

# $|V_{us}|$ from hadronic $\tau$ decays

Elvira Gámiz



Universidad de Granada / CAFPE

**7th International Workshop on the CKM Unitarity Triangle**

- Cincinnati, Ohio (USA) September 28-October 2, 2012.

# Contents

1. Introduction
2.  $|V_{us}|$  from inclusive Cabibbo-suppressed hadronic  $\tau$  decays
3.  $|V_{us}|$  from exclusive  $B(\tau \rightarrow K\pi\nu)$
4.  $|V_{us}|$  from exclusive  $B(\tau \rightarrow K\nu)/B(\tau \rightarrow \pi\nu)$  and  $B(\tau \rightarrow K\nu)$
5. Summary of results and conclusions

# 1. Introduction

**Cabibbo-Kobayashi-Maskawa matrix element**  $|V_{us}|$

# Fundamental parameter of the Standard Model

\* Check unitarity in the first row of CKM matrix.

$$\Delta_{CKM} = |V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 - 1 = 0.9999(6) \quad \text{PDG2012}$$

fits to  $K_{l3}, K_{l2}$  exper. data and lattice results for  $f_+(0)^{K \rightarrow \pi}$  and  $f_K/f_\pi$

→  $\mathcal{O}(10 \text{ TeV})$  bound on the scale of new physics **M. Antonelli et al, 1005.2323.**

\* Input in UT analysis.

# Look for new physics effects in the comparison of  $|V_{us}|$  extracted from different processes: helicity suppressed  $K_{\mu 2}$ , helicity allowed  $K_{l3}$ , hadronic  $\tau$  decays.

# 1. Introduction

The  $\tau$  is the only lepton massive enough to decay into hadrons

→ **ideal ground to investigate hadronic weak currents.**

# Using high precision experimental measurements of **ALEPH, OPAL, Belle, BaBar** (see **I. Nugent's** talk)

$$R_\tau \equiv \frac{\Gamma[\tau^- \rightarrow \text{hadrons}(\gamma)]}{\Gamma[\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau(\gamma)]}$$

(and related observables  $dR_\tau/ds$ )

# 1. Introduction

The  $\tau$  is the only lepton massive enough to decay into hadrons

→ **ideal ground to investigate hadronic weak currents.**

# Using high precision experimental measurements of **ALEPH, OPAL, Belle, BaBar** (see **I. Nugent's** talk)

$$R_\tau \equiv \frac{\Gamma[\tau^- \rightarrow \text{hadrons}(\gamma)]}{\Gamma[\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau(\gamma)]}$$

(and related observables  $dR_\tau/ds$ )

\* Determination of the strong coupling  $\alpha_s$ : **A. Pich**, summary talk TAU12:

$$\alpha_s(m_\tau^2)_{\tau,av} = 0.334 \pm 0.014 \quad \rightarrow \quad \boxed{\alpha_s(m_Z^2)_{\tau,av} = 0.1204 \pm 0.0016}$$

in perfect agreement with the value obtained from hadronic decays at the  $Z$ :  $\alpha_s(m_Z^2)_{Z \text{ width}} = 0.1190 \pm 0.0027$

→ **the most precise test of Asymptotic Freedom**

$$\boxed{\alpha_s^\tau(M_Z^2) - \alpha_s^Z(M_Z^2) = 0.0014 \pm 0.0016_\tau \pm 0.0027_Z}$$

# 1. Introduction

# Sizeable corrections in the semi-inclusive  $\tau$ -decay width into Cabibbo-suppressed modes due to  $SU(3)$  breaking.

$$\delta R_\tau \equiv \frac{R_{\tau,V+A}}{|V_{ud}|^2} - \frac{R_{\tau,s}}{|V_{us}|^2}$$

Dominated by  $m_s$  (flavour indep. uncertainties drop out in the difference)

→ extraction of the strange quark mass **Pich and Prades**, [hep-ph/9909244](https://arxiv.org/abs/hep-ph/9909244)

# 1. Introduction

# Sizeable corrections in the semi-inclusive  $\tau$ -decay width into Cabbibo-suppressed modes due to  $SU(3)$  breaking.

$$\delta R_\tau \equiv \frac{R_{\tau,V+A}}{|V_{ud}|^2} - \frac{R_{\tau,s}}{|V_{us}|^2}$$

Dominated by  $m_s$  (flavour indep. uncertainties drop out in the difference)

→ extraction of the strange quark mass **Pich and Prades**, hep-ph/9909244

\* Strong dependence of  $m_s$  on  $|V_{us}|$

⇒ **Determination of  $|V_{us}|$  from a fixed  $m_s$**

**E.G., Jamin, Pich, Prades,**

**Schwab**, hep-ph/0212230,0408044

$$|V_{us}|^2 = \frac{R_{\tau,S}^{exp}}{\frac{R_{\tau,V+A}^{exp}}{|V_{ud}|^2} - \delta R_\tau^{theor}}$$

