

Probing non-standard CC interactions: from cold neutrons to the LHC

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THE UNIVERSITY
of
WISCONSIN
MADISON

Motivation & goals

- Very precise measurements in some low-energy experiments (errors $\sim 0.1\%$);
- Very precise theoretical (th+lat) SM-calculations for these processes (errors $< 0.1\%$);
- Not only useful to extract SM parameters (V_{ij}) but also to search for New Physics!

$$\pi^+ \rightarrow \pi^0 e^+ \nu_e$$

$$\pi^+ \rightarrow l^+ \nu_l$$

$$K \rightarrow \pi l \nu_l$$

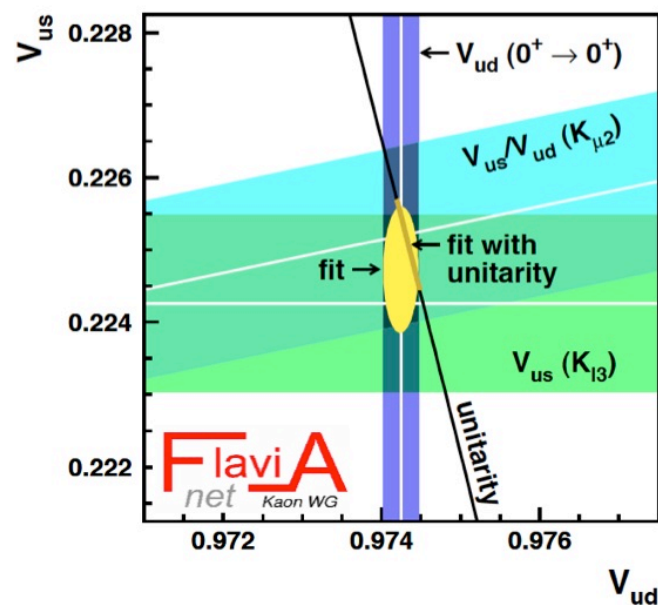
$$K^+ \rightarrow l^+ \nu_l$$

n decay

$$0^+ \rightarrow 0^+$$

...

$$(\mu \rightarrow e \bar{\nu}_e \nu_\mu)$$

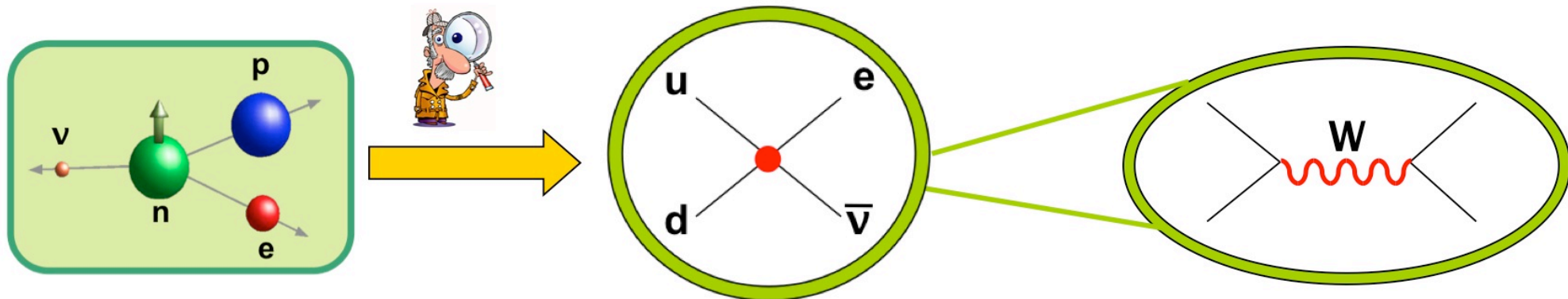


Questions:

- What kind of NP can we probe with SL beta decays? Which is the best process?
- LHC?

Motivation & goals

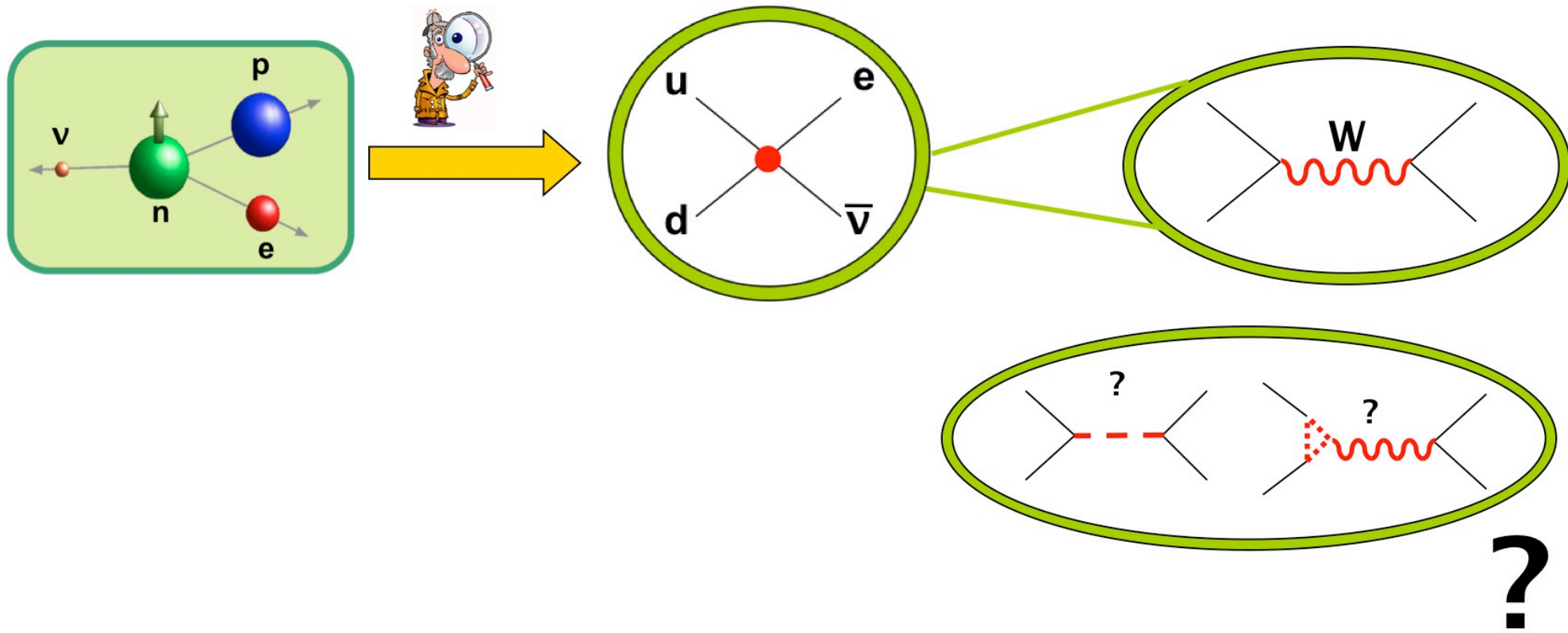
$$\mathcal{L}_{d \rightarrow u l \bar{\nu}_l} = -\frac{4G_F V_{ij}}{\sqrt{2}} \left[\bar{\ell}_L \gamma_\mu \nu \cdot \bar{u} \gamma^\mu d_L \right]$$



Motivation & goals

$$\mathcal{L}_{d \rightarrow u l \bar{\nu}_l} = -\frac{4G_F V_{ij}}{\sqrt{2}} \left[\bar{l}_L \gamma_\mu \nu \cdot \bar{u} \gamma^\mu d_L + \sum_{\rho \delta \Gamma} \epsilon_{\rho \delta}^\Gamma \bar{l}_\rho \Gamma \nu \cdot \bar{u} \Gamma d_\delta \right]$$

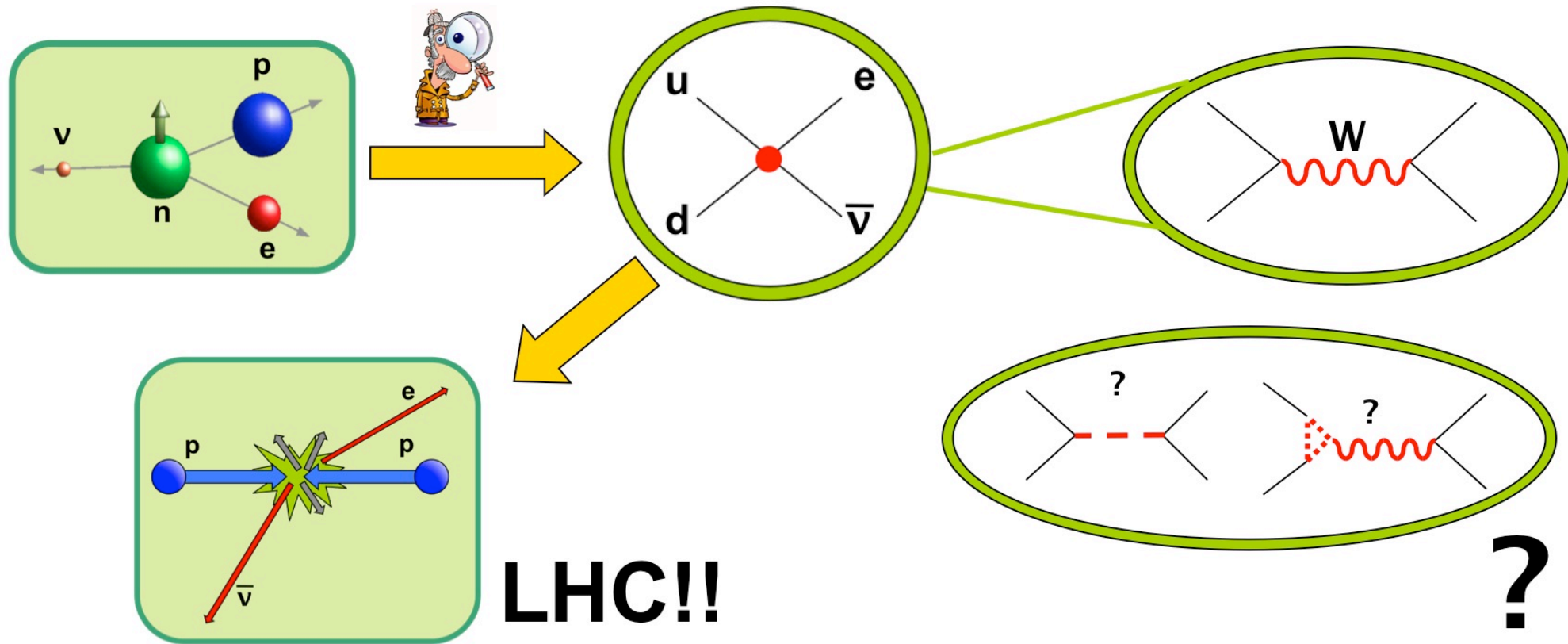
Model-independent analysis



Motivation & goals

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Model-independent analysis



Outline

□ Introduction and motivation;



□ EFT approach;

□ Low-energy bounds:

□ LHC bounds.

