

Phenomenology of exclusive rare semileptonic decays

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Theor. Physik 1



DFG FOR 1873

- concentrate on $\bar{B} \rightarrow (\bar{K}\pi)_P \ell^+ \ell^-$, i.e, on the \bar{K}^* resonance
- discuss influence of $\bar{B} \rightarrow (\bar{K}\pi)_S \ell^+ \ell^-$ on the decay distribution
- review methods to approach theory on both sides of the narrow charmonia (J/ψ and ψ')
- constrain $\Delta B = 1$ Wilson coefficients from available data on exclusive rare semileptonic and radiative decays

Effective Field Theory for $b \rightarrow sl^+l^-$ FCNCs

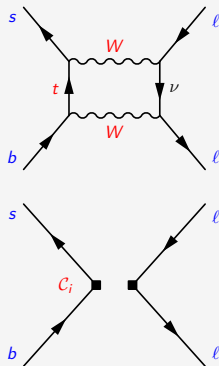
Flavor Changing Neutral Current (FCNC)

- expand amplitudes in $G_F \sim 1/M_W^2$ (OPE)
- basis of operators (physics below $\mu \simeq m_b$)

$$\mathcal{O}_i \equiv [\bar{s}\Gamma_i b] [\bar{l}\Gamma'_i l]$$

- Wilson coefficients (physics above $\mu \simeq m_b$)

$$C_i \equiv C_i(M_W, M_Z, m_t, \dots)$$



Effective Hamiltonian

$$\mathcal{H} = -\frac{4G_F}{\sqrt{2}} \left[V_{tb} V_{ts}^* \sum_i C_i \mathcal{O}_i + O(V_{ub} V_{us}^*) \right] + \text{h.c.}$$

Effective Field Theory for $b \rightarrow sl^+l^-$ FCNCs

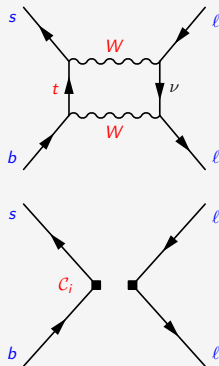
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Exclusive Modes

$$\bar{B}^0 \rightarrow \bar{K}^{(*)0} l^+ l^-$$

$$\bar{B}_s \rightarrow \phi l^+ l^-$$

$$\Lambda_b^0 \rightarrow \Lambda^0 l^+ l^-$$

$$B^- \rightarrow \bar{K}^{(*)-} l^+ l^-$$

$$\Lambda_b^- \rightarrow \Lambda^- l^+ l^-$$

Wilson Coefficients C_i

- treat C_i as uncorrelated, generalized couplings
- constrain their values from data
- confront new physics models with constraints
- complex value, two d.o.f. per $C_i \Rightarrow$ BSM CPV (SM: real C_i)

Basis of Operators O_i

- should include all relevant O_i , otherwise constraints are biased
- should include as few O_i as needed, otherwise fits are too involved
- balancing act, test statistically if choice of basis describes data well!

Basis of Operators (semileptonic)

Semileptonic Operators (SM-like: 9, 10 chirality-flipped: 9', 10')

$$\mathcal{O}_{9(9')} = \frac{\alpha_e}{4\pi} [\bar{s}\gamma_\mu P_{L(R)} b] [\bar{\ell}\gamma^\mu \ell] \quad \mathcal{O}_{10(10')} = \frac{\alpha_e}{4\pi} [\bar{s}\gamma_\mu P_{L(R)} b] [\bar{\ell}\gamma^\mu \gamma_5 \ell]$$

+ strong/EM penguins as in the SM

Semileptonic Operators ((pseudo-)scalar: S' , P') tensor: T , T_5)

complete the basis of $[\bar{s}\Gamma b][\bar{\ell}\Gamma\ell]$ operators

$$\begin{aligned} \mathcal{O}_{S(9')} &= \frac{\alpha_e}{4\pi} [\bar{s}P_{R(L)} b] [\bar{\ell}\ell] & \mathcal{O}_{P(10')} &= \frac{\alpha_e}{4\pi} [\bar{s}P_{R(L)} b] [\bar{\ell}\gamma_5 \ell] \\ \mathcal{O}_T &= \frac{\alpha_e}{4\pi} [\bar{s}\sigma_{\mu\nu} b] [\bar{\ell}\sigma^{\mu\nu} \ell] & \mathcal{O}_{T_5} &= \frac{\alpha_e}{4\pi} [\bar{s}\sigma_{\mu\nu} b] [\bar{\ell}\sigma_{\alpha\beta} \ell] \frac{i\epsilon^{\mu\nu\alpha\beta}}{2} \end{aligned}$$

Basis of Operators (current-current & penguins)

Current-Current

$$\mathcal{O}_1 = [\bar{s}\gamma_\mu P_L T^a c] [\bar{c}\gamma^\mu P_L T^a b] \quad \mathcal{O}_2 = [\bar{s}\gamma_\mu P_L c] [\bar{c}\gamma^\mu P_L b]$$

SM: $C_1 \simeq -0.3$, $C_2 \simeq 1$

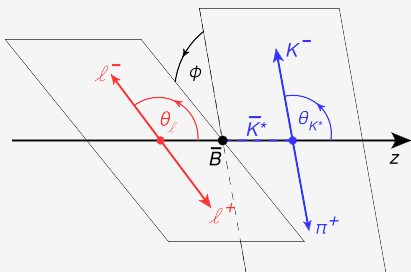
Penguins (photonic: 7(') gluonic: 8(') $\bar{q}q$: 3-6)

$$\begin{aligned} \mathcal{O}_{7(')} &= [\bar{s}\sigma_{\mu\nu} P_{R(L)} b] F^{\mu\nu} & \mathcal{O}_{8(')} &= [\bar{s}\sigma_{\mu\nu} P_{R(L)} b] G^{\mu\nu} \\ \mathcal{O}_3 &= [\bar{s}\gamma_\mu P_L b] [\bar{q}\gamma^\mu q] & \mathcal{O}_4 &= [\bar{s}\gamma_\mu T^a P_L b] [\bar{q}\gamma^\mu T^a q] \\ \mathcal{O}_5 &= [\bar{s}\gamma_{\mu\nu\rho} P_L b] [\bar{q}\gamma^{\mu\nu\rho} q] & \mathcal{O}_6 &= [\bar{s}\gamma_{\mu\nu\rho} T^a P_L b] [\bar{q}\gamma^{\mu\nu\rho} T^a q] \end{aligned}$$

$$\gamma_{\mu\nu\rho} \equiv \gamma_\mu \gamma_\nu \gamma_\rho$$

- $\mathcal{O}_{7(')}$ dominant when dilepton system is almost lightlike
- QED Penguins usually not included
- QCD Penguins ($\mathcal{O}_{3\dots 6}$) usually as in the SM, small Wilson coefficients

