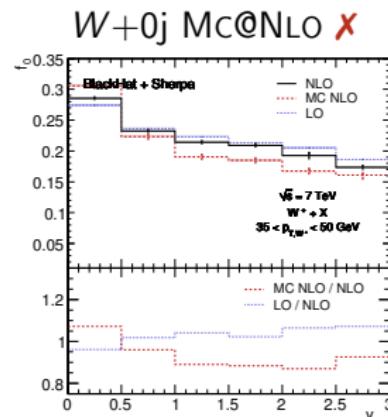
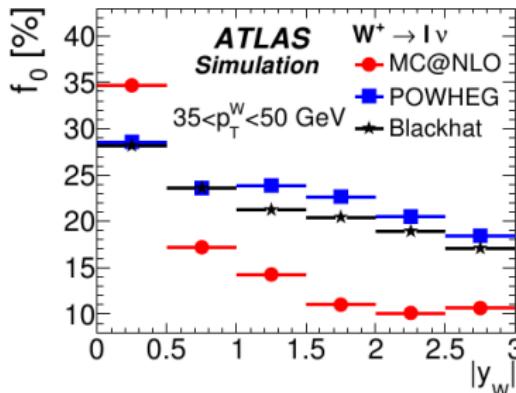
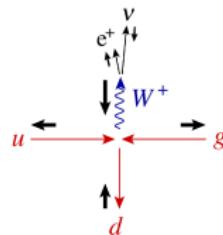
Usage issues

SLAC

Which NLO-tool for what?

Example: Mc@NLO \leftrightarrow POWHEG
in W -polarization measurement

[ATLAS] arXiv:1203.2165



Parton shower issues

SLAC

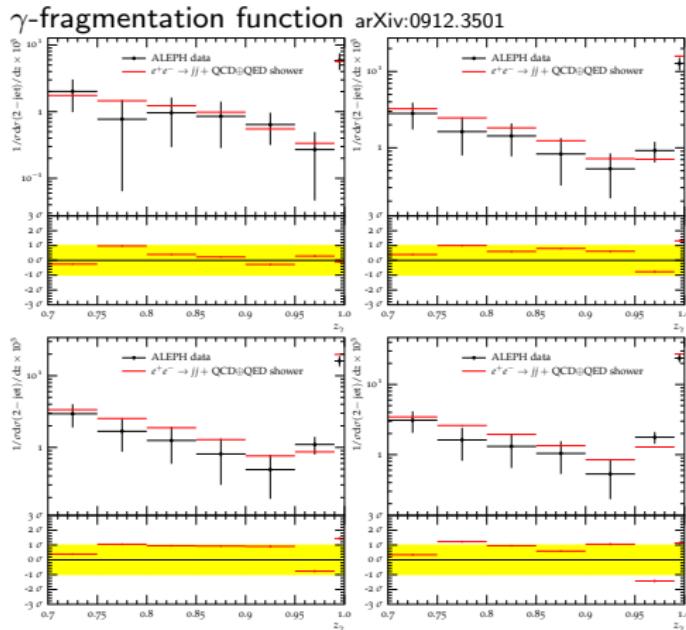
Mc@NLO and POWHEG both rely on general-purpose MC for subsequent showering

Kinematic effects & scale choices play a role → PS model affects accuracy of matched NLO result

Need improved parton showers as part of general-purpose MC

Various new implementations but few public codes on market

PS, Hadronization, & MPI linked
→ combined tuning necessary!



[Schumann,Sieger,SH] arXiv:0912.3501

Most promising progress with dipole-like parton showers
[Schumann,Krauss] arXiv:0709.1027, [Plätzer,Gieseke] arXiv:0909.5593

Sector showers interesting new alternative

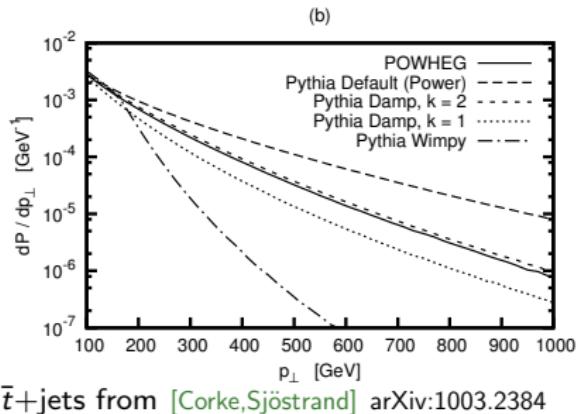
[Giele,Kosower,Skands] arXiv:1102.2126, [Larkoski,Peskin] arXiv:0908.2450

Parton shower issues

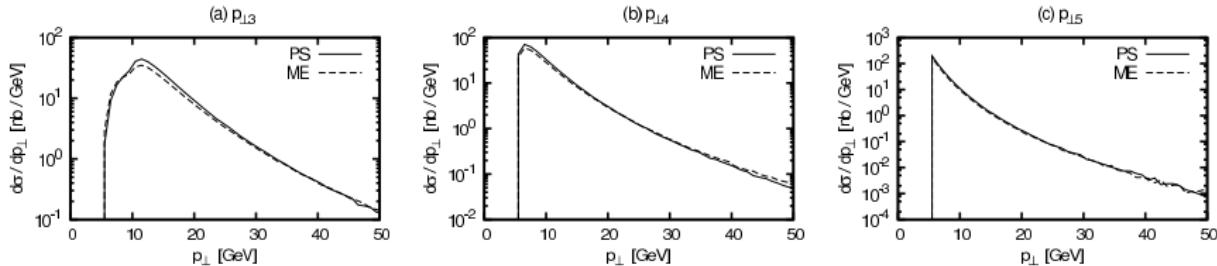
SLAC

Efforts to bridge gap between “power” and “wimpy” showers in PYTHIA by dampening factor $k^2 \mu^2 / (k^2 \mu^2 + p_T^2)$
Used for colored massive final states

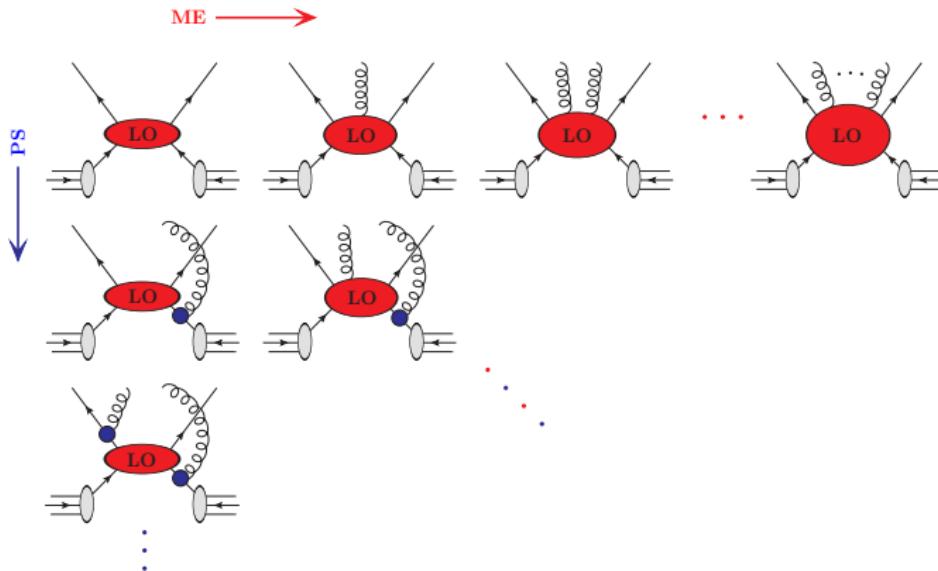
Improved default PS alleviates matching to NLO simulation MC@NLO, POWHEG



Study of PS emission pattern in pure QCD yields good agreement with ME
large region of phase space usually well described → reduced systematics in matching



[Corke,Sjöstrand] arXiv:1011.1759

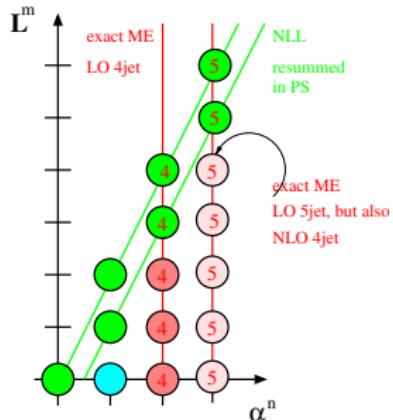


Prerequisites

- Jets defined with some IR-safe algorithm $\rightarrow k_T$, anti- k_T , SIScone
- n -jet observable O to be described at some fixed order (LO or NLO)