# 1. Introduction

# Sizeable corrections in the semi-inclusive  $\tau$ -decay width into Cabbibo-suppressed modes due to  $SU(3)$  breaking.

$$\delta R_\tau \equiv \frac{R_{\tau,V+A}}{|V_{ud}|^2} - \frac{R_{\tau,s}}{|V_{us}|^2}$$

Dominated by  $m_s$  (flavour indep. uncertainties drop out in the difference)

→ extraction of the strange quark mass **Pich and Prades**, hep-ph/9909244

\* Strong dependence of  $m_s$  on  $|V_{us}|$

⇒ **Determination of  $|V_{us}|$  from a fixed  $m_s$**

**E.G., Jamin, Pich, Prades,**

**Schwab**, hep-ph/0212230,0408044

$$|V_{us}|^2 = \frac{R_{\tau,S}^{exp}}{\frac{R_{\tau,V+A}^{exp}}{|V_{ud}|^2} - \delta R_\tau^{theor}}$$

**Advantage:** Final error dominated by experimental uncertainty

→ potential to be competitive with best determinations



**2.  $|V_{us}|$  from inclusive  
Cabibbo-suppressed  
hadronic  $\tau$  decays**

**E.G., Jamin, Pich, Prades, Schwab**

## 2.1. Theoretical Framework

The hadronic decay rate of the  $\tau$  is related to QCD correlators

$$R_\tau \equiv \frac{\Gamma[\tau^- \rightarrow \text{hadrons}(\gamma)]}{\Gamma[\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau(\gamma)]}$$

## 2.1. Theoretical Framework

The hadronic decay rate of the  $\tau$  is related to QCD correlators

$$R_\tau = 12\pi \int_0^{M_\tau^2} \frac{ds}{M_\tau^2} \left(1 - \frac{s}{M_\tau^2}\right)^2 \left[ \left(1 + 2\frac{s}{M_\tau^2}\right) \text{Im} \Pi^T(s) + \text{Im} \Pi^L(s) \right]$$

## 2.1. Theoretical Framework

The hadronic decay rate of the  $\tau$  is related to QCD correlators

$$R_\tau = 12\pi \int_0^{M_\tau^2} \frac{ds}{M_\tau^2} \left(1 - \frac{s}{M_\tau^2}\right)^2 \left[ \left(1 + 2\frac{s}{M_\tau^2}\right) \text{Im} \Pi^T(s) + \text{Im} \Pi^L(s) \right]$$

**basic objects**: Two-point correlation functions for vector and axial-vector two-quark currents ( $i, j = u, d, s$ ).

$$\Pi_{V,ij}^{\mu\nu}(q) \equiv i \int d^4x e^{iq \cdot x} \langle 0 | T \left( [V_{ij}^\mu]^\dagger(x) V_{ij}^\nu(0) \right) | 0 \rangle; \quad V_{ij}^\mu \equiv \bar{q}_i \gamma^\mu q_j$$

$$\Pi_{A,ij}^{\mu\nu}(q) \equiv i \int d^4x e^{iq \cdot x} \langle 0 | T \left( [A_{ij}^\mu]^\dagger(x) A_{ij}^\nu(0) \right) | 0 \rangle; \quad A_{ij}^\mu \equiv \bar{q}_i \gamma^\mu \gamma_5 q_j$$

Lorentz decomposition

$$\Pi_{ij,V/A}^{\mu\nu}(q) = \left( -g_{\mu\nu} q^2 + q^\mu q^\nu \right) \Pi_{ij,V/A}^T(q^2) + q^\mu q^\nu \Pi_{ij,V/A}^L(q^2)$$

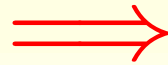
## 2.1. Theoretical Framework

The hadronic decay rate of the  $\tau$  is related to QCD correlators

$$R_\tau = 12\pi \int_0^{M_\tau^2} \frac{ds}{M_\tau^2} \left(1 - \frac{s}{M_\tau^2}\right)^2 \left[ \left(1 + 2\frac{s}{M_\tau^2}\right) \underbrace{\text{Im } \Pi^T(s)} + \underbrace{\text{Im } \Pi^L(s)} \right]$$

proportional to ↘ ↙

**ALEPH, OPAL**  
**BaBar, Belle**



**spectral functions**  
 $\tau$  decay data

## 2.1. Theoretical Framework

We can decompose  $R_\tau$  (experimentally and theoretically) into

$$R_\tau = R_{\tau,V} + R_{\tau,A} + R_{\tau,S}$$

according to the quark content

$$\Pi^J(s) \equiv |V_{ud}|^2 \left\{ \Pi_{V,ud}^J(s) + \Pi_{A,ud}^J(s) \right\} + |V_{us}|^2 \left\{ \Pi_{V,us}^J(s) + \Pi_{A,us}^J(s) \right\}$$