Kinematics of $\bar{B} \rightarrow \bar{K}\pi l^+ l^-$ (similar: $\bar{B}_s \rightarrow K^+ K^- l^+ l^-$)



Kinematic Variables

$$4m_l^2 \leq q^2 \leq (M_B - M_{K^*})^2$$

$$-1 \leq \cos \theta_l \leq 1$$

$$-1 \leq \cos \theta_{K^*} \leq 1$$

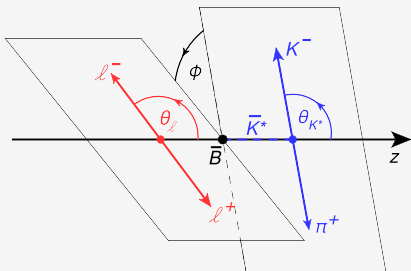
$$0 \leq \phi \leq 2\pi$$

$$[(M_K + M_\pi)^2 \leq k^2 \leq (M_B - \sqrt{q^2})^2]$$

On-shell and S-Wave

- one usually assumes on-shell decay of P-wave K^* ($\sim \sin \theta_{K^*}, \cos \theta_{K^*}$)
- for high precision: consider width of K^* , and $J = 0$ (S-wave) ($\propto \theta_{K^*}$)
 $K\pi$ -final-state from K_0^* and *non-resonant background*

Kinematics of $\bar{B} \rightarrow \bar{K}\pi\ell^+\ell^-$ (similar: $\bar{B}_s \rightarrow K^+K^-\ell^+\ell^-$)



Kinematic Variables

$$4m_\ell^2 \leq q^2 \leq (M_B - M_{K^*})^2$$

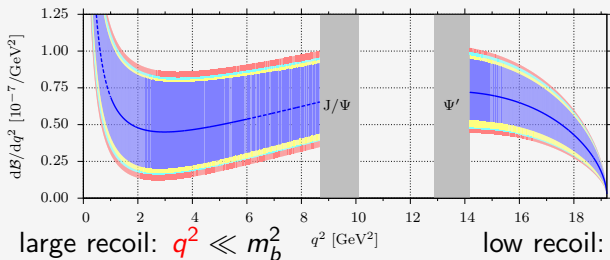
$$-1 \leq \cos \theta_\ell \leq 1$$

$$-1 \leq \cos \theta_{K^*} \leq 1$$

$$0 \leq \phi \leq 2\pi$$

$$[(M_K + M_\pi)^2 \leq k^2 \leq (M_B - \sqrt{q^2})^2]$$

Large vs. Low Recoil (for illustration)



Differential Decay Rate for pure P-wave state

$$\begin{aligned}
 \frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_{K^*} d\phi} &\sim J_{1s} \sin^2 \theta_{K^*} + J_{1c} \cos^2 \theta_{K^*} \\
 &+ (J_{2s} \sin^2 \theta_{K^*} + J_{2c} \cos^2 \theta_{K^*}) \cos 2\theta_\ell \\
 &+ (J_3 \cos 2\phi + J_9 \sin 2\phi) \sin^2 \theta_{K^*} \sin^2 \theta_\ell \\
 &+ (J_4 \sin 2\theta_{K^*}) \sin 2\theta_\ell \cos \phi \\
 &+ (J_5 \sin 2\theta_{K^*}) \sin \theta_\ell \cos \phi \\
 &+ (J_{6s} \sin^2 \theta_{K^*} + J_{6c} \cos^2 \theta_{K^*}) \cos \theta_\ell \\
 &+ (J_7 \sin 2\theta_{K^*}) \sin \theta_\ell \sin \phi \\
 &+ (J_8 \sin 2\theta_{K^*}) \sin 2\theta_\ell \sin \phi,
 \end{aligned}$$

$J_i \equiv J_i(q^2)$: 12 angular observables

Differential Decay Rate for mixed P- and S-wave state

$$\begin{aligned} \frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_{K^*} d\phi} \sim & J_{1s} \sin^2 \theta_{K^*} + J_{1c} \cos^2 \theta_{K^*} + J_{1i} \cos \theta_{K^*} \\ & + (J_{2s} \sin^2 \theta_{K^*} + J_{2c} \cos^2 \theta_{K^*} + J_{2i} \cos \theta_{K^*}) \cos 2\theta_\ell \\ & + (J_3 \cos 2\phi + J_9 \sin 2\phi) \sin^2 \theta_{K^*} \sin^2 \theta_\ell \\ & + (J_4 \sin 2\theta_{K^*} + J_{4i} \cos \theta_{K^*}) \sin 2\theta_\ell \cos \phi \\ & + (J_5 \sin 2\theta_{K^*} + J_{5i} \cos \theta_{K^*}) \sin \theta_\ell \cos \phi \\ & + (J_{6s} \sin^2 \theta_{K^*} + J_{6c} \cos^2 \theta_{K^*}) \cos \theta_\ell \\ & + (J_7 \sin 2\theta_{K^*} + J_{7i} \cos \theta_{K^*}) \sin \theta_\ell \sin \phi \\ & + (J_8 \sin 2\theta_{K^*} + J_{8i} \cos \theta_{K^*}) \sin 2\theta_\ell \sin \phi, \end{aligned}$$

