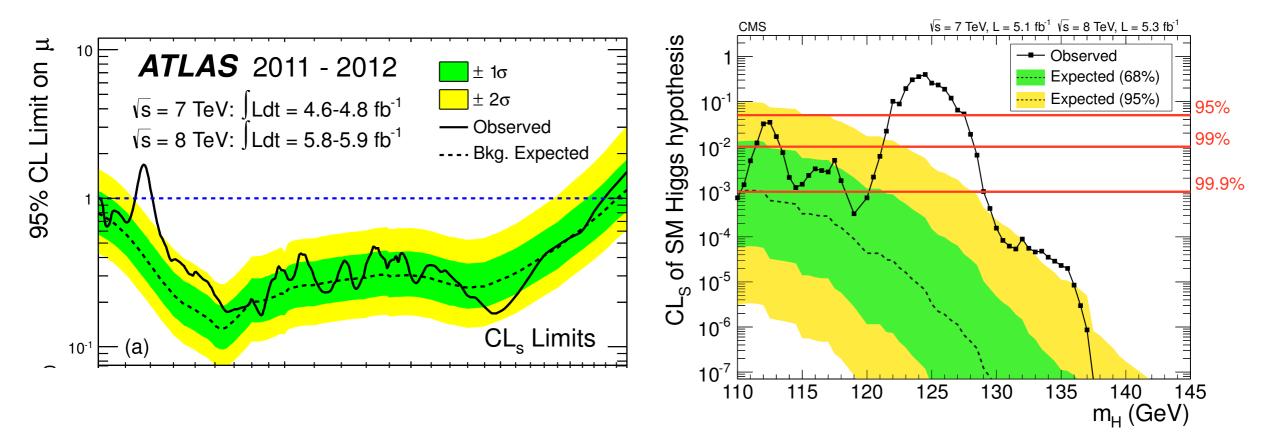
Higgs couplings and Electroweak Precision data

Lian-Tao Wang Universite of Chicago

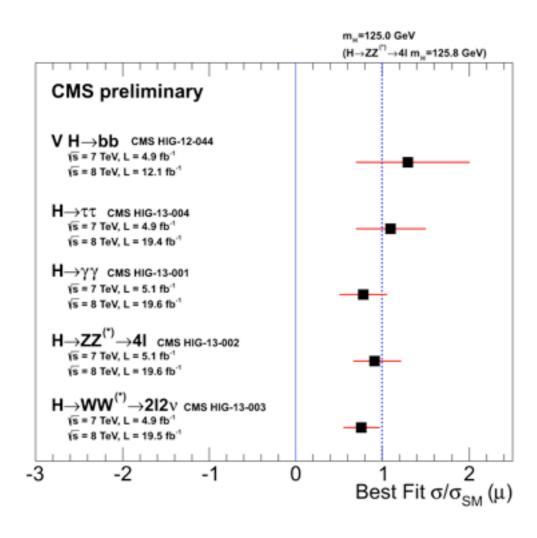
with Brian Batell and Stefania Gori arXiv:1209.6382

Beauty 2013, Bologna, Italy.

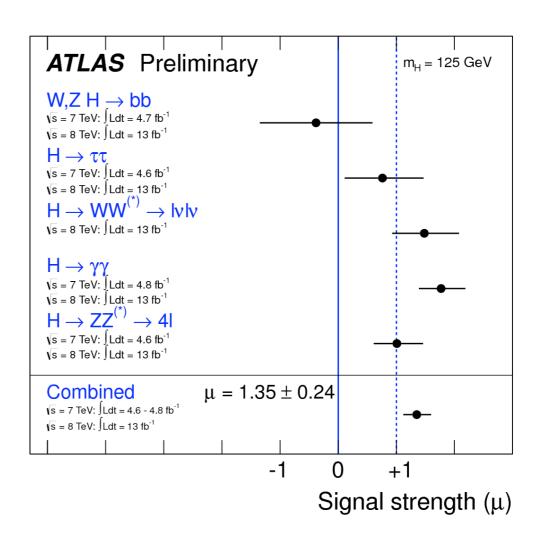
Much celebrated discovery!

