



# Enhanced $B_d^0 \rightarrow \mu^+ \mu^-$ Decay: What if?

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# Enhanced $B_d^0 \rightarrow \mu^+ \mu^-$ Decay: What if?



If observed  $\geq 4 \times 10^{-10}$  (2011-2012 data!),  
then the 126 GeV boson might not be the Higgs.

## I. Intro: from Straub to Stone

Mild Motivation:  $\sin 2\Phi_{B_d} \equiv \sin 2\beta/\phi_1$  tension

## II. Constraints & Formulas

$\Delta m_{B_d}$  and  $B^+ \rightarrow \pi^+ \mu^+ \mu^-$

## III. Pheno Results with $t'$ -in-loop

## IV. Discussion

$b \rightarrow d$  **quad**rangle; CKM hierarchy implication

## V. Conclusion

4G回馬槍?!



## I. Intro: from Straub to Stone

but, last chance for New Physics  
in flavor sector at LHC8

Mild Motivation:  $\sin 2\Phi_{B_d} \equiv \sin 2\beta/\phi_1$  tension

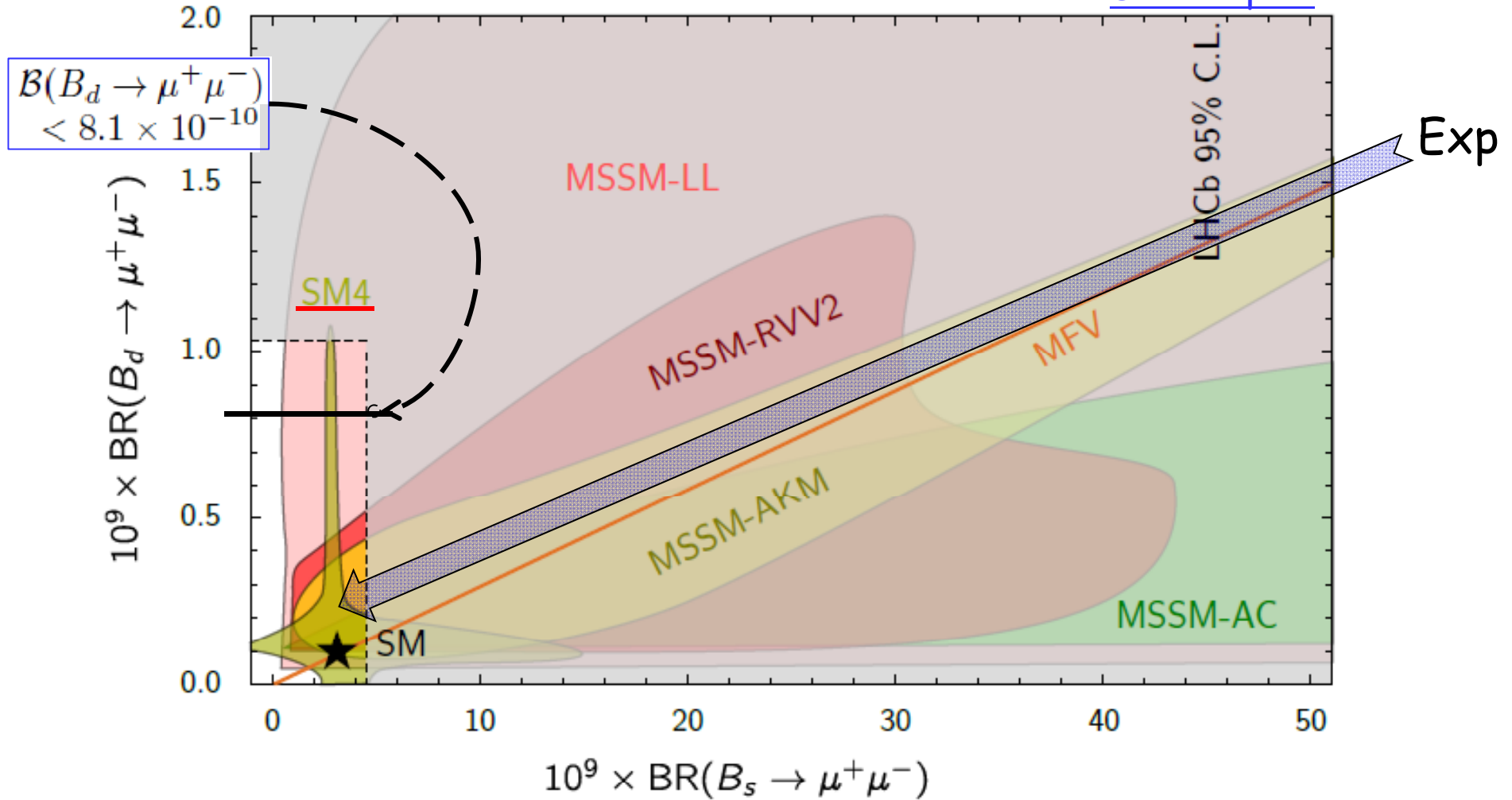


# Disappointment: No New Physics



the  $\sin\phi_s$  destroyer-of-hope ...

