

# Transport theory

$$p^\mu \partial_\mu f(x, p) = C_{22}$$

We consider two body collisions

$$C_{22} = \frac{1}{2E_1} \int \frac{d^3 p_2}{(2\pi)^3 2E_2} \frac{1}{\nu} \int \frac{d^3 p'_1}{(2\pi)^3 2E'_1} \frac{d^3 p'_2}{(2\pi)^3 2E'_2} f'_1 f'_2 |\mathcal{M}_{1'2' \rightarrow 12}|^2 (2\pi)^4 \delta^{(4)}(p'_1 + p'_2 - p_1 - p_2) \\ - \frac{1}{2E_1} \int \frac{d^3 p_2}{(2\pi)^3 2E_2} \frac{1}{\nu} \int \frac{d^3 p'_1}{(2\pi)^3 2E'_1} \frac{d^3 p'_2}{(2\pi)^3 2E'_2} f_1 f_2 |\mathcal{M}_{12 \rightarrow 1'2'}|^2 (2\pi)^4 \delta^{(4)}(p_1 + p_2 - p'_1 - p'_2)$$



$$\Delta t \rightarrow 0$$

$$\Delta^3 x \rightarrow 0$$



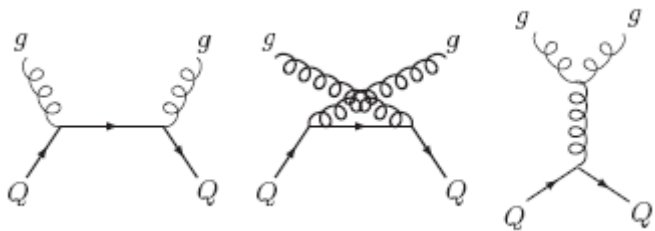
**Exact  
solution**

Collision integral is solved with a **local stochastic sampling**

[V. Greco et al PLB670, 325 (08)]  
[Z. Xhu, et al. PRC71(04)]

$$P_{22} = \frac{\Delta N_{\text{coll}}^{2 \rightarrow 2}}{\Delta N_1 \Delta N_2} = v_{\text{rel}} \sigma_{22} \frac{\Delta t}{\Delta^3 x}$$

# Cross Section $gc \rightarrow gc$



The infrared singularity is regularized introducing a **Debye-screening-mass**  $\mu_D$

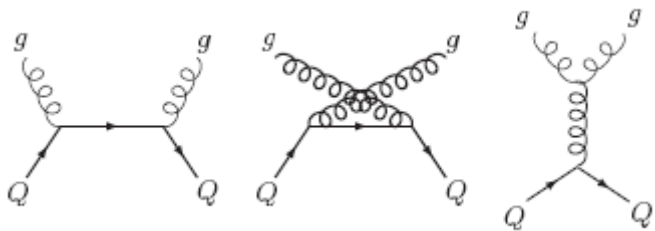
$$\begin{aligned} \sum |\mathcal{M}|^2 = \pi^2 \alpha^2 (Q^2) & \left[ \frac{32(s - M^2)(M^2 - u)}{t^2} + \frac{64}{9} \frac{(s - M^2)(M^2 - u) + 2M^2(s + M^2)}{(s - M^2)^2} \right. \\ & + \frac{64}{9} \frac{(s - M^2)(M^2 - u) + 2M^2(M^2 + u)}{(M^2 - u)^2} + \frac{16}{9} \frac{M^2(4M^2 - t)}{(s - M^2)(M^2 - u)} \\ & \left. + 16 \frac{(s - M^2)(M^2 - u) + M^2(s - u)}{t(s - M^2)} - 16 \frac{(s - M^2)(M^2 - u) - M^2(s - u)}{t(M^2 - u)} \right]. \end{aligned}$$

$$\frac{1}{t} \rightarrow \frac{1}{t - m_D}$$

$$m_D = \sqrt{4\pi\alpha_s} T$$

[B. L. Combridge, Nucl. Phys. B151, 429 (1979)]  
[B. Svetitsky, Phys. Rev. D 37, 2484 (1988) ]

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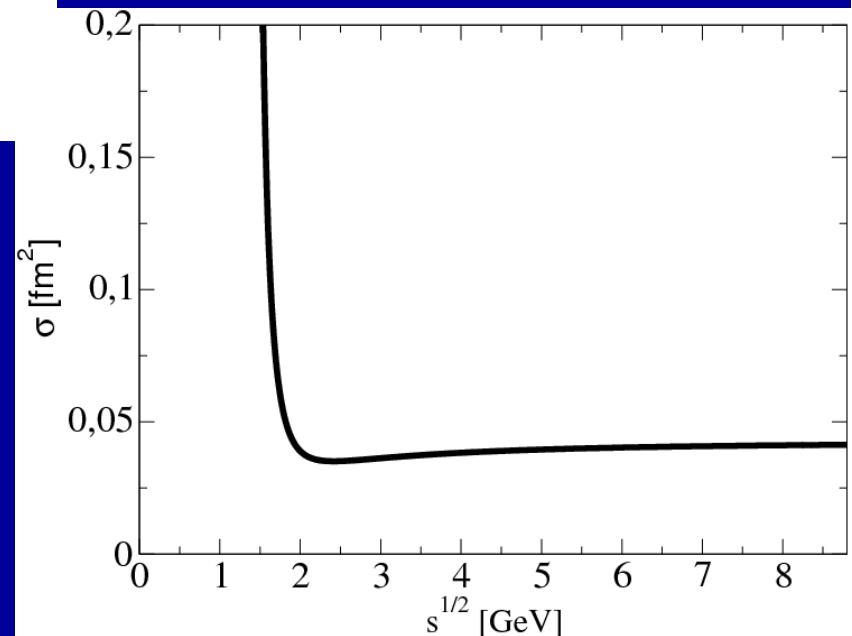
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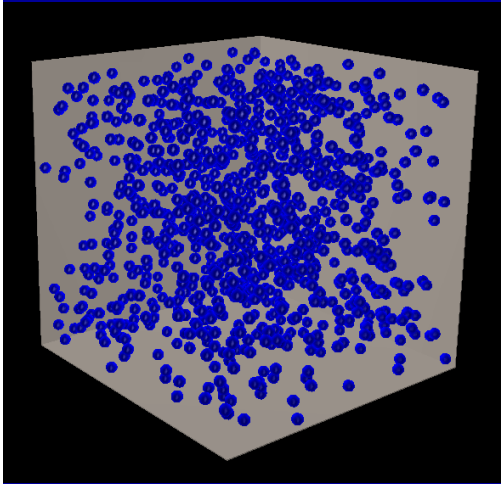
$$m_D = \sqrt{4\pi\alpha_s T}$$


$$\hat{\sigma} = \frac{1}{16\pi(s - M^2)^2} \int_{-(s - M^2)^2/s}^0 dt \sum |\mathcal{M}|^2 \longrightarrow$$

