## Quark-gluon plasma multiplicity from AdS spaces modifications Pozdeeva E.O.

### SINP MSU

#### based on I.Ya. Aref'eva, E.O. Pozdeeva, T.O.Pozdeeva to be bublished in Theor.Math.Phys. 176(1)(2013)

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Quark Gluon Plasma (QGP) has been discovered in Au+Au collision at energy 100 GeV for nucleon in 2005 @ RHIC

In holographic approch clasical gravity in  $AdS_5$  discribes strong coupling field theory in 4D Minkowski space

There is hypothesis that QGP formation in 4D space corresponds to Black Holes creation in dual 5D space.

Gubser, Klebanov, Polyakov, 9802109

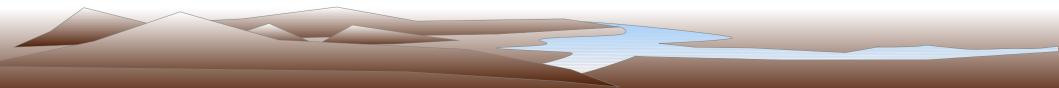
Witten, 9802150

The gravitational shock wave in  $AdS_5$  space is dual to ultrarelativistic heavy-ion in 4D space-time.

Thus,

- heavy-ion collisions can be represented such as gravitational shock waves collisions in  $AdS_5$
- QGP formation is equivalent BH creation in  $AdS_5$

Gubser et al.; 0805.1551, 0902.4062



#### Problem:

- How to get experimental dependence of multiplicity on energy from holographic model.
- Simplest holographic model is related with use of N=4 SYM [But QCD is not SYM]

• Our goal: to study more complicate models to fit experimental data.

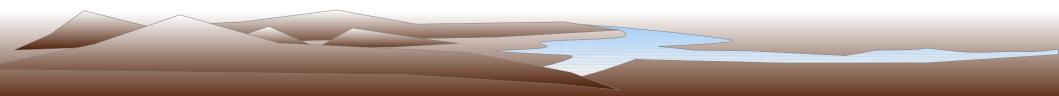
Main conjecture: multiplicity is proportional to entropy

 $S \sim N$ 

Gubser et al.; 0805.1551

On experiments can be measured only  $N_{ch}$  :  $N \sim N_{ch}$ 

B. B. Back et. al., 0210015[nucl-ex].



Accordingly experiment the charged-particles pseudorapidity density depends on colliding energy

 $\frac{dN_{ch}/d\eta \propto s_{NN}^{0.11}}{E = (1/2)\sqrt{s_{NN}}}$  pp collision K. Aamodt et al.[ALICE Collaboration], 1011.3916 [nucl-ex]. DISCREPANCY

for Pb-Pb and Au-Au collisions

The simple holographic model gives

 $dN_{ch}/d\eta \propto s_{NN}^{2/3}$ 

 $dN_{ch}/d\eta \propto s_{NN}^{0.15}$ 

The mininal black hole entropy can be estimated by trapped surface area

$$S \ge S_{trapped} = A_{trapped} / 4G_N$$

The trapped surface is surface whose null normals all propagate inward.

S. W. Hawking and D. Page, Thermodynamics Of Black Holes In Anti-de Sitter Space, Commun. Math. Phys. 87 (1983) 577.

C. S. Pe, ca, J. P. S. Lemos, 9805004 [gr-qc]

- *N*=4 SYM is not QCD
- For holographic description of QCD a modified  $AdS_5$  is used to study the dependence of entropy on energy

Gursoya, Kiritsis et al.,0707.1324, 0707.1349

Early the modification of  $AdS_5$  space-time by introduction of wrapping factor was appied for shock waves with masses specially distributed.

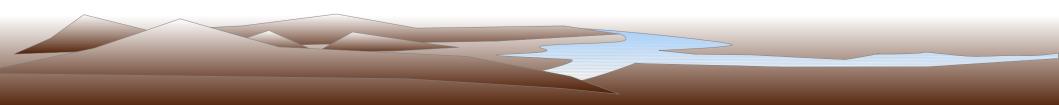
We consider wall-wall collisions with masses averaged over surfaces in the modified 5D space-time.