Objectives

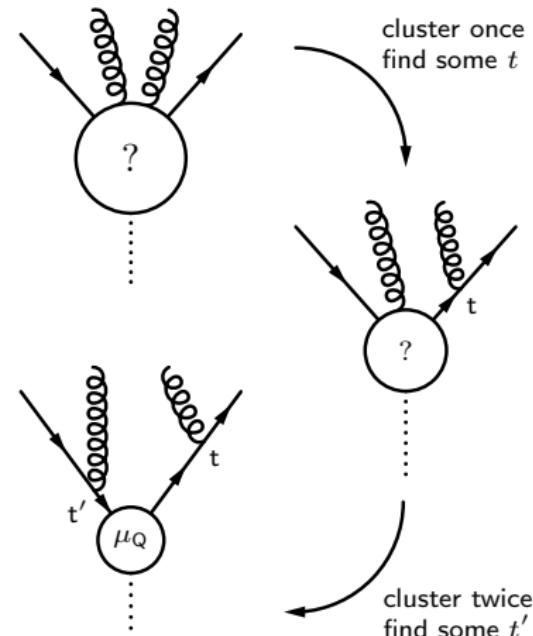
- In MC we can define jets using truth information
 \rightarrow distance measure Q for theory, close to k_T
- Want multi-jet rates for $Q > Q_{\text{cut}}$
correct to given fixed order in α_s
Current standard LO, first results for NLO
- Logarithmic accuracy of PS should be maintained



Parton-shower histories

[André,Sjöstrand] hep-ph/9708390

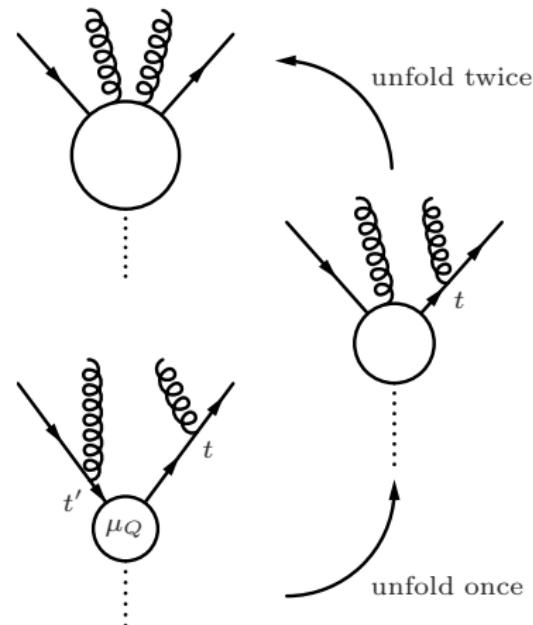
- Start with some “core” process for example $e^+e^- \rightarrow q\bar{q}$
- This process is considered inclusive It sets the resummation scale μ_Q^2
- Higher-multiplicity ME can be reduced to core by clustering
- If we want to match ME & PS the correct clustering algorithm suggests itself
 - Identify most likely splitting according to PS emission probability
 - Combine partons into mother according to PS kinematics
 - Continue until core process



Truncated parton showers

- If higher-multiplicity ME can be clustered back to core that means it is included in the inclusive cross section
- Must compute Sudakov suppression corresponding to no-decay probability of each intermediate parton
→ make inclusive ME exclusive
- Here the merging methods differ most

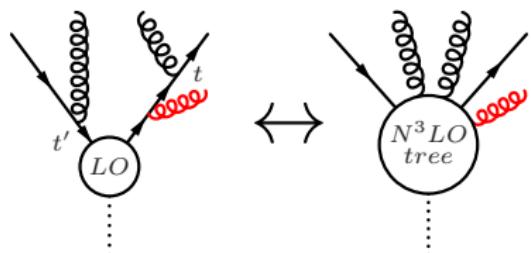
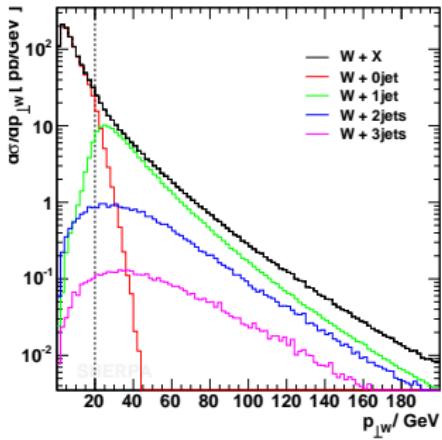
[Lönnblad] hep-ph/0112284
[Nason] hep-ph/0409146



[Catani,Krauss,Kuhn,Webber] hep-ph/0109231

Basic idea

- Separate phase space into “hard” and “soft” region
- Matrix elements populate hard domain
- Parton shower populates soft domain
- Need criterion to define “hard” & “soft”
 \rightarrow jet measure Q and corresponding cut, Q_{cut}



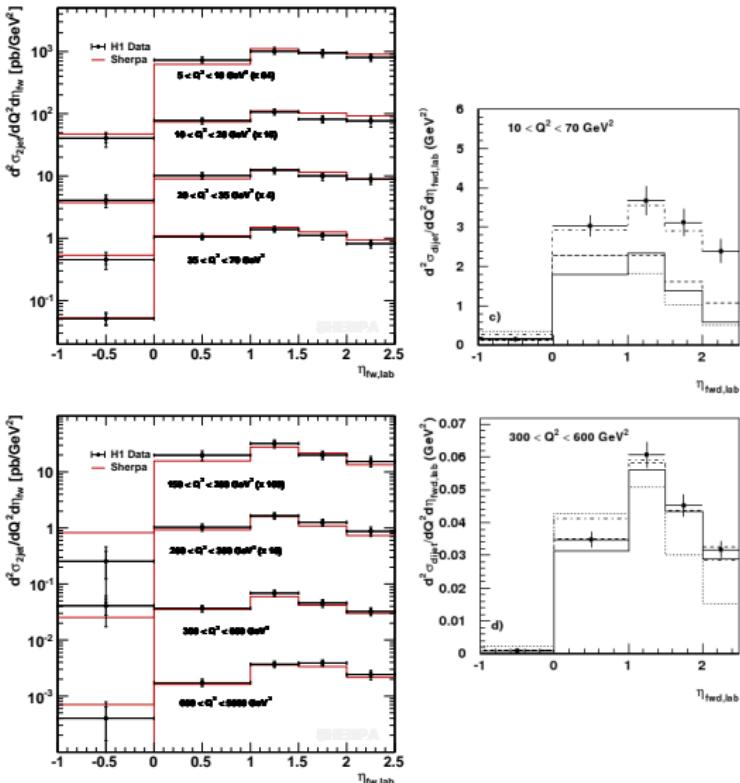
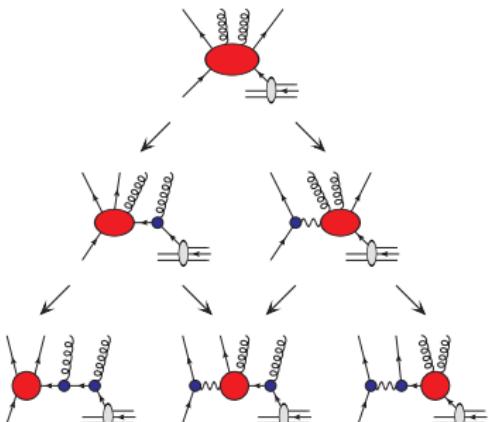
Method

- Start PS from core process
- Evolve until predefined branching
 \leftrightarrow truncated parton shower
- Emissions that would produce additional hard jets lead to event rejection (veto)

Lessons from DIS @ HERA:

Simulation often too focused
on resonant contributions

Sometimes need be inclusive
e.g. for low-mass Drell-Yan
or photon & diphoton events



[Carli, Gehrmann, SH] arXiv:0912.3715

Need control of PS to do things correctly → only two techniques with

- Exact correspondence between clustering & PS evolution
- Sudakov form factors as defined in parton shower