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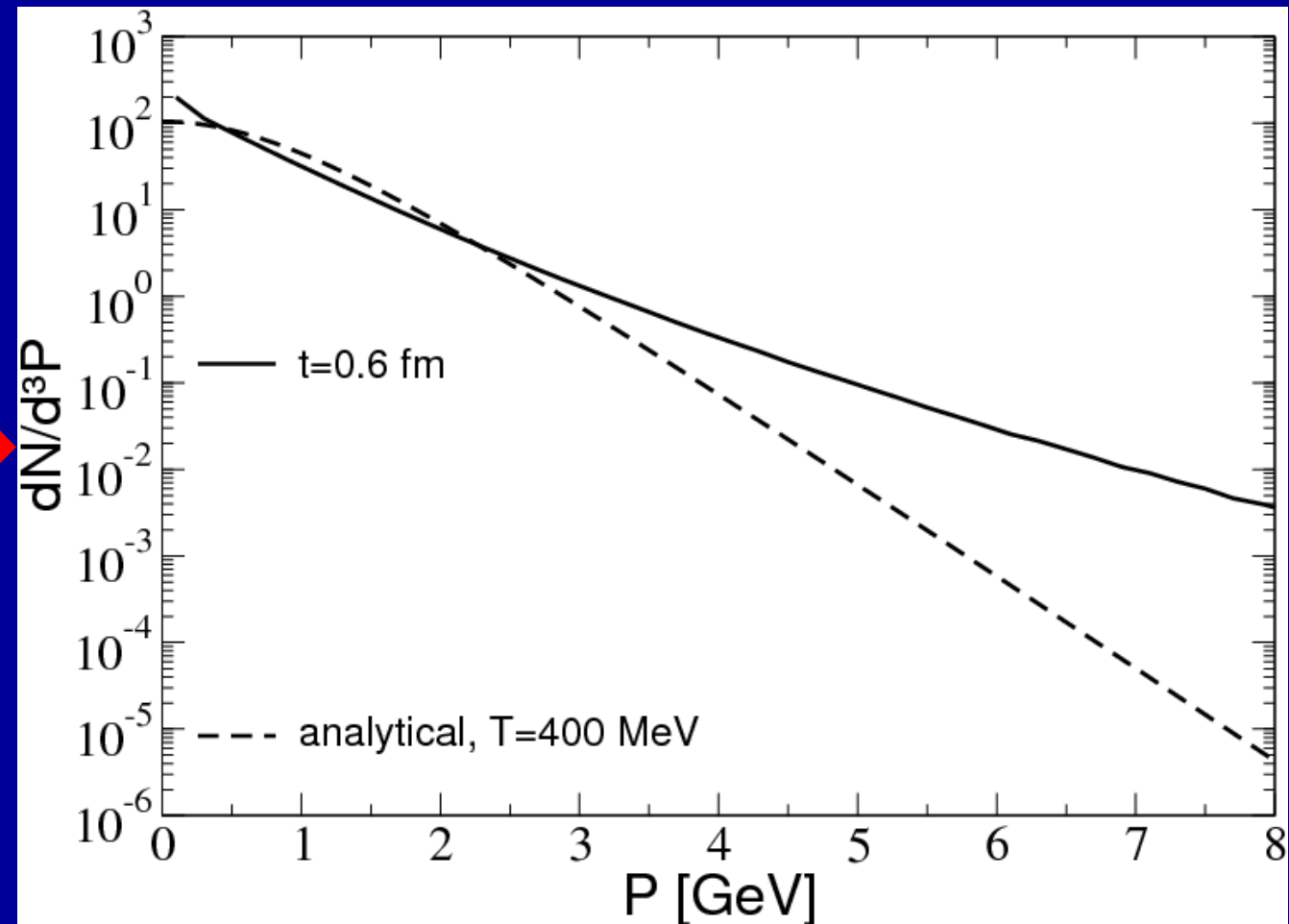
# Charm evolution in a static medium



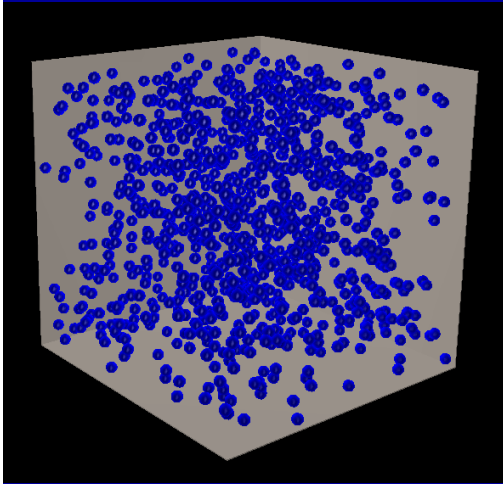
**C** and  $\bar{\text{C}}$  initially  
are distributed:  
**uniformly in  
r-space**, while in  
**p-space** 

