

# From fundamental quantum fields to properties of matter

## Heavy Ions Theory Overview

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CERN PH-TH

*Barcelona, 14 May 2013*

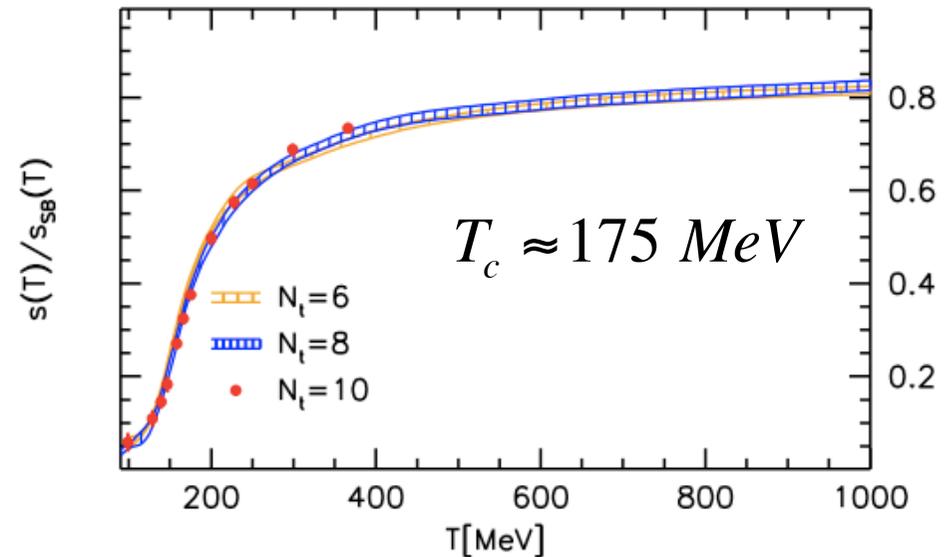
What do we know from 1<sup>st</sup> principles  
about hot and dense QCD?

