

NLO QCD Predictions for Vector-Boson Production

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ZPW 2013: Particle Physics in the LHC Era



Outline

1. Introduction
2. Setup of NLO QCD
Computation
3. W/Z +jets results
4. Summary

Introduction

Physics Motivation

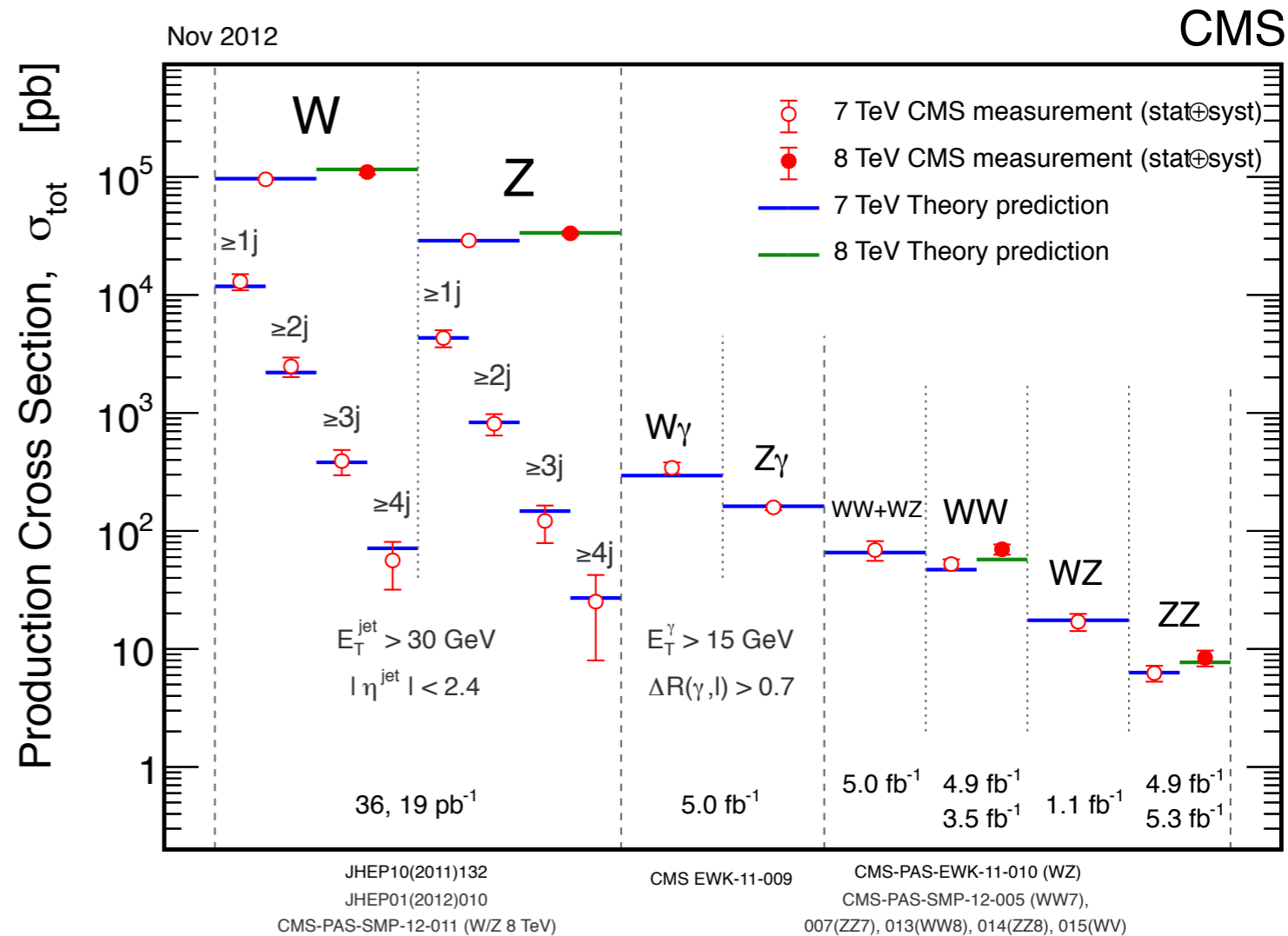
High-multiplicity events common @ LHC.

W/Z+n-jets:

- *test of perturbative QCD*
- *significant background (BSM, tt, Higgs)*

Many interesting observables:

- *jet-production ratios, conversion factors, jet substructure (see talk by D.Kosower)*

