

## Studies of decelerator tolerances.

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# Content

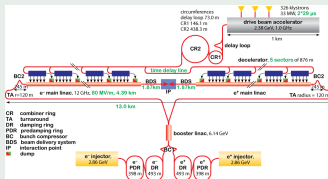
- 1 Introduction
- 2 Beam shape and width
- 3 Phase jitter
- 4 Brainstorming/Outlook

# Introduction

## Motivation

- Determine tolerances of the drive beam with respect to delivered beam from the DB complex.
- Try and inject interesting types of beams.
- Investigate "worst case" - first decelerator section.
- Main goals:
  - Keep  $3\sigma$  envelope ("the envelope") below 3mm.
  - Preserve machine efficiency.

## Layout

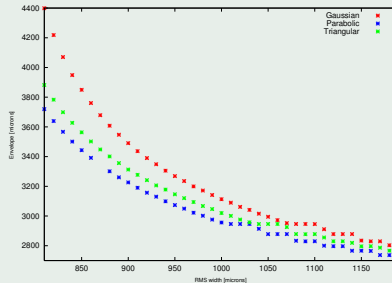


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# Beam shaping

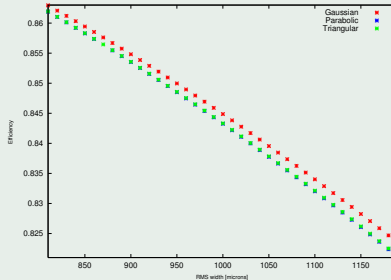
- Inject bunches of various longitudinal shapes (form factors) - vary RMS width.
- Gaussian, parabolic, triangular bunches injected. For each the charge is set to zero outside  $3\sigma$ ,  $\sqrt{5}\sigma$  and  $\sqrt{6}\sigma$ , respectively.



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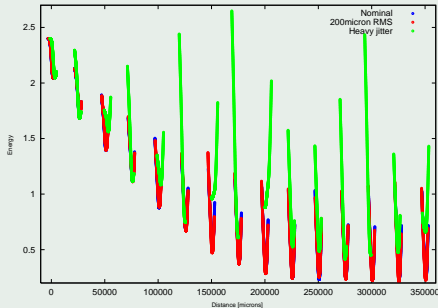
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# Starting point

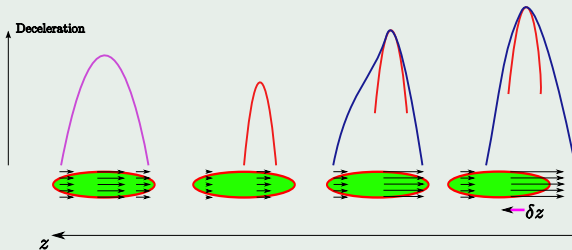
## Phase jitters

- Observation:
  - With even small longitudinal jitters ( $\sim 200\mu m$  RMS), some parts of bunches become more decelerated than nominally.
  - With very large jitters, some particles receive accelerating kicks instead of deceleration.
  - Source of **more** deceleration?



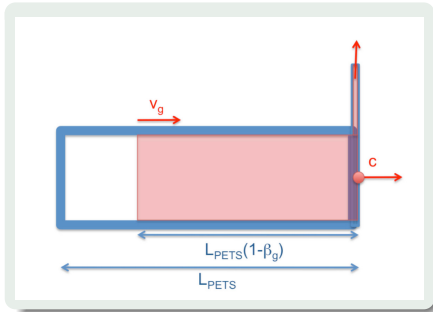


# Longitudinal wakefield



- The decelerating wake is the sum of **single-** and **multi-**bunch effects.
- The **multi-**bunch wake peaks at the center of a bunch.
- The **single-**bunch wake peaks towards the rear of the bunch.

