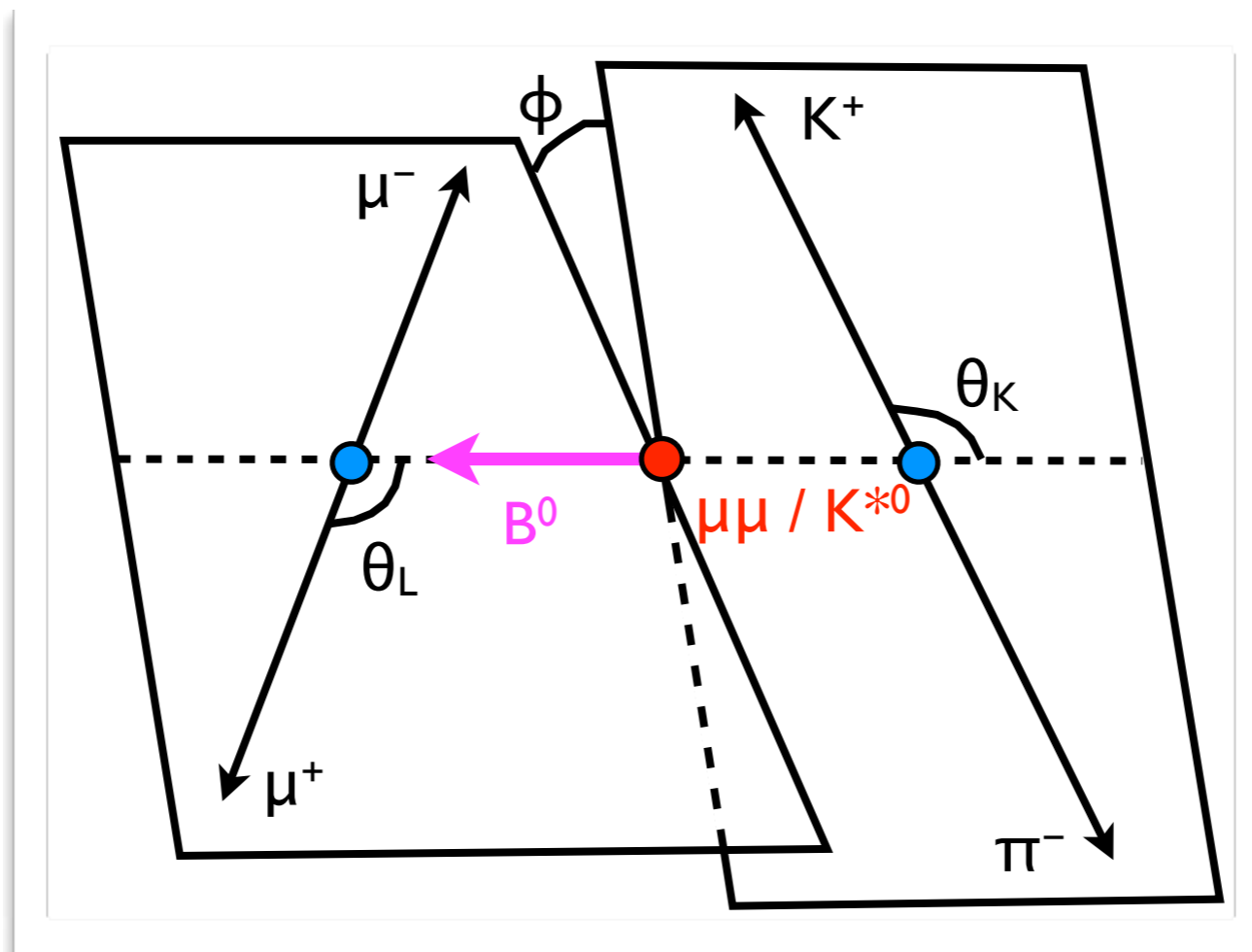


# Angular analysis and differential branching fraction of the decay $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

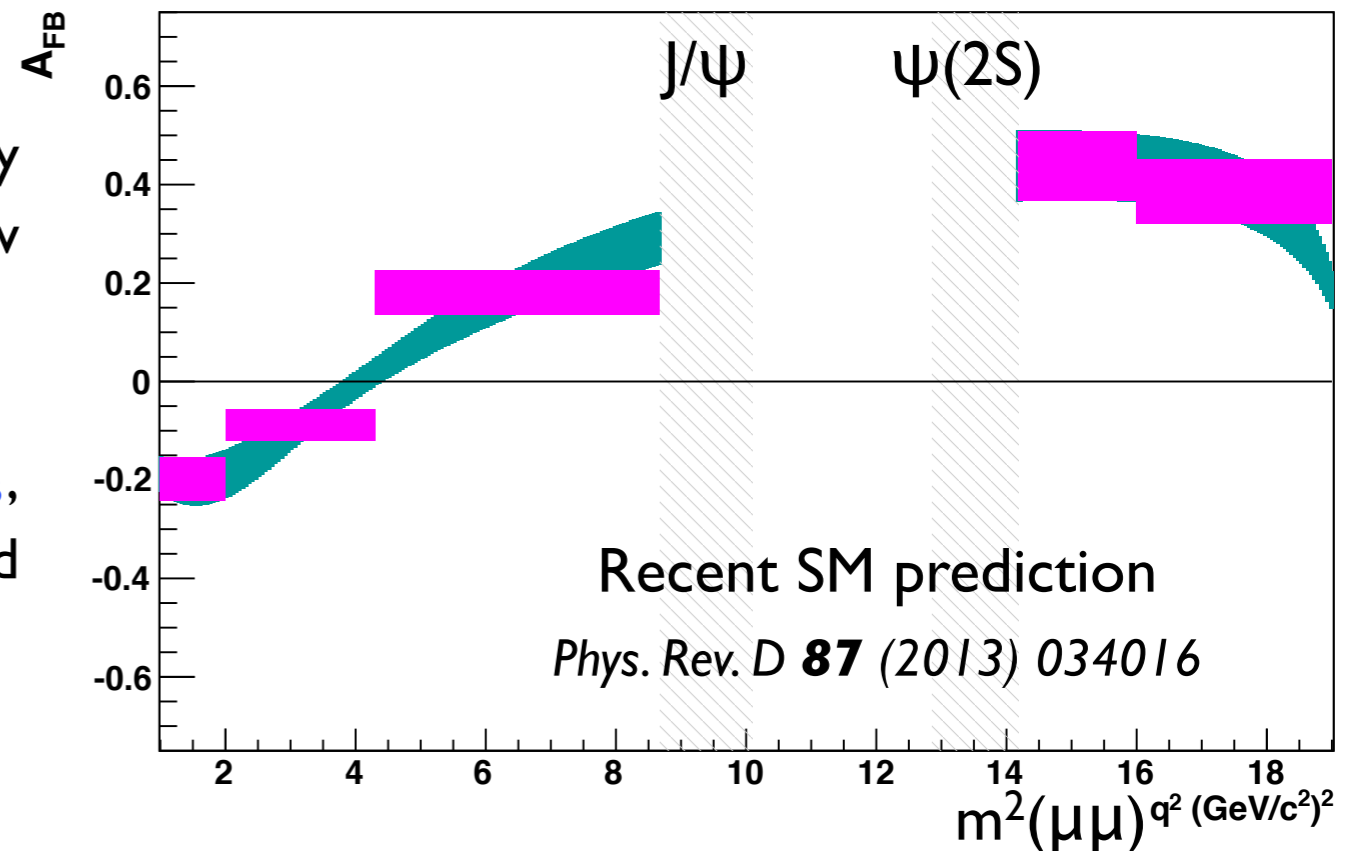
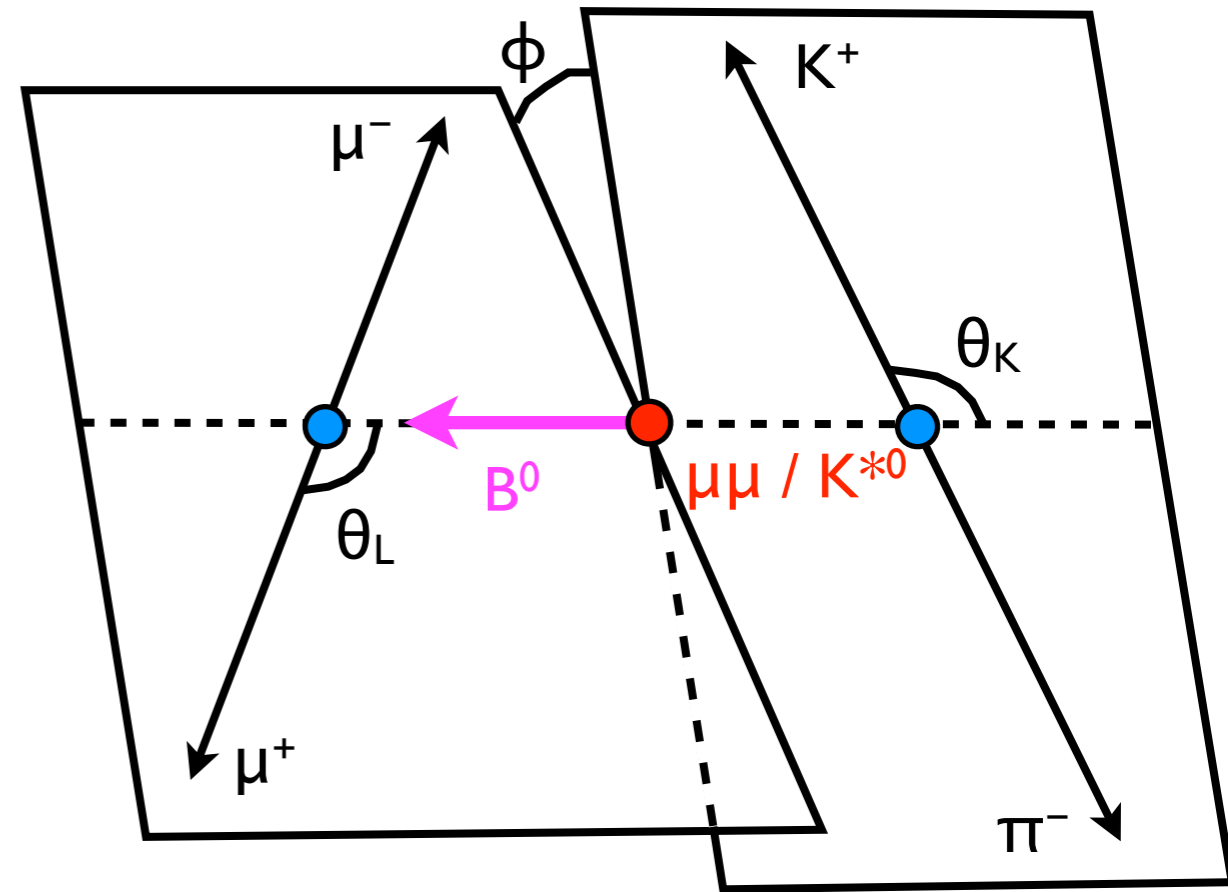


**Mauro Dinardo**

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on behalf of the CMS collaboration

- Introduction
- Event Selection and Signal Evidence
- Fit Strategy
- Systematic Uncertainties
- Analysis Validation with Control Channels
- Measurements
- Comparison with other Experiments
- Conclusions

- $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  described within the SM as flavor changing neutral current process  $\rightarrow$ 
  - (a) small SM rates
  - (b) small theoretical uncertainties
  - (c) new physics predictions that differ from SM
  - (d) experimental accessibility  $\rightarrow$  **good candidate for indirect searches for new phenomena**
- The decay is fully described with three angles ( $\theta_L$ ,  $\theta_K$ ,  $\Phi$ ) and  $q^2 = m^2(\mu\mu)$
- Example of angular observables theoretically predicted with relatively small uncertainties at low  $q^2$ :  $\mu\mu$  forward-backward asymmetry ( $A_{FB}$ )
- **Goal of the analysis:** measure  $A_{FB}$ , longitudinal polarization of  $K^{*0}$  ( $F_L$ ), and differential branching fraction ( $dBF/dq^2$ ) vs  $q^2$



**Remarks:**

- Total collected data:  $\sim 5.2 \text{ fb}^{-1}$  (full 2011 CMS statistics)
- Signal:  $B^0 \rightarrow K^{*0} (K^+\pi^-) \mu^+ \mu^-$
- Two control channels:  $B^0 \rightarrow K^{*0} (K^+\pi^-) J/\psi (\mu^+\mu^-)$  and  $B^0 \rightarrow K^{*0} (K^+\pi^-) \psi(2S) (\mu^+\mu^-)$
- Analysis performed in bins of dimuon mass<sup>2</sup> ( $q^2$ )  $\rightarrow$  control channels are naturally included
- Signal and control channels are treated identically