Kiritsis, 1111.1931

We describe heavy-ion collisions by the wall-wall shock wave collisions in  $AdS_5$  (or in its modification)

S. Lin, E. Shuryak, 1011.1918[hep-th]

I. Y. Aref'eva, A. A. Bagrov and E. O. Pozdeeva, Holographic phase diagram of quark-gluon plasma formed in heavy-ions collisions," JHEP 1205, 117 (2012)



# The Einstein equation for particle in dilaton field has the form:

$$\left(R_{\mu\nu} - \frac{g_{\mu\nu}}{2}R\right) - \frac{g_{\mu\nu}}{2}\left(-\frac{4}{3}(\partial\Phi_s)^2 + V(\Phi_s)\right) - \frac{4}{3}\partial_\mu\Phi_s\,\partial_\nu\Phi_s - g_{\mu\nu}\frac{d(d-1)}{2L^2} = 8\pi G_5 J_{\mu\nu},$$

where  $J_{++} = \frac{E}{b^3(z)} \,\delta(x^1) \delta(x^2) \delta(z - z_*) \delta(x^+).$ 

Shock wave metric modified by wrapping factor

$$ds^{2} = b^{2}(z) \left( dz^{2} + dx^{i} dx^{i} - dx^{+} dx^{-} + \phi(z, x^{1}, x^{2}) \delta(x^{+}) (dx^{+})^{2} \right)$$

Aref'eva I.Ya. 0912.5482[hep-th]

M. Hotta, M. Tanaka, Shock-wave geometry with nonvanishing cosmological constant, Class. Quantum Grav. **10**, 307, 1993

Using shock ansatz we reduce the Einstein equation to the differential equation for shock wave profile and two equations defining the connection of field and field potential with b-factor:

$$\left(\partial_{x^{1}}^{2} + \partial_{x^{2}}^{2} + \partial_{z}^{2} + \frac{3b'}{b}\partial_{z}\right)\phi(z, x_{\perp}) = -16\pi G_{5}\frac{E}{b^{3}}\delta(x^{1})\delta(x^{2})\delta(z^{2} + z)$$

$$V(\Phi_{s}) = \frac{3}{b^{2}}\left(\frac{b''}{b} + \frac{2(b')^{2}}{b^{2}} - \frac{4b^{2}}{L^{2}}\right) \qquad \Phi_{s}' = \pm \frac{3}{2}\sqrt{\left(\frac{2(b')^{2}}{b^{2}} - \frac{b''}{b}\right)}$$

The most interesting case is the collision of flat objects with masses uniformly distributed

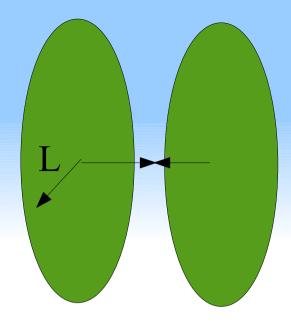
The equation corresponding to the domain profile with mass distributed over the domain wall

$$\left(\partial_z^2 + 3\frac{b'}{b}\partial_z\right)\phi^W(z) = -16\pi G_5 \frac{E}{b^3}\delta(z_* - z)$$

and equation corresponding to the domain profile with mass distributed over the finite region with radius L

$$\left(\partial_z^2 + \frac{3b'}{b}\partial_z\right)\phi^w(z) = -16\pi G_5 \frac{E^*}{b^3}\delta(z_* - z), \qquad E^* = \frac{E}{L^2}$$

coincide up to a constant factor  $L^2$ 



The solutions to equations with evenly distributed mass under finite and infinite surfaces coincide up to constant  $L^2$ 

$$\phi^w(z) = \frac{\phi^W(z)}{L^2}$$

We identify the black hole creation with trapped surface formation. The formation conditions are applied to schock wall wave profile at the trapped surface boundary points