“Straub plot”



David Straub (SNS & INFN, Pisa)

Moriond EW Session, 2012



# Disappointment: No New Physics

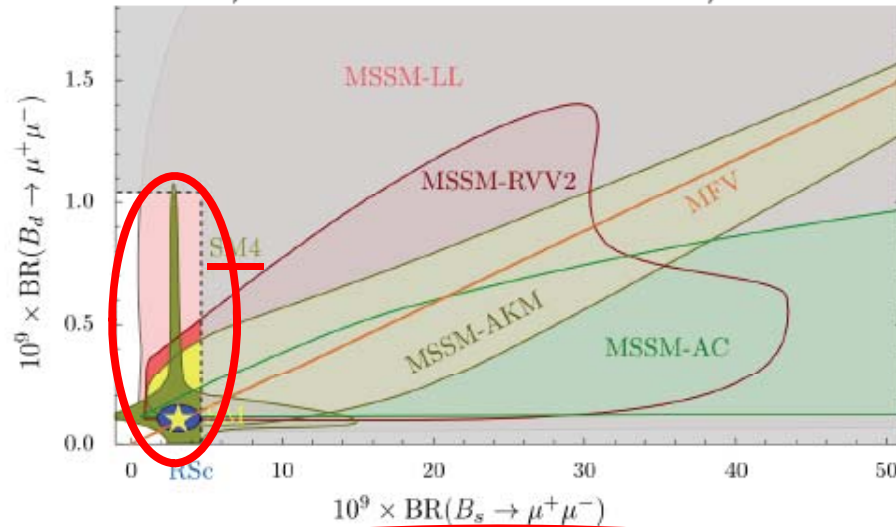


the  $\sin\phi_s$  destroyer-of-hope ...

Sheldon Stone @ ICHEP2012

## Implications II

David Straub, Rencontres de Moriond EW, La Thuile (2012)



The 125 GeV Higgs observations kills off 4<sup>th</sup> generation models as the production cross-section would be 9x larger & decays to  $\gamma\gamma$  suppressed



R.I.P.

ICHEP, Melbourne, July 9, 2012

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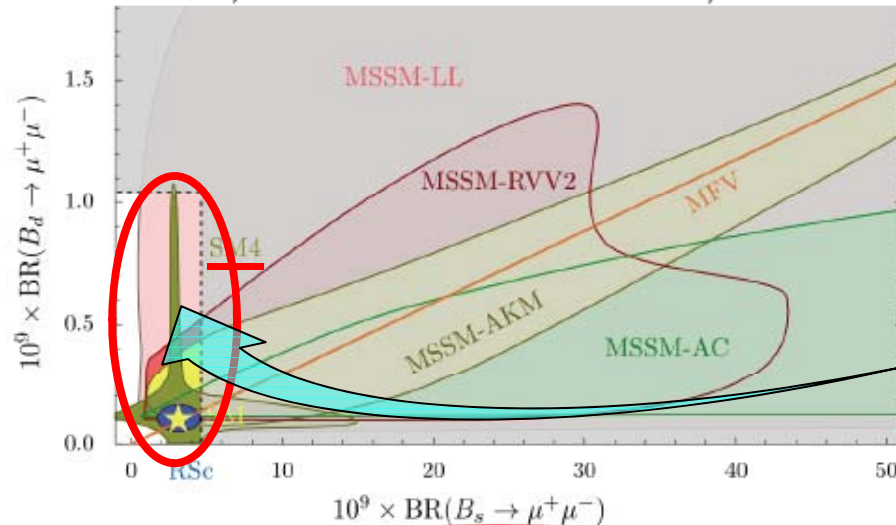
# However, SM Higgs is flavor-blind



Sheldon Stone @ ICHEP2012

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Flavor people should keep CKM-extension in mind.

Higgs does not enter these loops;

and, 126 GeV boson could be "dilaton" still ...

R T D

**Keep on Searching**  
w/ Gusto!

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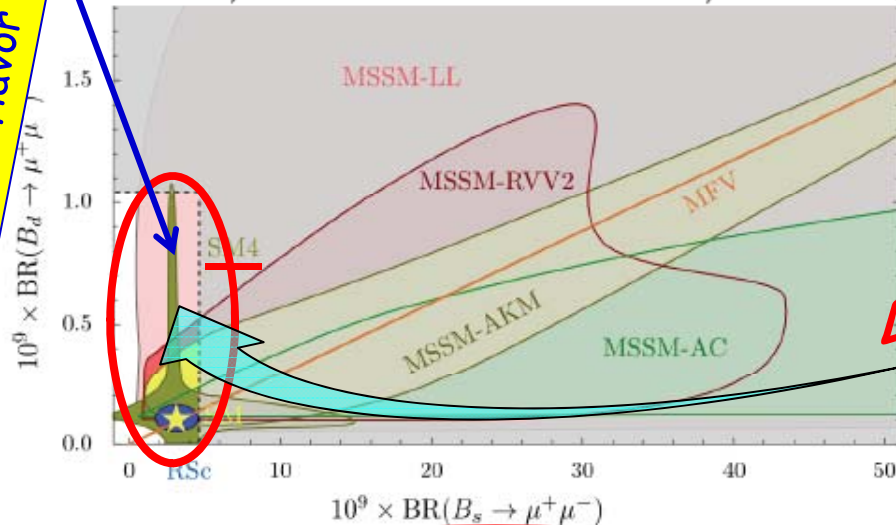


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last chance for New Physics in flavor sector at LHC8

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ICHEP, Melbourne, July 9, 2012

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N.B. For 4G dynamical EWSB that permits dilaton, see Mimura, WSH, Kohyama, 1206.6063



