

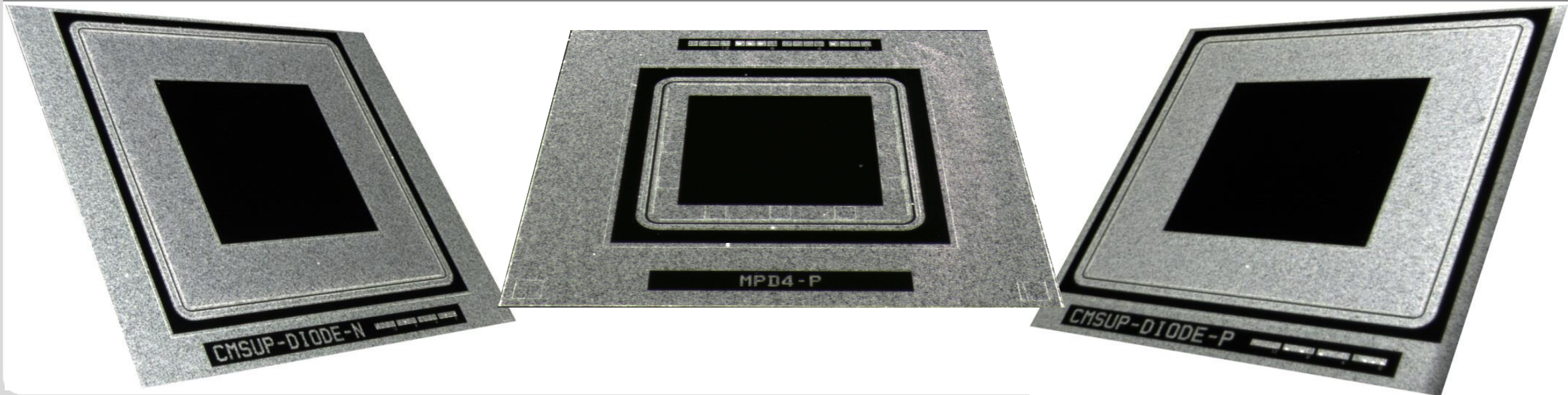
Simulation of CV, TCT and CCE with an effective 2-defect model

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22nd RD50 Workshop

Institut für Experimentelle Kernphysik



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Introduction

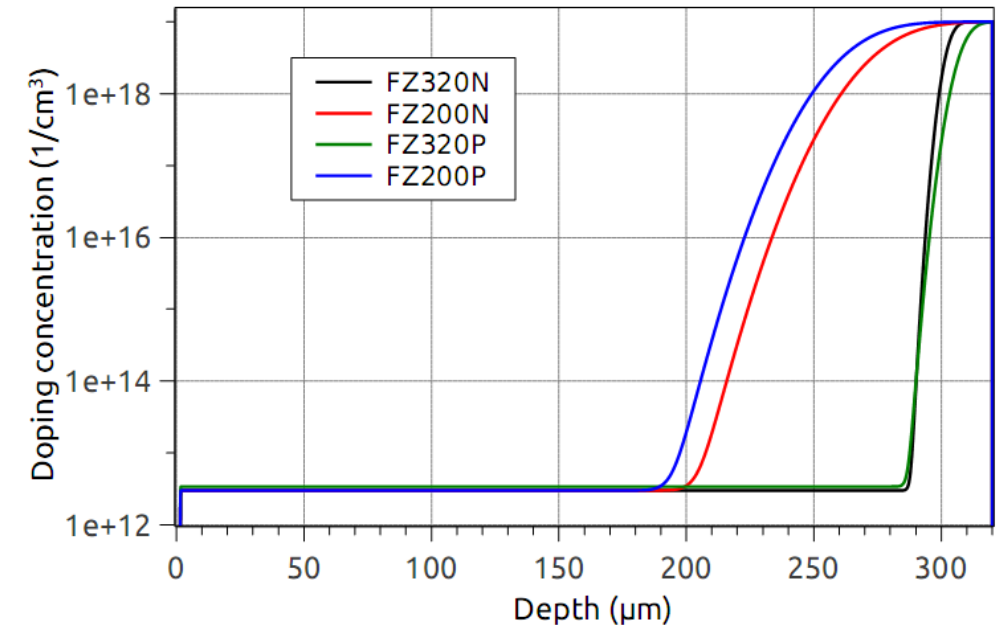
Simulation Device

- HPK like diodes: FZ material; thickness: 200 μm , 320 μm ; p-bulk / n-bulk
- Junction at front side: 1.5 μm depth gaussian shape
- Junction at back side: deep diffusion depending on thickness
- Very simple device 1 μm (x 1 μm) x 320 μm
- Irradiate device \rightarrow 2 Modify 2-defect model

Original Trap Model (EVL)

Trap	Energy	Cross section (e/h)	Intro rate
Donor	EV+0.48eV	1e-15/cm ²	1
Acceptor	EC-0.525eV	1e-15/cm ²	1

Doping Profiles of HPK Diodes



Matches unirradiated measurements (IV, CV)

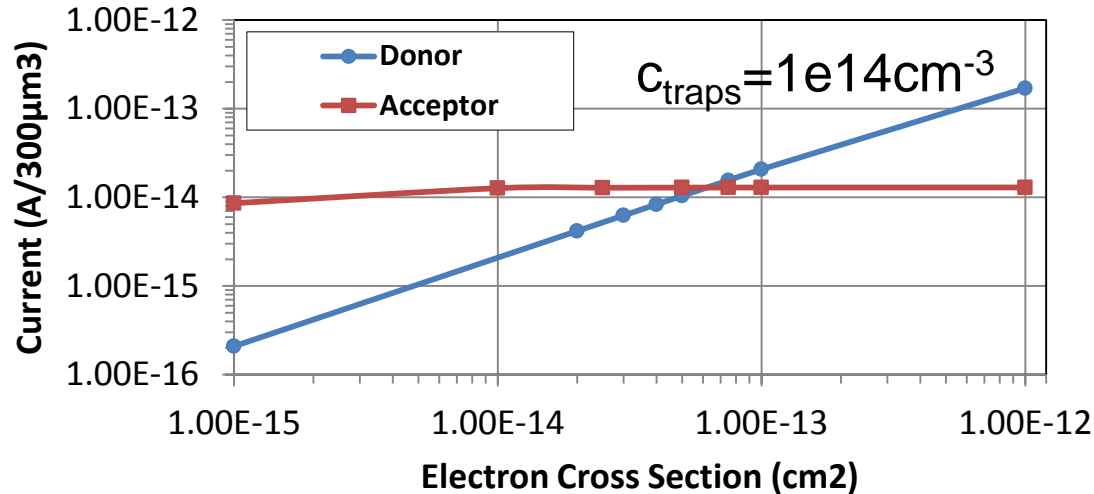
Motivation for correct electric field

- Current in irradiated devices
 - Only dependent on particle fluence
 - Independent of particle type
- Increase of bulk current well described by α
- Correct current has to be established in the simulation
 - Filling of traps / space charge dependent on current
 - Filling of traps determines electric field shape
- HPK diodes: 1st annealing step 10min@60°C
 - $\alpha = 8.9e-19$ A/cm
- How to determine current according to simulation parameters?

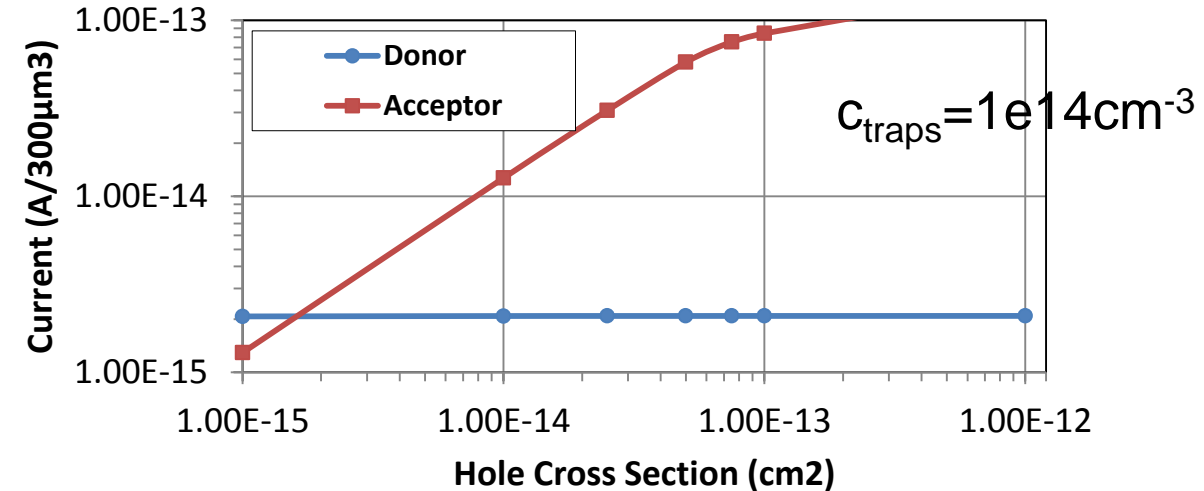
$$\Delta I = \alpha \times V \times F$$

Parameterisation of generated Current

Current vs. Electron Cross Section



Current vs. Hole Cross Section



- Current mainly produced by the cross section of one charge carrier $\Delta I = \alpha \times V \times F$
- Current also dependent on concentration of traps
- Calculate concentration of traps dependent on c , σ and α

$$X = \frac{I}{\sigma_{test} \times C_{test}}$$

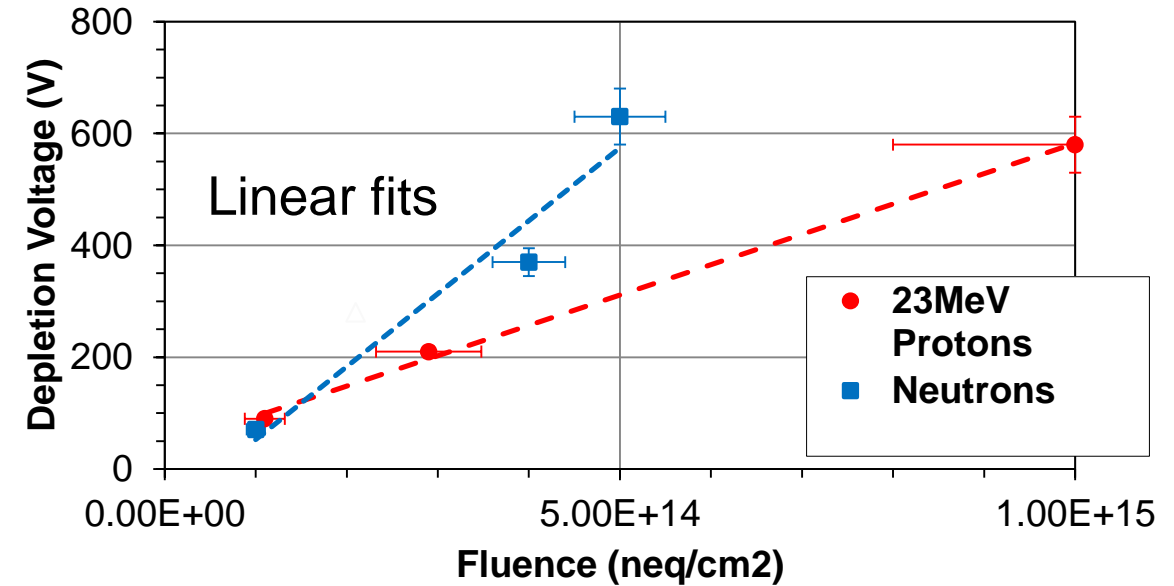
$$C_{Acc} = \frac{\alpha \times Vol. \times F}{r \times (X_{e,Don} \times \sigma_{e,Don} + X_{h,Don} \times \sigma_{h,Don}) + (X_{e,Acc} \times \sigma_{e,Acc} + X_{h,Acc} \times \sigma_{h,Acc})}$$

$$C_{Don} = r \times C_{Acc}$$

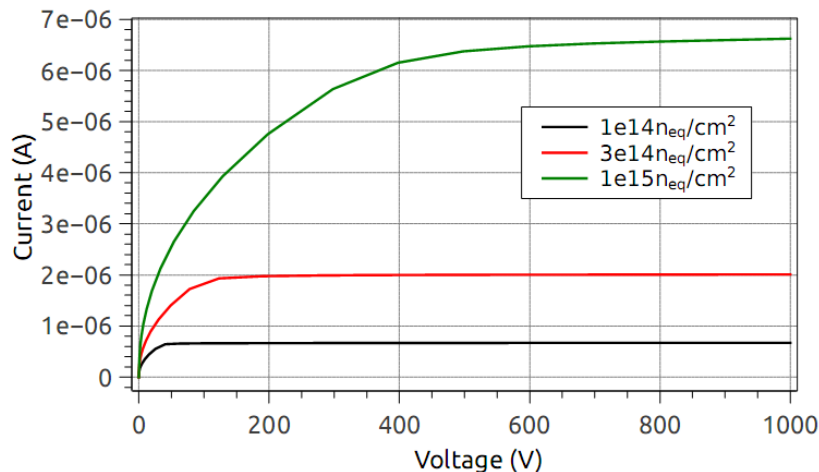
Depletion Voltage

- Different depletion voltage observed at -20°C , 1kHz
Annealing 10min@ 60°C
 - For 23MeV protons
 - For neutrons
- Linear approximation feasible
- Derive Models