## 2.1. Theoretical Framework

We can decompose  $R_\tau$  (experimentally and theoretically) into

$$R_\tau = R_{\tau,V} + R_{\tau,A} + R_{\tau,S}$$

according to the quark content

$$\Pi^J(s) \equiv |V_{ud}|^2 \left\{ \Pi_{V,ud}^J(s) + \Pi_{A,ud}^J(s) \right\} + |V_{us}|^2 \left\{ \Pi_{V,us}^J(s) + \Pi_{A,us}^J(s) \right\}$$

# Sensitivity to the **strange** quark mass enhanced by considering the  $SU(3)$ -breaking quantity

$$\delta R_\tau = \frac{R_{\tau,V+A}}{|V_{ud}|^2} - \frac{R_{\tau,S}}{|V_{us}|^2}$$

- ★ Dominated by the **strange quark mass**
- ★ **Flavour independent** uncertainties **drop out in the difference**

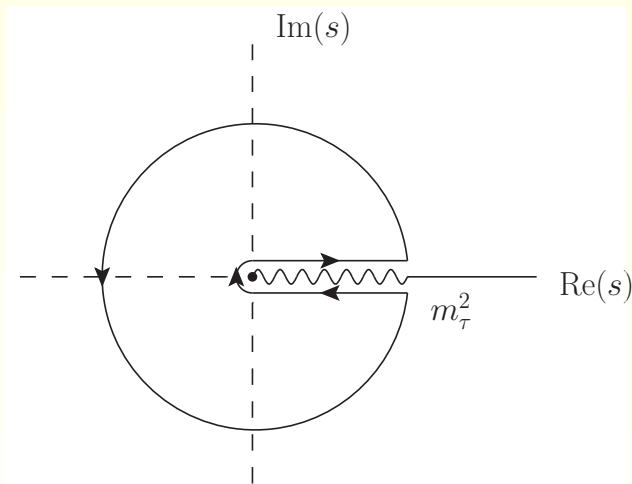
## 2.1. Theoretical Framework

Using the analytic properties of  $\Pi^J(s)$

$$R_\tau = -i\pi \oint_{|s|=M_\tau^2} \frac{ds}{s} \left[1 - \frac{s}{M_\tau^2}\right]^3 \left\{ 3 \left[1 + \frac{s}{M_\tau^2}\right] D^{L+T}(s) + 4 D^L(s) \right\}$$

$$D^{L+T}(s) \equiv -s \frac{d}{ds} [\Pi^{L+T}(s)];$$

$$D^L(s) \equiv \frac{s}{M_\tau^2} \frac{d}{ds} [s\Pi^L(s)]$$





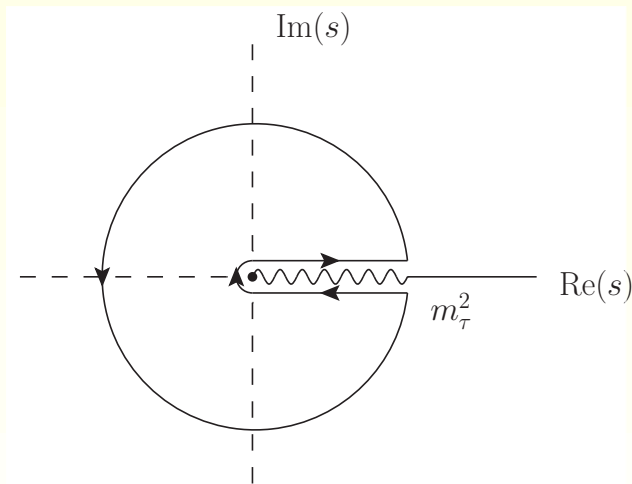
## 2.1. Theoretical Framework

Using the analytic properties of  $\Pi^J(s)$

$$R_\tau = -i\pi \oint_{|s|=M_\tau^2} \frac{ds}{s} \left[1 - \frac{s}{M_\tau^2}\right]^3 \left\{ 3 \left[1 + \frac{s}{M_\tau^2}\right] D^{L+T}(s) + 4 D^L(s) \right\}$$

$$D^{L+T}(s) \equiv -s \frac{d}{ds} [\Pi^{L+T}(s)];$$

$$D^L(s) \equiv \frac{s}{M_\tau^2} \frac{d}{ds} [s\Pi^L(s)]$$



- \* Eliminate renormalization scheme dependent subtraction constants
- \* phase space factor: order three zero in real axis

