

Physics Beyond the Standard Model 3.1

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Beyond the Standard Model

Lecture 1

- Why do we need to go Beyond the SM ?
- The Hierarchy Problem: what do we need to solve it ?

Lecture 2

- Supersymmetry and the Hierarchy Problem

Lecture 3

- New Dynamics at the TeV scale: the Higgs as a (pseudo) Nambu-Goldstone Boson

Beyond the Standard Model III

- Solve the Hierarchy problem with dynamics: QCD and the σ (Technicolor, ...)
- Dynamical (composite) *light* Higgs: is a (pseudo) Goldstone boson
The example of the pion in QCD
- Composite Higgs Models:
 - Little Higgs
 - Twin Higgs
 - Gauge-Higgs unification in AdS_5

Where is the Scalar Sector Coming From

- But what determines m and λ ?
- Is the scalar sector resulting from some underlying dynamics ?

E.g. Superconductivity:

Cooper pairs $\Rightarrow \langle \Phi \rangle \neq 0$

\mathcal{L}_Φ is the Ginzburg-Landau theory $\left\{ \begin{array}{l} \text{EM broken in the SC} \\ \text{Meissner effect} \\ \text{penetration depth} \\ \cdot \\ \cdot \\ \cdot \end{array} \right.$

But microscopic description is BCS

Physics Beyond the Standard Model

Organize by origin of Higgs sector or solution to HP


- Supersymmetry:

Higgs is elementary

SUSY protects m_h

- Higgs sector is composite:

Technicolor. No Higgs. 

Higgs is a pNGB 

Composite Scalars: the Example of QCD

Spontaneous breaking of chiral symmetry in QCD

QCD with 2 flavors:

$$\mathcal{L}_{\text{QCD}} = \bar{Q}_L i \not{D} Q_L + \bar{Q}_R i \not{D} Q_R - \bar{Q}_L M Q_R + \text{h.c.}$$

with

$$Q = \begin{pmatrix} u \\ d \end{pmatrix} \quad M = \begin{pmatrix} m_u & 0 \\ 0 & m_d \end{pmatrix}$$

If $M = 0$, is invariant under $SU(2)_L \times SU(2)_R$

$$\begin{array}{l} Q_L \longrightarrow e^{i\ell^a t^a} Q_L \\ Q_R \longrightarrow e^{i r^a t^a} Q_R \end{array} \quad \text{with} \quad \left\{ \begin{array}{l} t^a = \frac{\sigma^a}{2}, \quad a = 1, 2, 3 \\ \ell^a, r^a \text{ free parameters} \end{array} \right.$$

Chiral Symmetry Breaking

$SU(3)_c$ asymptotically free



At low energies, $\Lambda \simeq \Lambda_{\text{QCD}}$, quark condensation

$$\langle \bar{Q}_L Q_R \rangle \neq 0 \quad \Rightarrow \quad SU(2)_A \times SU(2)_R \longrightarrow SU(2)_V$$

- Quarks acquire a dynamical mass

$$m_Q \sim \Lambda_{\text{QCD}}$$

Chiral Symmetry Breaking

- 3 broken generators \implies 3 NGBs (π^+, π^-, π^0)

Since $SU(2)_L \times SU(2)_R = SU(2)_V \times SU(2)_A \longrightarrow SU(2)_V$

Axial current $j_\mu^{a5} = \bar{Q} \gamma_\mu \gamma^5 Q$

does not annihilate the vacuum

$$\langle 0 | j_\mu^{a5} | \pi^b(p_\mu) \rangle = i f_\pi p_\mu \delta^{ab}$$

But still conserved if $m_\pi = 0$

$$\partial^\mu j_\mu^{a5} = f_\pi m_\pi^2$$

Spontaneous Breaking of Chiral Symmetry

Linear σ model

$$\mathcal{L} = \frac{1}{4} \text{Tr} [\partial_\mu \Sigma^\dagger \partial^\mu \Sigma] + \frac{\mu^2}{4} \text{Tr} [\Sigma^\dagger \Sigma] - \frac{\lambda}{16} (\text{Tr} [\Sigma^\dagger \Sigma])^2$$

with

$$\Sigma = \sigma + i t^a \pi^a$$

If $\mu^2 > 0 \Rightarrow \langle \Sigma \rangle = v \neq 0 \quad v = \sqrt{\frac{\mu^2}{\lambda}}$