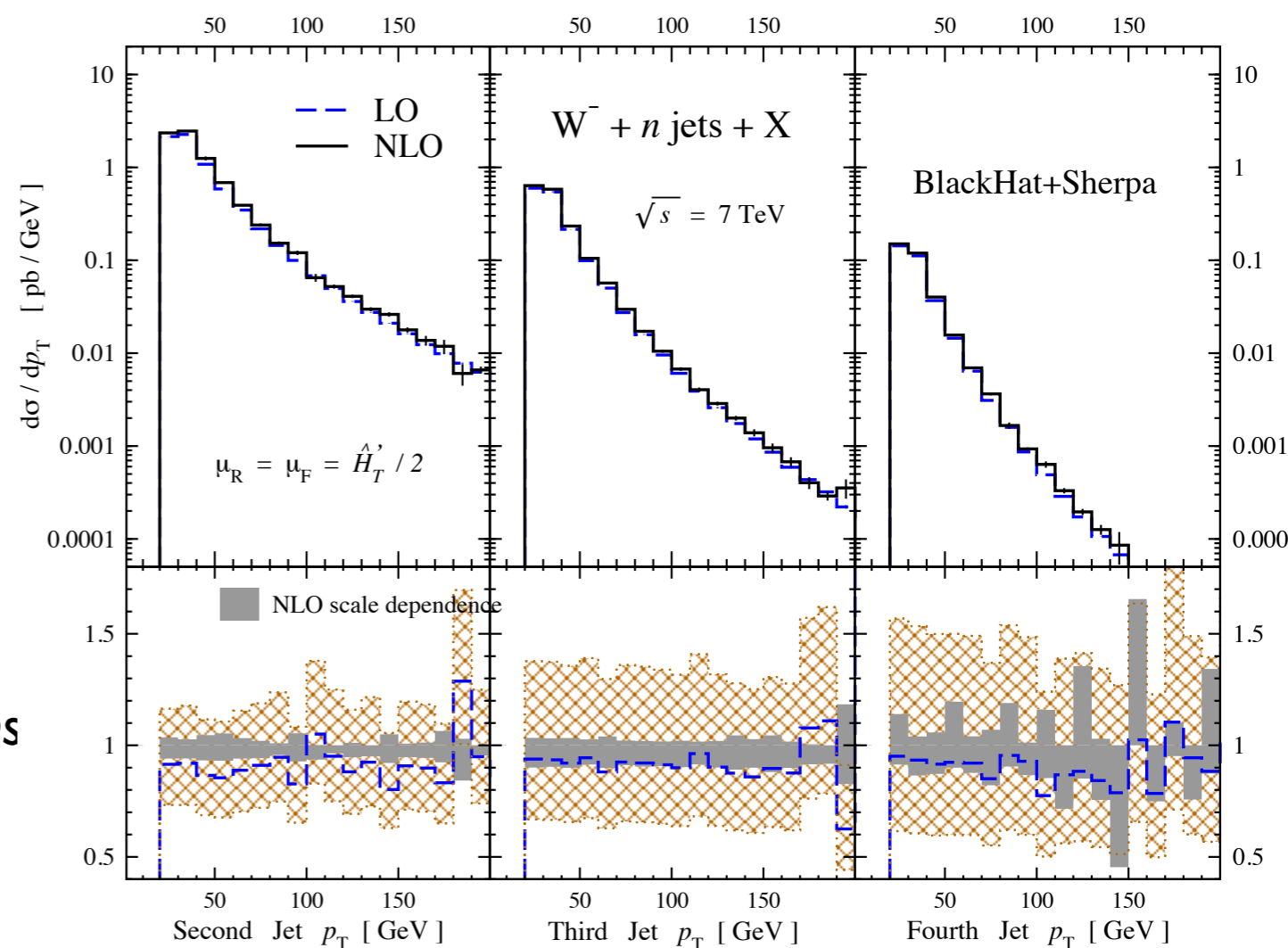


Impact of Precision Theory

Consider here parton-level @ NLO:

- Normalizations & shapes of cross sections:
 - *Large multiplicity \Rightarrow high powers of strong coupling*
 - *unphysical renormalization-scale dependence stabilizes at NLO*
- Inclusion of QCD effects: *multiple partons merged into jets, initial state radiation*
- Important ingredient for NLO parton shower

[BlackHat I | 09.6527]



BlackHat: Recent Progress

Pushed state-of-the-art in precision QCD:

- $pp \rightarrow W/Z/\gamma+4\text{-jets}$ and presently $W+5\text{jets}$ [BlackHat:1108.2229, 1009.2338]
- $pp \rightarrow 4\text{-jets}$ (see also talk by S.Badger) [BlackHat:1112.3940; Badger, Biedermann, Uwer, Yundin 1209.0100]

Automated methods for dealing with **color** d.o.f. [HI, Ozeren: 1111.4193]

Dissemination of results:

- Helped CMS experimenters with **supersymmetry search** [CMS-PAS-SUS-08-002 & 10-005; BlackHat 1206.6064 & 1106.1423]
- n-tuple **event files** (used by ATLAS) [ATLAS: 1111.2690 & 1201.1276]

Public BlackHat (manual on hepforge) for:

- $pp \rightarrow W/Z/\gamma+(n\leq 3)\text{-jets}$ and $pp \rightarrow (n\leq 4)\text{jets}$

Setup of NLO QCD Computation

BlackHat + Sherpa collaboration

Fixed-order parton-level cross section @ NLO:

$$\sigma_n^{NLO} = \int_{n+1} (d\sigma_n^{real} - d\sigma_{n+1}^{sub}) + \int_n (d\sigma_n^{virtual} + d\Sigma_n^{sub}) + \int_n d\sigma_n^{born}$$

The diagram shows the equation for the NLO cross section. Below the equation, the names 'BlackHat' and 'Sherpa' are written in blue and red respectively. Blue arrows point from 'BlackHat' to the terms $\int_n (d\sigma_n^{virtual} + d\Sigma_n^{sub})$ and $\int_n d\sigma_n^{born}$. Red arrows point from 'Sherpa' to the terms $\int_{n+1} (d\sigma_n^{real} - d\sigma_{n+1}^{sub})$ and $\int_n d\sigma_n^{born}$.

Loop-matrix-element generator:

- *BlackHat* [Berger, Bern, Dixon, Febres Cordero, Forde, Hl, Maitre, Kosower, Ozeren]

Tree-matrix-element generators:

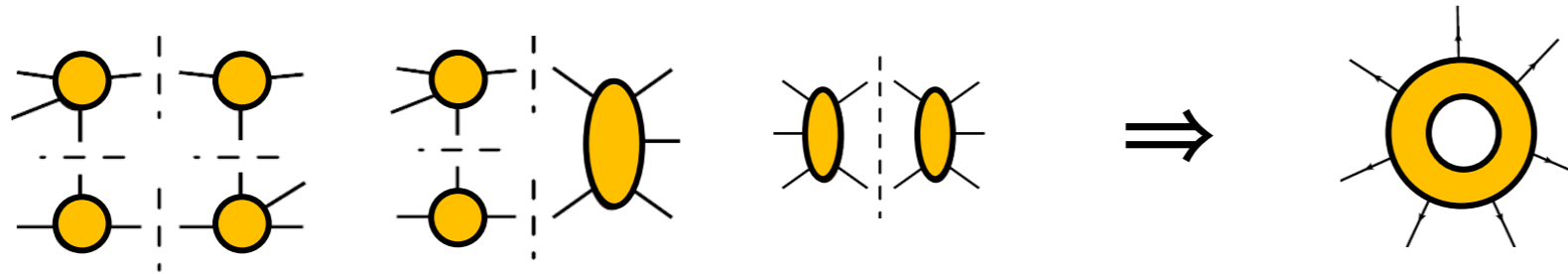
- *AMEGIC* (Feynman diagram based), *COMIX* (color flow + Berends Giele recursion)
- *BlackHat* (on-shell methods & N=4 inspired)

