

“My quark is heavier than your quark”

Gert Aarts

FASTSUM collaboration



Swansea University  
Prifysgol Abertawe

# Outline

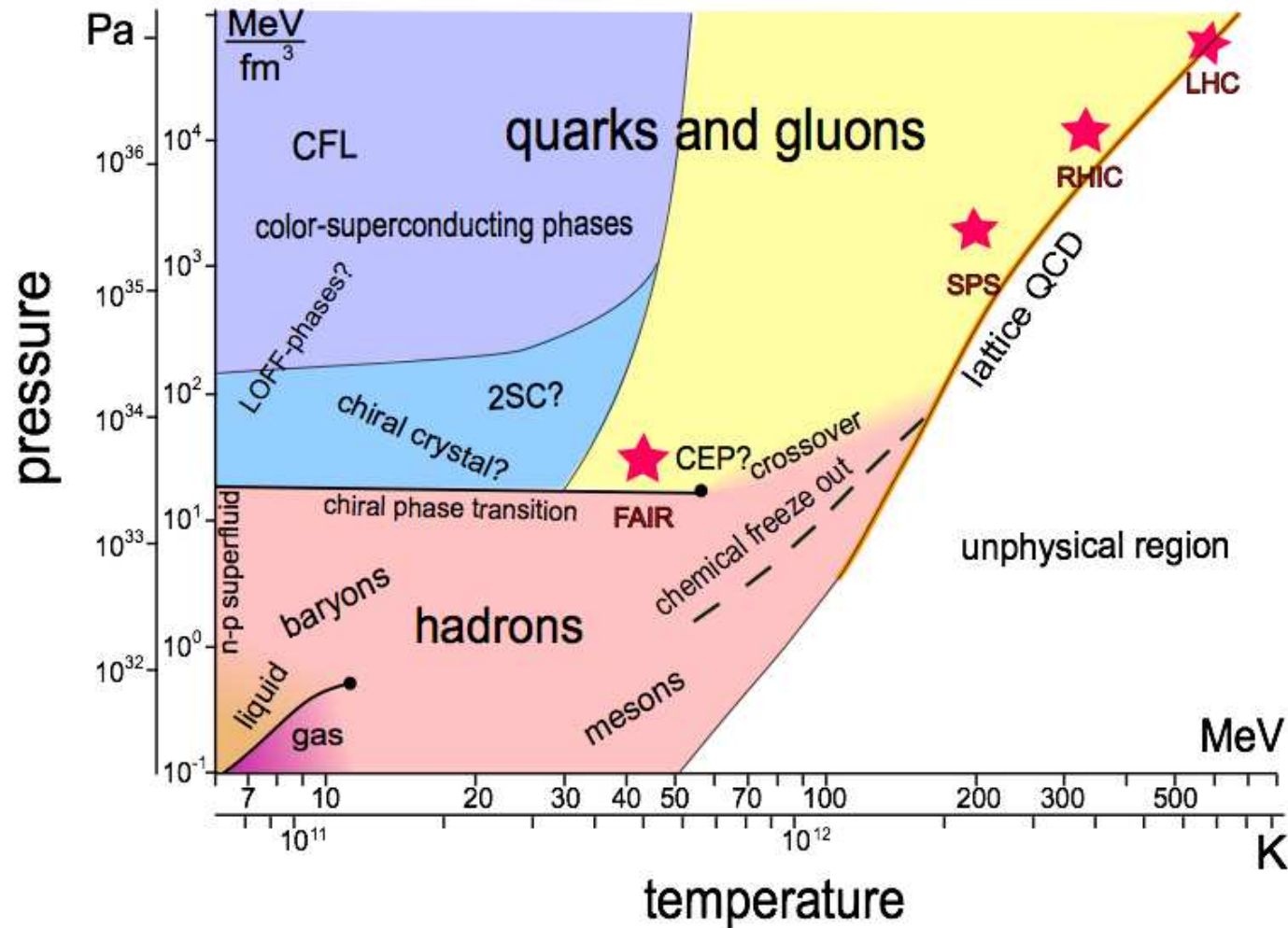
- introduction: why are we here? what is our purpose?
- bottomonium on the lattice
- bottomonium spectral functions in the QGP
  - S waves:  $\Upsilon$  at rest, moving
  - P waves:  $\chi_{b1}$  melting
- conclusion

# QCD phase diagram

- since this is the first talk, there is a moral obligation to show the QCD phase diagram

# QCD phase diagram

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# Quarkonia and the QGP

quarkonia as a thermometer for the quark-gluon plasma

Matsui & Satz 86

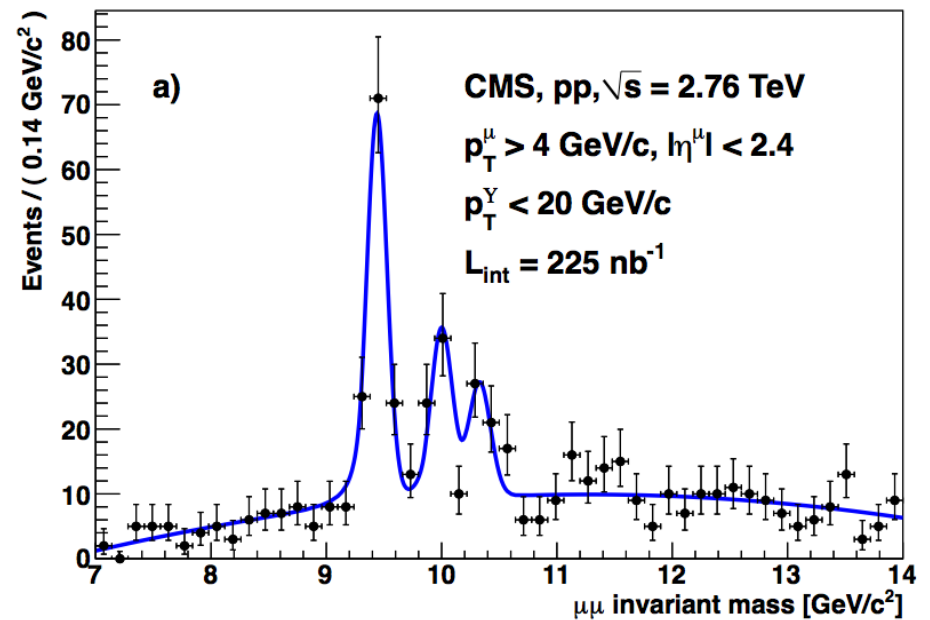
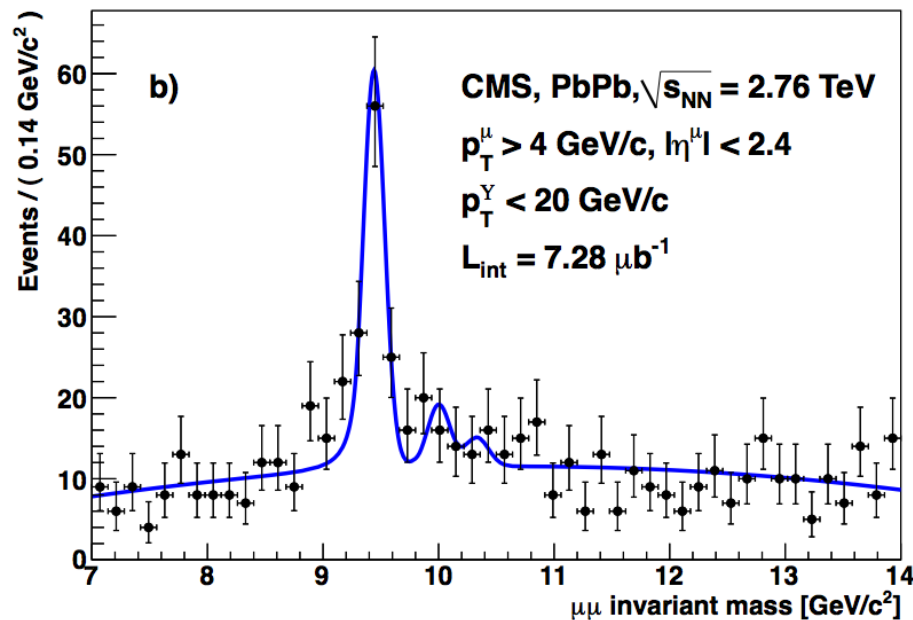
- tightly bound states of charm quarks ( $J/\psi, \dots$ ) or bottom quarks ( $\Upsilon, \dots$ ) survive to higher temperatures
- broader states melt at lower temperatures

melting pattern informs about temperature of the QGP

- relevant for heavy-ion collisions
- quantitative predictions required

# Quarkonia and the QGP

- CMS results at the LHC:  $\Upsilon$  spectrum
- compare PbPb collisions (left) and pp collisions (right)



- $\Upsilon(1S)$  survives –  $\Upsilon(2S,3S)$  suppressed
- sequential melting

# Quarkonia and the QGP

how to find the response of quarkonia to the QGP?