CKKW-L (**Pythia 8**)

[Lönnblad] hep-ph/0112284

[Lönnblad, Prestel] arXiv:1109.4829

- Truncated showers generate suppression, but no emissions
- Jet criterion dynamically redefined during PS evolution
- Simple and easy to implement

METS (**Herwig++** & **Sherpa**)

[SH,Krauss,Schumann,Siegert] arXiv:0903.1219

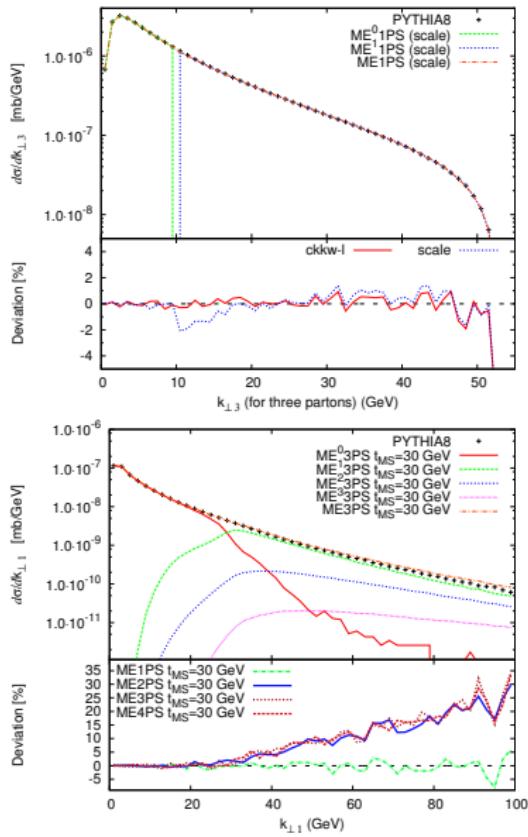
[Hamilton,Richardson,Tully] arXiv:0905.3072

- Truncated parton showers generate emissions and suppression
- Accounts for mismatch between jet criterion and evolution variable
- Requires intimate knowledge of PS

CKKW-L in Pythia 8

[Lönnblad, Prestel] arXiv:1109.4829

- Set up for interleaved showers → combine with arbitrary MPI tunes
- Flexibility due to LHE event files from MadGraph, SHERPA, ...
- Released with PYTHIA 8
Formal improvement over MLM
- Difficult to disentangle effects of phase-space separation analytically
Probably not an issue in practice

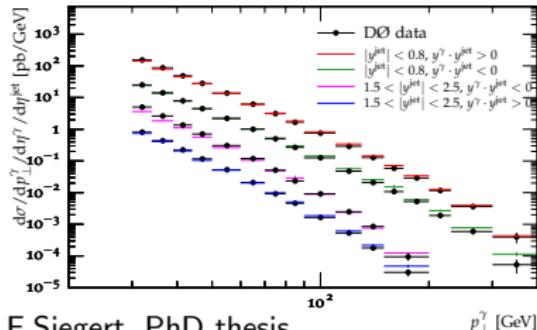


[Lönnblad, Prestel] arXiv:1109.4829

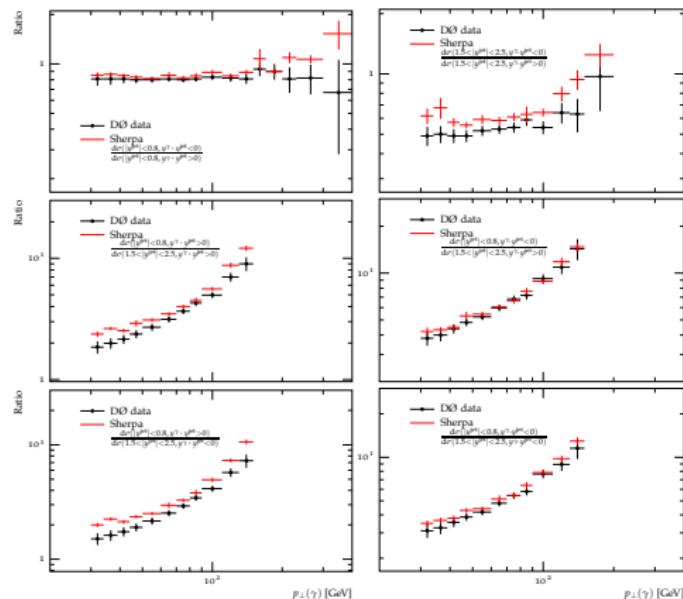
[Schumann,Siegert,SH] arXiv:0912.3501

“Democratic” model for γ 's

- Treat parton and γ equally
- Combine ME of various parton/ γ multiplicity with
- Interleaved QCD \oplus QED PS

Photon p_T spectra arXiv:0804.1107in regions of jet rapidity/orientation
scaled by 5, 1, 0.3 and 0.1 top to bottom

F.Siegert, PhD thesis

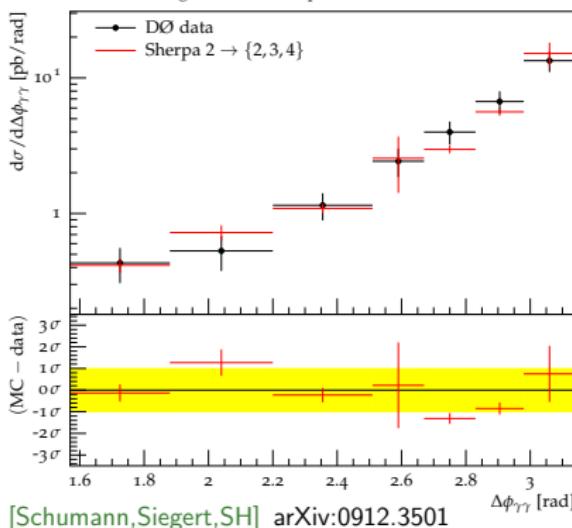
Ratio of photon p_T spectra arXiv:0804.1107
compare regions of jet rapidity/orientation

F.Siegert, PhD thesis

Di-photon production at D \emptyset

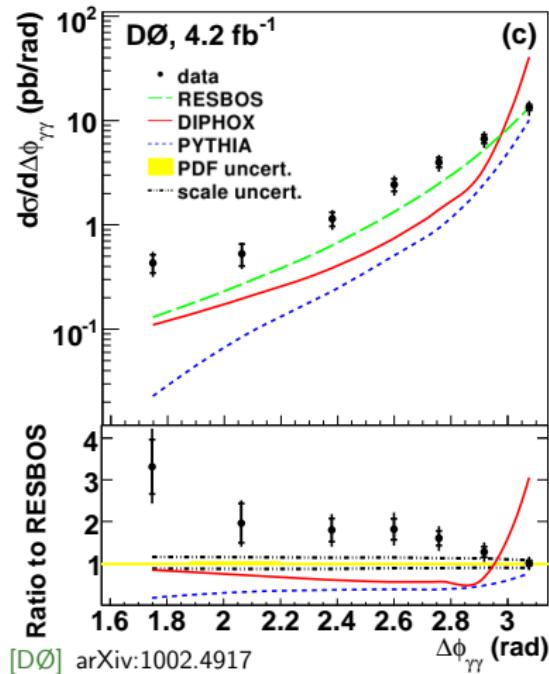
$$\begin{aligned} E_T^{\gamma 1} &> 21 \text{ GeV}, & E_T^{\gamma 1} &> 20 \text{ GeV}, \\ |\eta^\gamma| &< 0.9, & E_T^{R=0.4} - E_T^\gamma &< 2.5 \text{ GeV} \end{aligned}$$

Azimuthal angle between the photons



[Schumann,Sieger,SH] arXiv:0912.3501

SHERPA prediction: Merged $2 \rightarrow \{2,3,4\}$ -jet/ γ plus $gg \rightarrow \gamma\gamma$ box



