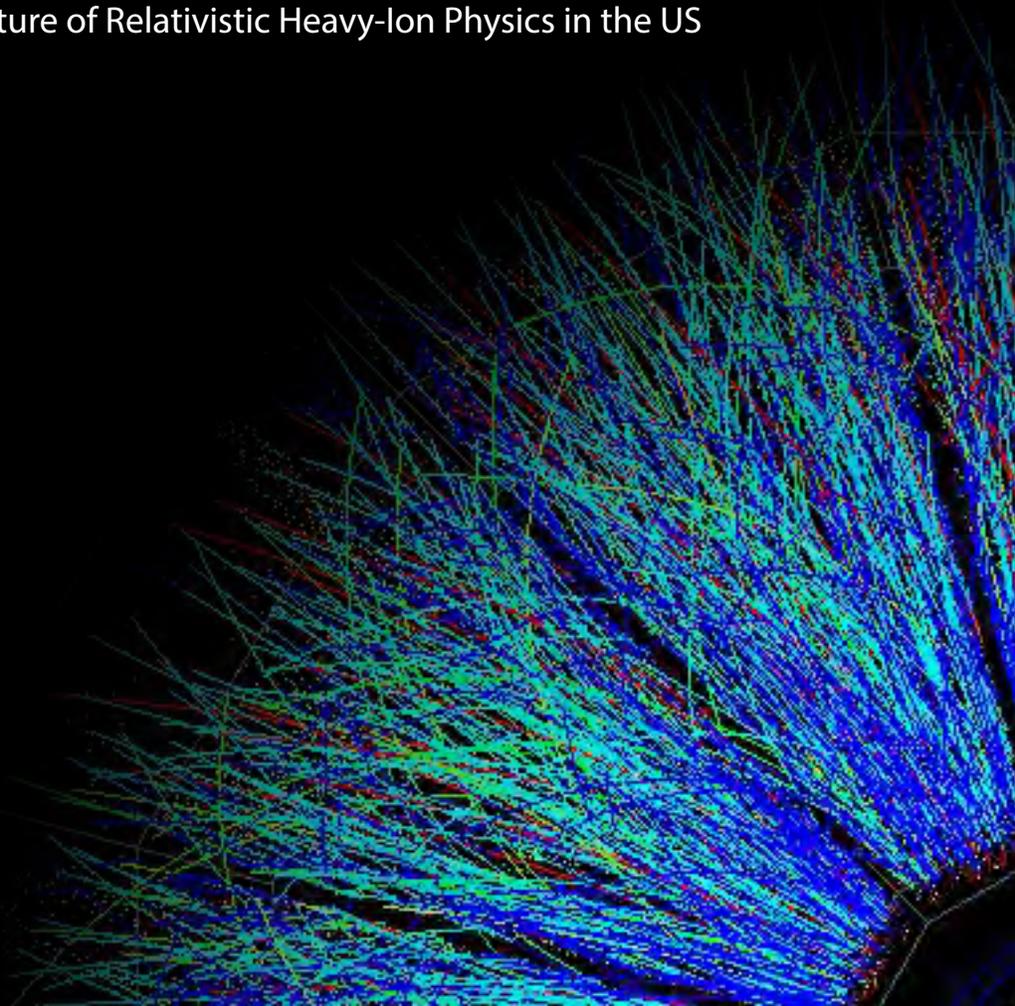


# Hot and Dense QCD Matter

Unraveling the Mysteries of the Strongly Interacting Quark-Gluon-Plasma

A Community White Paper on the Future of Relativistic Heavy-Ion Physics in the US



## 2 Executive Summary

3 This document presents the response of the US relativistic heavy-ion community to the NSAC Sub-  
4 committee, chaired by Robert Tribble, that is tasked to recommend optimizations to the US Nuclear  
5 Science Program over the next five years.

6 The study of the properties of hot and dense QCD matter is one of the four main areas of nuclear  
7 physics research described in the 2007 NSAC Long Range Plan. The US nuclear physics community  
8 plays a leading role in this research area and has been instrumental in its most important discovery made  
9 over the past decade, namely that hot and dense QCD matter acts as a strongly interacting system with  
10 unique and previously unexpected properties. The US relativistic heavy ion program has now entered a  
11 crucial phase, where many of the fundamental properties of the strongly interacting QCD plasma are  
12 approaching precision measurements ( $\sim 10\%$ ), sufficient to determine whether the conjectured lower  
13 bound of viscosity to entropy is achieved and to identify the primary energy loss mechanisms for hard  
14 partons traversing the plasma. And yet there are still important discoveries to be made in the search for  
15 a tri-critical point in the phase diagram and in seeking to understand the mysterious behavior of heavy  
16 quarks in the plasma. This document lays out the quantifiable deliverables and open questions the US  
17 relativistic heavy-ion program is going to address over the next several years, with the goal of gaining a  
18 comprehensive understanding of the dynamics and properties of this strongly interacting QCD matter,  
19 the long sought after Quark Gluon Plasma.

20 The execution of this scientific program will require a number of detector and accelerator upgrades as  
21 well as a significant amount of data taking, that have all been outlined in *The Case for Continued RHIC*  
22 *Operations* by Steve Vigdor. This document should be regarded as complementary to *The Case for*  
23 *Continued RHIC Operations* and focuses on the science goals of the US Heavy-Ion community.

24 The US relativistic heavy-ion program, including the research program outlined in this document, fully  
25 utilizes the complementarity of the Relativistic Heavy-Ion Collider (RHIC) and Large Hadron Collider  
26 (LHC) accelerator facilities: the LHC provides access to high energy probes such as jets and high  
27 momentum leptons in the baryon free regime beyond the reach of RHIC. However, RHIC provides  
28 unique access to high energy probes in kinematic regions at lower energy, given sufficient luminosity, and  
29 with leveraging longer heavy-ion operation times in its favor. Jets of similar energy and characteristics  
30 produced at RHIC and LHC are sensitive to different aspects of the system evolution. Most importantly,  
31 however, RHIC can explore a much wider region of the QCD phase diagram (critical point, phase  
32 structure, baryon density) than is possible at the LHC.

33 The next 5–10 years of the US relativistic heavy-ion program will deliver:

- 34 • a beam-energy scan program to establish the properties and location of the QCD critical point.
- 35 • the quantitative determination of the transport coefficients of the Quark Gluon Plasma, such as  
36 the temperature dependent shear-viscosity to entropy-density ratio  $\eta/s(T)$ , and the energy loss  
37 transport coefficients  $\hat{q}$  and  $\hat{e}$ .
- 38 • a jet physics program to study parton energy loss and the quasi-particle nature of the QGP.
- 39 • a heavy-flavor physics program to probe the nature of the surprisingly strong interactions of heavy  
40 quarks with the surrounding medium
- 41 • a systematic forward physics program to study the nature of gluon saturation and establish the  
42 foundation for the future Electron Ion Collider research program and facility.

43 This research program will ensure the continuing leadership of the US in relativistic heavy-ion physics  
44 and will optimally leverage the significant scientific investment the US government has made over the  
45 past two decades in this field of research.

# 1 Introduction

The study of the properties of hot and dense QCD matter, in particular its deconfined Quark Gluon Plasma (QGP) state, is one of the four main areas of nuclear physics research described in the 2007 NSAC Long Range Plan. The most important discovery made in this area over the past decade is that the QGP acts as a strongly interacting system with unique and previously unexpected properties.

We know of four systems in nature which permit a study of the bulk properties of strongly interacting matter: the interior of the atomic nucleus as well as the nucleon, the interior of a neutron star, and the Quark Gluon Plasma created in heavy-ion collisions. The US nuclear physics community plays a leading role in this research area through experiments at Thomas Jefferson National Laboratory (studying the interior of the nucleus as well as the nucleon) and Brookhaven National Laboratory (discovery and study of the Quark Gluon Plasma as well as the RHIC-Spin program<sup>1</sup> for studying the structure of the nucleon). In recent years, this leading role has extended to the heavy-ion program at the Large Hadron Collider. The study of the strong interaction in bulk is at the cutting edge of human understanding and is also a natural extension of the interests, talents, and traditions of classical nuclear physics and physicists. The US leadership role in this arena serves to advance related fields including particle physics, condensed matter physics, and ultra-cold atomic physics.

This document will describe the quantifiable deliverables and open questions the US relativistic heavy-ion program will address within the next 5-10 years. All of these are geared towards gaining a comprehensive understanding of the dynamics and properties of strongly interacting QCD matter, in particular the long sought after Quark Gluon Plasma, which was created well above the transition temperature for the first time at RHIC in 2000. RHIC is the only machine that can systematically probe the plasma in the vicinity of the transition by varying both temperature and baryon density. Without the continued operation of RHIC, the characterization of the fundamental properties of the Quark Gluon Plasma will be incomplete, and the full promise of the heavy-ion program will remain unfulfilled. The execution of this scientific program will require a number of detector and accelerator upgrades as well as a significant amount of data taking, that have all been outlined in *The Case for Continued RHIC Operations* by Steve Vigdor [1]. The timelines for the scientific program described here have been set up to take the projected detector and accelerator upgrades and data-taking schedules outlined in that document into account. Improvement of the RHIC facilities and detectors are already in full swing, others such as the sPHENIX upgrade proposal, have just undergone a successful internal review at BNL prior to submission to DOE, and the new EBIS source and luminosity upgrade to the accelerator have delivered huge improvements to the quality and versatility of the beam.

The next several years of the US relativistic heavy-ion program will deliver:

- a beam-energy scan program with unparalleled discovery potential to establish the properties and location of the QCD critical point and to chart out the transition region from hadronic to deconfined matter.
- the quantitative determination of the transport coefficients of the Quark Gluon Plasma, such as the temperature dependence of the shear-viscosity to entropy-density ratio  $\eta/s$  (including an assessment of whether the conjectured lower bound has been reached to within a precision of 10%), and that of the energy loss transport coefficients  $\hat{q}$  and  $\hat{e}$ .
- a jet physics program to study the nature of parton energy loss and the quasi-particle nature of the QGP.

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<sup>1</sup>this document does not address the RHIC-Spin program, which is topic of a separate White Paper

- 88 • a heavy-flavor physics program to probe the nature of the surprisingly strong interactions of  
89 heavy quarks with the surrounding medium (i.e. the "heavy-flavor puzzle"), as well as quarkonia  
90 measurements that will provide standard candles for the temperatures obtained in the early stages  
91 of a heavy-ion reaction.
- 92 • a systematic forward physics program to study the nature of gluon saturation. This program will  
93 build the foundation for the future Electron Ion Collider research program and facility.

94 RHIC and LHC facilities are complementary when it comes to successfully executing the outlined research  
95 program: the LHC provides access to high energy probes (quarkonia, high energy jets,  $W/Z/\gamma$ ) beyond  
96 the reach of RHIC and the continuing participation of the US in the LHC heavy-ion program is crucial  
97 for the success of the program outlined here. RHIC has complementary access to high energy probes  
98 in kinematic regions at lower energy, given sufficient luminosity, and can leverage longer heavy-ion  
99 operation time with beams in its favor. Jets of similar energy and characteristics produced at RHIC and  
100 LHC will be sensitive to different aspects of the system evolution. Most importantly, however, RHIC  
101 can explore a much wider region of the QCD phase diagram (critical point, phase structure, baryon  
102 density) than is possible at the LHC. Without the benefit of RHIC, many of the goals of the field, such  
103 as the discovery of the critical point, the temperature dependence and minimum value for  $\eta/s$ , and the  
104 solution to the heavy-flavor puzzle will be difficult, if not impossible to achieve.