- potential models
- lattice QCD

at  $T > 0$ :

- plethora of potential models: (seemingly) conflicting results
- interpretation of lattice correlators hindered by thermal (periodic) boundary conditions

re-addressed recently using first-principle approach:

- effective field theories (EFTs) and separation of scales

# Quarkonia and EFTs

$$M \gg T > \dots$$

hierarchy of scales:

- heavy quark mass  $M$
- temperature  $T$
- inverse size  $g^2 M$
- Debye mass  $gT$
- binding energy  $g^4 M$

|  
→ weak coupling

corresponding EFTs:

- NRQCD
- NRQCD + HTL
- pNRQCD
- pNRQCD + HTL
- ...

Laine, Philipsen, Romatschke & Tassler 07

Laine 07-08 Burnier, Laine & Vepsäläinen 08-09

Beraudo, Blaizot & Ratti 08 Escobedo & Soto 08

Brambilla, Ghiglieri, Vairo & Petreczky 08

Brambilla, Escobedo, Ghiglieri, Soto & Vairo 10

Escobedo, Soto & Mannarelli 11

...



# Quarkonia and EFTs

$$M \gg T > \dots$$

some perturbative results (assuming  $\alpha \ll 1$ ):

- potential obtains an imaginary part

Laine, Philipsen, Romatschke & Tassler

- thermal corrections to energy and width

Brambilla, Escobedo, Ghiglieri, Soto & Vairo

- use complex potential models

Laine et al, Strickland et al, Miao, Mocsy & Petreczky, ...

solve EFT nonperturbatively: lattice QCD

bottomonium:  $M_b \sim 4.5 \text{ GeV}$        $T \sim 150 - 400 \text{ MeV}$

use of NRQCD very well motivated

# Bottomonium in the QGP

FASTSUM COLLABORATION



Don  
Sinclair



Sinead  
Ryan



Jonivar  
Skullerud



Bugra  
Oktay



Maria-Paola  
Lombardo



GA



Seyong  
Kim



Chris  
Allton

PRL (2011), JHEP (2011, 2013), in preparation

# Lattice QCD

- QGP with two light flavours (Wilson-like)
- many time slices: highly anisotropic lattices ( $a_s/a_\tau = 6$ )
- lattice spacing:  $a_\tau^{-1} \simeq 7.35$  GeV,  $a_s \simeq 0.162$  fm
- lattice size:  $12^3 \times N_\tau$

$N_\tau$	80	32	28	24	20	18	16
$T/T_c$	0.42	1.05	1.20	1.40	1.68	1.86	2.09
$N_{\text{cfg}}$	250	1000	1000	500	1000	1000	1000

- bottom quark: NRQCD

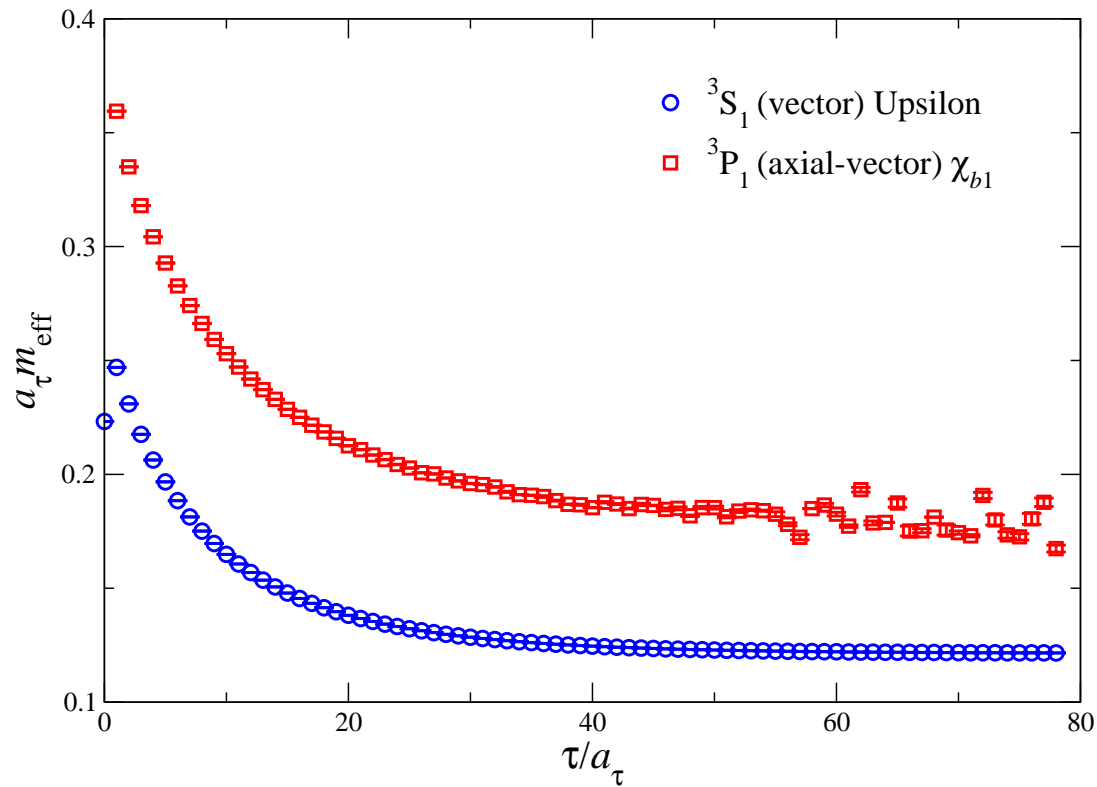
mean-field improved action with tree-level coefficients, including up to  $\mathcal{O}(v^4)$  terms

Davies et al 94

- see other FASTSUM talks for  $N_f = 2 + 1$  results

# Spectrum

- exponential decay  $G(\tau) \sim \exp(-m_{\text{eff}}\tau)$
- effective mass plot  $m_{\text{eff}} = -\log [G(\tau)/G(\tau - a_\tau)]$



$\Upsilon$  (S wave) and  $\chi_{b1}$  (P wave)

# Spectrum

zero temperature: ground and first excited states

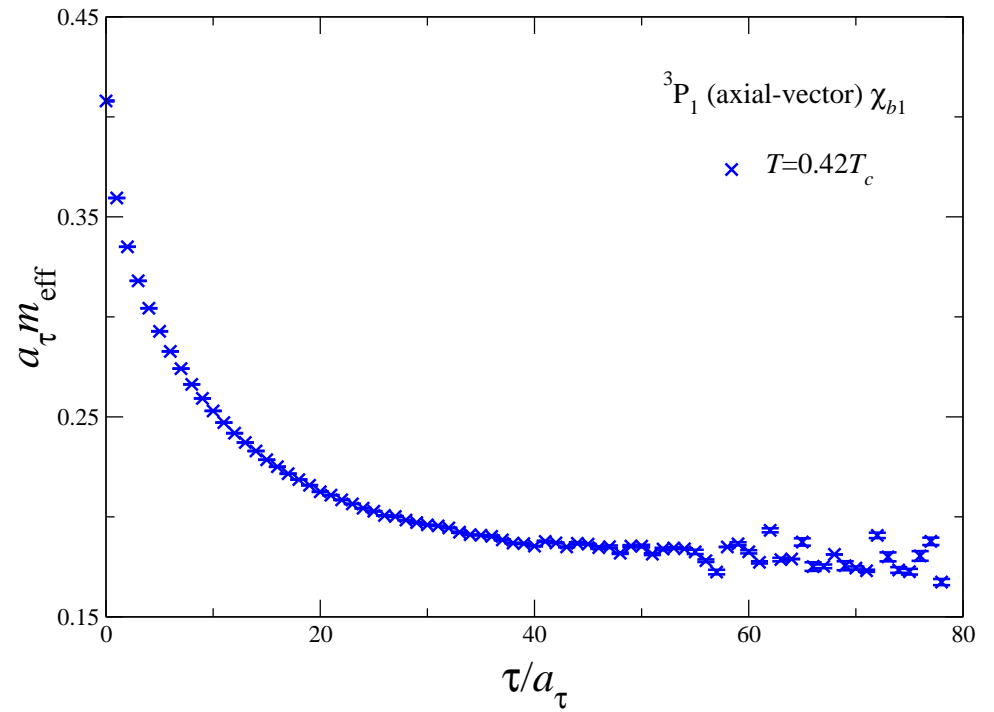
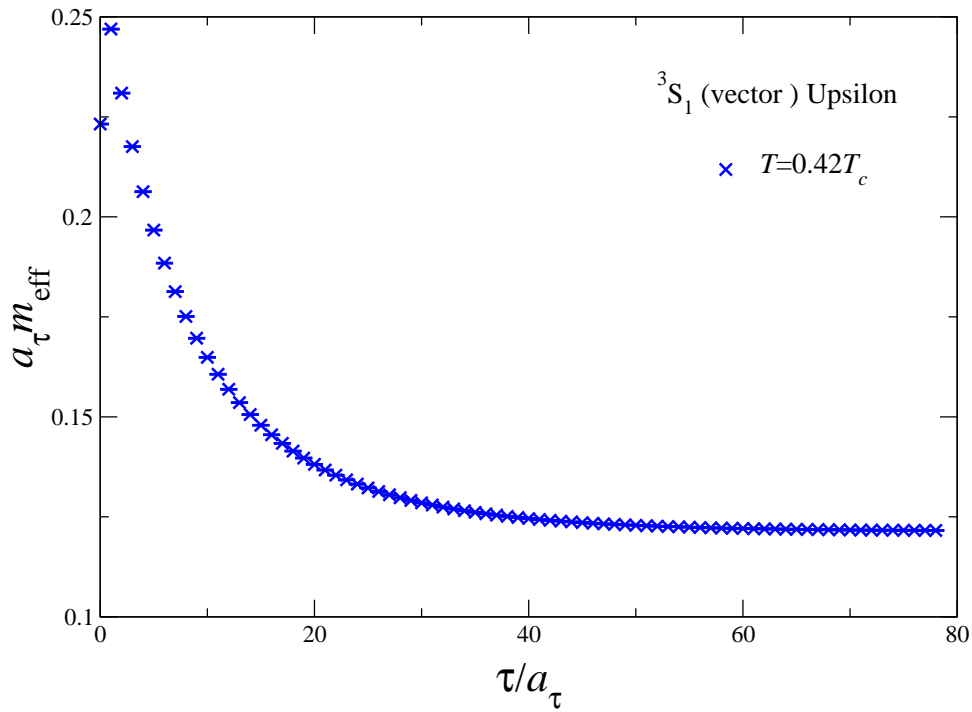
state	$a_\tau \Delta E$	Mass (MeV)	Exp. (MeV)
$1^1 S_0(\eta_b)$	0.118(1)	9438(8)	9390.9(2.8)
$2^1 S_0(\eta_b(2S))$	0.197(2)	10019(15)	-
$1^3 S_1(\Upsilon)$	0.121(1)	9460*	9460.30(26)
$2^3 S_1(\Upsilon')$	0.198(2)	10026(15)	10023.26(31)
$1^1 P_1(h_b)$	0.178(2)	9879(15)	9898.3(1.1)(1.1)
$1^3 P_0(\chi_{b0})$	0.175(4)	9857(29)	9859.44(42)(31)
$1^3 P_1(\chi_{b1})$	0.176(3)	9864(22)	9892.78(26)(31)
$1^3 P_2(\chi_{b2})$	0.182(3)	9908(22)	9912.21(26)(31)