Soft & collinear singularities:

- *dipole subtraction formalism* [Catani, Seymour '96; Dittmaier '99; Phaf, Weinzierl '01; Catani, Dittmaier, Seymour, Trocsanyi '02]
- *implementations: AMEGIC* [Gleisberg, Krauss] and *COMIX* [Hoeche]

Sherpa's multi-channel integration and analysis framework; BlackHat n-tuple analysis

On-shell Methods



Key features:

- multiplicity independent setup
- on-shell tree amplitudes as input
- numerically stable

For details see recent reviews: [Britto '11; H1 '11; Ellis, Kunszt, Melnikov, Zanderighi '11]

- Tensor reduction with on-shell loop momenta: [Ossola, Papadopoulos, Pittau; Harmeren]
- Unitarity methods: [Bern, Dixon, Kosower; Britto, Cachazo, Feng; Ellis, Giele, Kunszt, Melnikov]
- Recursive on-shell methods for loops: [Berger, Bern, Dixon, Febres-Cordero, Forde, H1, Kosower, Maitre]
- Numerical unitarity methods: [Berger, Bern, Dixon, Febres-Cordero, Forde, H1, Kosower, Maitre; Ossola, Papadopoulos, Pittau, Hameren; Giele, Kunszt, Melnikov]

BlackHat-library

[Berger, Bern, Dixon, Forde, Febres Cordero, HI, Kosower, Maitre, Ozeren]

Tree & loop matrix-element generator

Aim: computation of multi-leg loop matrix elements

Key: New field-theory methods important for LHC phenomenology @ LHC; these provide efficiency and numerical stability

Further recent programs giving collider cross sections:

- Helac-NLO: Bevilacqua, Czakon, Hameren, Ossola, Papadopoulos, Pittau, Worek
- Rocket+MCFM: Ellis, Giele, Kunszt, Melnikov, Zanderighi
- MadLoop: Hirchi, Maltoni, Frixione, Frederix, Garzelli, Pittau
- GoSam & Samurai: Cullen, Greiner, Heinrich, Luisoni, Mastrolia, Ossola, Reiter, Tramontano
- NJet: Badger, Biedermann, Uwer, Yundin
- OpenLoops: Cascioli, Maierhofer, Pozzorini
- Recola: Actis, Denner, Hofer, Scharf, Uccirati

BlackHat: Loop Setup

Express loop-matrix elements in terms of **primitive loop amplitudes**:

$$\mathcal{A}^{1\text{-loop}} = \sum_{\text{color traces } \rho} C_{\rho}[(T^a)^j_{\bar{k}}] \mathcal{A}_{\rho}^{\text{partial}} \quad \begin{array}{l} \text{L} \\ \text{blue arrow} \end{array} \quad \sum_{\text{ordered amplitudes } \sigma} g_{\rho\sigma}(N_c, N_f) \mathcal{A}_{\sigma}^{\text{primitive}}$$

Key features:

- explicit color dependence exposed \Rightarrow color expansion in powers of $(1/N_c)$
- primitive amplitude contain gauge invariant subset of Feynman diagrams

Convenient for on-shell methods:

- depend on ordered kinematic variables; s_{12} , s_{123} **but not** s_{13} , s_{134} \Rightarrow simplifies on-shell methods
- fine division into physical objects \Rightarrow excellent control over numerical stability

BlackHat: Color

Needed: **partial** loop amplitudes in terms of **primitive** amplitudes

$$A_\rho^{\text{partial}} = \sum_{\text{ordered amplitudes } \sigma} g_{\rho\sigma}(N_c, N_f) A_\sigma^{\text{primitive}}$$

Decompositions have been well known for some amplitudes:

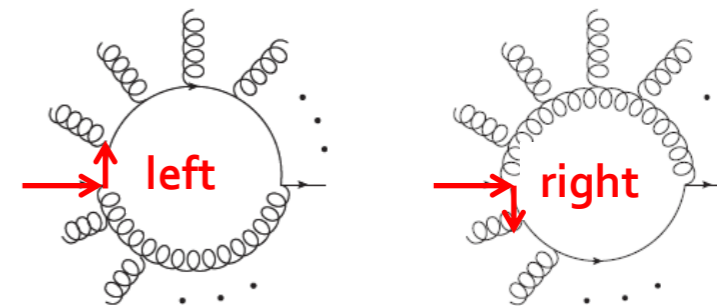
- n-gluons, 2-quarks & n-gluons, 4-quarks [Bern, Kosower '91; Kunszt Signer, Trocsanyi '94; Bern, Dixon, Kosower '94; Bern, Dixon, Kosower, Weinzierl '96]
- 4-quark & 1-gluon [Ellis, Giele, Kunszt, Melnikov, Zanderighi '08]; see also review by [Ellis, Kunszt, Melnikov, Zanderighi '11].

Explicit expressions given for various quark and gluon amplitudes [H1, Ozeren: 1111.4193]