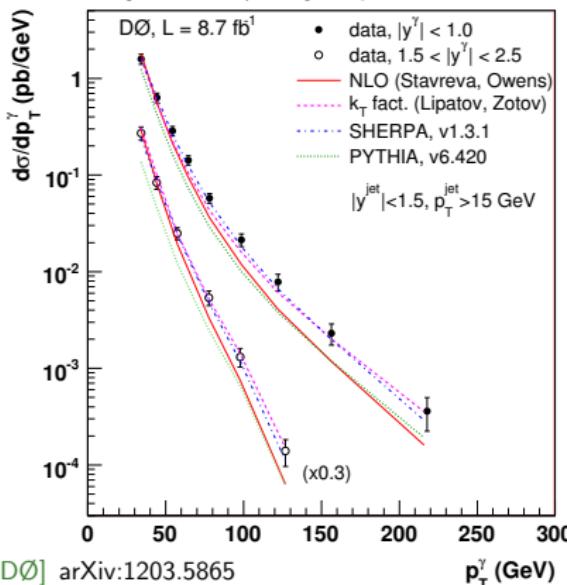
[DØ] arXiv:1002.4917

Z+b cross section

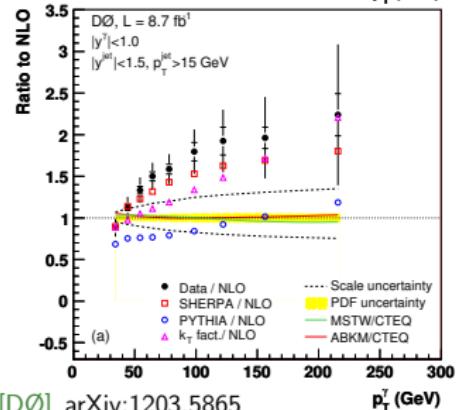
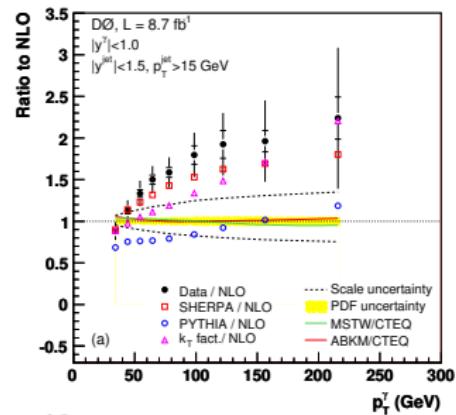
[ATLAS] arXiv:1109.1403

| | |
|------------|---|
| Experiment | $3.55^{+0.82}_{-0.74}(\text{stat})^{+0.73}_{-0.55}(\text{syst}) \pm 0.12(\text{lumi}) \text{ pb}$ |
| MCFM | $3.88 \pm 0.58 \text{ pb}$ |
| ALPGEN | $2.23 \pm 0.01 \text{ (stat only) pb}$ |
| SHERPA | $3.29 \pm 0.04 \text{ (stat only) pb}$ |

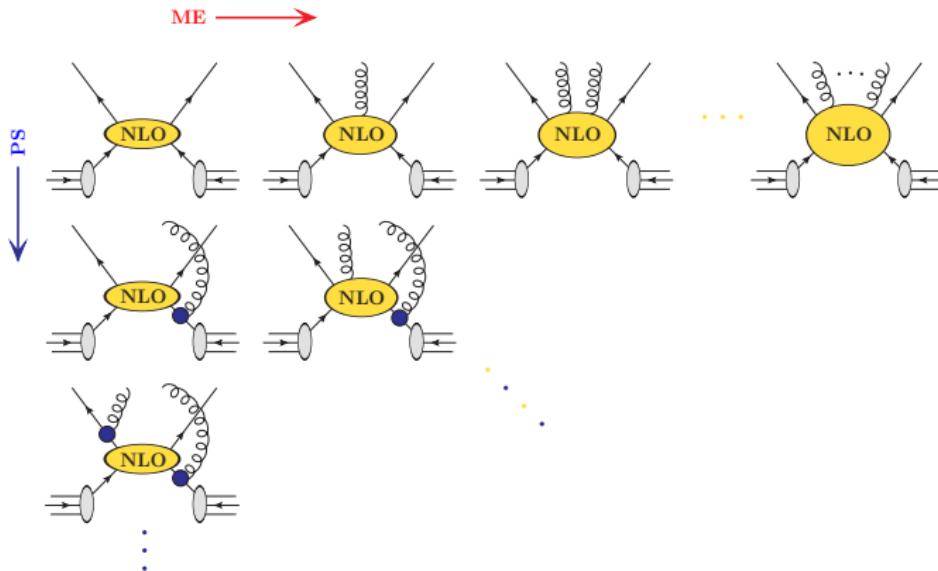
D \emptyset analysis of $\gamma+b\text{jet}$ production



[DØ] arXiv:1203.5865



ME \otimes PS merging at NLO



[Lavesson,Lönnblad] arXiv:0811.2912 [Lönnblad,Prestel] in preparation
 [Gehrmann,SH,Krauss,Schöherr,Siegert] arXiv:1207.5030, arXiv:1207.5031

Basic idea: Define MC@NLO for higher parton multiplicity,
 based on compound PS evolution kernel for $n + k$ -particle final state

$$\tilde{D}_{n+k}^{(A)} = D_{n+k}^{(A)} \Theta(t_{n+k} - t_{n+k+1}) + B_{n+k} \sum_{i=n}^{n+k-1} K_i \Theta(t_i - t_{n+k+1}) \Theta(t_{n+k+1} - t_{i+1})$$

t_i - nodal scales of parton emission in corresponding PS history

Extended modified subtraction, including $\mathcal{O}(\alpha_s)$ terms of truncated PS

$$\tilde{B}_{n+k}^{(A)} = \left(B_{n+k} + \tilde{V}_{n+k} + I_{n+k} \right) + \int d\Phi_1 \left(\tilde{D}_{n+k}^{(A)} - S_{n+k} \right)$$

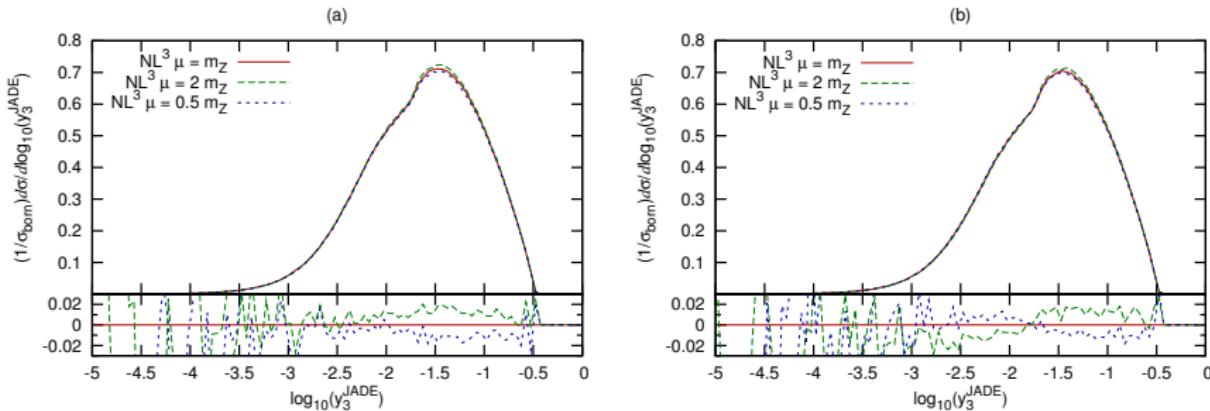
$$\tilde{H}_{n+k}^{(A)} = R_{n+k} - \tilde{D}_{n+k}^{(A)}$$

Otherwise arguments for ME \otimes PS merging at LO go straight through!