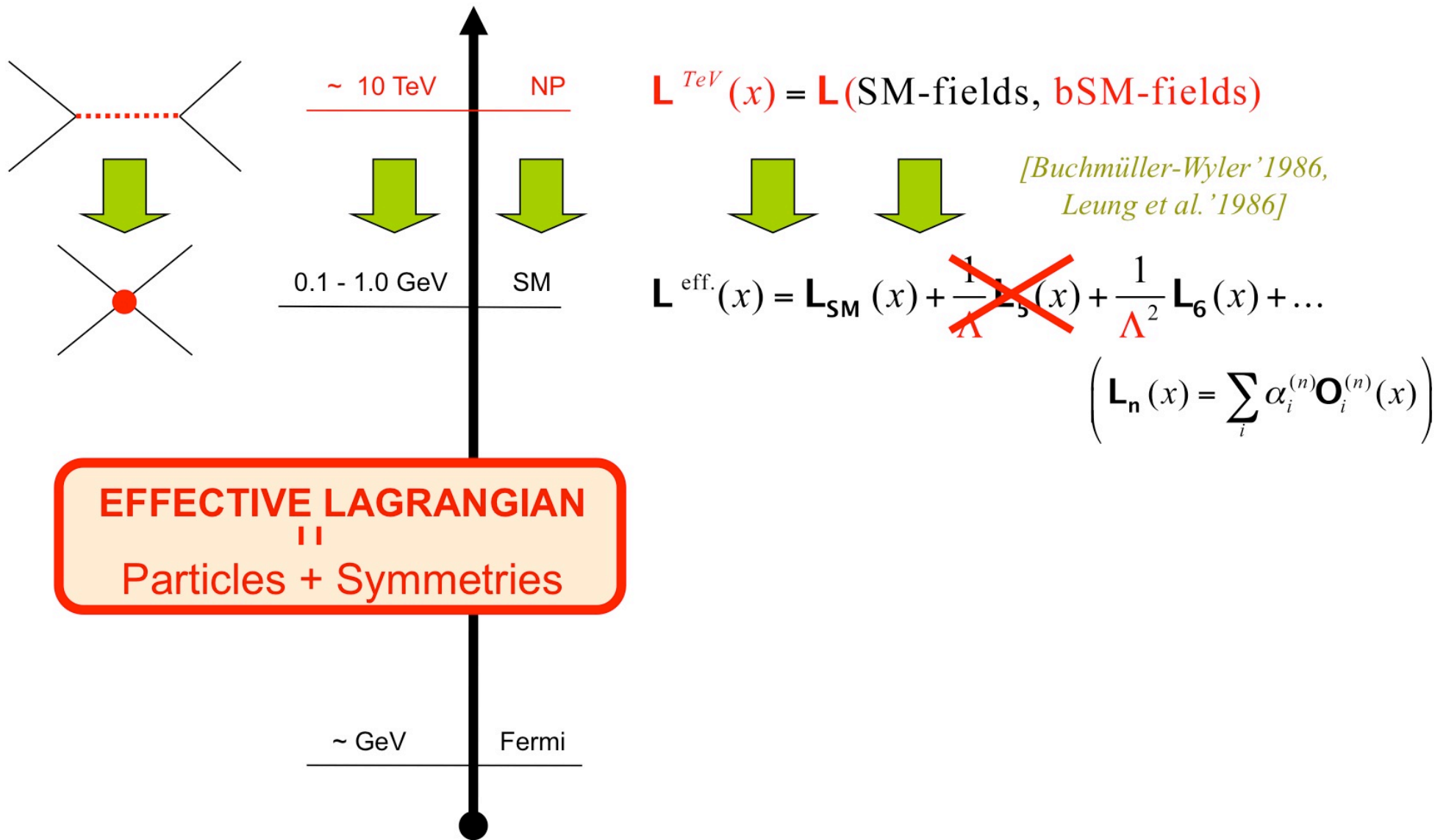
Cirigliano, MGA & Jenkins'2010

Bhattacharya, Cirigliano, Cohen, Filipuzzi, MGA, Graesser, Gupta, Lin'2012

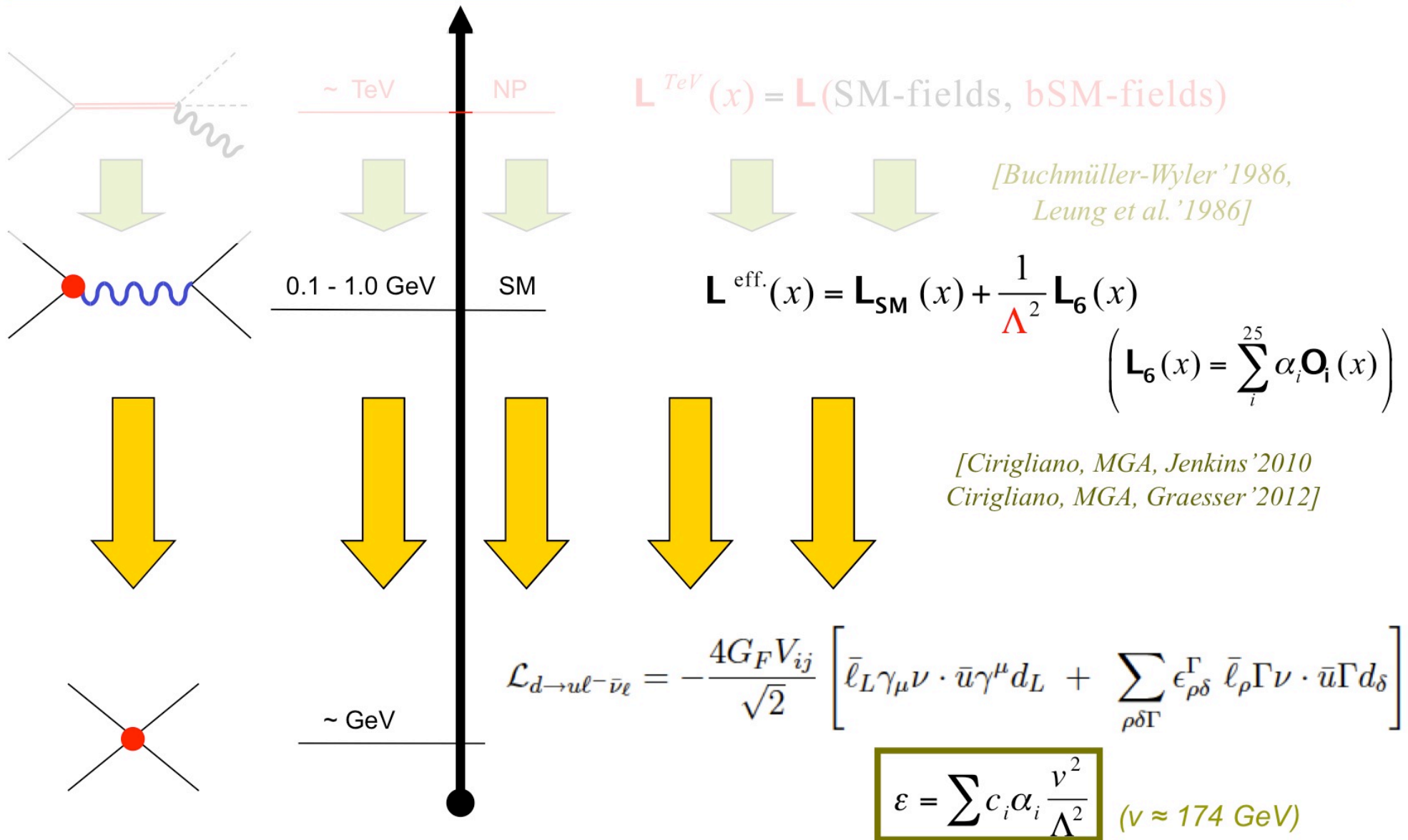
Cirigliano, MGA & Graesser'2012

Abele, MGA, Pitschmann, Ramsey-Musolf (in preparation)

The eff. Lagrangian for $E \sim 100$ GeV



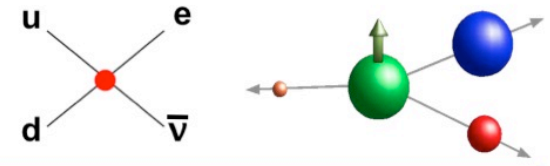
The eff. Lagrangian for $E \sim 1$ GeV



Outline

- Introduction and motivation; ✓
- EFT approach; ✓
- Low-energy bounds:
- LHC bounds.

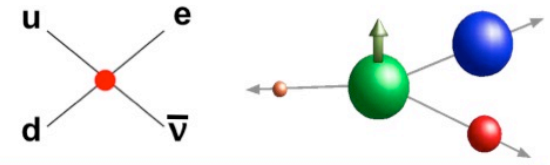
Low-energy searches



Eff. Lagrangian at the quark level

$$\begin{aligned} \mathcal{L} \sim & (1 + \epsilon_L)(V - A)(V - A) + \epsilon_R(V - A)(V + A) + \tilde{\epsilon}_L(V + A)(V - A) + \tilde{\epsilon}_R(V + A)(V + A) \\ & + \epsilon_S(S - P)S - \epsilon_P(S - P)P + \tilde{\epsilon}_S(S + P)S - \tilde{\epsilon}_P(S + P)P \\ & + \epsilon_T(T - T\gamma_5)(T + T\gamma_5) + \tilde{\epsilon}_T(T + T\gamma_5)(T - T\gamma_5) \end{aligned}$$

Low-energy searches



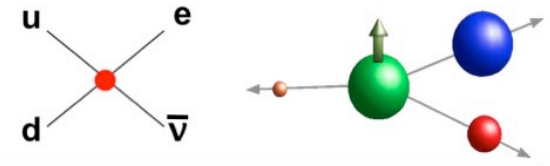
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 & + \epsilon_T(T - T\gamma_5)(T + T\gamma_5) - \tilde{\epsilon}_T(T + T\gamma_5)(T - T\gamma_5)
 \end{aligned}$$

$$R_\pi \equiv \frac{\Gamma(\pi \rightarrow e\nu)}{\Gamma(\pi \rightarrow \mu\nu)} \approx R_\pi^{SM} \left(1 - \frac{B_0}{m_e} \epsilon_P \right)$$

$$\mathcal{O} = \mathcal{O}_{SM} + \epsilon^2$$

Low-energy searches



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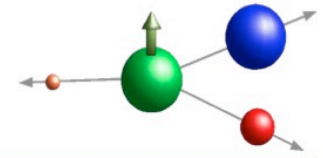
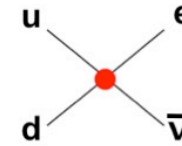
$$\mathcal{O} = \mathcal{O}_{SM} + \epsilon^2$$

Eff. Lagrangian at the hadron level

(for $n \rightarrow pe\nu$, up to ϵ^2 terms)

$$\mathcal{L}_{n \rightarrow pe\nu} = -\sqrt{2}G_F V_{ud} (1 + \epsilon_L + \epsilon_R) \left[\bar{e}_L \gamma_\mu \nu_L \cdot \bar{p} (\gamma^\mu - \tilde{\lambda}_A \gamma^\mu \gamma_5) n \right. \\ \left. + \lambda_S \epsilon_S \bar{e}_R \nu_L \cdot \bar{p} n + 2\lambda_T \epsilon_T \bar{e}_R \sigma_{\mu\nu} \nu_L \cdot \bar{p} \sigma^{\mu\nu} n_L \right]$$

Low-energy searches



$$\tilde{\lambda}_A \approx \lambda_A(1 - 2\epsilon_R)$$

$$\mathcal{L}_{n \rightarrow pe^- \bar{\nu}_e} = -\sqrt{2}G_F V_{ud} (1 + \epsilon_L + \epsilon_R) \left[\bar{e}_L \gamma_\mu \nu_L \cdot \bar{p} (\gamma^\mu - \tilde{\lambda}_A \gamma^\mu \gamma_5) n \right. \\ \left. + \lambda_S \epsilon_S \bar{e}_R \nu_L \cdot \bar{p} n + 2\lambda_T \epsilon_T \bar{e}_R \sigma_{\mu\nu} \nu_L \cdot \bar{p} \sigma^{\mu\nu} n_L \right]$$

Lifetime shift →
CKM unitarity

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 - 1 = (0.1 \pm 0.6) \cdot 10^{-3}$$

$$\epsilon_L + \epsilon_R \leq 5 \cdot 10^{-4}$$

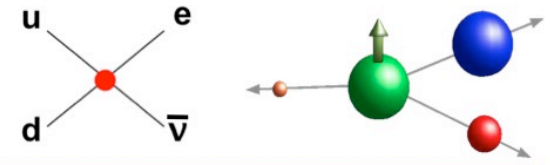
$$\Lambda_{NP} > 11 \text{ TeV (90\%CL)}$$

Marciano'2008

Cirigliano, MGA & Jenkins'2010

Bauman, Erler & Ramsey-Musolf'2012

Low-energy searches



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Lifetime shift →
CKM unitarity

S and T affect the angular distributions
and the spectrum!!