# Mild Motivation: $\sin 2\Phi_{B_d} \equiv \sin 2\beta/\phi_1$ tension



Lunghi & Soni, '08; Buras & Guadagnoli, '08

- $\sin 2\beta/\phi_1 = 0.679 \pm 0.020$

Direct Measurement

- $\sin 2\beta/\phi_1 = \begin{cases} 0.76 & \text{for } |V_{ub}|^{\text{ave}} \\ 0.63 & \text{for } |V_{ub}|^{\text{excl}} \end{cases}$

Indirect from other meas.

arg

$$\lambda_t^{\text{SM}} = -\lambda_u - \lambda_c \simeq -|V_{ud}||V_{ub}|e^{-i\phi_3} + |V_{cd}||V_{cb}|$$

taking  $|V_{ud}| = 0.974$ ,  $|V_{cd}| = 0.23$  and  $|V_{cb}| = 0.041$

$$\phi_3 = (68^{+11}_{-10})^\circ$$

parameterize  $t'$ -effect  
to alleviate tension

$$\lambda_u + \lambda_c + \lambda_t + \lambda_{t'} = 0$$

$$\lambda_t = \lambda_t^{\text{SM}} - \lambda_{t'}$$

$$V_{t'd}^* V_{t'b}$$



$$\lambda_{t'} = r_{db} e^{i\phi_{db}}$$



Constrain





## II. Constraints & Formulas

$$\Delta m_{B_d} \text{ and } B^+ \rightarrow \pi^+ \mu^+ \mu^-$$

LHCb 2012: rarest B decay measured

N.B.  $b \rightarrow d\gamma$  hard to separate from  $b \rightarrow s\gamma$ ,  
hard for LHCb, and insensitive to  $4G$ .

$B \rightarrow \pi\pi$  much hadronic effect.



$$\Delta m_{B_d} \simeq \frac{G_F^2 M_W^2}{6\pi^2} m_{B_d} \hat{B}_{B_d} f_{B_d}^2 \eta_B |\Delta_{12}^d|,$$

$$\sin 2\Phi_{B_d} \simeq \sin(\arg \Delta_{12}^d),$$

$\sin 2\beta/\phi_1$

$$\Delta_{12}^d \equiv (\lambda_t^{\text{SM}})^2 S_0(x_t)$$

$$+ 2\lambda_t^{\text{SM}} \lambda_{t'} \Delta S_0^{(1)} + \lambda_{t'}^2 \Delta S_0^{(2)}$$

$$\Delta S_0^{(1)} \equiv \tilde{S}_0(x_t, x_{t'}) - S_0(x_t),$$

$$\Delta S_0^{(2)} \equiv S_0(x_{t'}) - 2\tilde{S}_0(x_t, x_{t'}) + S_0(x_t),$$

$$x_i = m_i^2/M_W^2$$

**t'-effect**

Remaining hadronic uncertainty

$$\hat{B}(B_d \rightarrow \mu^+ \mu^-) \equiv \frac{\mathcal{B}(B_d \rightarrow \mu^+ \mu^-)}{\Delta m_{B_d}} \Delta m_{B_d}^{\text{exp}}$$

$$= C \frac{\tau_{B_d} \Delta m_{B_d}^{\text{exp}} \eta_Y^2}{\eta_B} \frac{|\lambda_t^{\text{SM}} Y_0(x_t) + \lambda_{t'} \Delta Y_0|^2}{|\Delta_{12}^d|}$$

Ratio w/ Box

Buras '03

$$\Delta Y_0 = Y_0(x_{t'}) - Y_0(x_t)$$

$$C = 6\pi \left( \frac{\alpha}{4\pi \sin^2 \theta_W} \right)^2 \frac{m_\mu^2}{M_W^2}$$

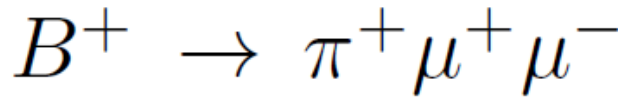


$$(2.3 \pm 0.6 \text{ (stat.)} \pm 0.1 \text{ (syst.)}) \times 10^{-8}$$

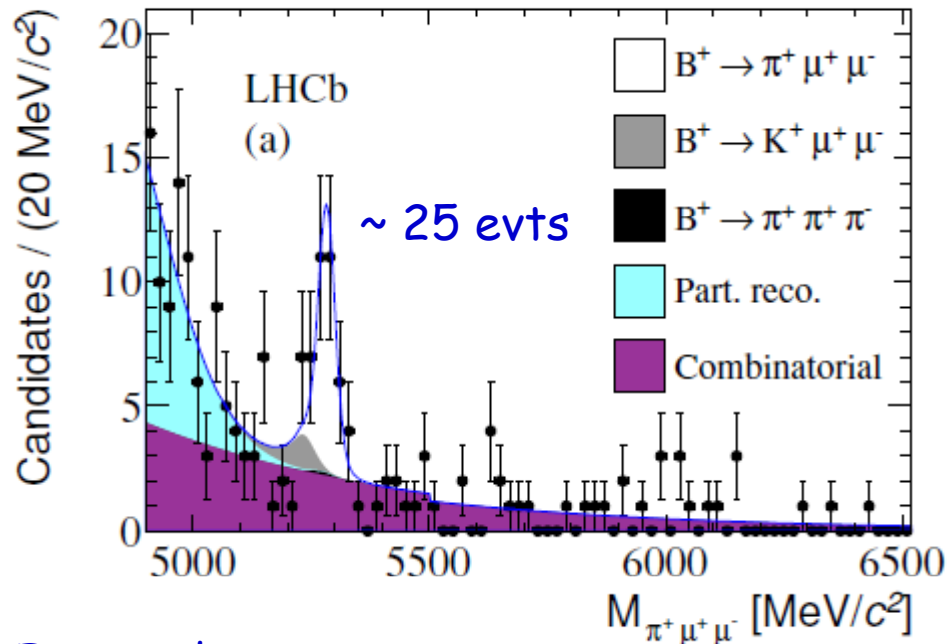


LHCb, JHEP 2012

first observation of



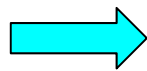
$b \rightarrow d\ell^+\ell^-$  transition