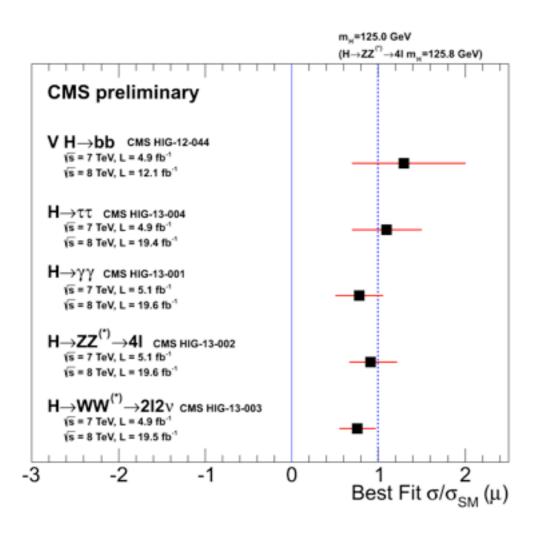


- Next step, detailed understanding its properties.
- Many possible connection to other searches, measurements.
 - Focusing on EWPT here.



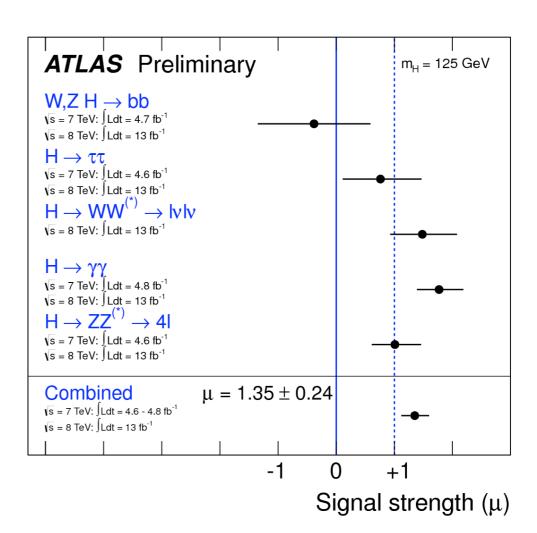


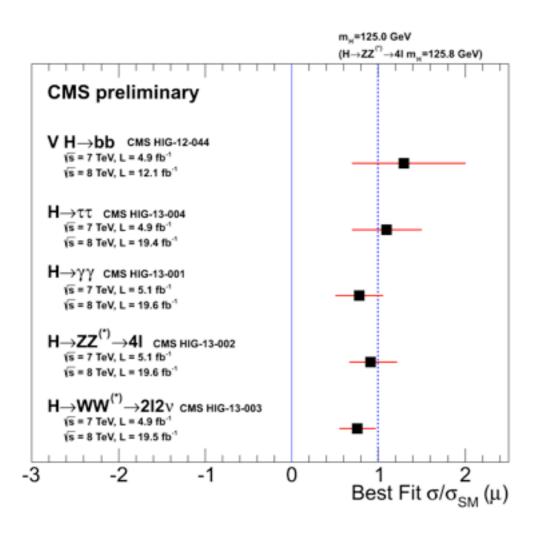






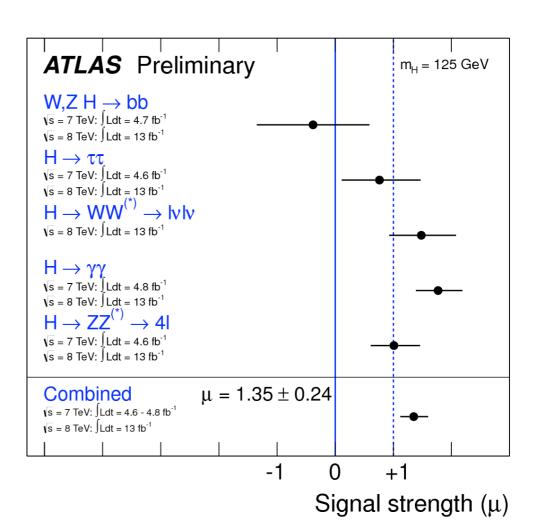
- Yes.