# Rapid cross-over at $T_c$

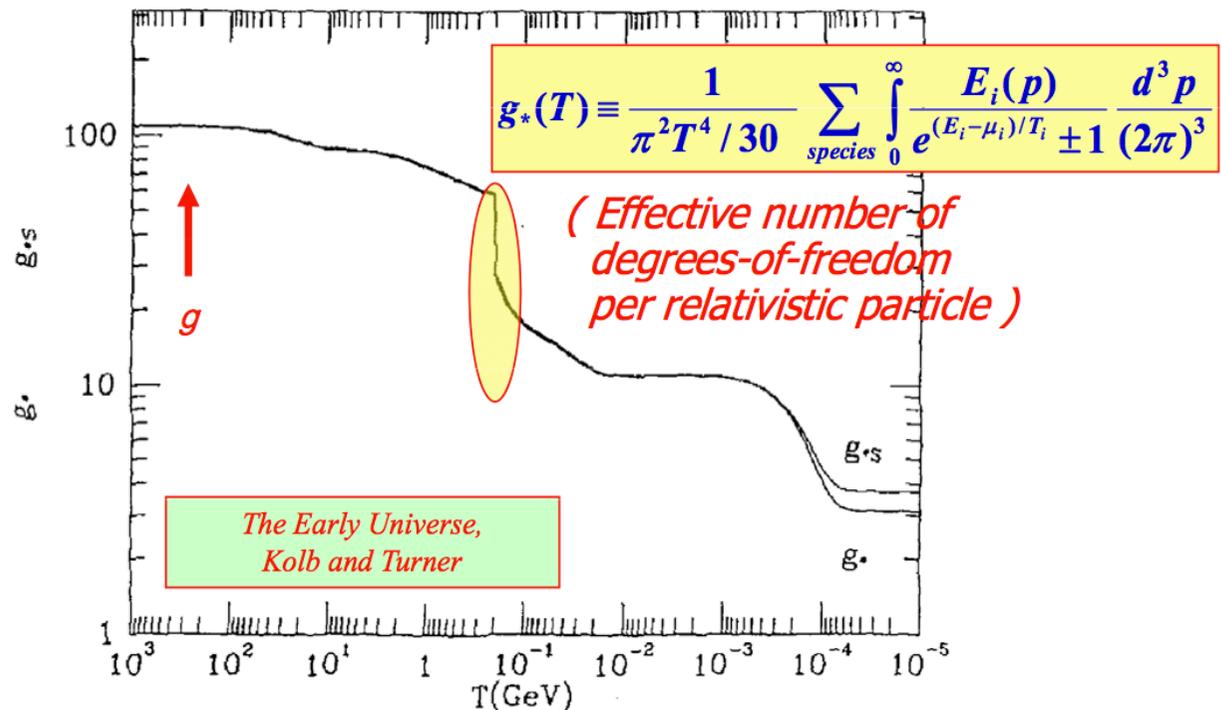
- QCD 'phase transition' at

$$\varepsilon_c \approx (3 - 5) \varepsilon_{nuclear\ matter}^{cold}$$

Wuppertal-Budapest,  
arXiv:1005.3508,  
arXiv:1007.2580



- change of effective number of degrees of freedom

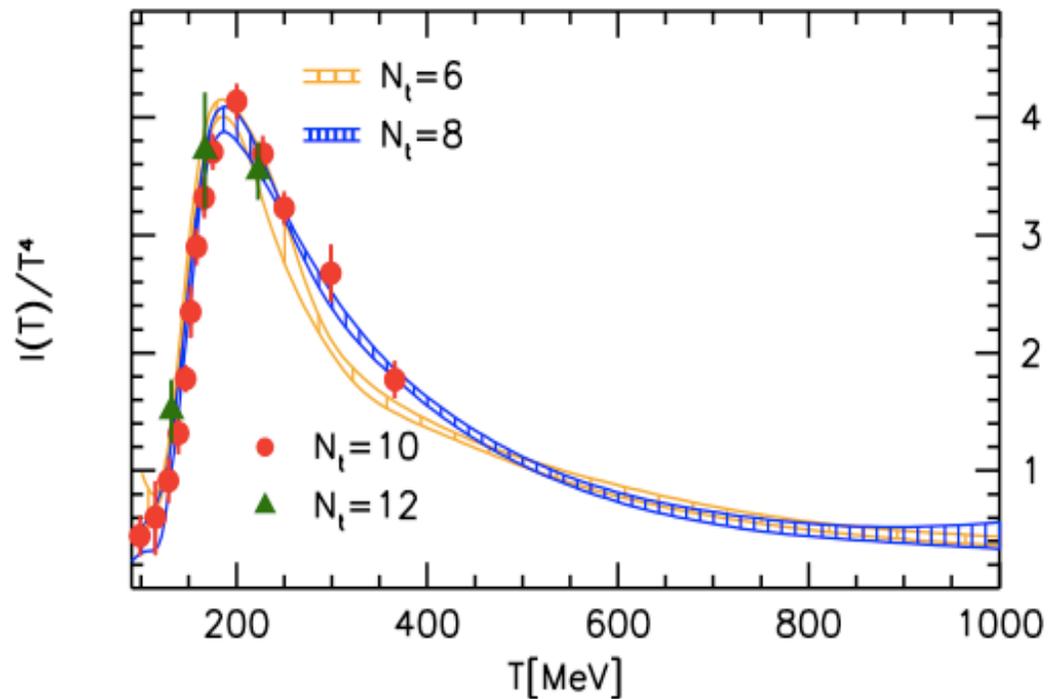


# QCD equation of state (eos)

- EOS is known

Interaction measure  $I = (\varepsilon - 3p)/T^4$

Wuppertal-Budapest,  
arXiv:1005.3508,  
arXiv:1007.2580



- access to sound velocity in QCD plasma

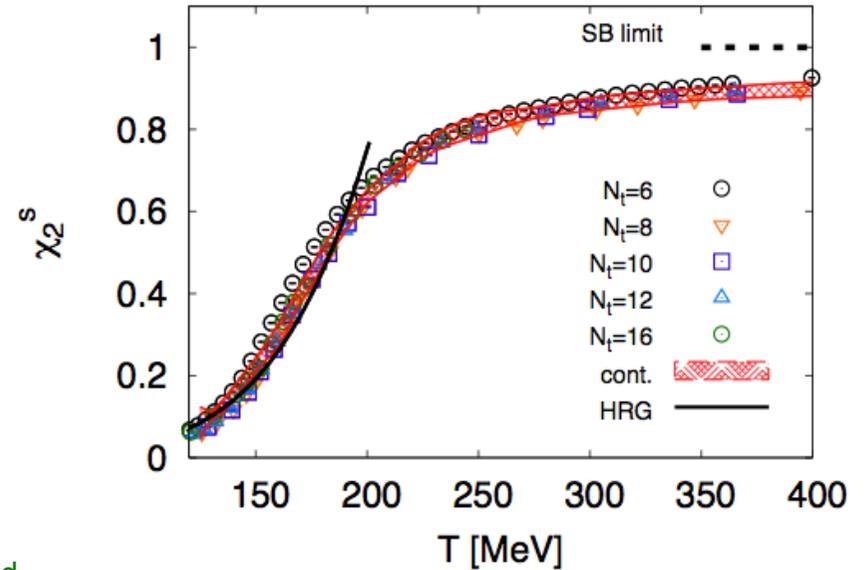
$$c_s = \partial p / \partial \varepsilon$$

- characterizes deviations from conformality

# more from finite temperature lattice QCD...

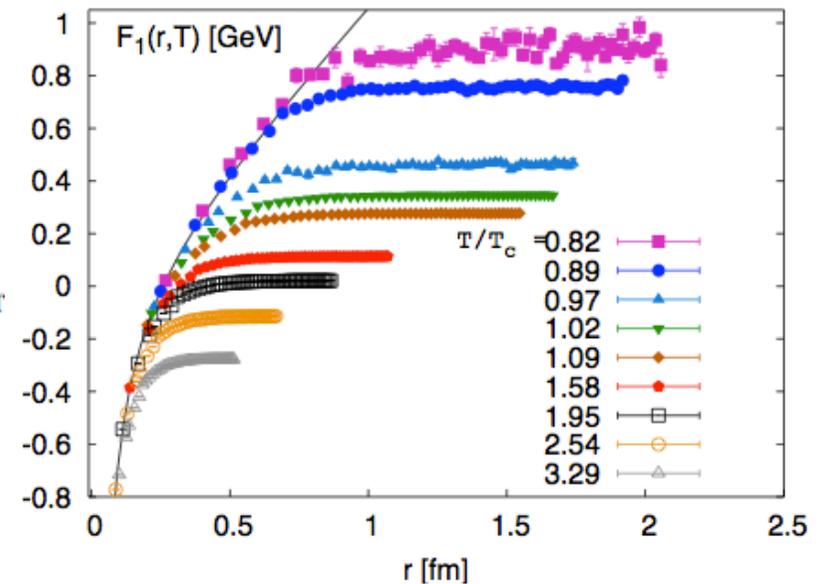
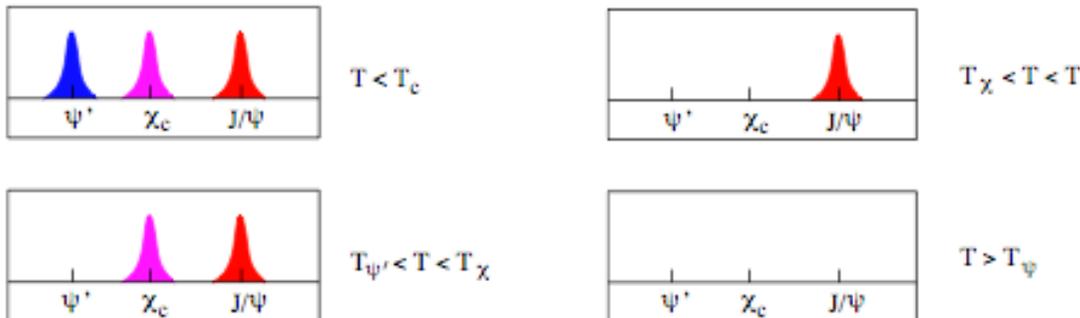
- various fluctuation measures such as quark number susceptibilities

Wuppertal-Budapest,  
arXiv:1112.4416



- Results relevant for sequential (T-dependent) suppression of quarkonia. Here: singlet free energy

Bielefeld,  
arXiv:1001.5284



# AdS/CFT insights into strongly coupled non-abelian plasmas

- equilibration time-scales
- transport properties
- propagating probes in hot QCD

Finite T Lattice QCD difficult to apply to

- Real time dynamics
- Hydrodynamic properties

(  $2\pi T$  is lowest Matsubara frequency, problem for limit  $\omega \rightarrow 0$  )

## Gauge/gravity duality (AdS/CFT correspondence) Maldacena, 1997

Strong coupling problems  
in non-abelian QFT



Classical Problem in a curved  
higher-dimensional space

$$g^2, N_c$$

$$\lambda \equiv g^2 N_c \quad \text{T' Hooft coupling}$$

$$g_s, \alpha' = l_s^2$$

String coupling and  
string tension

applicable to non-abelian plasmas of QFTs with gravity dual

$$T_H = \frac{r_0}{\pi R^2} = T$$

**Black hole  
horizon**  
**Curvature  
radius**

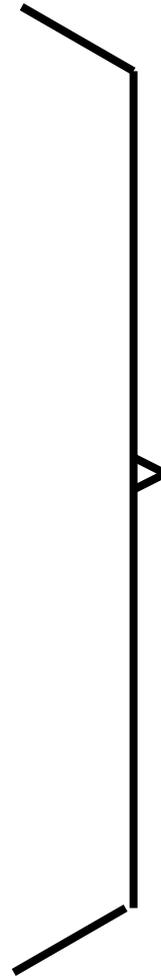
$$\frac{R^2}{\alpha'} = \sqrt{\lambda} = \sqrt{g^2 N_c}$$

But: gravity dual of QCD not known. How can this be relevant? =>

# QFTs with gravity duals vs QCD at T=0

## $N=4$ SYM theory

- conformal
- no asymptotic freedom  
no confinement
- supersymmetric
- no chiral condensate
  
- no dynamical quarks, 6 scalar  
and 4 Weyl fermionic fields in  
adjoint representation



Physics **near vacuum** and at **very high energy** is very different from that of QCD

## ... and at finite temperature ...

### $N=4$ SYM theory at finite $T$

- conformal
- no asymptotic freedom  
no confinement
- supersymmetric (badly broken)
- no chiral condensate
- no dynamical quarks, 6 scalar  
and 4 Weyl fermionic fields in  
adjoint representation

### QCD at $T \sim \text{few} \times T_c$

- near conformal (lattice)
- not intrinsic properties of  
QGP at strong coupling
- not present
- not present
- may be taken care of by  
proper normalization

In solid state physics, materials of different microscopic composition and interaction show similar thermal properties.

Here: non-abelian gauge theories of different particle content and symmetries show similar thermal properties above  $T_c$ .