\Rightarrow $\left\{ \begin{array}{l} \text{Spontaneous breaking of chiral symmetry} \\ m_\sigma = \sqrt{2\lambda} v \\ m_\pi = 0 \end{array} \right.$

Spontaneous Breaking of Chiral Symmetry

In real QCD:

- $\left\{ \begin{array}{l} m_\sigma \sim \Gamma_\sigma \sim O(1) \text{ GeV} \quad \text{Cutoff of the effective theory} \\ \sigma \text{ is not a low energy state (too broad to be observable)} \end{array} \right.$

- $m_u, m_d \neq 0 \implies$ Explicit symmetry breaking

$$m_\pi \neq 0 \quad \pi' \text{ s are pseudo NGBs}$$

But still light

$$m_\pi \simeq 0.14 \text{ GeV} \ll O(1) \text{ GeV}$$

GeV vs. TeV Scales

Build a TeV-scale model of $EWSB$ in analogy with QCD

Two avenues:

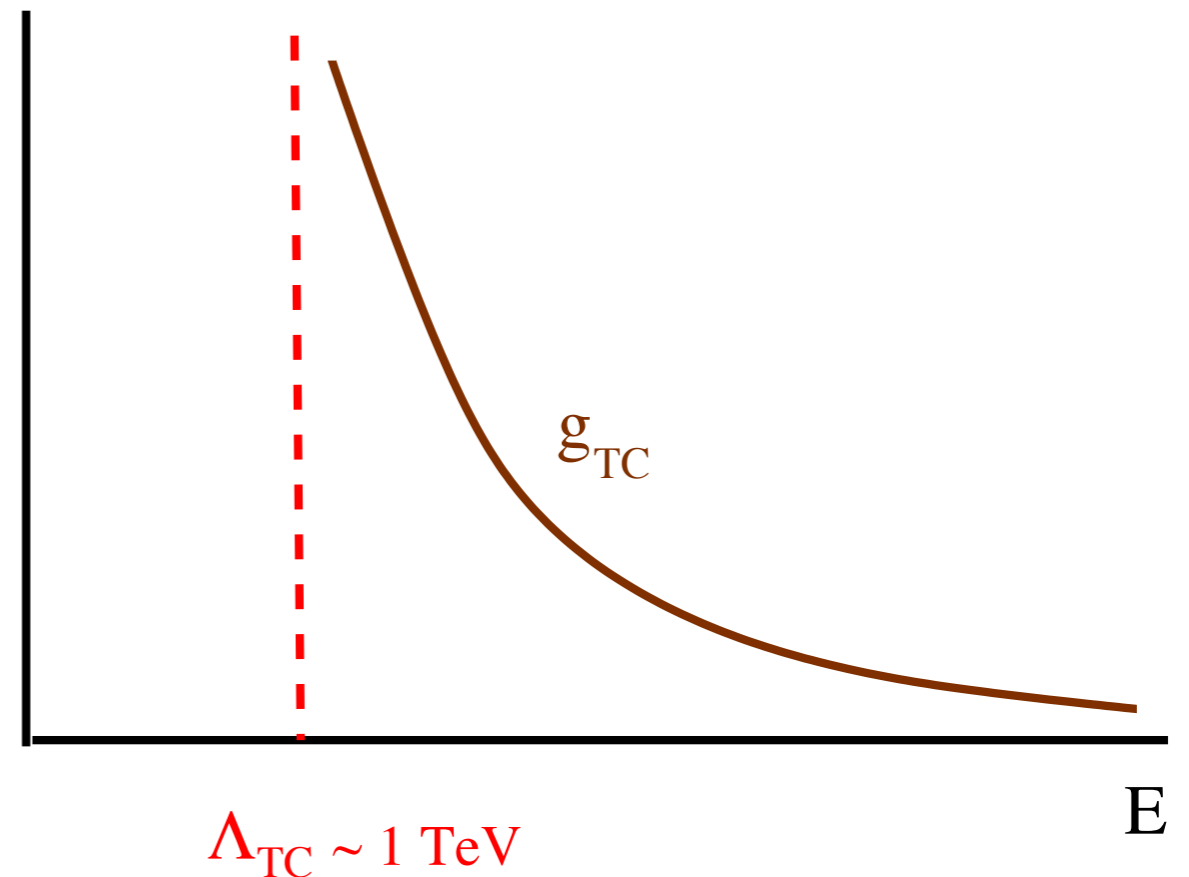
- Fermionic sector breaks EWS just as in QCD
Higgs (σ) is not in the light spectrum
- Strong sector breaks global symmetry
Higgs is a (pseudo) NGB remnant
just like the π 's