Currently two techniques

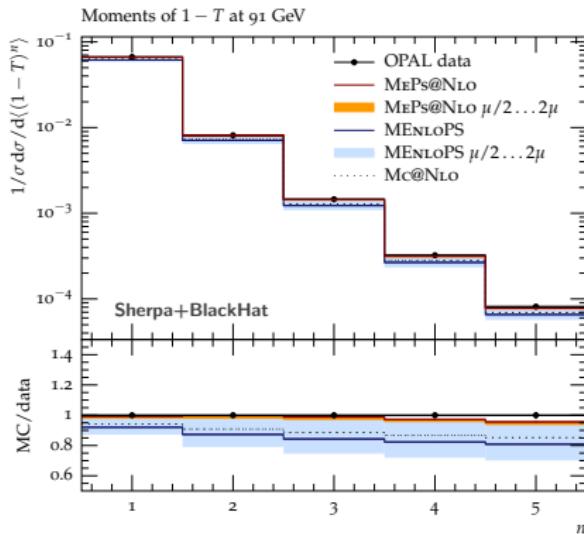
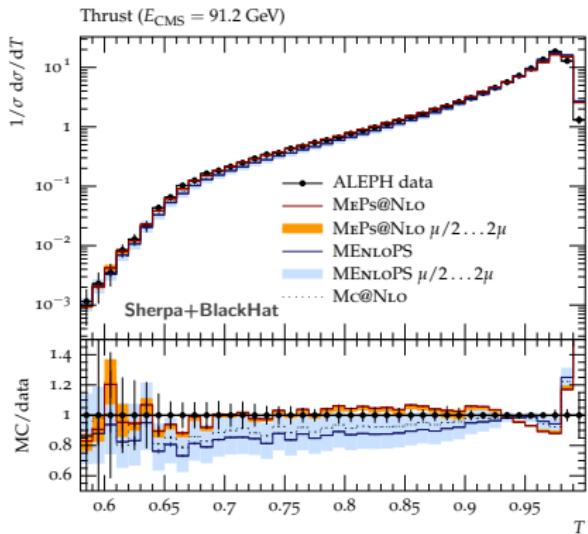
- Explicit subtraction (**Pythia 8**)
- Shower veto (**SHERPA**)

[Lavesson,Lönnblad] arXiv:0811.2912



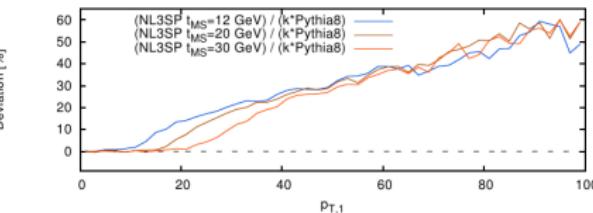
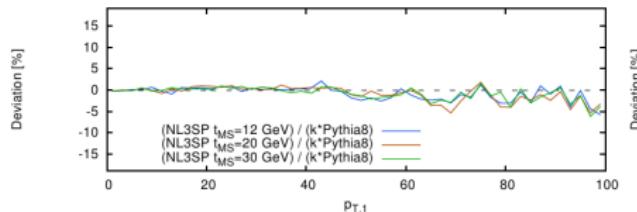
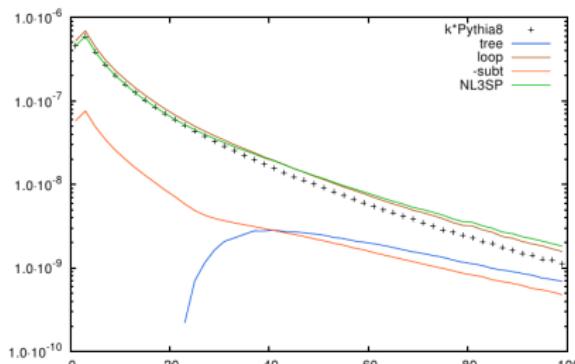
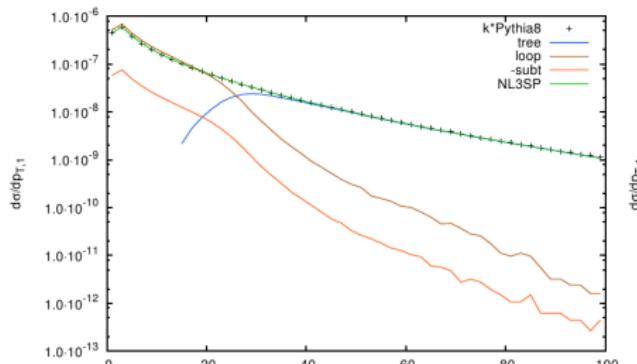
- Durham k_T -jet resolution in $e^+e^- \rightarrow \text{hadrons}$ at LEP
- MEPS@NLO with 2&3 jet PL at NLO / 2 jet PL at NNLO & 3 jet PL at NLO

[Gehrman, SH, Krauss, Schönherr, Siegert] arXiv:1207.5031

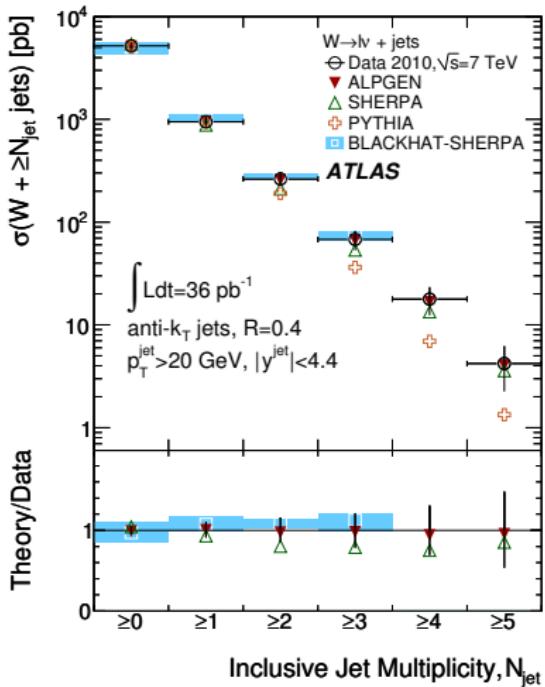


- MEPS@NLO with 2,3&4 jet PL at NLO plus 5&6 jet PL at LO
- MENLOPS with 2-6 jet PL at LO

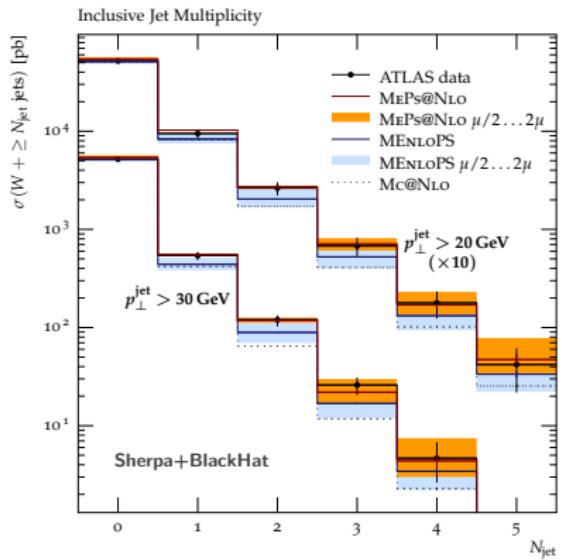
[Lönnblad,Prestel] ICHEP'12



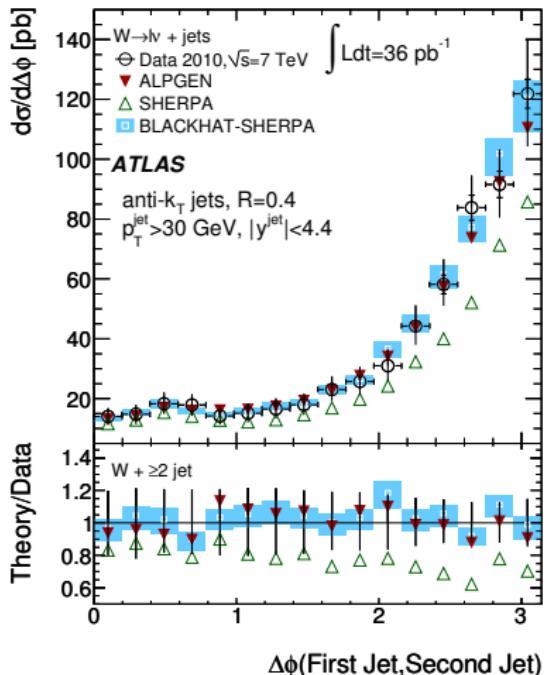
- Compare $W+0\text{-jet}$ at NLO $\leftrightarrow W+0,1\text{-jet}$ at NLO