Depletion Voltage of FZ320N Diodes

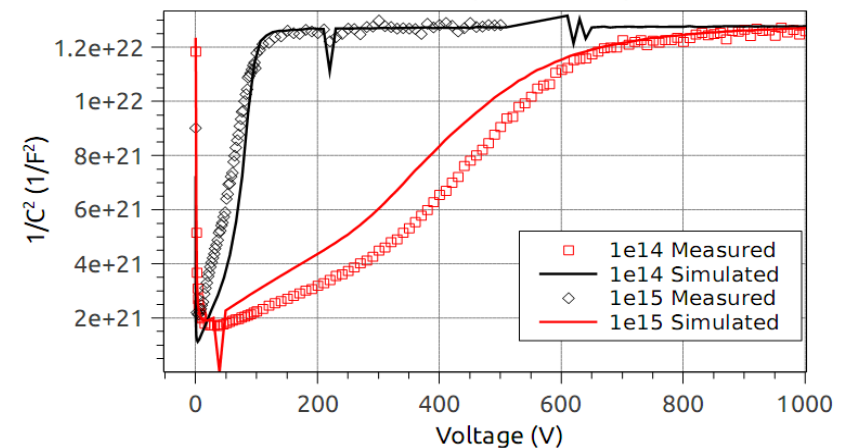


Current
HPK FZ320N Diodes



Comparison of Simulated and Measured CV
FZ320N Diodes, $T = -20^{\circ}\text{C}$, $f = 1\text{kHz}$

Proton irradiation



Radiation Damage Models

■ Neutron Irradiation

■ Donor

- $c = 0.9 * c(\text{Acc}) = 1.395 * F$
- $X(e) = X(h) = 1.2e-14\text{cm}^2$

■ Acceptor

- $c = 1.55 * F$
- $X(e) = X(h) = 1.2e-14\text{cm}^2$

■ Proton Irradiation

■ Donor

- $c = 5.598 * F - 3.959e14$
- $X(e) = X(h) = 1.0e-14\text{cm}^2$

■ Acceptor

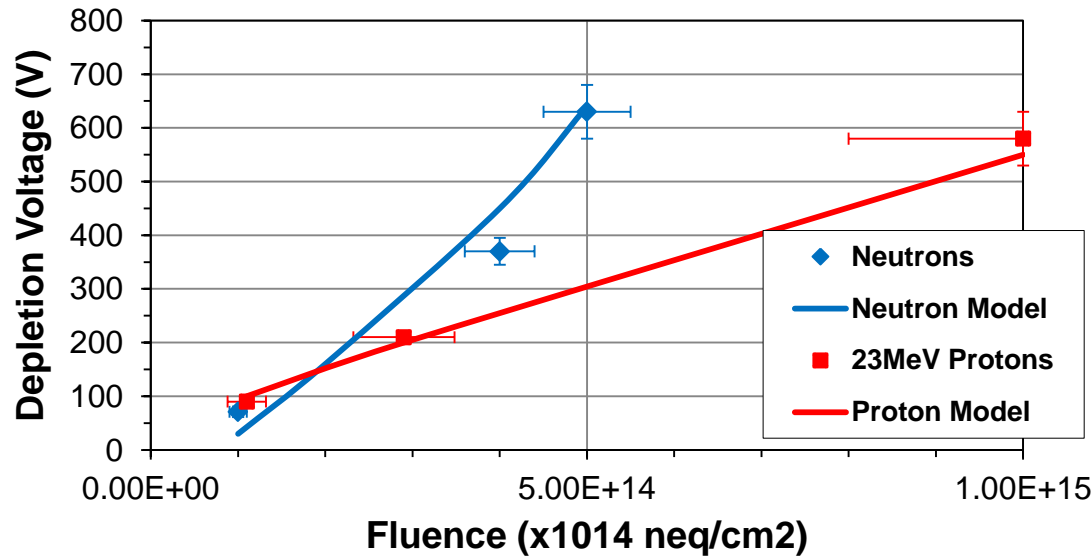
- $c = 1.189 * F + 0.645e14$
- $X(e) = X(h) = 1.0e-14\text{cm}^2$

■ Donor removal = 50% in n-bulk

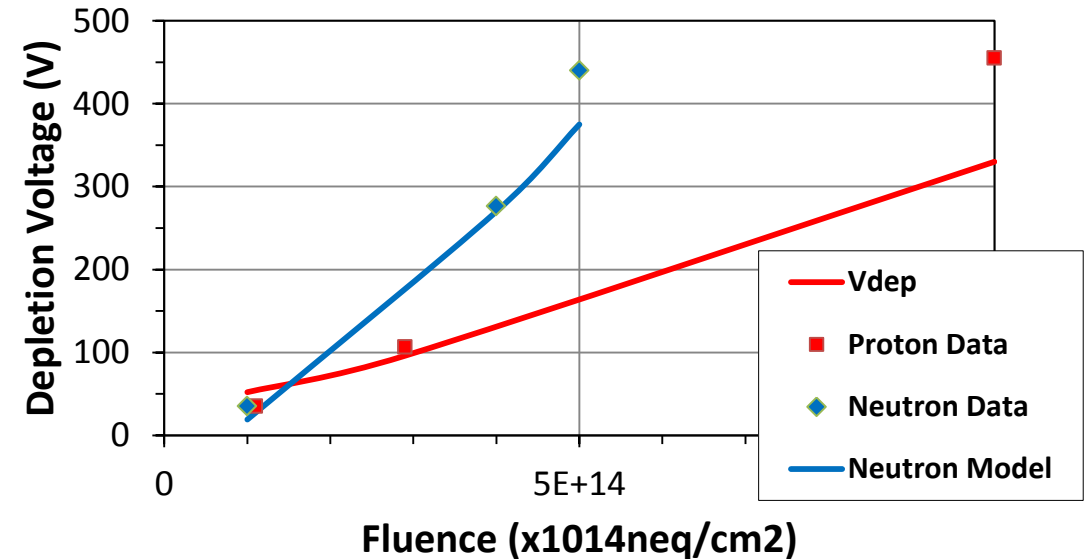
Valid for $1e14 - 1e15\text{neq/cm}^2$

Overview of Depletion Voltage (n-bulk)

Depletion Voltage of FZ320N Diodes



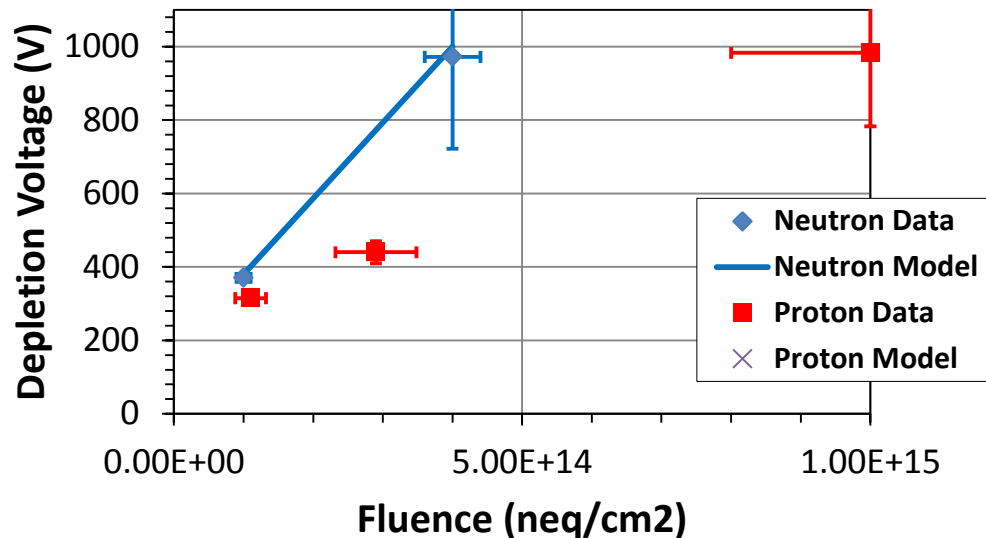
Depletion Voltage of FZ200N Diodes



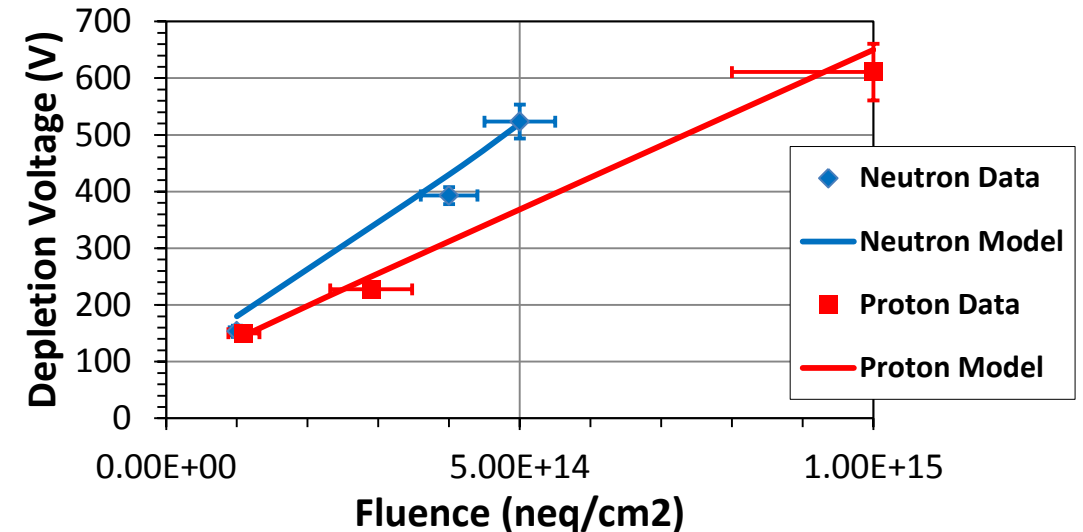
- Models describe the depletion voltage of all n-bulk diodes quite well
- Most problems experienced describing higher fluences for protons

Overview of Depletion Voltage (p-bulk)

Depletion Voltage FZ320P Diodes



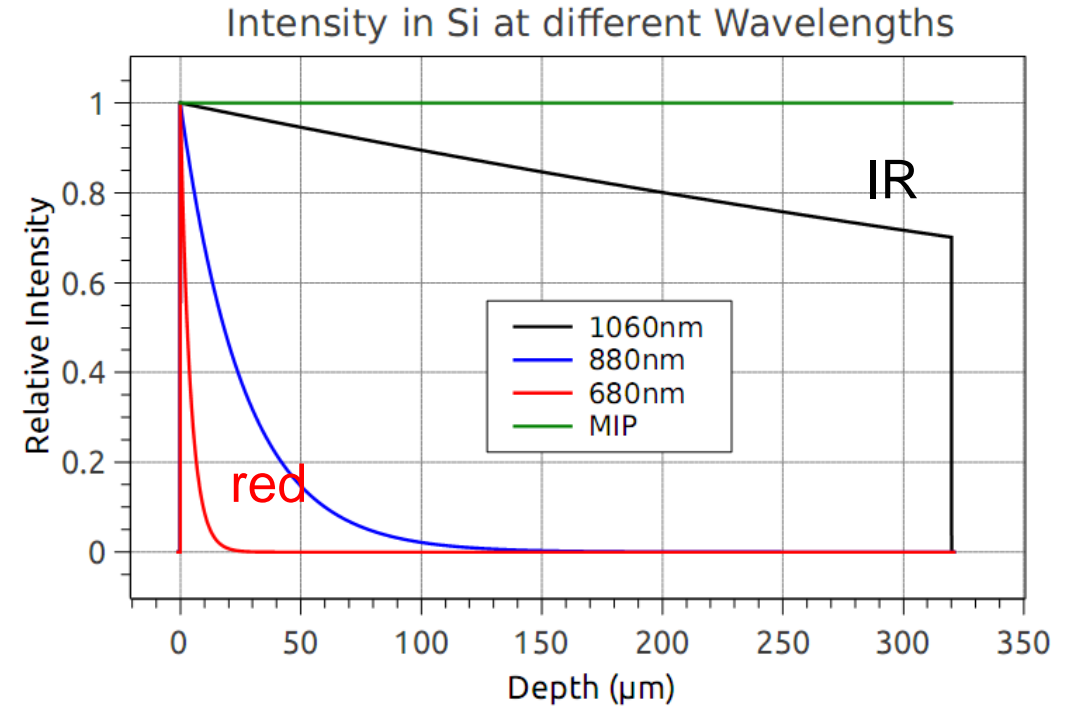
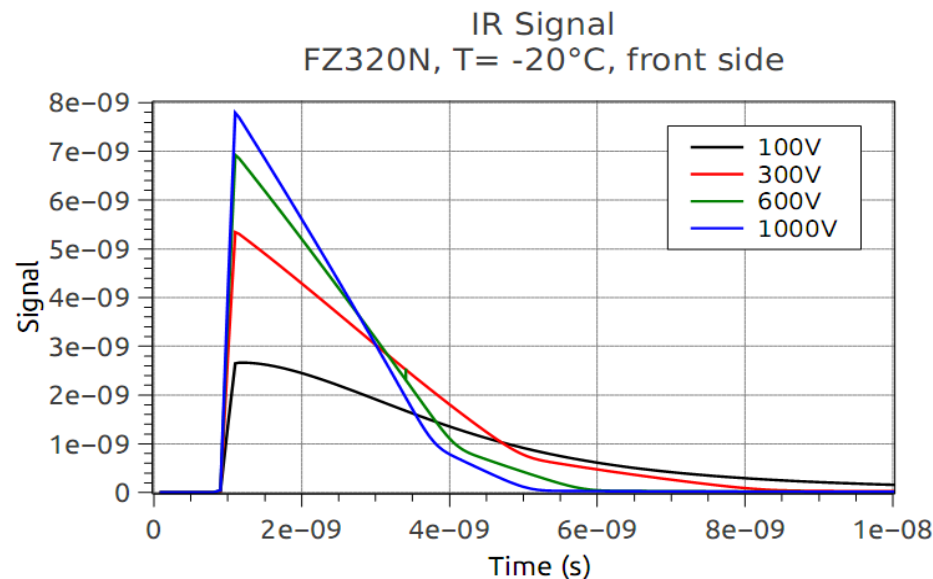
Depletion Voltage FZ200P Diodes



- Take same models – and plug them in for p-bulk diodes (320 μ m, 200 μ m)
- Neutron model fits again all points very well
- Proton model cannot be used for FZ320P – under investigation