Strong Dynamics at the TeV Scale

Scaled up QCD

- New gauge interaction
- Strong at the TeV scale
- Breaks EWS by

$$\langle \bar{F} F \rangle \neq 0$$



Basic Technicolor Model

- Asymptotically-free interaction $SU(N_T)$
- New fermions: $SU(2)_L$ doublet

$$Q_L = \begin{pmatrix} T \\ B \end{pmatrix}_L \quad (N_T, 1, 2, Y_Q)$$

$$T_R \quad (N_T, 1, 1, Y_T)$$

$$B_R \quad (N_T, 1, 1, Y_B)$$

- At Λ_{TC} we have $\langle \bar{Q}_L Q_R \rangle \neq 0$

\Rightarrow $\left\{ \begin{array}{l} \text{Spontaneous breaking of global } SU(2)_L \times SU(2)_R \\ \text{Also SB of the gauge } SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM} \end{array} \right.$

Higgs Mechanism without a Higgs

$$SU(2)_L \times SU(2)_R \rightarrow SU(2)_V \quad \Rightarrow \quad 3 \text{ Nambu-Goldstone bosons}$$

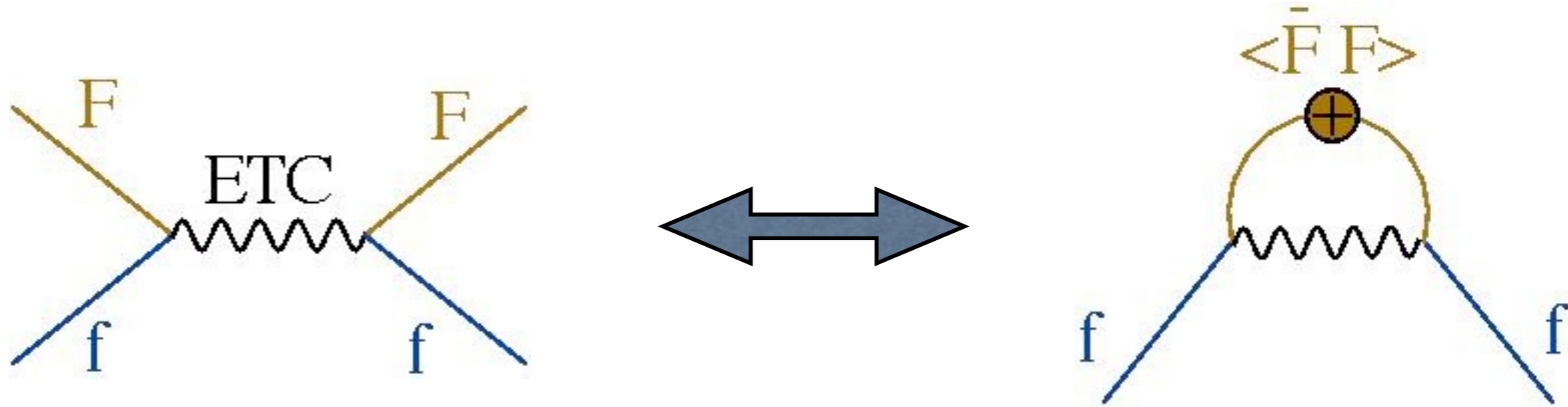
NGBs eaten as gauge boson longitudinal polarizations