$1.0 \text{ fb}^{-1}$

To reduce Form Factor dep.

$$R_{\pi\mu\mu} \equiv \frac{\mathcal{B}(B^+ \rightarrow \pi^+ \mu^+ \mu^-)|_{4G}}{\mathcal{B}(B^+ \rightarrow \pi^+ \mu^+ \mu^-)|_{SM}}$$



Will plot contours to 2x - 3x

otherwise LHCb could tell?

integrated from  $q^2 = (1, 6) \text{ GeV}^2$

better numerical control

W.C. @ NLO

LO amplitude in QCDF

Beneke, Feldmann, Seidel, '01, '03



### III. Pheno Results with $t'$ -in-loop



~ incl.

$$|V_{ub}| = 4.15 \times 10^{-3}$$

$$m_{t'} = 700 \text{ GeV}$$

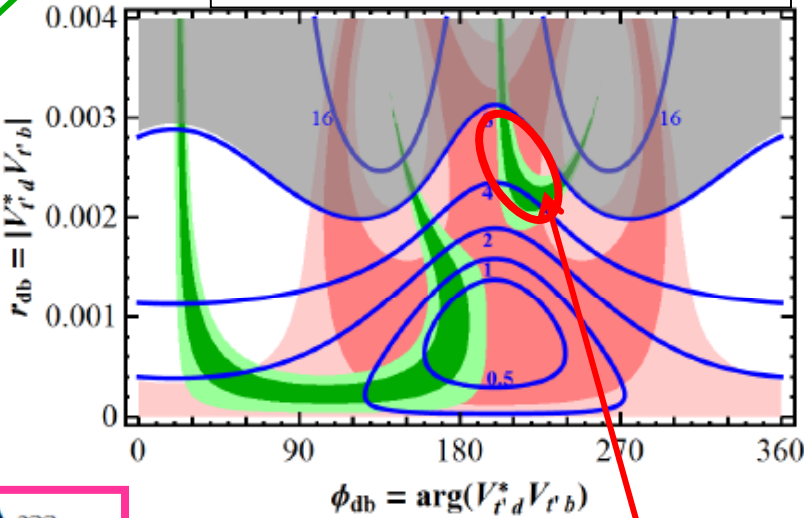
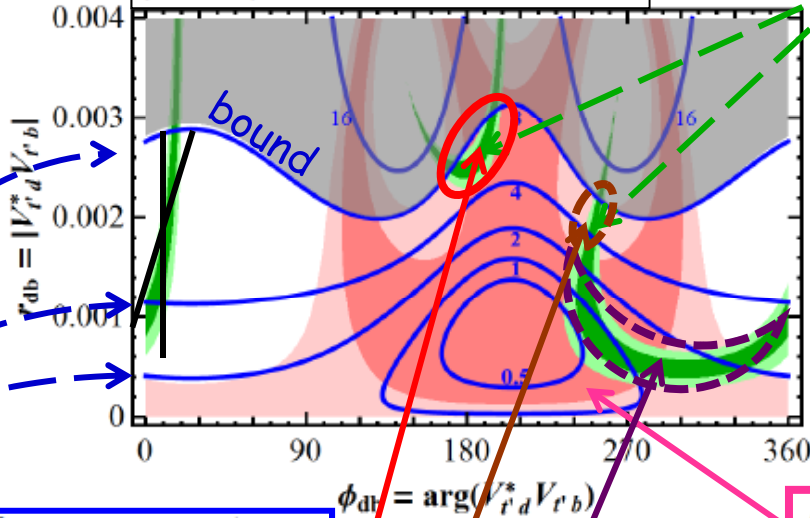
[LHC bound]



excl.

$$\sin 2\Phi_{B_d}$$

$$|V_{ub}| \sim 3.23 \times 10^{-3}$$



$$10^{10} \mathcal{B}(B_d \rightarrow \mu^+ \mu^-)$$

$$\Delta m_{B_d}$$

A'

Regions A, B & C: A & B give  $B_d \rightarrow \mu^+ \mu^- > 4x \text{ SM}$   
 C gives broad crescent in phase

A point each from A & A' is taken for later illustration



~ incl.