**Main muon selections:**

- events recorded with dimuon low-mass, vertex displaced trigger
- $\mu\mu$  vertex  $L / 3\sigma$  (transverse) (in trigger)
- $1 < m(\mu\mu) < 4.8 \text{ GeV}/c^2$  (in trigger)
- $p_T(\mu) > 3, 4, 4.5, 5 \text{ GeV}/c$  (depending on trigger)
- $\mu\mu$  vertex CL  $> 5\%, 15\%$  (depending on trigger)

 **$B^0$  selections:**

- $B^0$  vertex CL  $> 9\%$
- $B^0$  vertex  $L / 12\sigma$  (transverse)
- $\cos(\alpha) > 0.9994$ :  $\alpha$  angle in transverse plane between  $B^0$  momentum and line-of-flight

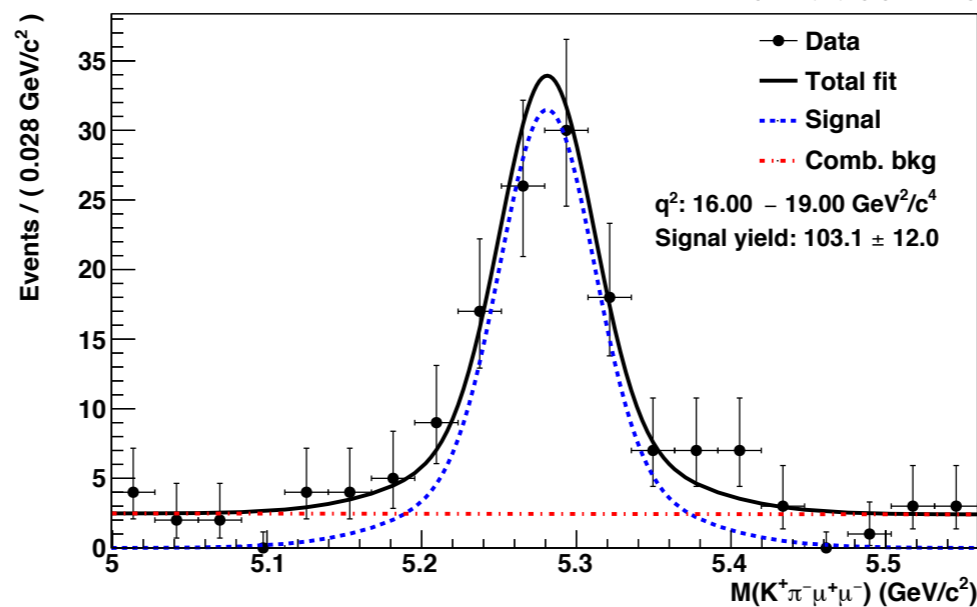
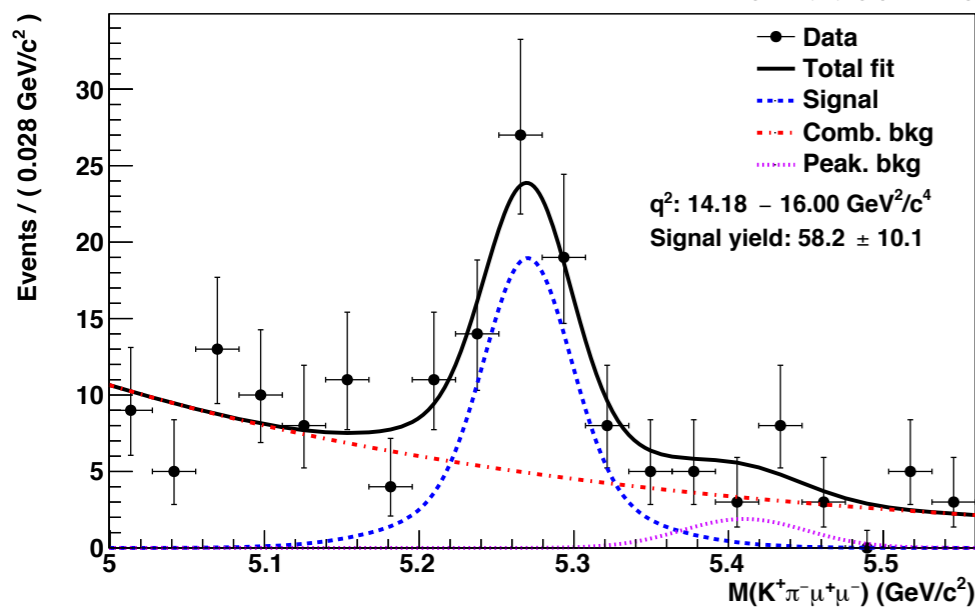
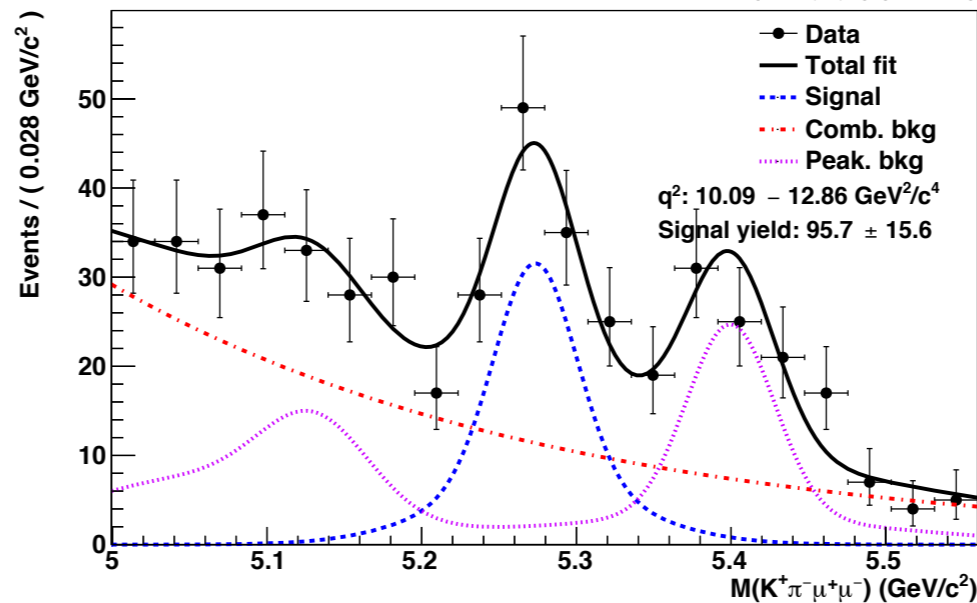
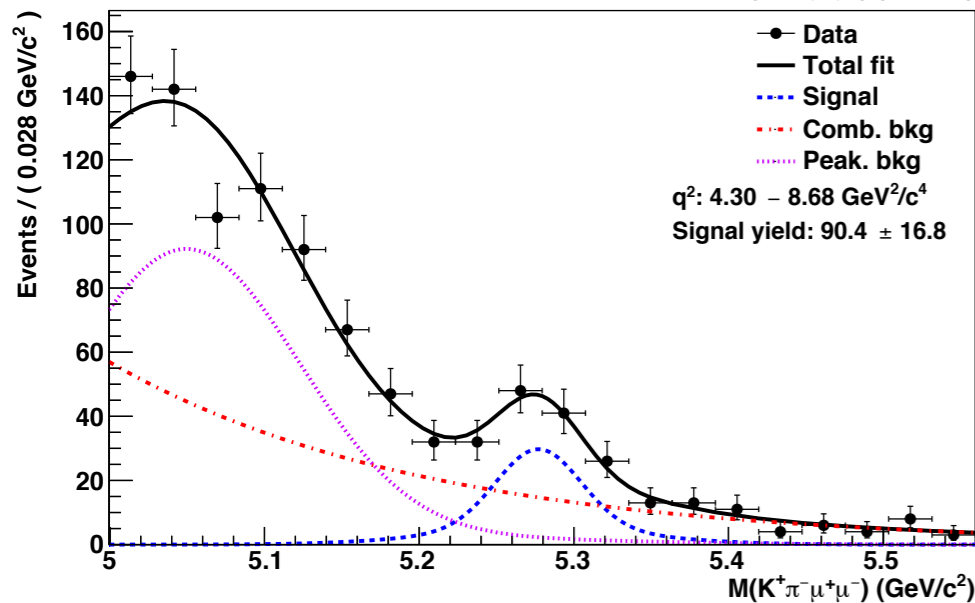
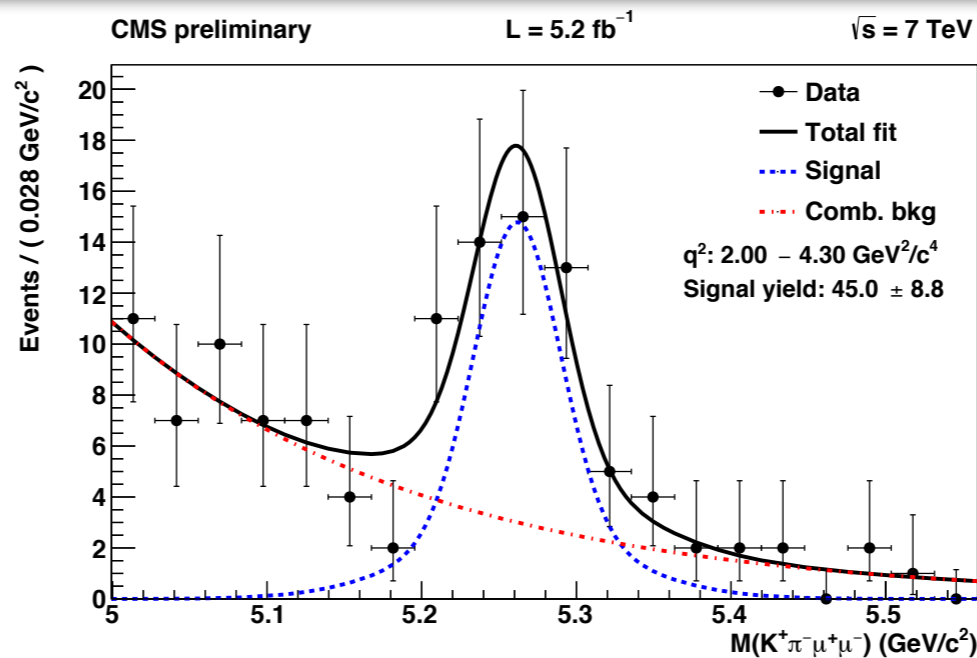
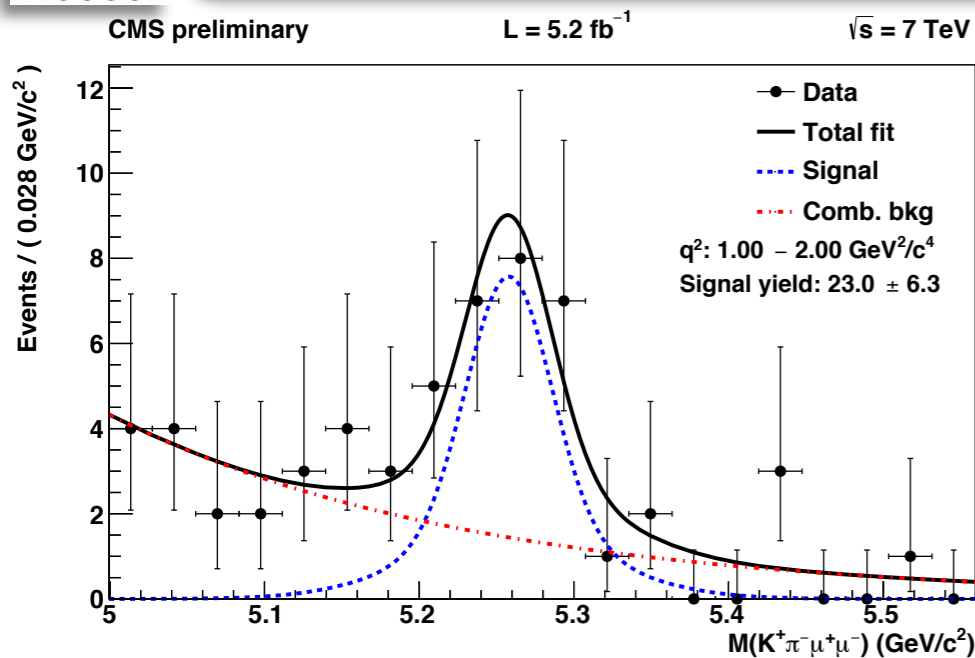
**Hadron selections:**

- hadron must fail muon ID
- $p_T(h) > 0.75 \text{ GeV}/c$
- Distance Closest Approach(h) /  $1.3\sigma$  (transverse)
- $|m(K\pi) - m_{\text{PDG}}K^{*0}| < 80 \text{ MeV}/c^2$

**CP state assignment:**

1. Reject event if both  $K^{*0}$  and  $\bar{K}^{*0}$  masses are within  $50 \text{ MeV}/c^2$  of PDG mass ( $\sim 1\Gamma$ )
2. Tag the CP state based on closest distance from  $K^{*0}$  PDG mass