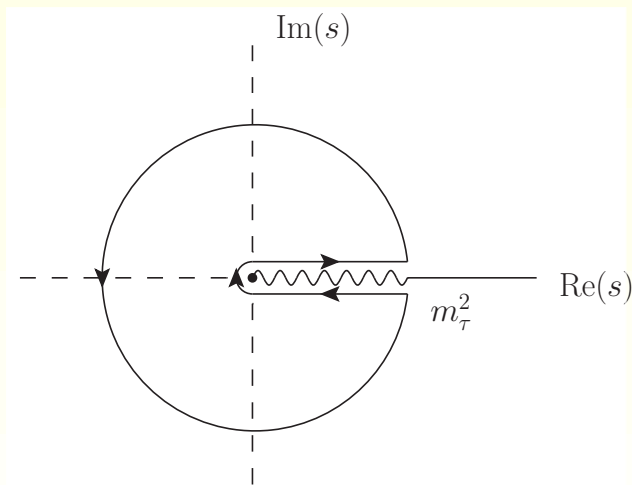
## 2.1. Theoretical Framework

Using the analytic properties of  $\Pi^J(s)$

$$R_\tau = -i\pi \oint_{|s|=M_\tau^2} \frac{ds}{s} \left[1 - \frac{s}{M_\tau^2}\right]^3 \left\{ 3 \left[1 + \frac{s}{M_\tau^2}\right] D^{L+T}(s) + 4 D^L(s) \right\}$$

$$D^{L+T}(s) \equiv -s \frac{d}{ds} [\Pi^{L+T}(s)];$$

$$D^L(s) \equiv \frac{s}{M_\tau^2} \frac{d}{ds} [s\Pi^L(s)]$$



- \* Eliminate renormalization scheme dependent subtraction constants
- \* phase space factor: order three zero in real axis

\* large enough Euclidean  $Q^2 = -s \implies D^{L+T}(Q^2)$  and  $D^L(Q^2)$  organized in series of operators of increasing dimension using *OPE*

## 2.1. Theoretical Framework

# Theoretically, performing an **OPE** of the correlators,  $R_\tau$  can be expressed

$$R_\tau = N_c S_{\text{EW}} \left\{ (|V_{ud}|^2 + |V_{us}|^2) [1 + \delta^{(0)}] + \sum_{D \geq 2} [ |V_{ud}|^2 \delta_{ud}^{(D)} + |V_{us}|^2 \delta_{us}^{(D)} ] \right\}$$

\*  $\delta_{ud}^{(D)}$  and  $\delta_{us}^{(D)}$  are corrections in the **OPE**

## 2.2. Theoretical Framework: OPE

$$\delta R_\tau = \frac{R_{\tau,V+A}}{|V_{ud}|^2} - \frac{R_{\tau,S}}{|V_{us}|^2} = N_c S_{EW} \sum_{D \geq 2} \left[ \delta_{ud}^{(D)} - \delta_{us}^{(D)} \right]$$

- \*  $\delta_{ij}^{(2)}$  are known to  $\mathcal{O}(\alpha_s^3)$  for both  $J = L$  and  $J = L + T$

Chetyrkin; Gorishny, Kataev, Larin, Sugurladze; Baikov, Chetyrkin, Kühn; Becchi, Narison, de Rafael; Bernreuther, Wetzel.

- \*  $\delta_{ij}^{(4)}$  fully included ( $m_q^4/M_\tau^4$ ,  $m_q \langle \bar{q}q \rangle / M_\tau^4$ )
- \*  $\delta_{ij}^{(6)}$  estimated (VSA) to be of order or smaller than error of  $D = 4$
- \* we disregard **OPE** corrections of  $D \geq 8$

## 2.2. Theoretical Framework: OPE

$$\delta R_\tau = \frac{R_{\tau,V+A}}{|V_{ud}|^2} - \frac{R_{\tau,S}}{|V_{us}|^2} = N_c S_{EW} \sum_{D \geq 2} \left[ \delta_{ud}^{(D)} - \delta_{us}^{(D)} \right]$$

- \*  $\delta_{ij}^{(2)}$  are known to  $\mathcal{O}(\alpha_s^3)$  for both  $J = L$  and  $J = L + T$

Chetyrkin; Gorishny, Kataev, Larin, Sugurladze; Baikov, Chetyrkin, Kühn; Becchi, Narison, de Rafael; Bernreuther, Wetzel.

- \*  $\delta_{ij}^{(4)}$  fully included ( $m_q^4/M_\tau^4$ ,  $m_q \langle \bar{q}q \rangle / M_\tau^4$ )
- \*  $\delta_{ij}^{(6)}$  estimated (VSA) to be of order or smaller than error of  $D = 4$
- \* we disregard **OPE** corrections of  $D \geq 8$

# Perturbative **L** series behave very badly !  $\rightarrow$

replace scalar/pseudoscalar QCD correlators with phenomenology

## 2.3. Theoretical Framework: Longitudinal contribution

★ Scalar spectral functions from s-wave  $K\pi$  scatt. data [Jamin, Oller, Pich, 0605095](#)

## 2.3. Theoretical Framework: Longitudinal contribution

★ Scalar spectral functions from s-wave  $K\pi$  scatt. data **Jamin, Oller, Pich, 0605095**

★ Dominant contribution: pseudoscalar  $us$  spectral function

$$s^2 \frac{1}{\pi} \text{Im} \Pi_{us,A}^L = 2f_K^2 m_K^4 \delta(s - m_K^2) + 2f_{K(1460)} M_{K(1460)}^4 BW(s)$$