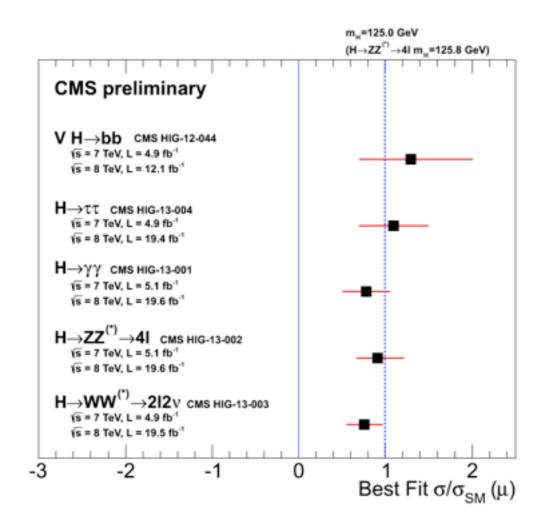


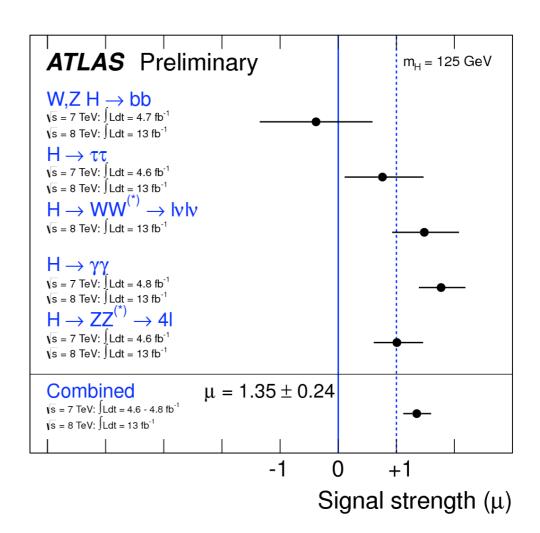




- Yes.
- Any deviations?







Coupling SM-like?

- Yes.
- Any deviations?

Nothing significant, of course. There are plenty of rooms though.

Precision fit after 2011

1. Electroweak two loop corrections for R_b [Freitas, Huang, 1205.0299]

Now $> 2\sigma$ discrepancy.

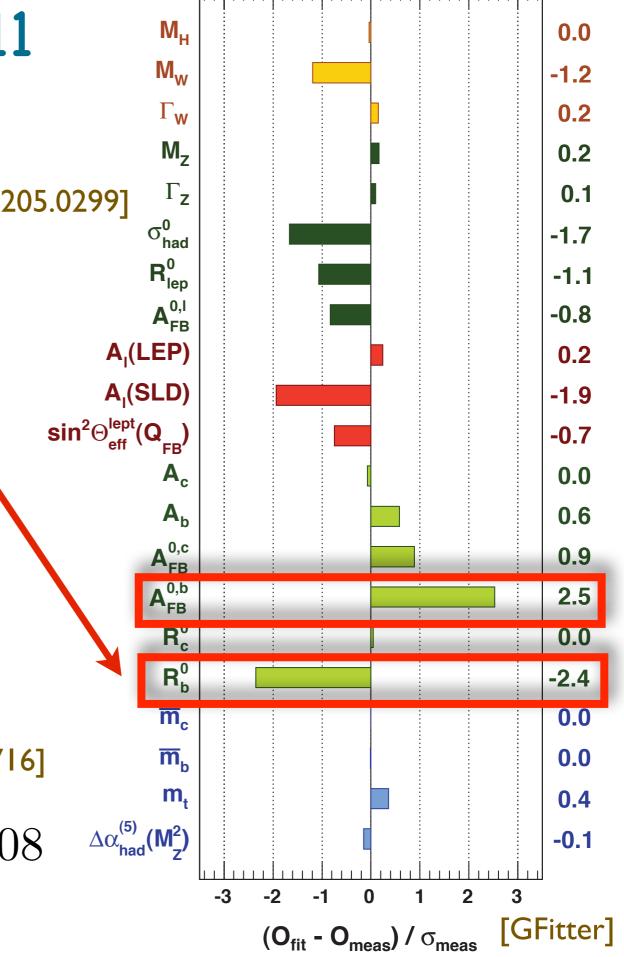
2. Higgs mass directly

measured!

Global fit (Gfitter): [arXiv:1209.2716]

$$\chi^2/\text{d.o.f.} = 21.8/14, \quad p = 0.08$$

$$p = 0.08$$



Interesting to ask:

- What new physics can "fix" Zbb?
- Implication for Higgs couplings.
 - Constraints!
 - Connection to possible deviations.