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 - 1 = (0.1 \pm 0.6) \cdot 10^{-3}$$

$$\frac{d\Gamma(\mathbf{J})}{dE_e d\Omega_e d\Omega_\nu} \sim \xi(E) \left\{ 1 + a \frac{\mathbf{p}_e \cdot \mathbf{p}_\nu}{E_e E_\nu} + b \frac{m_e}{E_e} + A \frac{\mathbf{p}_e \cdot \mathbf{J}}{E_e J} + (B + b_B \frac{m_e}{E_e}) \frac{\mathbf{p}_\nu \cdot \mathbf{J}}{E_\nu J} \right\}$$

$$\epsilon_L + \epsilon_R \leq 5 \cdot 10^{-4}$$

$$\Lambda_{NP} > 11 \text{ TeV (90\%CL)}$$

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Cirigliano, MGA & Jenkins'2010

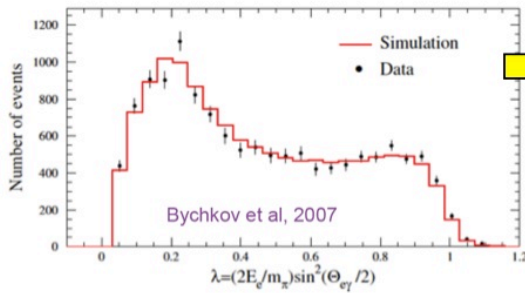
$$b \approx 0.3 g_S \epsilon_S - 5.0 g_T \epsilon_T$$

$$b_\nu - b \approx 0.1 g_S \epsilon_S - 0.3 g_T \epsilon_T$$

Form factors needed!

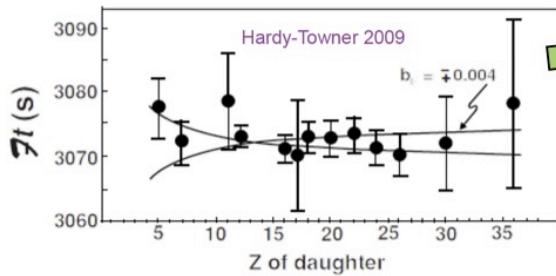
Low-energy searches: S & T

Radiative pion decay (PIBETA '2009)



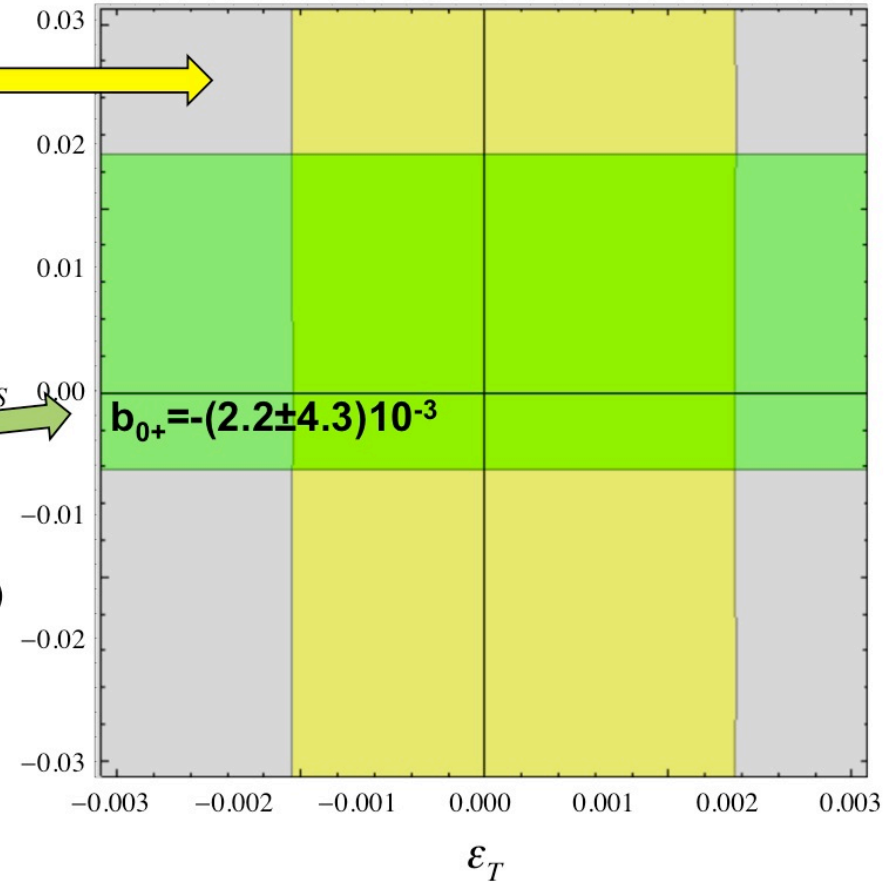
$f_T = 0.24(4)$
(Mateu & Portolés, 2007)

Superallowed nuclear β decays



$0.25 < g_S < 1.00$
 $0.60 < g_T < 2.30$
(Adler'1975, Herczeg'2001)

ϵ_S



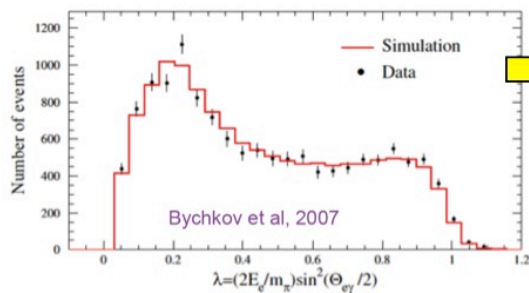
* Pion decay (R_π) also very powerful!

**Other nuclear decays getting close...

$$R_\pi \equiv \frac{\Gamma(\pi \rightarrow e\nu)}{\Gamma(\pi \rightarrow \mu\nu)}$$

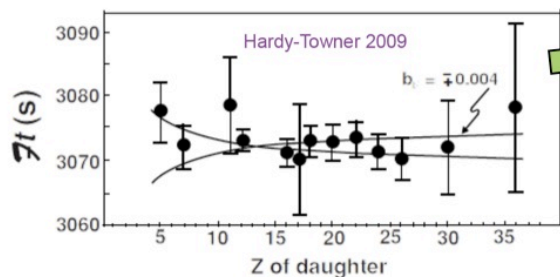
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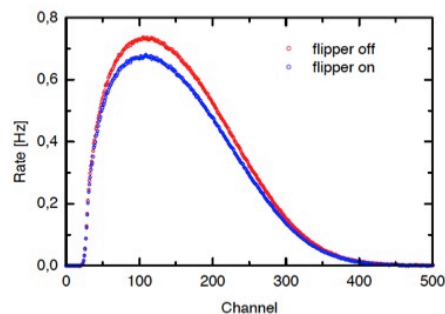
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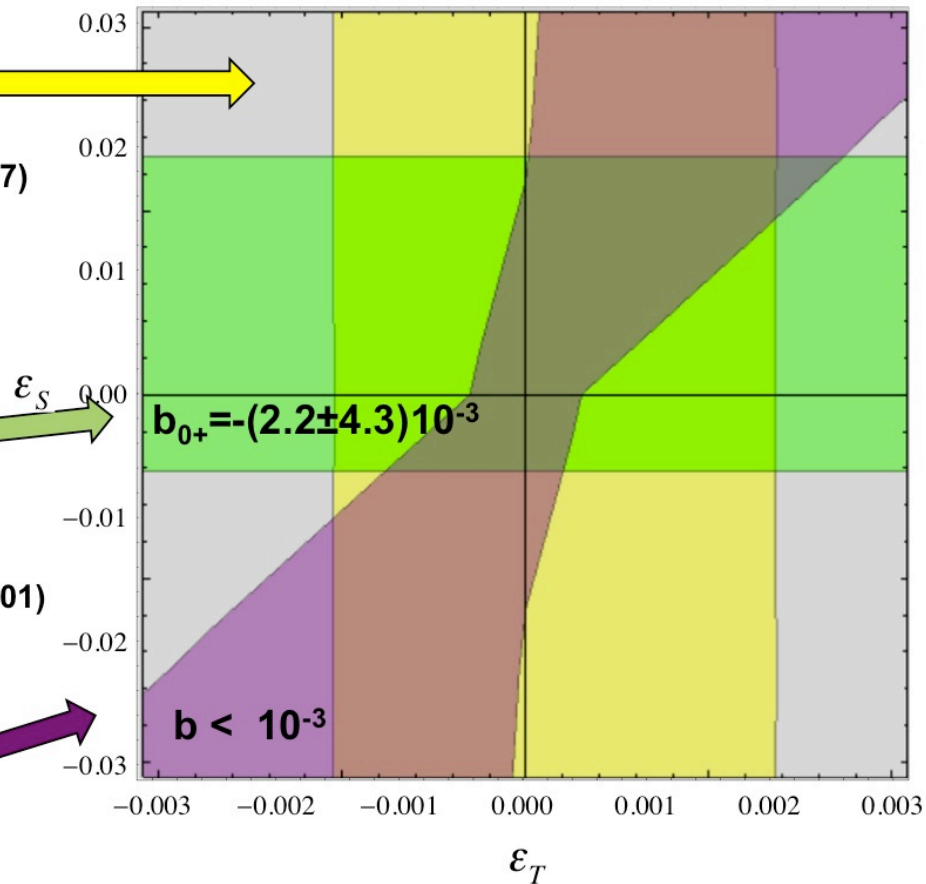


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Future neutron decay exp.

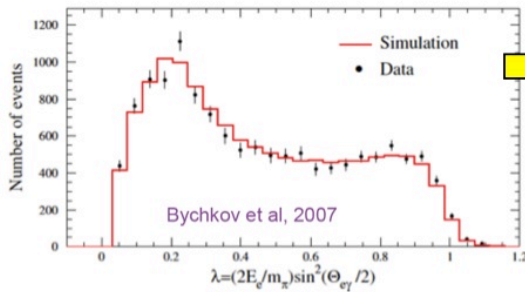


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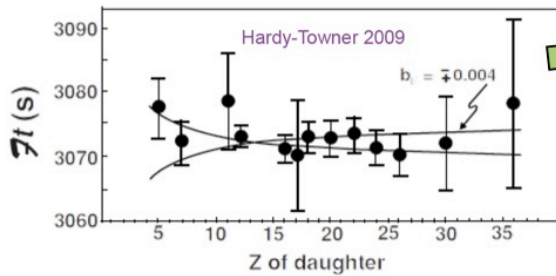
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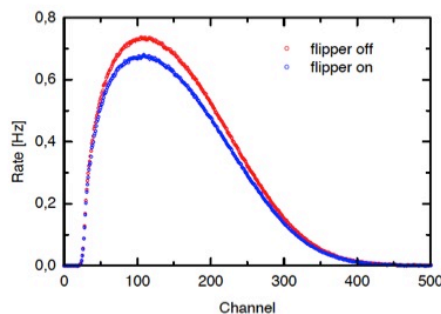
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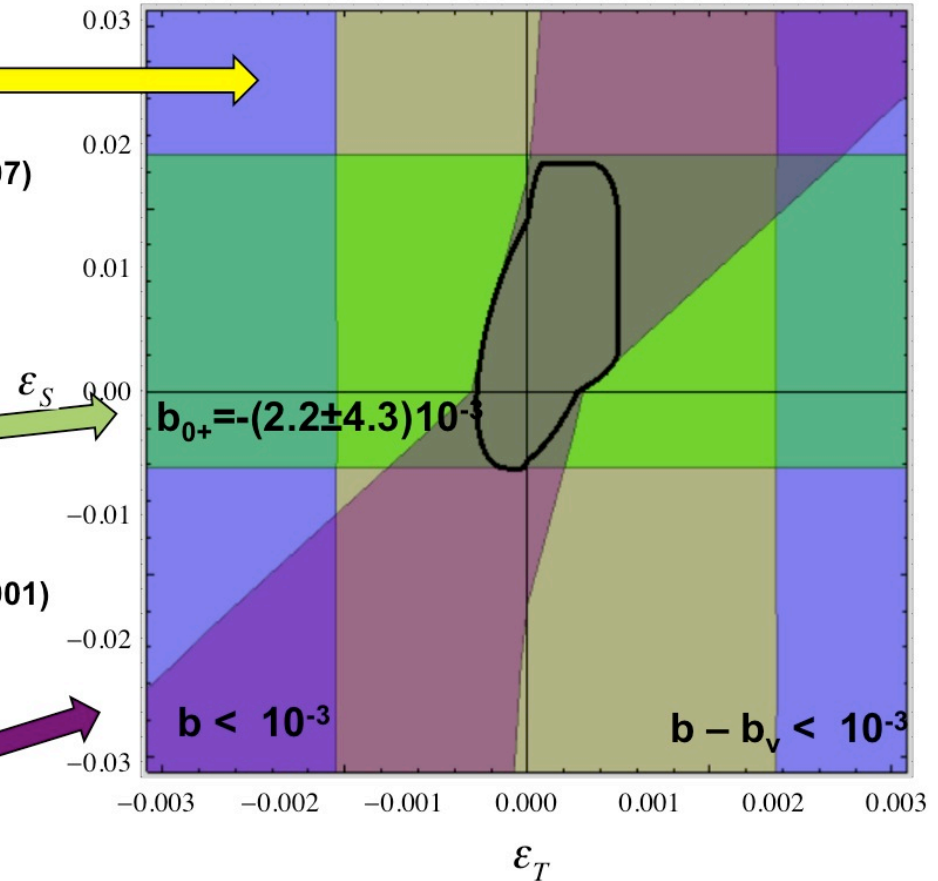