$BW(s)$ : Normalized Breit-Wigner **Kambor, Maltman**

## 2.3. Theoretical Framework: Longitudinal contribution

★ Scalar spectral functions from s-wave  $K\pi$  scatt. data **Jamin, Oller, Pich, 0605095**

★ Dominant contribution: pseudoscalar  $us$  spectral function

$$s^2 \frac{1}{\pi} \text{Im} \Pi_{us,A}^L = 2f_K^2 m_K^4 \delta(s - m_K^2) + 2f_{K(1460)} M_{K(1460)}^4 BW(s)$$

$BW(s)$ : Normalized Breit-Wigner **Kambor, Maltman**

### Comparison of these spectral functions with QCD

	$R_{us,A}^{00,L}$	$R_{us,V}^{00,L}$	$R_{ud,A}^{00,L}$
Theory:	$-0.144 \pm 0.024$	$-0.028 \pm 0.021$	$-(7.79 \pm 0.14) \cdot 10^{-3}$
Phenom:	$-0.135 \pm 0.003$	$-0.028 \pm 0.004$	$-(7.77 \pm 0.08) \cdot 10^{-3}$

→ Theory uncertainty much reduced using phenomenology for the  $J = L$  component in  $\delta R_\tau$



## 2.4. Results

$$|V_{us}|^2 = \frac{R_{\tau,S}}{\frac{R_{\tau,V+A}}{|V_{ud}|^2} - \delta R_{\tau,th}}$$

# Theoretically determined: **OPE** ( $L + T$ ) + **phenomenology** ( $L$ )

**E.G., Jamin, Pich, Prades, Schwab** (between two more recent estimates, **E.G., Jamin, Pich, Prades, Schwab**, 0709.0282, **Maltman**, 1011.6391)

$$\delta R_{\tau,th} = \underbrace{(0.1544 \pm 0.0037)}_L + \underbrace{(9.3 \pm 3.4)m_s^2(\overline{MS}, 2 \text{ GeV})}_{L+T, D=2} + (0.0034 \pm 0.0028)$$

## 2.4. Results

$$|V_{us}|^2 = \frac{R_{\tau,S}}{\frac{R_{\tau,V+A}}{|V_{ud}|^2} - \delta R_{\tau,th}}$$

# Theoretically determined: **OPE** ( $L + T$ ) + **phenomenology** ( $L$ )

**E.G., Jamin, Pich, Prades, Schwab** (between two more recent estimates, **E.G., Jamin, Pich, Prades, Schwab**, 0709.0282, **Maltman**, 1011.6391)

$$\delta R_{\tau,th} = \underbrace{(0.1544 \pm 0.0037)}_L + \underbrace{(9.3 \pm 3.4)m_s^2(\overline{MS}, 2 \text{ GeV})}_{L+T, D=2} + (0.0034 \pm 0.0028)$$

# Experimental data **HFAG 2012**:

$$R_{\tau,V+A} = 3.4671 \pm 0.0084 \quad R_{\tau,S} = 0.1612 \pm 0.0028$$

## 2.4. Results

$$|V_{us}|^2 = \frac{R_{\tau,S}}{\frac{R_{\tau,V+A}}{|V_{ud}|^2} - \delta R_{\tau,th}}$$

# Theoretically determined: **OPE** ( $L + T$ ) + **phenomenology** ( $L$ )

**E.G., Jamin, Pich, Prades, Schwab** (between two more recent estimates, **E.G., Jamin, Pich, Prades, Schwab**, 0709.0282, **Maltman**, 1011.6391)

$$\delta R_{\tau,th} = \underbrace{(0.1544 \pm 0.0037)}_L + \underbrace{(9.3 \pm 3.4)m_s^2(\overline{MS}, 2 \text{ GeV})}_{L+T, D=2} + (0.0034 \pm 0.0028)$$

# Experimental data **HFAG 2012**:

$$R_{\tau,V+A} = 3.4671 \pm 0.0084 \quad R_{\tau,S} = 0.1612 \pm 0.0028$$

# Other inputs:

\*  $|V_{ud}| = 0.97425 \pm 0.0022$  **Hardy and Towner 2008**

\*  $m_s(2 \text{ GeV}) = 93.4 \pm 1.1$  (lattice average from **Laiho, Lunghi, Van de Water**)

## 2.4. Results

$$|V_{us}|^2 = \frac{R_{\tau,S}}{\frac{R_{\tau,V+A}}{|V_{ud}|^2} - \delta R_{\tau,th}}$$

$$\begin{aligned} \delta R_{\tau,th} &= \underbrace{(0.1544 \pm 0.0037)}_L + \underbrace{(9.3 \pm 3.4)m_s^{\overline{MS}^2}(2 \text{ GeV})}_{L+T, D=2} + (0.0034 \pm 0.0028) \\ &= 0.239 \pm 0.030 \end{aligned}$$