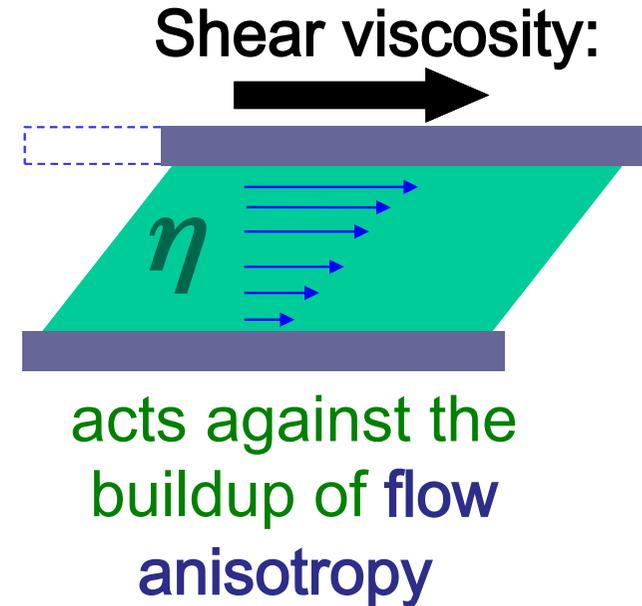
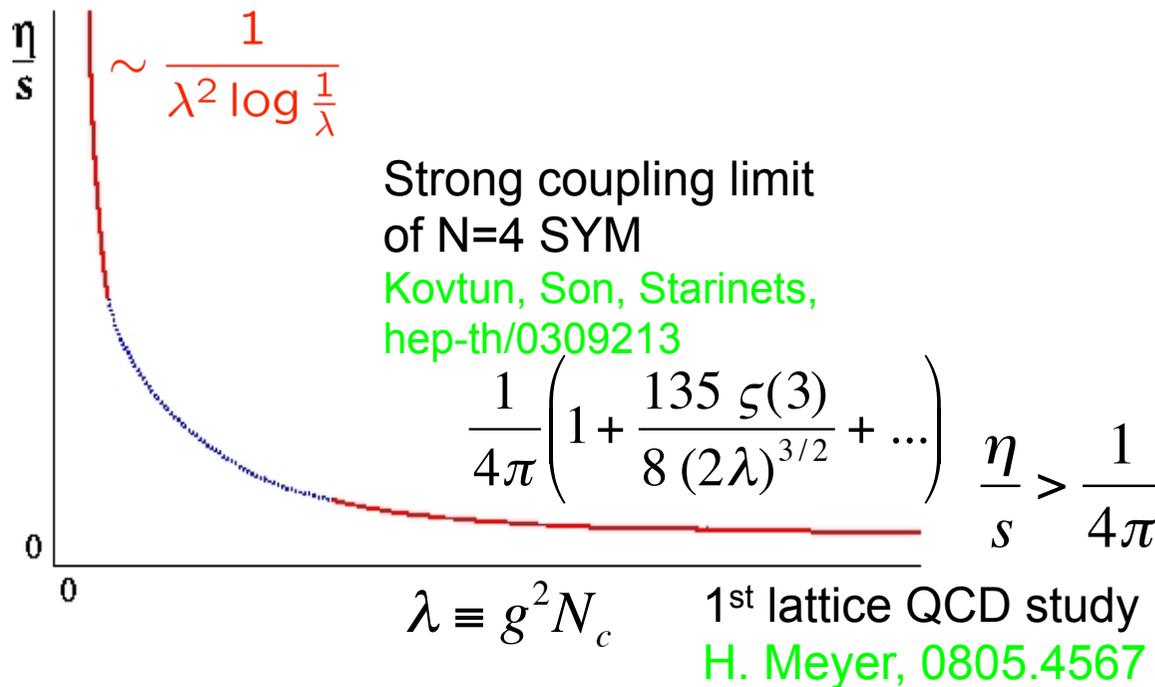
# Dissipative properties: shear viscosity

Calculable from first principles in quantum field theory (QCD)

$$G_{xy,xy}^R(\omega,0) \equiv \int dt dx e^{i\omega t} \Theta(t) \langle [T_{xy}(t,x), T_{xy}(0,0)] \rangle_{eq}$$

Arnold, Moore, Yaffe,  
JHEP 11 (2000) 001

$$\eta \equiv -\lim_{\omega \rightarrow 0} \frac{1}{\omega} \text{Im} G_{xy,xy}^R(\omega,0)$$



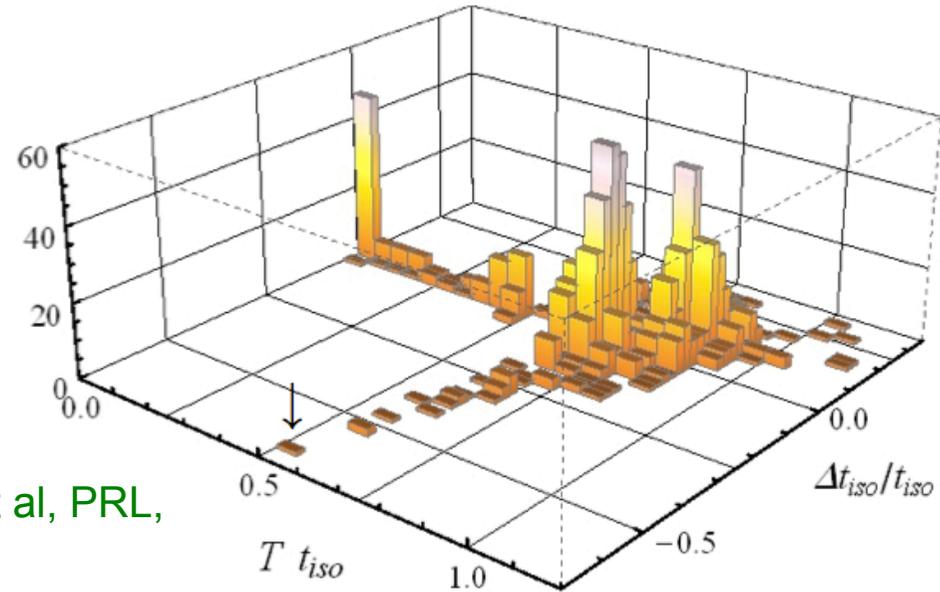
First rigorous example that a finite T QFT can evolve with minimal dissipation.

# Far from equilibrium dynamics at strong coupling

- Model-dependent in QCD but a rigorously calculable problem of numerical gravity in AdS/CFT
- Results show extremely short **non-perturbative isotropization**

$$\tau_{iso} < \frac{1}{T}$$

M. Heller et al, PRL, 1202.0981



- The first rigorous field theoretic set-up in which fluid dynamics applies at very short time scales