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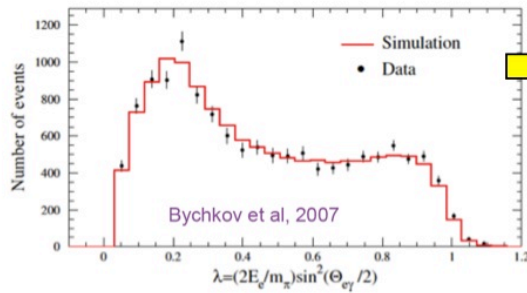


$b \approx 0.3 g_S \epsilon_S - 5.0 g_T \epsilon_T$
 $b_V - b \approx 0.1 g_S \epsilon_S - 0.3 g_T \epsilon_T$



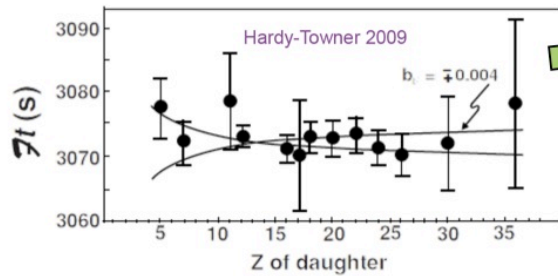
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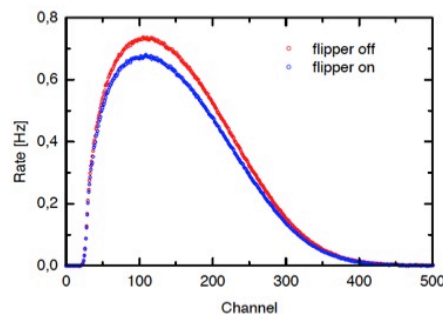
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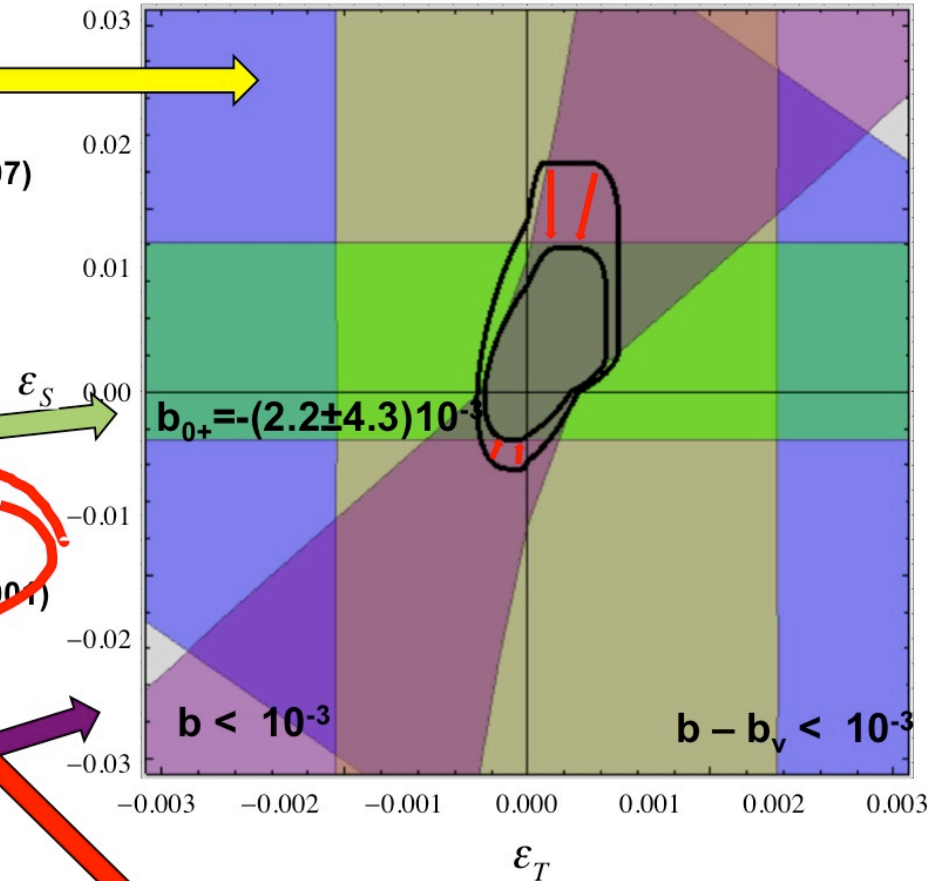


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LATTICE QCD!!

PNDME Coll.:

T. Bhattacharya, S. Cohen, R. Gupta, A. Joseph, H.W. Lin

$g_S = 1.05(35)$ $g_T = 0.8(4)$
(Bhattacharya et al. '2012)

NP bounds from low-energy searches

CKM unitarity tests

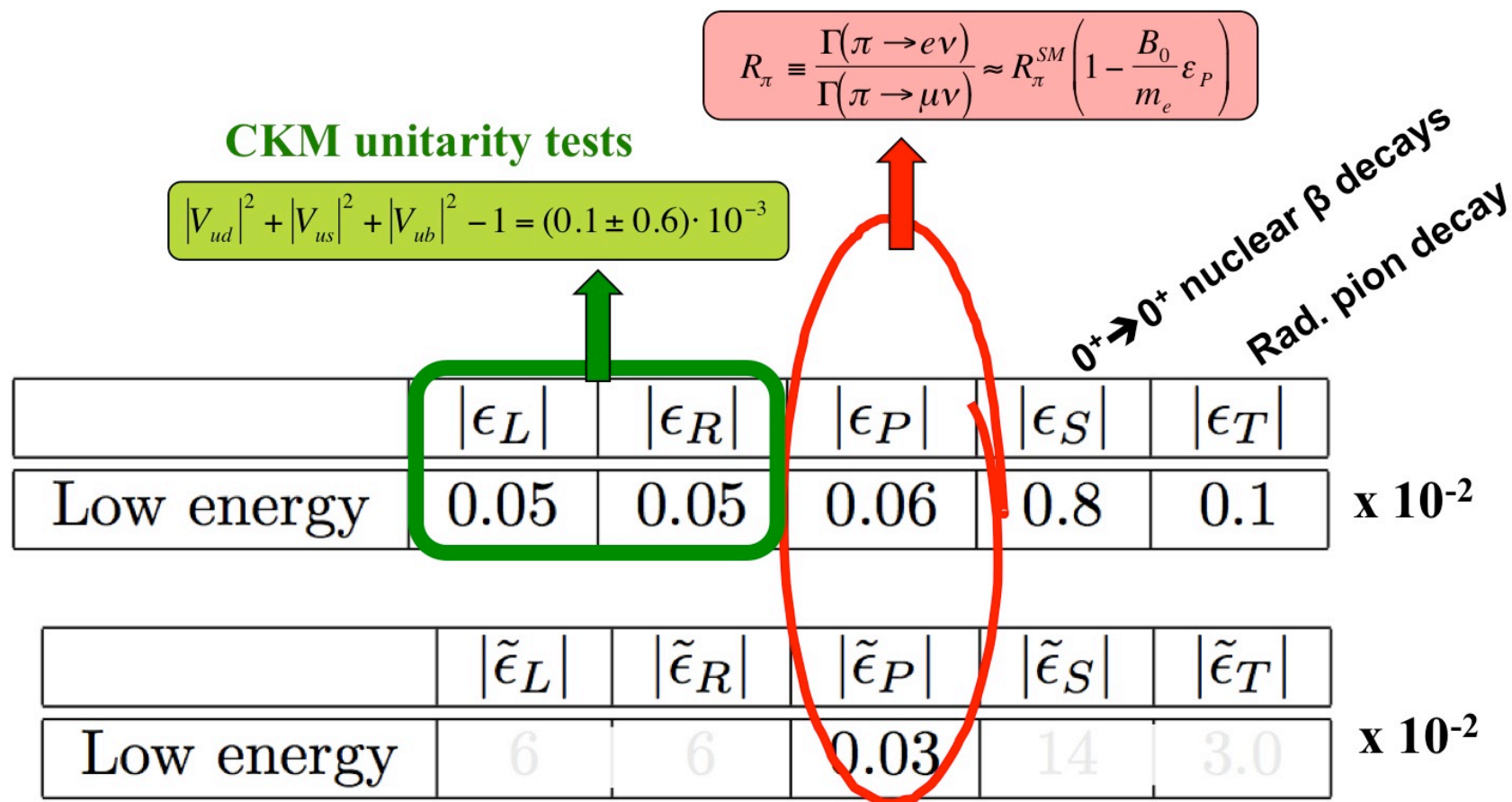
$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 - 1 = (0.1 \pm 0.6) \cdot 10^{-3}$$

	$ \epsilon_L $	$ \epsilon_R $	$ \epsilon_P $	$ \epsilon_S $	$ \epsilon_T $	
Low energy	0.05	0.05	0.06	0.8	0.1	$\times 10^{-2}$

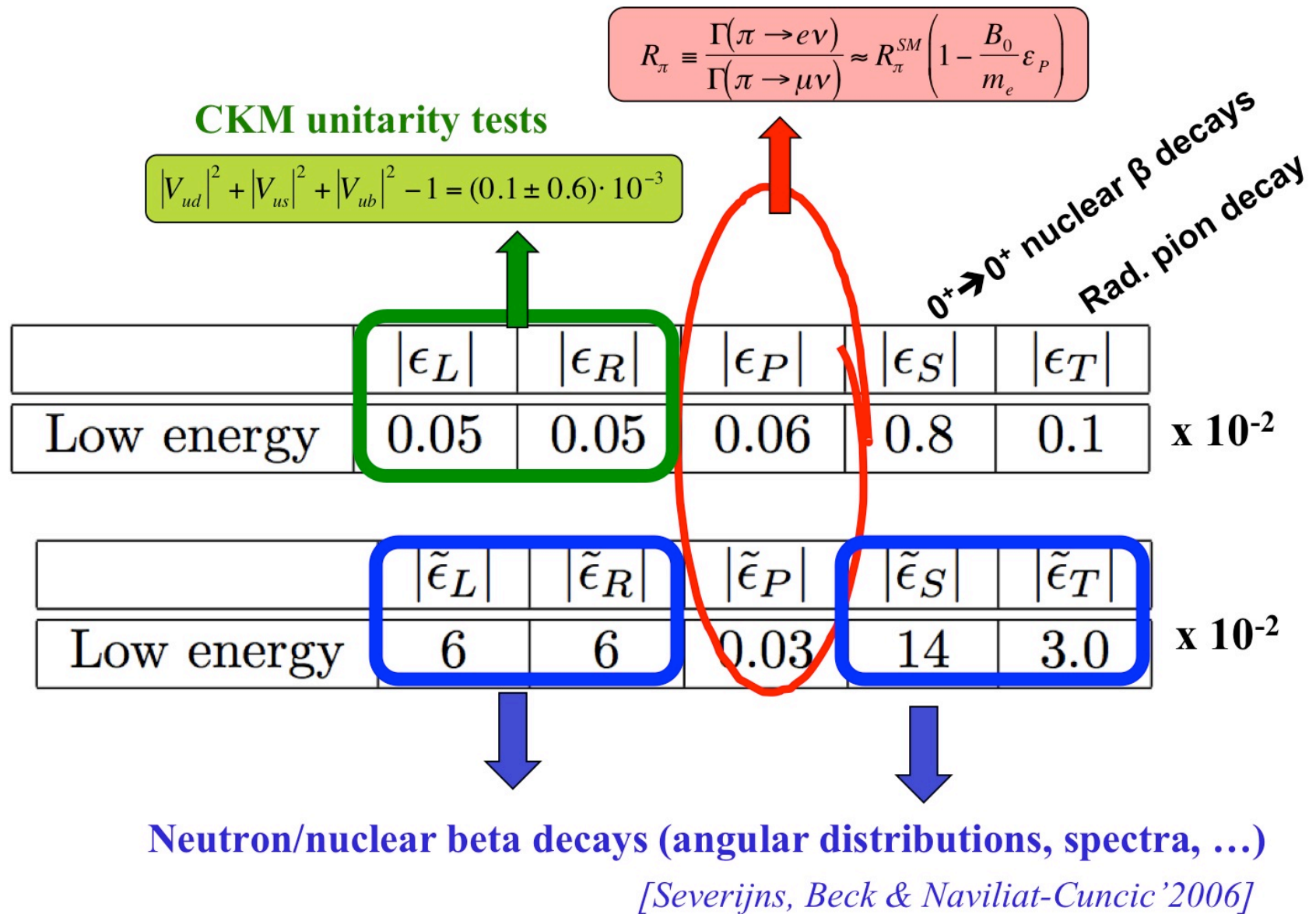
$0^+ \rightarrow 0^+$ nuclear β decays
Rad. pion decay