Transient Simulation

- Shoot Laser at front side of the diode
 - Generate e/h-pairs
- Look at time evolution of current
- Convolute current with readout network
- CCE: Integrate IR pulses and normalize to unirradiated charge

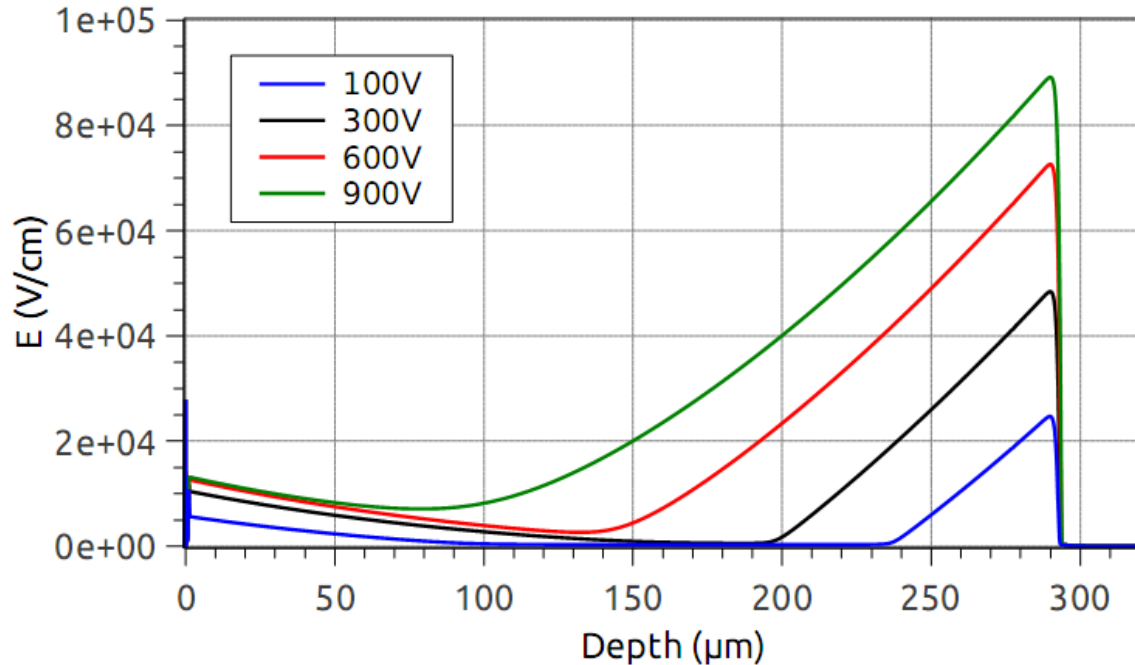


Focus on FZ320 n-bulk diodes

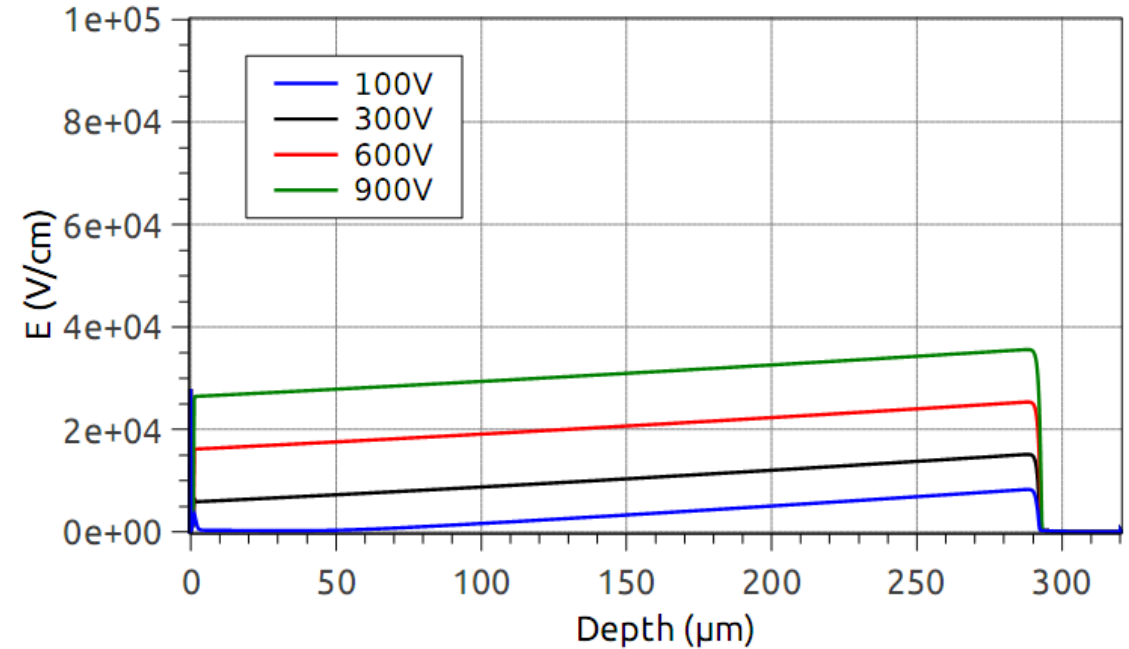
Electric Field – FZ320N

- Device "type inverted", start depletion from the back
- Double peak E-field visible

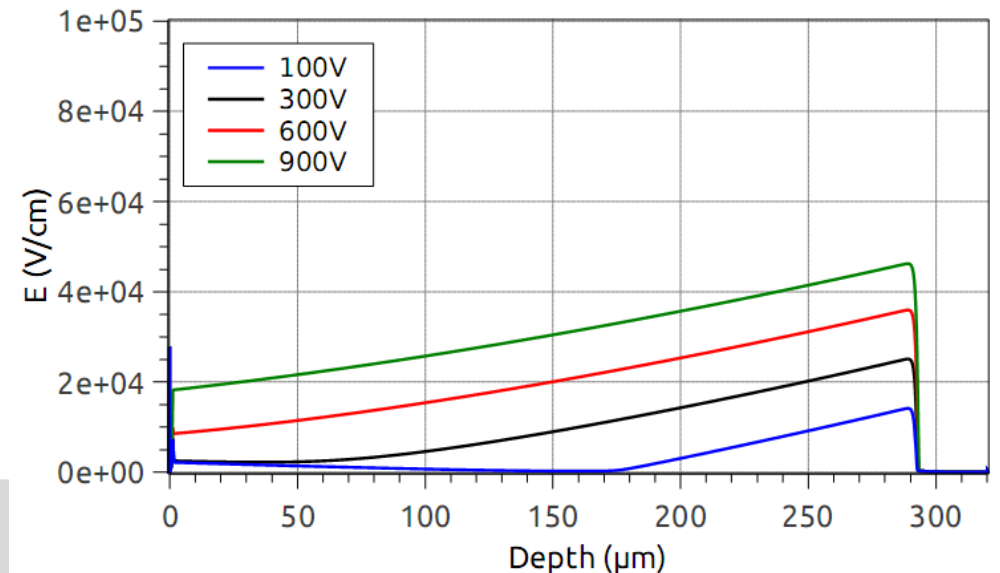
Electric Field
Proton Model, $F=1e15n_{eq}/cm^2$



Electric Field
Proton Model, $F=1e14n_{eq}/cm^2$



Electric Field
Proton Model, $F=3e14n_{eq}/cm^2$



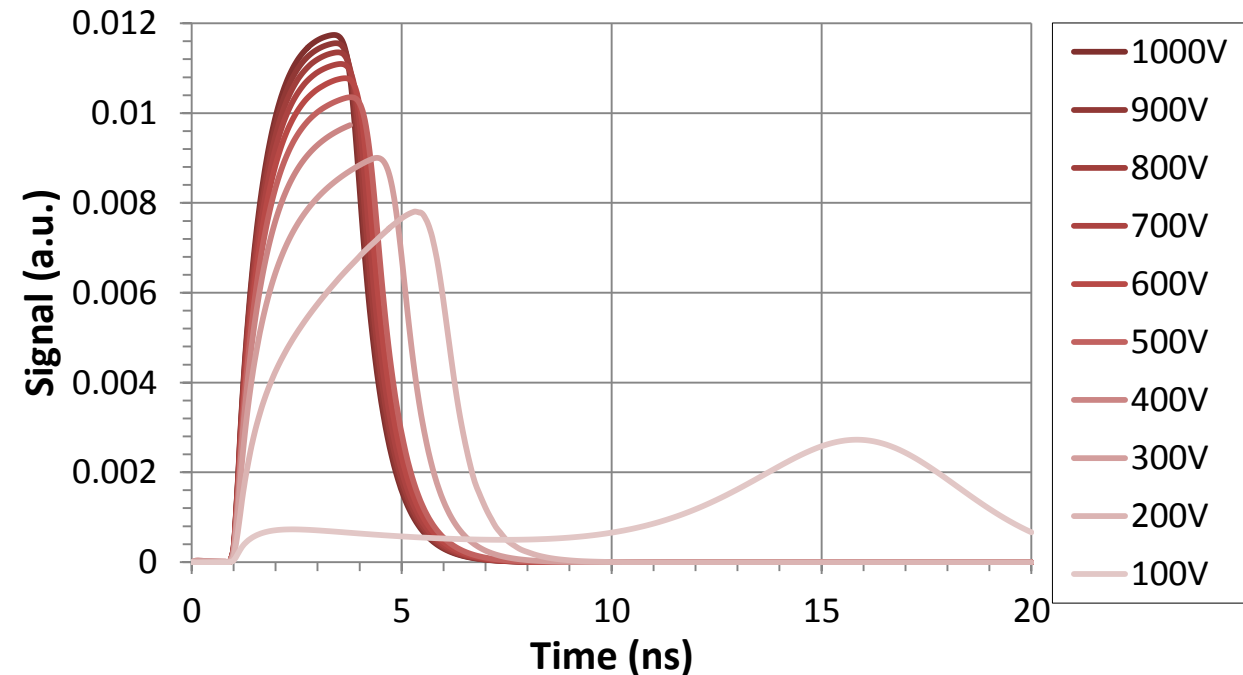
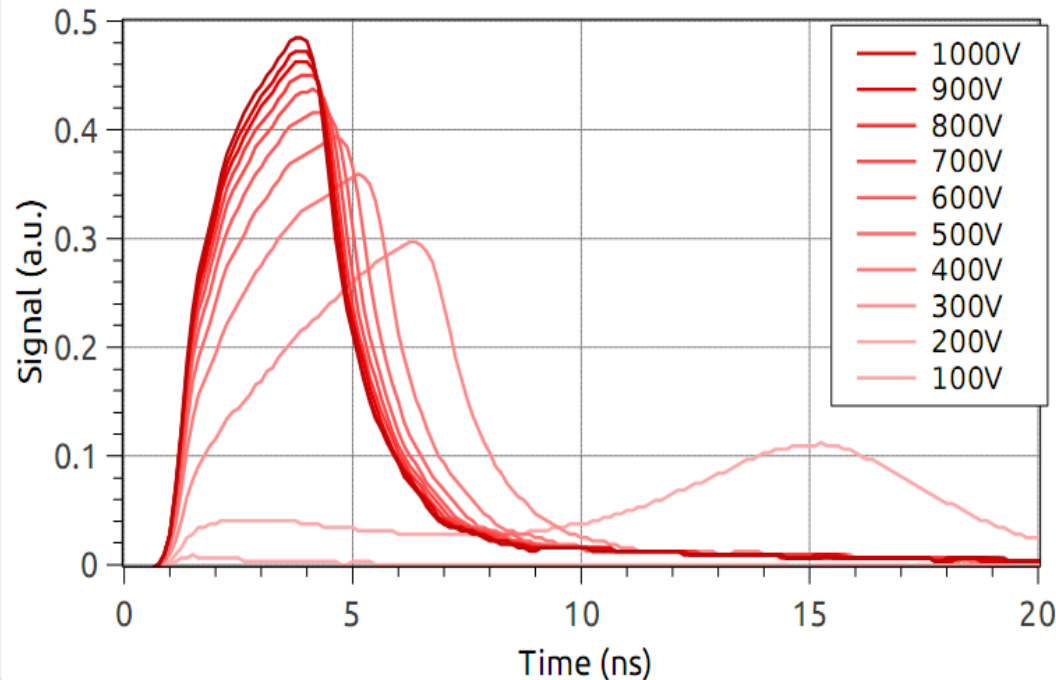
Results of the TCT Simulation

- 100V fits very good
- Peak heights well reproduced
- Shape and peak position at high voltages difficult – need to modify mobility / v_{sat}