$$\alpha_s \gg 1$$

$$\Rightarrow 0.65 \leq \tau_0 T_0$$

Chesler, Yaffe, PRL 102 (2009) 211601

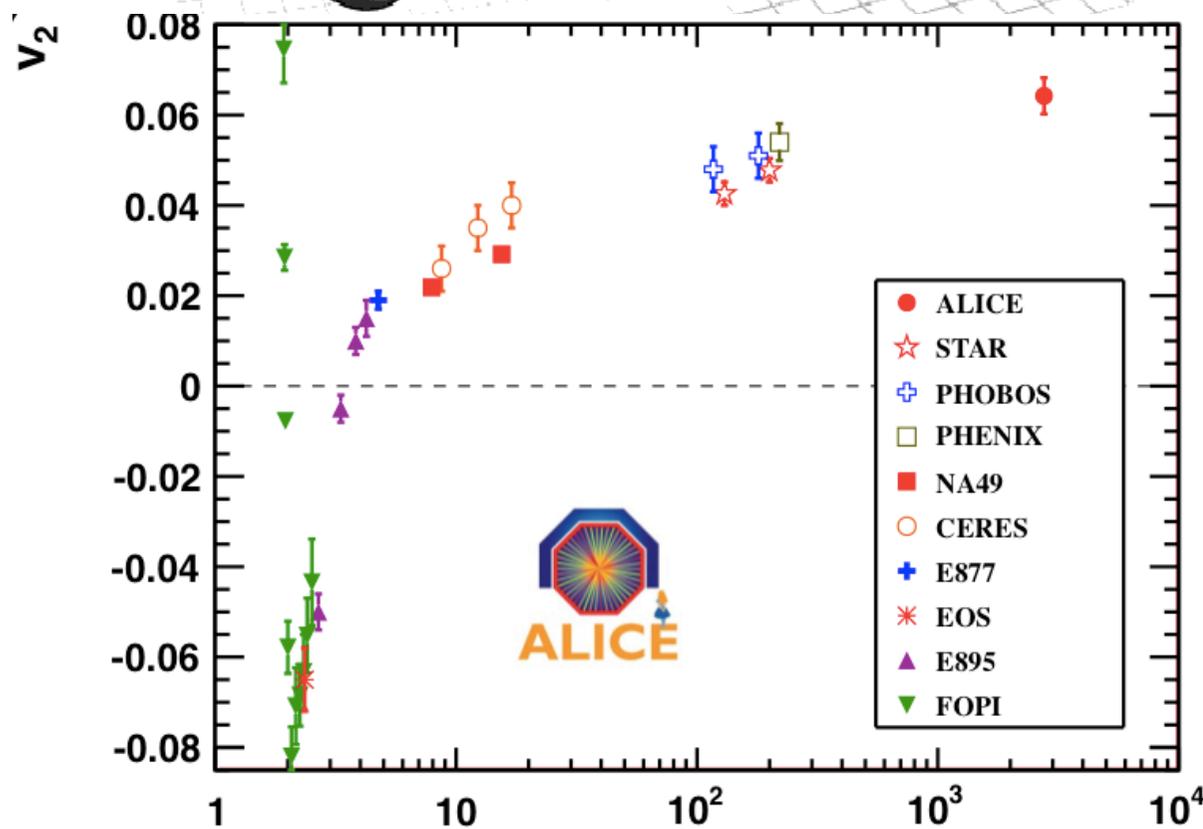
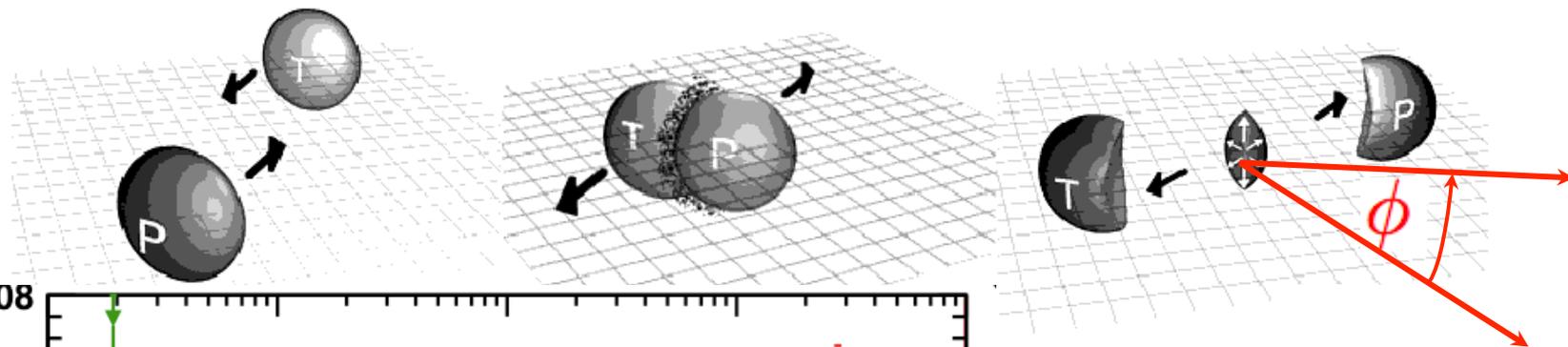
- These non-abelian plasma are unique in that they do not carry quasi-particle excitations:

perturbatively require  $\tau_{quasi} \sim \frac{1}{\alpha_s^2 T} \gg \frac{1}{T}$

but  $\tau_{quasi} \approx \frac{const \eta}{T s}$

Turning now to phenomenology of  
heavy ion collisions

# Elliptic Flow: hallmark of a collective phenomenon



$$\frac{dN}{d\phi} \propto [1 + 2v_2 \cos(2\phi)]$$

Compilation  
ALICE, PRL 105, 252302 (2010)

$\sqrt{s_{NN}}$  (GeV)

# Fluid dynamic simulations of heavy ion collisions

Based on 2nd order [Israel-Stewart](#) relativistic fluid dynamic equations of motion. Under simplifying assumptions, ...

$$(\varepsilon + p)Du^\mu = \nabla^\mu p - \Delta^\mu_\nu \nabla^\sigma \Pi^{\nu\sigma} + \Pi^{\mu\nu} Du_\nu$$

$$D\varepsilon = -(\varepsilon + p)\nabla_\mu u^\mu + \frac{1}{2}\Pi^{\mu\nu} \langle \nabla_\nu u_\mu \rangle$$

$$\tau_\pi \Delta^\mu_\alpha \Delta^\nu_\beta D\Pi^{\alpha\beta} + \Pi^{\mu\nu} = \eta \langle \nabla^\mu u^\nu \rangle - 2\tau_\pi \Pi^{\alpha(\mu} \omega_{\alpha}^{\nu)}$$

In general, dissipative dynamics involves several **relaxation times** and **transport coefficients**.

# Dissipative fluid dynamics relates flow to fundamental properties of matter

- based only on: E-p conservation:  $\partial_\mu T^{\mu\nu} = 0$   
2<sup>nd</sup> law of thermodynamics:  $\partial_\mu S^\mu(x) \geq 0$
- sensitive only to properties of matter that are

calculable from first principles in quantum field theory

**EOS:**  $\varepsilon = \varepsilon(p, n)$  and **sound velocity**  $c_s = \partial p / \partial \varepsilon$

**transport coefficients:** shear  $\eta$ , bulk  $\xi$  viscosity, conductivities ...

$$\eta = \lim_{\omega \rightarrow 0} \frac{1}{2\omega} \int dt dx e^{i\omega t} \left\langle \left[ T^{xy}(x, t), T^{xy}(0, 0) \right] \right\rangle_{eq}$$

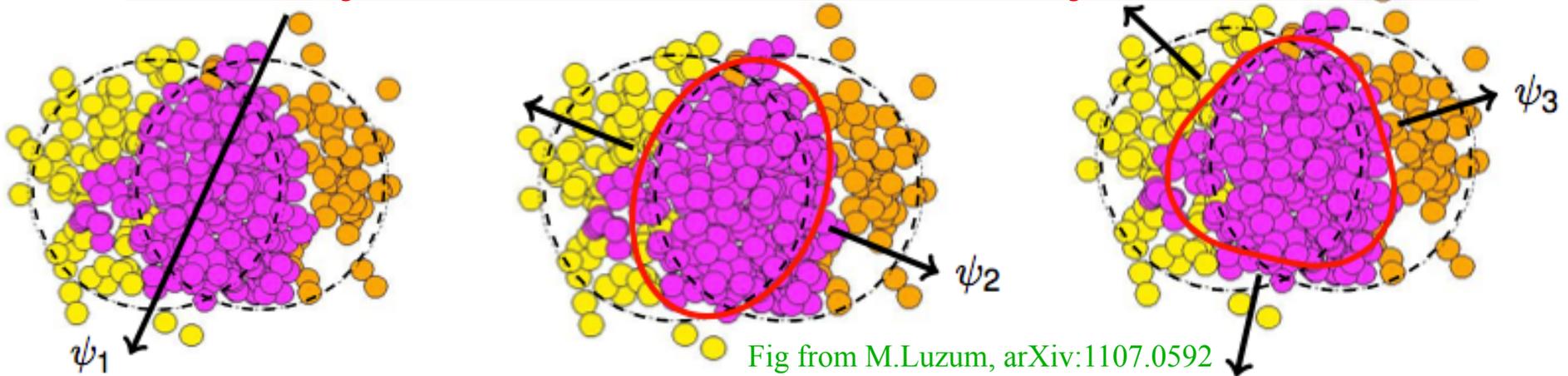
**relaxation times:**  $\tau_\pi, \tau_\Pi, \dots$