$$|V_{ub}| = 4.15 \times 10^{-3}$$

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[LHC bound



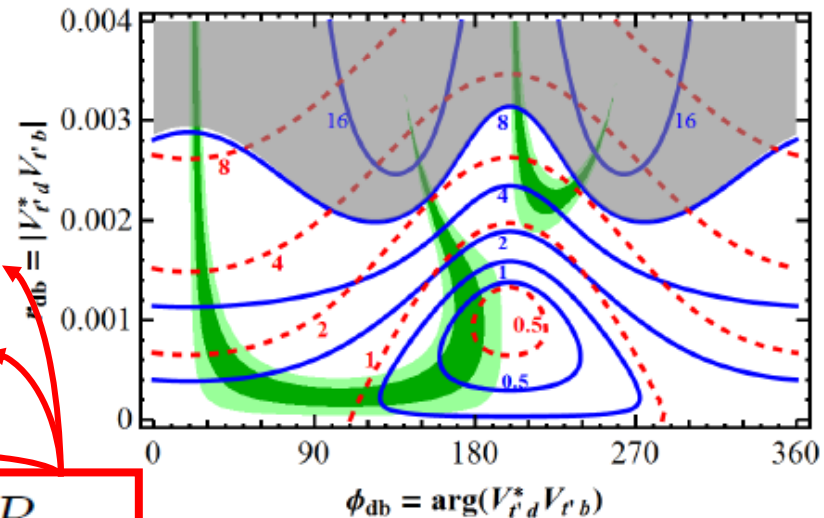
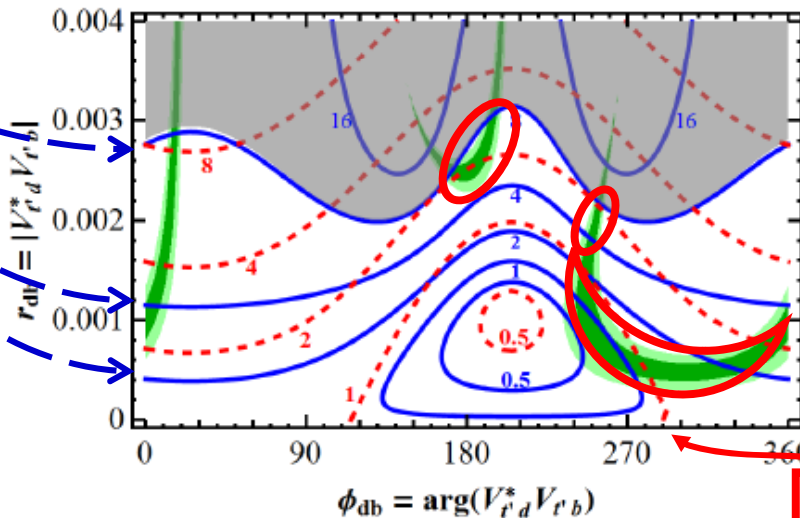
$$|V_{ub}| \sim 3.23 \times 10^{-3}$$

excl.

The 3 Regions survive  $R_{\pi\mu\mu} \lesssim 2 - 3$  Constraint!

$$R_{\pi\mu\mu} \equiv \frac{\mathcal{B}(B^+ \rightarrow \pi^+ \mu^+ \mu^-)|_{4G}}{\mathcal{B}(B^+ \rightarrow \pi^+ \mu^+ \mu^-)|_{SM}}$$

$$10^{10} \mathcal{B}(B_d \rightarrow \mu^+ \mu^-)$$



$$R_{\pi\mu\mu}$$



$\sim$  incl.

$$|V_{ub}| = 4.15 \times 10^{-3}$$

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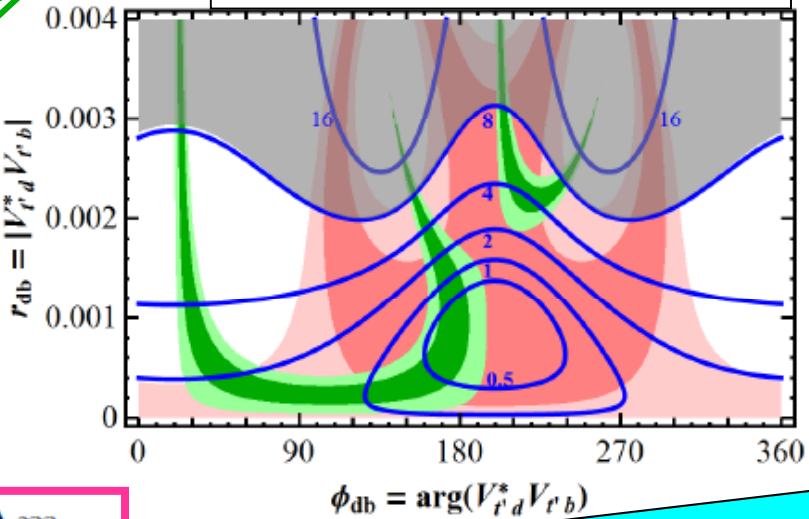
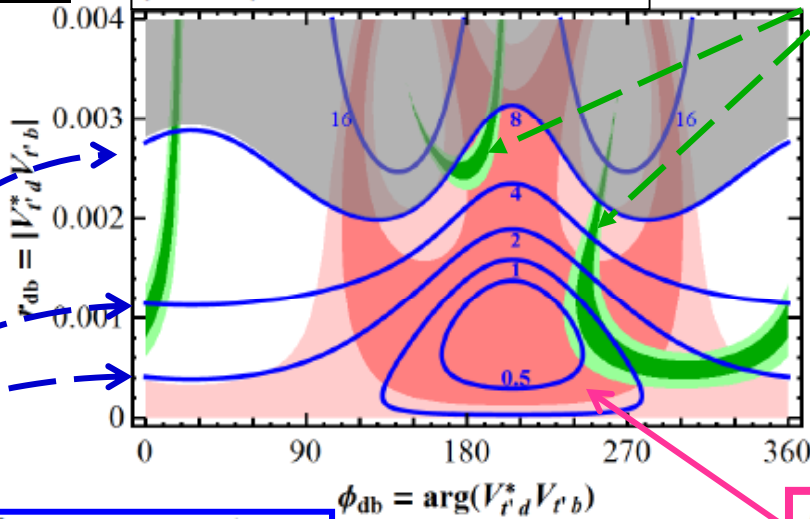
[LHC bound]



excl.