$\Rightarrow$

$$|V_{us}| = 0.2173 \pm 0.0020_{\text{exp}} \pm 0.0010_{\text{th}}$$

### 3. $|V_{us}|$ from $\tau \rightarrow K\pi\nu$

# Alternative way of extracting  $|V_{us}|$  using  $\Gamma(\tau \rightarrow K\pi\nu)$  **E. Passemar**,  
talk at TAU12, work in progress, **Antonelli, Banerjee, Cirigliano, Lusiani, Passemar**

$$\Gamma(\tau \rightarrow K\pi\nu) = N |f_+(0)V_{us}|^2 I_K^\tau \quad \text{with} \quad I_K^\tau = \int ds F(s, \bar{f}_+(s), \bar{f}_0(s))$$

where the form factors  $f_+(s)$  and  $f_0(s)$  are the same as in  $K \rightarrow \pi l\nu$ .

\* Parametrize  $f_{+,0}$  using dispersion relations **Bernard, Boito, Passemar** (in progress)  
and fit to  $K_{l3}$  and  $\tau \rightarrow K\pi\nu$  data  $\rightarrow$  constraints from different energy regions

### 3. $|V_{us}|$ from $\tau \rightarrow K\pi\nu$

# Alternative way of extracting  $|V_{us}|$  using  $\Gamma(\tau \rightarrow K\pi\nu)$  **E. Passemar**, talk at TAU12, work in progress, **Antonelli, Banerjee, Cirigliano, Lusiani, Passemar**

$$\Gamma(\tau \rightarrow K\pi\nu) = N |f_+(0)V_{us}|^2 I_K^\tau \quad \text{with} \quad I_K^\tau = \int ds F(s, \bar{f}_+(s), \bar{f}_0(s))$$

where the form factors  $f_+(s)$  and  $f_0(s)$  are the same as in  $K \rightarrow \pi l\nu$ .

- \* Parametrize  $f_{+,0}$  using dispersion relations **Bernard, Boito, Passemar** (in progress) and fit to  $K_{l3}$  and  $\tau \rightarrow K\pi\nu$  data  $\rightarrow$  constraints from different energy regions
- \* Using new Belle data for  $B(\tau \rightarrow K\pi\nu)$  (**S. Ryu's**, talk at TAU12)

$$|f_+(0)V_{us}| = 0.2140 \pm 0.0041_{I_k^\tau} \pm 0.0031_{exp}$$

and the lattice average  $f_+(0)^{lattice} = 0.9584 \pm 0.0044$ , **Laiho, Lunghi, Van de Water**, see **A. Juettner's** talk

$$|V_{us}| = 0.2233 \pm 0.0055$$

Not competitive with other methods yet but it can be an interesting check to the extraction from  $Kl3$  and inclusive  $\tau$  decays

### 3. $|V_{us}|$ from $\tau \rightarrow K\pi\nu$

# A sizeable fraction of the strange branching ratio is due to the decay  $\tau \rightarrow K\nu_\tau$ , which can be predicted theoretically with smaller errors than the direct experimental measurements

- \* From  $B(K \rightarrow \mu\nu_\mu(\gamma))$  Decker and Finkemeier, NPB438, PLB334  $\rightarrow$   
 $B(\tau \rightarrow K\nu_\tau) = (0.715 \pm 0.004) \cdot 10^{-2}$  Davier, Höcker, Zhang, 0507078

### 3. $|V_{us}|$ from $\tau \rightarrow K\pi\nu$

# A sizeable fraction of the strange branching ratio is due to the decay  $\tau \rightarrow K\nu_\tau$ , which can be predicted theoretically with smaller errors than the direct experimental measurements

\* From  $B(K \rightarrow \mu\nu_\mu(\gamma))$  **Decker and Finkemeier**, NPB438, PLB334  $\rightarrow$   
 $B(\tau \rightarrow K\nu_\tau) = (0.715 \pm 0.004) \cdot 10^{-2}$  **Davier, Höcker, Zhang**, 0507078

# Several branching fractions can be predicted using form factors obtained by fitting to  $K_{l3}$  and  $\tau \rightarrow K\pi\nu$  data and Kaon BR's very precisely measured **E. Passemar TAU12**

Branching fraction	HFAG Winter 2012 fit	Theory prediction <b>Preliminary</b>
$\Gamma_{10} = K^- \nu_\tau$	$(0.6955 \pm 0.0096) \cdot 10^{-2}$	$(0.713 \pm 0.003) \cdot 10^{-2}$
$\Gamma_{16} = K^- \pi^0 \nu_\tau$	$(0.4322 \pm 0.0149) \cdot 10^{-2}$	$(0.4473 \pm 0.0244) \cdot 10^{-2}$
$\Gamma_{35} = \pi^- \bar{K}^0 \nu_\tau$	$(0.8206 \pm 0.0182) \cdot 10^{-2}$	$(0.8627 \pm 0.0353) \cdot 10^{-2}$
$\Gamma_{110} = X_s^- \nu_\tau$	$(2.8746 \pm 0.0498) \cdot 10^{-2}$	$(2.9496 \pm 0.0571) \cdot 10^{-2}$