Lattice QCD =>

Finite Temp pQCD =>

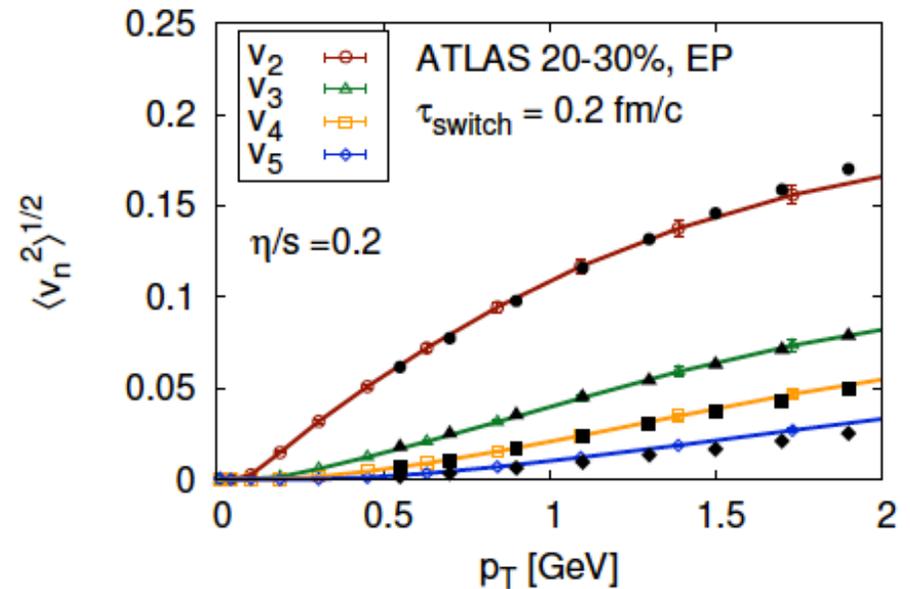
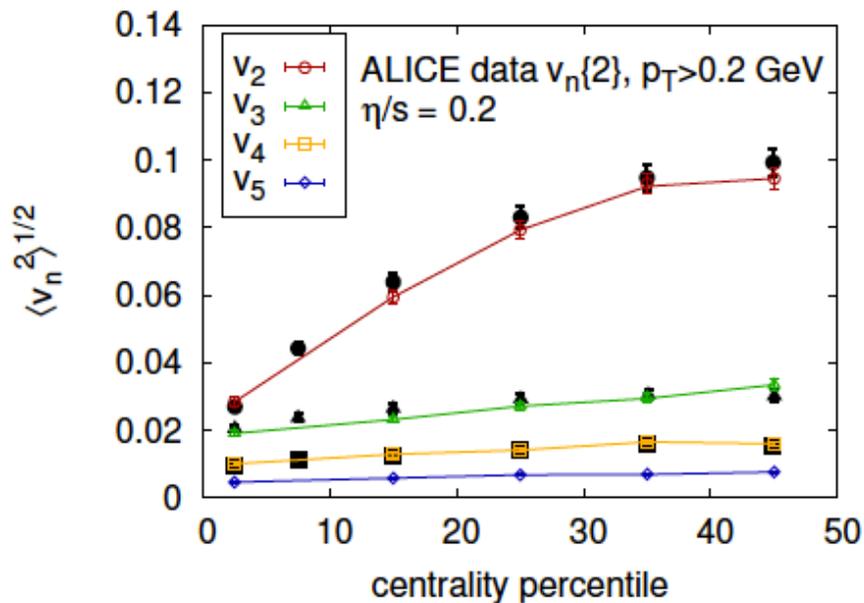
AdS/CFT =>

# Fluid dynamics of initial density fluctuations



- Fluid dynamics maps initial spatial eccentricities onto measured  $v_n$
- 3+1 D viscous hydro reproduces  $v_2, v_3, v_4, v_5$  in  $p_T$  and centrality

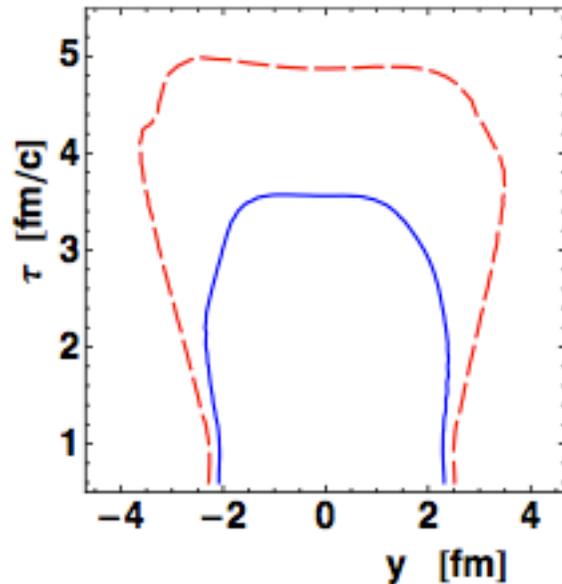
B. Schenke, MUSIC, .QM2012



# Do smaller systems show flow: pPb?

P. Bozek, 1112.0915

And if one treats evolution of pPb@LHC fluid dynamically?

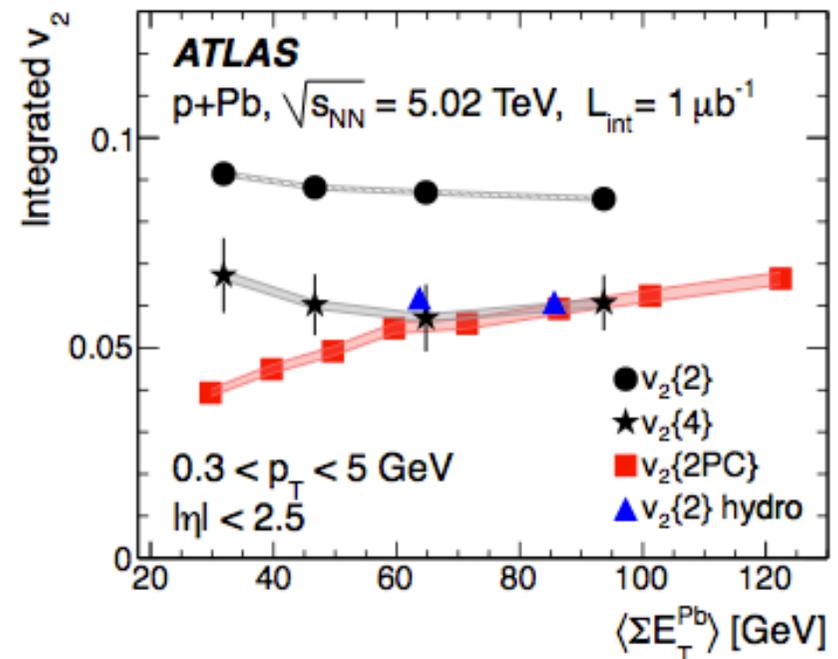
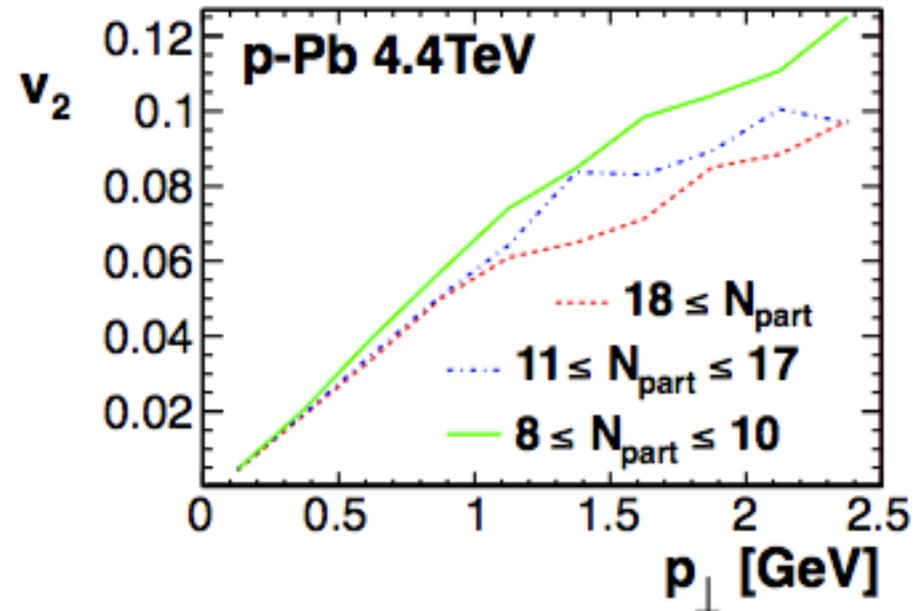