$J_i \equiv J_i(q^2, k^2)$: 12 angular observables, no further needed [Bobeth/Hiller/DvD '12]

Conclusion: remove S-wave in exp. analysis

- angular analysis [Egede/Blake/Shires '12]
- side-band analysis (for $J_{1s,1c,2s,2c}$) [Bobeth/Hiller/DvD '12]

Building Blocks of the Angular Observables (I)

Form Factors (P-Wave)

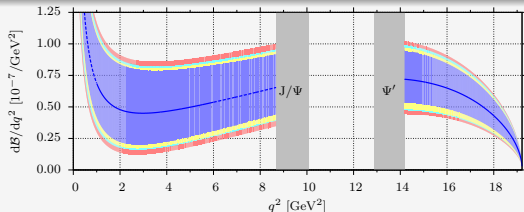
- hadronic matrix elements $\langle \bar{K}^* | \bar{s} \Gamma b | \bar{B} \rangle$ parametrized through 7 form factors:

$$\langle \bar{K}^* | \bar{s} \gamma^\mu b | \bar{B} \rangle \sim V \quad \langle \bar{K}^* | \bar{s} \gamma^\mu \gamma_5 b | \bar{B} \rangle \sim A_{0,1,2} \quad \langle \bar{K}^* | \bar{s} \sigma^{\mu\nu} b | \bar{B} \rangle \sim T_{1,2,3}$$

- form factors largest source of theory uncertainty
amplitude $\sim 10\% - 15\% \Rightarrow$ observables: $\sim 20\% - 50\%$
 - available from Light Cone Sum Rules [Ball/Zwicky '04, Khodjamirian et al. '11]
 - Lattice QCD: work in progress [e.g. Liu et al. '11, Wingate '11]
 - extract ratios from low recoil data

[Hambrock/Hiller '12, Beaujean/Bobeth/DvD/Wacker '12]

blue band:
form factor uncertainty



Building Blocks of the Angular Observables (II)

Transversity amplitudes A_i

- SM-like + chirality flipped: essentially four amplitudes $A_{\perp,\parallel,0,t}$
[Krüger/Matias '05]
- $\mathcal{O}_{S^{(\prime)}}$ give rise to A_S , $\mathcal{O}_{P^{(\prime)}}$ absorbed by A_t [Altmannshofer et al. '08]
- $\mathcal{O}_{T^{(5)}}$ give rise to 6 new amplitudes A_{ab} ,
 $(ab)=(0t),(\parallel\perp),(0\perp),(t\perp),(0\parallel),(t\parallel)$ [Bobeth/Hiller/DvD '12]
- altogether: 11 complex-valued amplitudes

Angular Observables

- J_i functionals of A_S, A_a, A_{ab} , $a, b = t, 0, \parallel, \perp$ e.g.

$$J_3(q^2) = \frac{3\beta_\ell}{4} [|A_\perp|^2 - |A_\parallel|^2 + 16(|A_{t\parallel}|^2 + |A_{0\parallel}|^2 - |A_{t\perp}|^2 - |A_{0\perp}|^2)]$$

β_ℓ : lepton velocity in dilepton rest frame

$$m_\ell^2/q^2 \rightarrow 0 \Rightarrow \beta_\ell \rightarrow 1$$

“Standard” Observables

considerable theory uncertainty due to form factors

Batch #1, to be extracted from CP average

$$\begin{aligned}\langle \Gamma \rangle &= \langle 2J_{1s} + J_{1c} - \frac{2}{3}J_{2s} - \frac{1}{3}J_{2c} \rangle & \langle A_{\text{FB}} \rangle &= \frac{\langle 2J_{6s} + J_{6c} \rangle}{2\langle \Gamma \rangle} \\ \langle F_L \rangle &= \frac{\langle 3J_{1c} - J_{2c} \rangle}{\langle 3\Gamma \rangle} & \langle F_T \rangle &= \frac{\langle 6J_{1s} - 2J_{2s} \rangle}{\langle 3\Gamma \rangle}\end{aligned}$$

Γ : decay width A_{FB} : forward-backward asymm. $F_L = 1 - F_T$: long./trans. pol.

Batch #2, CP (a)symmetries [Bobeth/Hiller/Piranishvili '08, Altmannshofer et al. '08]

$$\langle A_i \rangle \sim \frac{\langle J_i - \bar{J}_i \rangle}{\langle \Gamma + \bar{\Gamma} \rangle} \quad \langle S_i \rangle \sim \frac{\langle J_i + \bar{J}_i \rangle}{\langle \Gamma + \bar{\Gamma} \rangle}$$

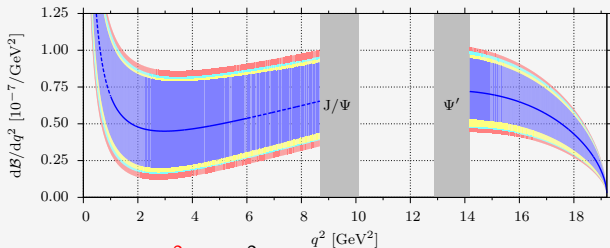
overline: CP conjugated mode, also: mixing-induced CP asymm in $B_s \rightarrow \phi \ell^+ \ell^-$

$$\langle X \rangle \equiv \int dq^2 X(q^2)$$

Pollution due to Charm Resonances

Narrow Resonances: J/ψ and $\psi(2s)$

- experiments veto q^2 -region of narrow charmonia J/ψ and $\psi(2s)$
- however: resonance affects observables outside the veto!



large recoil: $q^2 \ll m_b^2$

low recoil: $q^2 \simeq m_b^2$

Approach by Theorists: Divide and Conquer

- treat region below J/ψ (aka *large recoil*) differently than above $\psi(2s)$
- design combinations of J_i which have reduced theory uncertainty in only one kinematic region

Large Recoil (I)