$$\sin 2\Phi_{B_d}$$

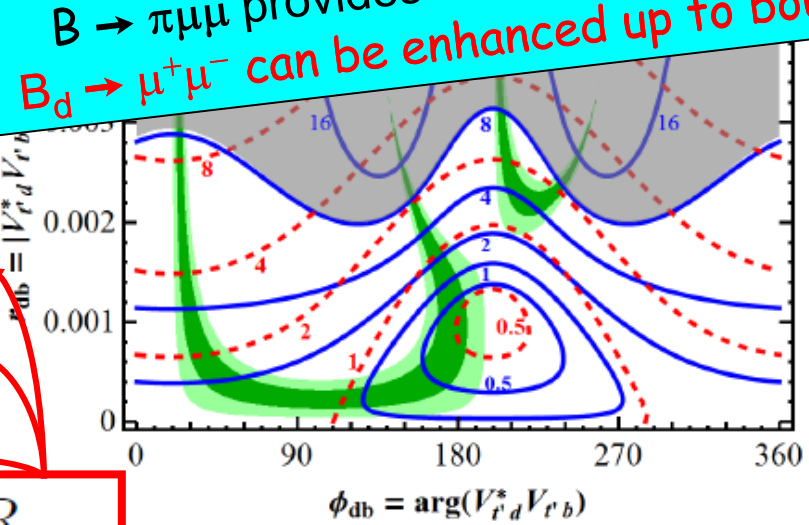
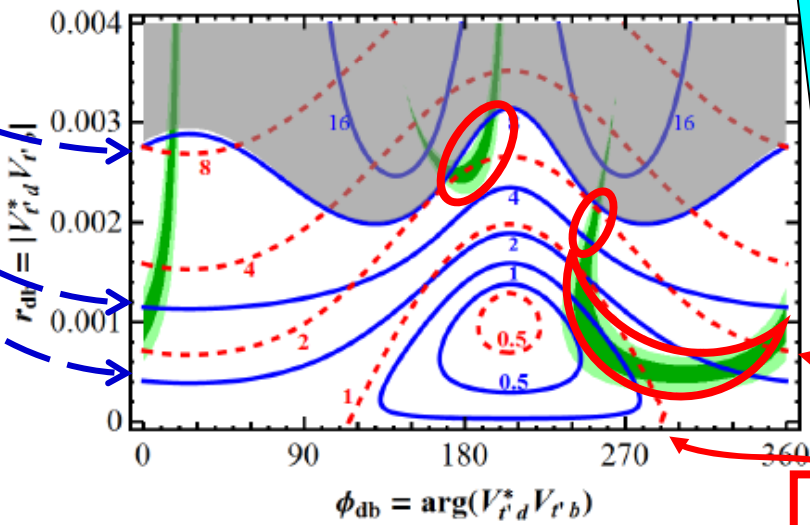
$$|V_{ub}| \sim 3.23 \times 10^{-3}$$



$$10^{10} \mathcal{B}(B_d \rightarrow \mu^+ \mu^-)$$

$$\Delta m_{B_d}$$

$B \rightarrow \pi \mu \mu$  provides useful sanity check;  
 $B_d \rightarrow \mu^+ \mu^-$  can be enhanced up to bound



$$R_{\pi \mu \mu}$$



$m_{t'} = 1000 \text{ GeV}$

[far beyond unitarity bound]

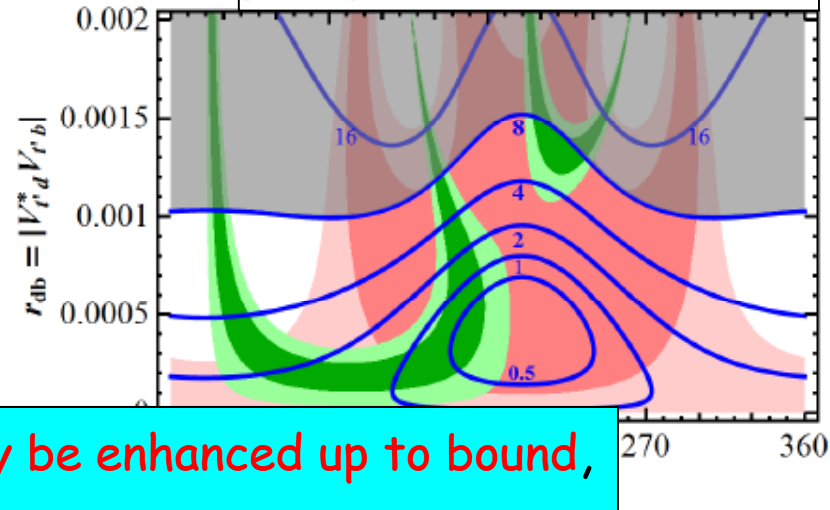
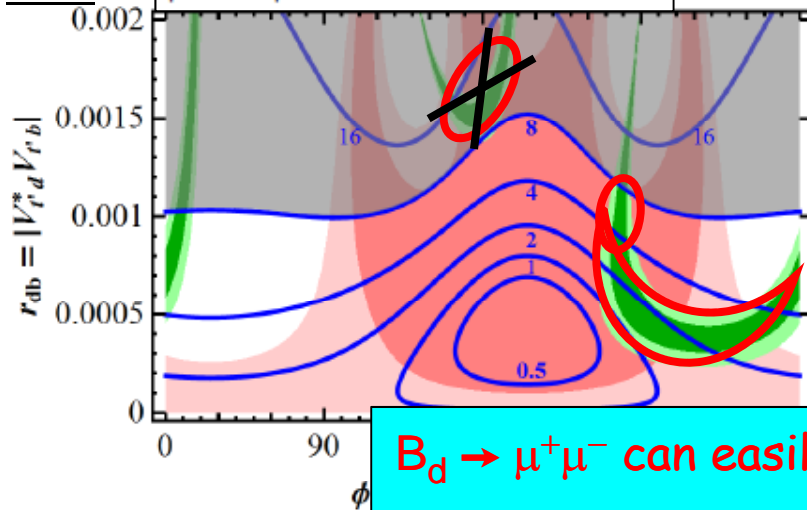