Fluid dynamics compares surprisingly well with

$$v_2 \{2\}, v_2 \{4\}, v_3 \{2\}$$

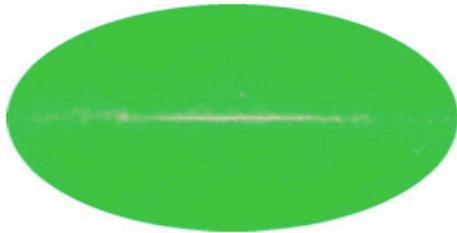
in pPb@LHC.

ATLAS, 1303.2084  
CMS, 1305.0609

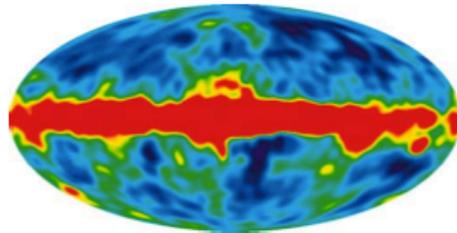


# A (valid) analogy

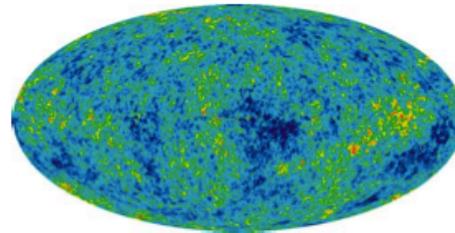
Penzias/Wilson  
1965



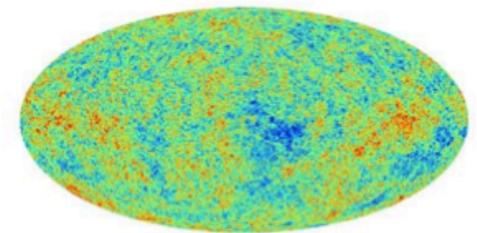
COBE  
2003



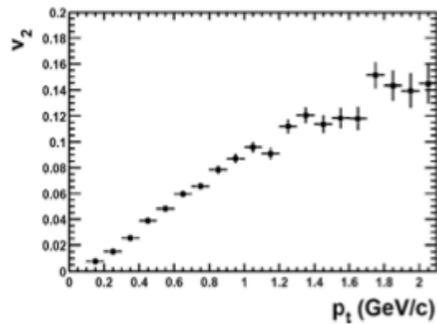
WMAP  
2007



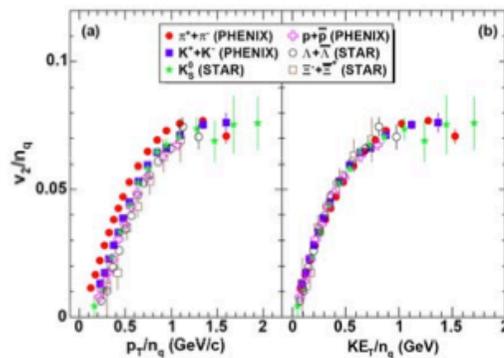
Planck  
2012



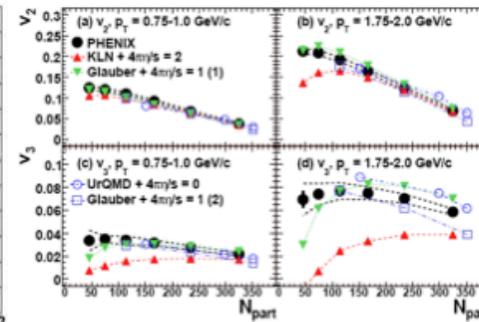
DISCOVERY.....  
.....PRECISION



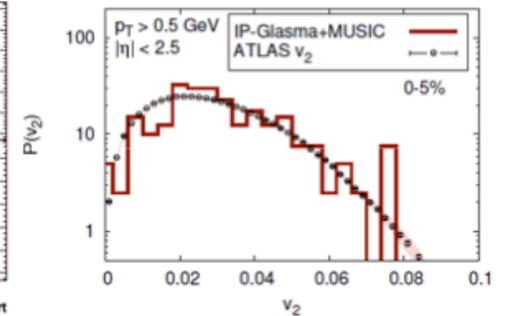
2001



2004



2008



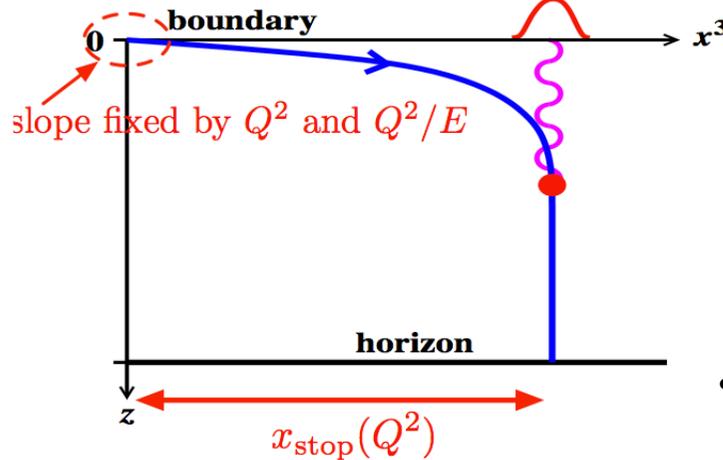
2012

Slide from W. Zajc

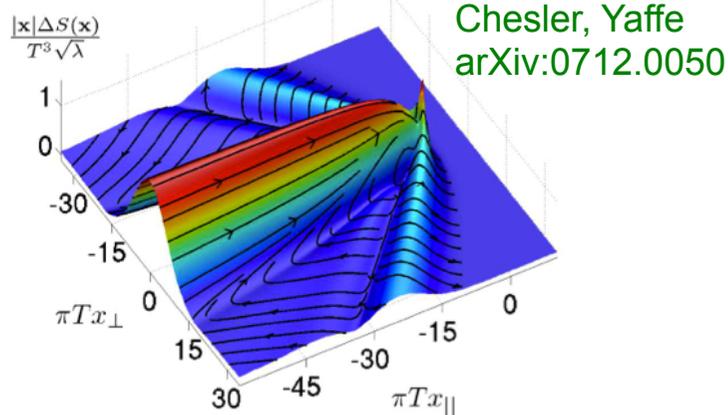
# How do high-momentum partons propagate?- theory

## In a perfect liquid (AdS/CFT view)

- Light partons/jets **thermalize** (no collinear structure remains)