$$\left(\partial_z \phi^w\right)^2 \big|_{TS} = 4$$

The trapped surface area is calculated as follows

$$S_{trap} = \frac{1}{2G_5} \int_C \sqrt{\det|g_{AdS_3}|} dz d^2 x_\perp$$

where det  $|g_{AdS_3}|$  is the metric determinant of  $AdS_3$ 

The relative area *s* dened with the formula

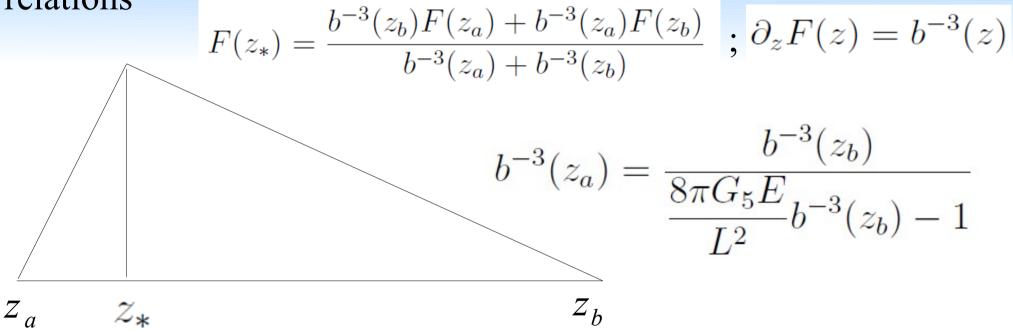
$$s = \frac{S_{trap}}{\int d^2 x_\perp}$$

We modify AdS space-time using 4 wrapping factors types

$$b = \left(\frac{L}{z - z_0}\right)^a \qquad b = \frac{L}{z} \exp\left(-\frac{z^2}{R^2}\right)$$
$$b = \exp\left(-\frac{z}{R}\right) \qquad b = \left(\frac{L}{z}\right)^a \exp\left(-\frac{z^2}{R^2}\right)$$

where a>0, R=1 fm,  $L \approx 4.4$  fm

Using the solution to general form of domain equation (for any wrapping factor) and the trapped surface conditions we obtain the relations  $h^{-3}(x) E(x) + h^{-3}(x) E(x)$ 



between trapped surface boundary  $(z_a < z_b)$  points and collision point  $\mathcal{Z}_*$ 

For the wrapping factor  $b = \exp\left(-\frac{z}{R}\right)$  we have obtained

following relations between boundary points and collision point

$$Z_A = \frac{L^2}{16\pi G_5 E} \cdot \frac{Z_B}{Z_B - \frac{L^2}{16\pi G_5 E}} , \quad Z_0 = \frac{L^2}{8\pi G_5 E}$$
$$Z_0 = \exp\left(\frac{3z_*}{R}\right), \quad Z_A = \exp\left(\frac{3z_a}{R}\right), \quad Z_B = \exp\left(\frac{3z_b}{R}\right)$$

For the considered case the collision point is fixed by energy.

The relative area of trapped surface dened by

$$s = \frac{3}{2RG_5} \left( \frac{1}{\exp\left(\frac{3z_a}{R}\right)} - \frac{1}{\exp\left(\frac{3z_b}{R}\right)} \right) = \frac{3}{2RG_5} \left( \frac{1}{Z_A} - \frac{1}{Z_B} \right)$$

The maximum entropy value is obtained for  $Z_b \gg 1$ , in this approximation

$$Z_a \sim \frac{L^2}{16\pi G_5 E}, \qquad s \sim \frac{24\pi E}{RL^2}$$

The entropy dependence on energy is linear for the exponential wrapping factor

Power b-factor  $b = (L/z)^a$  gives following relative area of trapped surface

$$s = \frac{1}{2G_5(3a-1)} \left( z_A \left(\frac{L}{z_A}\right)^{3a} - z_B \left(\frac{L}{z_B}\right)^{3a} \right)$$

$$z_A = \left(\frac{z_B^{3a}}{-1 + z_B^{3a}C^2}\right)^{\frac{1}{3a}} \quad z_* = \left(\frac{z_A^{3a}z_B^{3a}(z_B + z_A)}{z_A^{3a} + z_B^{3a}}\right)^{\frac{1}{3a+1}} \quad C^2 = \frac{8\pi G_5 E}{L^{3a+2}}$$

,

The maximal entropy value will at  $Z_b \gg 1$  in assumption 3a > 1

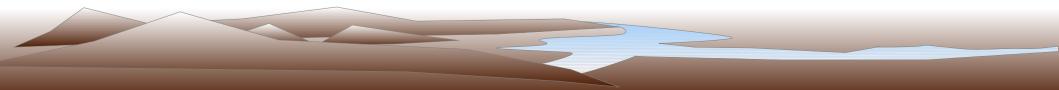
$$s \mid_{z_b \to \infty} = \frac{L^{3a}}{2G_5(3a-1)} z_A^{1-3a} = \frac{L}{2G_5} \left(\frac{8\pi G_5}{L^2}\right)^{\frac{3a-1}{3a}} E^{\frac{3a-1}{3a}}$$

For the power wrapping factor the entripy increase as  $E^{1-1/3a}$ 

The multiplicity of particles produced in collisions of heavy ions (PbPb-and AuAu-collisions) dependents on energy as  $s_{NN}^{0,15}$  ( $E^{0.3}$ ) in the range  $10-10^3$  GeV.