\*  $\Upsilon(1S)$  used to set the scale

# Increasing the temperature

$\Upsilon$  S wave

$\chi_{b1}$  P wave

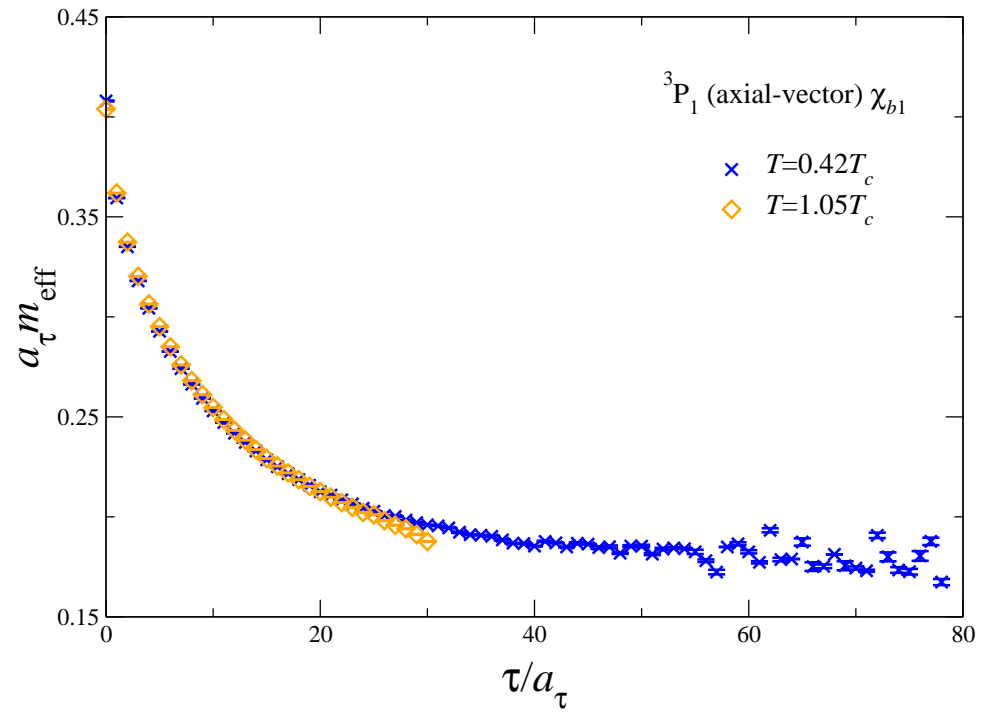
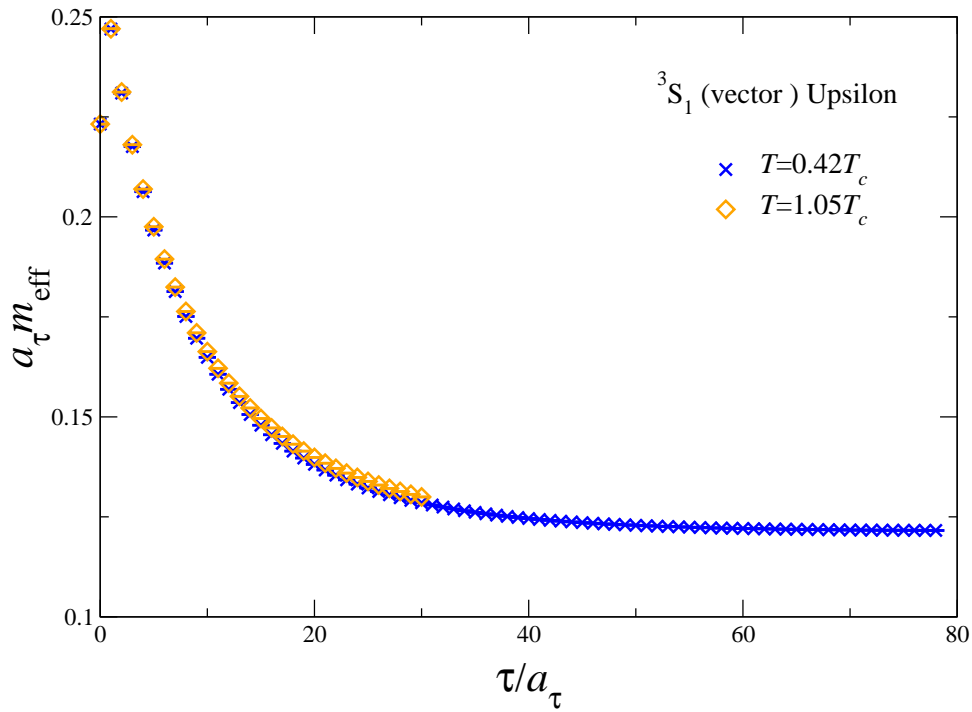