Measurement

$F=1.1e14 neq/cm2$ (protons), $T= -20^{\circ}C$

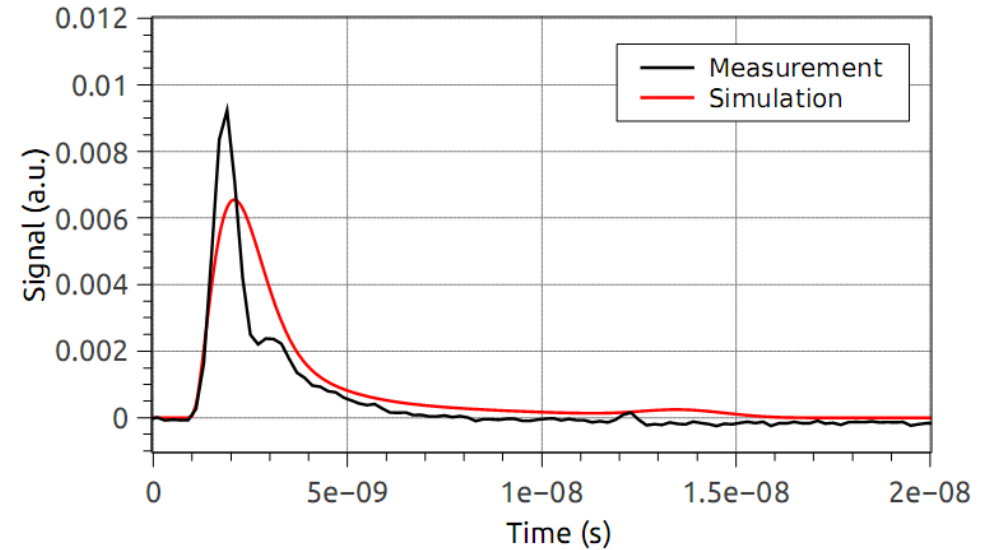
Simulation



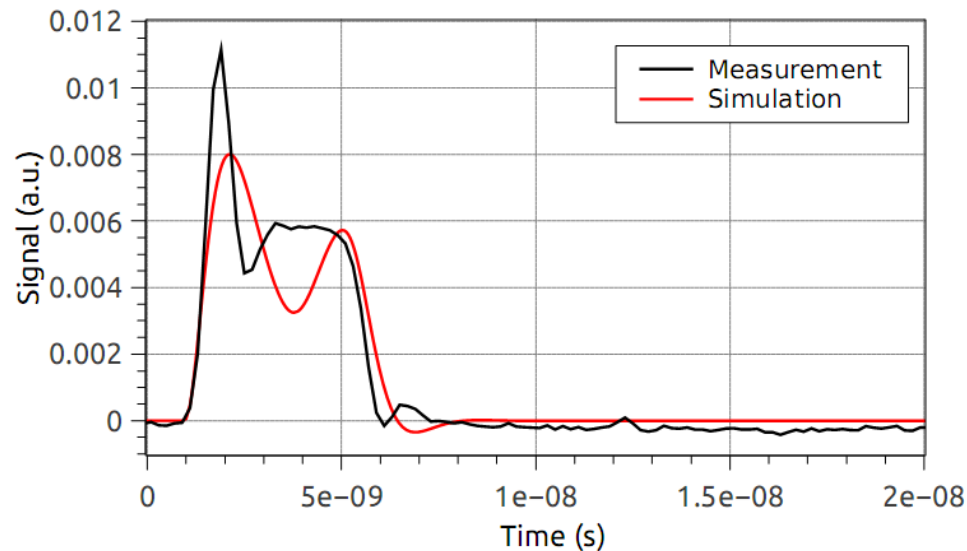
Results of the TCT Simulation

- TCT pulse is quite well reproduced by the simulation
- Second peak too high (?) – Trapping time too low?

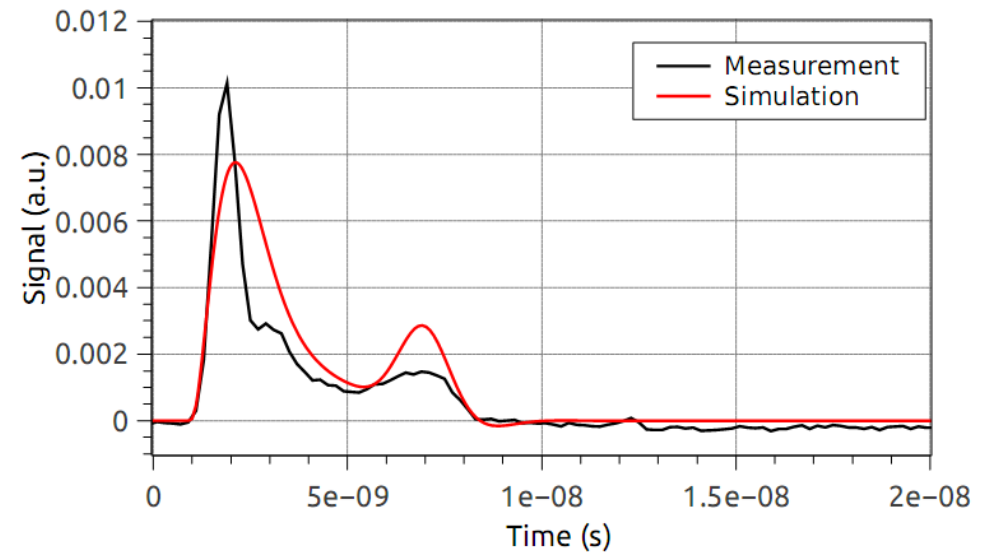
TCT Signal
 $F=1e15n_{eq}cm^{-2}$, $T= -20^{\circ}C$, $V=200V$



TCT Signal
 $F=1e15n_{eq}cm^{-2}$, $T= -20^{\circ}C$, $V= 600V$



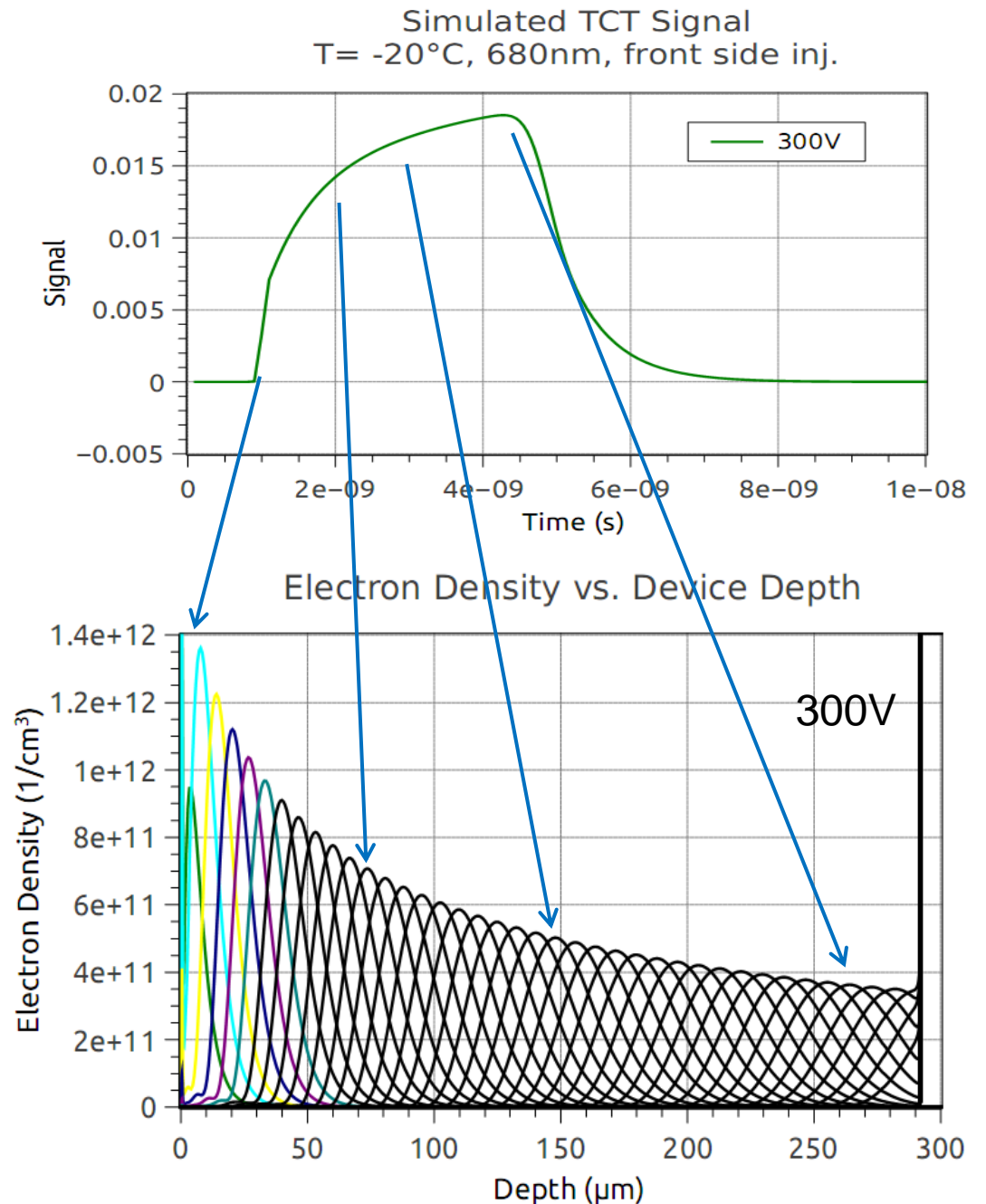
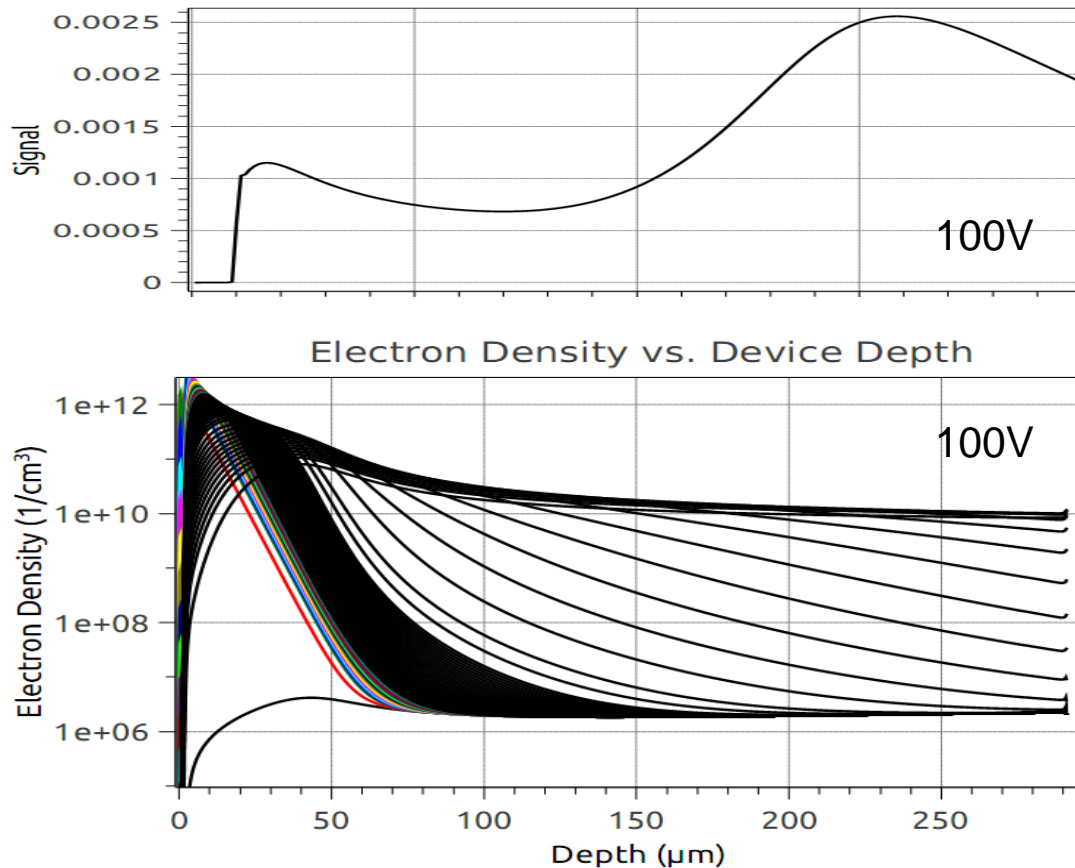
TCT Signal
 $F=1e15n_{eq}cm^{-2}$, $T= -20^{\circ}C$, $V=400V$



Investigation of Trapping

$F=1e14\text{neq/cm}^2$

- Electron density in the device is known
- Very fine simulation in time
- Investigate trapping of electrons during transport in the device