105 The document is organized in three main sections, detailing the success of the US relativistic heavy-ion  
106 program, the current Standard Model of relativistic heavy ion collisions that has emerged from these  
107 discoveries, and finally laying out a program for the next several years to quantify the properties of the  
108 Quark Gluon Plasma and gain insight into the physics driving the discoveries made previously. Clearly,  
109 the primary physics goal for the next decade of the US program is to characterize the properties of the  
110 Quark Gluon Plasma via the quantitative extraction of important medium parameters from precision  
111 measurements of sensitive observables. In addition, the discoveries over the past decade have led to  
112 compelling new questions, and without answers to these questions, our understanding of the strongly  
113 coupled QGP will be left incomplete:

- 114 • What is the nature of QCD matter at low temperature but high gluon density, and how does it  
115 affect plasma formation?
- 116 • How does the plasma thermalize so rapidly?
- 117 • The QCD plasma is strongly coupled, but at what scales? Does it contain quasiparticles, or does  
118 the strong coupling completely wipe out long-lived collective excitations?
- 119 • What impact does the coupling have on color screening? Is there a characteristic screening length,  
120 and if so, what is it?
- 121 • What is the mechanism for parton-plasma interactions, and how does the plasma respond to  
122 energy deposited in it?

123 The research program outlined in this document will ensure that the above questions about the nature of  
124 hot and dense QCD will be addressed quantitatively over the next 5–10 years, yielding another important  
125 milestone in the US relativistic heavy-ion program. Due to the abbreviated and general nature of this  
126 document, technical details have been mostly omitted – we refer the reader to the extensive list of  
127 references provided in order to follow-up on the pertinent details of the described measurements and  
128 theoretical calculations.

## 129 2 Major Discoveries and Scientific Advances

130 The physics program at the Relativistic Heavy Ion Collider began in the summer of 2000 and has yielded  
131 a series of fascinating discoveries [2, 3, 4, 5] that have intrigued nuclear physicists and captured the  
132 imagination of the public. Starting in 2010, the range of collision energies has been extended even  
133 higher energies in Pb+Pb collisions at the CERN Large Hadron Collider [6, 7, 8, 9, 9, 10, 11, 12]. The  
134 measurements by the four original experimental collaborations at RHIC have established, and the recent  
135 data from the LHC have confirmed, a novel quantitative framework for the theoretical description of  
136 QCD matter at energy densities in excess of  $1 \text{ GeV}/\text{fm}^3$  (more than six times normal nuclear energy  
137 density) as a strongly coupled plasma of quarks and gluons, which behaves as a nearly inviscid liquid  
138 and is highly opaque to energetic colored probes [13, 14].

139 This research has had broad impact across multiple physics disciplines and can be rightly identified as  
140 the source of several new sub-fields of physics research, such as relativistic viscous fluid dynamics or the  
141 application of gauge-gravity duality to strongly coupled Quantum Field Theories. The RHIC physics  
142 program has successfully measured or bracketed parameters that characterize the initial state of the  
143 reaction (such as the initial energy-density  $\epsilon_{init}$ , its initial temperature  $T_{init}$ , etc.) and also properties of  
144 fundamental physical importance to QCD (specific shear-viscosity  $\eta/s$ , momentum broadening transport  
145 coefficient  $\hat{q}$ , etc.). The measurements of these fundamental properties of the plasma are in various  
146 stages, but as will be described in Sec. 4, all require additional data from RHIC and LHC combined with  
147 advances in theory to achieve significant advances in our understanding of the Quark Gluon Plasma.

148 In this section we review the discoveries made, the theoretical and phenomenological advances motivated  
149 by these discoveries, and the plasma properties quantified during the first 12 years of the RHIC program  
150 and the first few years of the LHC program.

### 151 2.1 Discoveries

#### 152 • High-Momentum Hadron Suppression

153 A long-anticipated signature of a color-opaque medium, suppression by a factor-of-five for high-  
154 momentum hadron production in Au+Au collisions compared to a proton-proton collision base-line  
155 (“jet quenching”) [15, 16], was observed following the first RHIC run [17, 18]. It was later uniquely  
156 identified as a final-state effect via control measurements including prompt photon production  
157 [19] and the absence of suppression in  $d$ +Au collisions [20, 21].

#### 158 • Away-Side Jet Modification (Tomography)

159 The azimuthally back-to-back character of di-jet production allowed experiments to tag the  
160 production of an “away-side-jet” by the coincident observation of the “near-side-jet” [21, 22, 23,  
161 24, 6]. Such studies allowed the jet’s trajectory through the medium to be controlled, thereby  
162 furthering jets as a tomographic probe of the medium [25, 26, 27, 28].

#### 163 • Elliptic Flow at the Hydrodynamic Limit

164 Ideal hydrodynamics had long been proposed as a tentative, but rarely quantitatively accurate  
165 description of nuclear collisions. Measurements of elliptic (second Fourier moment) flow at  
166 RHIC [29, 30, 31, 32, 7], matched the maximally achievable collective flow predicted by ideal  
167 hydrodynamics (i.e. the hydrodynamic limit) [33] and provided the first indication that the medium  
168 (later dubbed the strongly interacting QGP acknowledging its strongly-interacting character)  
169 behaved as a fluid with a shear viscosity to entropy density ratio at or near the quantum lower  
170 bound.

- 171 • **Valence Quark Scaling of Elliptic Flow**  
 172 The varied elliptic flow patterns of identified hadrons were discovered to have a universal underlying  
 173 scaling character driven by the valence quark count of the final state hadron [34, 35, 36]. This  
 174 scaling identified the collective sQGP behavior as being established during the partonic phase of  
 175 the system evolution and serves as a direct signature for deconfinement [37, 38, 39].
- 176 • **Density-Fluctuation-Driven High Order Flow Moments**  
 177 Odd Fourier flow moments must vanish on average for central-rapidity particle production in a  
 178 symmetric colliding system. In contrast, they were discovered to persist to the final state via  
 179 two-particle correlation measurements [40, 7]. Driven by the non-uniformity of the initial-state,  
 180 these unanticipated observations of minute variations imposed onto the final-state momentum  
 181 distribution of produced particles provide not only tight constraints on the transport properties  
 182 of the medium, but also information about the quantum fluctuations of the initial state at the  
 183 nucleon and sub-nucleon scale [41].
- 184 • **Suppression & Flow of Heavy Quarks**  
 185 Kinematic modifications to heavy quark (charm & bottom) projectiles were anticipated to be  
 186 limited both by their mass and the “dead-cone effect” [42]. Startling results demonstrated heavy  
 187 quark spectral modification at a level comparable to light quarks [43, 44, 45, 46], indicating near  
 188 perfect color-opacity of the medium.
- 189 • **Sequential Melting of Heavy Quarkonia**  
 190 Heavy quarkonia ( $c\bar{c}$ ,  $b\bar{b}$ ), exhibiting well understood energy(mass) levels and physical size  
 191 comparable to the sQGP Debye screening length, were observed to sequentially dissociate ordered  
 192 by their physical size [9, 47].
- 193 • **Charge Correlations Suggesting Chiral-Magnetic Effect**  
 194 Instanton (tunneling) and sphaleron (hopping) transitions between QCD vacuum states of differing  
 195 Chern-Simons winding number generate local imbalances of chirality. The “Chiral-Magnetic Effect”  
 196 reveals this underlying topology as a finite electric dipole moment induced in any color-deconfined  
 197 state exposed to a strong external magnetic field. Measurements of charge sign correlations  
 198 [48, 49] are qualitatively consistent with expectations of the Chiral-Magnetic Effect [50, 51],  
 199 disappearing with either the absence of deconfinement (low collision energy) or a magnetic field  
 200 (central U+U collisions).
- 201 • **Suppression of particle production in the low- $x$  coherent regime**  
 202 Contrary to the naive extrapolation of the mid-rapidity Cronin enhancement in  $d$ +Au collisions,  
 203 RHIC experiments conclusively established large suppression of particle production at forward  
 204 rapidities [52, 53, 54]. Measurements of low Bjorken  $x_{Au}$  di-jet production in the  $d$ +Au system  
 205 exhibit both a suppression by a factor of ten and back-to-back decorrelation [55]. Such modifica-  
 206 tions are anticipated in a very high gluon density “saturation regime”, where the low- $x$  nuclear  
 207 structure consists of a Color-Glass Condensate (CGC) [56, 57, 58].
- 208 • **New Anti-Nuclei and Hyper-Nuclei created**  
 209 The detection of the first ever observed anti-hypernucleus, a  $\bar{p}\bar{n}\bar{\Lambda}$  bound state, and eighteen of  
 210 the heaviest anti-particles ever identified, antihelium-4, opened a new direction of exploration in  
 211 the nuclear chart. Confirmation that antimatter is produced at a rate consistent with statistical  
 212 coalescence expectations provides an important benchmark for possible future cosmic radiation  
 213 observations [59].

## 2.2 Theoretical and Phenomenological Advances

Discoveries made at RHIC and more recently at LHC have necessitated broad advances in theory and phenomenology to aid in our understanding and interpretation of the data. In some cases entire new areas of theoretical research have been created to address the RHIC data.

- **Statistical Hadronization**

Yields of all hadronic states created from a decaying quark-gluon-plasma follow a statistical distribution. The Statistical Model of hadro-chemistry describes the hadronic species distribution via thermodynamic variables ( $T$ ,  $\mu_B$ ,  $\mu_{\text{isospin}}$ ) remarkably well over all accessible beam energies [60, 61, 62, 63, 64].

- **Parton Recombination**

Hadronization can be understood as a statistical process of assembling constituent quarks into hadronic bound states of these quarks. The parton recombination model successfully explains the anomalously large baryon/meson ratios at intermediate transverse momentum and the observed quark number scaling law of elliptic flow [37, 38, 65, 39, 66].

- **Relativistic Viscous Hydrodynamics**

RHIC data has driven the development of a mature and reliable theory for Event-by-Event Three Dimensional Viscous Relativistic Hydrodynamics [67, 68, 69, 70, 71, 72].

- **AdS/CFT Modeling of Strongly-Coupled Media**

The duality between  $N=4$  supersymmetric Yang-Mills theory (serving as a model for QCD) and 5D Anti de Sitter space superstring theory, allows for the calculation of various QCD-like transport coefficients and properties (including heavy quark energy loss and shock waves) in the strong-coupling limit that are otherwise computationally not accessible [73, 74, 75, 76, 77, 78]. It has made the study of strongly coupled gauge plasma dynamics increasingly important in the string theory community.

- **Transport of pQCD Probes Through Strongly Interacting Matter**

Propagation of partons and hadrons of various masses and initial energies through the strongly-interacting medium has stimulated the development of innovative many-body perturbative QCD approaches [79, 80, 81, 82, 83, 84, 85, 86, 87]. Theoretical “jet tomography” tools, driven by precise experimental data, have emerged to quantitatively measure the complex sQGP properties [16, 88, 89, 90, 91, 92, 93].