$$T/T_c = 0.42$$

# Increasing the temperature

$\Upsilon$  S wave

$\chi_{b1}$  P wave

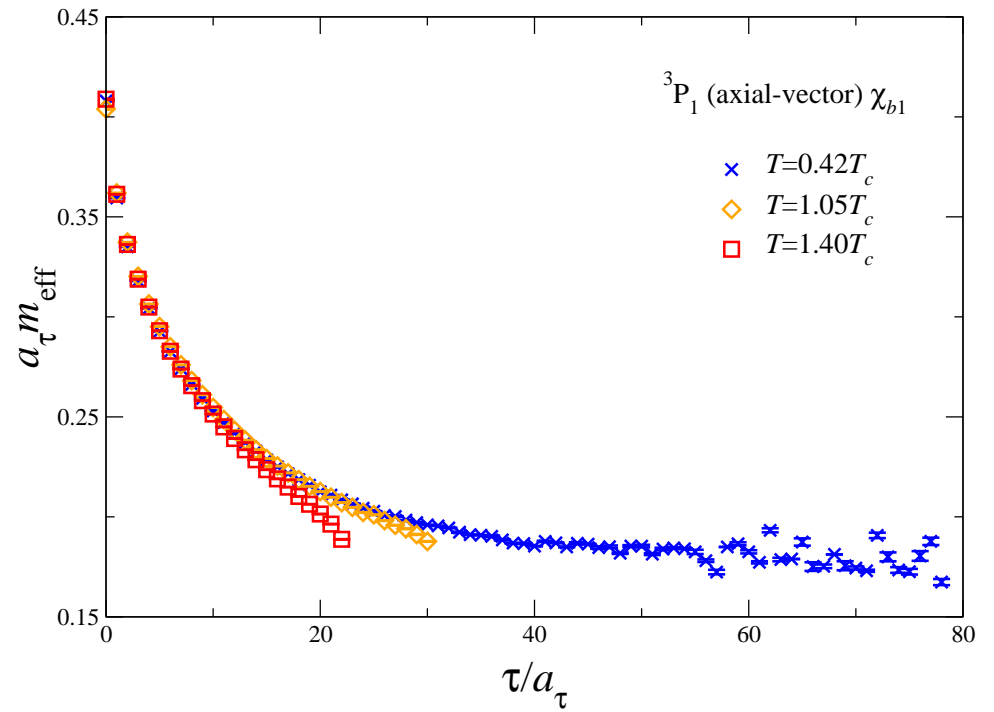
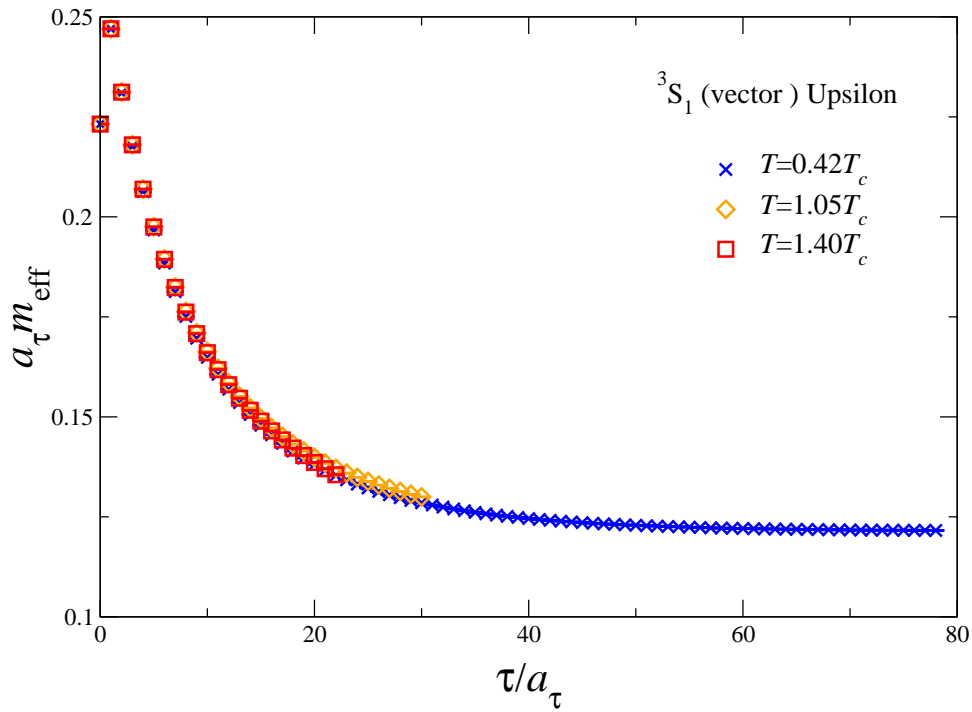


$$T/T_c = 1.05$$

# Increasing the temperature

$\Upsilon$  S wave

$\chi_{b1}$  P wave



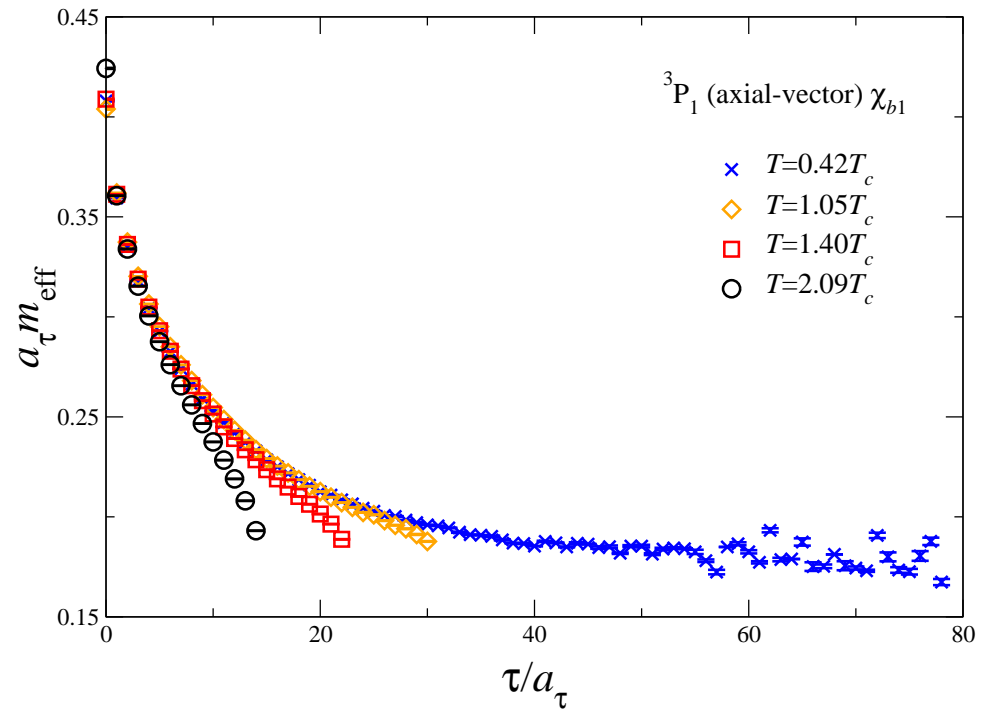
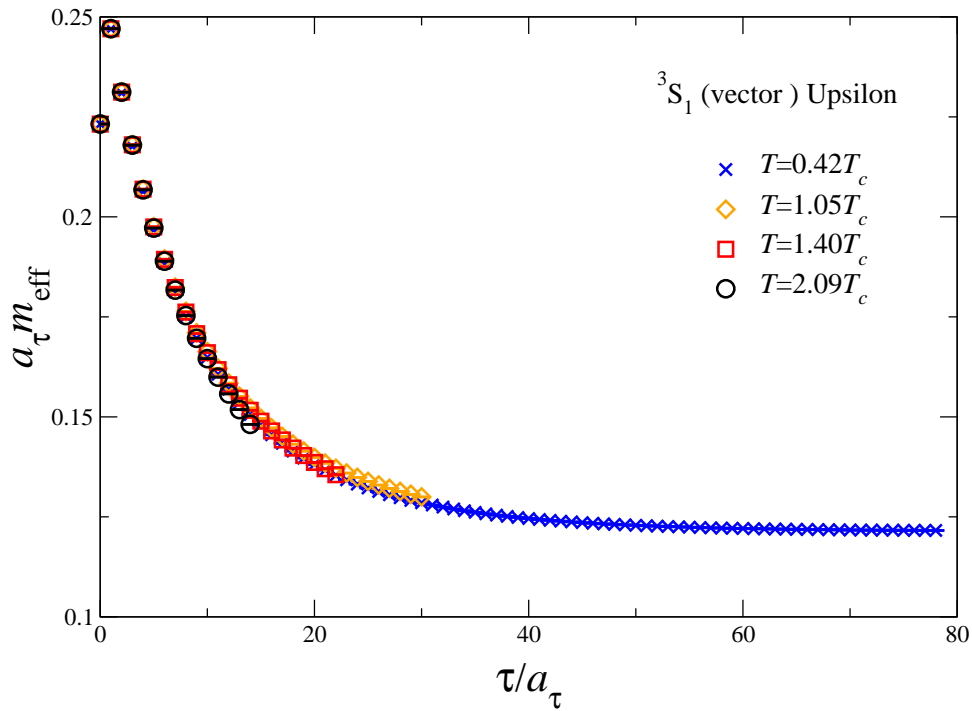
$$T/T_c = 1.40$$



# Increasing the temperature

$\Upsilon$  S wave

$\chi_{b1}$  P wave



$$T/T_c = 2.09$$

little  $T$  dependence

substantial  $T$  dependence  
no exponential decay  
melting

# Quarkonia at finite temperature

from euclidean correlators to spectral functions

$$G(\tau, \mathbf{p}) = \int d\omega K(\tau, \omega) \rho(\omega, \mathbf{p}) \quad K(\tau, \omega) = \frac{\cosh[\omega(\tau - 1/2T)]}{\sinh(\omega/2T)}$$

- use Maximal Entropy Method (MEM)
- first discussed quite some time ago ...

Asakawa & Hatsuda 1999, 2001

Karsch, Petreczky et al 2002

...