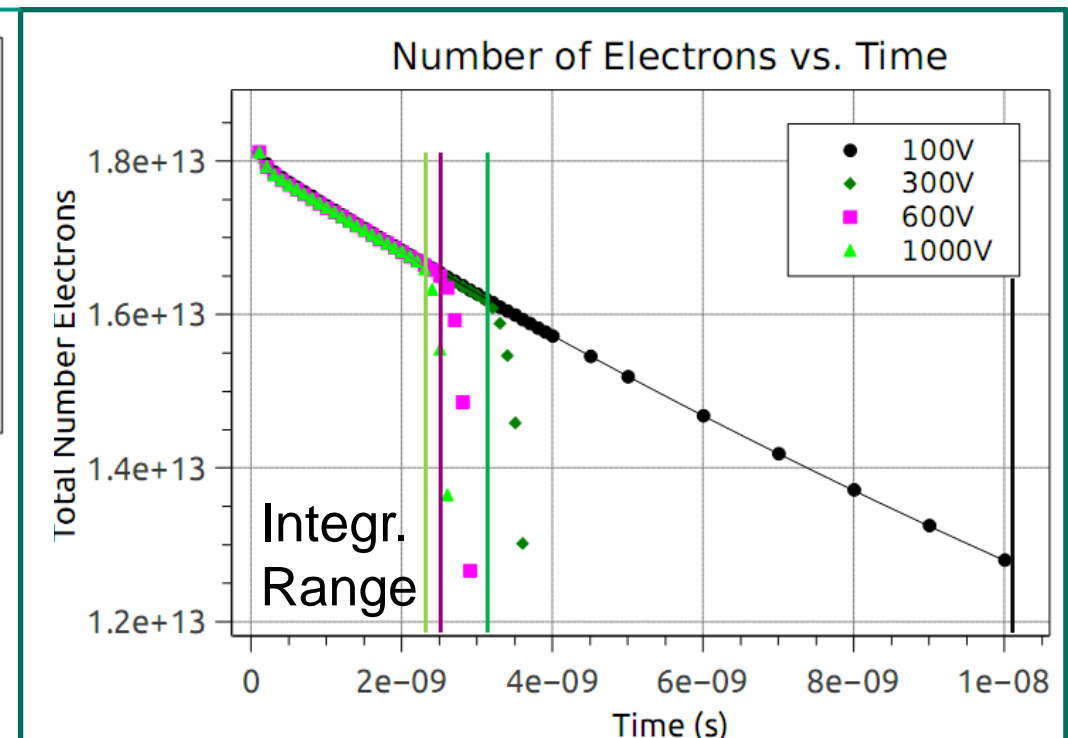
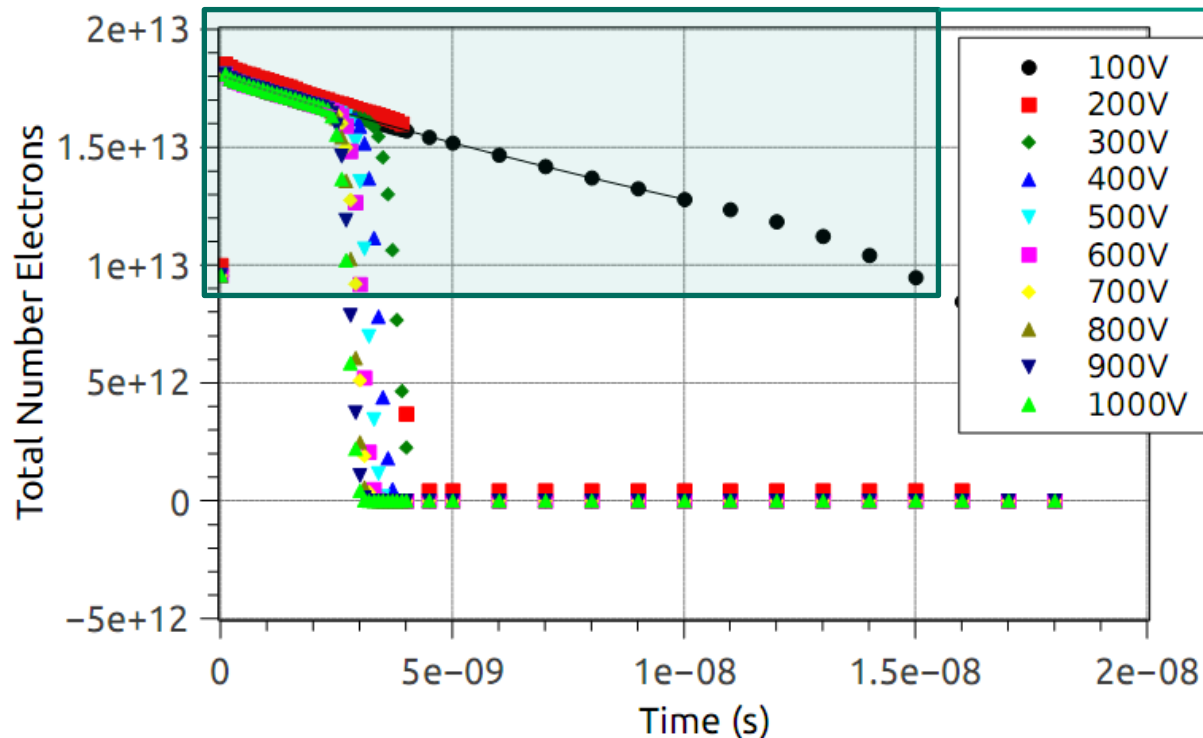


Electrons in the device

- Integration of the electron density at each time → total number of electrons
- Simple Approach: fit linear decay with trapping time
- Averaged trapping time: **28.5ns**

$$e = e_0 \times \exp\left(-\frac{t - t_0}{\tau}\right)$$

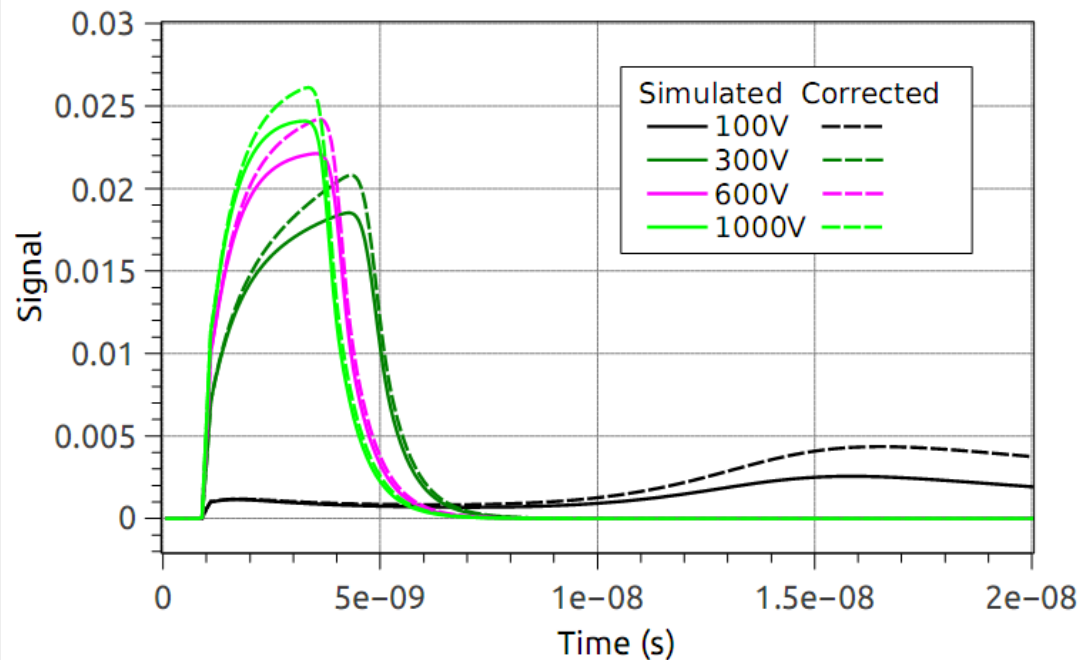
Number of Electrons vs. Time



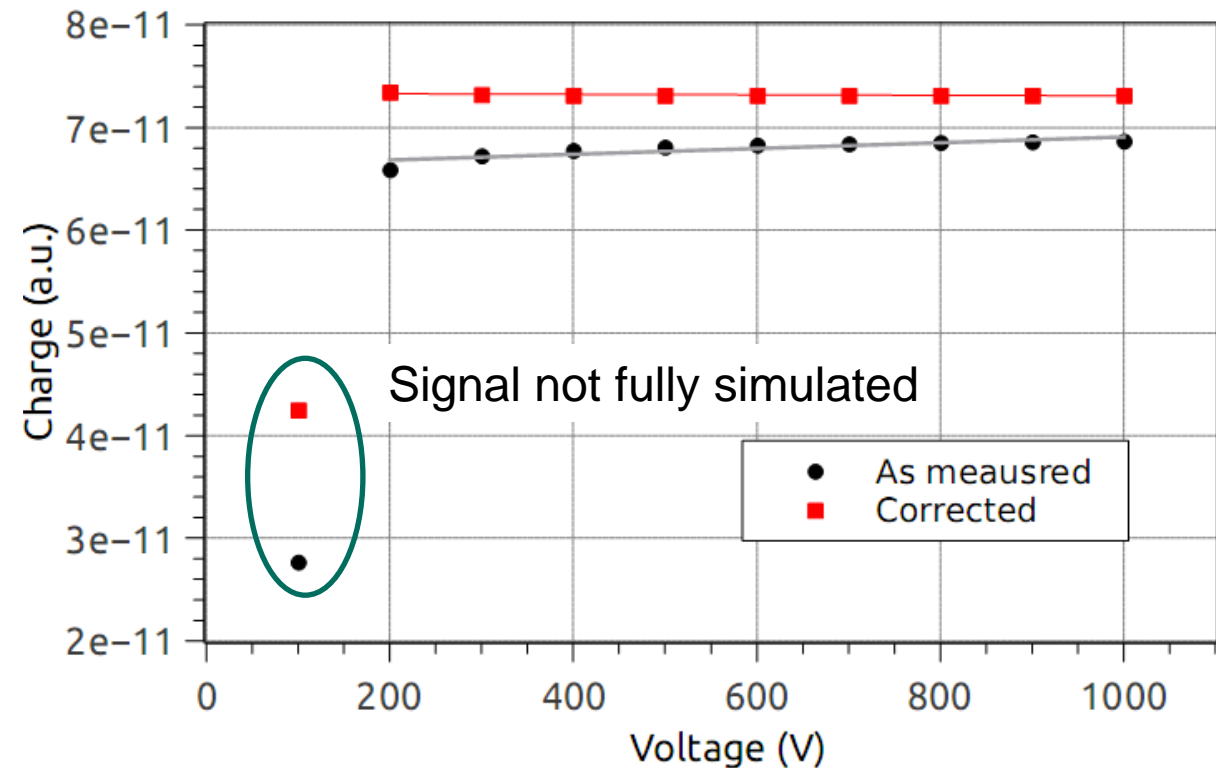
Integrated Signal

- Signal corrected by trapping time
- 28.5ns is in the range also found in the literature
 (~25ns @ $1e14\text{neq/cm}^2$ e.g. by G.Kramberger et al., NIMA 476, 645 and NIMA 481, 297)

Measured and corrected TCT Signal

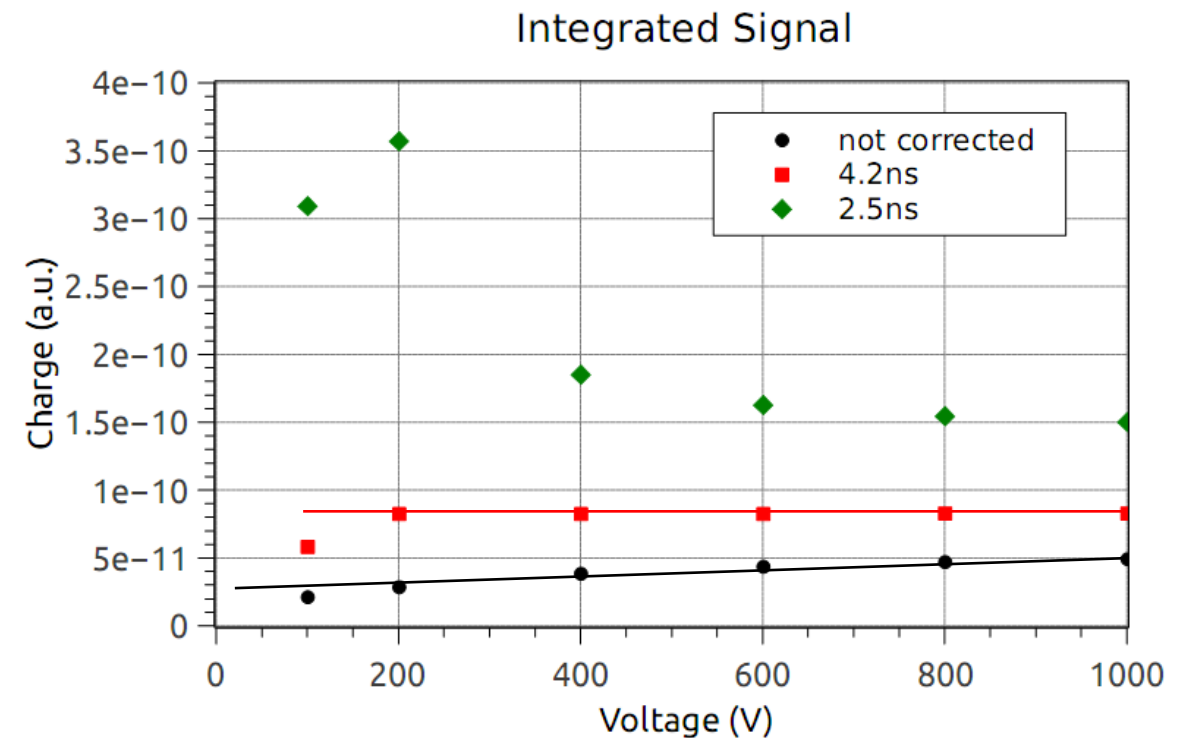
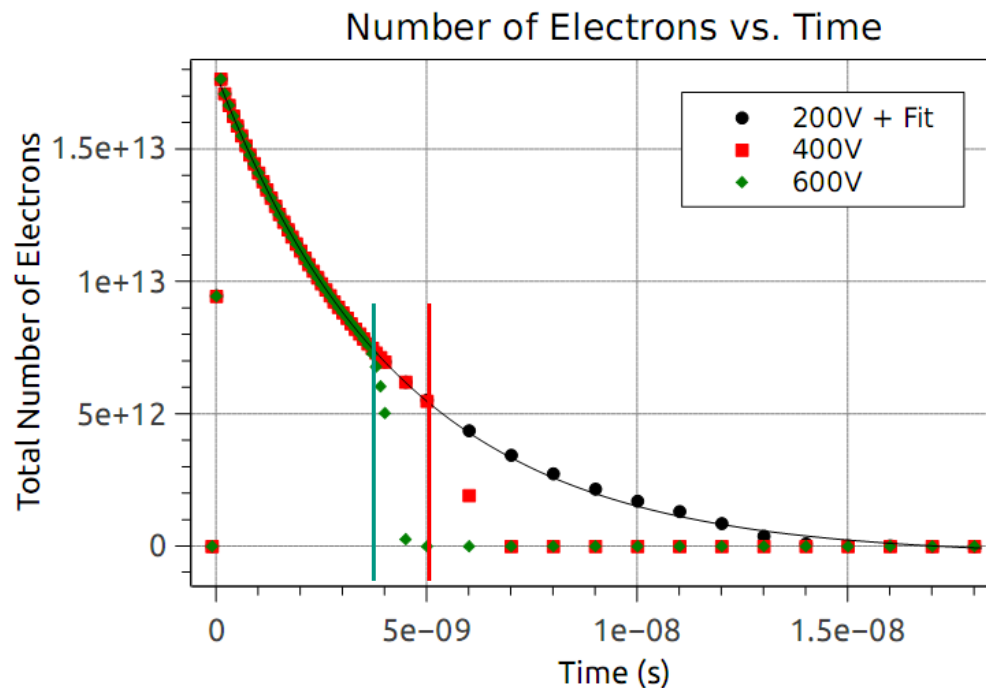