- **Lattice QCD**

Lattice calculations in QCD Thermodynamics are closely coupled to the RHIC experimental program, receiving guidance from and providing theoretical input to the experimental community. Past accomplishments include the determination location and nature of the chiral transition, now well established as a crossover, calculations of the Equation of State with sufficient precision to be used in hydrodynamic calculations, and the determination of melting temperatures for charmonium bound states within the plasma. Future lattice calculations combined with experiment will be used to establish the existence and location of a QCD critical point, and to understand the origin of fluctuations in the final state particle distributions [94, 95, 96, 97, 98, 99].

- **Small-x Physics and the Color Glass Condensate**

Hadron multiplicities and initial attempts at alternative explanations of high momentum hadron suppression include the recognition that nature must exhibit a “Saturation Scale” which can

256 influence RHIC initial state gluon density and must influence parton distribution functions at  
257 sufficiently low Bjorken- $x$  [100, 56, 101, 57, 102, 103, 58, 104],.

### 258 2.3 Quantitative Estimates of QGP Properties:

259 A rigorous phenomenological analysis in conjunction with precision data and theoretical advances has  
260 lead to quantitative estimates for some of the most important quantities characterizing the formation  
261 and transport properties of the QGP:

- 262 • **Initial State Characterization:**

263 The initial energy density  $\epsilon_{\text{init}}$ , initial temperature  $T_{\text{init}}$ , and formation time of the Quark-Gluon-  
264 Plasma  $\tau_{\text{init}}$  have been determined to lie within the following ranges:  $300 \text{ MeV} \lesssim T_{\text{init}} \lesssim 600 \text{ MeV}$ ,  
265  $0.2 \text{ fm}/c \lesssim \tau_{\text{init}} \lesssim 1.2 \text{ fm}/c$  (the ranges are correlated – a higher initial temperature goes hand in  
266 hand with an earlier formation time:  $\epsilon_{\text{init}}^{1/4} \tau_{\text{init}} = \text{const.}$ ).

- 267 • **Shear-Viscosity / Entropy-Density ( $\eta/s$ )**

268 Expressed in dimensionless units, the effective value for the shear viscosity to entropy density  
269 ratio in the QGP phase near  $T_C$  has been found to be  $\eta/s = (1 - 2) \frac{1}{4\pi}$  [70, 105] Figure 1 shows  
270 how the availability of precision data and advances in theory have resulted in increasingly better  
271 constraints on that quantity.

- 272 • **Momentum & Energy Transport coefficients**

273 The medium-induced part of the energy-loss transport coefficient  $\hat{q}$  at the very early stage in  
274 the evolution ( $\tau = 0.6 \text{ fm}$ ) of Au+Au collisions has been determined to  $\hat{q} = 2\text{--}10 \text{ GeV}^2/\text{fm}$   
275 [16, 106]. Figure 2 shows the availability of precision data and advances in theory have resulted  
276 in increasingly better constraints on  $\hat{q}$  and projects the anticipated improvement due to further  
277 measurements by the end of this decade.

## 278 3 A “Standard Model” of Heavy Ion Collisions

279 Prior to the first collisions at RHIC in 2000, expectations for the properties of the system formed in high  
280 energy nuclear collisions were varied. One widely-held view was that the extremely high temperatures  
281 reached in a RHIC collision would lead to a weakly coupled system of partons (due to asymptotic  
282 freedom) that would thermalize and then behave like an ideal gas and expand isotropically. The very first  
283 experimental results from RHIC showed that this view was wrong: the particles emerging from heavy ion  
284 collisions showed an unmistakable azimuthal anisotropy. This first result led to much more extensive and  
285 precise measurements as well as to striking new theoretical developments. Within a handful of years this  
286 process resulted in what could be called a “Standard Model”: a view of the key elements of the physics  
287 of high energy heavy ion collisions that is well supported by experimental evidence and widely accepted.  
288 It provides a foundation for relating the many observables relevant to the physics. The example of the  
289 anisotropy of particle emission provides a case study of the evolution of our understanding, involving  
290 new concepts, quantitative measurement, and theoretical modeling that is underway in many areas of  
291 heavy ion physics.

292 The measurement of “elliptic flow”, an event-by-event azimuthal modulation in the emission of hadrons  
293 from the collision, characterized by the second Fourier coefficient  $v_2$ , was one of the earliest results  
294 from RHIC. It was found to be nearly 50% larger than that measured at the SPS ( $\sqrt{s_{NN}}=17.3 \text{ GeV}$ ),  
295 which provided the highest energy heavy ion collisions before RHIC. More importantly, the elliptic

296 flow, averaged over transverse momentum, was found to agree with ideal hydrodynamic calculations  
297 initialized to account for the measured multiplicity and transverse momentum spectra [33, 107, 108].  
298 Ideal hydrodynamic calculations are only possible in a purely classical continuum limit where no  
299 particle degrees of freedom are evident. Already, this measurement implied a strongly-coupled system  
300 far different than naive expectations before RHIC. Follow-up measurements from the other RHIC  
301 experiments confirmed the STAR results and catalyzed enormous efforts from the theory community  
302 to develop both, more sophisticated hydrodynamic calculations, as well as to explore the microscopic  
303 conditions for hydrodynamics to be valid.

304 One area of particular interest at RHIC was the measurement of  $v_2$  for identified hadrons, over a wide  
305 range of masses. Ideal hydrodynamics predicted a characteristic dependence of  $v_2$  on the transverse  
306 momentum of the emitted particles, since the presence of the different particles sharing a velocity  
307 field would lead to a clear mass splitting. The observation of this “fine structure” in the flow data,  
308 which was straightforwardly incorporated into theoretical calculations, provided further evidence that  
309 the hydrodynamic paradigm was the most efficient way to understand the wide range of soft hadron  
310 measurements emerging from RHIC.

311 Despite these successes, early on it was noticed that at higher transverse momenta  $p_T$ , above 2 GeV,  
312 the different hadrons failed to show as much  $v_2$  as predicted from the calculations. Moreover, it was  
313 observed that the heavier baryons (protons, lambdas) had a much larger  $v_2$  at the same  $p_T$  than was  
314 seen for mesons like pions and kaons. A striking scaling was discovered in 2002 when it was proposed  
315 by several groups to consider the possibility that the hot, dense medium did not form hadrons directly  
316 but rather via a gas of dressed “constituent quarks” which carry their parent quark’s quantum numbers  
317 [37, 65, 39]. Constituent quark scaling provided a simple way to unify an even larger range of data,  
318 from low  $p_T$  to high  $p_T$ , although alternate descriptions have been proposed, and early data from the  
319 LHC suggest that some scaling violations occur at higher energies.

320 The importance of incorporating viscosity into the theoretical description of heavy ion collisions was  
321 never completely ignored but had been neglected in the early years of RHIC both by the apparent  
322 successes of ideal hydrodynamics in a large phase space regime, and by the lack of a straightforward  
323 formalism to incorporate it into practical relativistic hydrodynamic calculations. However, it was the  
324 realization in late 2003 that AdS/CFT calculations could be used to calculate the ratio of viscosity over  
325 entropy density in strongly-coupled systems, in a regime where standard kinetic theory was known to  
326 break down, that brought a real sense of urgency to the community. These calculations predicted that  
327 the viscosity of a strongly-coupled quantum system could never be zero, but were bounded below by  
328  $\eta/s = 1/4\pi$ , a value that can be rationalized by the argument that excitations can’t be localized with a  
329 precision smaller than their thermal wavelength, but which had not been reliably calculated previously.

330 While the theoretical community wrestled with how to systematically incorporate viscous corrections  
331 into hydrodynamics, experiments discovered the importance of fluctuations in the initial geometric  
332 configuration of nucleons in the colliding nuclei. The motivation for colliding copper ions at RHIC  
333 in 2005 was to provide a small system even in central events, one in which many of the interesting  
334 physics effects at RHIC might be found to turn off. Instead it was found that the  $v_2$  measured in  
335 central events was quite large, a surprising finding if the initial eccentricity of the overlap region was  
336 assumed to arise from the convolution of two smooth average densities. The puzzle was resolved by the  
337 invention of “participant eccentricity” where the shape of the overlap region was not calculated relative  
338 to the classical impact parameter, but relative to an axis determined by the participants themselves.  
339 This was the first indication that the fluctuations in the initial state survived the dynamical evolution  
340 before freeze-out, itself suggestive of a small viscosity. Subsequent measurements of flow fluctuations  
341 reinforced this viewpoint, that the initial state of a nuclear collision was not a smooth density, but

342 varied event to event. RHIC's capability of colliding different nuclear systems was instrumental to the  
343 discovery of the role of these fluctuations.

344 Before 2010, it had been assumed that odd harmonics of the Fourier expansion should not be present  
345 in the collision of symmetric nuclei, from the two-fold x-y reflection symmetry of the overlap of two  
346 spherically symmetric densities. However, these symmetries are not present event-by-event, as was  
347 realized in the work of Alver and Roland in 2010 [109]. Those authors proposed the existence of triangular  
348 flow based on the presence of a finite  $\cos(3\phi)$  modulation observed in the two-particle correlation  
349 functions measured by the RHIC experiments. This term provided a succinct, elegant explanation  
350 for two phenomena previously thought to be unrelated, a long range rapidity correlation leading to an  
351 enhanced distribution in the near-side azimuthal distribution of particles relative to a trigger, referred to  
352 as "the ridge", and opposite-side enhancement in the azimuth referred to as "the cone" First results  
353 on higher-order harmonic flow, beyond elliptic flow, by the RHIC and LHC experiments appeared just  
354 before and at the Quark Matter 2011 conference, where significant contributions from  $\cos(\phi)$  to  $\cos(6\phi)$ ,  
355 each with their own amplitudes and reaction plane angles, were found to exist. Most importantly, the  
356 higher order harmonics were shown to have a weak centrality dependence, characteristic of initial state  
357 geometric fluctuations. However they have a very strong dependence on the order  $n$ , as expected from  
358 the presence of viscosity during the system evolution, which more efficiently damps out higher order  
359 (smaller wavelength) fluctuations.

360 The contribution of initial state fluctuations to the average values of the various Fourier coefficients  
361 naturally suggests that the coefficients should vary strongly event to event. The fluctuations of  
362 elliptic flow had been inferred by the measurements of flow cumulants, which combined the event-wise  
363 measurement of multiple particles (2,4 and 6) into estimates of  $v_2$  which also contained contributions  
364 from flow fluctuations. It had also been directly measured by the PHOBOS experiment using its  
365 large charged particle acceptance. Subsequently, the LHC provided the large acceptance spectrometers  
366 missing at RHIC to provide the first direct measurements of  $v_2 - v_4$  with large acceptance in both  
367 pseudorapidity and transverse momentum, which could be compared to theoretical predictions tuned  
368 on the previous-available event-averaged data. At Quark Matter 2012 these predictions, from the  
369 BNL/McGill group incorporating subhadronic quantum fluctuations, were compared to new data from  
370 ATLAS with remarkable success.

371 After twelve years of steady progress, a "Standard Model" for heavy ion collisions has emerged, which  
372 provides a generally adopted framework, in which detailed dynamical questions can be phrased and  
373 addressed.