$$i \frac{g^2 F_T^2}{4} \left(g_{\mu\nu} - \frac{q_\mu q_\nu}{q^2} \right)$$

Fermion Masses without a Higgs

Need extended interaction mixing SM fermions with tfermions



$$-\frac{g_{\text{ETC}}^2}{M_{\text{ETC}}^2} \bar{f} f \bar{F} F \quad \Rightarrow \quad m_f \sim \frac{g_{\text{ETC}}^2}{M_{\text{ETC}}^2} \Lambda_{\text{TC}}^3$$

Extended Technicolor

ETC requires more techni-fermions

$$\left(\begin{array}{c} T \\ B \end{array} \right)_L^i \quad T_R^i, B_R^i \quad \text{techni-quarks}$$

$$\left(\begin{array}{c} N \\ E \end{array} \right)_L \quad N_R, E_R \quad \text{techni-leptons}$$

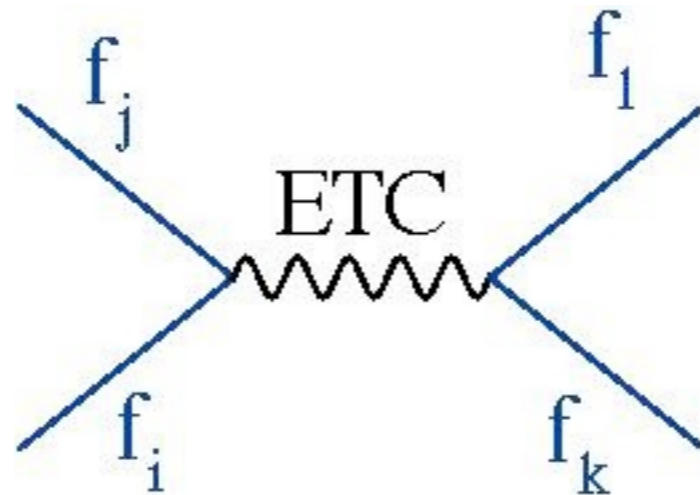
- Number of doublets higher $N_D = 4$

Problems with EWPC

- Larger chiral symmetry broken $SU(8)_L \times SU(8)_R \longrightarrow SU(8)_V$
 $63 - 3 = 60$ NGBs left in the spectrum!

Flavor Violation from ETC Interactions

ETC leads to tree-level flavor violation



\Rightarrow effects in $(K^0 - \bar{K}^0)$, $(B^0 - \bar{B}^0)$, mixing, ...

