

Heavy quarks in a hot bath in the 't Hooft limit

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Heavy quarks and quarkonia in thermal QCD
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Outline

- 1 QCD in the large- N limit
- 2 An example: Free energy of a static source
- 3 Conclusions

Based on:

- [B. Lucini and M. P., 1210.4997] (to appear in Phys. Rep.)
- [A. Mykkänen, M. P. and K. Rummukainen, JHEP 1205 (2012) 069]



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Generalities

QCD in the 't Hooft limit

Consider a QCD-like theory with $SU(N)$ gauge group

Double limit $N \rightarrow \infty$ and $g \rightarrow 0$, with $\lambda = g^2 N$ and n_f fixed

Double-line notation:

- Quark: fundamental rep. \Rightarrow single line
- Gluon: adjoint rep. \Rightarrow double line

Terms proportional to different powers of $1/N$ can be arranged in a *topological series*

$$\mathcal{A} = \sum_{h,b=0}^{\infty} \left(\frac{1}{N}\right)^{2h+b-2} \sum_{n=0}^{\infty} c_{(h,b),n} \lambda^n$$

Dominance of *planar diagrams without dynamical quark loops*

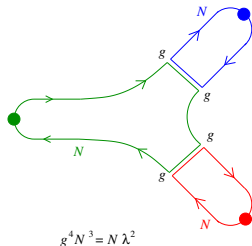
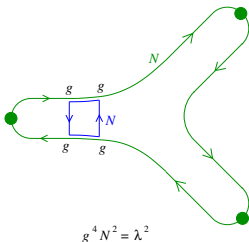
The theory *simplifies* but does not become *integrable*



Elementary phenomenological implications

If large- N QCD is confining:

- Light spectrum: infinitely many, non-interacting glueballs and mesons, masses $O(N^0)$: **large- N QCD is a theory of weakly coupled hadrons**
- No exotica (tetraquarks, molecules, et c.)
- The OZI rule is exact



- Chiral Lagrangian exact at tree level
- Axial anomaly and $m_{\eta'}^2$ are $O(1/N)$
- Baryons as “non-relativistic” ($m_B = O(N)$) solitons of the theory



The large- N limit in the holographic correspondence

Maldacena conjecture: A correspondence between gauge theories and string theories in a higher-dimensional, curved spacetime

Famous example: $\mathcal{N} = 4$ super-Yang–Mills in 4D vs. type IIB string theory in 10D

Arises as *open/closed string duality* in a background of D3-branes

Relations between the gauge and string parameters:

- ★ Large- N limit of the gauge theory \longleftrightarrow *Classical* limit of the string theory

$$\frac{\lambda}{N} = 4\pi g_s$$

- ★ Strong-coupling limit of the gauge theory \longleftrightarrow *Gravity* limit of the string theory

$$\lambda = \frac{R^4}{l_s^4}$$



From $\mathcal{N} = 4$ super-Yang–Mills to QCD (I)

Can results for $\mathcal{N} = 4$ SYM have any relevance for QCD?

At zero temperature, $\mathcal{N} = 4$ SYM and QCD are *radically qualitatively different*

- QCD is not supersymmetric; $\mathcal{N} = 4$ SYM is (*maximally*)
- QCD has fundamental quarks; $\mathcal{N} = 4$ SYM has adjoint fermions
- QCD is confining; $\mathcal{N} = 4$ SYM is not
- In QCD, the coupling runs; in $\mathcal{N} = 4$ SYM it does not
- QCD has a finite mass gap and discrete spectrum; the $\mathcal{N} = 4$ SYM spectrum is continuous
- QCD exhibits χ SB; $\mathcal{N} = 4$ SYM does not



From $\mathcal{N} = 4$ super-Yang–Mills to QCD (II)

Can results for $\mathcal{N} = 4$ SYM have any relevance for QCD?

The situation is more favourable in the *deconfined phase* at finite temperature

- Finite temperature breaks supersymmetry
- QCD is not confining at high temperature
- Both QCD and $\mathcal{N} = 4$ SYM display Debye screening
- The QCD coupling runs (*logarithmically*) slowly
- Chiral symmetry restored



From $\mathcal{N} = 4$ super-Yang–Mills to QCD (III)

Is there a holographic dual for *any* gauge theory?

- ★ *Top-down* approach: Break explicitly some symmetries of $\mathcal{N} = 4$ SYM
- ★ *Bottom-up* approach: Construct “by hand” a suitable gravity dual of QCD

Essentially *all* holographic results rely on the large- N approximation \rightarrow test on the lattice



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Free energy of a heavy source in Yang–Mills

In YM, the Polyakov loop is the order parameter for deconfinement

Bare free energy is divergent \rightarrow renormalization [Dotsenko and Vergeles, 1980]

Perturbative predictions [Burnier, Laine and Vepsäläinen, 2009; Brambilla et al., 2010; Ghiglieri, 2012]

Do sources in different irreps obey Casimir scaling [Ambjørn, Olesen and Peterson, 1984]? (See [Dumitru et al., 2003; Döring et al., 2007; Gupta, Hübner and Kaczmarek, 2008; Hübner and Pica, 2008] for tests in SU(2) and SU(3))