Mistag rate evaluated on MC  $\sim 8\%$  and on data  $\sim 10\%$



• Signal

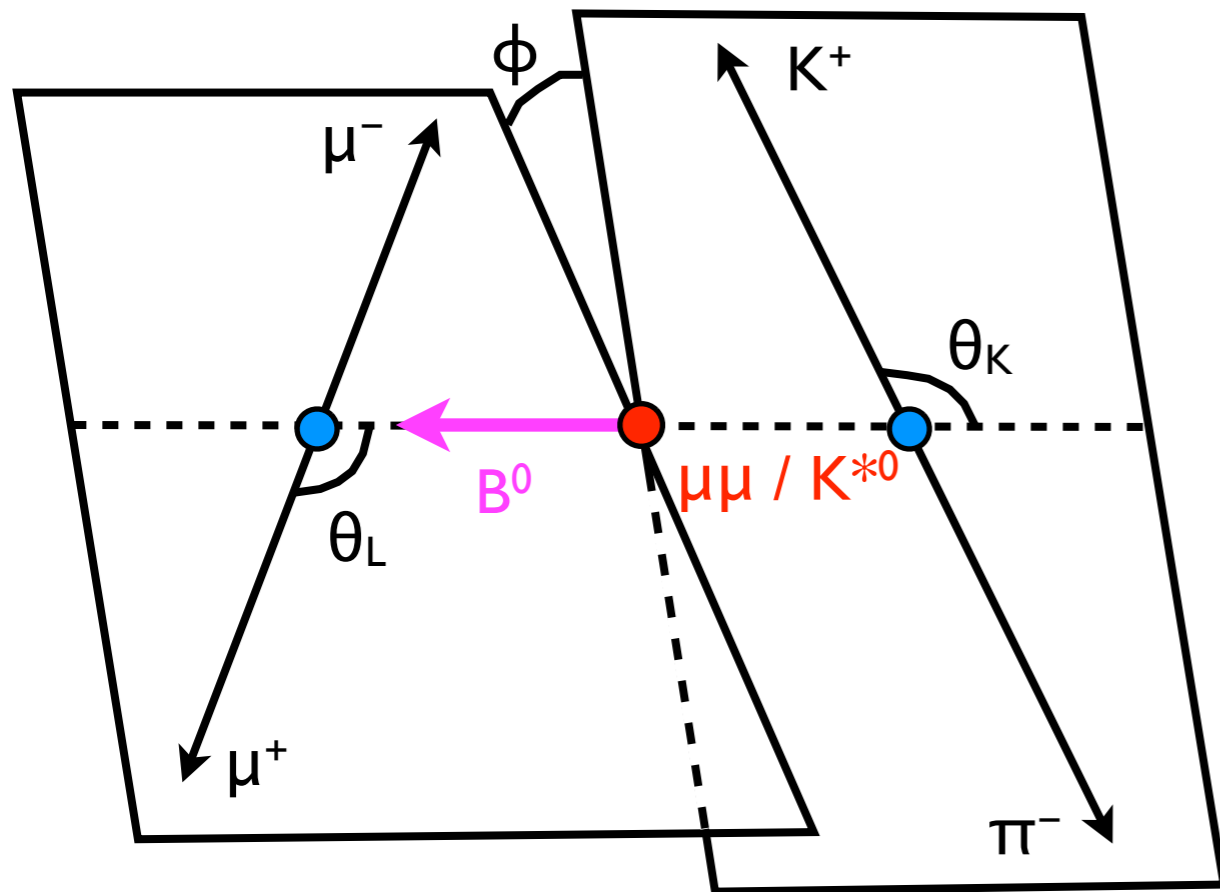
• Combinatorial background: random association hadrons-muons

• Peaking background: feed-through from resonant channels

- We perform unbinned extended maximum likelihood fits to three variables:  $B^0$  invariant mass and two angular variables  $\theta_K$  and  $\theta_l$  for each  $q^2$  bin to extract  $F_L(q^2)$  and  $A_{FB}(q^2)$

$$\frac{1}{\Gamma} \frac{d^3\Gamma}{d \cos \theta_k d \cos \theta_l dq^2} = \frac{9}{16} \left\{ \left[ \frac{2}{3} F_S + \frac{4}{3} A_S \cos \theta_k \right] (1 - \cos^2 \theta_l) + (1 - F_S) \left[ 2F_L \cos^2 \theta_k (1 - \cos^2 \theta_l) + \frac{1}{2} (1 - F_L) (1 - \cos^2 \theta_k) (1 + \cos^2 \theta_l) + \frac{4}{3} A_{FB} (1 - \cos^2 \theta_k) \cos \theta_l \right] \right\}$$

The full decay rate is weakly dependent on the  $\Phi$  angle, therefore integrated in this analysis



- Using previous fit results, unbinned extended maximum likelihood fits to  $B^0$  invariant mass is used for each  $q^2$  bin to extract  $dBF/q^2(q^2)$

$$\frac{dBF}{dq^2} = \frac{Y_S \epsilon_N BF[B^0 \rightarrow K^{*0} (K^+\pi^-) J/\psi (\mu^+\mu^-)]}{Y_N \epsilon_S dq^2}$$

- In small fraction (few %) of decays  $K\pi$  are in  $S$ -wave state (*BaBar: Phys. Rev. D* **76** (2007) 031102)
- We are interested in decays where  $K\pi$  are in  $P$ -wave
- In our p.d.f. the decay rate describes both  $P$  and  $S$  wave, together with their interference

$$\frac{1}{\Gamma} \frac{d^3\Gamma}{d \cos \theta_k d \cos \theta_l dq^2} = \frac{9}{16} \left\{ \left[ \frac{2}{3} F_S + \frac{4}{3} A_S \cos \theta_k \right] (1 - \cos^2 \theta_l) \right. \\ + (1 - F_S) \left[ 2F_L \cos^2 \theta_k (1 - \cos^2 \theta_l) \right. \\ + \frac{1}{2} (1 - F_L) (1 - \cos^2 \theta_k) (1 + \cos^2 \theta_l) \\ \left. \left. + \frac{4}{3} A_{FB} (1 - \cos^2 \theta_k) \cos \theta_l \right] \right\}$$

- **$F_S$** : fraction of  $S$ -wave
- **$A_S$** : forward-backward asymmetry of kaons

**$F_S$**  and  **$A_S$**  are determined from  $B^0 \rightarrow K^{*0} (K^+\pi^-) J/\psi (\mu^+\mu^-)$  channel and fixed, with Gaussian constraints, for non-resonant  $q^2$  bins



$$\text{p.d.f.}_i = \text{Kernel}_i \cdot \text{Penalty}_i =$$

$$(\mathbf{Y} \cdot \mathbf{S}^M(\mathbf{m}) \cdot \mathbf{S}^A(\theta_K, \theta_I) \cdot \varepsilon(\theta_K, \theta_I) +$$

$$+ \mathbf{Y} \cdot \mathbf{B}^M(\mathbf{m}) \cdot \mathbf{B}^K(\theta_K) \cdot \mathbf{B}^I(\theta_I) +$$

$$+ \mathbf{Y} \cdot \mathbf{B}^M(\mathbf{m}) \cdot \mathbf{B}^K(\theta_K) \cdot \mathbf{B}^I(\theta_I))_i \cdot \text{Penalty}_i$$

Index  $i$  run on  $q^2$  bins

### Peaking background:

$\mathbf{Y}$  from data

### $\mathbf{B}^M(\mathbf{m})$ from MC:

- 1 or 2 single/double Gaussians

### $\mathbf{B}^K(\theta_K) \cdot \mathbf{B}^I(\theta_I)$ from MC:

- polynomials

### Signal:

$\mathbf{Y}$  from data

### $\mathbf{S}^M(\mathbf{m})$ :

- double Gaussian → from MC

### $\mathbf{S}^A(\theta_K, \theta_I)$ : decay rate

- polynomials → from theory & data

### $\varepsilon(\theta_K, \theta_I)$ : efficiency

- polynomials → fixed from MC

### Combinatorial background:

$\mathbf{Y}$  from data

### $\mathbf{B}^M(\mathbf{m})$ from data:

- single exponential

### $\mathbf{B}^K(\theta_K) \cdot \mathbf{B}^I(\theta_I)$ from data:

- polynomials

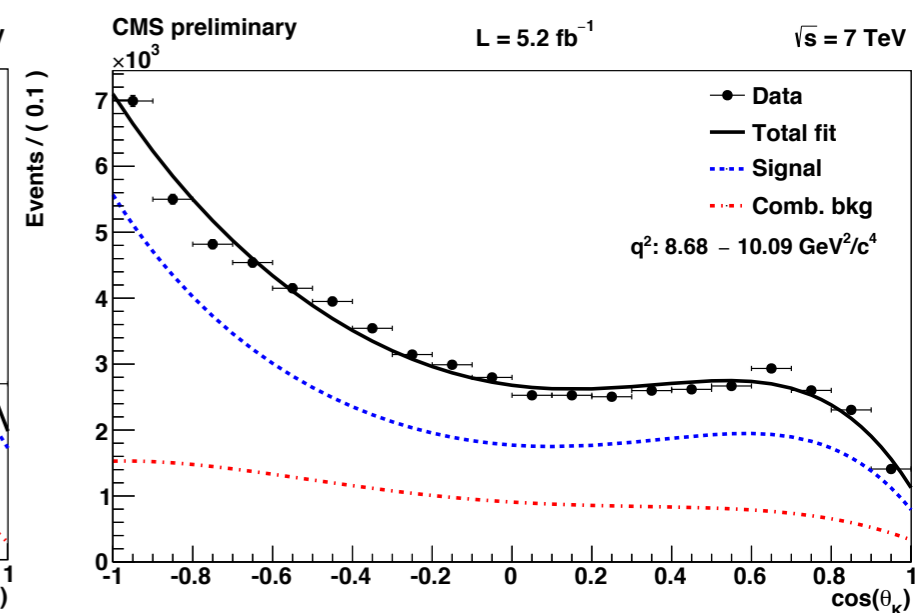
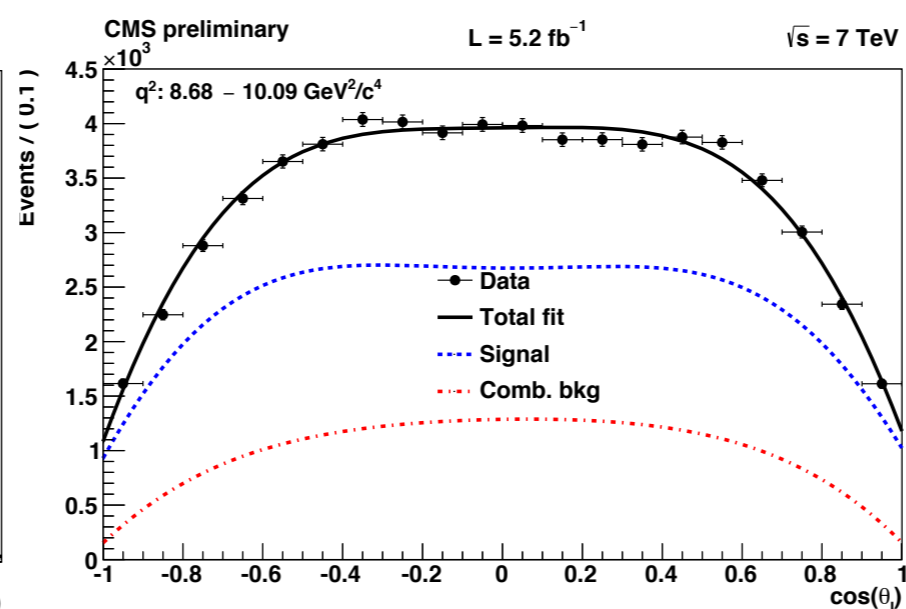
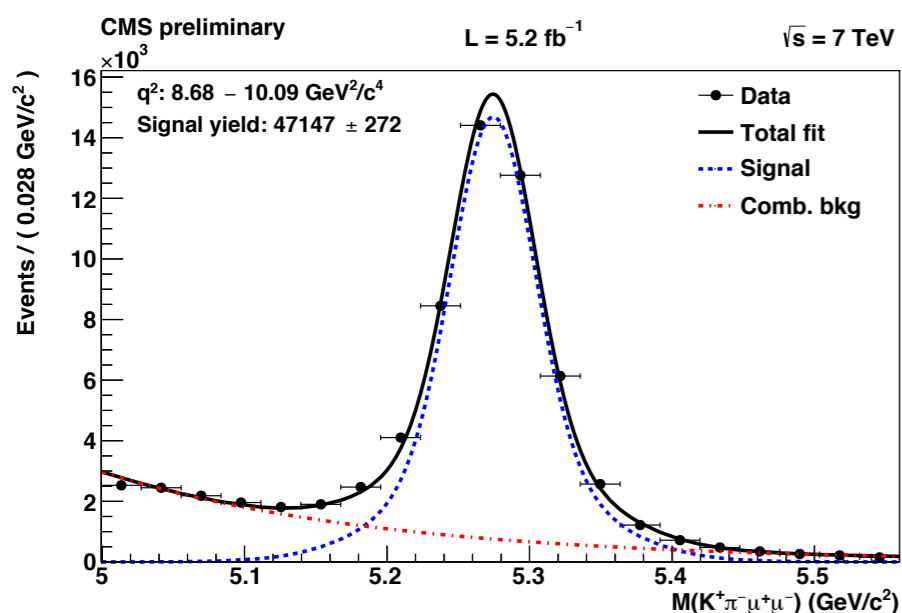
- The kernel p.d.f. is multiplied by Gaussian **penalty terms** for the parameters determined **from MC**
- Final fit ALL parameters are free