- 374 • The initial state is understood to fluctuate event by event, with contributions from the nucleons  
375 themselves, as well as the energy deposit per nucleon-nucleon collisions, which fluctuates according  
376 to classical color dynamics relevant at subhadronic size scales (resulting from gluon saturation).  
377 These are usually of negative binomial form.
- 378 • There is a rapid changeover from the glue-field dominated initial off-equilibrium stage of the  
379 reaction to its hydrodynamic evolution at a "thermalization" time, estimated between 0.15 fm/c  
380 and 1fm/c after the nuclei cross. There is debate whether transverse velocity fields can develop  
381 before this time and whether the system fully thermalizes or merely becomes isotropic in the  
382 transverse direction. The shorter the thermalization time, the higher the initial temperature at  
383 thermalization time. The actual mechanism of thermalization is still unknown and represents one  
384 of the open questions to be addressed in the coming years.
- 385 • The dynamical evolution of the liquid proceeds using second order viscous hydrodynamic equations.  
386 Currently, 2+1 boost-invariant hydrodynamics codes are common but the state-of-the-art is rapidly

387 progressing towards a consistent use of 3+1 dimensional codes.

- 388 • The equation of state is taken from lattice QCD calculations. At temperatures below the  
389 deconfinement transition temperature, the lattice QCD equation of state resembles that of a  
390 hadron gas. Partial chemical equilibrium needs to be implemented in the equation of state for  
391 the hadronic phase to account for the cessation of inelastic flavor-changing reactions prior to the  
392 kinetic break-up of the system.
- 393 • The kinetic break-up of the system (freeze-out) occurs at temperatures well below the deconfine-  
394 ment transition temperature. From the transition temperature to freeze-out the system evolves as  
395 an expanding hadron gas that is optimally and reliably described with a microscopic transport  
396 calculation based on the Boltzmann equation.

## 397 4 Discovery Potential, Quantifiable Deliverables and Open Questions

398 After little more than a decade of operation, many of the initial discoveries at RHIC have lead to  
399 precision measurements of Quark Gluon Plasma properties. Yet, due to advances spurred by these  
400 initial discoveries and new measurements at higher  $\sqrt{s_{NN}}$  provided by the LHC, there are aspects of the  
401 RHIC program that are still in a discovery phase. The RHIC beam energy scan serves as prime example  
402 that RHIC, even with the LHC operational, remains the only facility in the world capable of providing  
403 the necessary collision energies in order to execute a program with unparalleled discovery potential to  
404 establish the properties and location of the QCD critical point and to chart out the transition region  
405 from hadronic to deconfined matter.

406 The significant progress towards precision physics of strongly interacting QCD matter under extreme  
407 conditions (QGP), as outlined for the case of  $\eta/s$  in the previous chapter, is a success in its own  
408 right of the experimental and theoretical community, but it is only a stepping stone in the overall  
409 goal of characterizing the QGP via its transport properties ( $\eta/s$ ,  $\hat{q}$ ,  $\hat{e}$ , ...), including their temperature  
410 dependence. These transport coefficients  $\eta/s$  and  $\hat{q}$  and their temperature dependence serve as examples  
411 of precision measurements of the RHIC program for the next 5-10 years. To facilitate such a program,  
412 the unique collision energy and system size coverage of RHIC is essential and will be discussed in more  
413 detail in the following sections.

414 Another important aspect of the outlined programs is that it is not only confined to increase the precision  
415 to which we determine certain QGP properties, but that it will also add fundamental knowledge to  
416 our understanding of QCD matter, such as the precise nature of quasi-particles in the QGP phase and  
417 the determination of the stopping power  $-dE/dx$  of a hot and dense QGP for colored partons. This  
418 determination of the stopping power will provide us with information that is analogous to our precise  
419 knowledge of the stopping power of ordinary matter for electrically charged particles [110, 111, 112].

420 The previously discussed Standard Model of heavy-ion physics based on the hydrodynamic paradigm  
421 is still incomplete at present. It requires additional new insights, such as the detailed nature of the  
422 initial state, in particular how to describe the nuclear wave function at low Bjorken  $x$ , as well as the  
423 determination of the fundamental process which allows fast thermalization at early times to occur in  
424 heavy-ion collisions. In the following sections we will discuss in more detail additional important aspects  
425 of the discovery potential, quantifiable deliverables, and open questions of the future US heavy-ion  
426 physics program in the coming years.

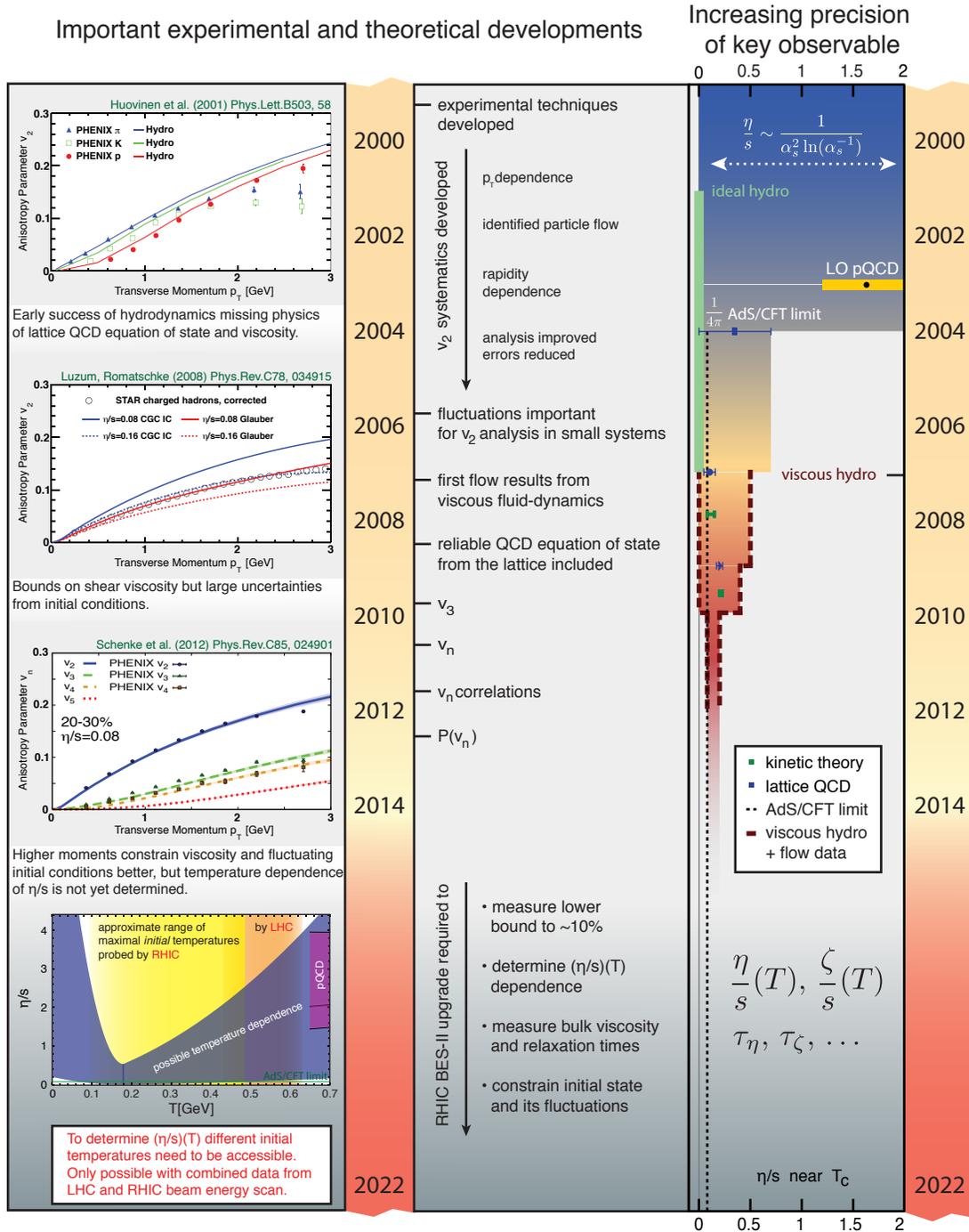


Figure 1: Timeline of important experimental and theoretical developments leading towards increasingly precise understanding of flow, transport properties of the quark-gluon plasma, and the initial state and its fluctuations. The three key figures are taken from [113, 70, 114]. On the right, the increasing precision in one key observable, the shear viscosity to entropy density ratio  $\eta/s$  near its minimal value, is illustrated. Shown results were obtained in [115] (pQCD) [73] (AdS/CFT limit) [116, 117, 118] (lattice QCD - pure glue at  $\sim 1.6 T_c$ ,  $1.24 T_c$ , and  $1.58 T_c$ , respectively) [119, 120] (ideal hydrodynamics) [121, 122] (perturbative QCD/kinetic theory) [123, 70, 124, 105] (viscous hydrodynamics constrained by flow measurements).

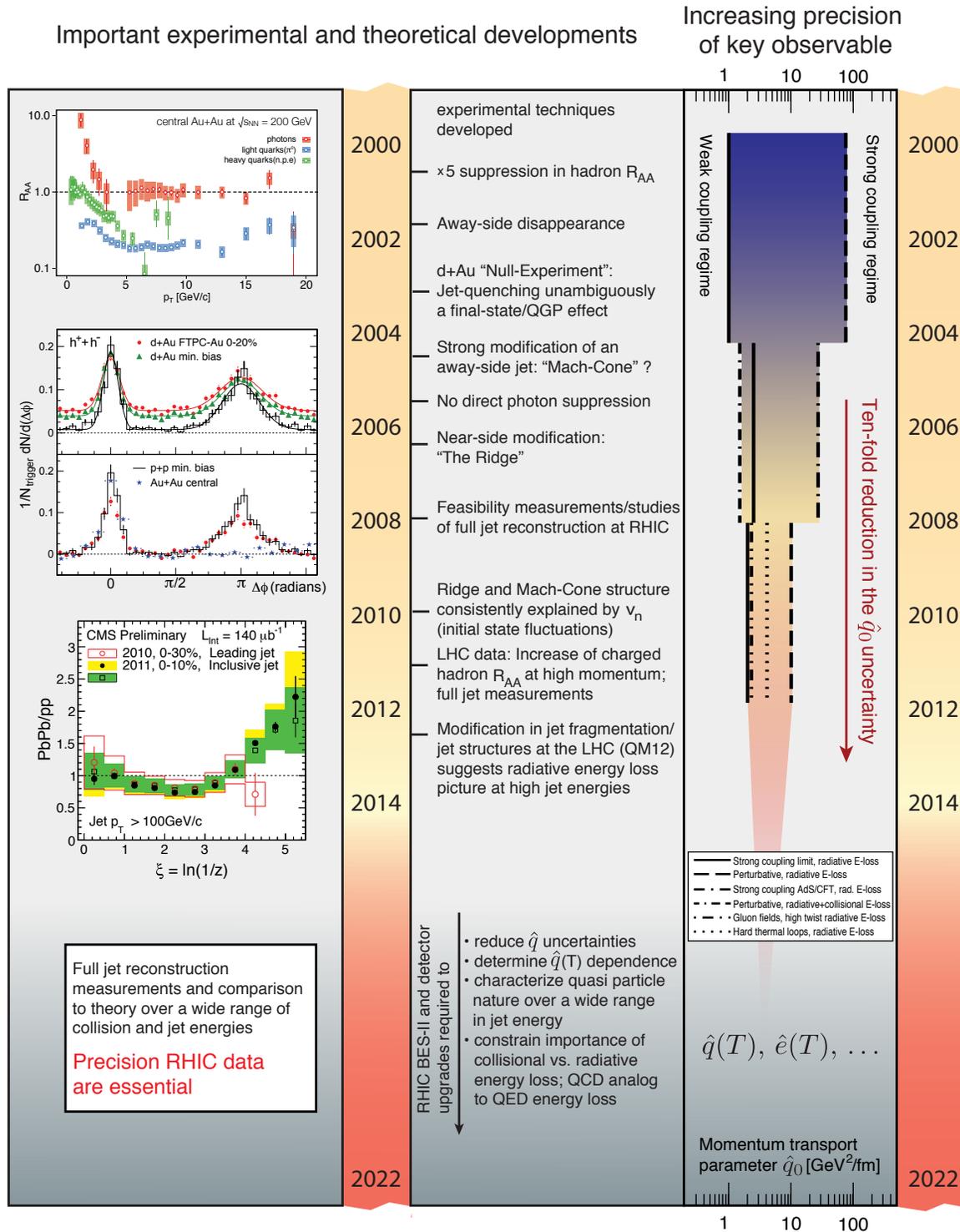


Figure 2: Timeline of important experimental and theoretical developments leading towards the increasingly precise understanding of jet energy-loss mechanisms and its related transport coefficients ( $\hat{q}$ ) as illustrative example on the r.h.s.). The future determination of the temperature dependence of  $\hat{q}(T)$  and  $\hat{e}(T)$  relies on the proposed detector upgrades to STAR and PHENIX as well as the BES-II program and future LHC measurements.