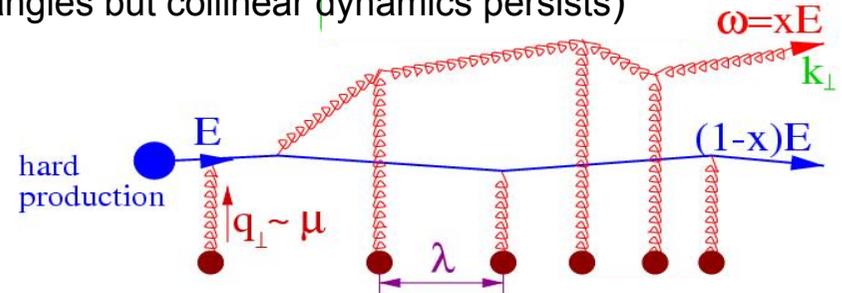


- Heavy quarks lose momentum via sound modes and wake



## In system with finite mean free path

- Light hard partons **fragment** in medium (Energy moved to softer scales/larger angles but collinear dynamics persists)



- Heavy quarks **fragment** with smaller branching probabilities (*dead-cone effect*)

$$\frac{1}{k_T^2} \Rightarrow \frac{k_T^2}{\left(k_T^2 + \frac{M^2}{E^2} \omega^2\right)^2}$$

testable hierarchy in mass and color charge

$$\Delta E_{gluon} > \Delta E_{quark, m=0} > \Delta E_c > \Delta E_b$$

- For  $M \ll E$ , mass unimportant. In high energy limit (eikonal limit)  $\Delta E$  determined by  $\hat{q}$

➔ Motivates experimental study of medium-dependent jet fragmentation

# Open heavy flavor at low pt

- ‘No-quasiparticle conjecture’ implies that light low-momentum dressed quarks do not exist (i.e. do not propagate beyond  $L \approx 1/T$ )

In contrast, charm & bottom propagate (consequence of flavor conservation).  
How?

- At low pt, Langevin dynamics determines how charm & beauty quarks move:  
The perfect liquid is source of **random forces**

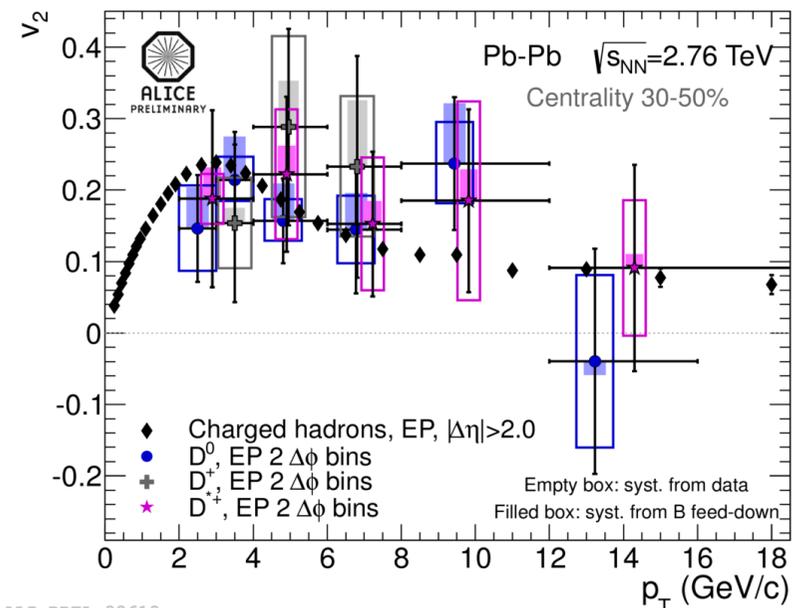
$$\frac{dp_L}{dt} = \xi_L(t) - \mu(p_L)p_L, \quad \langle \xi_L(t) \xi_L(t') \rangle \equiv \kappa_L(p_L) \delta(t - t')$$

$$\frac{dp_T}{dt} = \xi_{Ti}(t) \quad \langle \xi_{Ti}(t) \xi_{Tj}(t') \rangle \equiv \kappa_T(p_L) \delta_{ij} \delta(t - t')$$

calculable from 1<sup>st</sup> principles in quantum field theory, e.g. in strong coupling limit:

$$\kappa_T = \pi \sqrt{\lambda} T^3 \sqrt{\gamma} \quad \kappa_L = \pi \sqrt{\lambda} T^3 \gamma^{5/2}$$

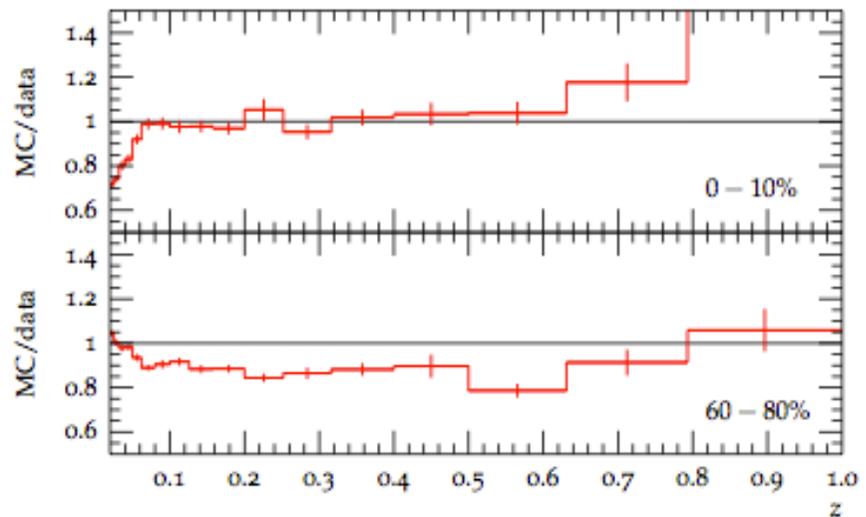
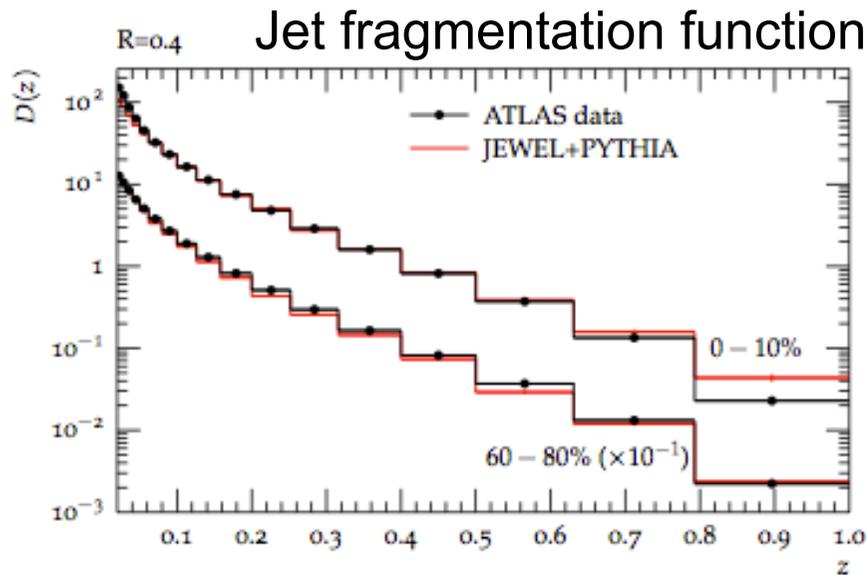
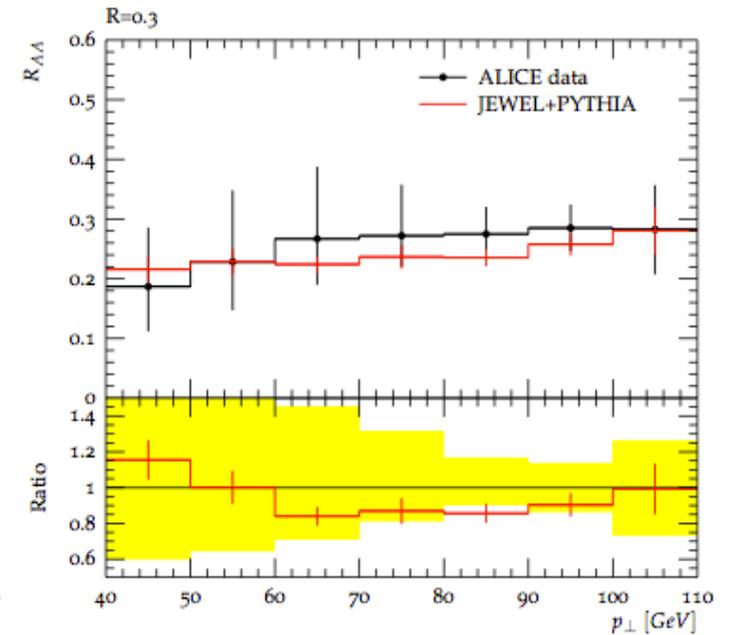
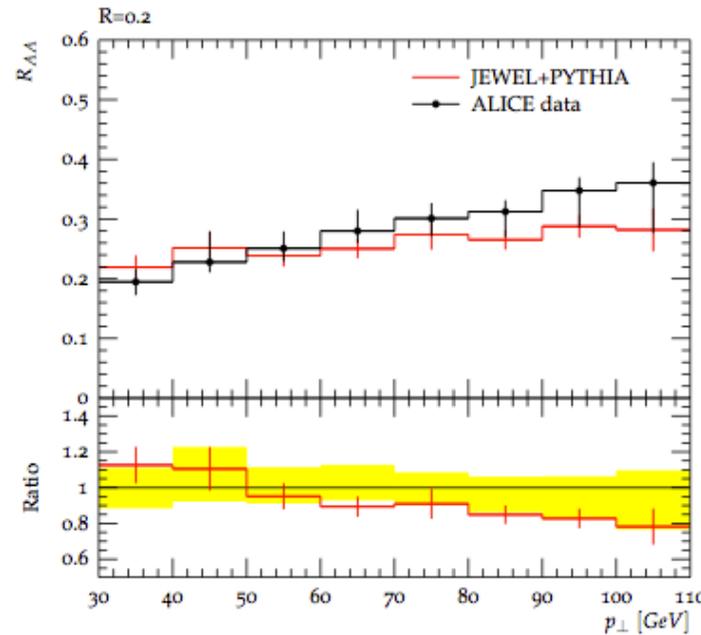
- This hard probe is unique in that we know already that it is moved by the flow.