QCD Factorization (QCDF) + Soft Collinear Effective Theory (SCET)

- calculate $\bar{q}q$ loops perturbatively, expand in $1/m_b$, $1/E_{K^*}$
- relate matrix elements to universal hadronic quantities:
 - ▶ Light Cone Distribution Amplitudes (LCDAs)
 - ▶ form factors
 - ▶ decay constants

[Beneke/Feldmann '00, Beneke/Feldmann/Seidel '01 & '04]

Light Cone Sum Rules (LCSR)

- calculate $\langle \bar{c}c \rangle$, $\langle \bar{c}cG \rangle$ on the light cone for $q^2 \ll 4m_c^2$
- achieves resummation of soft gluon effects
- use analyticity of amplitude to relate results to $q^2 < M_{\psi'}^2$
- uses many of the same inputs as QCDF+SCET
- includes parts of QCDF+SCET results

[Khodjamirian/Mannel/Pivovarov/Wang '11]

Large Recoil (I)

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 - ▶ form factors
 - ▶ decay constants

[Beneke/Feldmann '00, Beneke/Feldmann/Seidel '01 & '04]

Combination of QCDF+SCET and LCSR Results

- not yet!
 - ▶ no studies yet to find impact on optimized observables at large recoil!
 - ▶ LCSR results are not included in following discussion

Large Recoil (II)

SM + chirality flipped

- transversity amplitudes factorize up to power suppressed terms

$$A_{\perp}^{L,R} \sim X_{\perp}^{L,R} \times \xi_{\perp} \quad A_{\parallel}^{L,R} \sim X_{\parallel}^{L,R} \times \xi_{\perp} \quad A_0^{L,R} \sim X_0^{L,R} \times \xi_{\parallel}$$

$\xi_{\perp, \parallel}$: soft form factors

$X_i^{L,R}$: combinations of Wilson coefficients

[Beneke/Feldmann/Seidel '01 & '04, Bobeth/Hiller/Piranishvili '08, Altmannshofer et al. '08]

Optimized Observables

enhanced sensitivity to right-handed currents, reduced form factor dependence

[Krüger/Matias '05, Egede et al. '08 & '10]

$$A_T^{(2)} = \frac{|A_{\perp}|^2 - |A_{\parallel}|^2}{|A_{\perp}|^2 + |A_{\parallel}|^2} \sim J_3 \quad A_T^{(3)} = \frac{|A_0^L A_{\parallel}^{L*} + A_0^{R*} A_{\parallel}^R|}{\sqrt{|A_0|^2 |A_{\parallel}|^2}} \sim J_4, J_7$$
$$A_T^{(4)} = \frac{|A_0^L A_{\perp}^{L*} - A_0^{R*} A_{\perp}^R|}{\sqrt{|A_0|^2 |A_{\perp}|^2}} \sim J_5, J_8 \quad A_T^{(5)} = \frac{|A_{\perp}^L A_{\parallel}^{R*} + A_{\perp}^{R*} A_{\parallel}^L|}{|A_{\perp}|^2 + |A_{\parallel}|^2}$$

Large Recoil (II)

SM + chirality flipped

- transversity amplitudes factorize up to power suppressed terms

$$A_{\perp}^{L,R} \sim X_{\perp}^{L,R} \times \xi_{\perp} \quad A_{\parallel}^{L,R} \sim X_{\parallel}^{L,R} \times \xi_{\perp} \quad A_0^{L,R} \sim X_0^{L,R} \times \xi_{\parallel}$$

$\xi_{\perp, \parallel}$: soft form factors

$X_i^{L,R}$: combinations of Wilson coefficients

[Beneke/Feldmann/Seidel '01 & '04, Bobeth/Hiller/Piranishvili '08, Altmannshofer et al. '08]

Further Optimized Observables

enhanced sensitivity to right-handed currents, reduced form factor dependence

[Becirevic/Schneider '11]

$$A_T^{(\text{re})} \propto \frac{J_{6s}}{J_{2s}}$$

$$A_T^{(\text{im})} \propto \frac{J_9}{J_{2s}}$$

SM basis [Bobeth/Hiller/DvD '10] + chirality flipped [Bobeth/Hiller/DvD '12]

- transversity amplitudes factorize

$$A_{\perp,\parallel,0}^{L,R} \sim C_{\pm}^{L,R} \times f_{\perp,\parallel,0} + O\left(\frac{\alpha_s \Lambda}{m_b}, \frac{C_7 \Lambda}{C_9 m_b}\right) \quad \text{SM: } C_+^{L,R} = C_-^{L,R}$$

f_i : helicity form factors

$C_{\pm}^{L,R}$: combinations of Wilson coeff.

- 4 combinations of Wilson coefficients enter observables:

$$\rho_1^{\pm} \sim |C_{\pm}^R|^2 + |C_{\pm}^L|^2$$

$$\text{Re}(\rho_2) \sim \text{Re}(C_+^R C_-^{R*} - C_-^L C_+^{L*}) \quad \text{and } \text{Re}(\cdot) \leftrightarrow \text{Im}(\cdot)$$

Tensor operators [Bobeth/Hiller/DvD '12]

- 6 new transversity amplitudes, still factorize!

$$A_{ab} \sim C_{T(T5)} \times f_{\perp,\parallel,0} + O\left(\frac{\Lambda}{m_b}\right)$$

- 3 new combinations of Wilson coefficients

$$\rho_1^T \sim |C_T|^2 + |C_{T5}|^2 \quad \text{Re}(\rho_2^T) \sim \text{Re}(C_T C_{T5}^*) \quad \text{and } \text{Re}(\cdot) \leftrightarrow \text{Im}(\cdot)$$