<b>Sources of systematic uncertainty</b>	<b><math>F_L</math></b>	<b><math>A_{FB}</math></b>	<b><math>dBF/dq^2</math></b>
Potential bias from fit ingredients	0	0–0.017	0–7.1%
Test of $\Gamma(B^0 \rightarrow K^{*0}J/\psi) / \Gamma(B^0 \rightarrow K^{*0}\psi(2S))$	0	0	14.3%
Potential bias from fit algorithm (toy MC)	0.004–0.040	0.012–0.077	0–2.7%
Incorrect CP assignment of decay	0.002–0.006	0.002–0.006	0%
Effect of $K\pi$ S-wave contribution	0.005–0.023	0.006–0.014	5%
Peaking background mass shape	0–0.026	0–0.008	0–15.2%
Combinatorial background shape vs $\cos(\theta_{K/l})$	0.003–0.179	0.004–0.161	0–3.3%
Angular resolution	0–0.019	0	0
Signal mass shape	0	0	0.9%
Statistical uncertainty of simulated events	0.005–0.007	0.003–0.005	1%
<b>Total systematic uncertainty</b>	<b>0.027–0.185</b>	<b>0.018–0.179</b>	<b>15.5–21.5%</b>

**The uncertainty is dominated by the statistical error** (see next slides)

## $B^0 \rightarrow K^{*0} (K^+\pi^-) J/\psi (\mu^+\mu^-)$



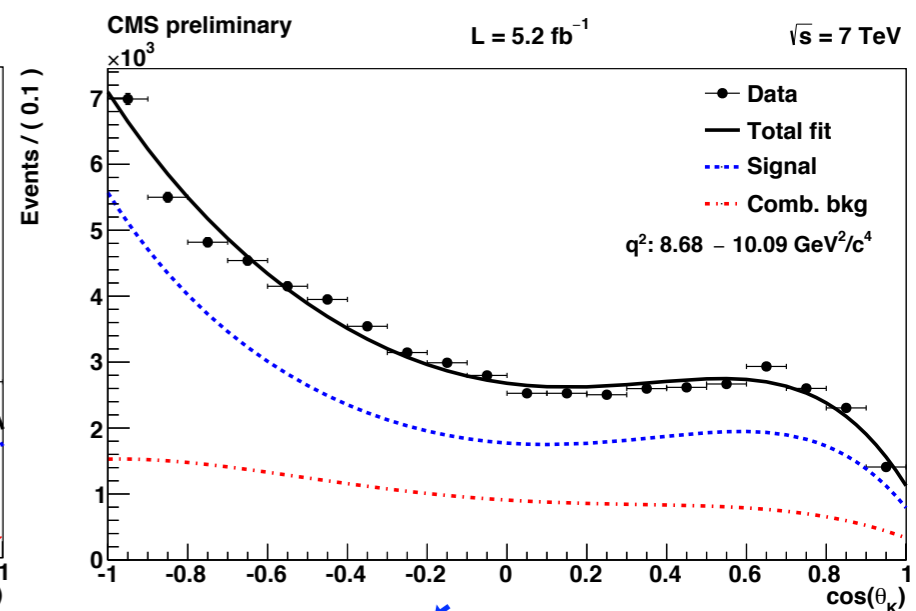
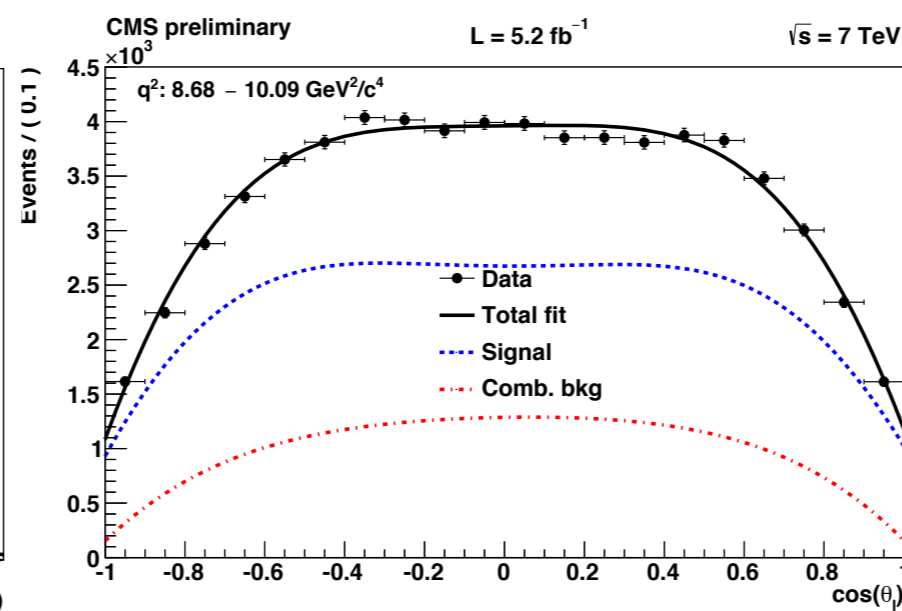
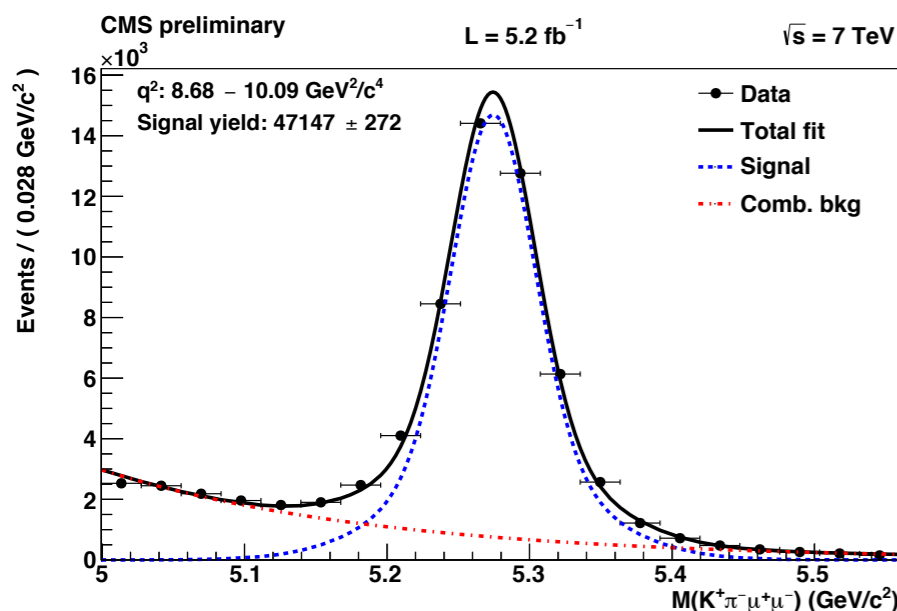
## $B^0 \rightarrow K^{*0} (K^+\pi^-) J/\psi (\mu^+\mu^-)$

- **$F_L$** :  $0.554 \pm 0.004$  (stat)  $\rightarrow$  PDG value  $0.570 \pm 0.008$
- **$A_{FB}$** :  $-0.004 \pm 0.004$  (stat)  $\rightarrow$  compatible with zero

## $B^0 \rightarrow K^{*0} (K^+\pi^-) \psi(2S) (\mu^+\mu^-)$

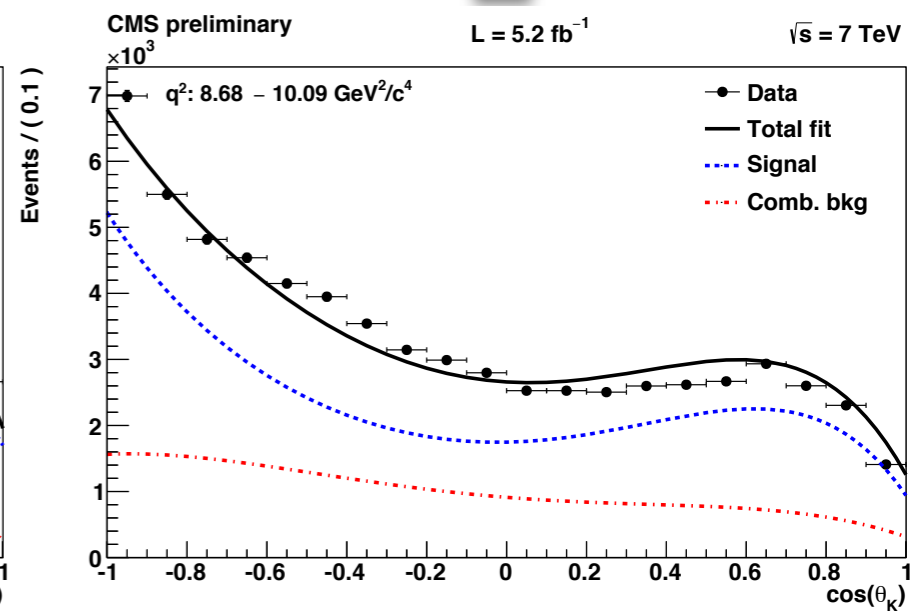
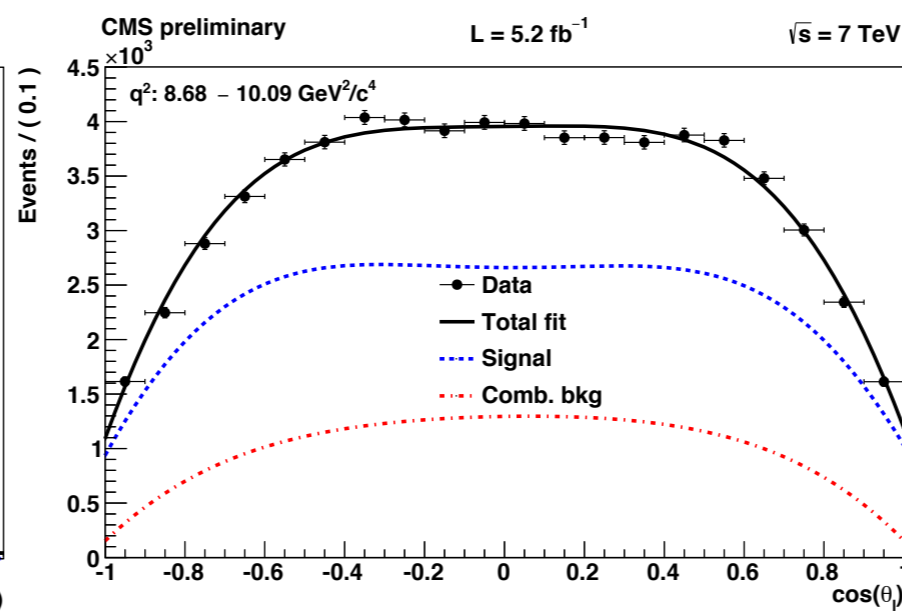
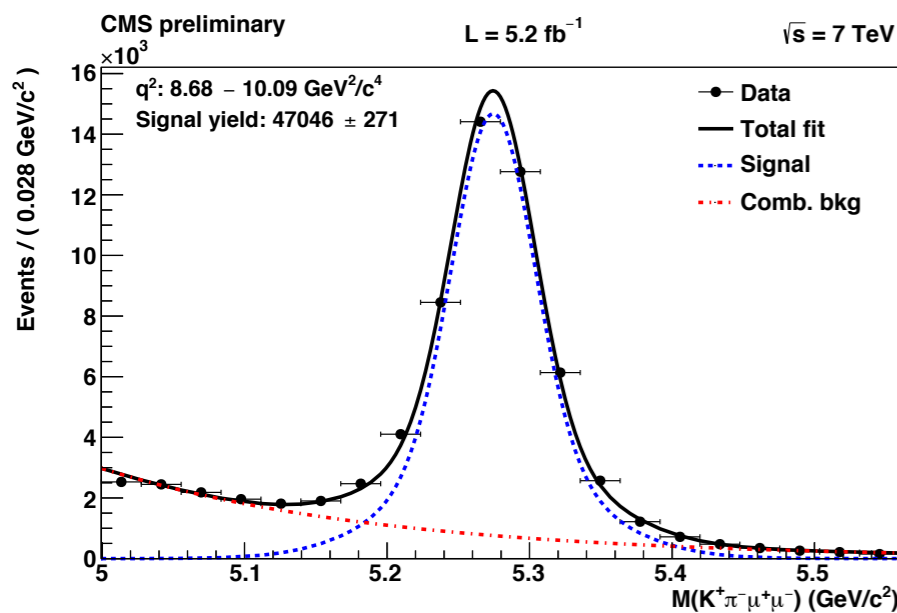
- **$F_L$** :  $0.509 \pm 0.016$  (stat)  $\rightarrow$  PDG value  $0.46 \pm 0.04$
- **$A_{FB}$** :  $0.013 \pm 0.014$  (stat)  $\rightarrow$  compatible with zero