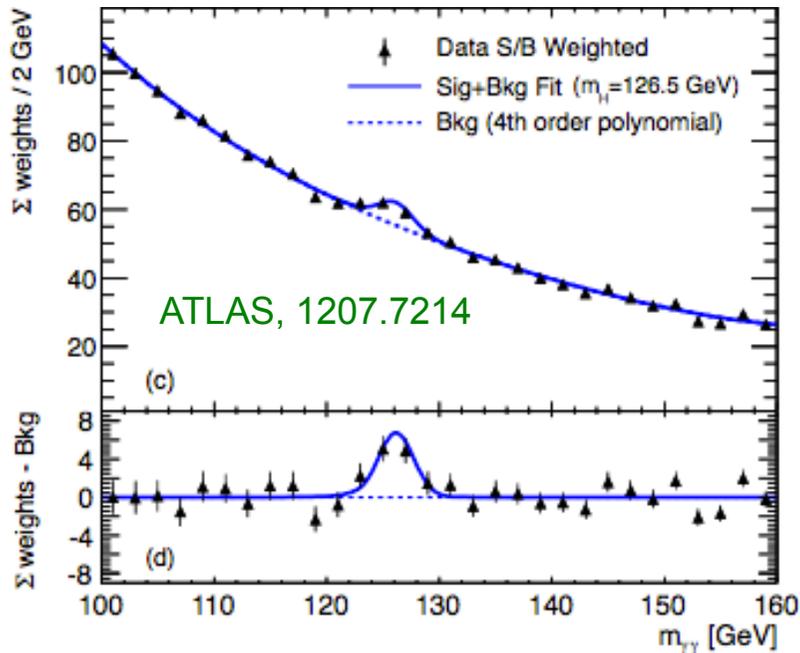
# Perturbative description of 'high-pt' jet quenching fairs well

Nuclear  
Modification  
factor

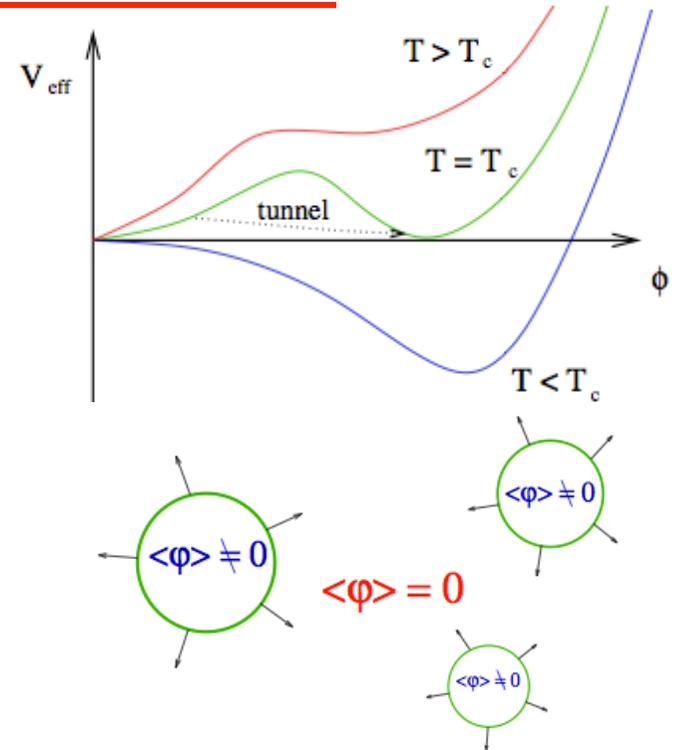
K. Zapp, F. Krauss, UAW,  
JHEP 1303 (2013) 080



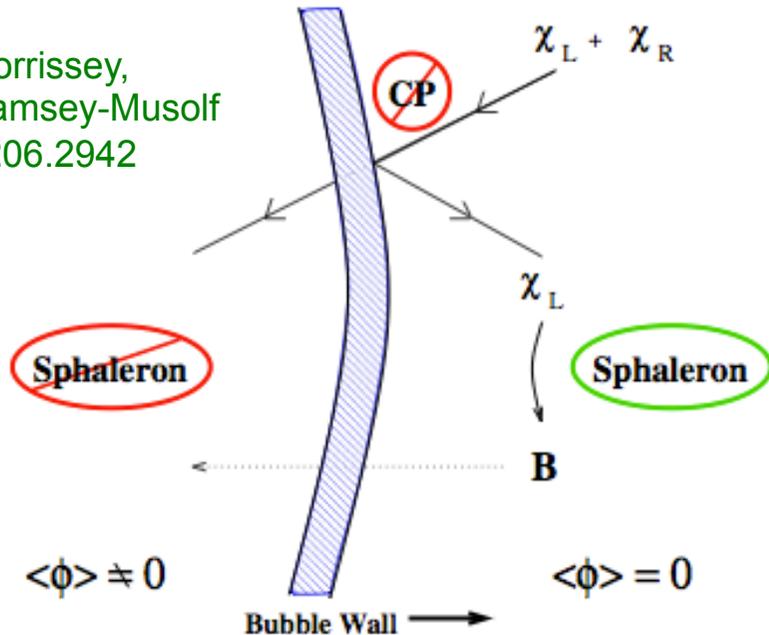
# From quantum fields to properties of matter



Early  
  
 Universe



Morrissey,  
 Ramsey-Musolf  
 1206.2942



If the particle content of the fundamental lagrangian is known,

We ask how collective phenonema and properties of matter arise from it.

The LHC heavy ion programme addresses this question for the theory of strong interactions.

**End**