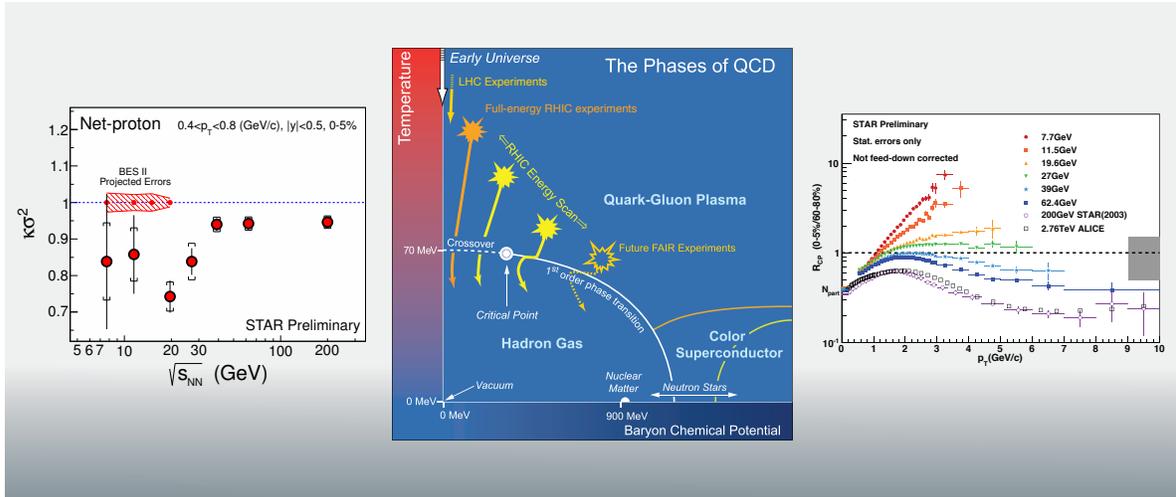


Figure 3: Left: current and projected uncertainties on the net-proton kurtosis  $\times$  variance, a measure of the shape of the event-by-event distribution of net protons. Center: illustration of the phase-diagram of QCD matter, including the area of the phase diagram probed by the beam energy scan. Right: nuclear modification factor  $R_{AA}$  in central Au+Au collisions measured for different collision energies during phase #1 of the beam energy scan demonstrating the transition from confined to deconfined matter.

#### 4.1 Search for the QCD Critical Point: Beam Energy Scan Phase II

Bulk matter in which the interactions are governed by QCD has a rich phase structure, as shown in the center frame of Figure 3, which can be explored by varying the collision energy between heavy nuclei. In collisions of two nuclei, versus collisions of nuclei with their antimatter partner, the matter is formed with a net baryon density, or baryochemical potential ( $\mu_b$ ), which decreases with increasing collision energy. At zero baryochemical potential, lattice gauge calculations have firmly established that the transition from normal nuclear matter to the Quark Gluon Plasma is of the crossover type, in which no thermodynamic quantity diverges even in the infinite volume limit. At high baryochemical potential and low temperature, the transition is strongly first order, which leads to the conjecture that there must be a critical endpoint in the QCD phase diagram. In recent years lattice calculations have been extended to finite baryochemical potential, with many of these calculations finding a critical endpoint, though its location (and even its existence) are highly uncertain due to the difficulty of performing lattice calculations in this regime. The identification of the QCD critical point is therefore presently an experimental question: should it be found, its location and existence would provide a unique landmark in the understanding of the QCD phase diagram from first principles.

The collision energies currently available at heavy ion colliders span almost three orders of magnitude, from the lowest center of mass energy per nucleon  $\sqrt{s_{NN}}$  of 7.7 GeV first performed at RHIC in 2010, to 5.5 TeV eventually available at the LHC. A first-phase scan over the lower end of this range was performed in 2010 and 2011. This scan indicates that RHIC sits at a "sweet spot" in energy, in which rapid changes occur in a number of signatures for energies up to approximately 30 GeV, while remaining surprisingly stable beyond that over the two orders of magnitude to the LHC. As an illustrative example, the right frame of Figure 3 shows the hadron suppression  $R_{CP}$  in central collisions for  $\sqrt{s_{NN}}$  from 7.7 GeV to 2.76 TeV, in which it is clear that the strongest changes occur at the lowest energies. Combined, these measurements provide a substantial hint that collisions at energies at the lower range available at

451 RHIC probe a region of non-trivial structure in the QCD phase diagram. The disappearance of many key  
452 signatures of deconfined matter as the collision energy is lowered hints that the matter is moving from  
453 one with partonic degrees of freedom to one with hadronic degrees of freedom as the initial temperature  
454 decreases.

455 However, many of these measurements are of limited statistical power. In order to convert these into  
456 conclusive statements, more luminosity is needed. A cooling upgrade to RHIC can provide an order  
457 of magnitude higher luminosity for  $\sqrt{s_{NN}} < 20$  GeV, on the timescale of 2017. Figure 3, shows the  
458 current and projected uncertainties on the net-proton kurtosis  $\times$  variance, a measure of the shape of  
459 the event-by-event distribution of net protons. As one passes through a critical point from high to low  
460 energies, this quantity is expected to first go below unity, and then become large as the correlation  
461 length diverges near the critical point. The uncertainties in the current measurements do not allow for  
462 an identification of this behavior, clearly more precise measurements are needed, especially at the lower  
463 energies.

## 464 4.2 Parity-Violating Fluctuations

465 QCD matter created in relativistic heavy-ion collisions may possess a very rich set of features, reflecting  
466 the fundamental symmetries (and violations thereof) of QCD. Among the more intriguing features which  
467 are currently being searched for is the presence of the Chiral Magnetic Effect (CME) [50, 51, 125, 126]:  
468 the QCD Lagrangian in principle permits the existence of a so-called  $\theta$ -term which violates time-reversal  
469 and thus CP symmetry. While precision measurements of the electric dipole moment have not found any  
470 indications of CP violation, the presence of a strong external magnetic field can be used to probe the  
471 CP-odd sector of QCD which otherwise may not be accessible. As was pointed out in [50], non-central  
472 heavy-ion collisions create a coherent magnetic field that may convert topological charge fluctuations in  
473 the QCD vacuum into global electric charge fluctuations with respect to the reaction plane.

474 While initial measurements of charge sign correlations [48, 49] are qualitatively consistent with  
475 expectations of the Chiral-Magnetic Effect [50, 51], the uncertainties associated with these measurements  
476 remain large and preclude any definitive assessment. Since the CME should disappear with either the  
477 absence of deconfinement (i.e. at low collision energy) or the absence of a magnetic field (as in very  
478 central U+U collisions), the planned Beam Energy Scan Phase II as well as extended runs with U+U  
479 provide a unique discovery potential for this effect. We should note that the search for the CME has  
480 the virtue of being the only known means of testing in the laboratory the gauge theory dynamics that  
481 might (in its SU(2) incarnation) be responsible for the matter/antimatter excess in the universe and is  
482 thus of highly significant theoretical importance [51].

## 483 4.3 Differential Measurements of Transport Properties of the sQGP

### 484 4.3.1 Precision Measurement: Temperature dependence of $\eta/s$ and other bulk transport 485 parameters

486 Given the outlined success of hydrodynamics and the *Standard Model of heavy ion physics* the next  
487 natural step is to systematically measure the temperature dependent values of bulk transport parameters.  
488 In addition to  $(\eta/s)(T)$  these include the temperature dependent bulk viscosity over entropy density  
489 ratio  $(\zeta/s)(T)$  as well as corresponding relaxation times. With the development of comprehensive event-  
490 by-event viscous relativistic hydrodynamic simulations coupled to hadronic cascade models, theoretical  
491 simulations are just reaching the necessary maturity to undertake such investigations. At the same time,  
492 a differential measurement of  $(\eta/s)(T)$  requires experimental control over the initial temperature. Thus,

493 high precision measurements of higher harmonic flow coefficients  $v_n$ , that are sensitive to  $(\eta/s)(T)$ ,  
 494 at both LHC and varying RHIC energies are absolutely essential. The behavior of  $(\eta/s)(T)$  near the  
 495 critical temperature  $T_c$ , where typical liquids (e.g.  ${}^4\text{He}$  and even water) show rapid changes in  $\eta/s$ , is  
 496 particularly useful to establish a deeper understanding of the nature of QCD matter. Furthermore, to  
 497 establish effects of non-zero bulk viscosity, one has to utilize the strength of RHIC by exploring a broad  
 498 variety of both collision energies and system sizes. The phase II of the RHIC Beam Energy Scan is  
 499 crucial for these measurements.

### 500 4.3.2 Precision Measurement: Jets – The Physics of Partonic Energy Loss

501 The emission of hadrons with large transverse momentum is observed to be strongly suppressed in  
 502 central collisions of heavy nuclei [17, 18] compared to proton-proton interactions. The origin of this  
 503 phenomenon, commonly referred to as *jet-quenching*, can be understood in the following way: during  
 504 the early pre-equilibrium stage of the relativistic heavy-ion collision, scattering of partons which leads  
 505 to the formation of deconfined quark-gluon matter often engenders large momentum transfers which  
 506 leads to the formation of two back-to-back hard partons. The interaction of these partons with the  
 507 surrounding medium leads to significant energy loss, and is sensitive to the structure of the QGP and  
 508 its transport properties.

509 Compared to the bulk medium dynamics described in the previous sections, the physics of partonic  
 510 energy loss in the QGP [79, 127, 128, 80, 81, 82, 83, 84, 85, 86, 77, 78, 87] is not yet in a similarly  
 511 advanced state. Nevertheless, significant progress in constraining the underlying microscopic processes  
 512 has been made, with RHIC pioneering this field [17, 18, 21, 22, 23, 24].