# Longitudinal wakefield



- Three players in the wakefield:
  - 1.) Emitting slice,
  - 2.) Field, (velocity  $c\beta_g$ )
  - 3.) Pickup slice - distance  $d$  away

$$z_1(t) = ct$$

$$z_2(t) = \beta_g ct$$

$$z_3(t) = ct - d$$

$$z_2 = z_3 \Rightarrow ct_{catch-up} = d/(1 - \beta_g)$$

$$z_3 = \beta_g d/(1 - \beta_g)$$

- The trailing charge only feels the field during a distance

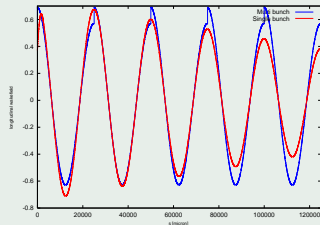
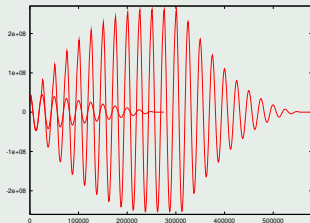
$$L_{eff} = L_{pets} - \beta_g d/(1 - \beta_g)$$

# Longitudinal wakefield

- Longitudinal wakefield for a (longitudinal delta function) charge.

$$W_l(d) \propto \begin{cases} \left( L_{pets} - \frac{\beta d}{1-\beta} \right) \cos\left(\frac{2\pi d}{\lambda}\right) & , \text{ for } [d > 0] \cap [L_{pets} - \frac{\beta d}{1-\beta}] > 0 \\ 0 & , \text{ otherwise} \end{cases}$$

- Fill time of  $\sim 10$  bunches.
- Effect of bunch  $n$  on bunch  $n + k$  decreases linearly in  $k$ .
- Distance from maximum of multi bunch wakefield to maximum of single bunch is  $1637\mu\text{m}$ .
- Expect  $7\%$  extra deceleration from a bunch displaced by that amount from field calculation.

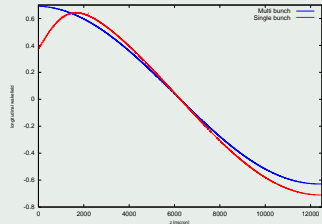
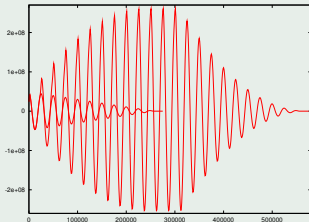


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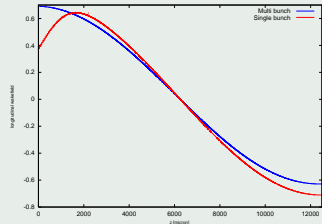
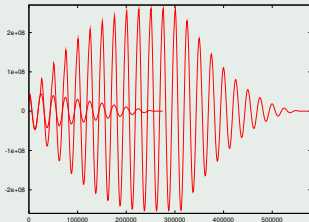


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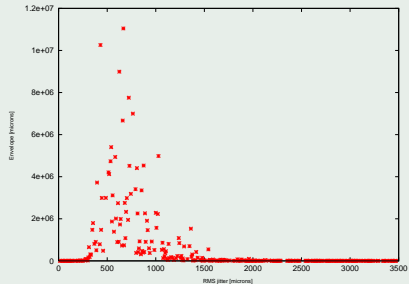
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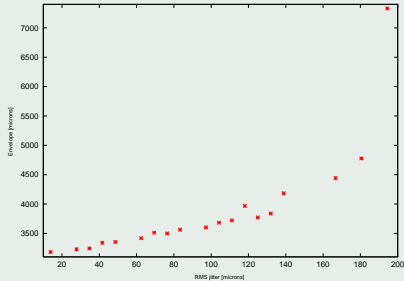


- The envelope of the beam blows up for phase-jittered beams - up to unphysical "meter-scales".
- Even with small jitters, the envelope is unacceptable.
- It is confirmed that the excess deceleration is constant throughout the machine - and in the range 0-3.5%.
- Some jitters are worse than others - 400-1000 $\mu\text{m}$ . above that magnitude of jitter, decoherence of the wake occurs.
- How about "freak" bunches - bunches that have got very large displacements?