Optimized Observables at Low Recoil

”Form Factor Free“ Observables

- optimized for low recoil: $H_T^{(1,2,3,4,5)}$ [Bobeth/Hiller/DvD '10 & '12]
- $H_T^{(1)}$: probes low-recoil framework before new physics
- $H_T^{(2,3,4,5)}$: access to combination of Wilson coefficients

$$\rho_2 / \sqrt{\rho_1^+ \rho_1^-} \quad \xrightarrow{\text{SM basis}} \quad \frac{c_9 c_{10}}{|c_9|^2 + |c_{10}|^2}$$

up to $O\left(\frac{\alpha_s \Lambda}{m_b}, \frac{c_7 \Lambda}{c_9 m_b}\right)$ corrections, complementary to large recoil

”Short-Distance Free“ Observables

- form factor ratios, relevant for comparison with lattice
- SM: all ratios f_i/f_j available, chirality-flipped: only $f_0/f_{||}$

Optimized CP Asymmetries (SM-like and chirality-flipped basis)

$$a_{\text{CP}}^{(1,\pm)} = \frac{\rho_1^\pm - \bar{\rho}_1^\pm}{\rho_1^\pm + \bar{\rho}_1^\pm} \xrightarrow{\text{SM basis}} A_{\text{CP}}$$

$$a_{\text{CP}}^{(2,\pm)} = \frac{\frac{\rho_2}{\rho_1^\pm} - \frac{\bar{\rho}_2}{\bar{\rho}_1^\pm}}{\frac{\rho_2}{\rho_1^\pm} + \frac{\bar{\rho}_2}{\bar{\rho}_1^\pm}} \xrightarrow{\text{SM basis}} A_{\text{CP,FB}}$$

$$a_{\text{CP}}^{(3)} = \frac{\text{Re}(\rho_2 - \bar{\rho}_2)}{\sqrt{(\rho_1^+ + \bar{\rho}_1^+)(\rho_1^- + \bar{\rho}_1^-)}} \sim H_T^{(2,3)}$$

$$a_{\text{CP}}^{(4)} = \frac{\text{Im}(\rho_2 - \bar{\rho}_2)}{\sqrt{(\rho_1^+ + \bar{\rho}_1^+)(\rho_1^- + \bar{\rho}_1^-)}} \sim H_T^{(4,5)}$$

- driven by strong phase $\text{Im}(Y)$

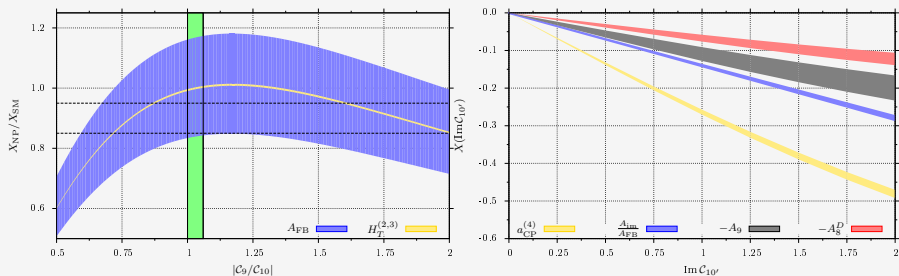
$$\text{Im}(Y) = \text{Im}\left(Y_9 + \frac{2m_b M_B}{q^2} Y_7\right) \quad Y_i \equiv C_i^{\text{eff}} - C_i$$

low recoil OPE predicts $\text{Im}(Y) \simeq 0.2$ for $q^2 \geq 14\text{GeV}^2$

- also: $A_{\text{im}}/A_{\text{FB}} = J_9/J_{6s} = \text{Im}(\rho_2)/\text{Re}(\rho_2)$
both A_{im} and A_{FB} measured, but error on ratio not known

Probing BSM Physics at Low Recoil

Sensitivity Studies for NP only in $C_{9,10}(\prime)$



Results [Bobeth/Hiller/DvD '12]

- $H_T^{2,3}$ probe $|C_9/C_{10}|$ better than A_{FB}
- $a_{CP}^{(4)}$ probes $\text{Im}(C_{10}')$ better than other CP asymm.

$$\langle a_{CP}^{(4)} \rangle \simeq (-0.240 \pm 0.005) \text{Im}(C_{10}')$$

Global Analysis of Exclusive Decays

Global Analysis of Exclusive Decays

- following results from [Beaujean/Bobeth/DvD/Wacker '12]
- see also further analyses [Altmannshofer/Straub '12, Descotes-Genon et al. '12]

Available Data for Exclusive Processes

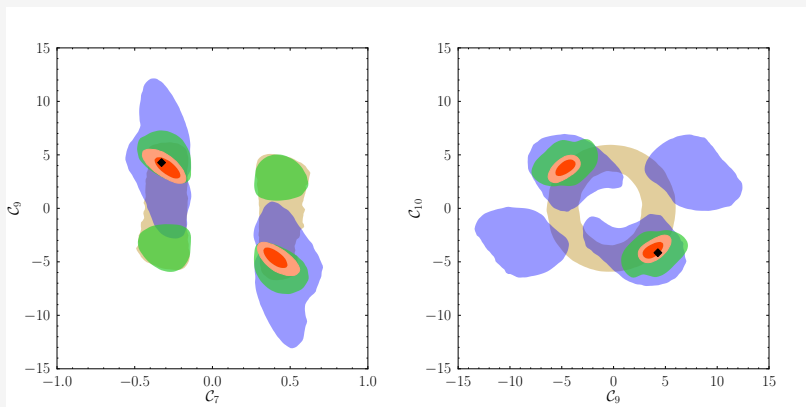
$\bar{B} \rightarrow \bar{K}^* \ell^+ \ell^-$	$\mathcal{B}, A_{\text{FB}}, S_3, A_T^{(2)}, A_I$	BaBar, Belle, CDF, LHCb
$\bar{B} \rightarrow \bar{K} \ell^+ \ell^-$	$\mathcal{B}, A_{\text{FB}}, F_H, A_I$	BaBar, Belle, CDF, LHCb
$\bar{B} \rightarrow \bar{K}^* \gamma$	$\mathcal{B}, S_{K^* \gamma}$	CLEO, BaBar, Belle
$\bar{B}_s \rightarrow \mu^+ \mu^-$	upper bound on \mathcal{B}	LHCb

blue observables: used in following analysis

orange: new data available since analysis

Global Analysis of Exclusive $b \rightarrow s\{l^+l^-, \gamma\}$

95% credibility regions: Two Solutions



all regions include $B \rightarrow K^*\gamma$ inputs

blue incl. $B \rightarrow K^*l^+l^-$ (low)

