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# News on $\gamma$ from $B \rightarrow DK$

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# Introduction and outline

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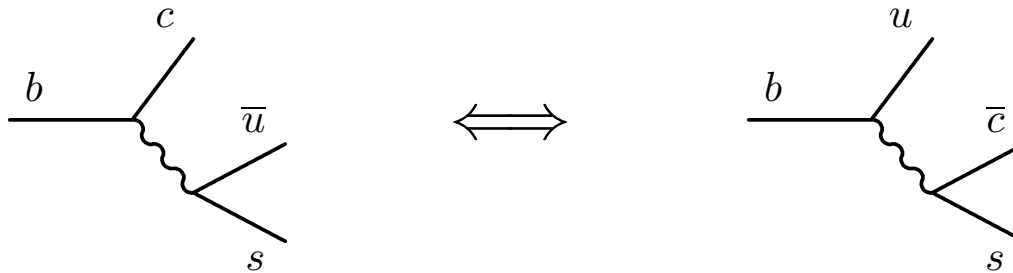
- We all know that  $B \rightarrow DK$  can be used to get  $\gamma$ , basically with no hadronic uncertainties
- On the theory side, what are the errors?
  - Charm mixing (old)
  - CPV in charm decay (new)
  - CPV in  $K_S$  decay (new)



# The basic of $B \rightarrow DK$

Gronau and Wyler

Use interference between  $b \rightarrow c\bar{u}s$  and  $b \rightarrow u\bar{c}s$



Interference between

$B^+ \rightarrow DK^+$  follows by  $D \rightarrow f$

$B^+ \rightarrow \bar{D}K^+$  follows by  $\bar{D} \rightarrow f$

$f$  can be any common final state to  $D$  and  $\bar{D}$

# Factorization and interference

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Why is  $B \rightarrow DK$  so clean?

Factorization and interference: they are both needed

- Interference: we need it in order to get CP violation
- Factorization: it helps us calculating

$$A(B \rightarrow \psi K_S \rightarrow (\mu^+ \mu^-)_\psi (\pi^+ \pi^-)_{K_S}) = \\ A(B \rightarrow \psi K_S) \times A(\psi \rightarrow \mu^+ \mu^-) \times A(K_S \rightarrow \pi^+ \pi^-)$$

Usually, these two do not come together

# $B \rightarrow DK$ : both

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$B \rightarrow DK$  is clean: we have factorization and interference

- $B \rightarrow DK$  and  $D \rightarrow f_D$  amplitudes factorized
- $B \rightarrow DK$  and  $B \rightarrow \bar{D}K$  interfere
- Look for  $n$  different  $f_D$  states
- Look for  $k$  different  $B \rightarrow DK(X)$  decays
- $n + k$  amplitudes and  $n \times k$  observables

All hadronic parameters can be measured



No hadronic uncertainties

# Assumptions

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- Naively, there are several assumptions that are good to  $\text{few} \times 10^{-3}$ 
  - No charm mixing
  - One  $D$  decay amplitude
  - $K_S$  is a CP eigenstate
- How good these assumptions are?
- Can we correct for them?

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# Charm mixing

# Effect of charm mixing

YG, Soffer, Zupan, hep-ph/0505270; Bondar, Poluektov, Vorobiev, arXiv:1004.2350

- We assume the SM (always!)
- We expect correction of order  $x_D$  and  $y_D$

$$x \equiv \frac{\Delta m}{\Gamma} \sim 10^{-2} \quad y \equiv \frac{\Delta \Gamma}{2\Gamma} \sim 10^{-2}$$

- For CP conserving mixing, the effect is much smaller
  - $O(x^2, y^2)/r_D$  for ADS
  - Very small in Dalitz.  $r_B x$  if charm data is used
- It can be corrected for
- Overall, it does not seem to be a problem



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# CPV in charm decay

# Direct CPV

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- CP violation in SCS decays is of order  $\text{few} \times 10^{-3}$
- Again, we assume the SM, and assume that the data is explained by the SM
- We expect corrections of order  $a_{\text{CP}}$
- Relevant only to cases when the  $D$  decays to a SCS final state
- The effect is enhanced by  $1/r_B$
- While the effect is at the 1% level it not a big worry:
  - In principle it can be corrected (GLW becomes ADS)
  - The effect cancels to a large degree when we add  $K^+ K^-$  and  $\pi^+ \pi^-$

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# CPV in kaons

# Kaons CPV

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Before we get to  $B \rightarrow DK$ , look at  $\tau^- \rightarrow K_S \pi^- \nu$ . We define

$$A_\tau \equiv \frac{\Gamma(\tau^+ \rightarrow \pi^+ K_S \bar{\nu}_\tau) - \Gamma(\tau^- \rightarrow \pi^- K_S \nu_\tau)}{\Gamma(\tau^+ \rightarrow \pi^+ K_S \bar{\nu}_\tau) + \Gamma(\tau^- \rightarrow \pi^- K_S \nu_\tau)}$$

- Babar reported an  $O(3\sigma)$  deviation from the SM

$$A_\tau = -(3.6 \pm 2.3 \pm 1.1) \times 10^{-3}$$

- The SM prediction is

$$A_\tau = +(3.6 \pm 0.1) \times 10^{-3}$$

- The discrepancy is not due to an odd numbers of sign mistakes

# Kaon induced CPV

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What we have is

$$\tau^+ \rightarrow K^0 \pi^+ \bar{\nu} \quad \tau^- \rightarrow \bar{K}^0 \pi^- \nu$$

We detect the kaon as  $K_S$

$$\langle K_S | K \rangle = p \quad \langle K_S | \bar{K} \rangle = q$$

Then we get an asymmetry

$$a_{\text{CP}} \propto |p|^2 - |q|^2 = 2\text{Re}(\epsilon_K) \approx 3.3 \times 10^{-3}$$

- What about  $K_L$ ?
- Both  $\tau \rightarrow K_S$  and  $\tau \rightarrow K_L$  have the same asymmetry. What is going on?

# Interference, $K_S$ and CPT

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- We cannot tag a  $K_S$ . We just see two pions
- There is a CPV effect due to the interference between  $K_S$  and  $K_L$
- Recall,  $K_S$  and  $K_L$  are not orthogonal states
- The CPV effect due to the interference is exactly twice that of  $K_S$  but with opposite sign. CPT is restored
- Experimentally, the effect due to  $K_S$  and interference terms are what was measured
- The SM prediction depends on the time cut. For Babar it is small correction, but can be important for LHCb

# Back to $B \rightarrow DK$

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- This effect is important when we have  $K_S$  somewhere
  - $B^0 \rightarrow DK_S$
  - $D \rightarrow K_S \pi^+ \pi^-$
- We expect it to be of order  $\epsilon_K$
- Depend on the cut
- Can be corrected for

Thus, while interesting theoretically, kaon CPV effects are not a big issue for  $\gamma$  determination

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# Conclusions



# Conclusions

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- $B \rightarrow DK$  is unique: theory errors are still much smaller than the experimental ones
- There are few theoretical uncertainties that are below the 1% level
- The only news I could think about is that these sources of uncertainties are much larger than what I used to think, but they are still negligible