## $B^0 \rightarrow K^{*0} (K^+\pi^-) J/\psi (\mu^+\mu^-)$

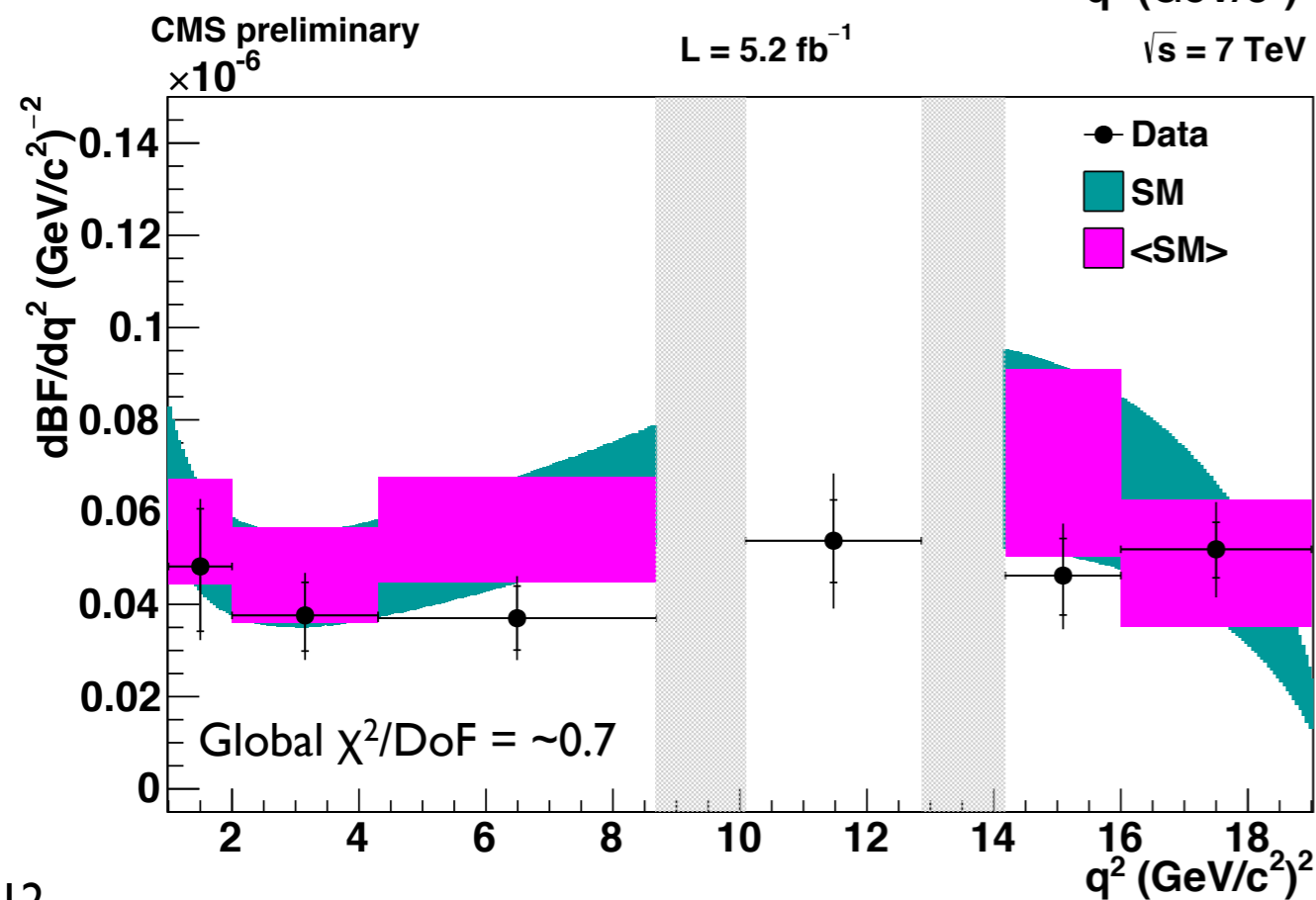
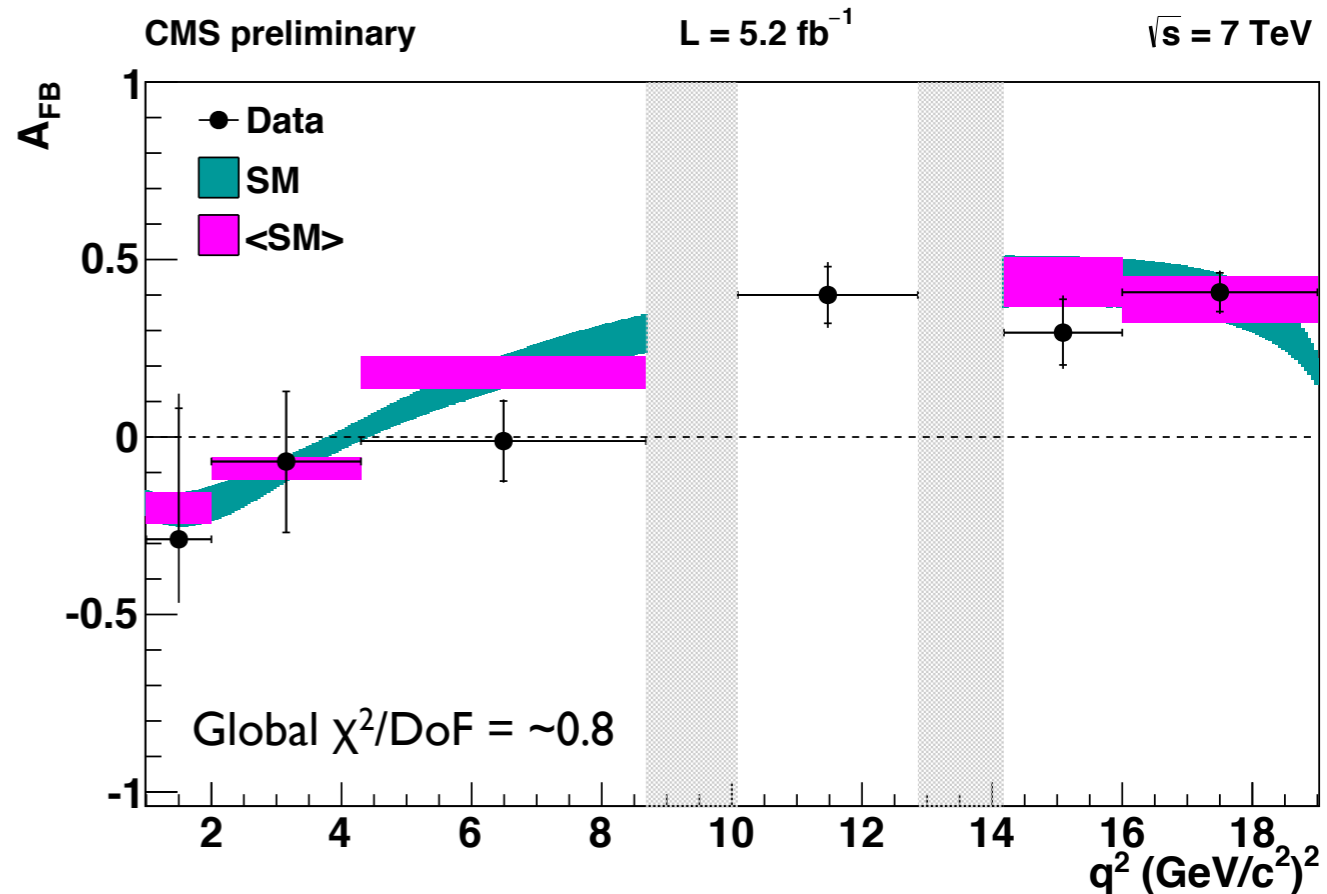
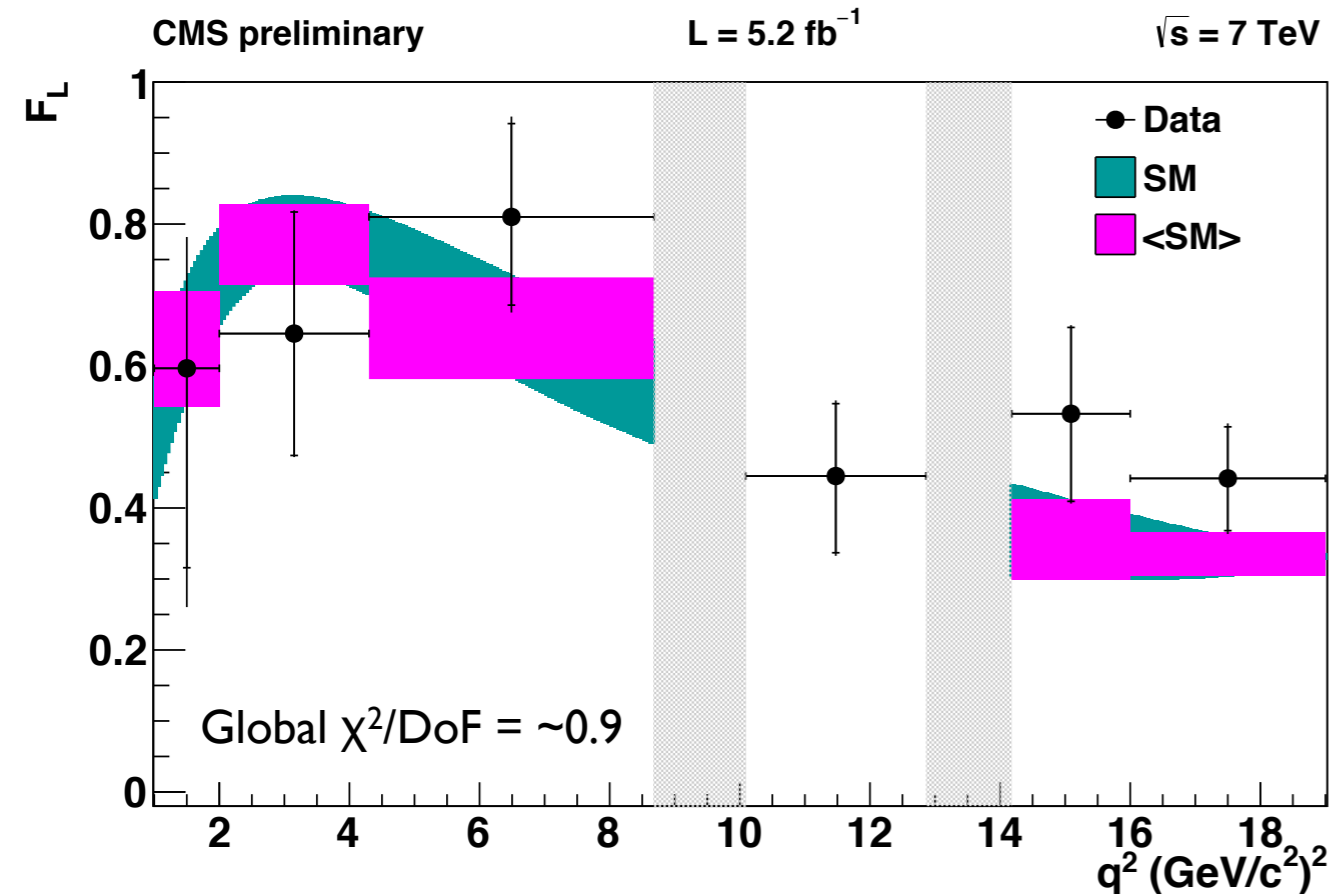


Fit performed considering both vector and scalar  $K\pi$  contributions

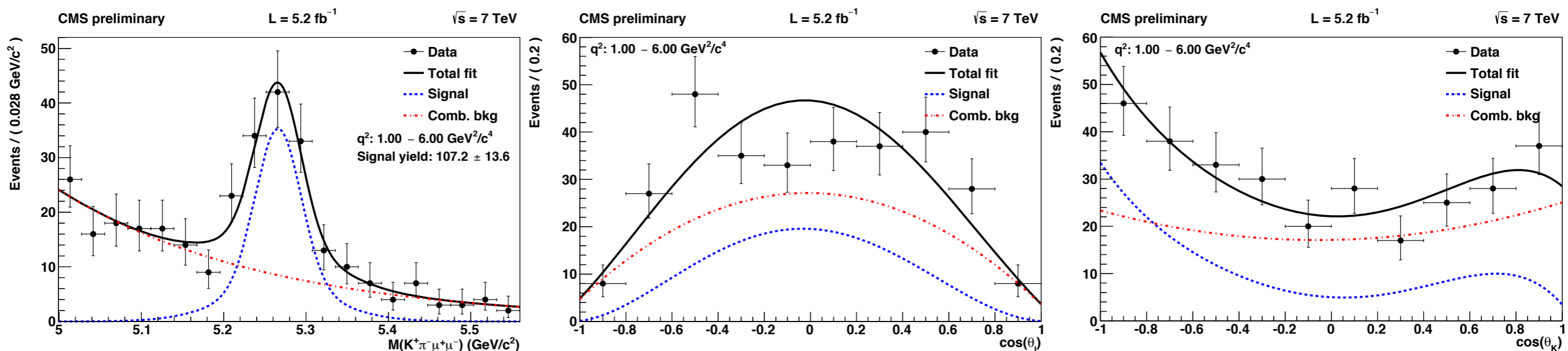
Clear improvement



Fit performed ignoring the scalar  $K\pi$  contribution



- Error bars with edges: statistical uncertainty
- Edgeless error bars: total uncertainty
- Purple region: standard model properly averaged over the bin (Phys. Rev. D **87** (2013) 034016)