~ incl.

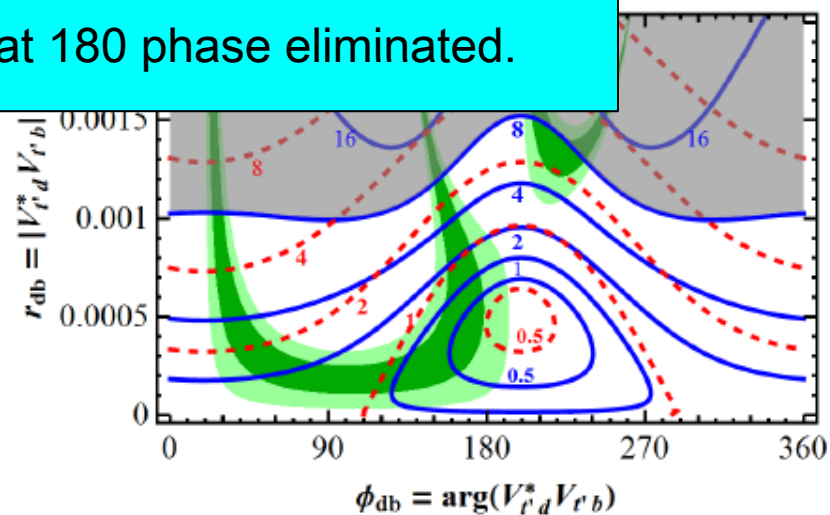
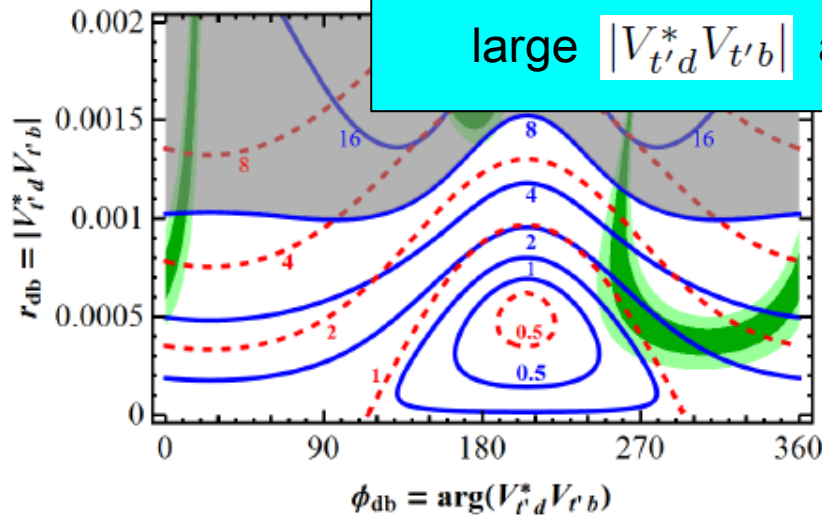
$|V_{ub}| = 4.15 \times 10^{-3}$

$|V_{ub}| \sim 3.23 \times 10^{-3}$

excl.



$B_d \rightarrow \mu^+ \mu^-$  can easily be enhanced up to bound,  
 but  $|V_{t'd}^* V_{t'b}|$  strength drop by more than  $\frac{1}{2}$ ;  
 large  $|V_{t'd}^* V_{t'b}|$  at 180 phase eliminated.