Simulations in which a particle  
ensemble in a **box** evolves dynamically

**Bulk** composed only by **gluons** in  
**thermal equilibrium** at **T=400 MeV**



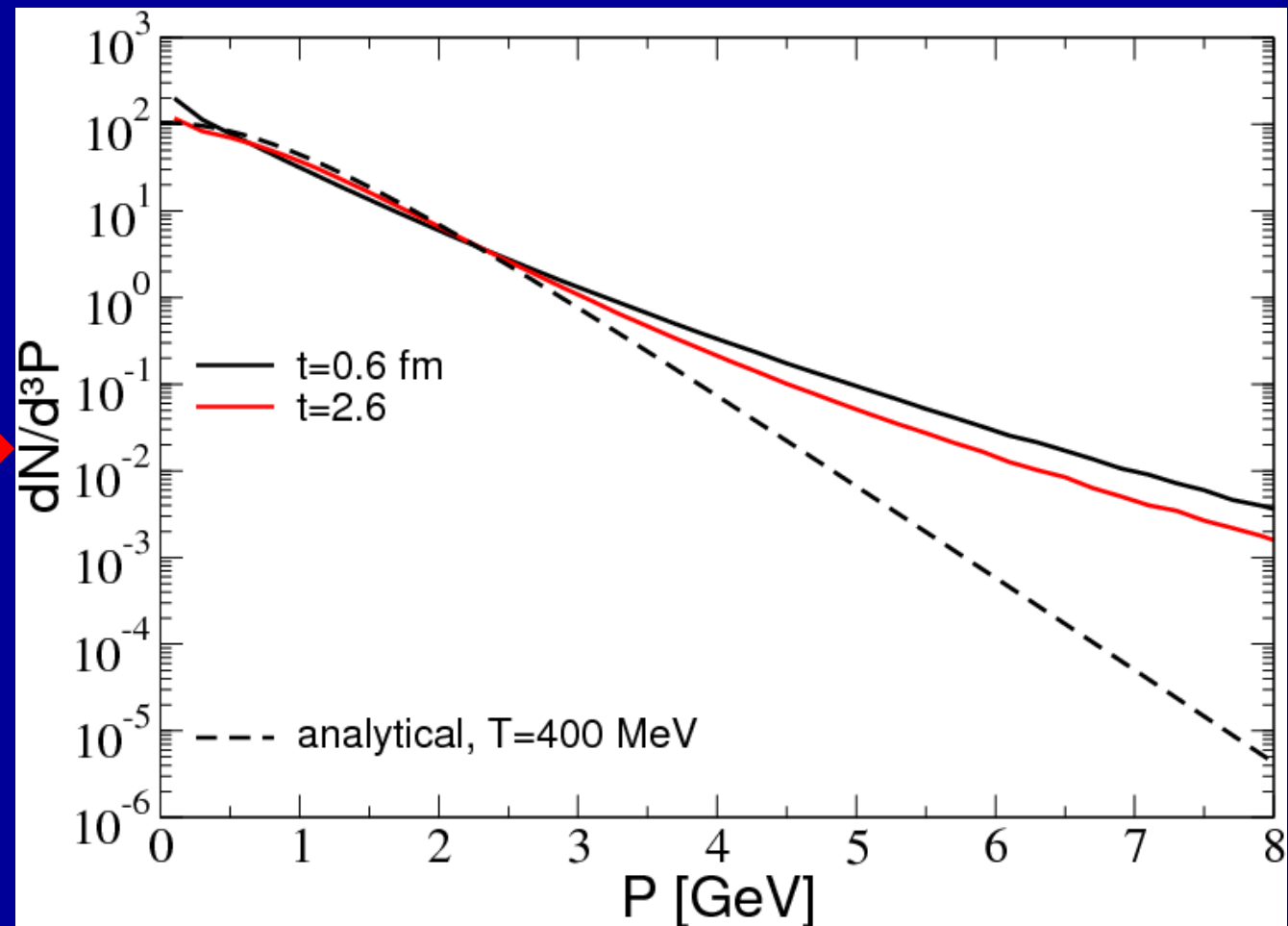
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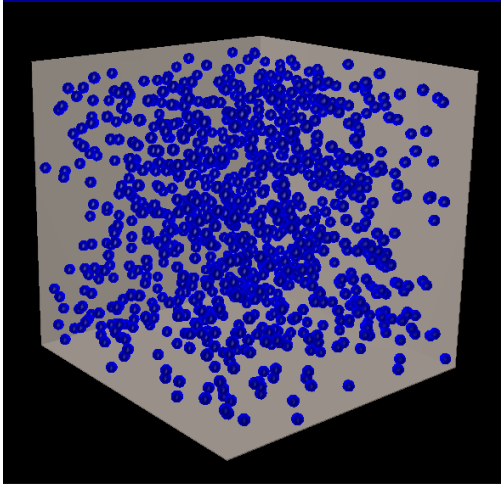
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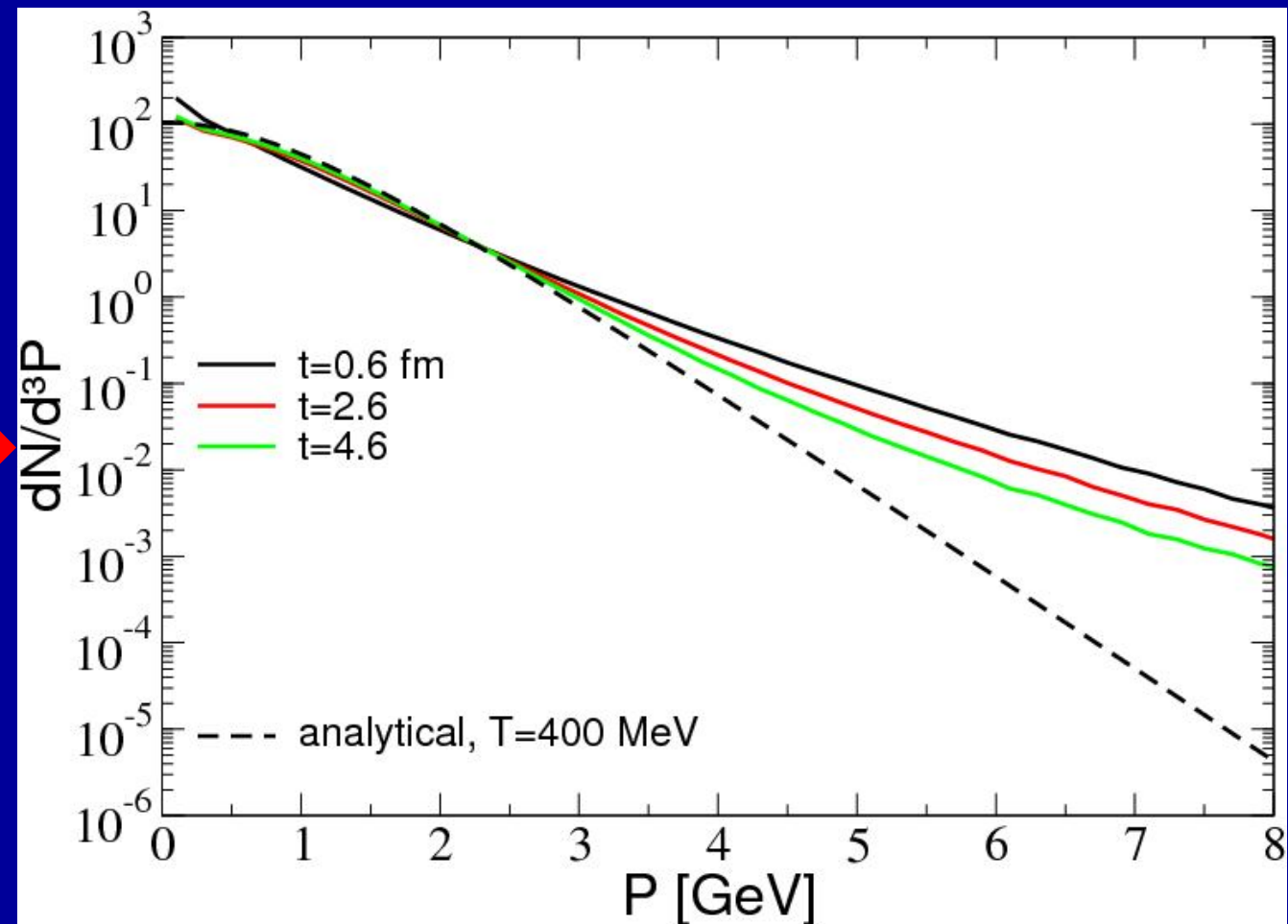