$\Rightarrow M_{\text{ETC}} > 1000 \text{ TeV}$

But M_{ETC} cannot be too large or it would suppress

m_t, m_b, m_c too much

Walking Technicolor and Separation of Scales

To get heavier masses need to enhance TC condensate

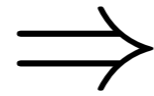
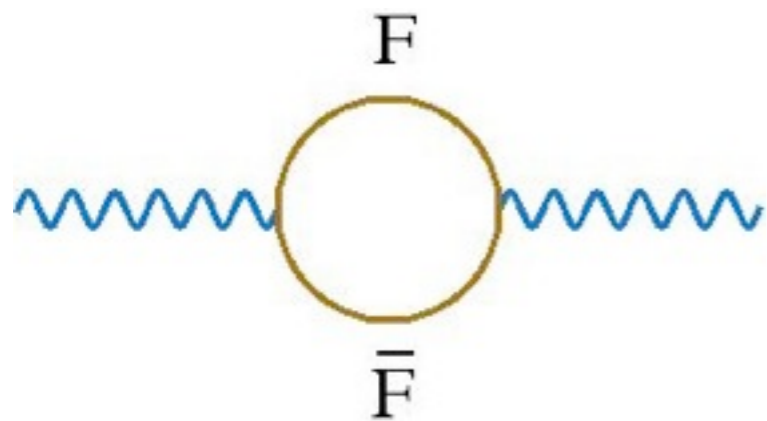
\Rightarrow $\left\{ \begin{array}{l} \text{Near-conformal behavior of TC interaction} \\ \text{Coupling walks} \end{array} \right.$

But walking takes long time for coupling to become super-critical

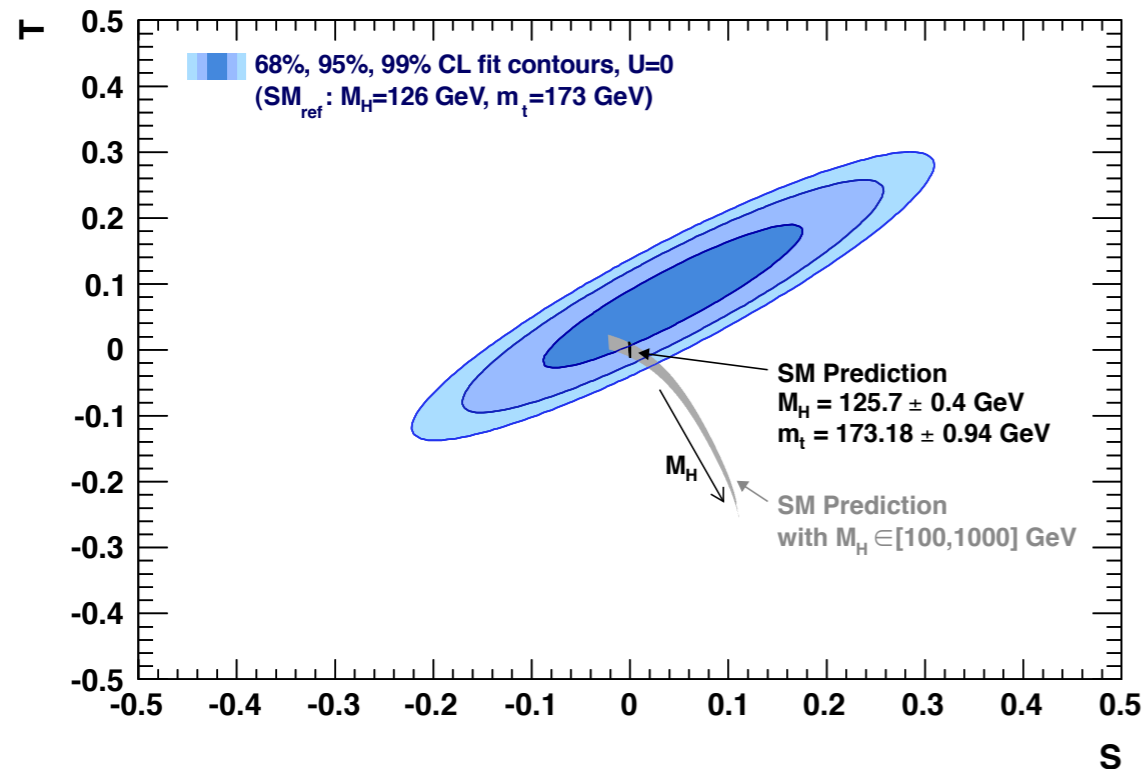
\Rightarrow Walking generates large separation of scale