- ... but full of pitfalls and obstacles

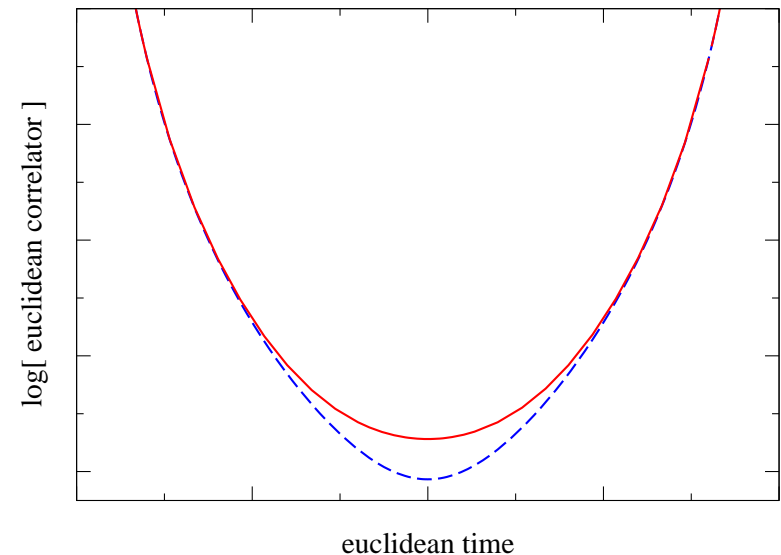
# Quarkonia at finite temperature

- in equilibrium: thermal boundary conditions
- euclidean correlators periodic
- spectral relation

$$G(\tau) = \int d\omega K(\tau, \omega) \rho(\omega)$$

$$K(\tau, \omega) = \frac{\cosh[\omega(\tau - 1/2T)]}{\sinh(\omega/2T)}$$

- problematic small  $\omega$  region: constant contribution  
transport, susceptibilities



G.A. & Martinez Resco 02, Petreczky & Teaney 05

# Quarkonia at finite temperature

relativistic formulation:

- melting of quarkonia obscured by constant contribution

Umeda 07, Petreczky et al 07-09

NRQCD:

- constant contribution absent
- no thermal boundary condition
- simple spectral relation  $G(\tau) = \int d\omega e^{-\omega\tau} \rho(\omega)$

why?

- factor out heavy quark mass scale:  $\omega = 2M + \omega'$
- $M \gg T$ : thermal effects exponentially suppressed

# Quarkonia at finite temperature

- no thermal boundary conditions
- simple spectral relation  $G(\tau) = \int d\omega e^{-\omega\tau} \rho(\omega)$

example:

correlators for free quarks with kinetic energy  $E_{\mathbf{p}} = \frac{\mathbf{p}^2}{2M}$

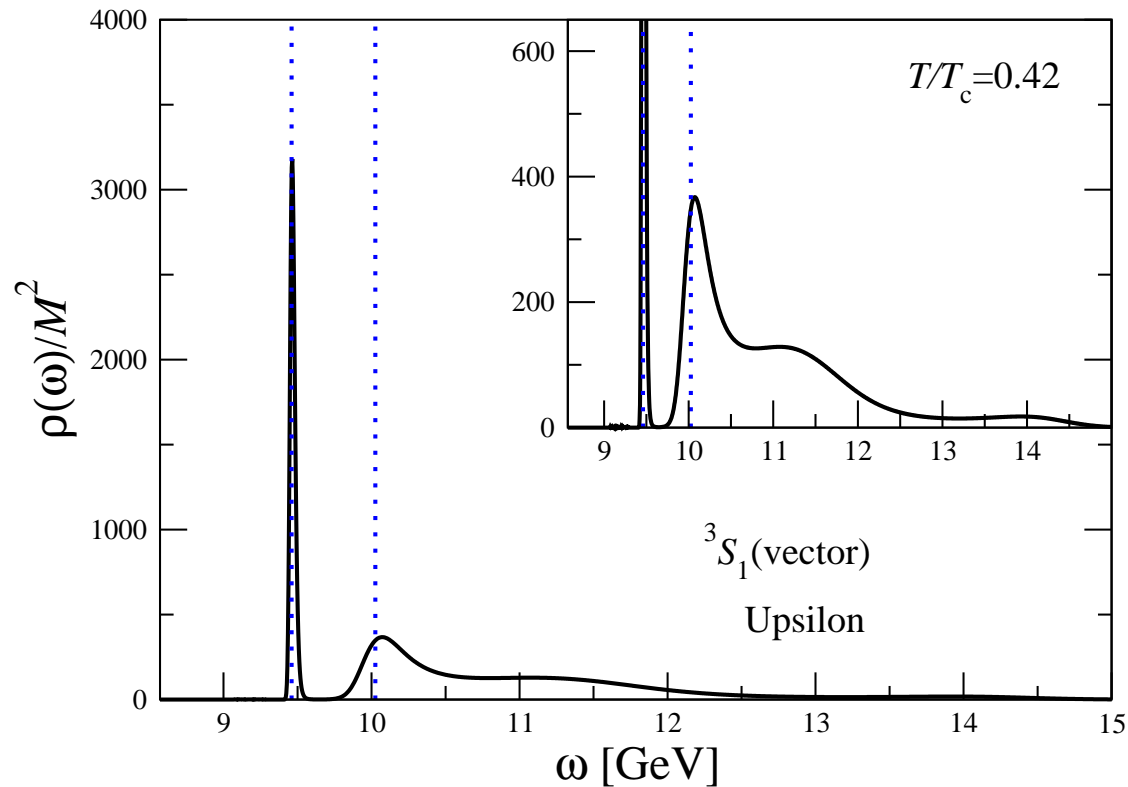
$$\begin{aligned} G_S(\tau) &\sim \int d^3p \exp(-2E_{\mathbf{p}}\tau) & \rho_S(\omega) &\sim \int d^3p \delta(\omega - 2E_{\mathbf{p}}) \\ G_P(\tau) &\sim \int d^3p \mathbf{p}^2 \exp(-2E_{\mathbf{p}}\tau) & \rho_P(\omega) &\sim \int d^3p \mathbf{p}^2 \delta(\omega - 2E_{\mathbf{p}}) \end{aligned}$$

Burnier, Laine & Vepsäläinen 08

- temperature dependence only enters via medium !

# $\Upsilon$ at finite temperature

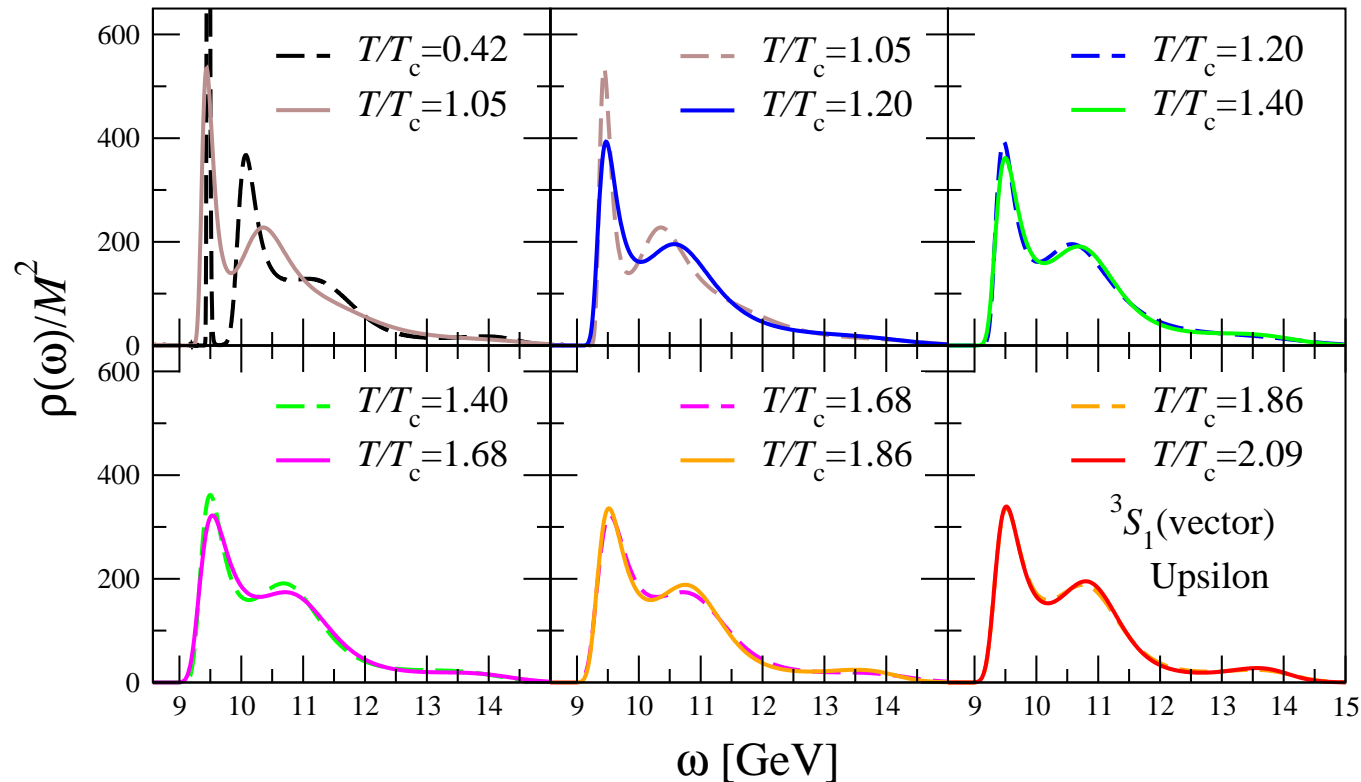
- nonperturbative spectral function: zero temperature