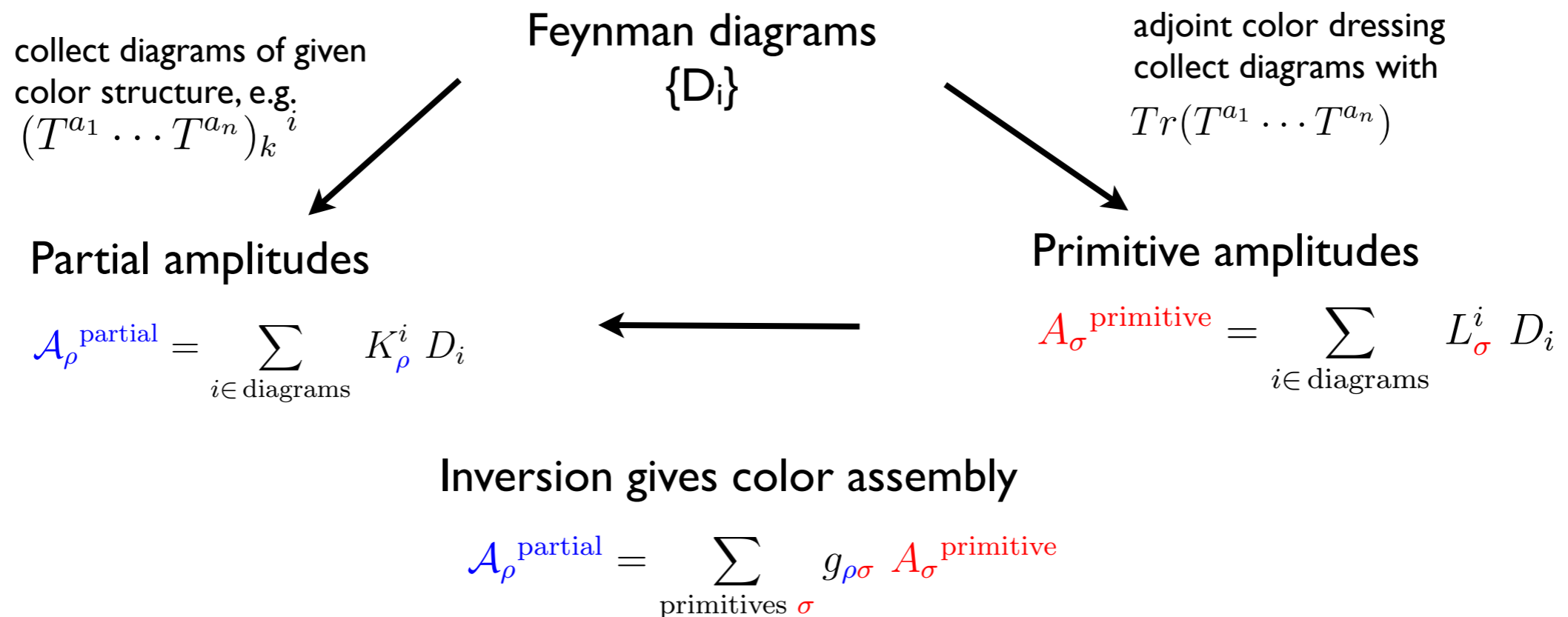
BlackHat: Color

Primitive amplitudes [Bern, Dixon, Kosower '94]:

- Ordered amplitudes (as for adjoint fermions and gluons)
- Further split up into **left-turners** and **right-turners**. Following fermion as it moves towards loop.



Color algorithm: [HI, Ozeren: 1111.4193]

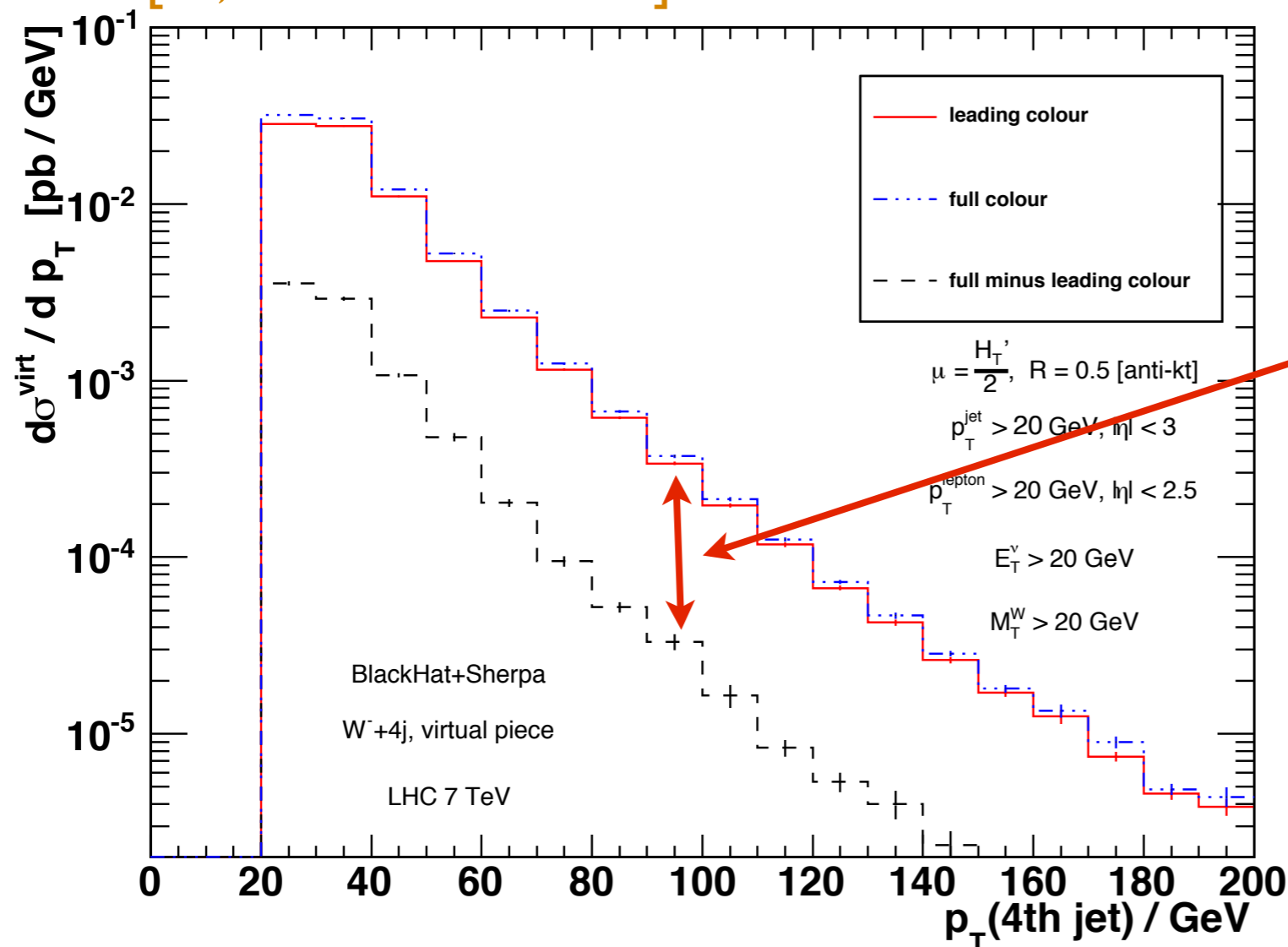


BlackHat: Color - W+4jets

Color organization in powers of $(1/N_c)$ useful for efficiency:

- mostly evaluate bigger, leading-color contributions
- reduced number of evaluations of demanding sub-leading color terms

[HI, Ozeren: 1111.4193]

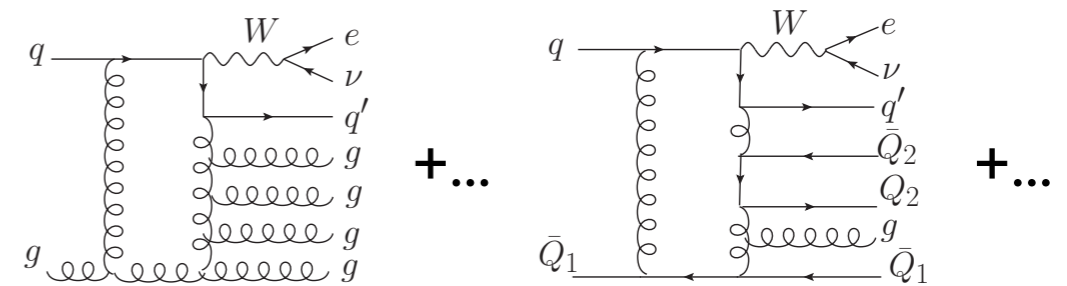
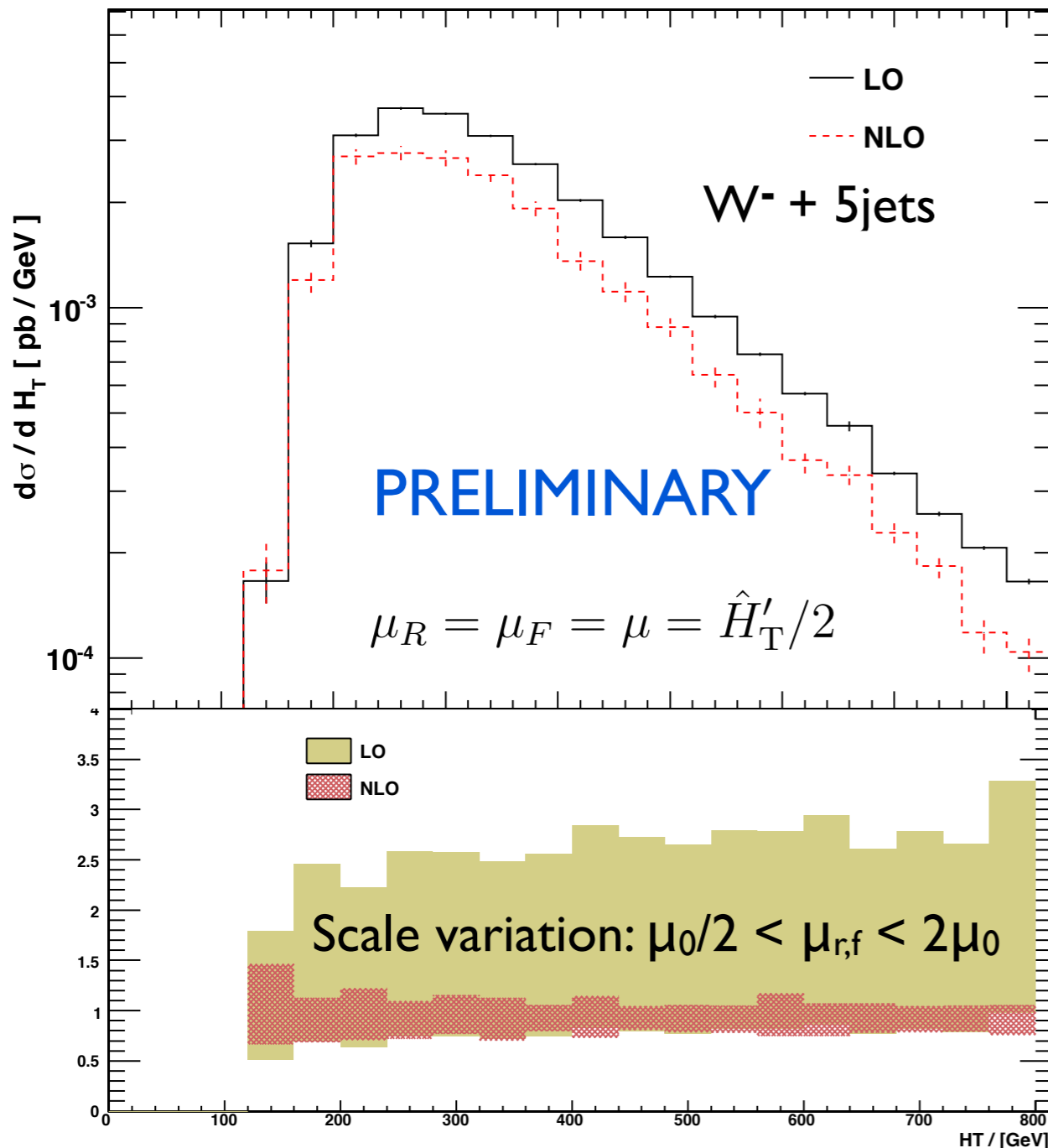


- confirm expected $(1/N_c)^2$ suppression
- leading-color approximation excellent in bulk of distribution

BlackHat: $W+5$ -jets - Work in Progress

Bern, Dixon, Febres Cordero, Hoeche, HI, Kosower, Maitre, Ozeren

First NLO QCD $2 \rightarrow 6$ process @ LHC.



Leading-color approximation of virtual part. Good to about 3% based on $W+(n \leq 4)$ -jet experience.

Scale variation reduction:

- 50% @ LO \rightarrow 15% @ NLO

BlackHat: Public Event Files - Work in Progress

Bern, Dixon, Febres
Cordero, Hoeche, Hl,
Kosower, Maitre, Ozeren

Public event files: $pp \rightarrow W/Z/\gamma + n\text{-jets}$, $n\text{-jets}$ with ($n \leq 4$) @ NLO

Event files: Standardized ROOT-format n-tuples for NLO fixed order predictions. (Can be generated by Sherpa.)