## IV. Discussion

$b \rightarrow d$  quadrangle

CKM hierarchy implication



# Discussion on CKM4

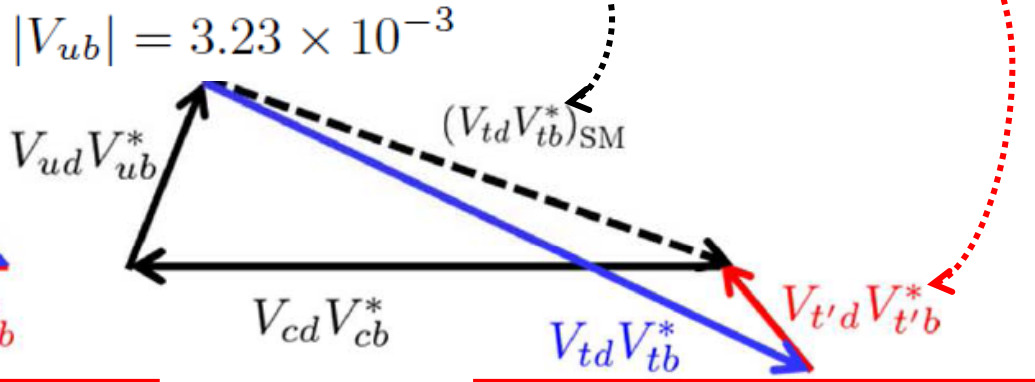
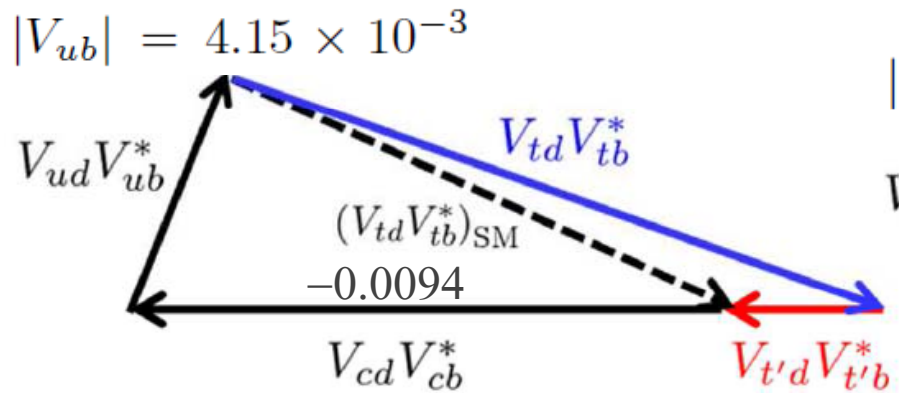


CPV4BAU?

- $b \rightarrow d$  quadrangle in our lap!

$$\lambda_u + \lambda_c + \lambda_t + \lambda_{t'} = 0$$

$-\lambda_t^{\text{SM}}$



from: Region A  $V_{t'd}^* V_{t'b} = 0.0025 e^{i180^\circ}$

A'  $V_{t'd}^* V_{t'b} = 0.0023 e^{i230^\circ}$

- The above CKM4 values are quite large. [ $V_{t'b} < 0.1$  necessary]

If we learn from  $\sin\phi_s$  experience [CKM hierarchy seem upheld], then  $B_d \rightarrow \mu^+ \mu^- > 4x \text{ SM}$  is possible, but not particularly likely.

Heavier  $t'$  could still do it with more “naturally” small CKM4.

WSH & Ma, PRD'11



## V. Conclusion



- 2013 Pivotal: If  $B_d \rightarrow \mu^+\mu^- > 4x SM$ , We Will Discover It! Certainly in expt'l range, and w/ some  $\sin 2\Phi_{B_d}$  motivation. Chance is finite, but not large, because of CKM hierarchy.

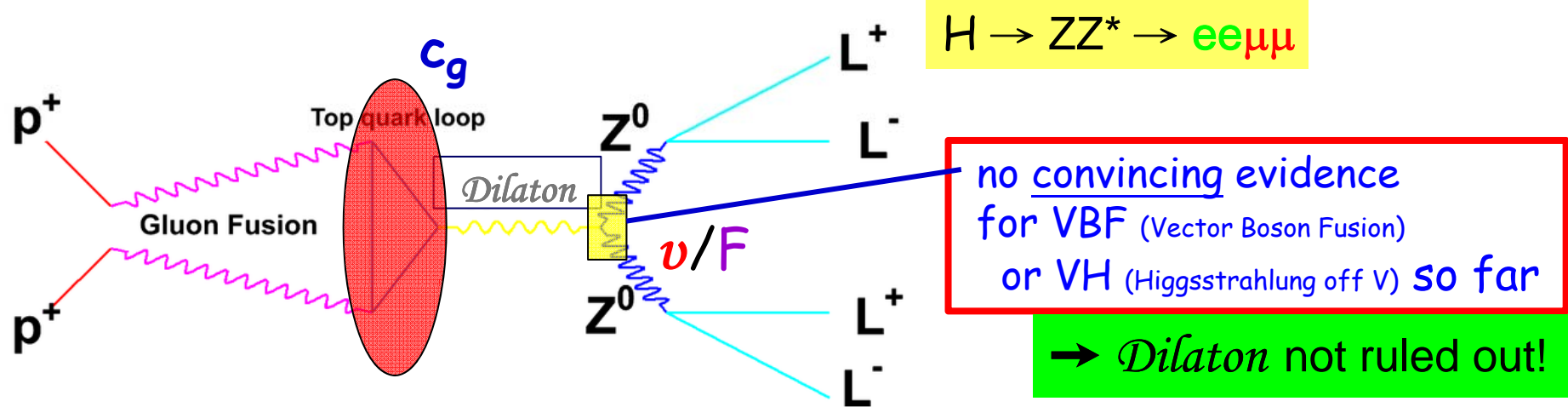
- If discovery with 2011-2012 data, then
  - Uplifting **4G** (hopes again for CPV4BAU), but only in loop ...
  - Cast doubt on “the Higgs” — turning “it” into New Physics?
  - Theorist might scramble, but will need much fine-tuning ...

- If Discovery, Great !!  
More Likely: LHC (CMS+LHCb+...) pushes down towards SM ...  
Still Needs to Be Pursued with 13 TeV.





# How does *Dilaton* rescue the situation ?



## Leading Processes

Elander, Piai, 8/12  
Treat 3 parameters  
 $v/F, C_g, C_\gamma$