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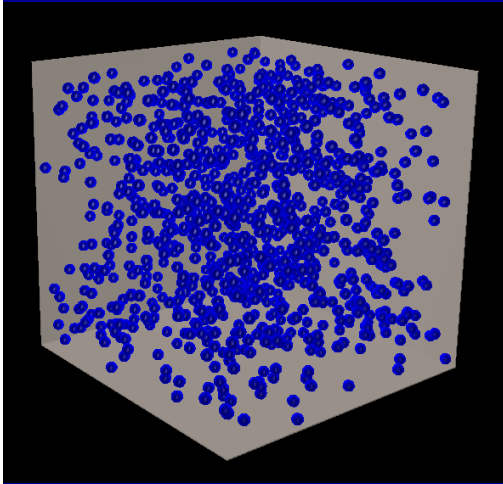
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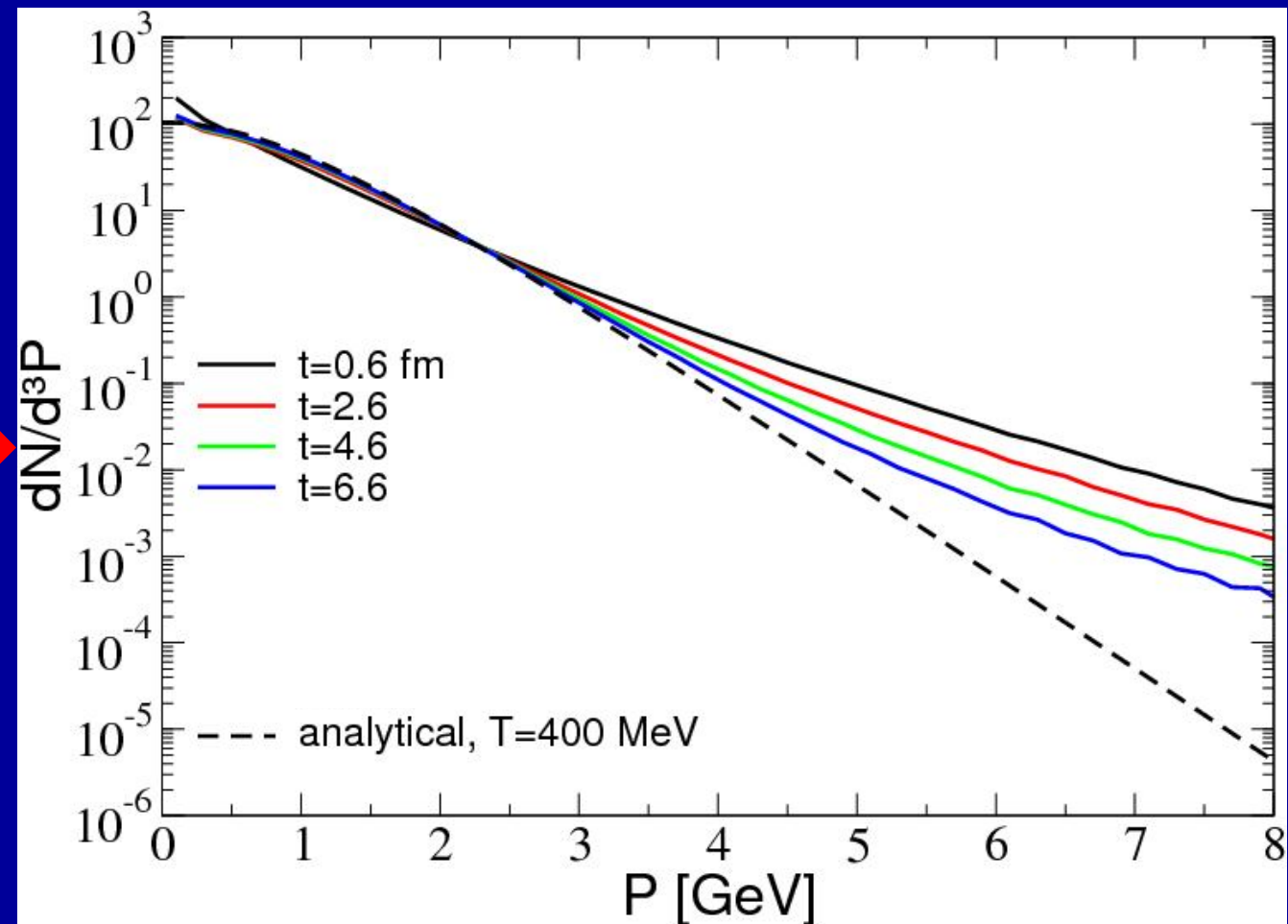
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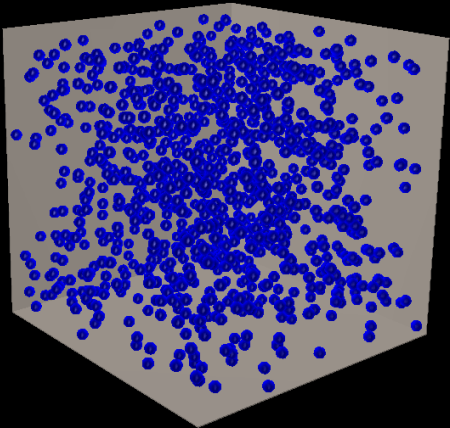
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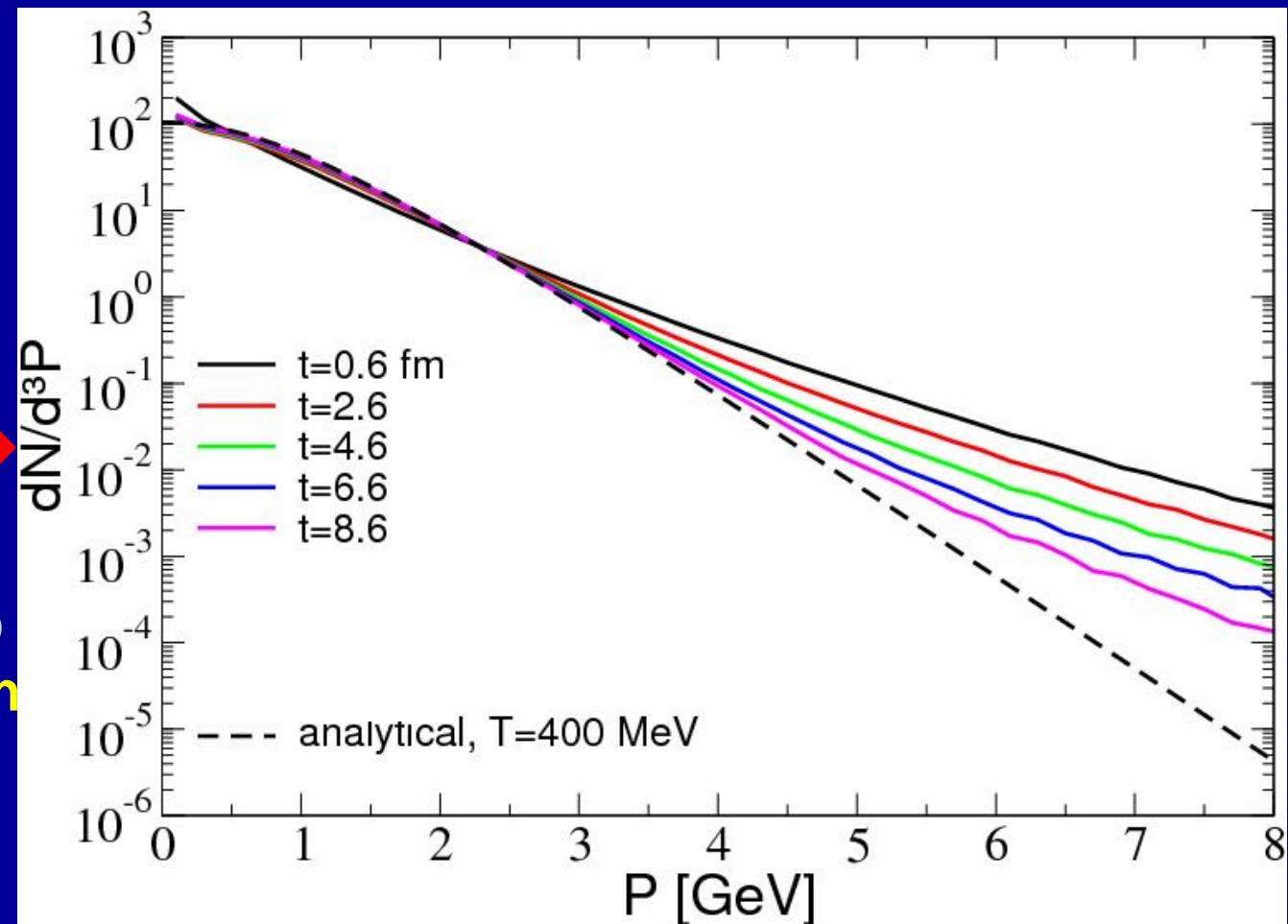