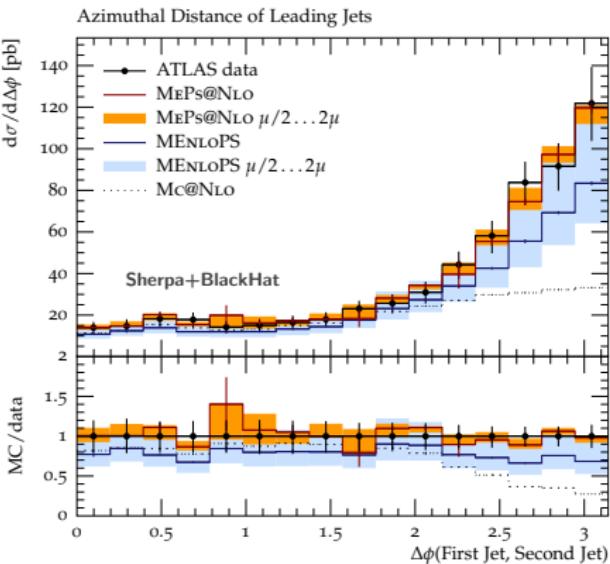
[ATLAS] arXiv:1201.1276
 [SH,Krauss,Schönherr,Sieger] arXiv:1207.5030



- MEPS@NLO with 0,1&2 jet PL at NLO plus 3&4 jet PL at LO
- MENLOPS with 0-4 jet PL at LO



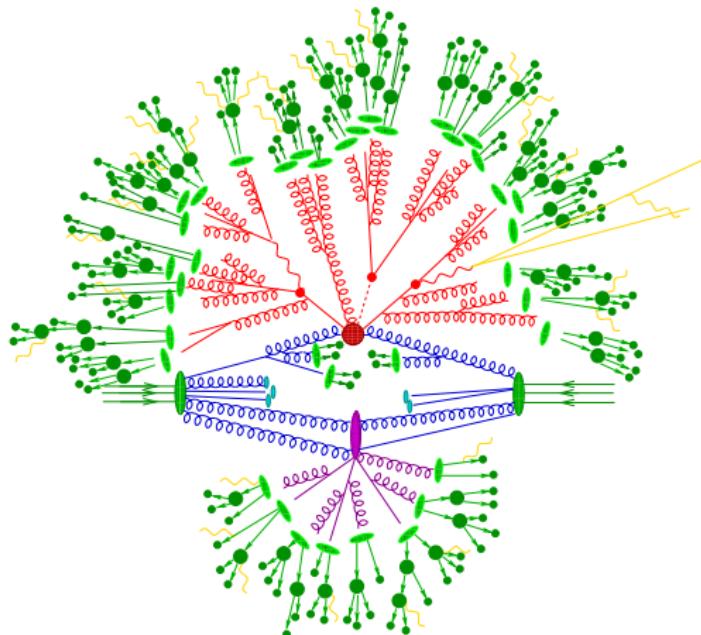
[ATLAS] arXiv:1201.1276
[SH,Krauss,Schönherr,Sieger] arXiv:1207.5030



- MEPS@NLO with 0,1&2 jet PL at NLO plus 3&4 jet PL at LO
- MENLOPS with 0-4 jet PL at LO

Structure of the simulation

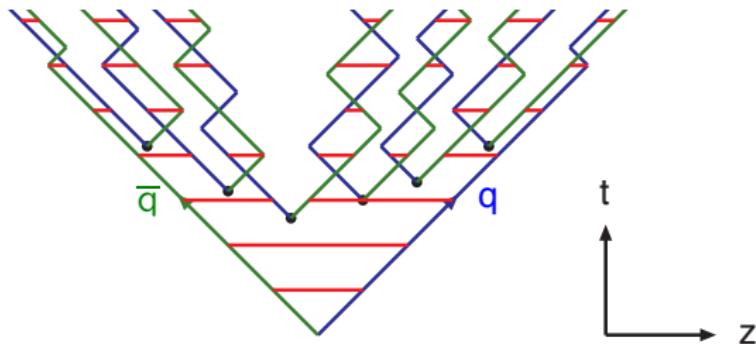
- Hard interaction
- QCD evolution
- Secondary hard interactions
- Jet fragmentation
- Hadron decays
- Higher-order QED corrections



[Andersson,Gustafson,Ingelman,Sjöstrand] PR97(1983)31

Lund string model of PYTHIA

- $e^+e^- \rightarrow q\bar{q} \Rightarrow$ QCD flux tube with constant dE/dy \leftrightarrow 
- New $q\bar{q}$ -pairs created by tunneling
- Gluons are kinks on string \rightarrow IR safe model
- Expanding string breaks into hadrons, then yo-yo modes
- Baryons modeled as quark-diquark pairs



Very well motivated, but many parameters, especially for baryon production

[Webber] NPB238(1984)492

[Krauss,Winter] hep-ph/0311085

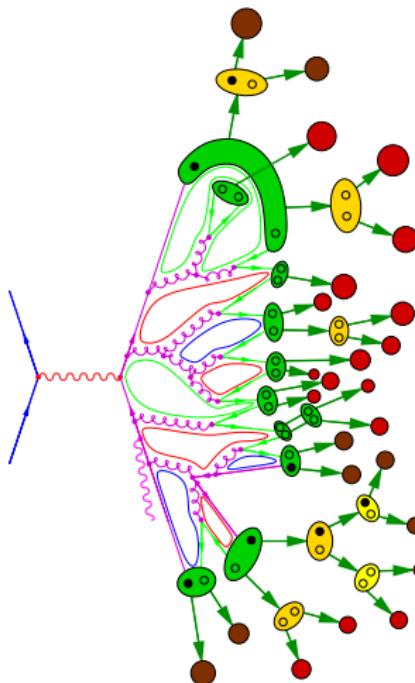
Cluster models of HERWIG++ & SHERPA

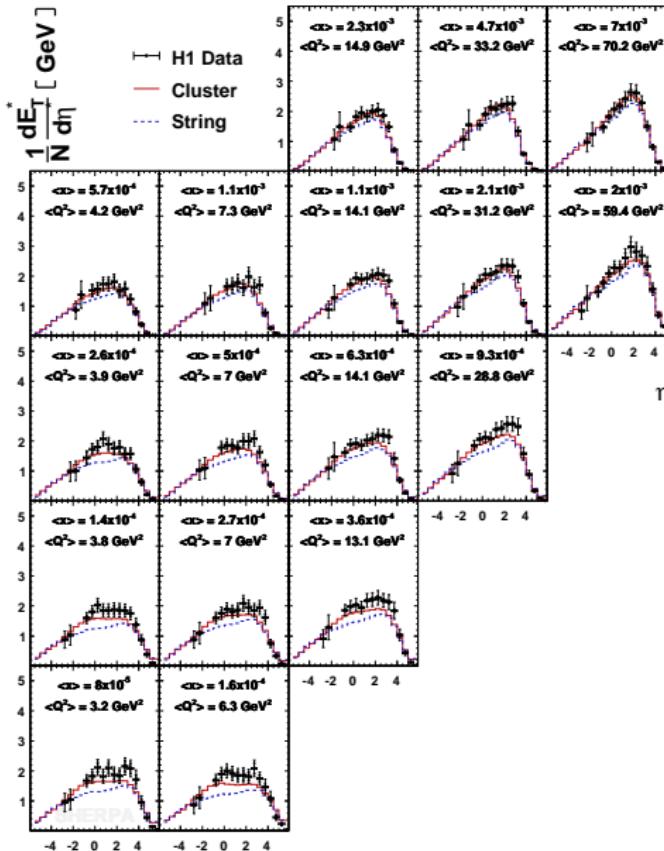
Naïve model

- After PS split gluons into $q\bar{q}$
- Color-adjacent pairs form primordial clusters
- Clusters decay into hadrons according to phase space
→ baryons & heavy quarks naturally suppressed

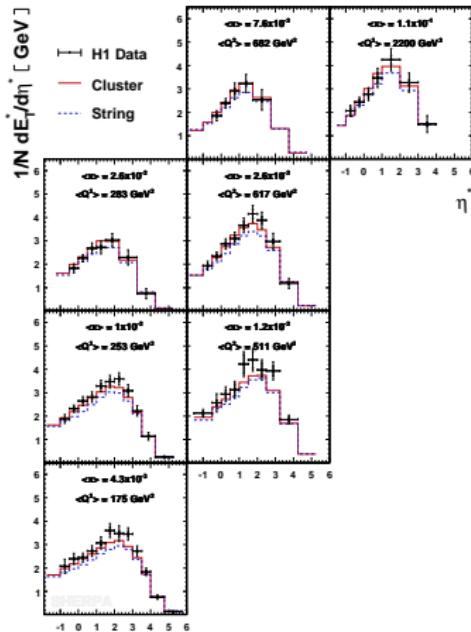
Improved model

- Heavy clusters decay into lighter ones
 $C \rightarrow CC$,
 $C \rightarrow CH$ & $C \rightarrow HH$
- Leading particle effects missing
→ make model more string-like