513 One of the parameters that characterizes the interaction of an energetic jet with the QGP medium is the  
 514 momentum transport parameter  $\hat{q}$ , defined as the typical momentum transfer squared per unit length  
 515 incurred by the hard parton in the strongly interacting medium [127, 128]. It depends on the coupling  
 516 regime (strong versus weak) at the scale of the interaction, the nature of the plasma (quasi-particle-  
 517 dominated versus quasi-particle-less) and the micro-physics of many-body QCD in strongly-interacting  
 518 matter. The measurement of  $\hat{q}$  relies on an interplay between experiment and theory, since it is not  
 519 a directly measurable quantity.  $\hat{q}$  is commonly extracted via a comparison between data, e.g. on the  
 520 nuclear modification factor  $R_{AA}$  or two particle correlation functions, and theoretical calculations of  
 521 the same quantities with  $\hat{q}$  as parameter of the calculation. The extraction of  $\hat{q}$  thus inherently is not  
 522 only dependent on experimental uncertainties, but also on the model assumptions that go into the  
 523 respective theoretical calculation. A significant fraction of the  $\hat{q}$  uncertainties quoted here stem from  
 524 these theoretical uncertainties. The measurement of correlation observables at high precision will not  
 525 only reduce experimental uncertainties, but also significantly constrain the theory calculations, thus  
 526 reducing their systematic uncertainties as well.

527 Over the past decade considerable progress has been made at RHIC in constraining the value of  $\hat{q}_0$ ,  
 528 the value of  $\hat{q}$  at the formation time of the QGP  $\tau_0$ , as illustrated in Figure 2. Shown in the right  
 529 hand side is the value of the momentum transfer parameter at time  $\tau_0 = 0.6$  fm, typical of the  
 530 formation time of the QGP at RHIC. Most of the constraints are based on (single particle) light hadron  
 531 measurements [129, 130]. Initial  $\hat{q}_0$  estimates covered a staggering two orders of magnitude, ranging  
 532 from the weak coupling [16, 88] to the strong coupling limit, where nuclear matter created in RHIC  
 533 collisions transitions from a completely opaque core to a fully transparent corona [131, 132]. This  
 534 significant uncertainty in the value of  $\hat{q}_0$  was due in part to the large experimental uncertainties in the  
 535 early days of RHIC.

536 Initial theoretical attempts to constrain  $\hat{q}_0$  concentrated mainly on radiative energy loss. Subsequent

537 efforts have included both radiative and collisional energy loss in the QGP [133, 134] resulting in a new  
 538 definition of the lower bound. On the strong coupling side, the AdS/CFT correspondence has been used  
 539 to calculate  $\hat{q}_0$  as well [77] and can be interpreted as an upper limit for that quantity. This resulted in a  
 540 reduction in the uncertainties of  $\hat{q}$  by a factor of three. The latest analysis of increasingly more precise  
 541 RHIC measurements decreased the allowed range of  $\hat{q}_0$  from 2 GeV<sup>2</sup>/fm to 10 GeV<sup>2</sup>/fm [130, 135].

542 Concurrent developments in theory and experiment have allowed to reduce the uncertainty of the  
 543 momentum transport parameter at RHIC by an overall factor of twenty. The continuing improvement in  
 544 the precision determination of  $\hat{q}$  is a remarkable progress and success of the field, but the remaining  
 545 uncertainty of roughly of a factor of five still hinders the precise determination of the medium transport  
 546 properties. In particular, the QGP response to different jet energies and the temperature dependence of  
 547 the transport parameter cannot be constrained at this stage with sufficient precision. A program of  
 548 RHIC upgrades with optimal kinematic coverage is expected to reduce these uncertainties to a factor of  
 549 two in 2020 and key aspects will be discussed in the following:

550 • **Study of low energy jets in medium:**

551 The interactions of the full parton shower (i.e. the full jet) with the medium probes the transport  
 552 properties of the QGP at scales that range from the bulk scale set by the temperature  $\sim T$ , to a  
 553 scale  $\sim \sqrt{E_T T}$  (with  $E_T$  being the transverse energy of the shower). The measurement of jets  
 554 at relatively small jet energies around 40-50 GeV will allow for the mapping of the energy and  
 555 momentum transport coefficients in the most interesting and least understood region between the  
 556 weak and strong coupling limits. Reconstruction of these jets of relatively small energies can be  
 557 achieved at RHIC with higher efficiency than at the LHC, due to the underlying background at  
 558 RHIC being smaller than at LHC.

559 • **Temperature dependence of  $\hat{q}$ :**

560 The measurement of the temperature dependence of  $\hat{q}$  is of analogous importance to to the future  
 561 studies of temperature dependence of  $\eta/s$ . Since the expected scaling of  $\hat{q}$  with temperature is a  
 562 strong function of  $T$  [16, 77, 136, 137], jet quenching measurements are sensitive to the earliest  
 563 times and highest temperatures. In order to achieve sensitivity to temperatures around 1 - 2  
 564  $T_C$ , measurements at RHIC are needed for different colliding systems and smaller center of mass  
 565 energies as opposed to LHC energies, where larger initial temperatures are produced.

566 • **Probing the coupling strength of the medium:**

567 Both the *soft*  $\eta/s$  bulk transport parameter and the *hard* partonic energy loss parameters such  
 568 as  $\hat{q}$  (and analogously  $\hat{e}$ , defined as the longitudinal momentum transfer per unit length) are  
 569 sensitive to the underlying coupling of the matter, but in different ways. If precise measurements  
 570 of bulk and jet observables are accessible, one can utilize the relationship between the energy and  
 571 momentum transfer parameters (for example in weak coupling  $\hat{q} = 1.25T^3/(\eta/s)$  [137]), to test  
 572 the nature and coupling strength of the QGP medium.

573 • **Testing the quasi-particle nature of the QGP:**

574 It is expected that at some sufficiently large momentum scale a quasiparticle picture of the QGP  
 575 must be valid, even though on its natural length scale it is a strongly coupled fluid. To determine  
 576 this scale and the detailed nature of the quasi particles, jet measurements over a wide range of  
 577 energies and with different medium temperatures (RHIC complementary to LHC) are essential.  
 578 Even though recent measurements at the LHC suggest that a strongly coupled AdS/CFT like  
 579 picture at the scales currently accessible is not favored [138], precision jet measurements at RHIC  
 580 will allow to map out the currently unexplored regime closer to the strongly coupled limit.

581 • **Radiative vs. elastic energy-loss:**

582 The exact nature of what the parton is scattering off in the medium is tied directly to the balance  
583 between radiative energy loss and inelastic collisional energy loss in the medium and will allow to  
584 measure the relative importance of these processes. In QED, the stopping power of matter for  
585 electrically charged particles is known to within a few percent. At the LHC, in the  $E_T > 50$  GeV  
586 regime, jet modification appears to be dominated by radiative energy loss. RHIC can provide  
587 the necessary kinematic coverage to study the relative significance of collisional and radiative  
588 processes, thereby advancing our understanding of dense QCD matter at high energies. Therefore  
589 RHIC and LHC combined will allow to map out the stopping power  $-dE/dx$  of hot and dense  
590 QGP for colored patrons [139] in analogy to our precise knowledge of the stopping power of  
591 ordinary matter for electrically charged particles [110, 111, 112].

592 **4.3.3 Heavy Flavor and Quarkonia**

593 Heavy quark observables promise enormous potential for insight into the dynamics of the QGP. Because  
594 charm and bottom quarks are so massive, they must be produced in the very earliest stages of the  
595 collision. Once produced, heavy quarks act as identifiable test particles, navigating the entire evolution  
596 of the medium, participating in and being affected by its dynamics. Produced as  $q\bar{q}$  pairs, the heavy  
597 flavor may emerge together as quarkonia (closed heavy flavor) or in separate hadrons (open heavy  
598 flavor). As tomographic probes of strongly-interacting matter, heavy flavors provide a well-defined  
599 physical scale against which the temperature of the medium can be gauged via the pattern of quark  
600 diffusion. Due to their different Lorentz boost factor at a given momentum transfer, heavy quarks shed  
601 light on the mechanisms of collisional and radiative energy loss in the QGP. Furthermore, the large D  
602 and B meson masses suggest early hadronization and have stimulated a fresh look in the in-medium  
603 fragmentation and dissociation of open and closed heavy flavor. Charm and beauty quarks are also  
604 sensitive to resonant states just above the QCD chiral transition temperature.

605 The small production cross sections involved mean that heavy flavor measurements require high luminosity  
606 and extremely capable detectors. Interestingly, now that RHIC is effectively operating at the luminosities  
607 foreseen for the RHIC II project, the statistics expected for produced heavy flavor at RHIC and at LHC  
608 are comparable [140]. The higher  $b$  and  $c$  production cross sections at the LHC are largely compensated  
609 by the higher heavy ion luminosity and longer per year running time of RHIC. In any case, a complete  
610 program to investigate the QGP using heavy flavor probes will be a multi-year program of integrating  
611 luminosity and performing necessary reference measurements.

612 Measurements of heavy flavor at RHIC already present an intriguing puzzle to the high-energy nuclear  
613 physics community. Early theoretical expectation was that heavy quarks would lose considerably less  
614 energy in their passage through the medium than light quarks do, but PHENIX and STAR measurements  
615 of the suppression of non-photonic electrons coming from the decays of D and B mesons indicate that  
616 heavy quarks do, in fact, lose a considerable amount of energy in the QGP. Furthermore, the elliptic flow  
617 of non-photonic electrons suggests heavy quarks have largely thermalized in the medium. This surprising  
618 behavior of heavy mesons has recently been observed to be even more pronounced at the LHC.

619 The heavy quark diffusion coefficient is a quantity that the heavy flavor program at RHIC will determine  
620 over the next several years to a precision of  $\sim 10\text{--}15\%$ : In the quasi-particle picture, heavy quarks  
621 lose energy in the QGP medium through both elastic collisions and gluon emission. The first process  
622 dominates at the low to intermediate heavy quark momenta predominantly accessible at RHIC while  
623 the latter dominates at the large heavy quark momenta mostly accessible at the LHC. In the domain  
624 dominated by collisional energy loss, heavy quark evolution can be described as a diffusion process with

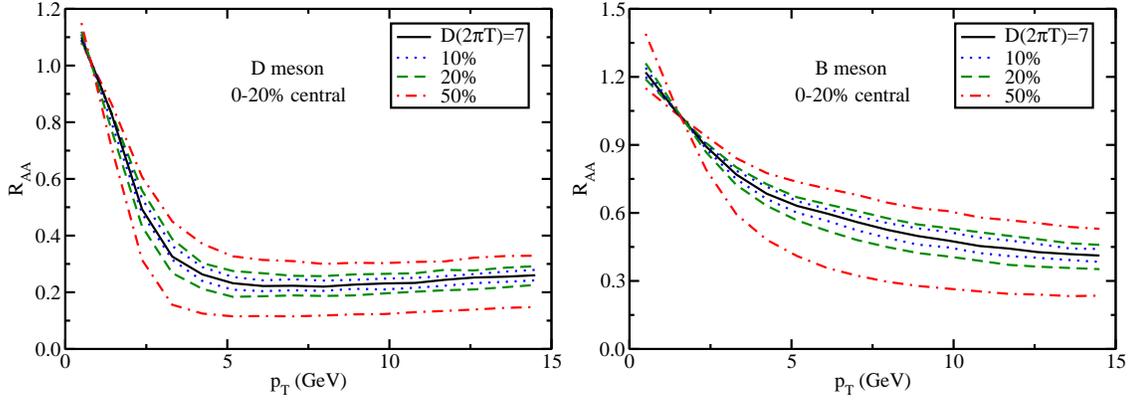


Figure 4: Diffusion calculation of the nuclear modification factor  $R_{AA}$  for D-mesons (left) and B-mesons (right) in central Au+Au collisions at RHIC. Shown is how a  $\pm 10\%$ ,  $\pm 20\%$  and  $\pm 50\%$  variation in the diffusion coefficient translates into a respective change of the nuclear modification factor. For a determination of the diffusion coefficient within  $\pm 10\%$ , the nuclear modification factor needs to be measured with similar precision.