Electroweak Precision Constraints

For the simple scaled up QCD scenario



$$S \sim \frac{N_T N_D}{6\pi}$$



S is very large in QCD-like models

New Ideas in Techni-Color Models

- Minimal Walking Technicolor (F. Saninno *et al.*)

$$N_T = 2, N_D = 1$$

No flavor theory

Not clear how to get a light Higgs

Can be modeled in AdS_5

- Conformal Technicolor (M. Luty *et al.*)

Strong sector is near a conformal fixed point in the UV

Explicit conformal breaking \rightarrow EWSB

First basic models accommodate light Higgs as pNGB

Higgs is a pseudo Nambu-Goldstone Boson

Back to the analogy of QCD at low energies

- Build models where the Higgs is like π instead of σ

Need to break global symmetry spontaneously

$$SU(2)_L \times SU(2)_R \rightarrow SU(2)_V$$

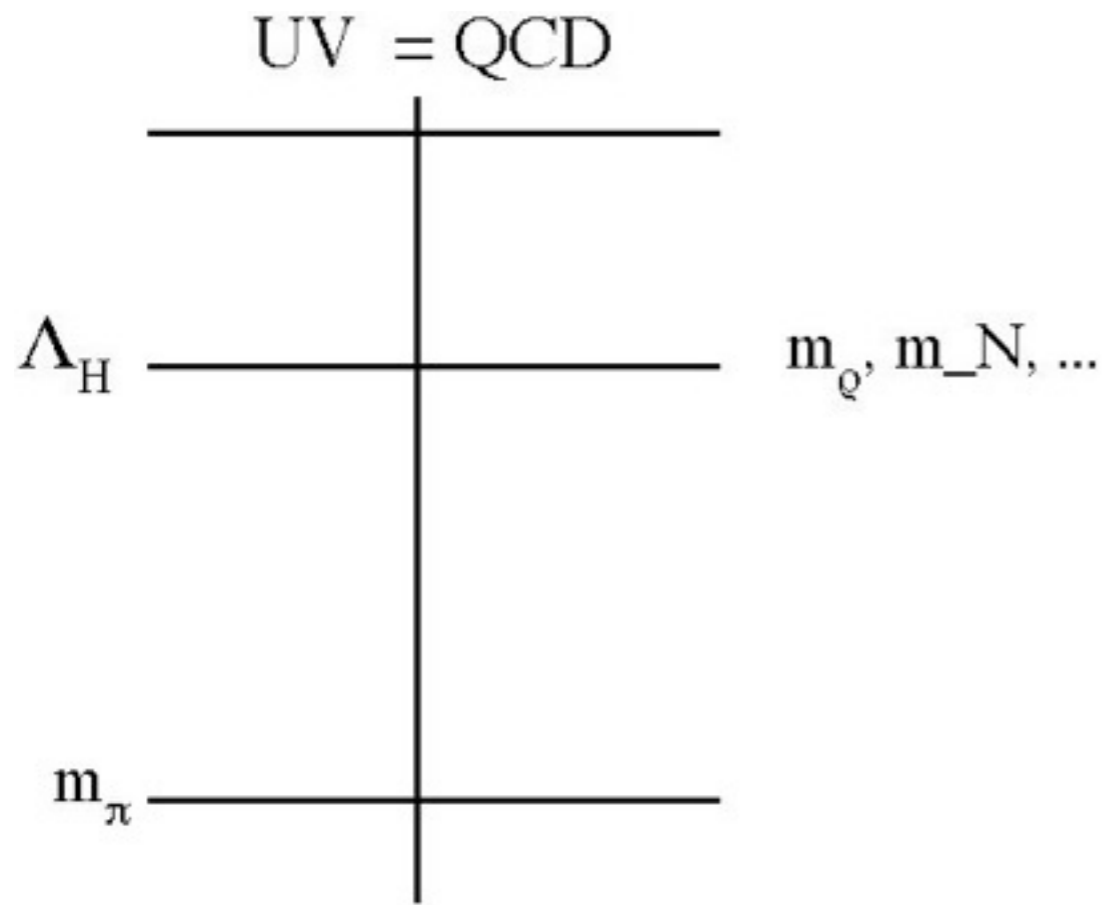
Number of NGBs: $3 + 3 - 3 = 3$ (π^+ , π^- , π^0)