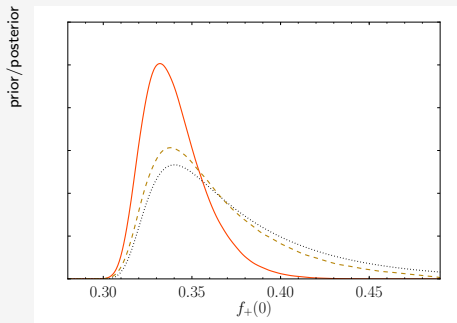
light red all data + $B_s \rightarrow \mu^+\mu^-$ (dark red 68%)

brown incl. $B \rightarrow Kl^+l^-$ (high + low)

green incl. $B \rightarrow K^*l^+l^-$ (high)

◆ SM value

What We Also Learn from Data



dotted: prior [Khodjamirian et al. '11]

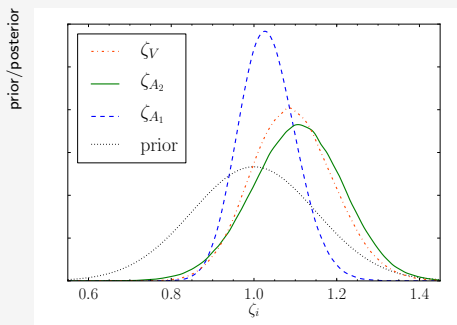
dashed: posterior w/ $B \rightarrow K l^+ l^-$ data

solid: posterior w/ all data

$B \rightarrow K$ form factor: f_+

- $B \rightarrow K l^+ l^-$ data and prior agree well
- $B \rightarrow K^* l^+ l^-$ data has strong impact on posterior

What We Also Learn from Data



$V(q^2) \rightarrow \zeta_V V(q^2)$, similar for $A_{1,2}$

ζ_i : common gauss prior

V, A_1, A_2 : [Ball/Zwicky '04]-results

$B \rightarrow K^* l^+ l^-$

- prior/posterior agree well for ζ_{A_1}
- considerable shifts in posterior ($\sim 10\%$) for ζ_V and ζ_{A_2} !
- agrees with findings by [Hambrock/Hiller '12]

Conclusion

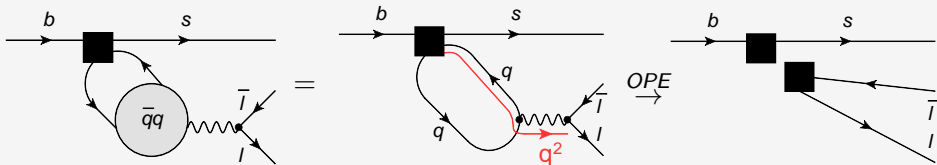
- systematic framework for exclusive $b \rightarrow sl^+l^-$ at large *and* low recoil
- rich phenomenology of $\bar{B} \rightarrow \bar{K}^*(\rightarrow K\pi)\ell^+\ell^-$
 - ▶ large recoil: rich spectrum of observables, good (B)SM sensitivity
 - ▶ low recoil: framework/OPE can be probed
 - ▶ low recoil: (B)SM sensitivity complementary to large recoil, very small theory uncertainty
- data also allows inference of hadronic quantities
- looking forward to LHCb analyses and the prospects of Belle II

Omissions due to Time Constraints

- very large recoil: $4m_e^2 \leq q^2 \leq 1\text{GeV}^2$ [Camalich/Jäger '12]
- symmetry relations between transversity amplitudes, how to build basis of observables [Descotes-Genon et al. '13]

Backup Slides

$$i \int d^4x e^{iqx} \langle \bar{K}^* | T \{ \mathcal{O}_i(0), j_\mu^{\text{e.m.}}(x) \} | \bar{B} \rangle = \sum_{j,k} C_{i,j,k}(q^2/m_b^2, \mu) \langle \mathcal{O}_j^{(k)} \rangle_\mu$$



Operators

$k = 3$ form factors, α_s corrections known, absorbed into effective Wilson coefficients $C_{7,9} \rightarrow C_{7,9}^{\text{eff}}$

$k = 4$ absent

$k = 5$ $\Lambda^2/m_b^2 \sim 2\%$ corrections, first new had. matrix elements explicitly: $< 1\%$ for $q^2 = 15\text{GeV}^2$ [Beylich/Buchalla/Feldmann]

$k = 6$ first isospin breaking correction, Λ^3/m_b^3 suppressed

Details on Calculation of Angular Observables

Helicity Decomposition

Use polarization vectors η (of K^*) and ε (of $\ell^+\ell^-$ state)

$$g_{\mu\nu} = \sum_{n,m} g_{nm} \varepsilon_{\mu}^{\dagger}(n) \varepsilon_{\nu}(m) \quad n, m = t, 0, +, -$$

$$-g_{\mu\nu} + \frac{k_{\mu}k_{\nu}}{k^2} = \sum_{n,m} \delta_{mn} \eta_{\mu}^{\dagger}(n) \eta_{\nu}(m) \quad n, m = 0, +, -$$

Transversity Amplitudes (SM-like and chirality flipped)

- introduce helicity amplitudes $H_{ab} = \eta_{\mu}^{\dagger}(a) \mathcal{M}^{\mu\nu} \varepsilon_{\nu}^{\dagger}(b)$
- four non-vanishing amplitudes: $H_{\pm\pm}, H_{00}, H_{0t}$
- switch to transversity basis:

$$\sqrt{2}A_{\perp,\parallel} = H_{++} \mp H_{--} \quad A_0 = H_0 \quad A_t = H_{0t}$$