625 the heavy quark diffusion coefficient as the governing transport coefficient [141, 142]. The precision  
 626 with which the diffusion coefficient can be determined scales directly with the uncertainties of the  
 627 experimental measurements for the nuclear modification factor  $R_{AA}$  and elliptic flow coefficient  $v_2$  of D  
 628 and B mesons; if these quantities can be measured with an uncertainty of  $\sim 10\%$  this will translate into  
 629 a determination of the diffusion coefficient to similar precision (Fig. 4).

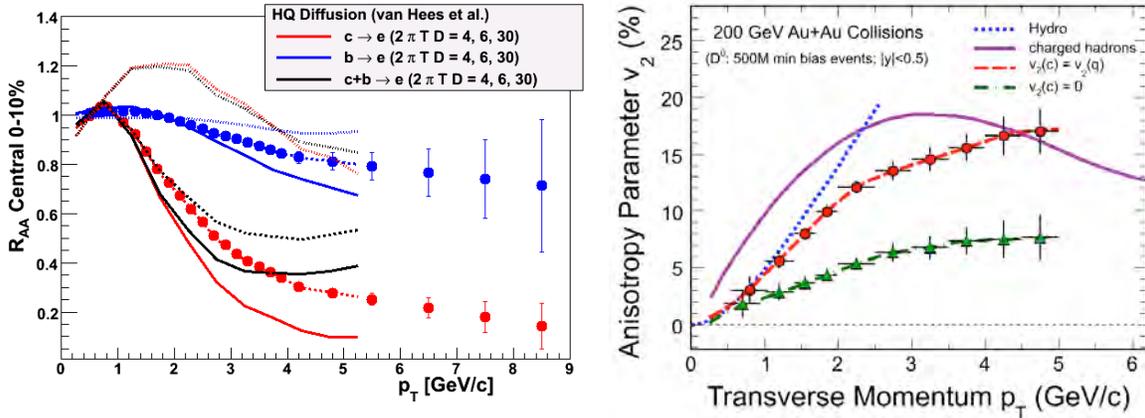


Figure 5: Projected uncertainties for the determination of flavor separated  $R_{AA}$  for the most central 10% of  $4.3 \text{ nb}^{-1}$  of Au+Au collisions and  $14.8 \text{ pb}^{-1}$  of  $p+p$  collisions (left). Also shown are diffusion calculations by van Hees et al Projected uncertainties for  $D^0$   $v_2$  measurement using the STAR detector in a 10 week 200 GeV Au+Au RHIC run (right).

630 Measuring heavy quarks by their semi-leptonic decay alone does not distinguish between the decays of  
 631 D and B mesons [43] and represents an admixture of information about charm and bottom quarks.  
 632 Since bottom quarks are more than three times as massive as charm quarks, making them much less  
 633 abundant than charm quarks, but also leading to significant differences in their dynamical behavior [143],  
 634 separating the two signals has clear significance. One can employ various techniques to decompose the

635 separate contributions of charm and bottom [144], but to make direct measurements both STAR and  
636 PHENIX have developed a physics program for the next several years centered around sophisticated  
637 vertex detectors that are able to distinguish the different decay lengths of the D and B mesons. The  
638 PHENIX VTX and STAR HFT are barrel detectors near mid-rapidity; the PHENIX FVTX is an endcap  
639 detector. The PHENIX VTX has recently demonstrated first results for  $c/b$  separation in heavy ion  
640 collisions. The left panel of Figure 5 shows the projected uncertainties one would obtain on the nuclear  
641 modification factor,  $R_{AA}$ , with a high statistics Au+Au run and two years of accumulated  $p+p$  data.

642 The identification of heavy flavor through its semi-leptonic decay is well complemented by a direct  
643 measurement of topologically reconstructed D mesons. This technique has some very positive features,  
644 especially at low transverse momentum, as one does not need to unfold the spectrum of a decay  
645 electron to obtain the momentum of the parent meson. The right panel of Figure 5 shows the projected  
646 uncertainties one would obtain for the  $v_2$  of charm quarks under two different assumptions in a ten  
647 week Au+Au run. The  $v_2$  for charm flow from reconstructed D mesons has also been measured by  
648 ALICE [145], and a measurement at RHIC would enable a statement about the temperature dependence  
649 of the coupling of charm to the flowing medium.

650 Measurements of quarkonia provide different information about the properties of the QGP. At high  
651 temperatures one expects the emergence of Debye screening of the interaction between quarks and  
652 gluons. This leads to the dissolution of hadronic bound states [146]. A particularly interesting subset of  
653 hadronic states consists of those comprised of heavy quarks since the spectrum of low lying states can be  
654 found using potential-based non-relativistic treatments. Based on such potential models there were early  
655 predictions [147, 148] that  $J/\psi$  production would be suppressed in heavy ion collisions relative to the  
656 corresponding production in proton-proton collisions scaled by the number of nucleons participating in the  
657 collision. In recent years there have been important theoretical advances in the understanding of heavy  
658 quark states at finite temperature using analytic techniques [149, 150, 151, 152, 153, 154, 155, 156, 157]  
659 and lattice QCD [158, 159, 160, 161, 162, 163, 164].

660 Practitioners are, for the first time, using realistic viscous hydrodynamical models to describe the  
661 evolution of the matter in which the heavy quark bound states are embedded [165, 166, 167]. With  
662 these advances, the study of heavy quarkonium suppression has moved into a new quantitative era, in  
663 which precise comparison of experimental data and theoretical predictions is vitally important. The  
664 measurement of the suppression of the ground and excited states of heavy quarkonium will enable the  
665 determination of key plasma properties such as the initial temperature, degree of momentum space  
666 anisotropy, and the shear viscosity to entropy ratio. RHIC's ability to perform beam energy and system  
667 size scan are essential for these measurements.

668 Already there are results from CMS showing that the higher mass states of the upsilon are relatively  
669 more suppressed in Pb+Pb collisions at 2.76 TeV than in control  $p+p$  collisions [9]. STAR's muon  
670 telescope detector (MTD) will enable measurements at RHIC energies of the upsilon family of states,  
671 and the right panel of Figure 6 shows the uncertainties one could achieve within a few years.

672 Quarkonia can be produced directly, but there is also the possibility of producing a  $q\bar{q}$  state through  
673 recombination of a quark and an anti-quark from different initially produced pairs. The degree to which  
674 recombination plays a role can be controlled by studies of the  $c\bar{c}$  and  $b\bar{b}$  systems at RHIC and LHC.

675 ALICE  $J/\psi$  measurement [168] compared to PHENIX data is shown in the left panel of Figure 6. The  
676  $J/\psi$  in central Pb+Pb at 2.76 TeV are relatively less suppressed than is the case in central Au+Au at 200  
677 GeV. Charm is so abundant at the higher collision energy of LHC that recombination of independently  
678 produced charm quarks into quarkonia may be responsible for the difference. This is a particular example  
679 where complementary measurements at the LHC and RHIC illuminate the physics of the QGP.

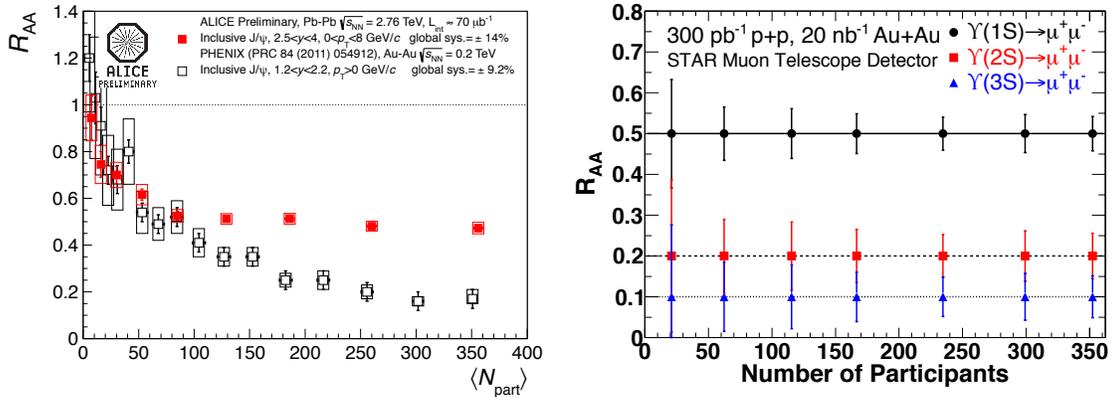


Figure 6: left) A comparison of ALICE results for  $J/\psi$  suppression versus centrality compared to the results obtained by PHENIX. The relatively weaker suppression in central collisions may be due to recombination of charm from abundantly produced  $c\bar{c}$  pairs at the LHC. (right) Projected uncertainties for the suppression of the different mass states of the epsilon family.

#### 680 4.4 Pre-Equilibrium Physics

681 One of the fundamental open questions in the study of the Quark Gluon Plasma is to what extent the  
682 system that is produced in relativistic heavy ion collisions achieves local isotropic thermal equilibrium  
683 and at what timescale this may occur. Immediately after the initial nuclear impact, the Quark Gluon  
684 Plasma is not a thermal isotropic plasma. The constituents must interact for some period of time in  
685 order to reach a (quasi)-thermal state. In the high-energy limit the incoming nuclei are dominated by  
686 small- $x$  gluons whose occupation numbers are large,  $n \sim 1/\alpha_s$  [169]. The question then becomes, how  
687 does one connect such a coherent nuclear state to an incoherent plasma of quarks and gluons on the  
688 fm/c timescale. The answer to this question is highly relevant for Quark Gluon Plasma phenomenology  
689 since a key component of the Standard Model of heavy-ion collisions described in section 3 is the  
690 viscous hydrodynamic evolution of the QGP phase, which requires local isotropization of the Quark  
691 Gluon Plasma. Standard hydrodynamical fits to RHIC elliptic flow data suggested that the Quark Gluon  
692 Plasma has a thermalization and isotropization time on the order of 0.2 – 1.0 fm/c. However, some  
693 recent viscous hydrodynamic analyses have shown that the pre-equilibrium phase of the Quark Gluon  
694 Plasma evolution can last for up to 2 - 3 fm/c after the initial nuclear impact [70, 170].