- dotted: ground and first excited states from exp. fits

# $\Upsilon$ at finite temperature

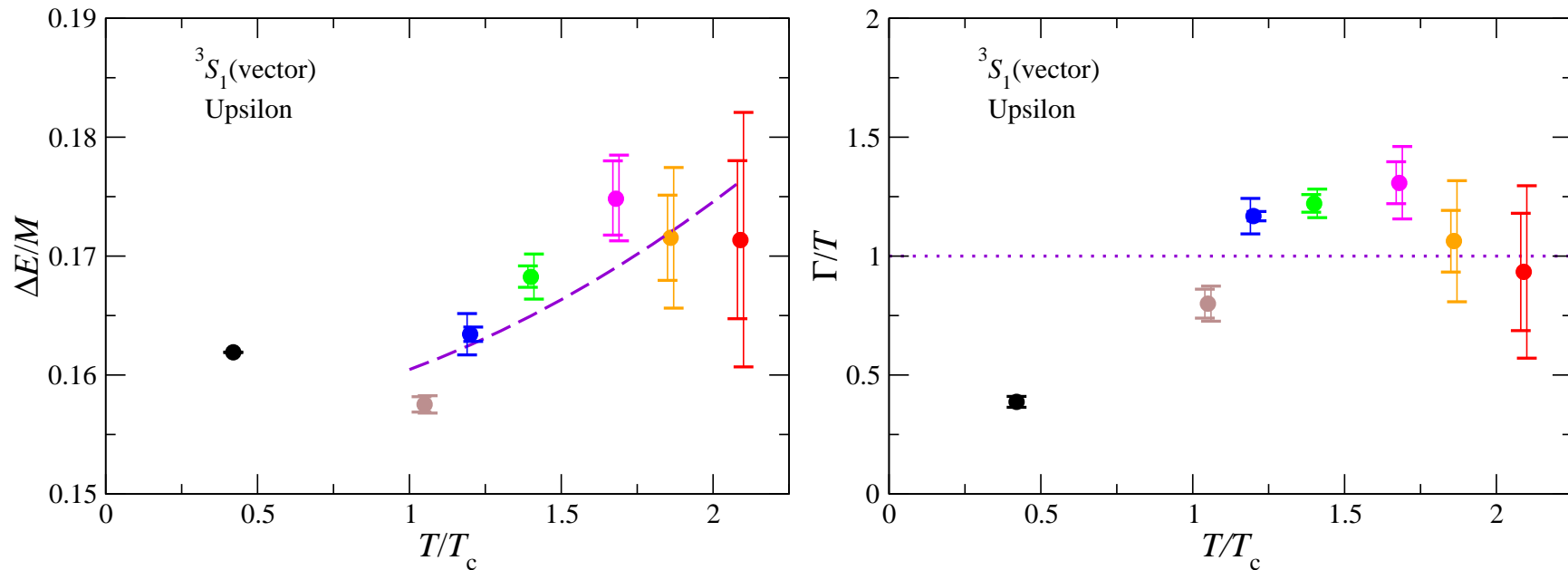
- construct spectral function: temperature dependence



- ground state survives – excited states suppressed  
compare with CMS results

# $\Upsilon$ at finite temperature

- extract mass shift and width of the ground state



- lines are analytical weak-coupling predictions

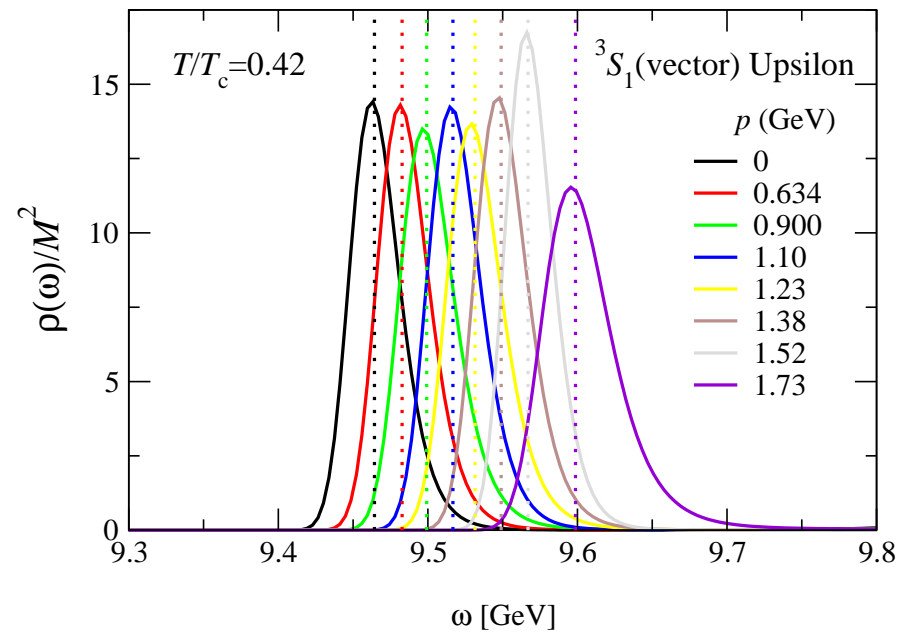
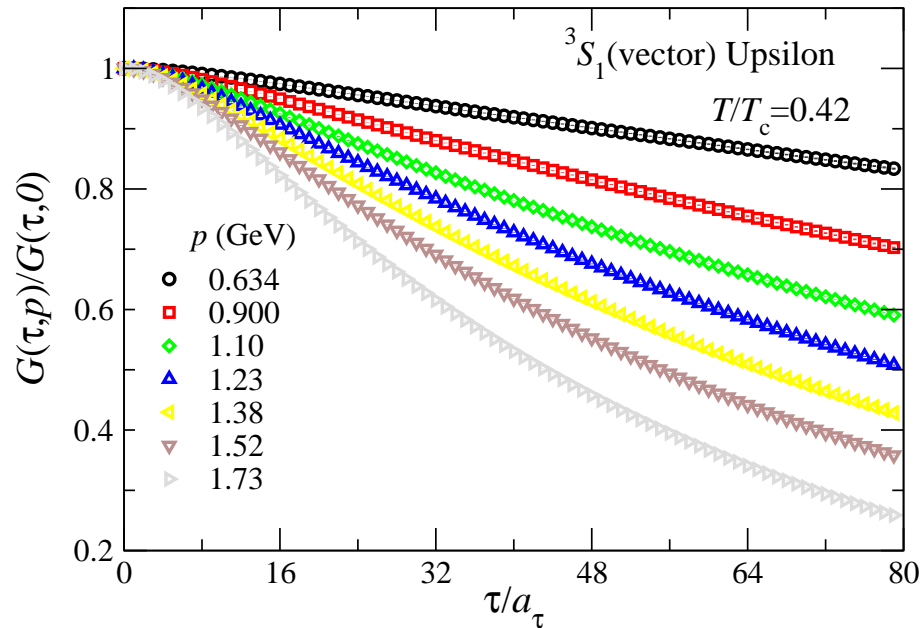
$$\Delta E \sim \alpha_s T^2 / M \quad \Gamma/T \sim \alpha_s^3 \quad \alpha_s \sim 0.4$$

Brambilla, Escobedo, Ghiglieri, Soto & Vairo 10



# moving $\Upsilon$ at finite temperature

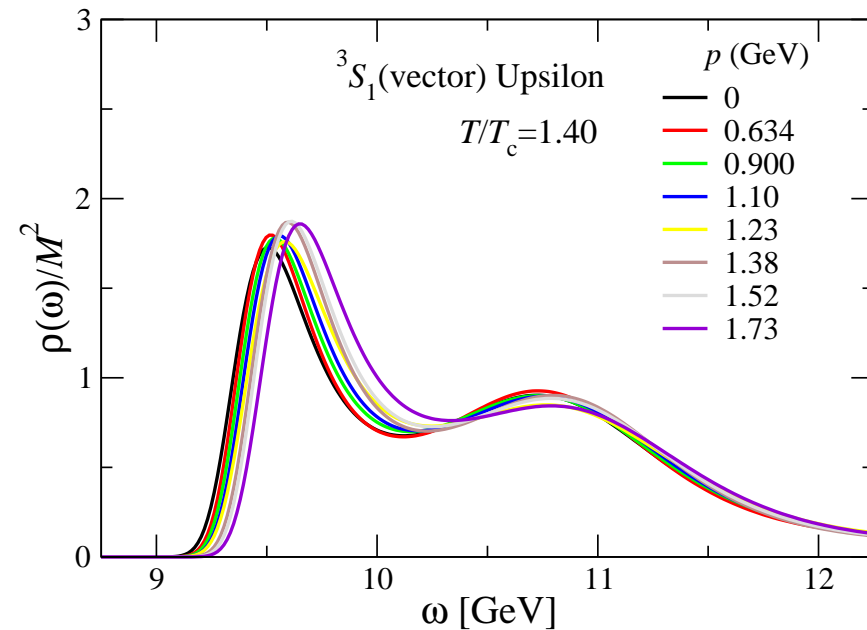
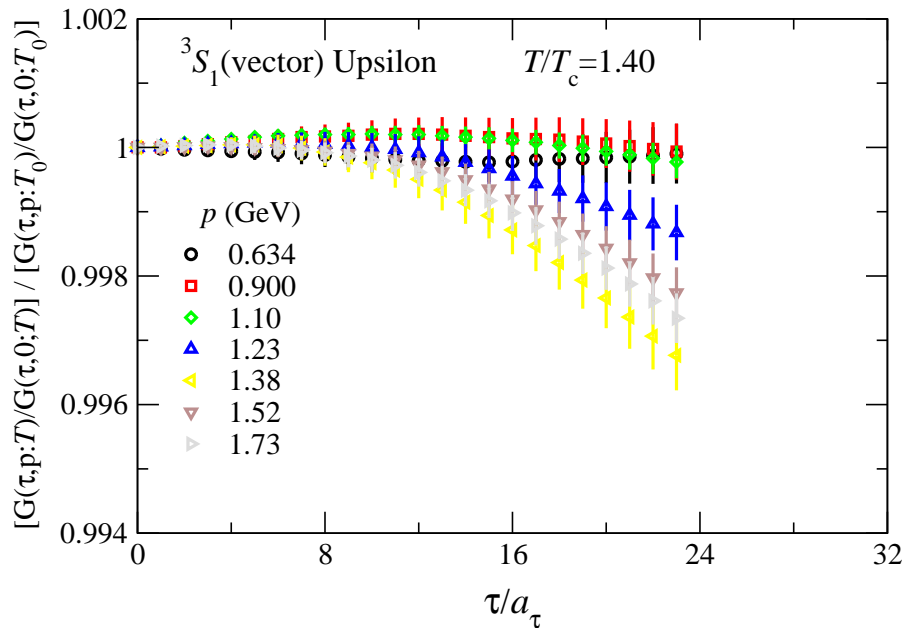
- non-relativistic speeds:  $v/c \lesssim 0.2$