Integrated Signal



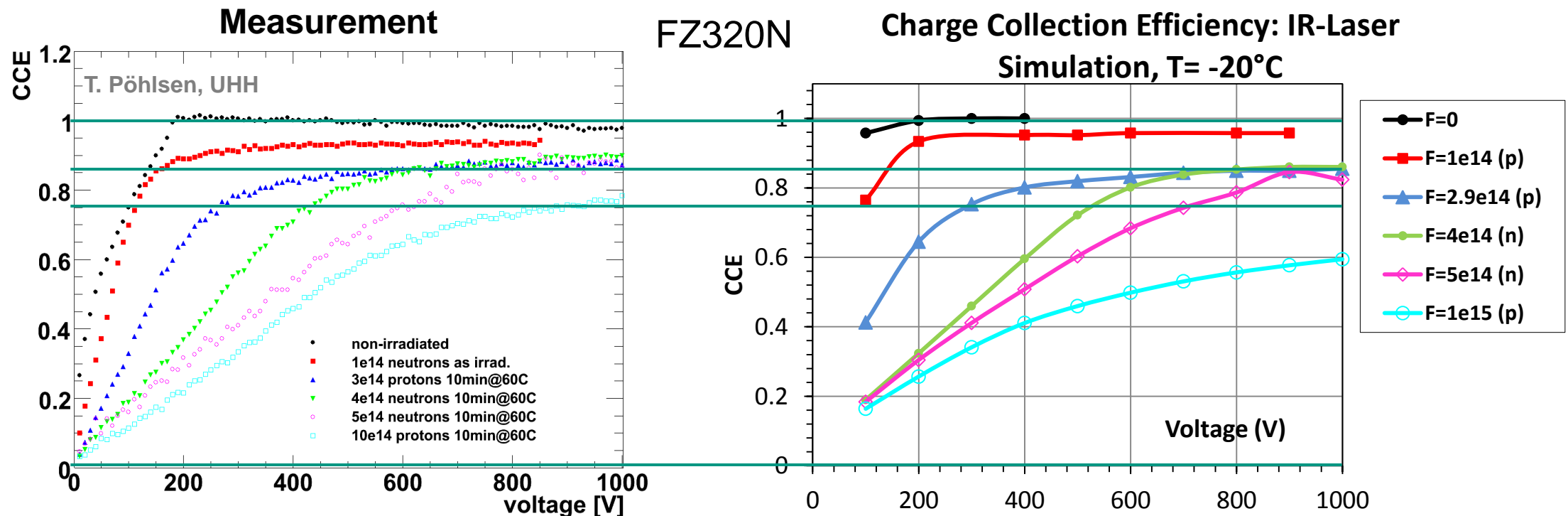
Investigation of Trapping $F=1e15n_{eq}/cm^2$

- Averaged trapping time: $4.2ns > 2.5ns$ (expected trapping time @ $1e15n_{eq}/cm^2$)
- Correction with $2.5ns$ leads to over-correction of collected charge



Results of the CCE Simulation

- Charge Collection Efficiency
 - Simulated with IR laser
- Agreement between Measurement and Simulation quite good
 - Although trapping time is larger at $1e15n_{eq}/cm^2$ – simulated CCE is lower



Summary

- Starting from the EVL model, a two-defect model has been tuned to describe diodes from the HPK campaign
- Linear fits for the defect concentrations matching
 - Leakage current
 - Depletion voltage
- Simulation of TCT pulses possible
 - Matching not perfect – tuning of mobility, saturation velocity may be needed
- Trapping time implemented in the simulator
 - Agreement with measured values at $1e14n_{eq}/cm^2$
 - At $1e15n_{eq}/cm^2$ trapping time is larger – but also V_{dep} is quite low
 - Simulation may be a way to determine trapping times
- Agreement of the CCE simulation with measurements (except $1e15n_{eq}/cm^2$)

Last Words

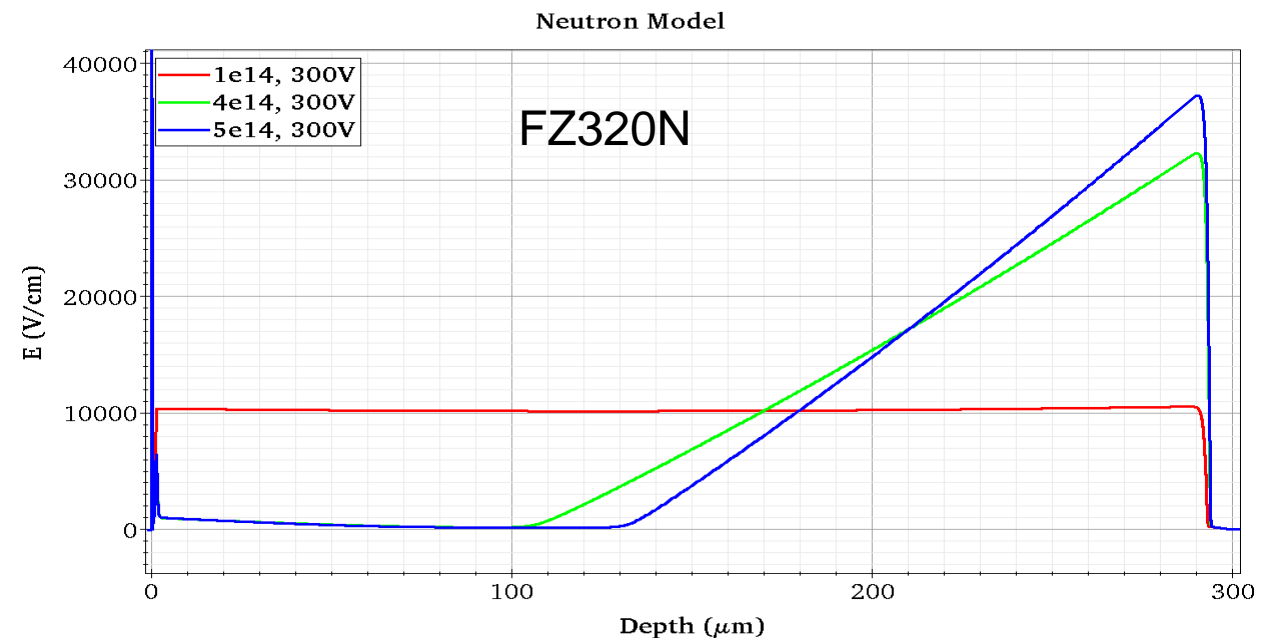
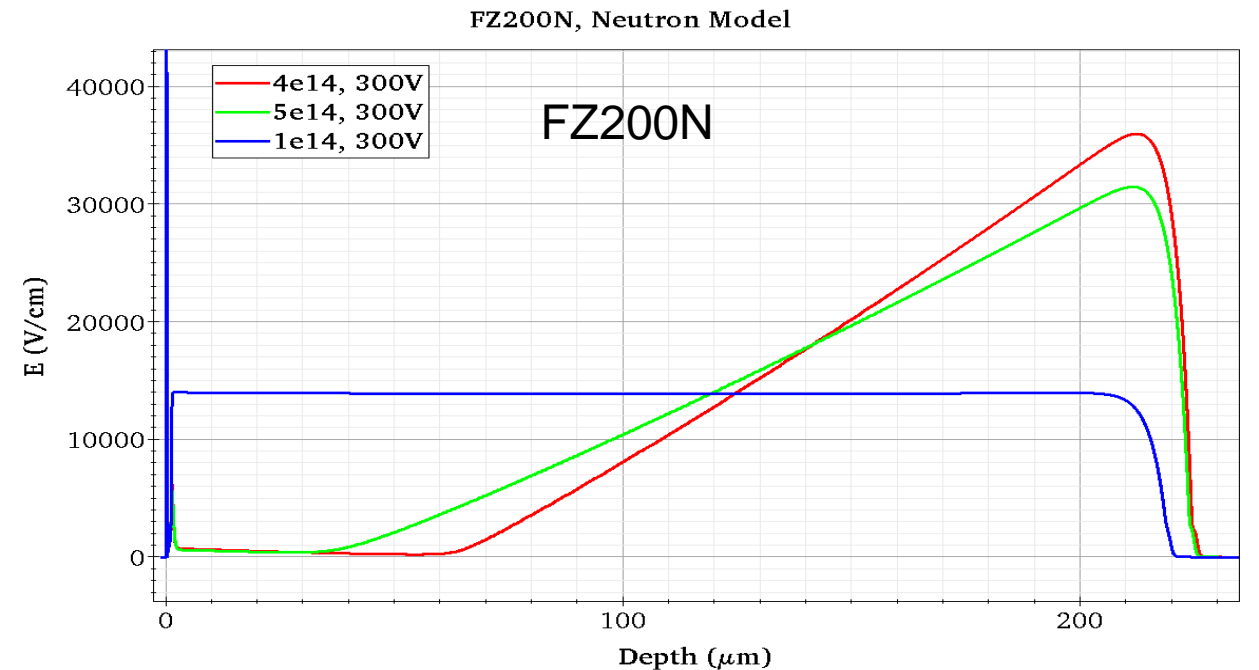
- Simulations are a mighty tool for description of irradiated silicon detectors
- Converging to a **coherent overall picture** including
 - Leakage current
 - Depletion Voltage
 - TCT
 - CCE
- Still a long way to go to include **all effects**:
Temperature, Annealing, mixed Irradiation (p+n)

Thanks for your attention!

ADDITIONAL INFORMATION

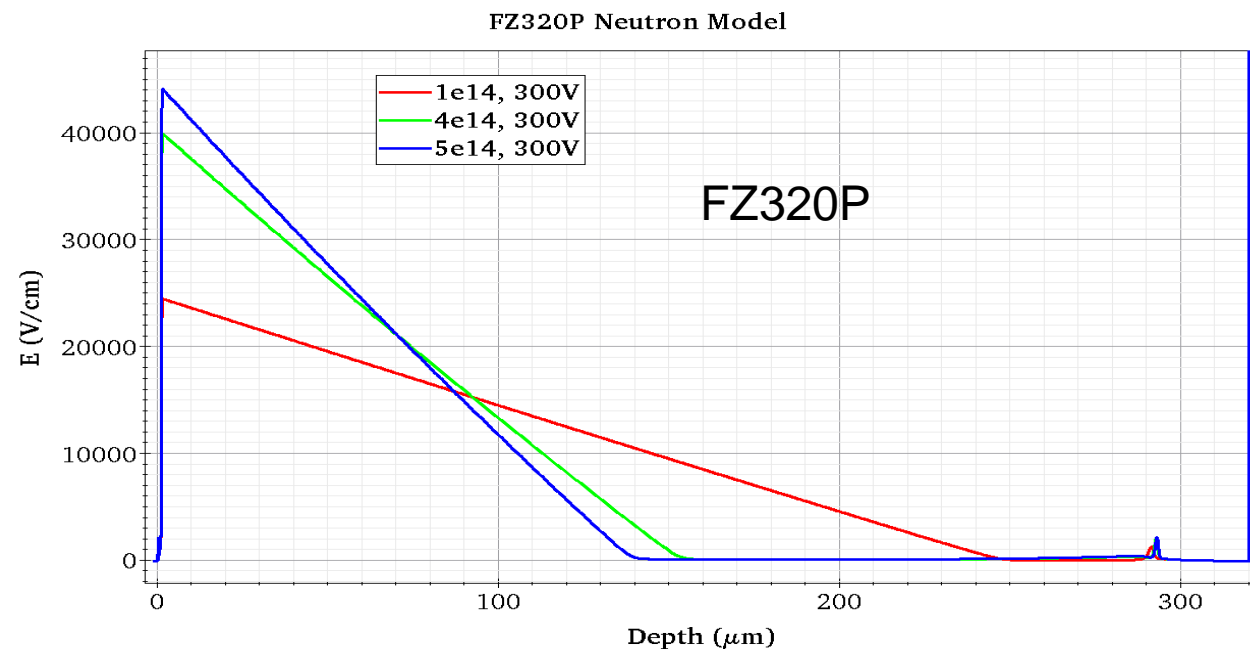
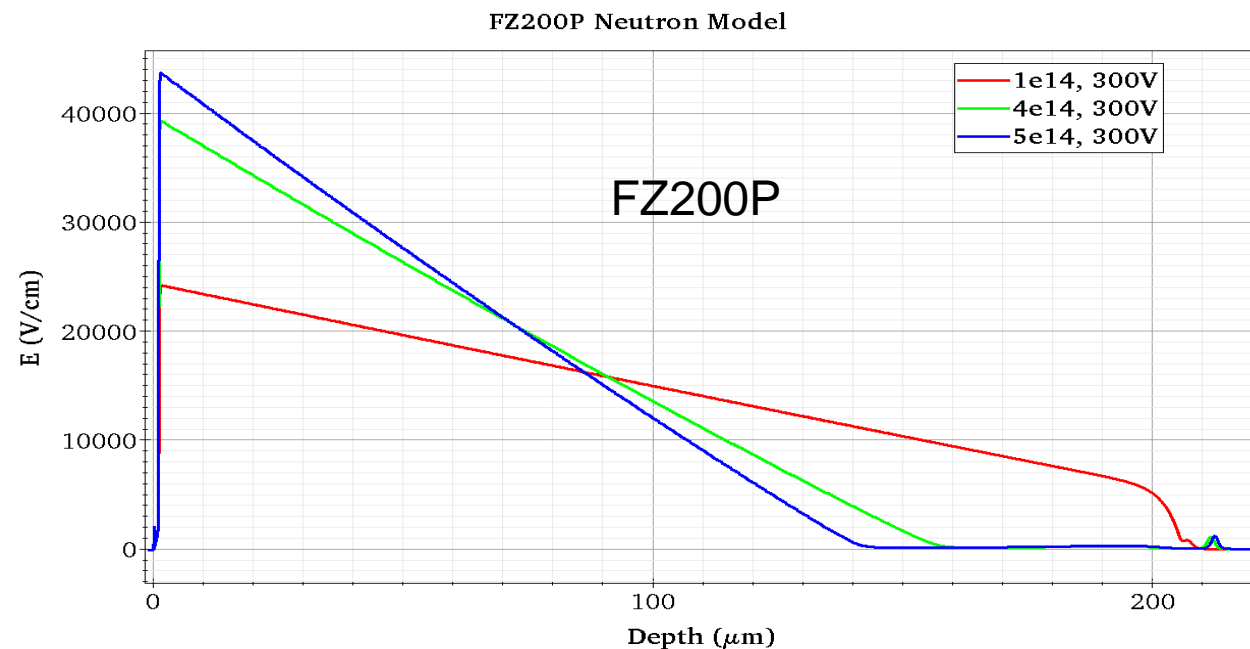
Electric field for n-type detectors