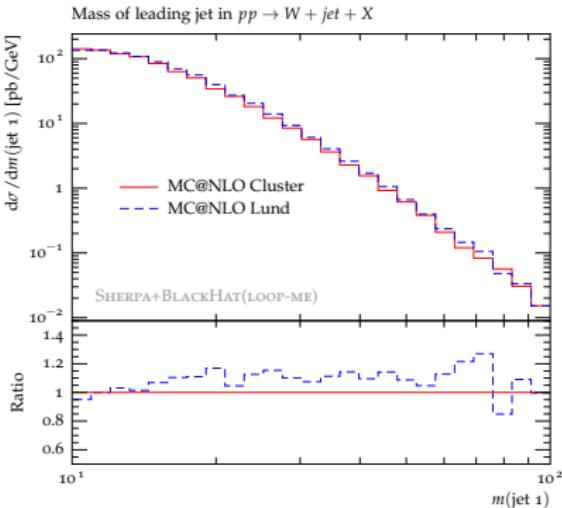
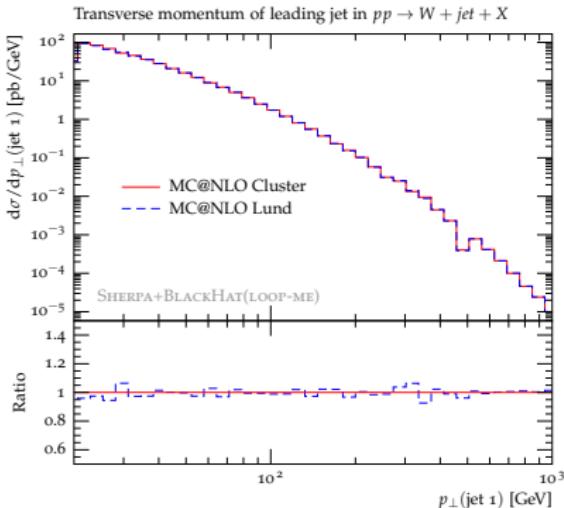
Transverse energy flow in DIS
SHERPA cluster fragmentation vs. Lund string fragmentation



[Carli, Gehrman, SH] arXiv:0912.3715

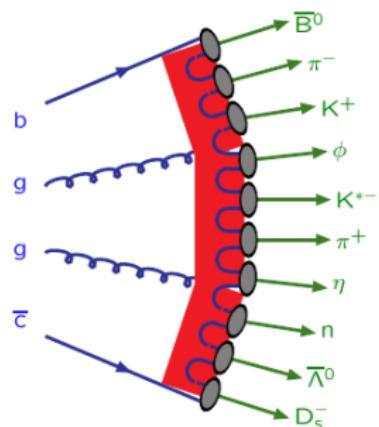
Hadronization uncertainties

[Krauss,Schönherr,Sieger,SH] arXiv:1111.1220



- MC@NLO for $pp \rightarrow h + j$ with SHERPA
- Lund string vs. Sherpa cluster fragmentation
- Correlated variation

[T.Sjöstrand, Durham'09]

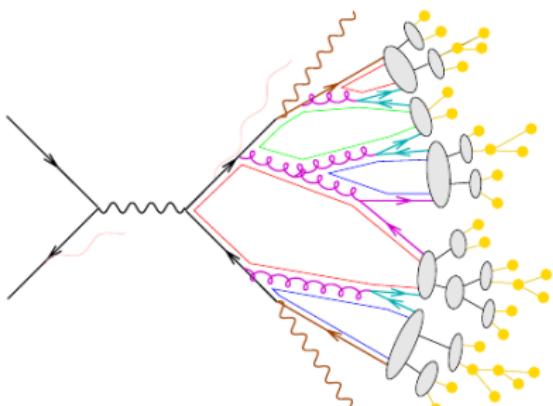
program
model

energy-momentum picture

parameters

flavour composition

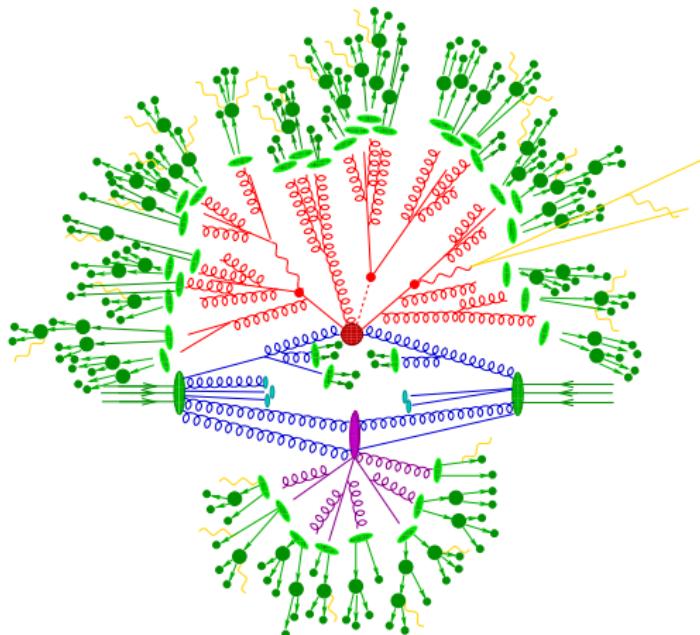
parameters

PYTHIA
stringpowerful
predictive
fewmessy
unpredictive
manyHERWIG
clustersimple
unpredictive
manysimple
in-between
few

"There ain't no such thing as a parameter-free *good* description"

Structure of the simulation

- Hard interaction
- QCD evolution
- Secondary hard interactions
- Jet fragmentation
- Hadron decays
- Higher-order QED corrections

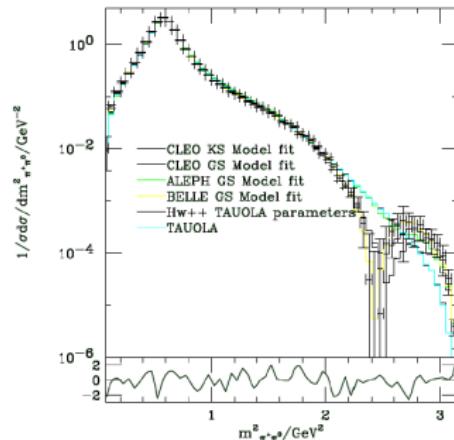


Secondary particle decays

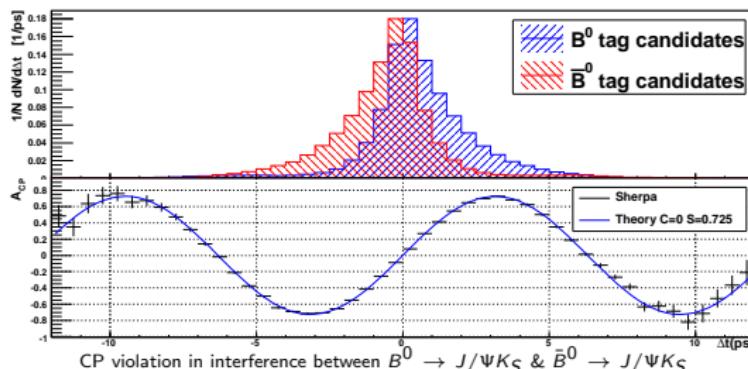
SLAC

- Previous generations of generators relied on external decay packages Tauola & EvtGen
- New generation programs Herwig++ & Sherpa contain at least as complete a description
- Spin correlations and B-mixing built in
- No interfacing issues