- ratio  $G(\tau, \mathbf{p})/G(\tau, \mathbf{0})$ : clear momentum dependence in correlators, as expected
- reflected in spectral functions, agreement with exp. fits

# moving $\Upsilon$ at finite temperature

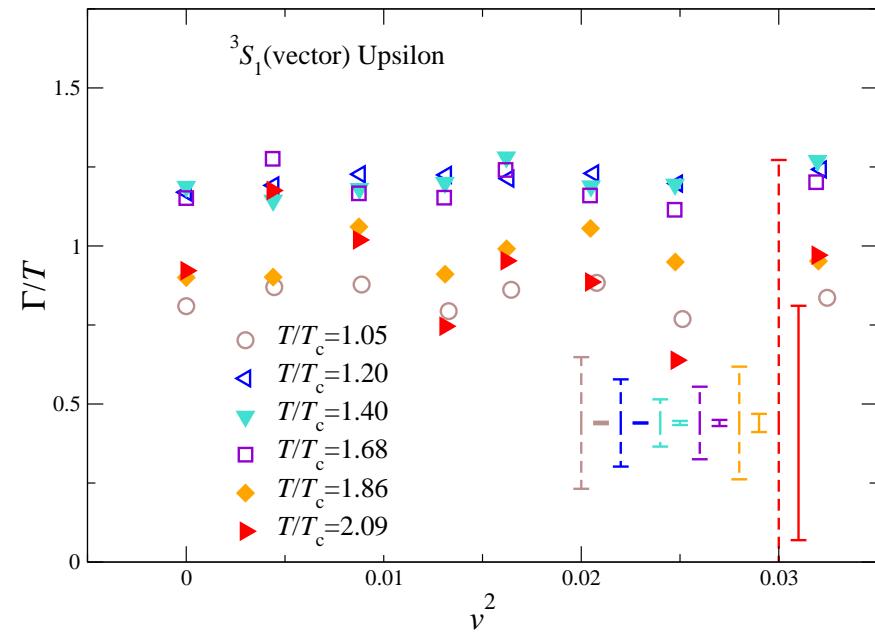
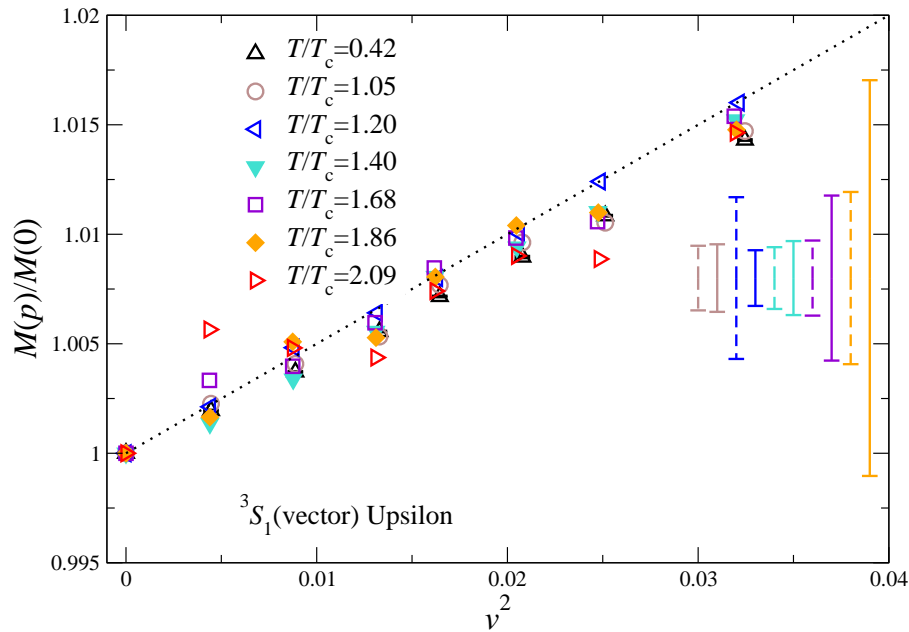
- non-relativistic speeds:  $v/c \lesssim 0.2$



- ratio  $[G(\tau, \mathbf{p}; T)/G(\tau, \mathbf{0}; T)]/[G(\tau, \mathbf{p}; T_0)/G(\tau, \mathbf{0}; T_0)]$ :  
very little temperature dependence in the momentum dependence
- survival of moving groundstate

# moving $\Upsilon$ at finite temperature

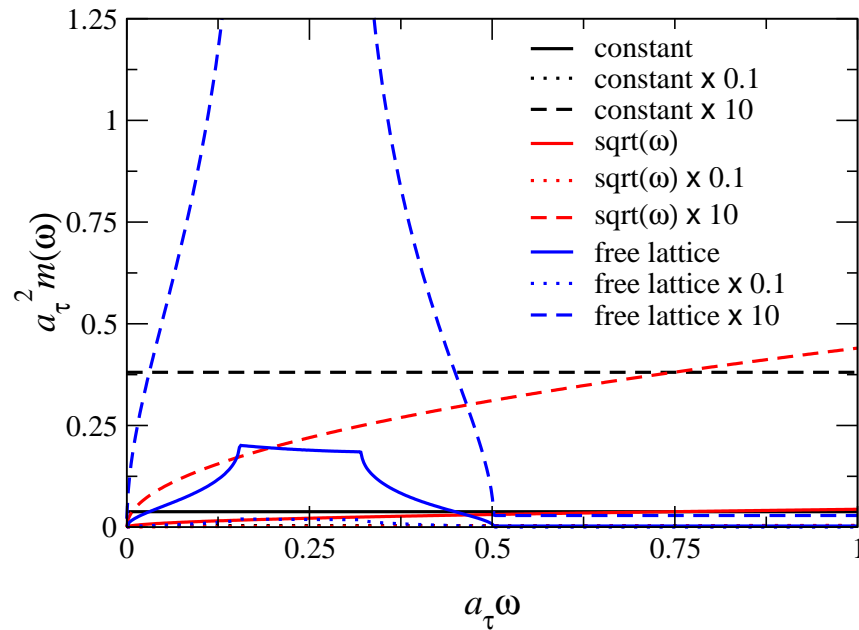
- non-relativistic speeds:  $v/c \lesssim 0.2$



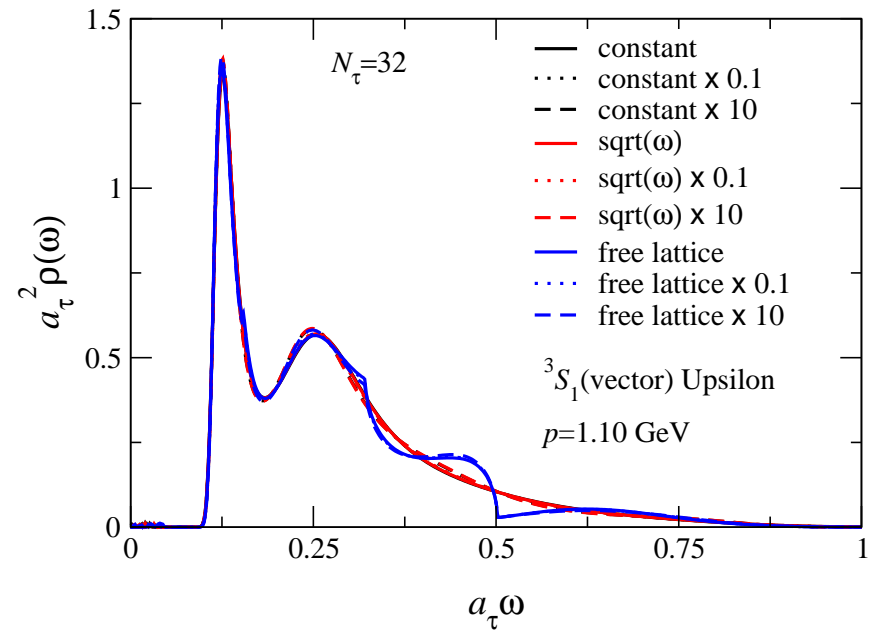
- extract dispersion relation  $E(p)/M = 1 + \frac{1}{2}v^2$  and thermal width in the QGP
- thermal deviations? need to control uncertainties