- extended operator basis \rightarrow more amplitudes

Details on Calculation of Angular Observables

(Pseudo)Scalar Operators

- introduce additional form factor
- \Rightarrow breaks form factor free ratios involving $J_{1c,2c}$
- only $\Delta_{S,P} \equiv \mathcal{C}_{S,P} - \mathcal{C}_{S',P'}$ enter
- $\mathcal{O}_{S^{(l)}}$ give rise to A_S , $\mathcal{O}_{P^{(l)}}$ absorbed by A_t [Altmannshofer et al. '08]

Tensor Operators

- $\mathcal{O}_{T^{(5)}}$ give rise to 6 new amplitudes A_{ab} , $(ab)=(0t),(\parallel\perp),(\perp\perp),(\perp\parallel),(\parallel\parallel),(\perp\parallel)$

$$H_{abc} = \eta_{\mu}^{\dagger}(a) \mathcal{M}^{\mu\nu\rho} \varepsilon_{\nu}^{\dagger}(b) \varepsilon_{\rho}^{\dagger}(c)$$

$$A_{0\perp} \sim H_{+0+} + H_{-0-}$$

$$A_{0\parallel} \sim H_{+0+} - H_{-0-}$$

$$A_{t\perp} \sim H_{-t-} - H_{+t+}$$

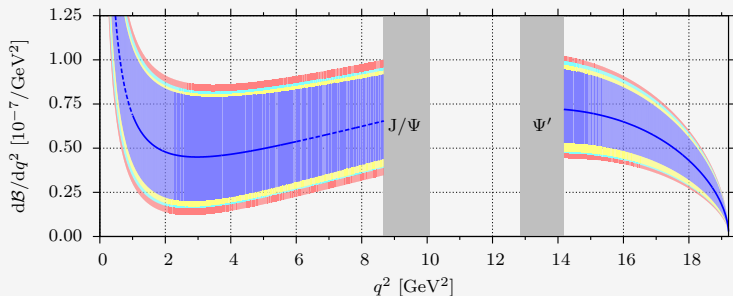
$$A_{t\parallel} \sim H_{-t-} + H_{+t+}$$

$$A_{\parallel\perp} \sim H_{0-+}$$

$$A_{t0} \sim H_{0t0}$$

- all other H_{abc} vanish [Bobeth/Hiller/DvD '12]

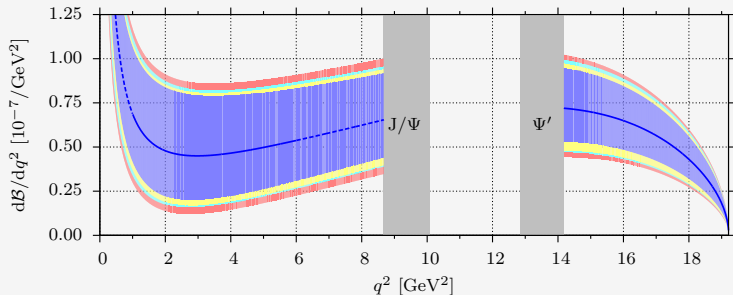
q^2 Spectrum of the Branching Ratio $\mathcal{B} = \tau_B \Gamma$



$\bar{q}q$ Pollution

- 4-quark operators like $\mathcal{O}_{1c,2c}$ induce $b \rightarrow s\bar{c}c (\rightarrow \ell^+\ell^-)$ via loops
- hadronically $B \rightarrow K^* J/\psi (\rightarrow \ell^+\ell^-)$ or higher charmonia
- experiment: cut narrow resonances $J/\psi \equiv \psi(1S)$ and $\psi' = \psi(2S)$
- theory: handle non-resonant quark loops/broad resonances $> 2S$

q^2 Spectrum of the Branching Ratio $\mathcal{B} = \tau_B \Gamma$



Large Recoil $E_{K^*} \sim m_b$ QCDF, SCET

- expand in $1/m_b$, $1/E_{K^*}$, α_s
- symmetry: $7 \rightarrow 2$ form factors

[Beneke/Feldmann/Seidel '01 & '04]

[Egede et al. '08 & '10]

Low Recoil $q^2 \sim m_b^2$ OPE, HQET

- expand in $1/m_b$, $1/\sqrt{q^2}$, α_s
- symmetry: $7 \rightarrow 4$ form factors

[Grinstein/Pirjol '04], [Beylich/Buchalla/Feldmann '11]

[Bobeth/Hiller/DvD '10 & '11]

Relations at Low Recoil

Scenario	$ H_T^{(1)} = 1$	$H_T^{(2)} = H_T^{(3)}$	$H_T^{(4)} = H_T^{(5)}$	$J_7 = 0$	$J_{8,9} = 0$
SM	✓	✓	(✓)	✓	✓
SM \otimes S, P	✓	$\frac{m_\ell}{Q} \text{Re}(C_-^{L,R} \Delta_S^*)$	(✓)	$\frac{m_\ell}{Q} \text{Im}(C_+^{L,R} \Delta_S^*)$	✓
SM \otimes T, T5	$\frac{\Lambda^2}{Q^2} \rho_1^T$	$\frac{m_\ell}{Q} \text{Re}(\rho_2^T)$	$\frac{\Lambda}{Q} \text{Im}(\rho_2^T)$	$\frac{m_\ell}{Q} \text{Im}(C_i C_{T5}^*)$	$\text{Im}(\rho_2^T)$
SM \otimes SM'	✓	✓	✓	✓	$\text{Im}(\rho_2)$
all	$\frac{\Lambda^2}{Q^2} \rho_1^T$	$\text{Re}(C_{T5} \Delta_S^*)$	$\frac{\Lambda}{Q} \text{Im}(\rho_2^{(T)})$	$\text{Im}(C_{T5} \Delta_S^*)$	$\text{Im}(\rho_2^{(T)})$

Probing the Low Recoil OPE

- deviations from $H_T^{(2)} = H_T^{(3)}$, $J_7 = 0$ signal OPE breaking
- deviations from $J_{8,9} = 0$ signal of NP (CPV right-handed current, tensors)