**Preliminary**, using only Belle  $\tau \rightarrow K\pi\nu$  data in the form factors fits.



### 3. $|V_{us}|$ from $\tau \rightarrow K\pi\nu$

Shift in  $R_{\tau,S}$ , and then in  $|V_{us}|$  from inclusive  $\tau$  decays.

$$|V_{us}| = 0.2173 \pm 0.0022 \quad \rightarrow \quad |V_{us}| = 0.2203 \pm 0.0025$$

### 3. $|V_{us}|$ from $\tau \rightarrow K\pi\nu$

Shift in  $R_{\tau,S}$ , and then in  $|V_{us}|$  from inclusive  $\tau$  decays.

$$|V_{us}| = 0.2173 \pm 0.0022 \quad \rightarrow \quad |V_{us}| = 0.2203 \pm 0.0025$$

# **PDG2012**: “Eighteen of the 20 B-factory branching fraction measurements are smaller than the non-B-factory values. The average normalized difference between the two sets of measurements is -1.30(-1.41 for the 11 Belle measurements and -1.24 for the 9 BaBar measurements)”

**Missing modes?**

**4.**  $|V_{us}|$  from exclusive  $B(\tau \rightarrow K\nu)/B(\tau \rightarrow \pi\nu)$  and  $B(\tau \rightarrow K\nu)$

#  $|V_{us}|$  can be extracted from the ratio:

$$\frac{B(\tau \rightarrow K\nu)}{B(\tau \rightarrow \pi\nu)} = \frac{f_K^2 |V_{us}|^2 (1 - m_K^2/m_\tau^2)^2 r_{LD}(\tau^- \rightarrow K^- \nu_\tau)}{f_\pi^2 |V_{ud}|^2 (1 - m_\pi^2/m_\tau^2)^2 r_{LD}(\tau^- \rightarrow \pi^- \nu_\tau)}$$

where  $r_{LD}$  corresponds to the long-distance EW radiative correction, see [HFAG2012, 1207.1158](#).

## 4. $|V_{us}|$ from exclusive $B(\tau \rightarrow K\nu)/B(\tau \rightarrow \pi\nu)$ and $B(\tau \rightarrow K\nu)$

#  $|V_{us}|$  can be extracted from the ratio:

$$\frac{B(\tau \rightarrow K\nu)}{B(\tau \rightarrow \pi\nu)} = \frac{f_K^2 |V_{us}|^2 (1 - m_K^2/m_\tau^2)^2 r_{LD}(\tau^- \rightarrow K^- \nu_\tau)}{f_\pi^2 |V_{ud}|^2 (1 - m_\pi^2/m_\tau^2)^2 r_{LD}(\tau^- \rightarrow \pi^- \nu_\tau)}$$

where  $r_{LD}$  corresponds to the long-distance EW radiative correction, see [HFAG2012, 1207.1158](#).

- \* Using [HFAG2012](#):  $r_{LD}(\tau^- \rightarrow K^- \nu_\tau)/r_{LD}(\tau^- \rightarrow \pi^- \nu_\tau) = 1.0003 \pm 0.0044$ ,  
 $B(\tau \rightarrow K\nu)/B(\tau \rightarrow \pi\nu) = 0.0643 \pm 0.0009$
- \*  $|V_{ud}| = 0.97425 \pm 0.0022$  from [Hardy and Towner 2008](#)
- \* and the lattice average  $f_K/f_\pi = 1.1936 \pm 0.0053$ , see [J. Laiho's talk](#)

$$|V_{us}|_{\tau K \pi} = 0.2229 \pm 0.0021$$

4.  $|V_{us}|$  from exclusive  $B(\tau \rightarrow K\nu)/B(\tau \rightarrow \pi\nu)$  and  $B(\tau \rightarrow K\nu)$

#  $|V_{us}|$  can also be extracted from:

$$B(\tau \rightarrow K\nu) = \frac{G_F^2 f_K^2 |V_{us}|^2 m_\tau^3 \tau_\tau}{16\pi\hbar} \left(1 - \frac{m_K^2}{m_\tau^2}\right) S_{EW}$$

\* Using again **HFAG2012 averages** for exp. quantities

\* and the lattice average  $f_K = (156.1 \pm 1.1)$  MeV, see **Laiho, Lunghi, Van de Water**

$$|V_{us}|_{\tau K} = 0.2214 \pm 0.0022$$

#### 4. $|V_{us}|$ from exclusive $B(\tau \rightarrow K\nu)/B(\tau \rightarrow \pi\nu)$ and $B(\tau \rightarrow K\nu)$

#  $|V_{us}|$  can also be extracted from:

$$B(\tau \rightarrow K\nu) = \frac{G_F^2 f_K^2 |V_{us}|^2 m_\tau^3 \tau_\tau}{16\pi\hbar} \left(1 - \frac{m_K^2}{m_\tau^2}\right) S_{EW}$$