## CMS measurements:

- **$F_L$ :**  $0.68 \pm 0.10$  (stat)  $\pm 0.02$  (syst)
- **$A_{FB}$ :**  $-0.07 \pm 0.12$  (stat)  $\pm 0.01$  (syst)
- **$dBF/dq^2$ :**  $(4.4 \pm 0.6$  (stat)  $\pm 0.7$  (syst))  $\times 10^{-8} \text{ c}^4/\text{GeV}^2$

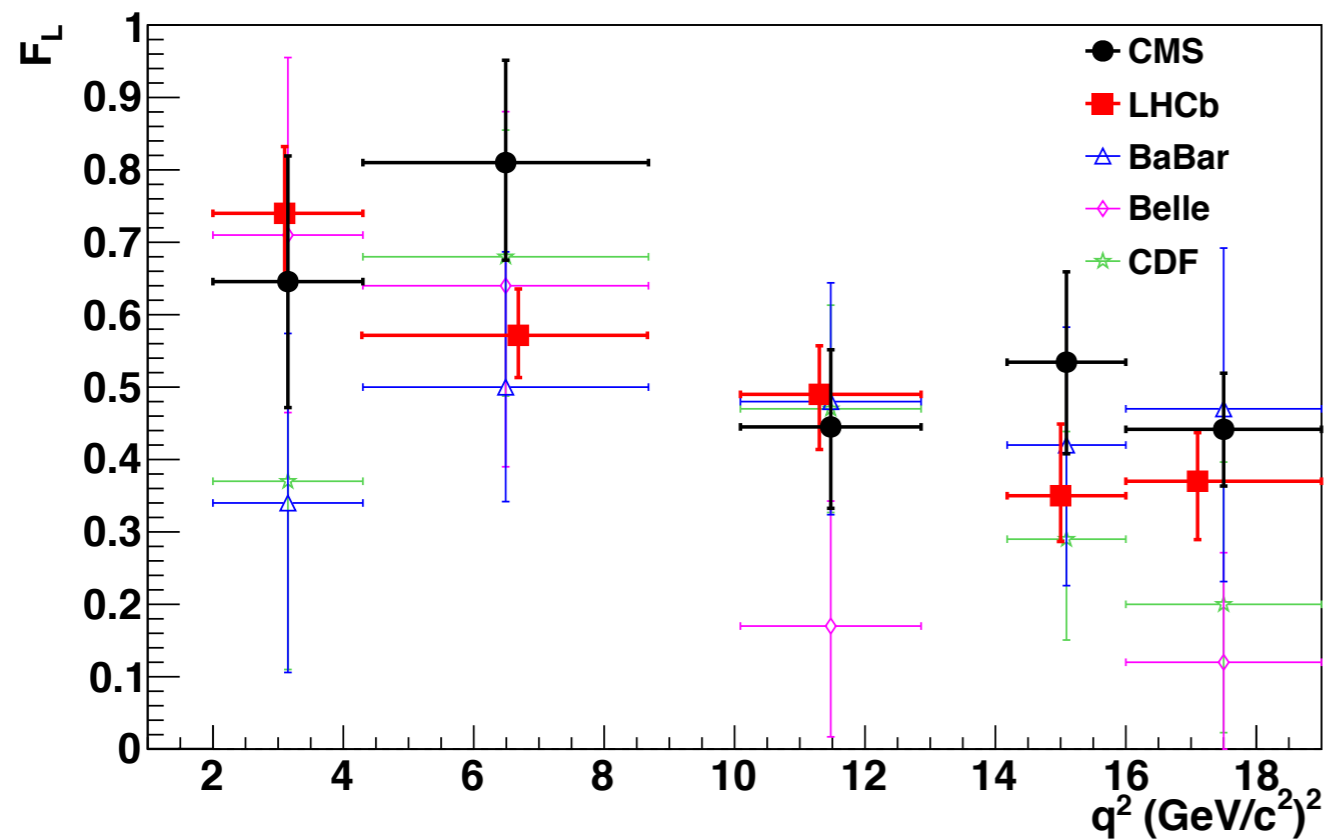
## SM predictions (*Phys. Rev. D* **87** (2013) 034016):

- **$F_L$ :**  $0.74 + 0.06 - 0.07$
- **$A_{FB}$ :**  $-0.04 \pm 0.03$
- **$dBF/dq^2$ :**  $(4.9 + 1.0 - 1.1) \times 10^{-8} \text{ c}^4/\text{GeV}^2$

CMS preliminary

$L = 5.2 \text{ fb}^{-1}$

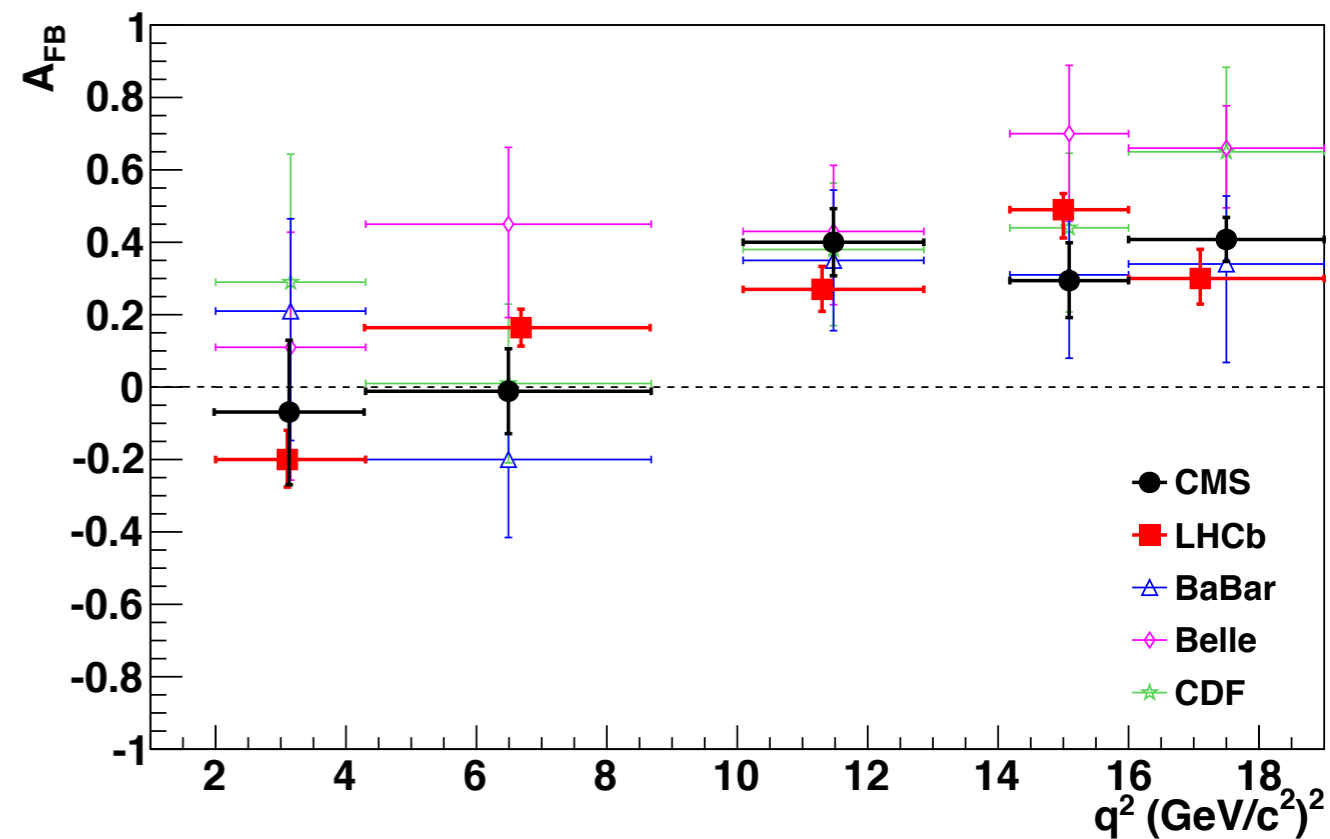
$\sqrt{s} = 7 \text{ TeV}$



CMS preliminary

$L = 5.2 \text{ fb}^{-1}$

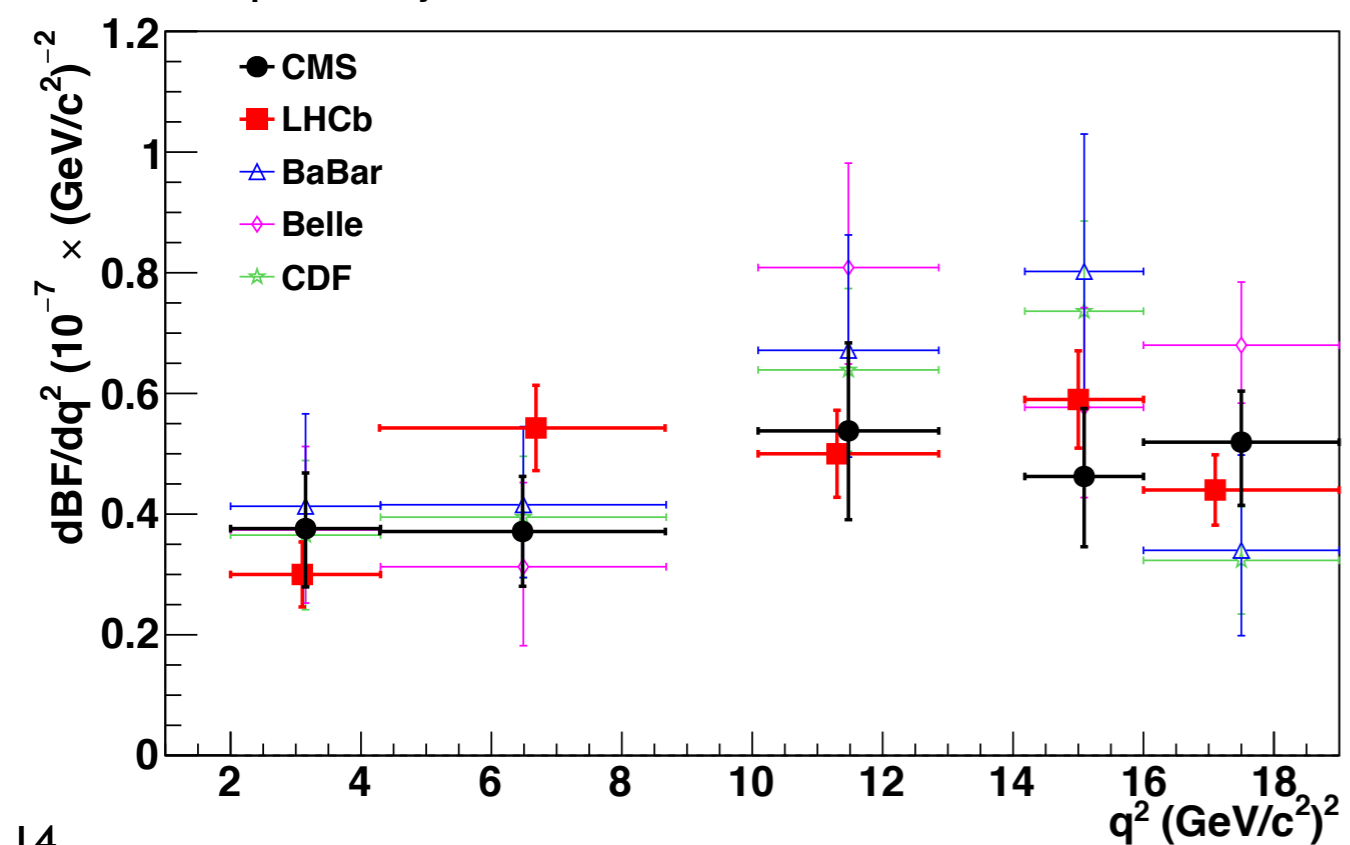
$\sqrt{s} = 7 \text{ TeV}$



CMS preliminary

$L = 5.2 \text{ fb}^{-1}$

$\sqrt{s} = 7 \text{ TeV}$



- CMS uncertainties are better than CDF, Belle, BaBar but not as good as LHCb (LHCb statistics:  $\sim 1 \text{ fb}^{-1}$ )
- CMS measurements are the second best