Analysis library: used to change renormalization and factorization scale setting and PDFs of events.

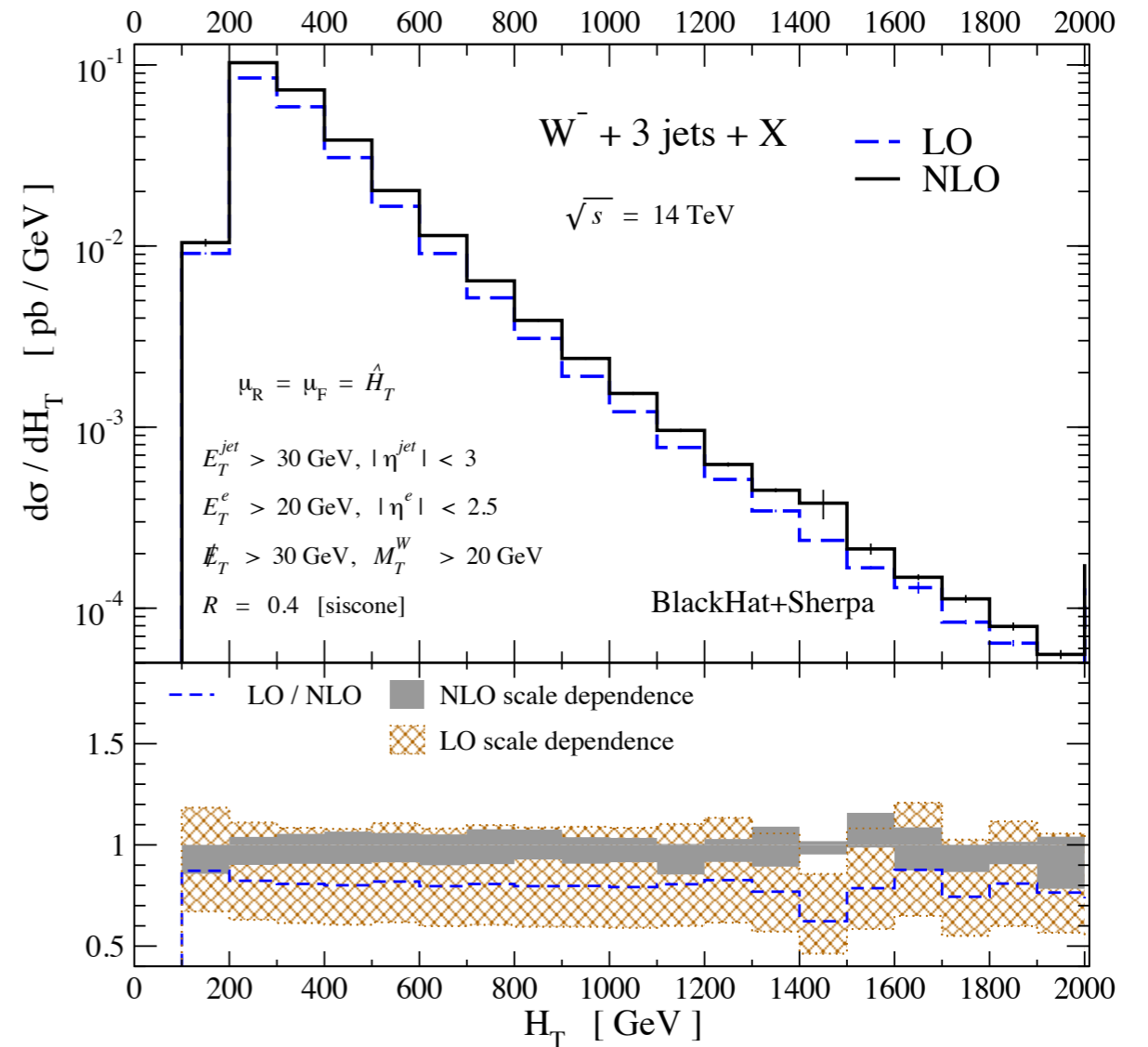
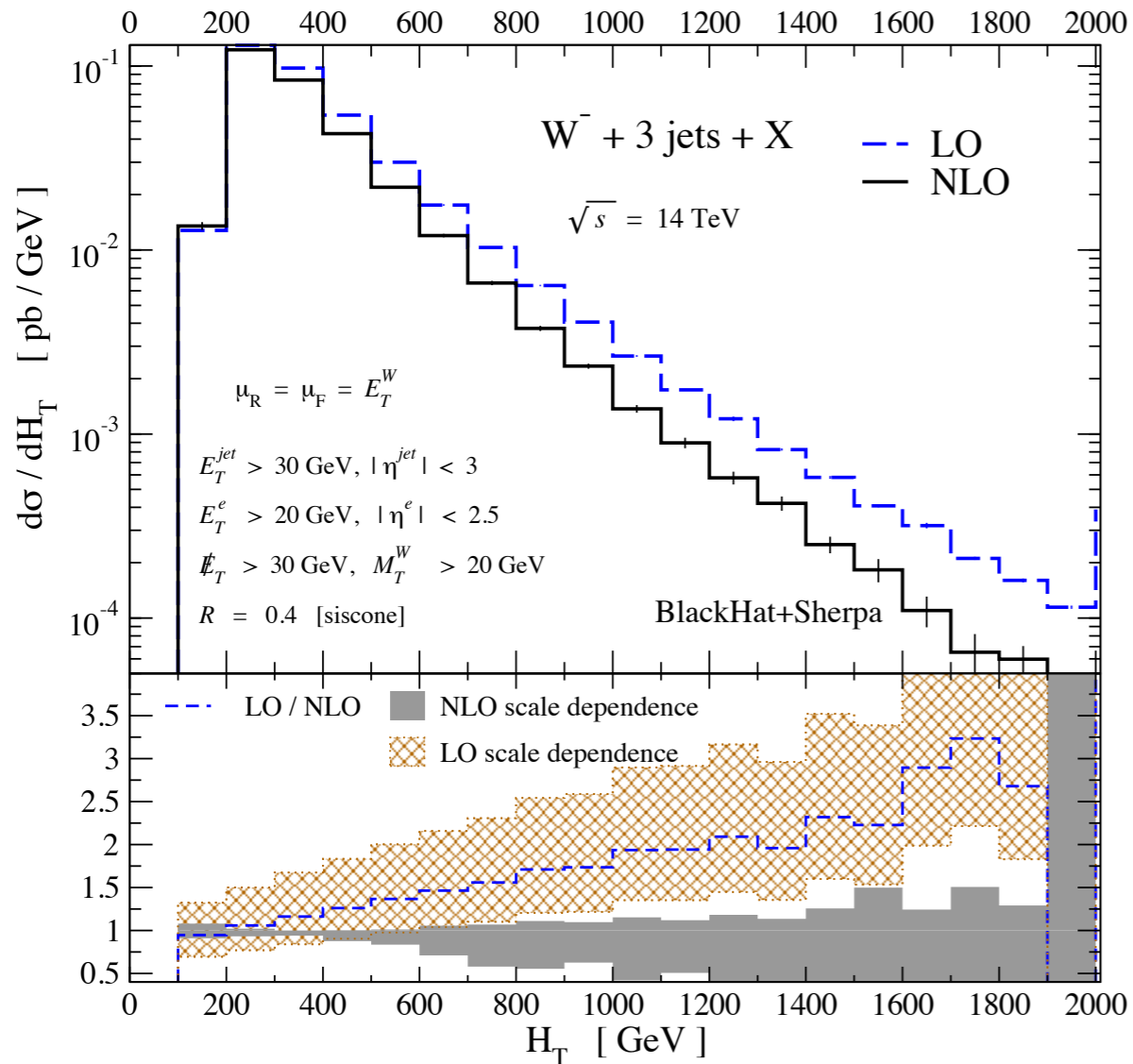
Key features of n-tuple approach:

- makes available NLO results to experimenters (used by ATLAS in [1111.2690 & 1201.1276])
- change scales and PDFs cheaply (without re-evaluating real/loop/born parts and dipole-terms)
- tighten cuts and study new distributions

WIZ-results

Renormalization Scale

[BlackHat: 0907.1984]

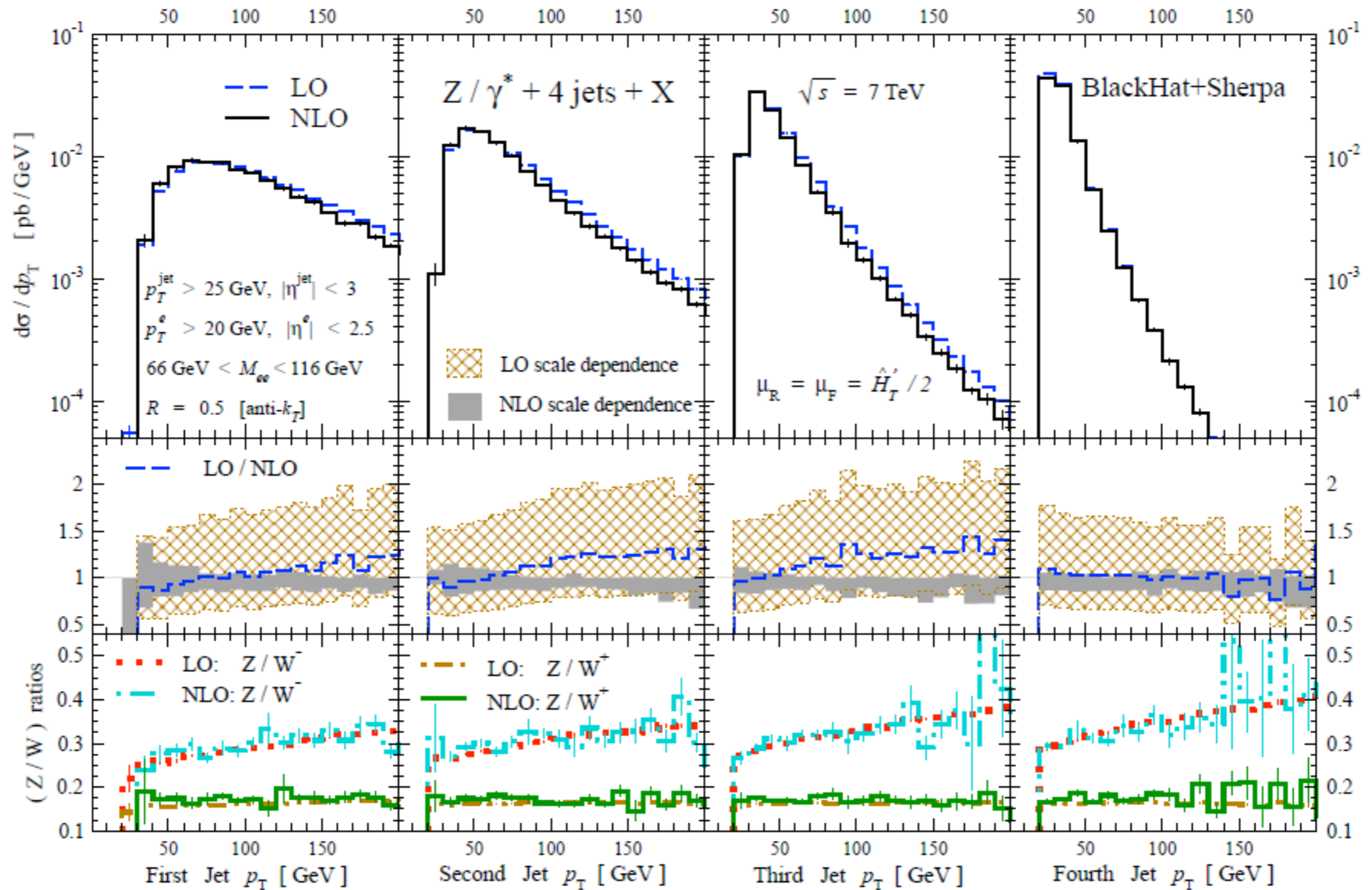


$$\mu = E_T^W \equiv \sqrt{M_W^2 + p_T^2(W)}$$

$$\mu = \hat{H}_T = \sum_p E_T^p + E_T^e + E_T^\nu$$

W/Z+jets @ NLO

[BlackHat: 1108.2229]