- Explicit symmetry breaking:

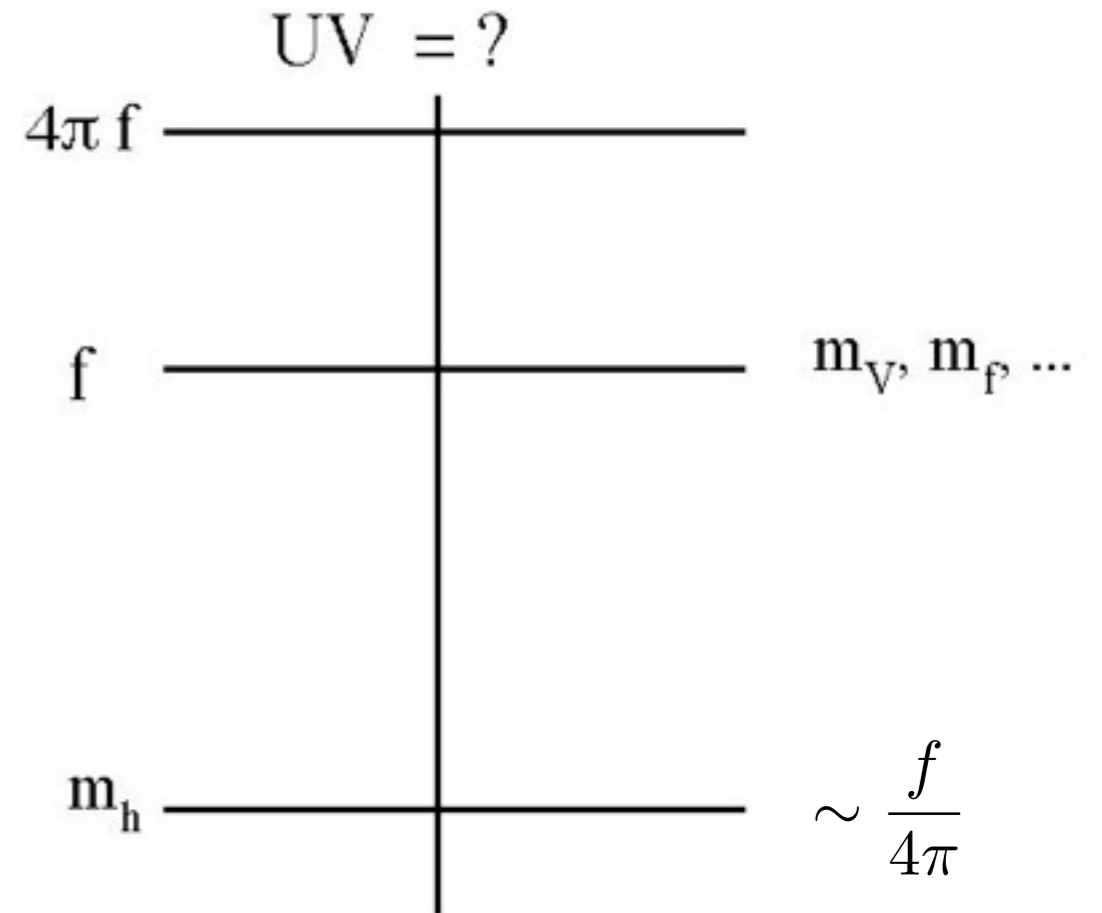
$$m_\pi^2 = B_0 m_q$$

gives mass to the NGB

Higgs is a pNGB



QCD



Electroweak