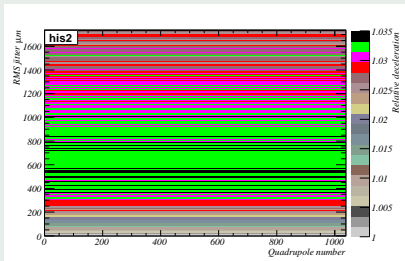
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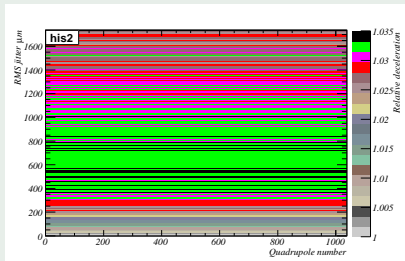
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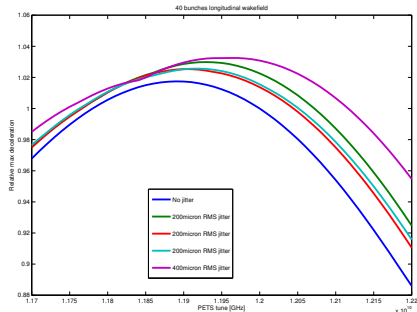
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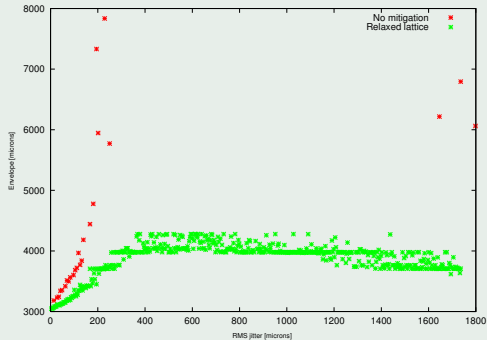
# Detuning the cavities?

- Try to detune the cavities away from (towards?) the wakefield enhancement.
- Observe the maximum field.
- Detuning does not decrease sensitivity to jitter (possibly even worse).
- The effect of detuning on machine efficiency has not been studied.



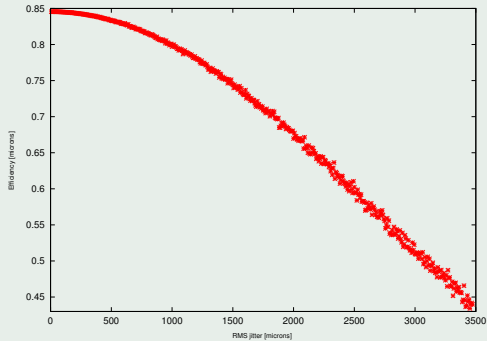
# Tapering the lattice

- Relaxing the quadrupole gradient towards the end of the lattice helps.
- This is very preliminary, and can certainly be optimized further.



# Efficiencies

- Efficiency:  $\eta = \frac{E_0 - \frac{\sum_i E_i N_i}{\sum_i N_i}}{E_0}$  -  $E_i, N_i$  measured at the end of decelerator.
- With relatively small changes in efficiency, very large changes in envelope (with nominal lattice) can occur.



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## Further studies

- Extract info from CTF3 on phase jitter/bunch shape?
- More work for the “worst case” displacement ( $1637\mu\text{m}$ ).
- More work on optimizing the lattice to cope with jitter and longitudinal displacement.
- Need to optimize parameters with a constraint on the machine efficiency.
- Additional understanding of the interplay between detuning and phase jitter.
- Optimization for “worst case” is worse than for jitters: 3.5% extra deceleration  $\rightarrow$   $\sim 7\%$  extra deceleration. Can “worst case” occur?