Jet-Parameter Dependence

anti-kt, R=0.5

[BlackHat 1090.2338]

no. jets	W^- LO	W^- NLO
0	1614.0(0.5) ^{+208.5} _{-235.2}	2077(2) ⁺⁴⁰ ₋₃₁
1	264.4(0.2) ^{+22.6} _{-21.4}	331(1) ⁺¹⁵ ₋₁₂
2	73.14(0.09) ^{+20.81} _{-14.92}	78.1(0.5) ^{+1.5} _{-4.1}
3	17.22(0.03) ^{+8.07} _{-4.95}	16.9(0.1) ^{+0.2} _{-1.3}
4	3.81(0.01) ^{+2.44} _{-1.34}	3.55(0.04) ^{+0.08} _{-0.30}

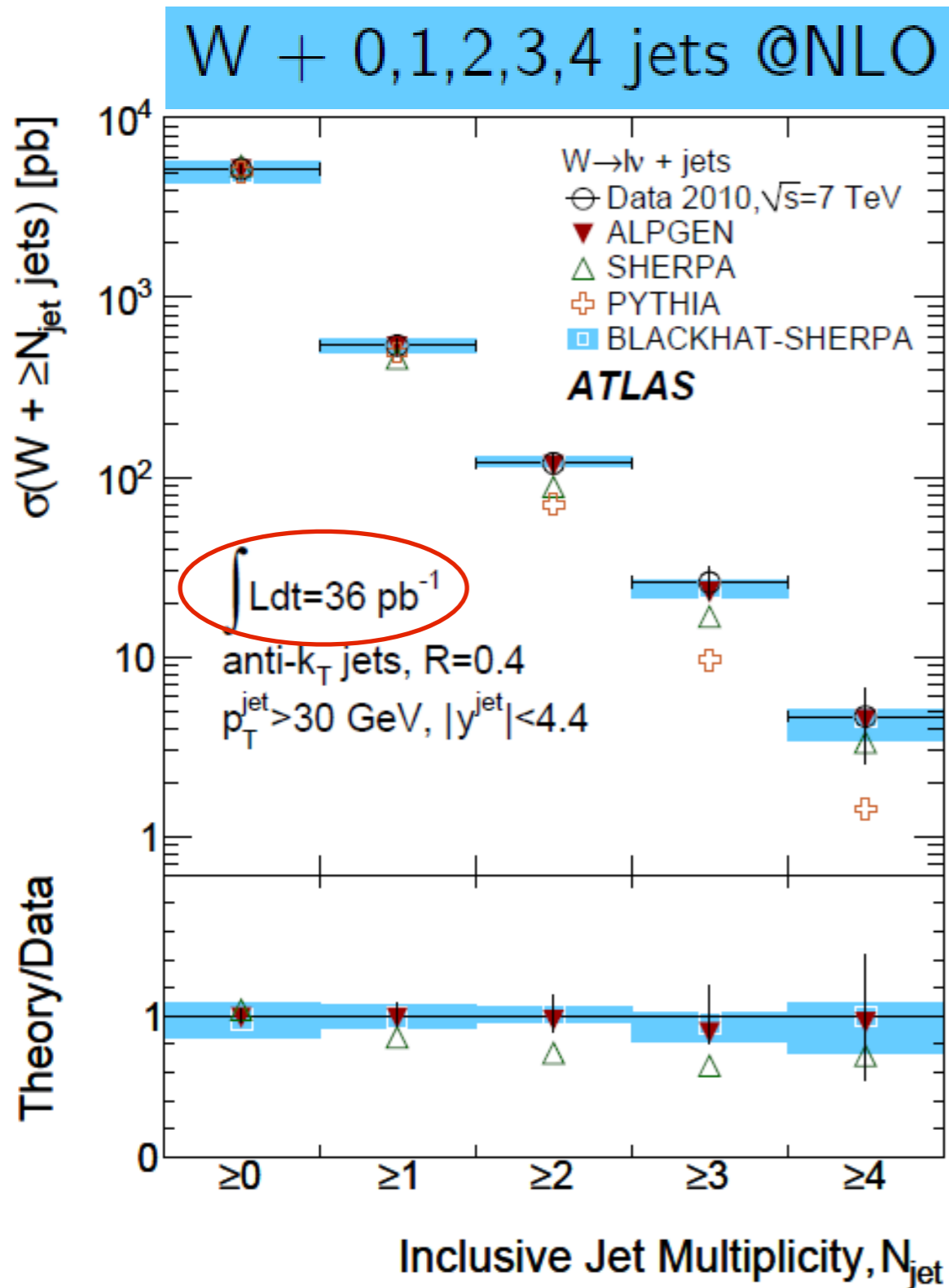
NLO decreasing

anti-kt, R=0.4

LO increasing

no. jets	W^- LO	W^- NLO
0	1614.0(0.5) ^{+208.5} _{-235.2}	2077(2) ⁺⁴⁰ ₋₃₁
1	264.4(0.2) ^{+22.6} _{-21.4}	324(1) ⁺¹⁴ ₋₁₁
2	74.17(0.09) ^{+21.08} _{-15.12}	76.2(0.5) ^{+0.8} _{-3.4}
3	18.42(0.03) ^{+8.61} _{-5.29}	17.0(0.1) ^{+0.0} _{-1.0}
4	4.41(0.01) ^{+2.82} _{-1.55}	3.81(0.04) ^{+0.00} _{-0.44}

ATLAS Comparison



Data: [ATLAS I201.I276]

Theory: [BlackHat I090.2338]

Excellent agreement between data and theory.

Particle level; $\sim 3\%$ non-perturbative corrections included by ATLAS.

Theory limited by scale dependence ($< 15\%$).
 Data limited by JES uncertainty ($< 30\%$).

New methods work!

Conclusions

- New theory developments in order to deal with color d.o.f in QCD. Automated sub-leading color of one-loop matrix elements in BlackHat.
- Discussed recent NLO computations in NLO QCD: **Z+4 jets, W+4/5-jets.**
- Precision theory can play a central role in order to fully exploit the LHC potential.
- Recently made BlackHat matrix elements publicly available to experimenters.
- Advertised n-tuple event files.

Thanks.