	$ \tilde{\epsilon}_L $	$ \tilde{\epsilon}_R $	$ \tilde{\epsilon}_P $	$ \tilde{\epsilon}_S $	$ \tilde{\epsilon}_T $	
Low energy	6	6	0.03	14	3.0	$\times 10^{-2}$

NP bounds from low-energy searches



NP bounds from low-energy searches



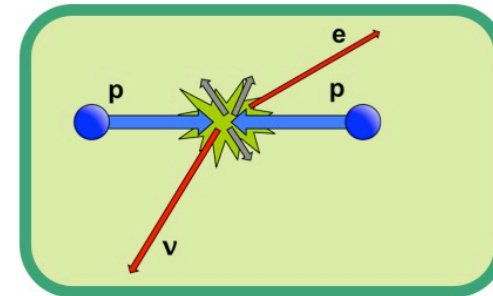
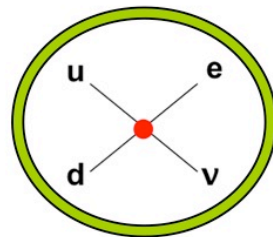
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- Introduction and motivation; ✓
- EFT approach; ✓
- Low-energy bounds: ✓
- LHC bounds.

LHC limits on $\epsilon_{S,T}$



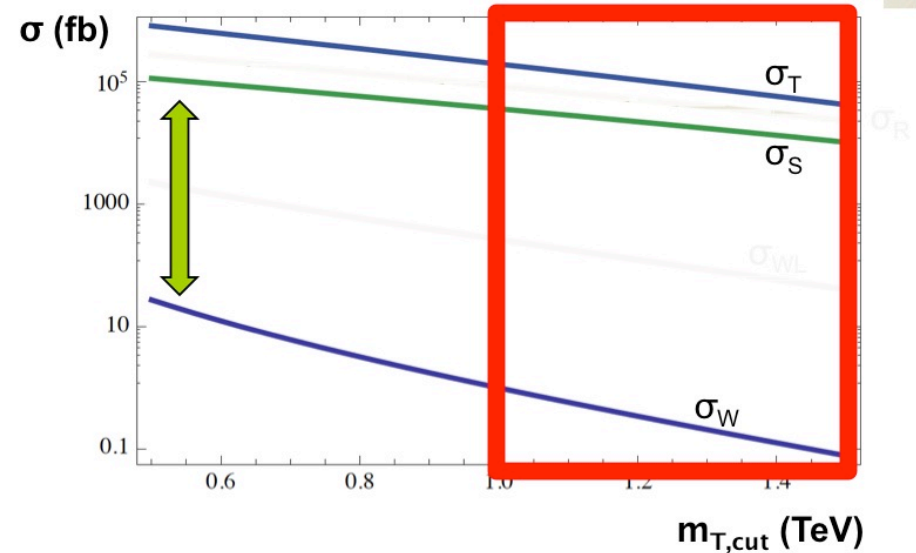
- EFT approach:



- To suppress the bkg, we look for $(e+\nu)$ -events with high m_T :

$$N_{pp \rightarrow e\nu X}(m_T^2 > m_{T,cut}^2) = \epsilon \times L \times \sigma_{pp \rightarrow e\nu X}(m_T^2 > m_{T,cut}^2) = \epsilon \times L \times (\sigma_W + \sigma_S \epsilon_S^2 + \sigma_T \epsilon_T^2)$$

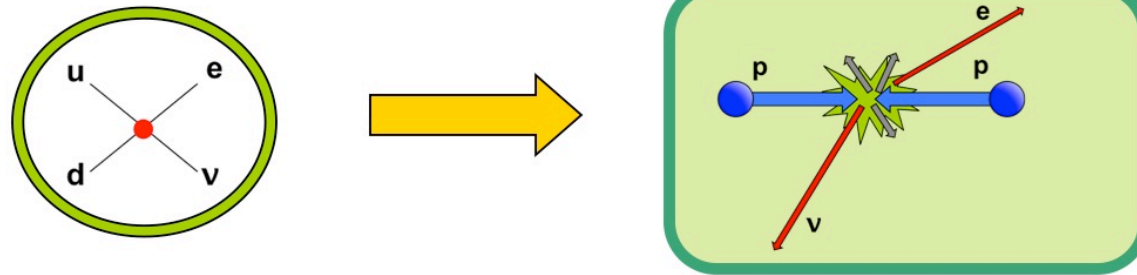
$$m_T \equiv \sqrt{2E_T^e E_T^\nu (1 - \cos \Delta\phi_{e\nu})}$$



LHC limits on $\epsilon_{S,T}$

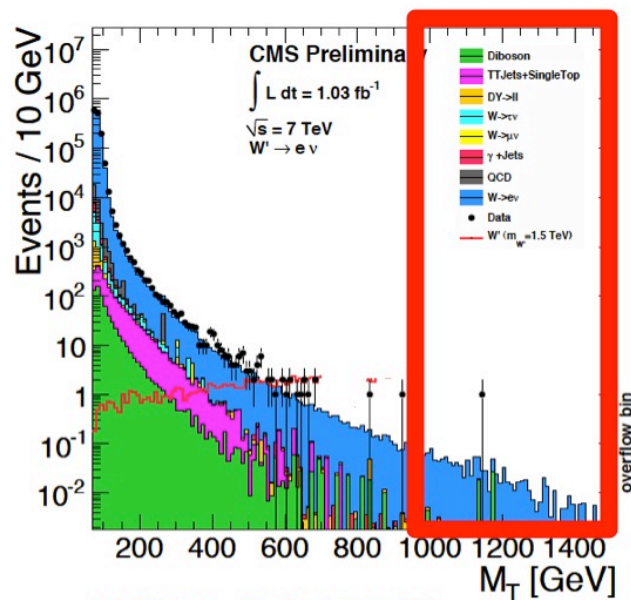


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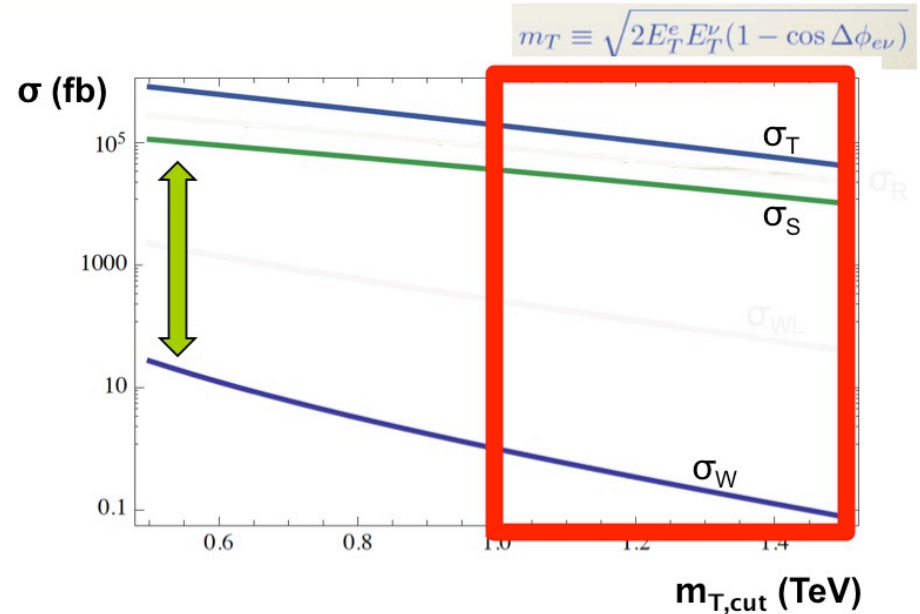


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(CMS 1 fb⁻¹, 7 TeV)

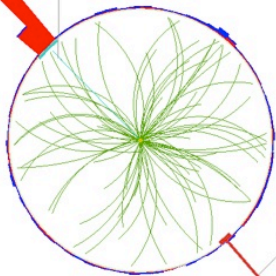


LHC limits on $\epsilon_{S,T}$

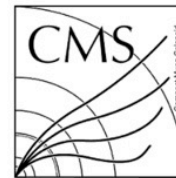


CMS Experiment at LHC, CERN
Data recorded: Wed Sep 21 11:35:51 2011 CEST
Run/Event: 176841 / 213192769
Lumi section: 189
Orbit/Crossing: 49420229 / 1640

Electron pt: 799.5 GeV

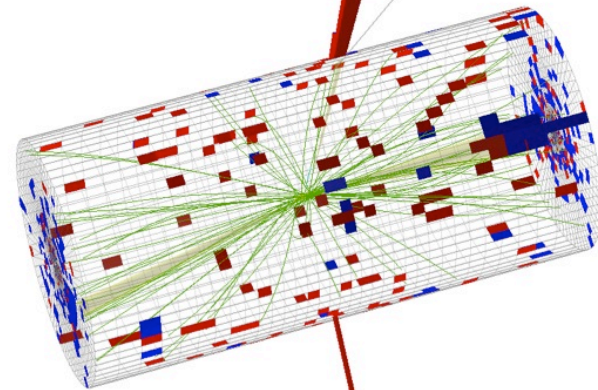


pfMet: 822.2 GeV



CMS Experiment at LHC, CERN
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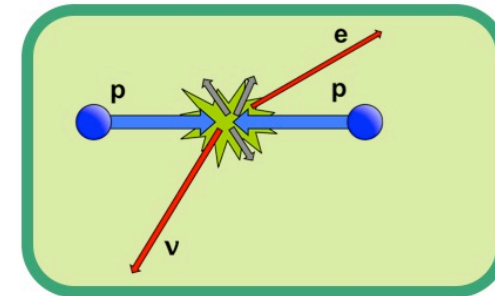
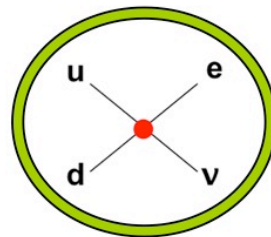


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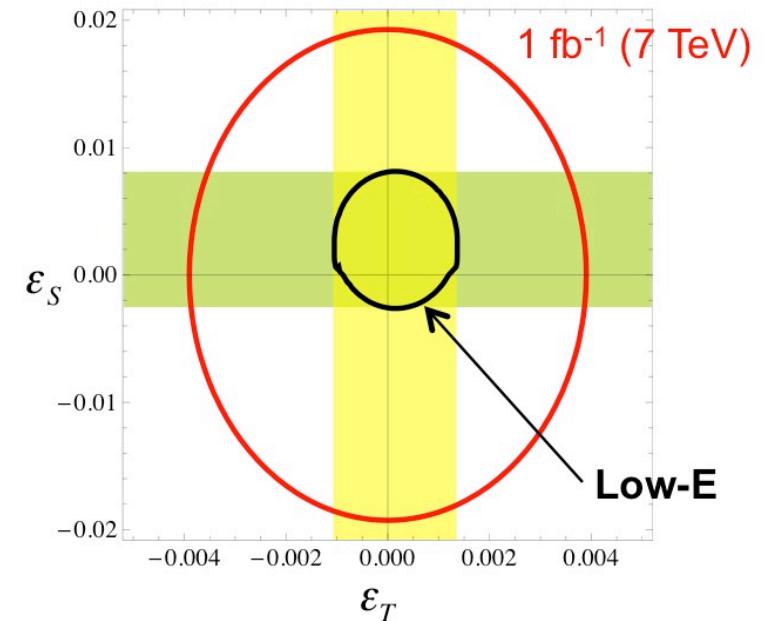
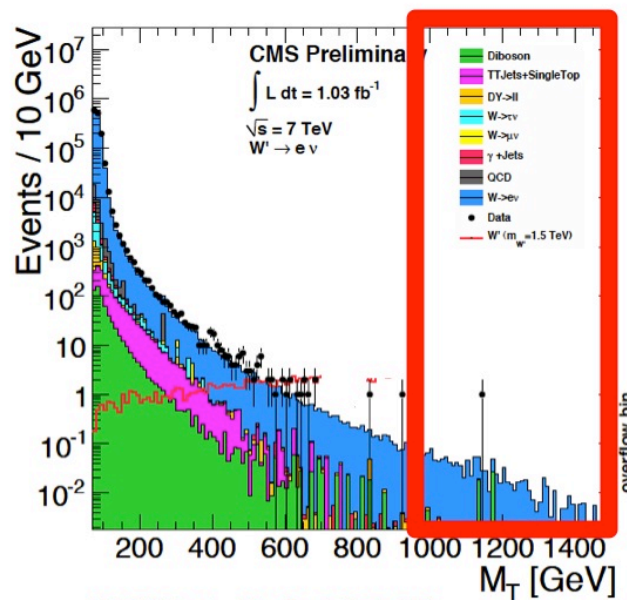