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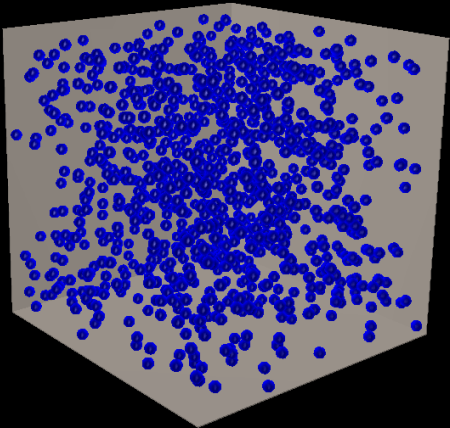
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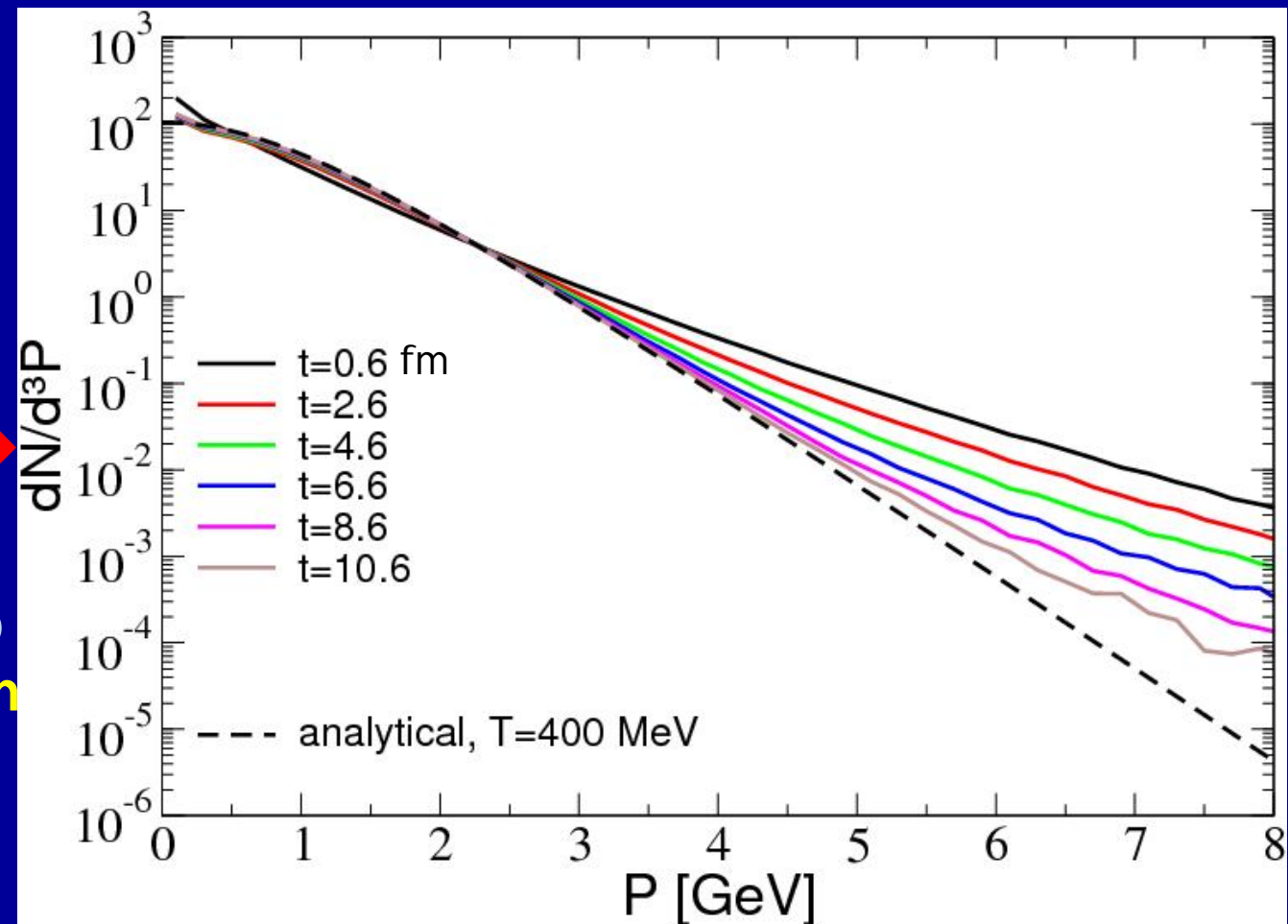