[Krauss,Sieger] in arXiv:0811.4622

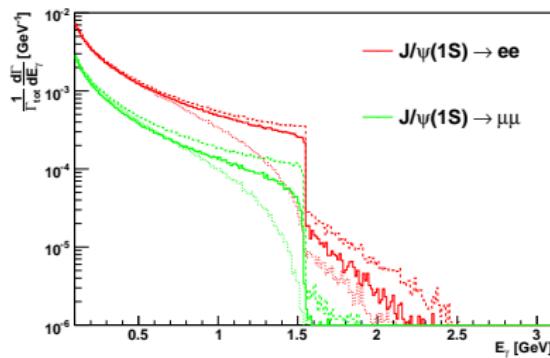
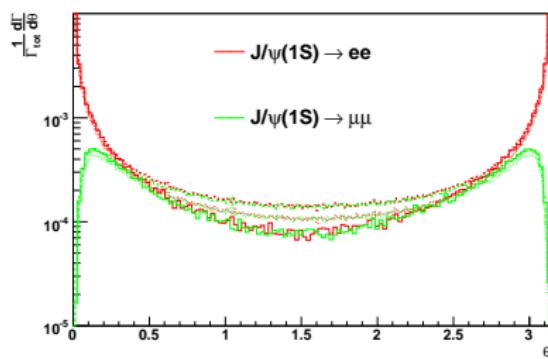


[Grellscheid,Richardson] arXiv:0710.1951



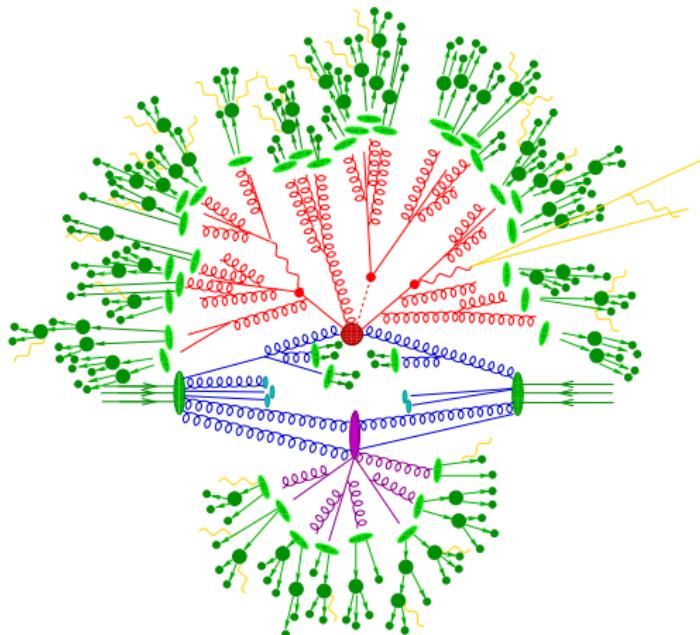
[Yennie,Frautschi,Suura] AP13(1961)379

- Previous generations of generators relied on external package Photos to simulate QED radiation
- New generation programs Herwig++ & Sherpa have simulation of QED radiation built in

Total photon energy in J/ψ rest frameAngular radiation pattern in $\ell^+ - \ell^-$ frame

Structure of the simulation

- Hard interaction
- QCD evolution
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- Higher-order QED corrections



Multiple Parton Interactions

SLAC

Same evolution variable, k_T , for ISR/FSR and MPI in PYTHIA

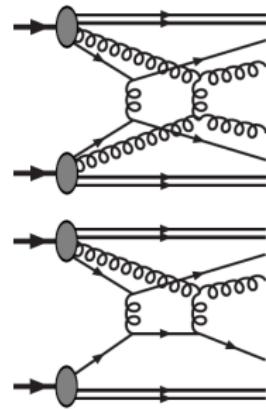
Interleave PS & MPI to arrive at more inclusive picture

[Sjöstrand,Skands] hep-ph/0408302, [Corke,Sjöstrand] arXiv:0911.1909

$$\frac{dP}{dp_T} = \frac{d}{dp_T} \exp \left\{ - \int_{p_T} d\bar{p}_T \left(\frac{d\mathcal{P}_{PS}}{d\bar{p}_T} + \frac{d\mathcal{P}_{MPI}}{d\bar{p}_T} \right) \right\}$$

Add rescattering \rightarrow important at higher energies

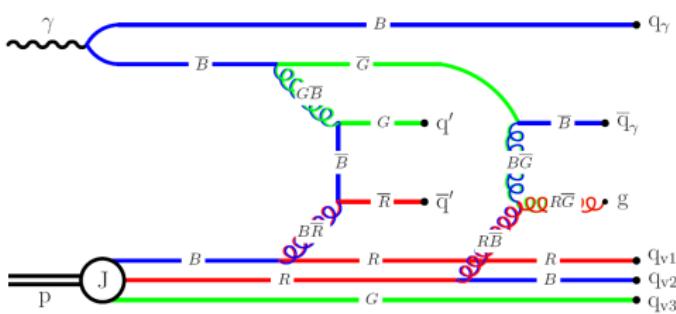
| | Tevatron | | LHC | |
|----------------------|----------|----------|----------|----------|
| | Min Bias | QCD Jets | Min Bias | QCD Jets |
| Normal scattering | 2.81 | 5.09 | 5.19 | 12.19 |
| Single rescatterings | 0.41 | 1.32 | 1.03 | 4.10 |
| Double rescatterings | 0.01 | 0.04 | 0.03 | 0.15 |



[Corke,Sjöstrand]

arXiv:0911.1909

- New models embed scatters into existing color topology
- Three different options for string drawing
 - At random
 - Rapidity ordered
 - String length optimized



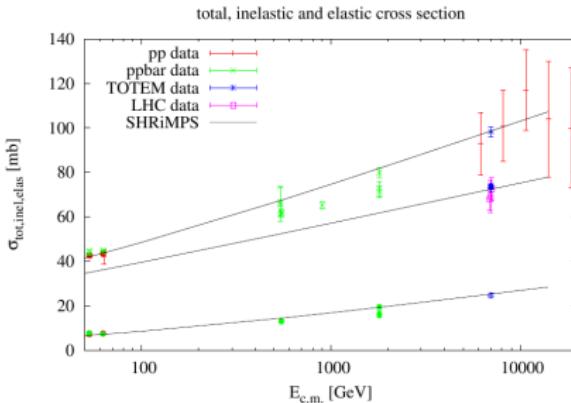
New generator based on KMR model in Sherpa 1.4.0

Optical theorem relates σ_{tot} to elastic forward scattering (Pomeron)

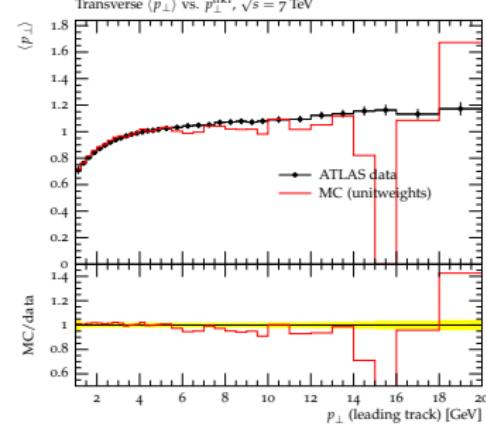
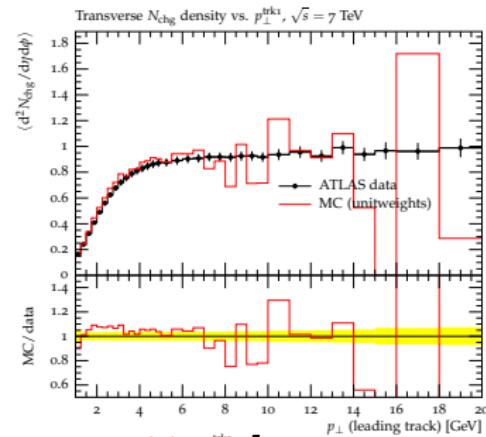
Elastic bare Pomeron exchange simulated as rapidity evolution

Rescattering in high density & strong coupling regime

Proton FF \leftrightarrow diffractive Eigenstates



[Hoeth,Khoze,Krauss,Martin,Ryskin,Zapp] SM@LHC'12



Exp. data: [ATLAS] arXiv:1012.0791

- HERWIG++, PYTHIA & SHERPA provide frameworks for event simulation
- Lots of progress to combine NLO tools with these general-purpose MC
- Interesting new developments regarding inclusive QCD
- More systematic uncertainty studies needed
- Improved resummation needed if accuracy to be increased further
- High-energy effects may need to be included