\* Using again **HFAG2012 averages** for exp. quantities

\* and the lattice average  $f_K = (156.1 \pm 1.1)$  MeV, see **Laiho, Lunghi, Van de Water**

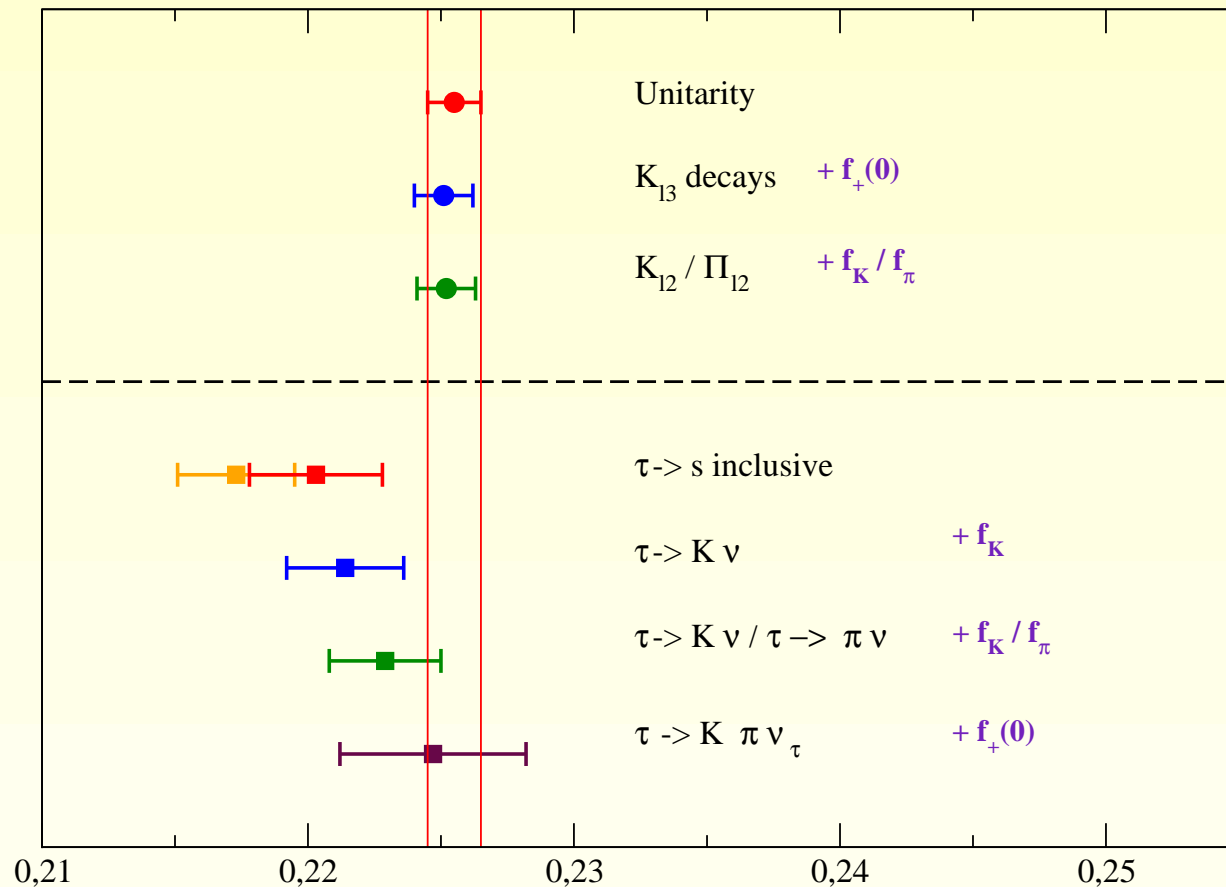
$$|V_{us}|_{\tau K} = 0.2214 \pm 0.0022$$

(Using instead the theory prediction from

**Antonelli, Banerjee, Cirigliano, Luisiani, Passemar** for  $B(\tau \rightarrow K\nu_\tau)$ )

$$(|V_{us}|_{\tau K} = 0.2242 \pm 0.0016 \quad \text{Preliminary})$$

## 5. Summary of results and conclusions



From inclusive Cabibbo-suppressed hadronic  $\tau$  decays:

$$|V_{us}| = 0.2173 \pm 0.0020_{exp} \pm 0.0010_{th}$$

Error is dominated by experiment  $\rightarrow$  potential to be the most precise determination of  $|V_{us}|$

## 5. Summary of results and conclusions

- # Need experimental improvement: BaBar, Belle, Belle II, SuperB, see **I. Nugent's** talk
- \* Systematic uncertainties now greatly exceed the statistical uncertainties.
- # Some questions that remain to be studied.
  - \* Branching fractions from **B-factories** systematically smaller than previous measurements.