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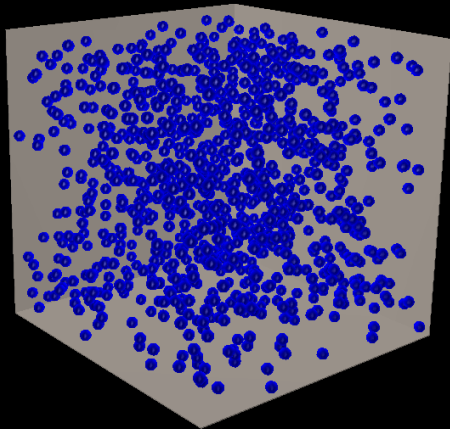
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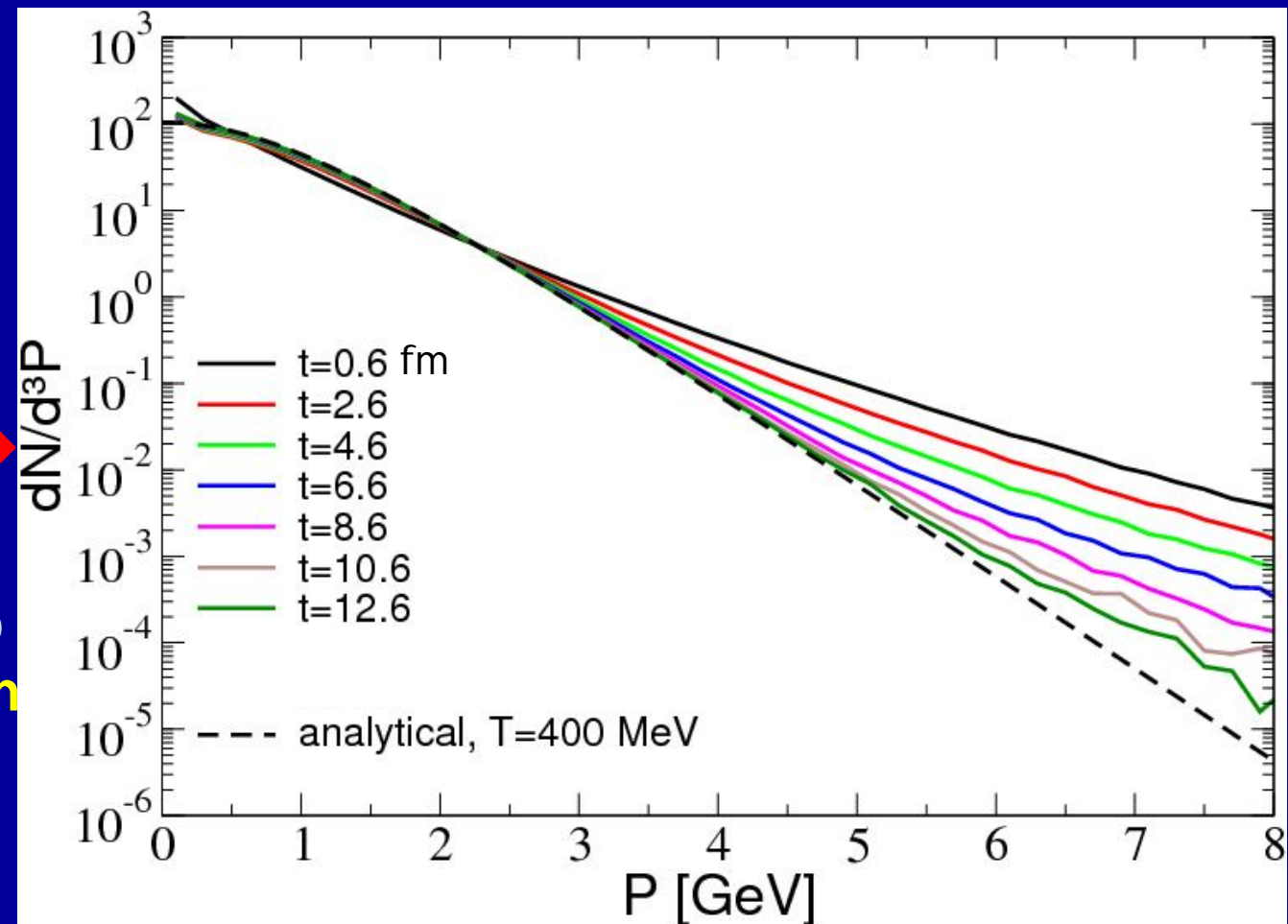