- $1e14 \text{ neq/cm}^2$ is just at "type inversion"
- Higher fluences clearly deplete from the backside



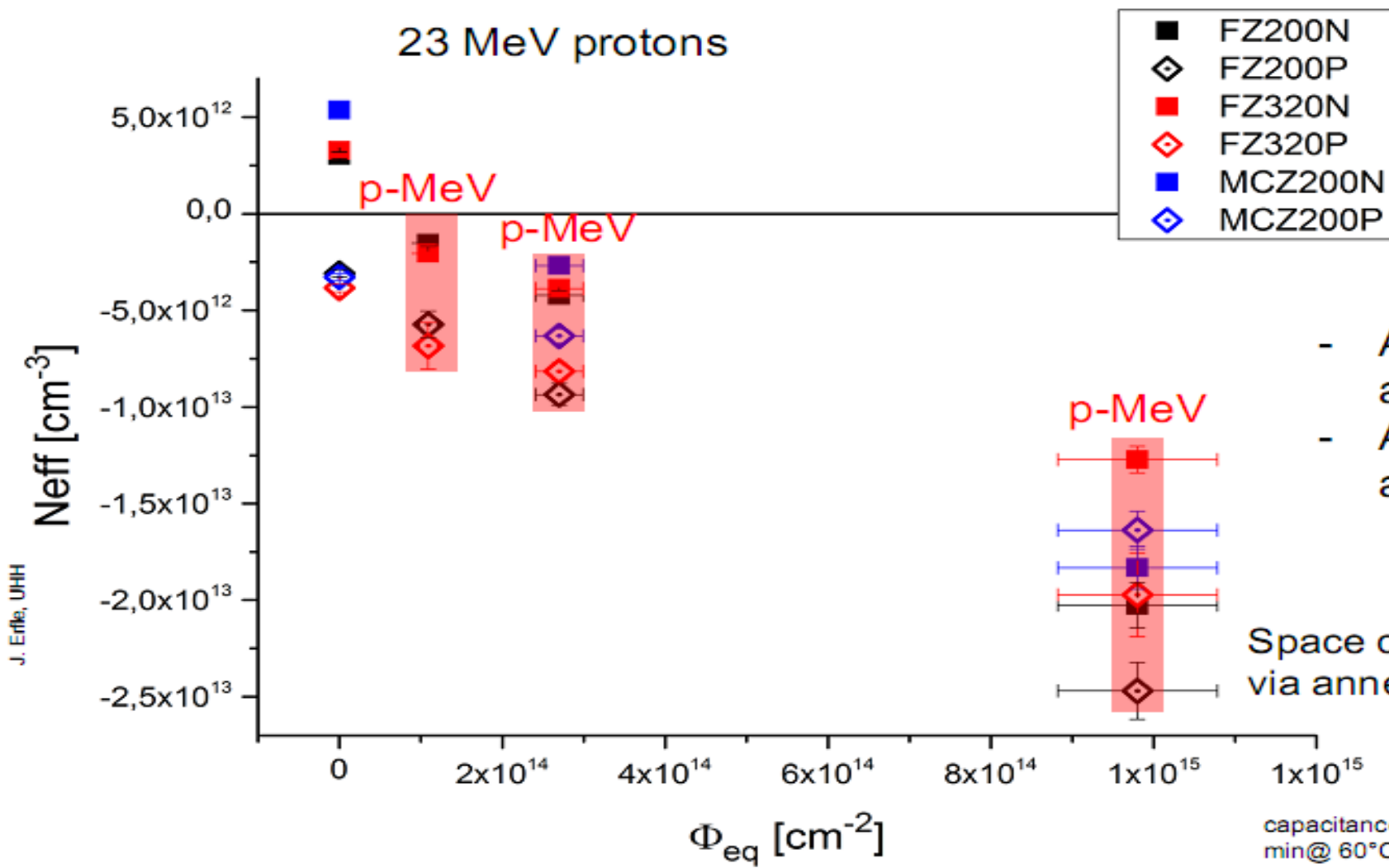
Electric field for p-type detectors

- P-type clearly depletes from the front (not "type inverted")



Proton irradiation

$$|N_{eff}| = \frac{2\epsilon\epsilon_0}{q_0} \frac{V_{dep}}{d^2}$$

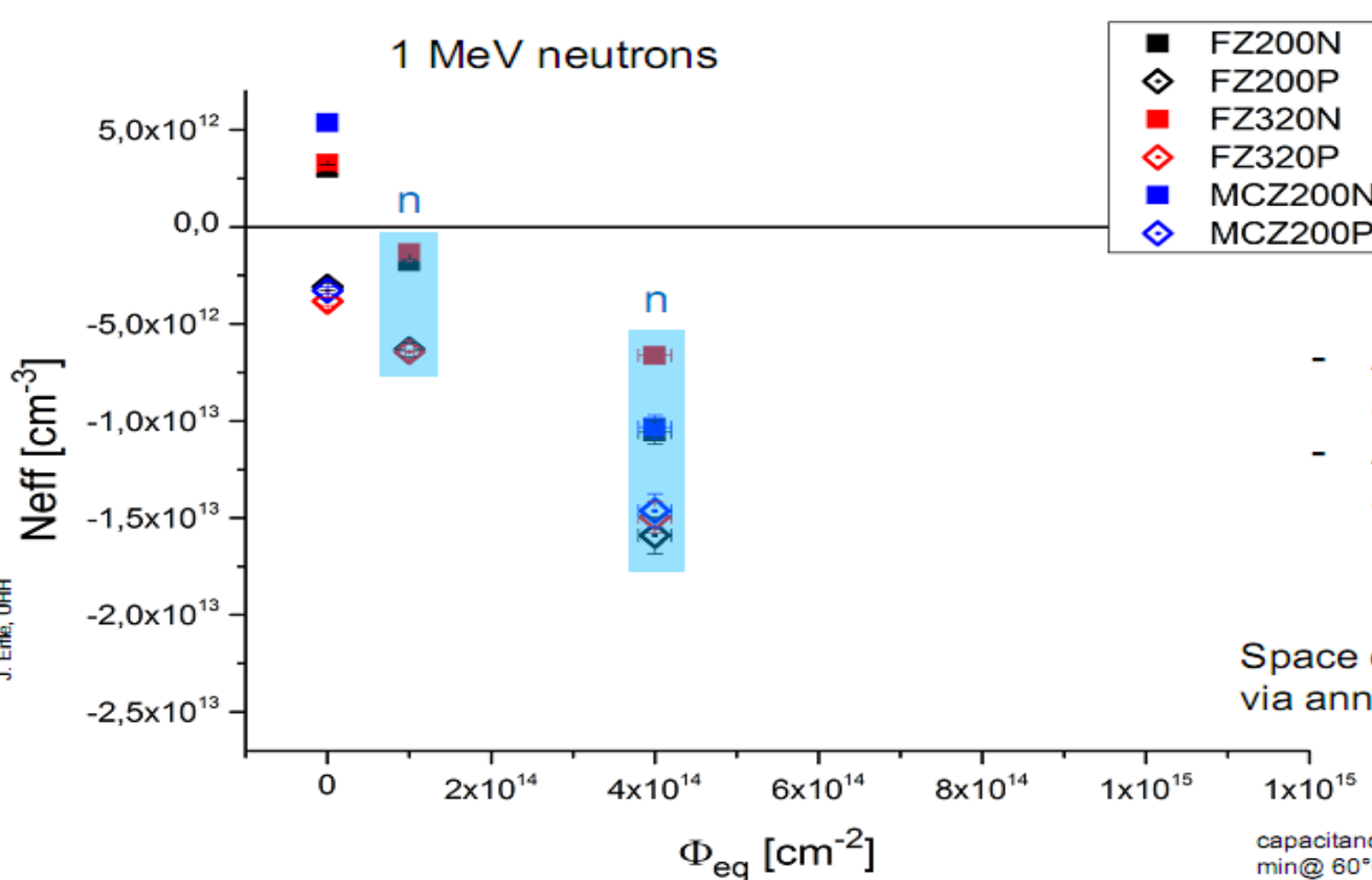


- All n-type materials are type inverted
- All p-type materials are not type inverted

Space charge sign determined via annealing and TCT.

capacitances are measured after annealing of 10 min @ 60°C at 0°C, 1kHz, guard ring grounded

Neutron irradiation



$$|N_{eff}| = \frac{2\epsilon\epsilon_0 V_{dep}}{q_0 d^2}$$

- All n-type materials are type inverted
- All p-type materials are not type inverted

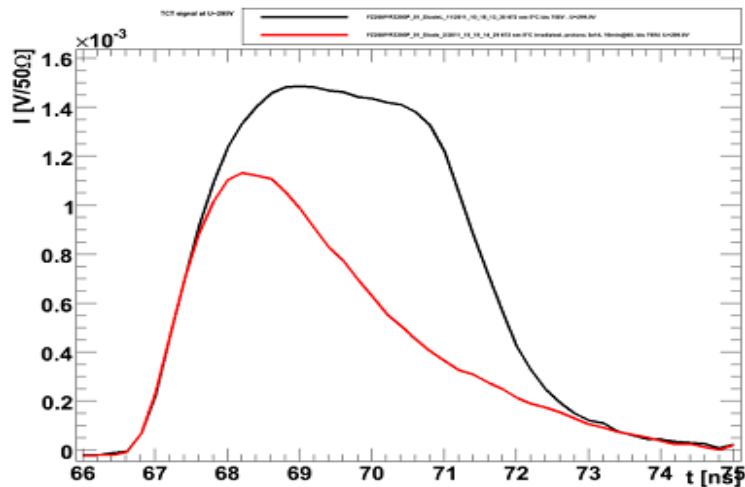
Space charge sign determined via annealing and TCT.

capacitances are measured after annealing of 10 min @ 60°C at 0°C, 1kHz, guard ring grounded

The experimental situation for FZ P-type

- TCT Signals of FZ P-type
- Unirradiated
- **Proton irradiation: $3e14 neq/cm^2$**
- Not type inverted: Depletion from the front