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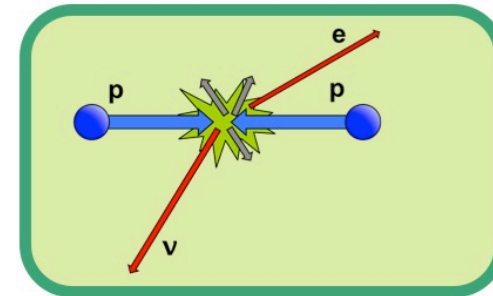
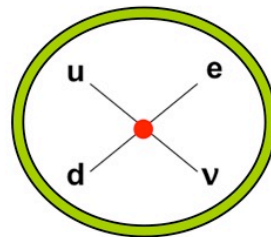
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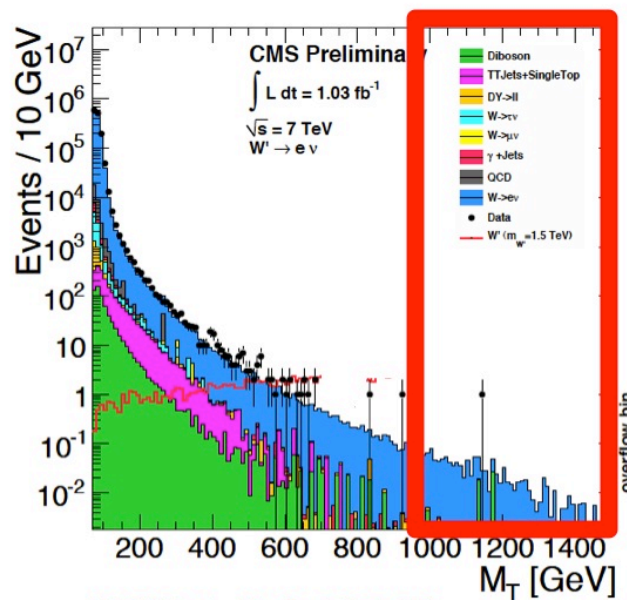


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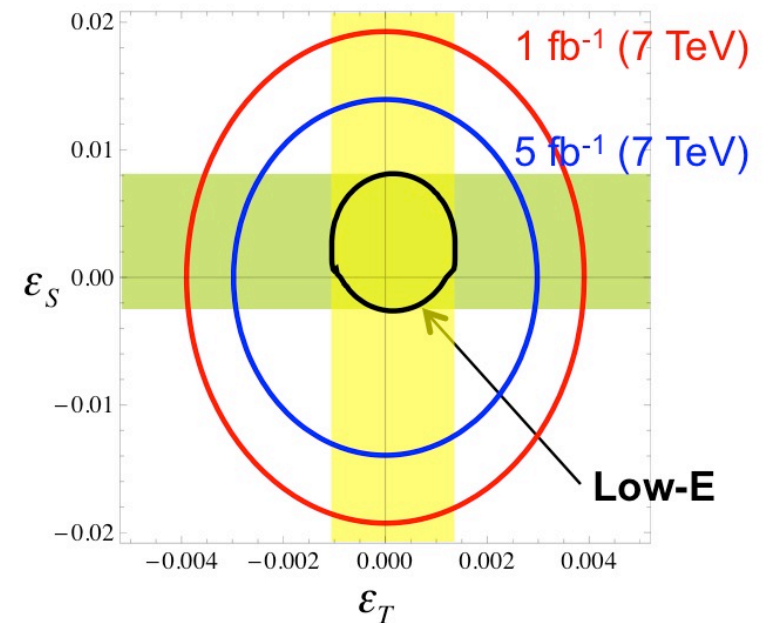


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$$N_{pp \rightarrow e\nu X}(m_T^2 > m_{T,cut}^2) = \epsilon \times L \times \sigma_{pp \rightarrow e\nu X}(m_T^2 > m_{T,cut}^2) = \epsilon \times L \times (\sigma_W + \sigma_S \epsilon_S^2 + \sigma_T \epsilon_T^2)$$



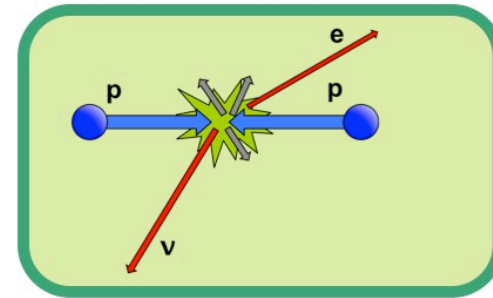
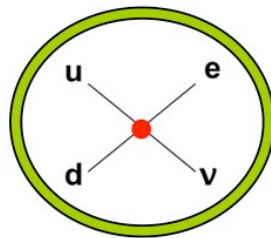
(CMS 1 fb⁻¹, 7 TeV)



LHC limits on $\epsilon_{S,T}$

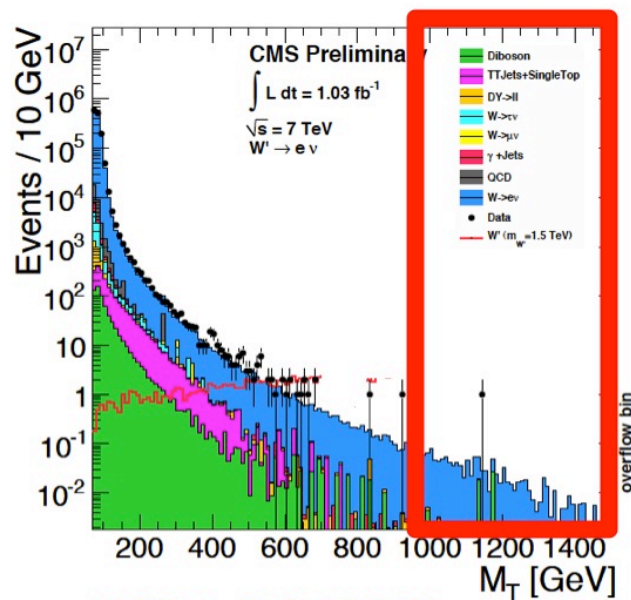


- EFT approach:

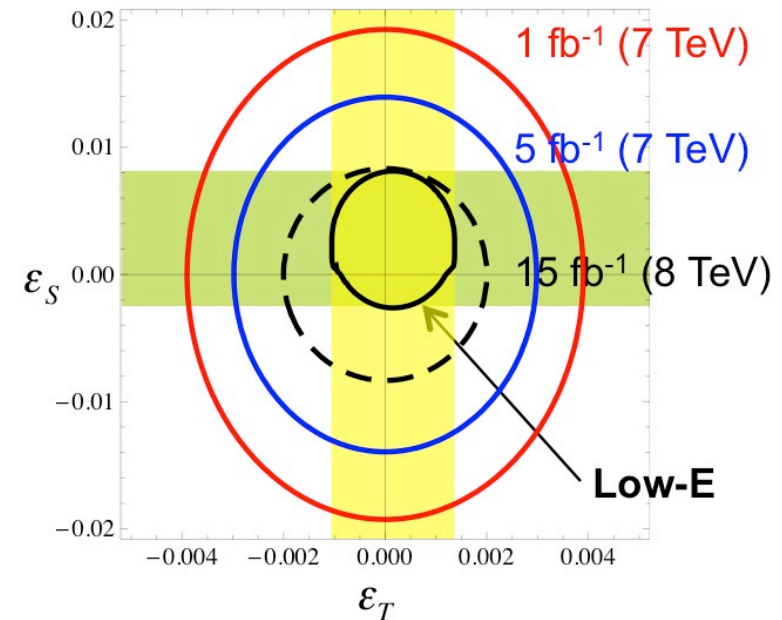


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(CMS 1 fb⁻¹, 7 TeV)

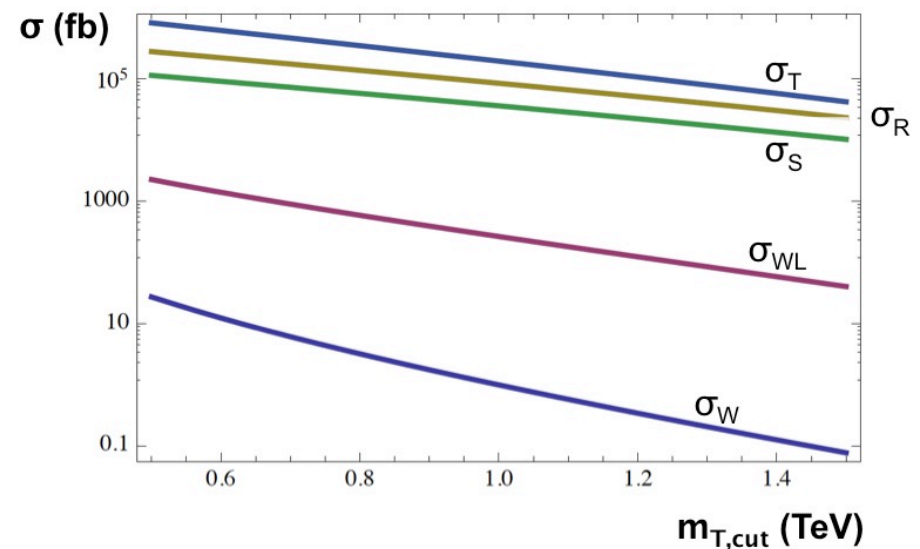


What about the other ϵ_x ?



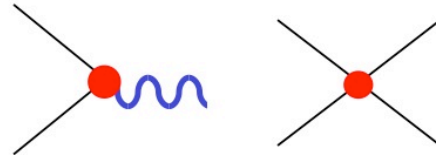
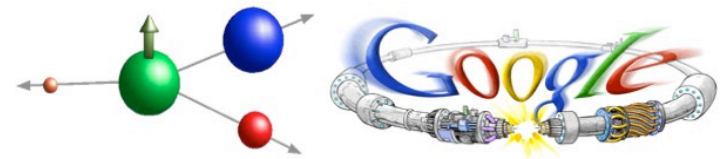
$$\begin{aligned}\sigma(m_T > \bar{m}_T) &= \sigma_W \left[(1 + \epsilon_L^{(v)})^2 + |\tilde{\epsilon}_L|^2 + |\epsilon_R|^2 \right] - 2\sigma_{WL} \epsilon_L^{(c)} (1 + \epsilon_L^{(v)}) \\ &+ \sigma_R \left[|\tilde{\epsilon}_R|^2 + |\epsilon_L^{(c)}|^2 \right] + \sigma_S \left[|\epsilon_S|^2 + |\tilde{\epsilon}_S|^2 + |\epsilon_P|^2 + |\tilde{\epsilon}_P|^2 \right] \\ &+ \sigma_T \left[|\epsilon_T|^2 + |\tilde{\epsilon}_T|^2 \right],\end{aligned}$$

- Strong bounds on S, T, P with LH neutrinos.
- Strong bounds on S, P, T, V+A with RH neutrinos;
- LHC not sensitive to the rest of couplings.