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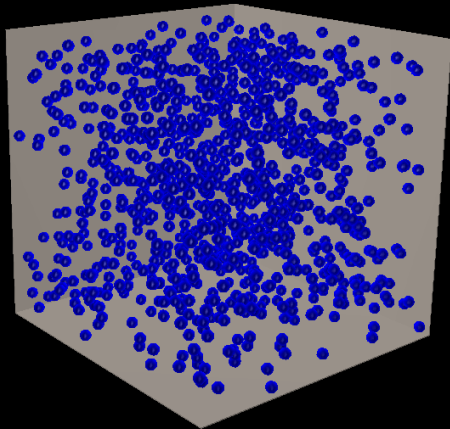
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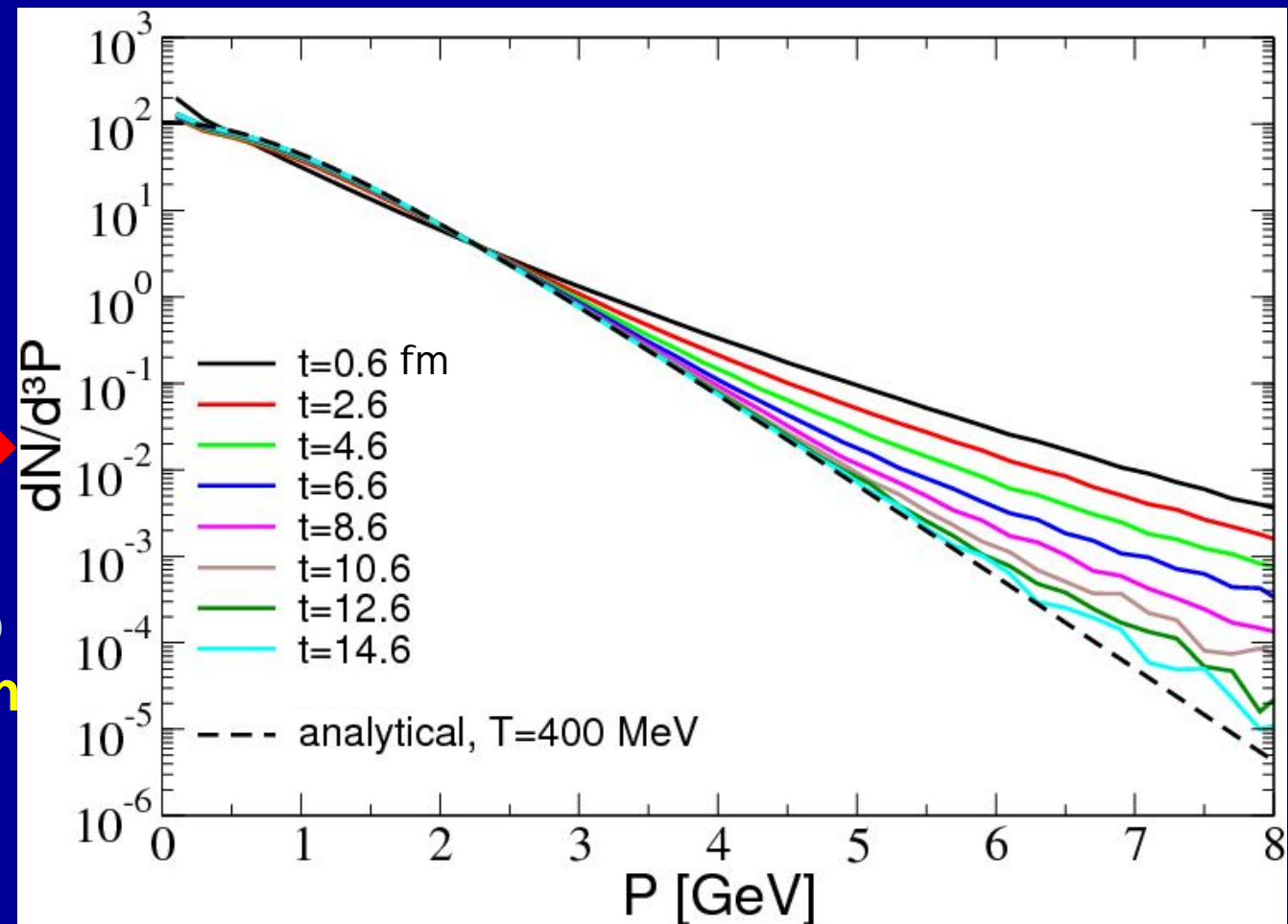


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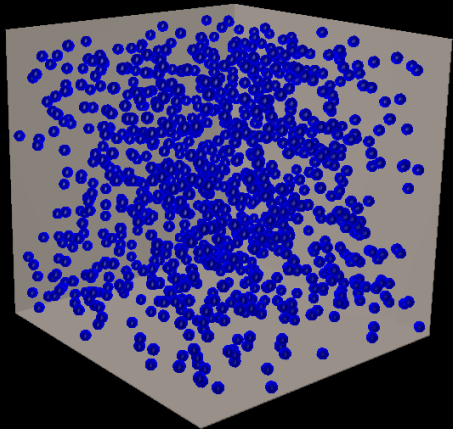
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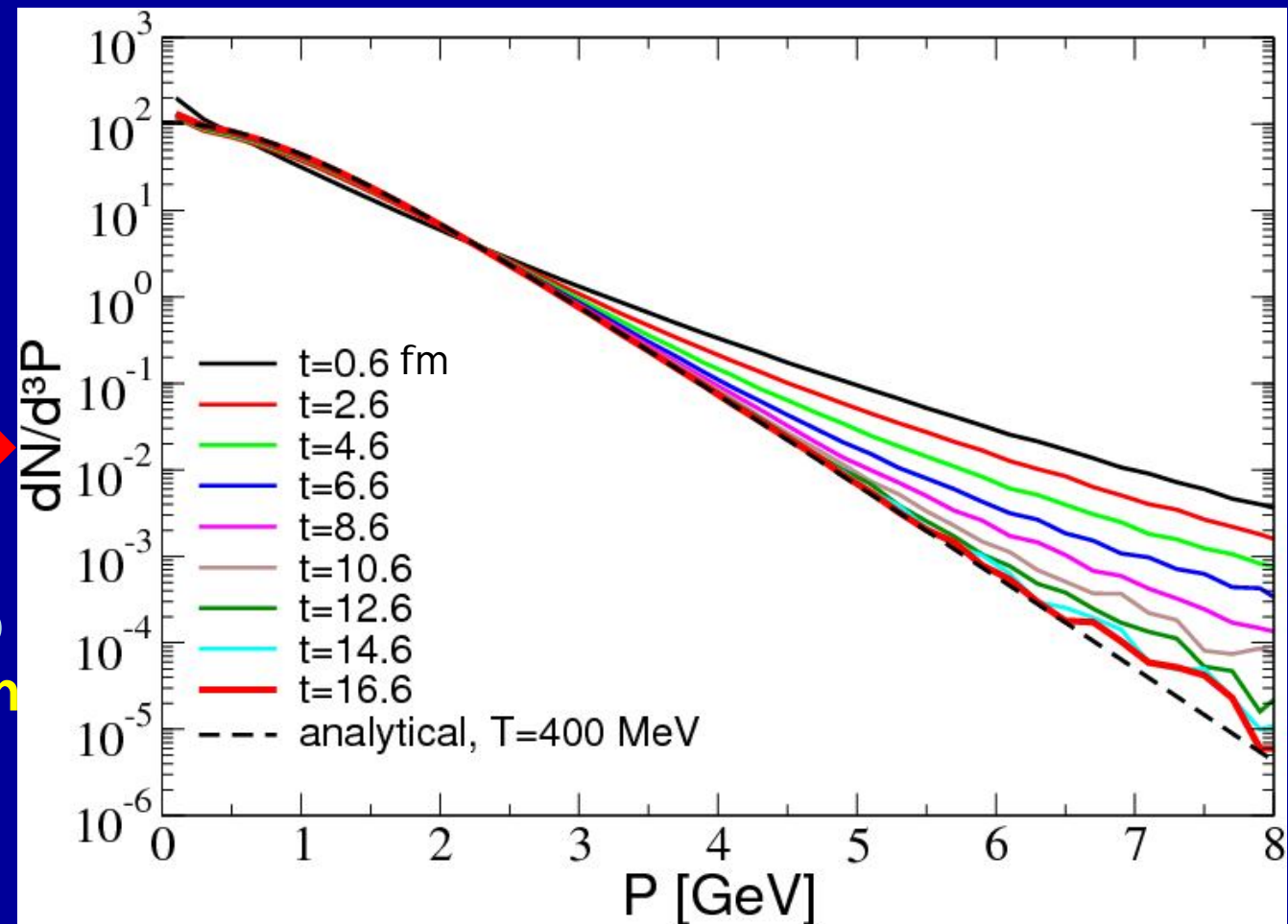