- BaBar: *Phys. Rev. D* **79** (2009) 031102
- Belle: *Phys. Rev. Lett.* **103** (2009) 171801
- CDF: *Phys. Rev. Lett.* **108** (2012) 081807
- LHCb: *Phys. Rev. Lett.* **108** (2012) 181806



- We performed an angular analysis of  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ , using  $\sim 5.2 \text{ fb}^{-1}$  of data (2011)
- More than 400 signal (non-resonant) decays and nearly 50 000 normalization mode decays ( $B^0 \rightarrow K^{*0} J/\psi$ ) are observed
- Unbinned maximum likelihood fits were performed in bins of dimuon invariant mass squared ( $q^2$ ) with three independent variables:  $B^0$  invariant mass,  $\cos(\theta_K)$ , and  $\cos(\theta_l)$  to obtain values of forward-backward asymmetry of the muons,  $A_{FB}$ , and fraction of longitudinal polarization of the  $K^{*0}$ ,  $F_L$
- Using these results, unbinned maximum likelihood fits to  $B^0$  invariant mass in  $q^2$  bins were used to extract differential branching fraction,  $dBF/dq^2$
- **No deviations from the standard model predictions are found**
- Results with 2011 data are statistically limited  $\rightarrow$  analysis of the 2012 data is starting, with significantly more statistics  $\sim 20 \text{ fb}^{-1}$

**Documentation:**

- Physics Analysis Summary: CMS-PAS-2011/009
- Public web page: <https://twiki.cern.ch/twiki/bin/view/CMSPublic/PhysicsResultsBPH11009>



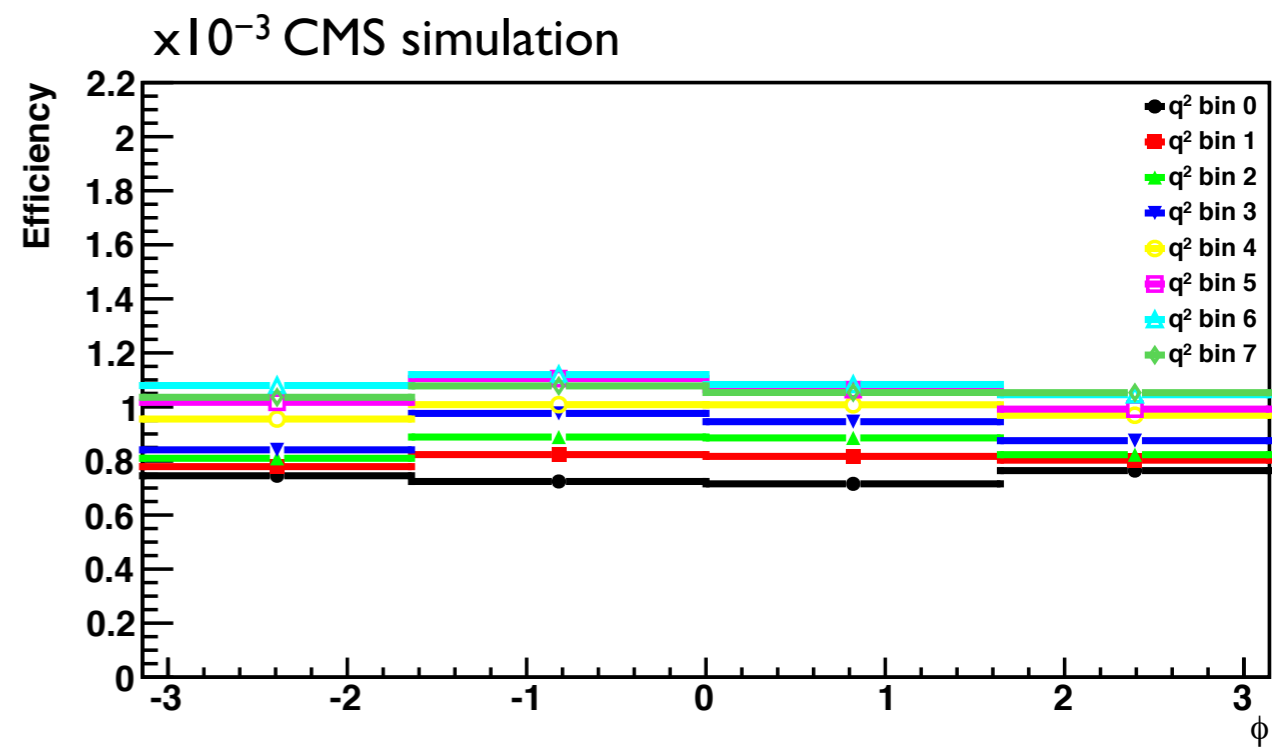
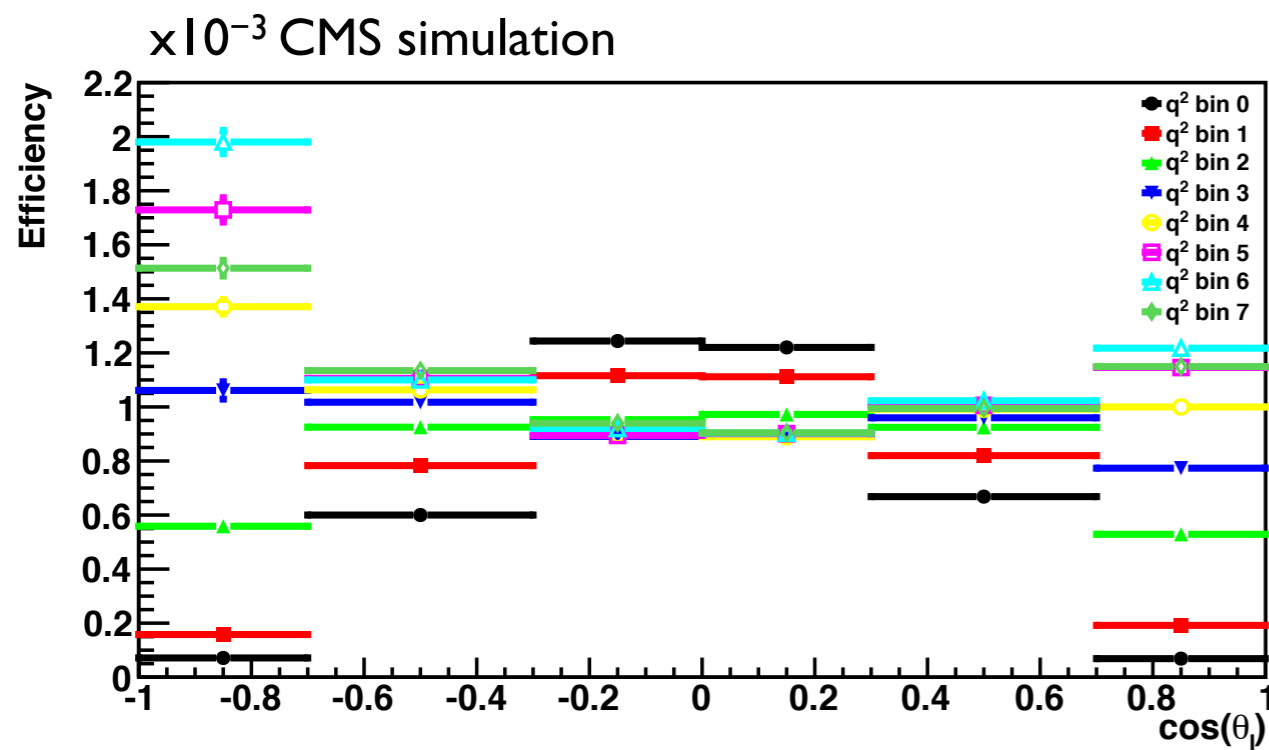
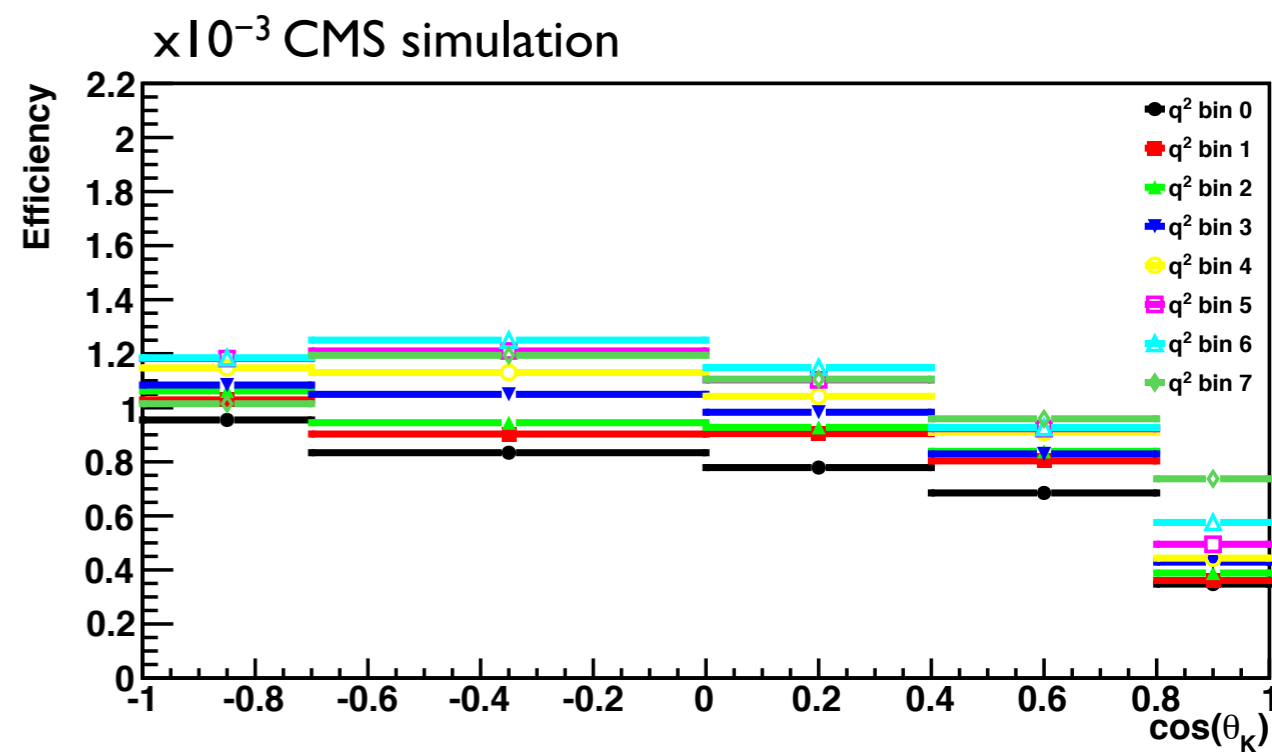
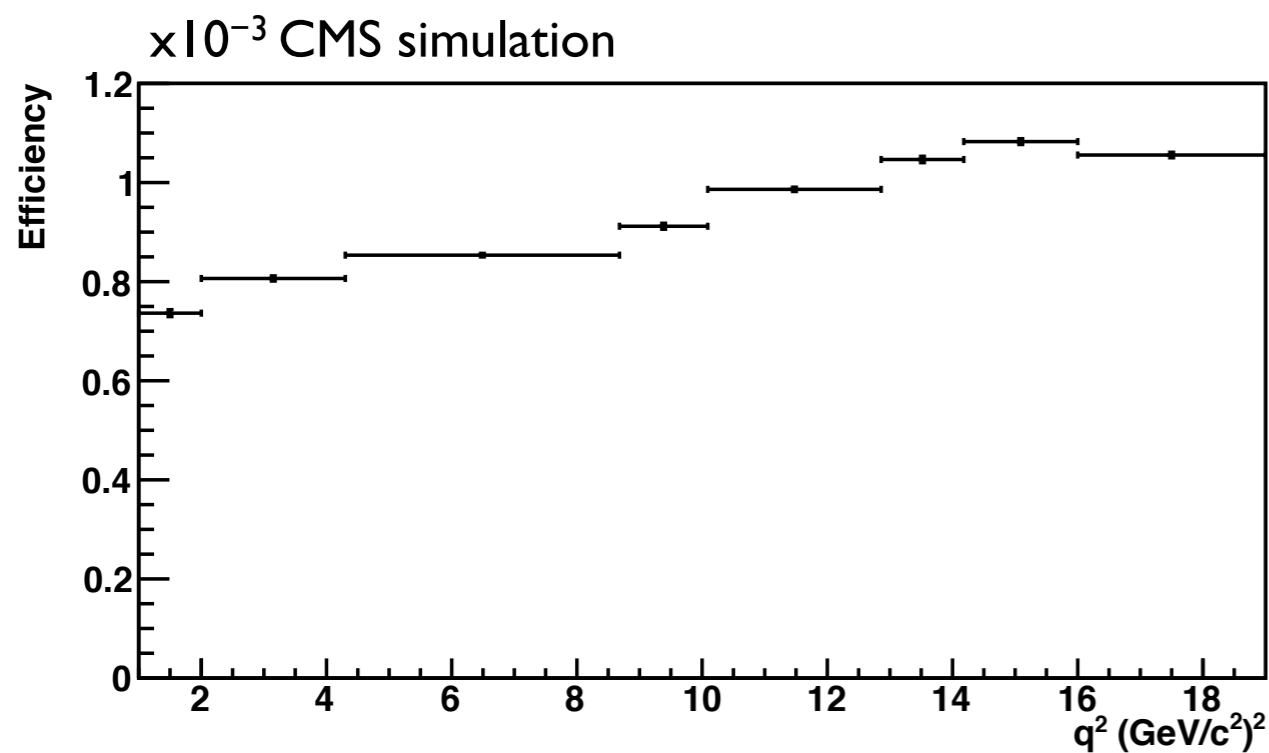
- Ilse Kraetschmer, “Quarkonium polarization from CMS and Tevatron” Mon. 16:40 - 17:00, Heavy Flavour Production (I)
- Torsten Dahms, “Upsilon melting in CMS / ALICE” Tue. 9:30 - 9:50, Heavy Flavour Production (II)
- Marco de Mattia, “ $B_s \rightarrow \mu \mu$  in CMS” Tue. 14:30 - 14:50, Rare B Decays (I)
- Luigi Guiducci, “ATLAS, CMS and LHCb Trigger/DAQ systems for flavour physics” Wed. 14:40 - 15:10, Aspects of LHC Data Taking
- Sara Fiorendi, “Heavy flavour spectroscopy and production in CMS” Thu. 11:35 - 11:55, Spectroscopy