[Cirigliano, MGA & Graesser, 2012]

β decays vs. the LHC

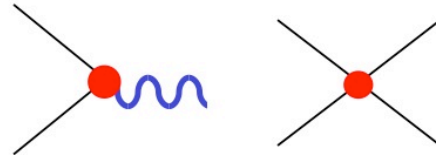
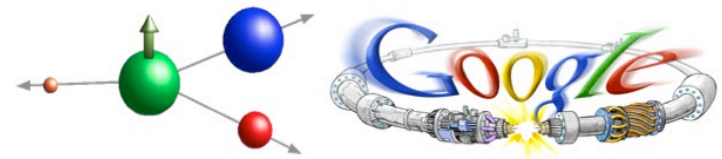


	$ \epsilon_L^{(v)} $	$\epsilon_L^{(c)}$	$ \epsilon_R $	$ \epsilon_P $	$ \epsilon_S $	$ \epsilon_T $	
Low energy	0.05	0.05	0.05	0.06	0.8	0.1	$\times 10^{-2}$
LHC ($e\nu$)	-	(-0.3, +0.8)	-	1.3	1.3	0.3	$\times 10^{-2}$

Interesting competition

	$ \tilde{\epsilon}_L $	$ \tilde{\epsilon}_R $	$ \tilde{\epsilon}_P $	$ \tilde{\epsilon}_S $	$ \tilde{\epsilon}_T $	
Low energy	6	6	0.03	14	3.0	$\times 10^{-2}$
LHC ($e\nu$)	-	0.5	1.3	1.3	0.3	$\times 10^{-2}$

β decays vs. the LHC



	$ \epsilon_L^{(\nu)} $	$\epsilon_L^{(e)}$	$ \epsilon_R $	$ \epsilon_P $	$ \epsilon_S $	$ \epsilon_T $	
Low energy	0.05	0.05	0.05	0.06	0.8	0.1	$\times 10^{-2}$
LHC ($e\nu$)	-	(-0.3, +0.8)	-	1.3	1.3	0.3	$\times 10^{-2}$

Low energy dominates!

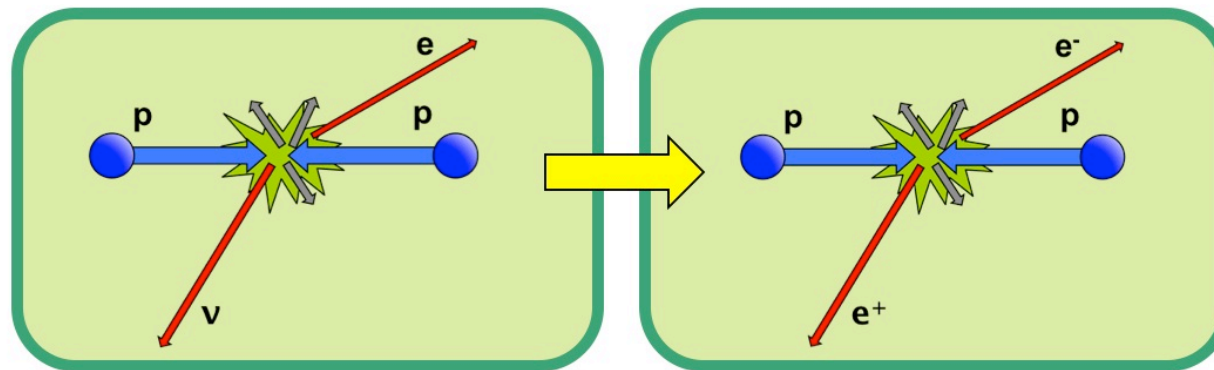
Interesting competition

	$ \tilde{\epsilon}_L $	$ \tilde{\epsilon}_R $	$ \tilde{\epsilon}_P $	$ \tilde{\epsilon}_S $	$ \tilde{\epsilon}_T $	
Low energy	6	6	0.03	14	3.0	$\times 10^{-2}$
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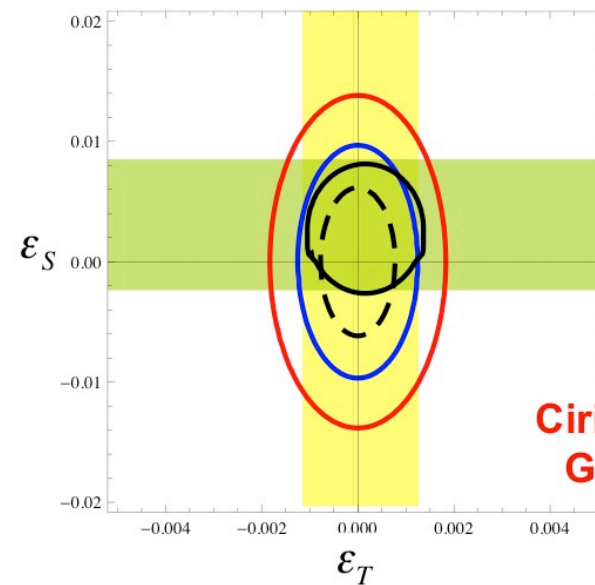
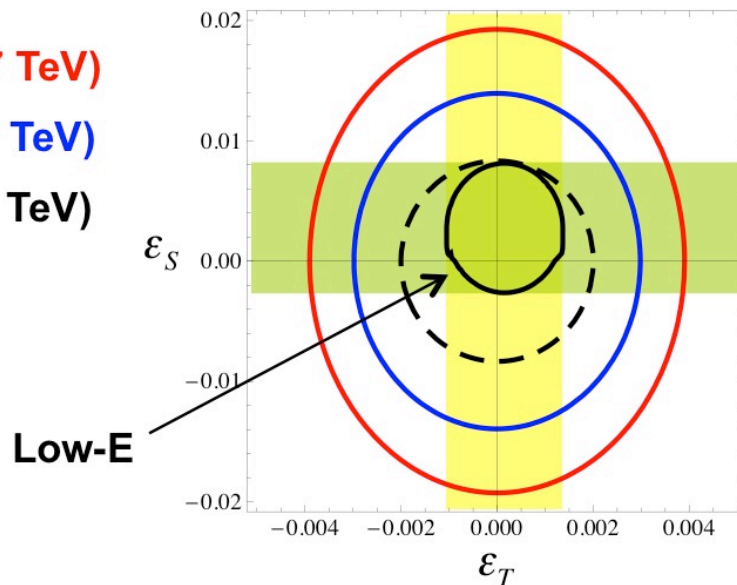
LHC dominates!

Beyond the $pp \rightarrow e\nu X$ channel

- Using SU(2) gauge invariance, we can also extract bounds from...



1 fb⁻¹ (7 TeV)
5 fb⁻¹ (7 TeV)
15 fb⁻¹ (8 TeV)



Cirigliano, MGA & Graesser, 2012

What if we see sth?

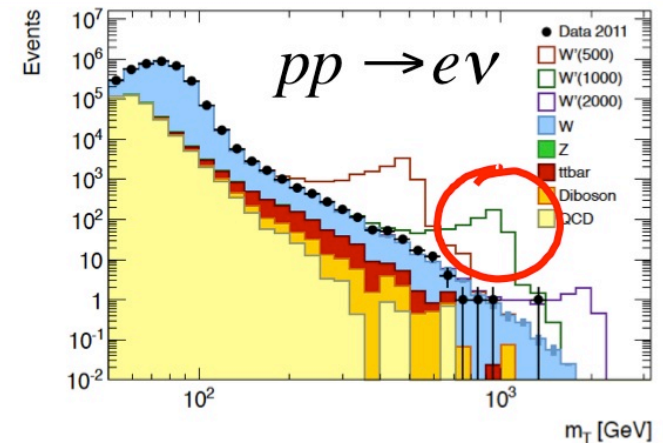
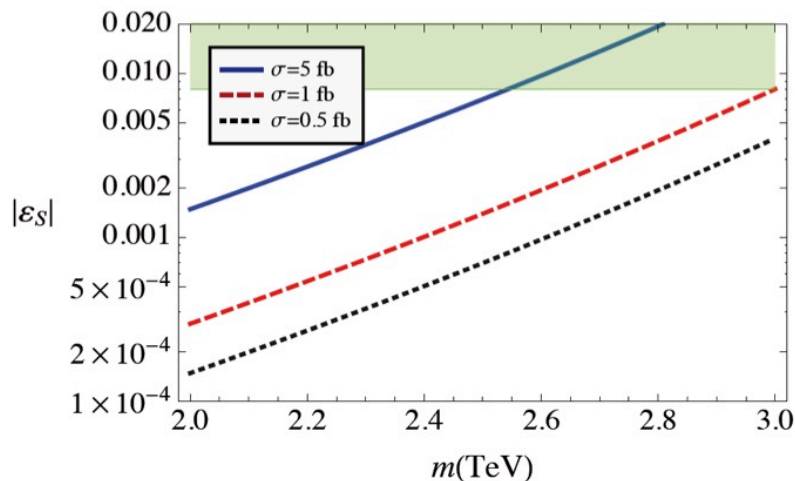


- What if we see a bump? EFT breaks down...
TOY model: scalar resonance:

$$\mathcal{L} = \lambda_S V_{ud} \phi^+ \bar{u} d + \lambda_l \phi^- \bar{e} P_L \nu_e$$

- Then we have a lower-limit value for ϵ_S :

$$\sigma \cdot \text{BR} \leq \frac{|V_{ud}|}{12v^2} \frac{\pi}{\sqrt{2N_c}} |\epsilon_S| \tau L(\tau)$$



$$L(\tau) = \int_{\tau}^1 dx f_q(x) f'_q(\tau/x)/x$$

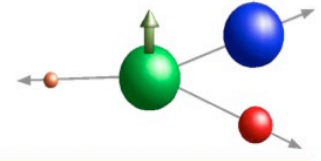
$$\tau = m^2/s$$

$$\epsilon_S = 2\lambda_S \lambda_l \frac{v^2}{m^2}$$

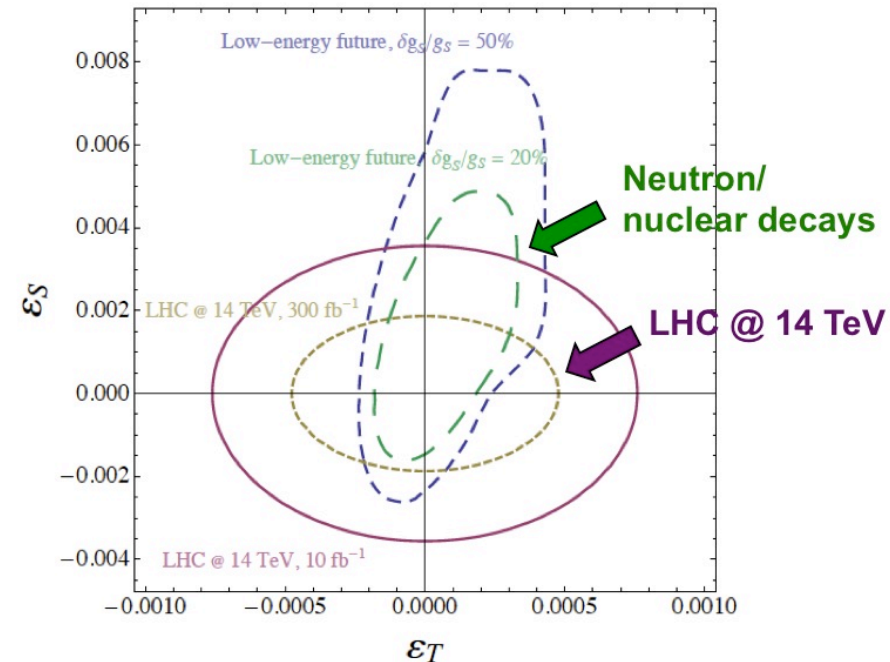
Nice interplay of two experiments separated for so many orders of magnitudes!!!!

(T. Battacharya et al., 2012)

Conclusions



- Connecting HEP and β decays: EFT approach (heavy mediators);
- β decays are exploring the TeV scale!
- Both LHC & low-energy searches needed to get a complete picture.
- Needless to say, this interplay becomes way more interesting if we see a NP signal!