This model can coinside with experimental data at  $a \approx 0.47$ 

K. Aamodt et al. [ALICE Collaboration], arXiv:1011.3916 [nucl-ex].



Mixed factor of the form 
$$b = \frac{L}{z} \exp\left(-\frac{z^2}{R^2}\right)$$
 gives the another

relative area of trapped surface energy dependence

$$s = \frac{L^3}{2G_5} \left( -\frac{1}{2\exp\left(\frac{3z_b^2}{R^2}\right)z_b^2} + \frac{1}{2\exp\left(\frac{3z_a^2}{R^2}\right)z_a^2} + \frac{3\operatorname{Ei}\left(1,\frac{3z_b^2}{R^2}\right)}{2R^2} - \frac{3\operatorname{Ei}\left(1,\frac{3z_a^2}{R^2}\right)}{2R^2} \right) \right)$$

which has the maximal value at  $z_b \rightarrow \infty$ 

$$s \mid_{z_b \to \infty} = \frac{3}{4} \frac{L^3}{G_5 R^2} \left( -\text{Ei}\left(1, \frac{3z_a^2}{R^2}\right) + \frac{1}{3} \frac{R^2}{\exp\left(\frac{3z_a^2}{R^2}\right) z_a^2} \right)$$
  
and roughly is  $E^{\frac{2}{3}}(1 + 0.007 \ln \dot{E}) - 3$  at  $10 \text{GeV} \le E < 1 \text{TeV}$ 

The wrapping factor

$$b = \left(\frac{L}{z}\right)^a \exp\left(-\frac{z^2}{R^2}\right)$$

gives the most complicate relative area of trapped surface energy dependence

$$s = \frac{F(z_B) - F(z_A)}{2G_5}$$

$$F(z) = \frac{\left(\frac{L}{z}\right)^{3a} z \exp\left(-\frac{3z^2}{2R^2}\right) \left(2\left(\frac{3z^2}{R^2}\right)^{\frac{3a-1}{4}} \mathbf{M}\left(\frac{-3a+1}{4}, \frac{3(-a+1)}{4}, \frac{3z^2}{R^2}\right) + 3(1-a)\exp\left(-\frac{3z^2}{2R^2}\right)\right)}{3\left(-1+3a\right)\left(-1+a\right)}$$

$$\mathbf{M}(\mu,\nu,z) = \exp\left(-\frac{z}{2}\right) z^{\frac{1}{2}+\nu} {}_{1}F_{1}\left(\frac{1}{2}+\nu-\mu,1+2\nu,z\right)$$

Which has maximal value at  $z_B \to \infty$ :  $s \to \frac{-F(z_A)}{2G_5}$ 

The entropy can be roughly estimate at a=1/2 such as

$$S \sim E^{0.3}(1 + C_1(\ln(E + 100))) - C_2$$
  
 $C_1 = -0.738$ ,  $C_2 = 0.393$  at  $10 < E < 100$  GeV  
 $C_1 = -0.073$ ,  $C_2 = 0.827$  at  $100 < E < 1000$  GeV

#### Conclusions

The black holes formation in the domain wall-wall collisions is investigated in the deformed  $AdS_5$  with b-factors.

The several b-factor types: power, exponential and mixed are considered.

The dependence of the entropy on the energy for different b-factors is analyzed.

These results (with the account of AdS/CFT-duality) allow to simulte the multiplicity dependence on the energy of the colliding heavy-ions

$$b = (L/z)^{a}$$
,  $a \approx 0.47$ ,  $S \sim E^{0.3}$ 

(in agreement with experimental data  $s_{NN}^{0,15}$  ).

The additional logarithms appear when considering the mixed factor.