### Poster session:

- Alexis Pompili, “Observation of two structures in the  $J/\psi \Phi$  mass spectrum of exclusive  $B^+ \rightarrow J/\psi \Phi K^+$  decays in CMS”
- Martino Dall'Osso, “Measurement of the  $X(3872)$  production cross section via decays to  $J/\psi \pi \pi$ ”

# Backup

The efficiency is entirely computed from MC versus angles and  $q^2$  bins



Projections of the efficiency on angular variables and  $q^2$

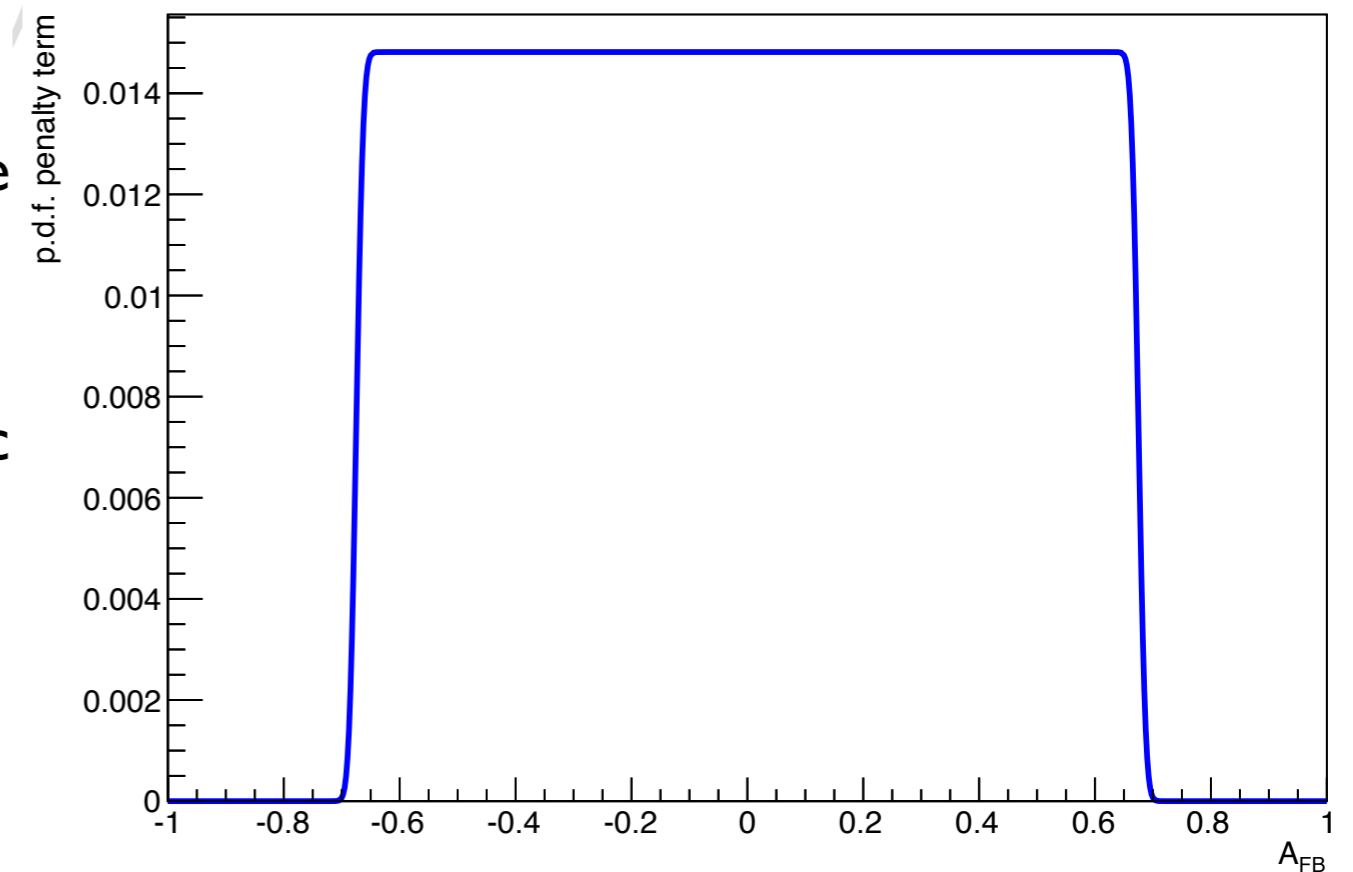
$$\text{p.d.f.}_i = \text{Kernel}_i \cdot \text{Penalty}_i =$$

$$(\mathbf{Y} \cdot \mathbf{S}^M(\mathbf{m}) \cdot \mathbf{S}^A(\theta_k, \theta_l) \cdot \varepsilon(\theta_k, \theta_l) + \mathbf{Y} \cdot \mathbf{B}^M(\mathbf{m}) \cdot \mathbf{B}^k(\theta_k) \cdot \mathbf{B}^l(\theta_l) + \\ + \mathbf{Y} \cdot \mathbf{B}^M(\mathbf{m}) \cdot \mathbf{B}^k(\theta_k) \cdot \mathbf{B}^l(\theta_l))_i \cdot \text{Penalty}_i \quad \text{Index } i \text{ run on } q^2 \text{ bins}$$

In order to keep the decay rate always positive special penalty terms are added

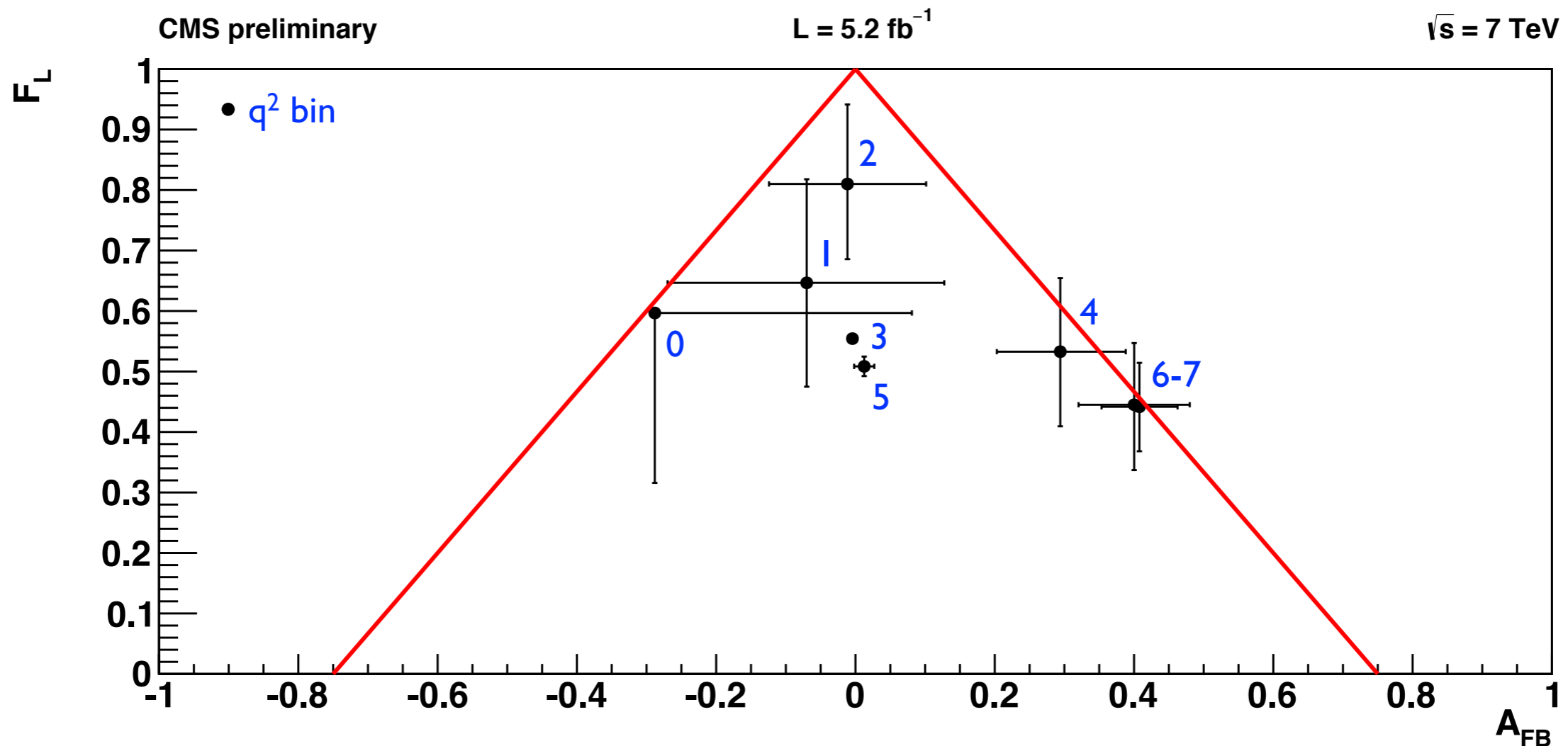
The special penalty terms implement dynamic constraints on variable boundaries:

- $|\mathbf{A}_{FB}| < 3/4 (1 - \mathbf{F}_L)$
- $|\mathbf{A}_S| < 1/2 (\mathbf{F}_S + 3\mathbf{F}_L (1 - \mathbf{F}_S))$



From  $B^0 \rightarrow K^{*0} (K^+\pi^-) J/\psi (\mu^+\mu^-)$  fit:

- $F_S = 0.013 \pm 0.010$  (stat.)
- $A_S = -0.098 \pm 0.005$  (stat.)
- $|A_S| < 1/2 (F_S + 3F_L (1 - F_S))$  satisfied if  $F_L > 0.16$   $\Rightarrow$  true for all measurements



**All results lie in the physically-allowed region**

- Potential bias from fit ingredients
  - \* Run analysis on high statistics MC to check asymptotic behavior
- Test of  $\Gamma(B^0 \rightarrow K^{*0}J/\psi) / \Gamma(B^0 \rightarrow K^{*0}\psi(2S))$ 
  - \* Compare measured BF with PDG and assign higher error as systematic uncertainty
- Potential bias from fit algorithm (toy MC)
  - \* Generate 1000 toy-MC for each  $q^2$  bin
  - \* Systematic errors are evaluated as the average deviation of fit parameters from p.d.f. values
- Incorrect CP assignment of decay
  - \* Estimated from  $B^0$  width from data control channel  $B^0 \rightarrow K^{*0} (K^+\pi^-) J/\psi (\mu^+\mu^-)$ :
  - \* Generate MC samples with artificially injected CP-mistag
  - \* Compare  $B^0$  width between data and MC samples
  - \* Run analysis on MC with 12% mistag rate (consistent with data +  $1\sigma$ ) and take difference to nominal as systematic uncertainty
- Effect of  $K\pi$  S-wave contribution
  - \* Re-fit data with P-wave only p.d.f. and compare with nominal p.d.f.
- Peaking background mass shape
  - \* Re-fit data with peaking background mass shape free to float and compare with nominal p.d.f.
- Combinatorial background shapes vs  $\cos(\theta_{K/I})$ 
  - \* Re-fit data with combinatorial background polynomial degree +1 and compare with nominal p.d.f.
- Angular resolution
  - \* Re-fit MC comparing results using reconstructed and generated angular values