Backup slides

The eff. Lagrangian for $E \sim 1$ GeV

[Cirigliano, MGA & Jenkins, Nucl. Phys B830 (2010)]

- Beta decay: $d^j \rightarrow u^i \bar{\nu}_l$

$$\mathbf{L}_{d^j \rightarrow u^i \bar{\nu}_l}^{eff}(x) = \frac{-g^2}{2m_W^2} V_{ij} \left[\begin{aligned} & (1 + \epsilon_L) \overline{(u^i \gamma^\mu d^j)}_{L} \overline{(\bar{l} \gamma_\mu \nu_{lL})} + \epsilon_R \overline{(u^i \gamma^\mu d^j)}_{R} \overline{(\bar{l} \gamma_\mu \nu_{lL})} \\ & + \epsilon_L^S \overline{(u^i d^j)}_{R} \overline{(\bar{l} \nu_{lL})} + \epsilon_R^S \overline{(u^i d^j)}_{L} \overline{(\bar{l} \nu_{lL})} \\ & + \epsilon_T \overline{(u^i \sigma^{\mu\nu} d^j)}_{R} \overline{(\bar{l} \sigma_{\mu\nu} \nu_{lL})} \end{aligned} \right] + h.c.$$

where...

$$\begin{aligned} V_{ij} \cdot [\epsilon_L]_{llij} &= 2 V_{ij} [\hat{\alpha}_{\varphi l}^{(3)}]_{ll} + 2 V_{im} [\hat{\alpha}_{\varphi q}^{(3)}]_{jm}^* - 2 V_{im} [\hat{\alpha}_{lq}^{(3)}]_{llmj} \\ V_{ij} \cdot [\epsilon_R]_{llij} &= -[\hat{\alpha}_{\varphi\varphi}]_{ij} \\ V_{ij} \cdot [\epsilon_L^S]_{llij} &= -[\hat{\alpha}_{lq}]_{llji}^* \\ V_{ij} \cdot [\epsilon_R^S]_{llij} &= -V_{im} [\hat{\alpha}_{qde}]_{lljm}^* \\ V_{ij} \cdot [\epsilon_T]_{llij} &= -[\hat{\alpha}_{lq}^t]_{llji}^* \end{aligned}$$

CKM tests vs. HEP

[Cirigliano, MGA & Jenkins, Nucl. Phys B830 (2010)]

$$\Delta_{CKM} = 4 \left(-\hat{\alpha}_{\phi l}^{(3)} + \hat{\alpha}_{\phi q}^{(3)} - \hat{\alpha}_{lq}^{(3)} + \hat{\alpha}_{ll}^{(3)} \right) = -(1 \pm 6) \cdot 10^{-4}$$

$$O_{ll}^{(3)} = \frac{1}{2} (\bar{l} \gamma^\mu \sigma^a l) (\bar{l} \gamma_\mu \sigma^a l)$$

$$O_{lq}^{(3)} = (\bar{l} \gamma^\mu \sigma^a l) (\bar{q} \gamma_\mu \sigma^a q)$$

$$O_\phi^{(3)} = i (\phi^\dagger D^\mu \sigma^a \phi) (\bar{l} \gamma_\mu \sigma^a l) + \text{h.c.},$$

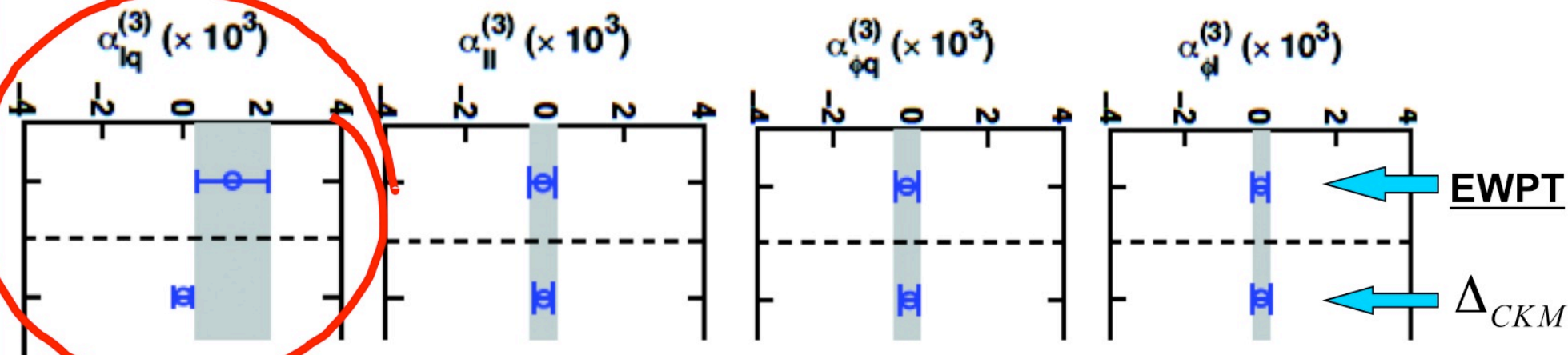
$$O_\phi^{(3)} = i (\phi^\dagger D^\mu \sigma^a \phi) (\bar{q} \gamma_\mu \sigma^a q) + \text{h.c.}$$

What did we know about them from colliders and other EWPT?

Han & Skiba, PRD71, 2005:

$$4 \left(-\bar{\alpha}_{\phi l}^{(3)} + \bar{\alpha}_{\phi q}^{(3)} - \bar{\alpha}_{lq}^{(3)} + \bar{\alpha}_{ll}^{(3)} \right) = -(4.7 \pm 2.9) \cdot 10^{-3}$$

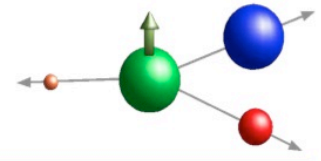
5 times less precise!



M. González-Alonso

β decays vs. the LHC

Angular/Energy distribution



$$\mathcal{L}_{n \rightarrow pe^- \bar{\nu}_e} \sim \bar{e}_L \gamma_\mu \nu_L \cdot \bar{p} \left(\gamma^\mu - \tilde{\lambda}_A \gamma^\mu \gamma_5 \right) n + \lambda_S \epsilon_S \bar{e}_R \nu_L \cdot \bar{p} n + 2\lambda_T \epsilon_T \bar{e}_R \sigma_{\mu\nu} \nu_L \cdot \bar{p} \sigma^{\mu\nu} n_L$$



(spectrum)

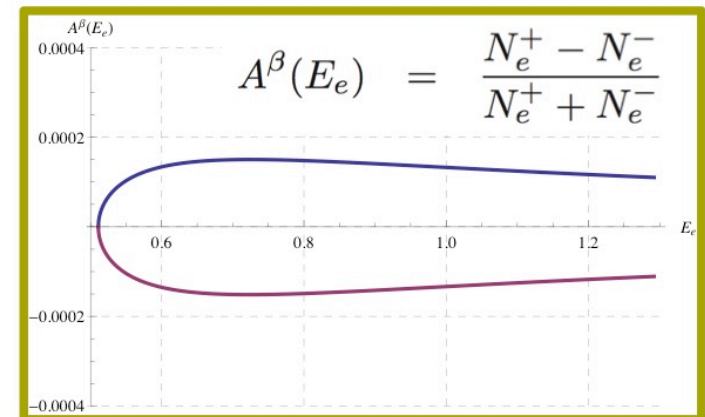
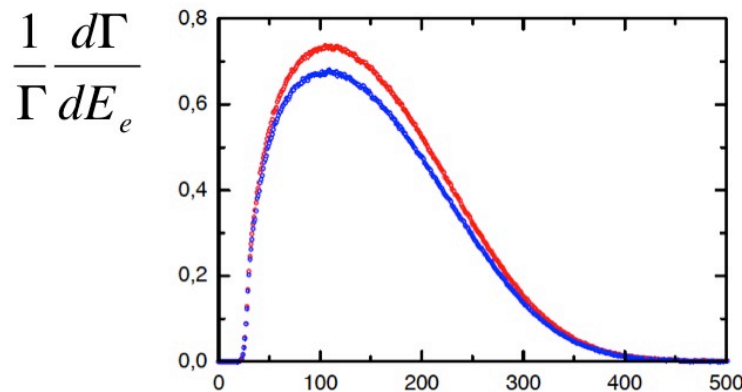
Angular distribution altered... and E-dependent!

$$\frac{d\Gamma(\mathbf{J})}{dE_e d\Omega_e d\Omega_\nu} \sim \xi(E) \left(1 + b \frac{m_e}{E_e} \right) \left\{ 1 + a \left(1 - b \frac{m_e}{E_e} \right) \frac{\mathbf{p}_e \cdot \mathbf{p}_\nu}{E_e E_\nu} + A \left(1 - b \frac{m_e}{E_e} \right) \frac{\mathbf{p}_e \mathbf{J}}{E_e J} + \left(B + (b_B - b) \frac{m_e}{E_e} \right) \frac{\mathbf{p}_\nu \mathbf{J}}{E_\nu J} \right\}$$

(Jackson, Treiman & Wyld, 1957)

$$b \approx 0.3 \lambda_S \epsilon_S - 5.0 \lambda_T \epsilon_T$$

$$b_B - b \approx 0.1 \lambda_S \epsilon_S - 0.3 \lambda_T \epsilon_T$$



S & T bounds from low-E searches

□ Pion decay $R_\pi \equiv \frac{\Gamma(\pi \rightarrow e\nu)}{\Gamma(\pi \rightarrow \mu\nu)}$

- Strong limits on the flavor structure of ϵ_P :

$$\frac{R_\pi}{R_\pi^{\text{SM}}} = \frac{\left[\left(1 - \frac{B_0}{m_e} \epsilon_P^{ee}\right)^2 + \left(\frac{B_0}{m_e} \epsilon_P^{e\mu}\right)^2 + \left(\frac{B_0}{m_e} \epsilon_P^{e\tau}\right)^2 \right]}{\left[\left(1 - \frac{B_0}{m_\mu} \epsilon_P^{\mu\mu}\right)^2 + \left(\frac{B_0}{m_\mu} \epsilon_P^{\mu e}\right)^2 + \left(\frac{B_0}{m_\mu} \epsilon_P^{\mu\tau}\right)^2 \right]}$$

$$-1.4 \times 10^{-7} < \epsilon_P^{ee} < 5.5 \times 10^{-4}$$

Where...

$$\mathcal{L}_{\text{eff}} \supset \frac{G_F}{\sqrt{2}} V_{ud} \epsilon_P^{\alpha\beta} \bar{e}_\alpha (1 - \gamma_5) \nu_\beta \cdot \bar{u} \gamma_5 d$$

$$B_0(\mu) \equiv \frac{M_\pi^2}{m_u(\mu) + m_d(\mu)}$$

- S, T generate P through loops:
(Voloshin'92, Campbell-Maybury'05)

$$|\epsilon_T| \leq 10^{-5} - 10^{-3}$$

$$|\epsilon_S| \leq 10^{-3} - 10^{-1}$$

$$\frac{-1.4 \times 10^{-7}}{\log(\Lambda/\mu)} < \gamma_{SP} \epsilon_S + \gamma_{TP} \epsilon_T < \frac{5.5 \times 10^{-4}}{\log(\Lambda/\mu)}$$

$$\gamma_{SP} = \frac{15}{72} \frac{\alpha_1}{\pi} \approx 6.7 \times 10^{-4}$$

$$\gamma_{TP} = -\frac{9}{2} \frac{\alpha_2}{\pi} - \frac{15}{2} \frac{\alpha_1}{\pi} \approx -7.3 \times 10^{-2}$$

*RH neutrinos can also make the job (Herczeg'94)

LHC limits on $\epsilon_{S,T}$



□ EFT approach:

$$N_{pp \rightarrow evX}(m_T^2 > m_{T,cut}^2) = \epsilon \times L \times \sigma_{pp \rightarrow evX}(m_T^2 > m_{T,cut}^2) = \epsilon \times L \times (\sigma_W + \sigma_S \epsilon_S^2 + \sigma_T \epsilon_T^2)$$

□ Estimate of future bounds: assuming $n=0$ with $m_T > 2.5(4.0)$ TeV

- 14 TeV, 10 fb⁻¹;
- 14 TeV, 300 fb⁻¹;

Comment:

Sizable QCD running of $\epsilon_{S,T}$:

$$\epsilon_S(\mu = 2 \text{ GeV}) = 1.79 \epsilon_S(\mu = 1 \text{ TeV})$$

$$\epsilon_T(\mu = 2 \text{ GeV}) = 0.83 \epsilon_T(\mu = 1 \text{ TeV})$$

Bhattacharya et al.'2012