# moving $\Upsilon$ at finite temperature

- non-relativistic speeds:  $v/c \lesssim 0.2$



MEM input

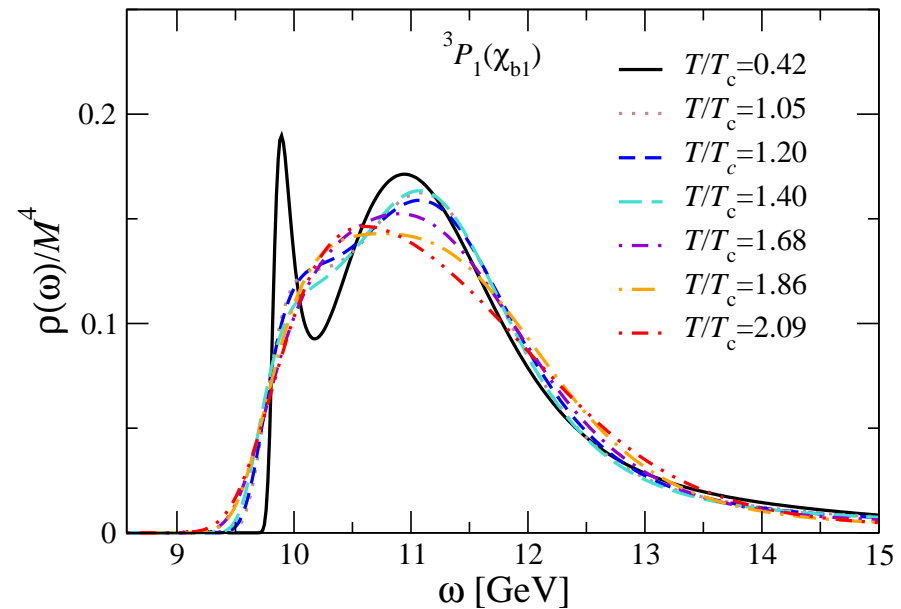
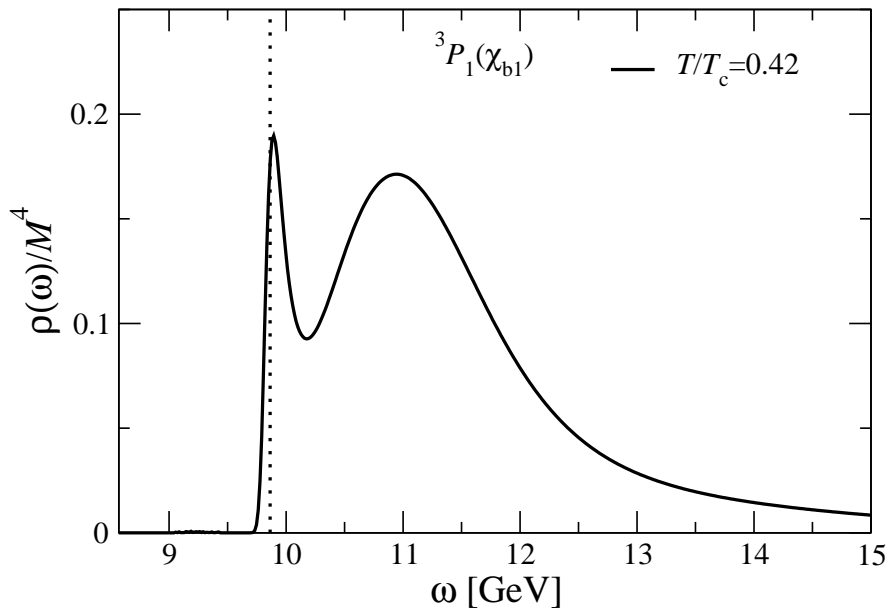


MEM output

- insensitivity to default model
- sensitivity to maximal  $\tau$  used

# P waves at finite temperature

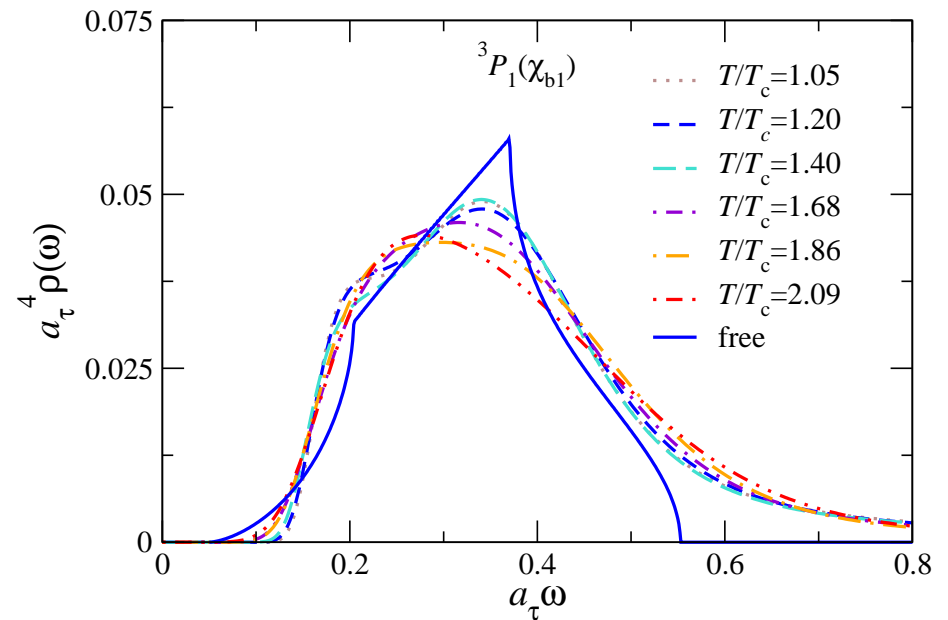
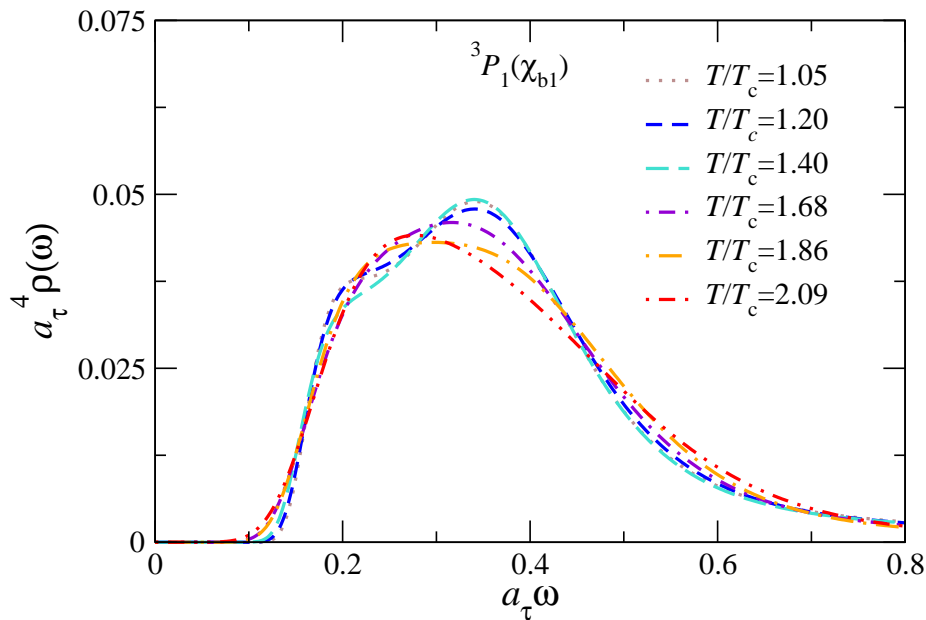
- $\chi_{b1}$  axial-vector channel (preliminary)



- groundstate below  $T_c$ , agreement with exp. fit
- melting immediately above  $T_c$
- sensitive to  $\tau_{\max}$ : reflects thermal boundary conditions?  
stable when  $\tau_{\max} \leq N_\tau - 3$

# P waves at finite temperature

- $\chi_{b1}$  axial-vector channel (preliminary)



- melting above  $T_c$ : a featureless blob ?
- shape similar to free lattice spectral function ?
- in progress

# Summary

- bottomonium: NRQCD on QGP background
- S wave ground states survive, at rest and moving excited states appear suppressed
- P wave states melt immediately above  $T_c$
- use of NRQCD greatly improves reliability of MEM
- in progress: extension to  $N_f = 2 + 1$  on a finer lattice

EMMI workshop:



## SIGN 2014

3rd international workshop on the sign problem  
in QCD and related theories

4 days in February 2014

GSI, Darmstadt, Germany

organisers: Owe Philipsen and GA