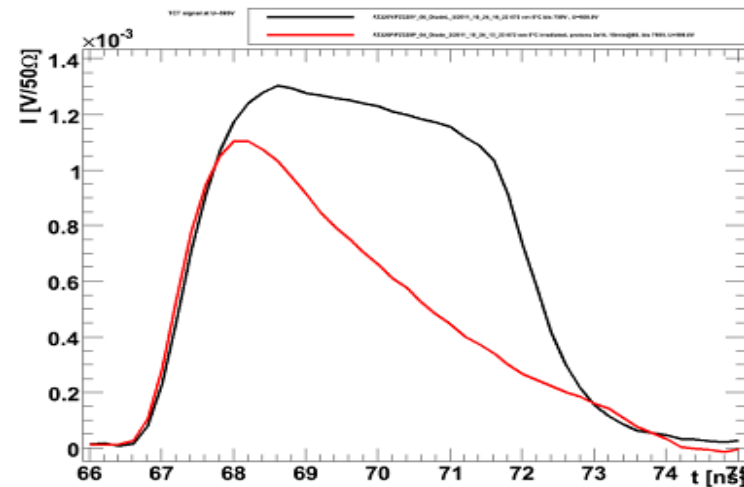
FZ200P



courtesy of T. Pöhlsen

300V

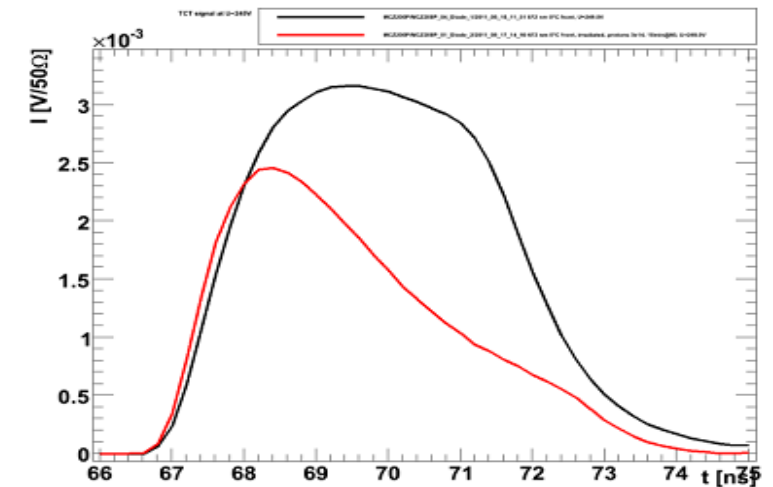
FZ320P



courtesy of T. Pöhlsen

600V

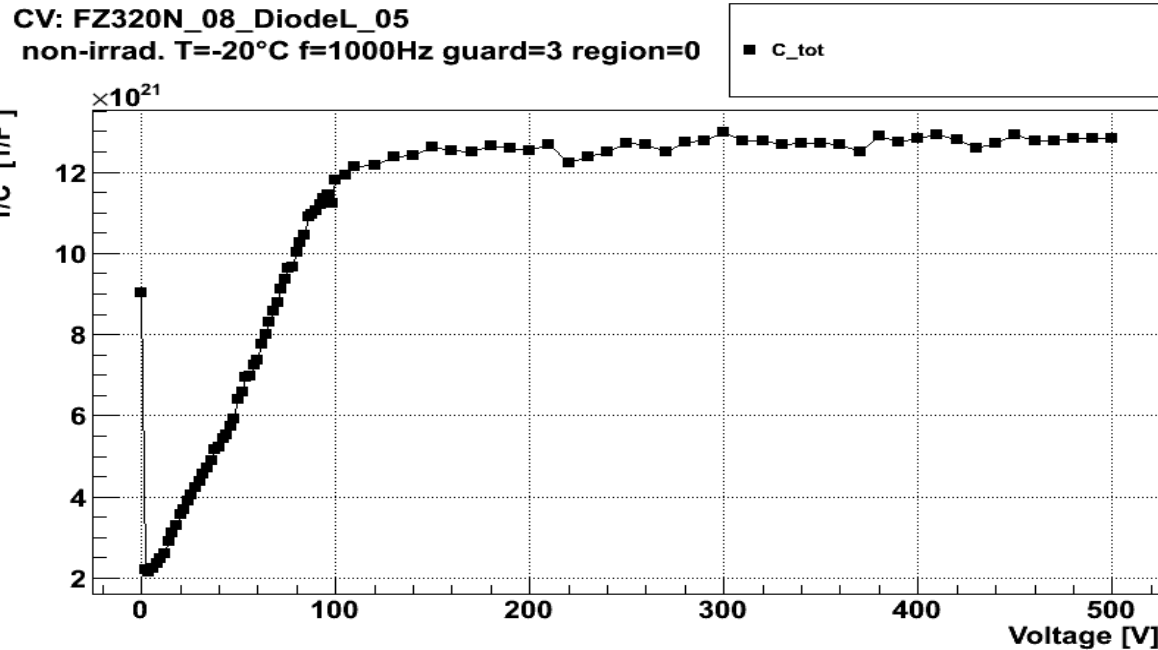
MCZ200P



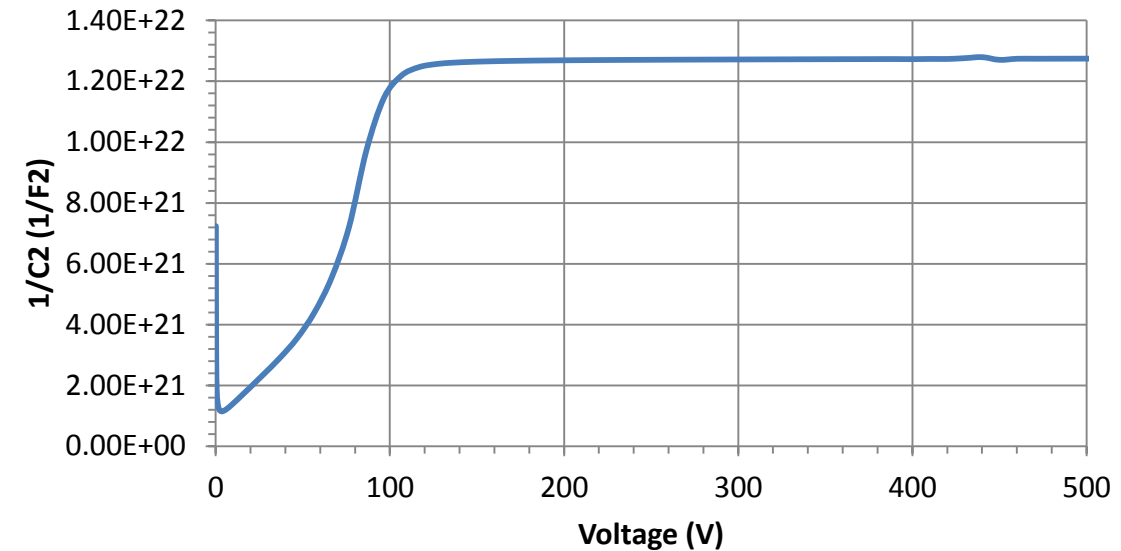
courtesy of T. Pöhlsen

250V

1e14neq/cm2, -20°C, 1kHz



Capacitance - Voltage (F=1e14neq/cm2, T=253K)

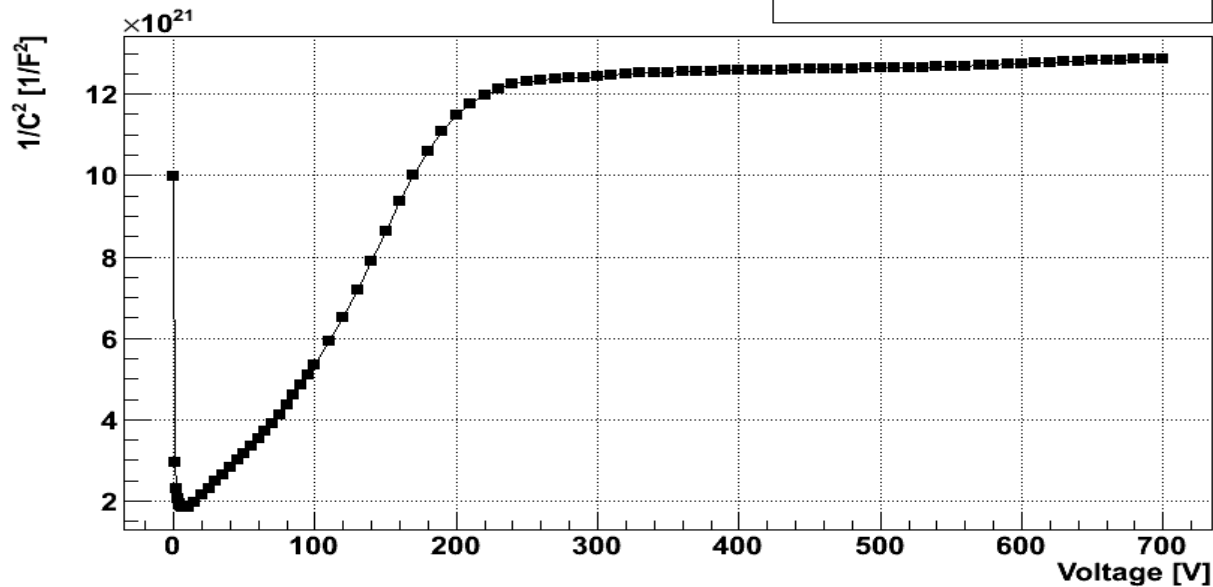


- Very good agreement
- Correct end capacitance
- Kink in the low voltage region
 - Maybe tunable by the cross sections of holes (for donor) or electrons (for acceptor)

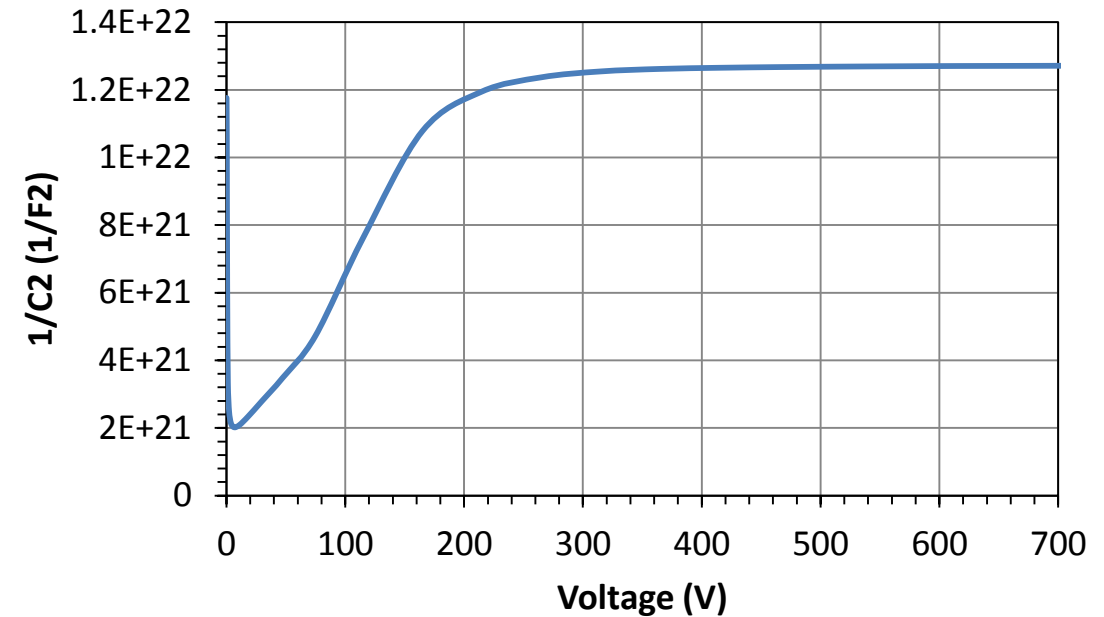
2.9e14, -20°C, 1kHz

CV: FZ320N_04_Diode_1

non-irrad. T=-20°C f=1000Hz guard=3 region=1

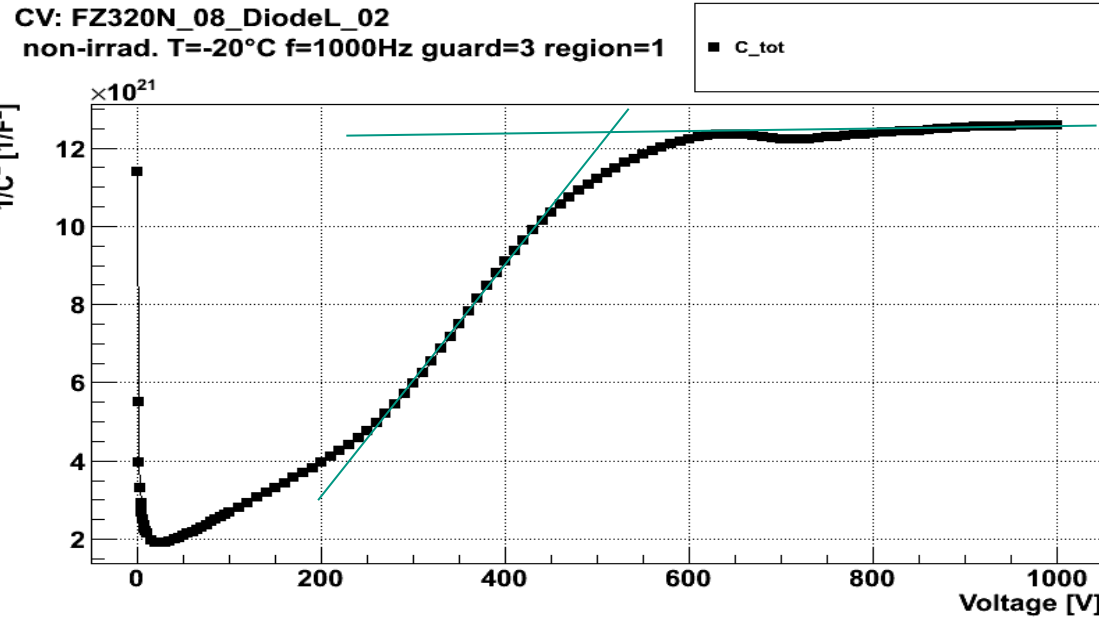


Depletion Voltage
 $F=3e14\text{neq/cm}^2$, T=-20°C, 1kHz

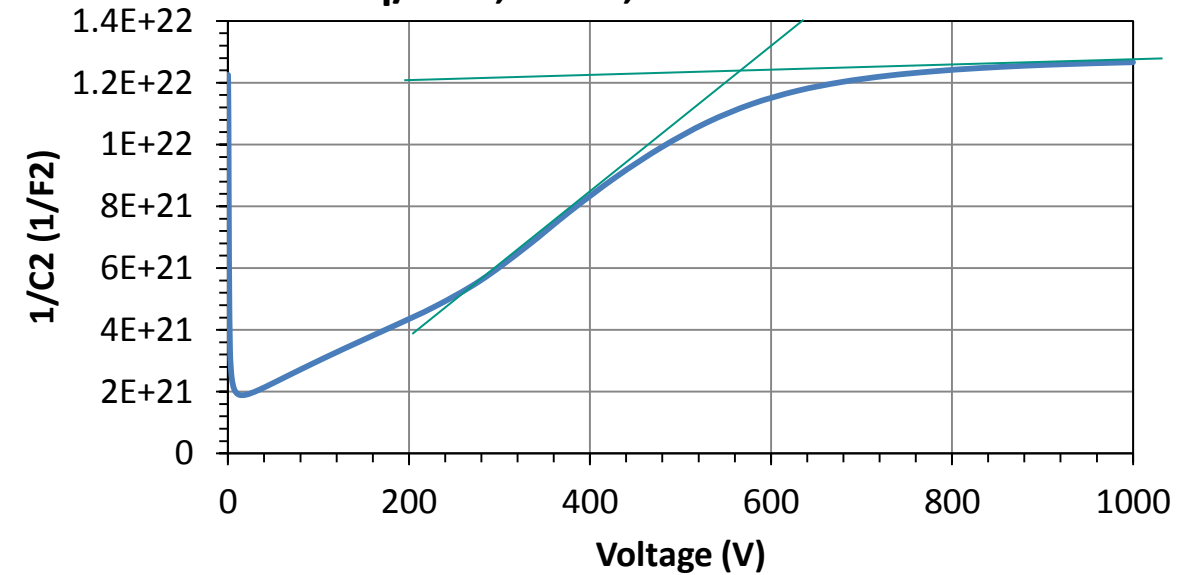


- Very good agreement
- Slight slope before depletion also visible in measurement
- Correct end capacitance

1e15neq/cm2, -20°C, 1kHz



Depletion Voltage 1e15neq/cm2, -20°C, 1kHz



- Kink at 300V correct
- Depletion Voltage (linear fits) about the same
- Slight disagreement around depletion voltage