Status of Optimized Observables

Scenario	$H_T^{(1)}$	$H_T^{(2)}$	$H_T^{(3)}$	$H_T^{(4)}$	$H_T^{(5)}$
SM	✓	✓	✓	—	—
SM \otimes S, P	✓	A_0	✓	—	—
SM \otimes T, T5	✓	✓	✓	✓	✓
SM \otimes SM'	✓	✓	✓	✓	✓
all	✓	A_0	✓	✓	✓

— vanishes in that scenario

✓ form factor free up to m_e/Q

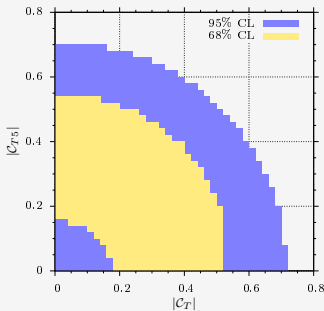
A_0 factorization broken by terms $\propto A_0$

$B \rightarrow K\ell^+\ell^-$ at Low Recoil

Observables

- $\mathcal{B}^K, A_{\text{FB}}^K, F_H^K$ (flat term)
- F_H^K sensitive to (pseudo)scalar ops. complementary to $B \rightarrow K^*\ell^+\ell^-$ and $B_s \rightarrow \ell^+\ell^-$
- correlations between $B \rightarrow K^*\ell^+\ell^- \leftrightarrow B \rightarrow K\ell^+\ell^-$, common SD factors ρ_1^+, ρ_1^T

Fit Results

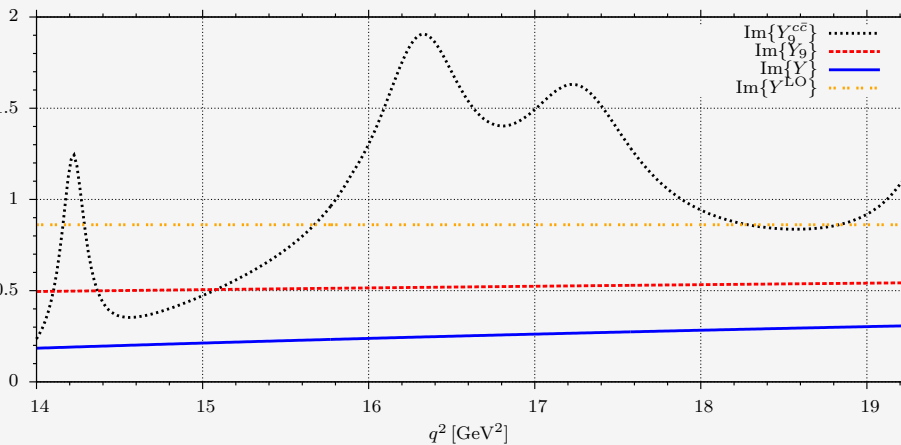


strongest constraints on $|C_{T, T5}|$ to date, based on 2012 LHCb data [[arXiv:1209.4284](https://arxiv.org/abs/1209.4284)]

Constraints

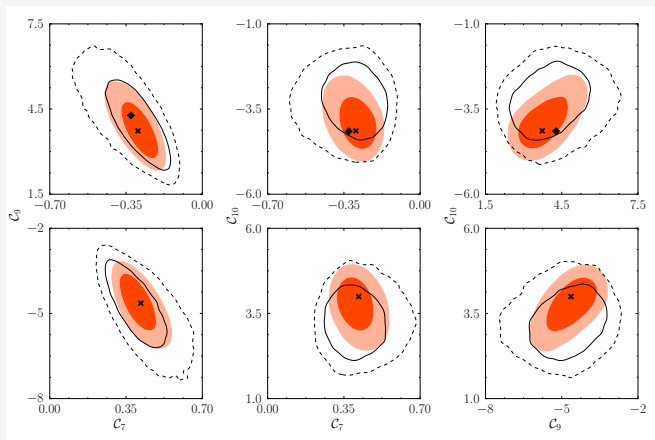
$$|C_{T, T5}| \leq 0.55 \text{ (0.70) @ 68\% (95\%) CL}$$

Y at Low Recoil



Global Analysis of Exclusive $b \rightarrow s\{\ell^+\ell^-, \gamma\}$

Check stability for different choices of priors:



color: normal priors (dark: 68%, light: 95%)

lines: wide priors (solid: 68%, dashed: 95%)

diamond: SM, cross: MAP

[Beaujean/Bobeth/DvD/Wacker '12]

Global Analysis of Exclusive $b \rightarrow s\{\ell^+\ell^-, \gamma\}$

	C_7	C_9	C_{10}
68%	$[-0.34, -0.23] \cup [0.35, 0.45]$	$[-5.2, -4.0] \cup [3.1, 4.4]$	$[-4.4, -3.4] \cup [3.3, 4.3]$
95%	$[-0.41, -0.19] \cup [0.31, 0.52]$	$[-5.9, -3.5] \cup [2.6, 5.2]$	$[-4.8, -2.8] \cup [2.7, 4.7]$
max	$-0.28 \cup 0.40$	$-4.56 \cup 3.64$	$-3.92 \cup 3.86$
68%	$[-0.39, -0.19] \cup [0.30, 0.48]$	$[-5.6, -3.8] \cup [2.9, 5.1]$	$[-4.0, -2.5] \cup [2.6, 3.9]$
95%	$[-0.53, -0.13] \cup [0.24, 0.61]$	$[-6.7, -3.1] \cup [2.2, 6.2]$	$[-4.7, -1.9] \cup [2.0, 4.6]$
max	$-0.30 \cup 0.38$	$-4.64 \cup 3.84$	$-3.24 \cup 3.30$

upper: normal priors, lower: wide priors

What We Learn

- very good agreement with the SM!
- of 59 exper. inputs, only one pull $> 2\sigma!$ ($\mathcal{B}[B \rightarrow K^*\ell^+\ell^-]_{>16}$ Belle)