Setup of the simulations

Wilson action [Wilson, 1974] and tree-level improved action [Curci, Menotti and Paffuti, 1983; Lüscher and Weisz, 1985]

Heat-bath and overrelaxation updates on $SU(2)$ subgroups

Non-perturbative definition of the scale (string tension and/or Sommer parameter)

Polyakov loop renormalization from $T = 0$ static potential [Kaczmarek, Karsch, Petreczky and Zantow, 2002]

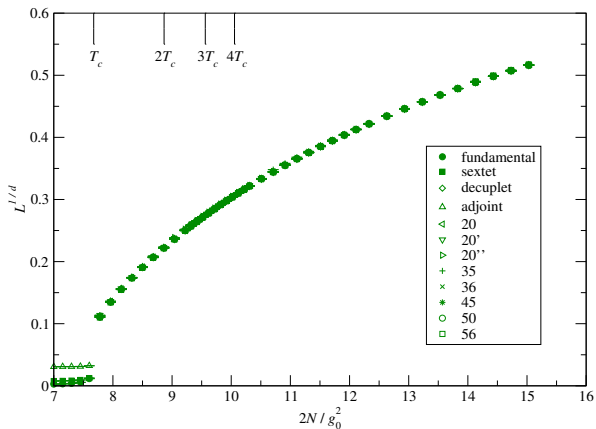
Scheme choice: Set constant term in the renormalized $T = 0$ potential to zero

(Alternative renormalization methods exist [Gupta, Hübner and Kaczmarek, 2008; Gavai, 2010])



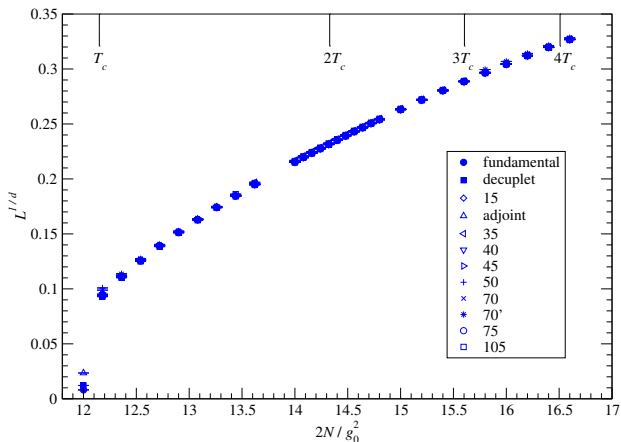
Results: Casimir scaling (I)

Strong evidence for Casimir scaling

SU(4), $N_t = 5$ 

Results: Casimir scaling (II)

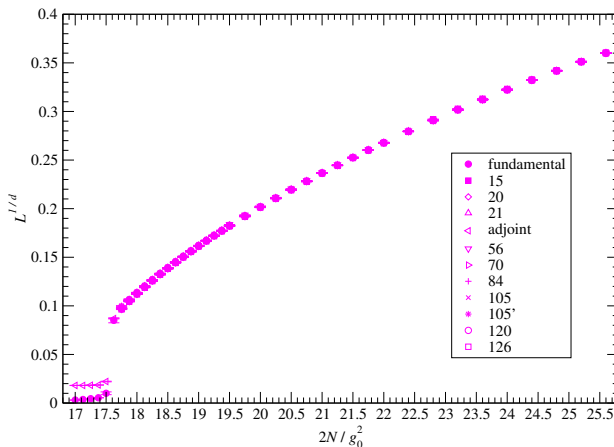
Strong evidence for Casimir scaling

SU(5), $N_t = 5$ 

Results: Casimir scaling (III)

Strong evidence for Casimir scaling

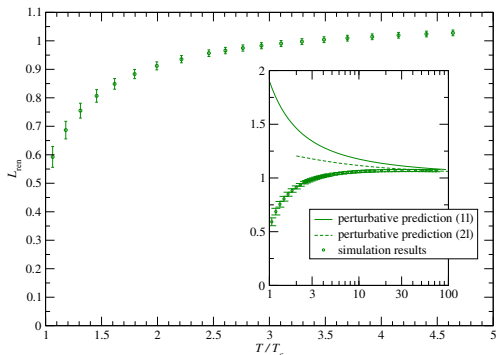
$SU(6), N_t = 5$



Results: Renormalized loop

Renormalized SU(4) fundamental loop

SU(4), fundamental representation



Strong similarities with SU(3) [Gupta, Hübner and Kaczmarek, 2008]

Comparison with perturbative predictions [Burnier, Laine and Vepsäläinen, 2009; Brambilla et al., 2010]

Comparison with strong-coupling expectations from holography [Noronha, 2010]

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Conclusions

- Large- N QCD as an interesting theoretical laboratory
- Interest revived by the relevance in holographic computations
- Finite-temperature setup may be suitable for comparisons with real-world QCD
- **Lattice tests**
- An example: Free energy of static sources in quenched QCD