695 In order to address the question of the precise thermalization and isotropization times of the Quark  
696 Gluon Plasma there are two prevailing approaches in the literature. The first is to take the high-energy  
697 limit in which the plasma is weakly-coupled and extrapolate the resulting perturbative series to the  
698 couplings relevant ( $\alpha_s = 0.3$ ) for phenomenological applications [171, 172, 173, 174]. The second is  
699 to study the problem using the conjectured anti de Sitter space / conformal field theory (AdS/CFT)  
700 formalism in the infinitely strong coupling limit [175, 176, 177, 178, 179, 180, 181]. On the perturbative  
701 side we have learned in the last ten years that there exist non-Abelian plasma instabilities which help to  
702 accelerate the isotropization of the Quark Gluon Plasma. Such predictions began over two decades ago  
703 [182, 183, 184] but in the last decade we have seen tremendous advances in our ability to simulate the  
704 complicated dynamics of non-Abelian plasma instabilities [185, 186, 187, 188, 189, 190, 191, 192, 193].  
705 Such studies are of key importance since it can be shown that plasma instabilities induce an anomalous  
706 shear viscosity in the plasma which is lower than what one obtains in a static thermally equilibrated  
707 Quark Gluon Plasma [194, 195]. The other important conceptual change due to the existence of  
708 non-Abelian plasma instabilities is that their dynamics naturally drives the system to a state which has

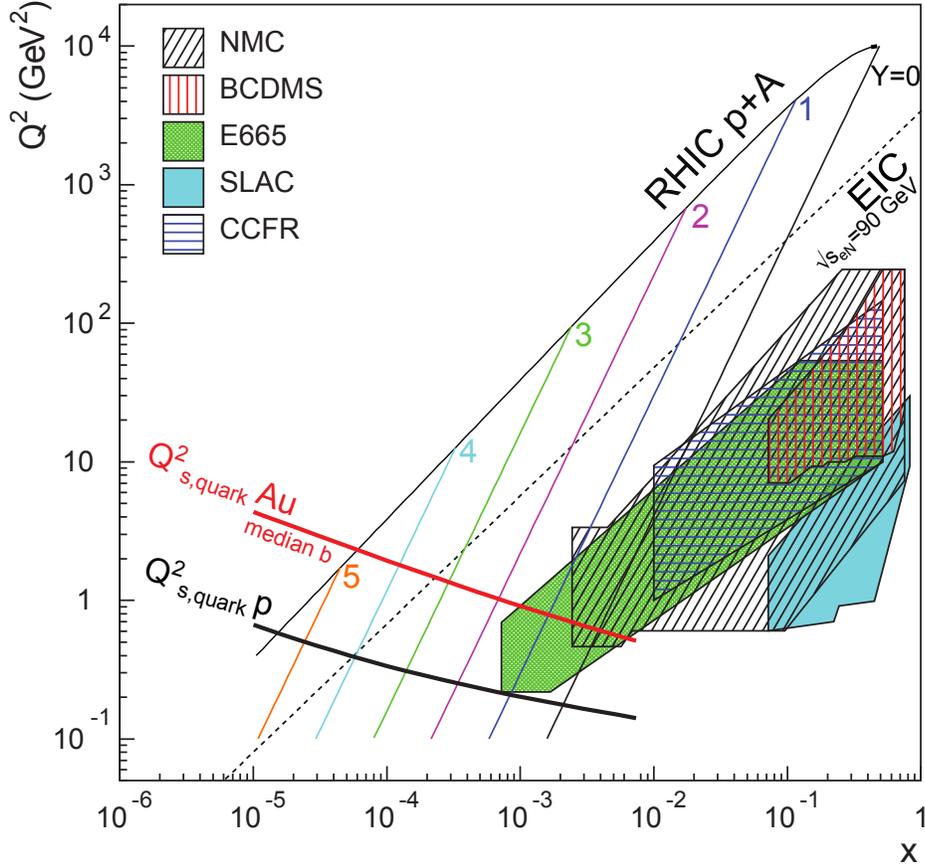


Figure 7: Kinematic coverage in the  $x - Q^2$  plane for p+A collisions at RHIC, along with previous e+A measurements, the kinematic reach of an electron-ion collider (EIC), and estimates for the saturation scale  $Q_s$  in Au nuclei and protons. Lines are illustrative of the range in  $x$  and  $Q^2$  covered with hadrons at various rapidities.

709 parametrically large field occupation numbers. Such large occupation numbers cause the system to  
 710 interact strongly even though the coupling constant itself may not be large.

711 The cleanest and most sensitive probes to the pre-equilibrium phase of the heavy-ion collision are  
 712 photons and leptons, since they do not interact with the concurrently forming QGP medium after their  
 713 production [196, 197]. However, a very high precision is required for these measurements in order to  
 714 de-convolute the pre-equilibrium photon and lepton emission from the subsequent thermal emission  
 715 of these probes during the Quark Gluon Plasma evolution. The planned upgrades to the STAR and  
 716 PHENIX detectors are designed to deliver the required precision in the measurement of leptons and  
 717 photons that are crucial for the unraveling of the thermalization mechanism. These measurements have  
 718 to be augmented by data from the LHC, since thermalization times are expected to be shorter at higher  
 719 temperatures and energy-densities.

## 720 4.5 The Nature of the Initial State / Gluon Saturation

721 The nature of the initial state, in particular how to describe the nuclear wave function at low Bjorken  
722  $x$ , is still an area with large experimental and theoretical uncertainties at the current stage of our  
723 understanding. Recent theoretical developments combine the color-glass-condensate framework to  
724 describe fluctuating gluon fields in highly energetic nuclei with a dynamic pre-equilibrium glasma stage  
725 immediately after the collision and viscous hydrodynamics to describe further evolution in heavy-ion  
726 collisions. This provides a promising framework for the study of the initial state and transport parameters  
727 of the quark-gluon plasma by analyzing higher harmonic flow coefficients  $v_n$  and their fluctuations  
728 [198, 199]. First comparisons to flow measurements at RHIC and LHC have been remarkably successful  
729 [41]. However, to access in more detail the subhadronic correlations and dynamics governed by saturation  
730 physics requires further measurements at small  $x$ , and therefore forward rapidities, with the cleanest  
731 measurements possible in p+A and e+A collisions.

732 Experiments at HERA have shown conclusively that as one probes to lower fractional momentum  $x$   
733 in the wave function, the gluon density rises rapidly. This rise cannot continue forever, since it would  
734 eventually lead to a violation of unitarity in high-energy scattering processes. At some point, the  
735 nonlinear nature of QCD will enter to tame this rise, entering into a regime where occupation numbers  
736 are high enough that the process of gluon recombination competes with gluon splitting. The scale at  
737 which this happens is known as the saturation scale. Reaching this scale would open up a new and  
738 unique regime of tractable QCD calculations, in which weak coupling is combined with extremely intense  
739 gluon fields. There is no question that this regime exists somewhere in nature; the main question is  
740 whether it is experimentally accessible at the energies available at current colliders.

741 Current measurements at RHIC of the suppression of single hadrons [52, 54] and back-to-back di-hadron  
742 correlations [55] in d+Au collisions have been interpreted as strong hints that the saturation scale, and  
743 the onset of saturation effects, are accessible at forward rapidities at RHIC [200]. At this point, though,  
744 these interpretations are not unique, for two main reasons.

745 First, as shown in Figure 7, for the kinematic reach of RHIC energies the saturation scale is moderate,  
746 on the order of a few  $\text{GeV}^2$ , so measurements sensitive to the saturation scale are by necessity limited  
747 to semi-hard processes, and effects due to kinematic limits must be fully addressed. To some level  
748 this can be addressed at the LHC, where the larger energies allow for measurements deeper into the  
749 saturation regime, especially at forward rapidities. First measurements have been made at mid-rapidity  
750 by ALICE [201], which correspond approximately to  $y=3-4$  at RHIC. This measurement shows no  
751 suppression of single hadrons for  $p_T > 2 \text{ GeV}$ , as predicted by saturation models [202, 203], however,  
752 alternative models also predict this feature of the data [204]. Key tests at the LHC will come at more  
753 forward rapidities, where saturation effects are stronger and distinct from other descriptions [203, 204].

754 Second, and more importantly, in measurements to date in p+A collisions both the entrance and exit  
755 channels have components that interact strongly, leading to severe complications in the theoretical  
756 treatment. In p+A collisions, these complications can be ameliorated by removing the strong interaction  
757 from the final state, using photons and Drell-Yan electrons. Both PHENIX and STAR have upgrade plans  
758 to make these difficult measurements, which are planned to be in place for high precision towards the  
759 end of this decade. Beyond this, the possibility of using polarized protons at RHIC to probe saturation  
760 phenomena is just beginning to be explored [205], utilizing the large transverse single-spin asymmetries  
761 seen in p+p collisions at forward rapidity (which do not require a polarized ion beam) to explore the  
762 onset of saturation. In addition, measurements of direct photons at forward rapidities over a large  $Q^2$   
763 regime at the LHC could be used, with appropriate upgrades, to probe deeper into the saturation regime.

764 The ultimate level of precision can be obtained using an electron-ion collider, in which strong interactions

765 are removed from the initial scattering, and in which the full kinematics can be reconstructed in the  
766 final state. The rich program available at an electron-ion collider is detailed in a separate White Paper.  
767 Besides the close match in instrumental capability necessary for both p+A and e+A collisions, the  
768 combination of a strong p+A and e+A program allows for detailed tests of universality within the  
769 saturation approach.

## 770 **5 The Future of Relativistic Heavy Ion Physics**

771 In this document we have outlined a research program that will address the most relevant open questions  
772 in the physics of strongly interacting hot and dense QCD matter. It will lead to the quantitative  
773 determination of the most important Quark Gluon Plasma properties, such as the temperature dependence  
774 of its transport coefficients, while also enabling new discoveries, such as the existence and location  
775 of the QCD critical point. This program relies on a number of detector and accelerator upgrades as  
776 specified in *The Case for Continued RHIC Operations* by Steve Vigdor [1].

777 The key pillars of this 5–10 year program are:

- 778 • a beam-energy scan program with unparalleled discovery potential to establish the properties  
779 and location of the QCD critical point and to chart out the transition region from hadronic to  
780 deconfined matter.
- 781 • the quantitative determination of the transport coefficients of the Quark Gluon Plasma, such as  
782 the temperature dependence of the shear-viscosity to entropy-density ratio  $\eta/s$  (including an  
783 assessment of whether the conjectured lower bound has been reached to within a precision of  
784 10%), and that of the energy loss transport coefficients  $\hat{q}$  and  $\hat{e}$ .
- 785 • a jet physics program to study the nature of parton energy loss and the quasi-particle nature of  
786 the QGP.
- 787 • a heavy-flavor physics program to probe the nature of the surprisingly strong interactions of  
788 heavy quarks with the surrounding medium, as well as quarkonia measurements that will provide  
789 standard candles for the temperatures obtained in the early stages of a heavy-ion reaction.
- 790 • a systematic forward physics program to study the nature of gluon saturation.

791 As noted earlier, the last bullet leads naturally to the physics program for the Electron Ion Collider. It is  
792 also important to note that this physics program cannot be pursued with data from the Large Hadron  
793 Collider. RHIC provides essential measurements that span the range above and below the transition  
794 region in temperature as well as regions of the phase diagram at higher baryon density. The science  
795 objectives presented in this document can only be achieved in a heavy ion program that includes the  
796 continued operation of the Relativistic Heavy Ion Collider in addition to continued participation in the  
797 LHC heavy ion program. The heavy ion program described herein will ensure continued leadership in  
798 the field and will complete the scientific investment the US government has made in seeking to discover  
799 and understand the bulk properties of strongly interacting matter.

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