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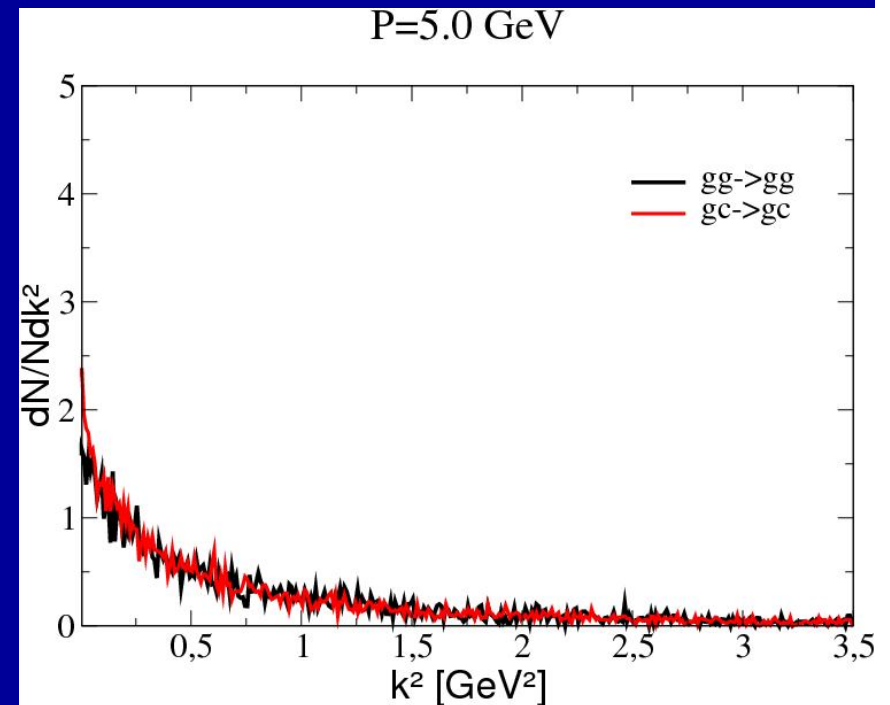
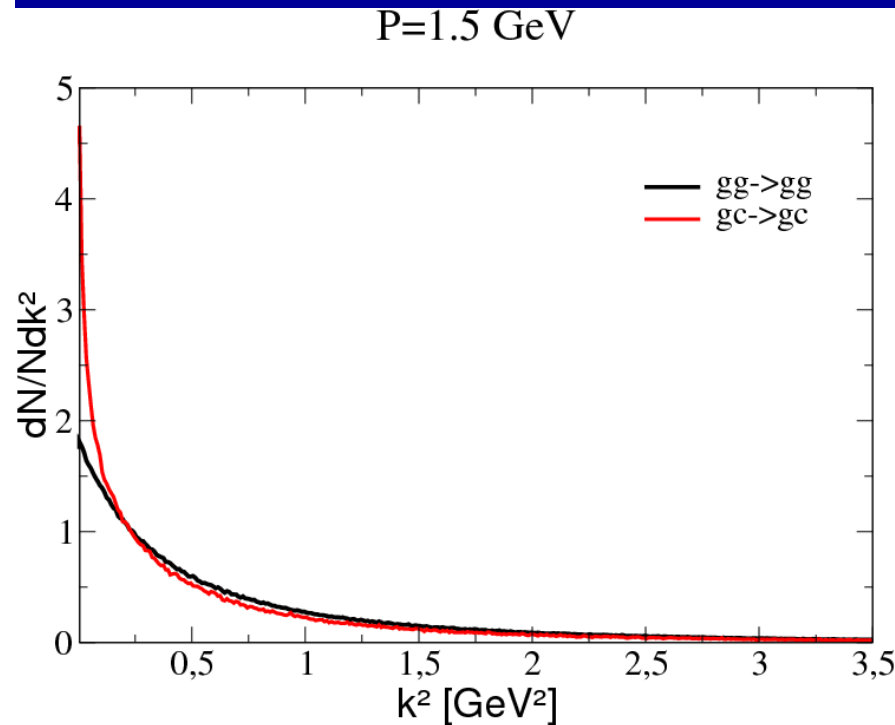
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# Momentum transfer

Distribution of the squared momenta transfer  $k^2$  for fixed momentum  $P$  of the charm



The momenta transfer of  $gg \rightarrow gg$  and  $gc \rightarrow gc$  are not so different