Possible resolutions of A_{FB}^{b}, R_{b} discrepancies

- **1.** New physics directly alters A_{FB}^b, R_b
 - ullet Focus on tree level shifts to $Zbar{b}$ couplings
- **2.** A_{FB}^b, R_b due to measurement errors
 - Remove measurements from EW fit. Is there tension with 125 GeV Higgs?

How compelling are each of these resolutions?

To answer this question, we have performed a global fit to the precision electroweak data

A_{FB}^{b}, R_{b} due to systematic effect

EW data alone (w/o LHC Higgs mass measurement)

SM w/o
$$A_{FB}^b, R_b$$
:

SM w/o
$$A_{FB}^{b}, R_{b}$$

+ $S, T, m_{h}^{\text{ref}} = 125$:

$$\chi^2/d.o.f = 5.6/12$$
 $m_h = 70 \pm 30 \text{ GeV}$

$$\chi^2/d.o.f = 5.6/9$$

 $S = -0.08 \pm 0.10$
 $T = 0.0 \pm 0.08$

- Only Slight tension between m_h = 70 and 125 GeV
- New contribution to S and T \Rightarrow marginal improvements.
- No obvious motivation for NP in this case.

Modify $Zb_R \overline{b}_R$ coupling

$$\mathcal{L} \supset rac{g}{c_W} Z_\mu \bar{b} (g_{Lb} P_L + g_{Rb} P_R) b$$

$$g_{Lb} = -\frac{1}{2} + \frac{1}{3}s_w^2 \approx -0.43$$
$$g_{Rb} = \frac{1}{3}s_w^2 \approx 0.0771$$

Goal: shift A_{FB}^b and R_b

$$A_{FB} = \frac{3}{4} \frac{g_{Le}^2 - g_{Re}^2}{g_{Le}^2 + g_{Re}^2} \frac{g_{Lb}^2 - g_{Rb}^2}{g_{Lb}^2 + g_{Rb}^2} \quad R_b \equiv \frac{\Gamma(Z \to b\bar{b})}{\Gamma(Z \to \text{hadrons})} \simeq \frac{g_{Lb}^2 + g_{Rb}^2}{\sum_q [g_{Lq}^2 + g_{Rq}^2]}$$

Z-pole data allows 4 solutions in $(\delta g_{Lb}, \delta g_{Rb})$, off-peak data for A_{FB}^b eliminate 2 possible solutions

This approach leads to a better fit then SM-alone

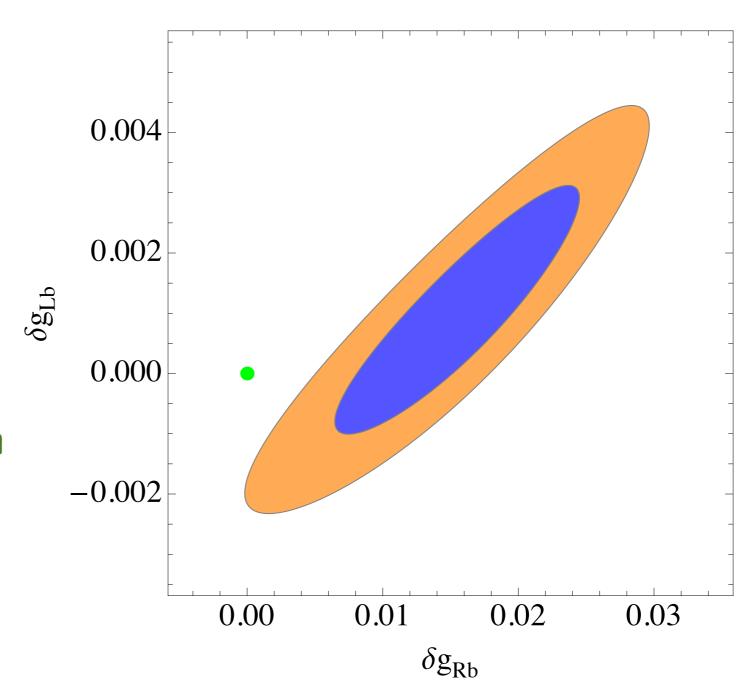
Best-fit region: positive δg_{Rb}

$$\delta g_{Lb} \sim 0.001 \pm 0.001$$

$$\delta g_{Rb} \sim 0.015 \pm 0.005$$

Another possible region (not shown in Fig) large negative δg_{Rb}

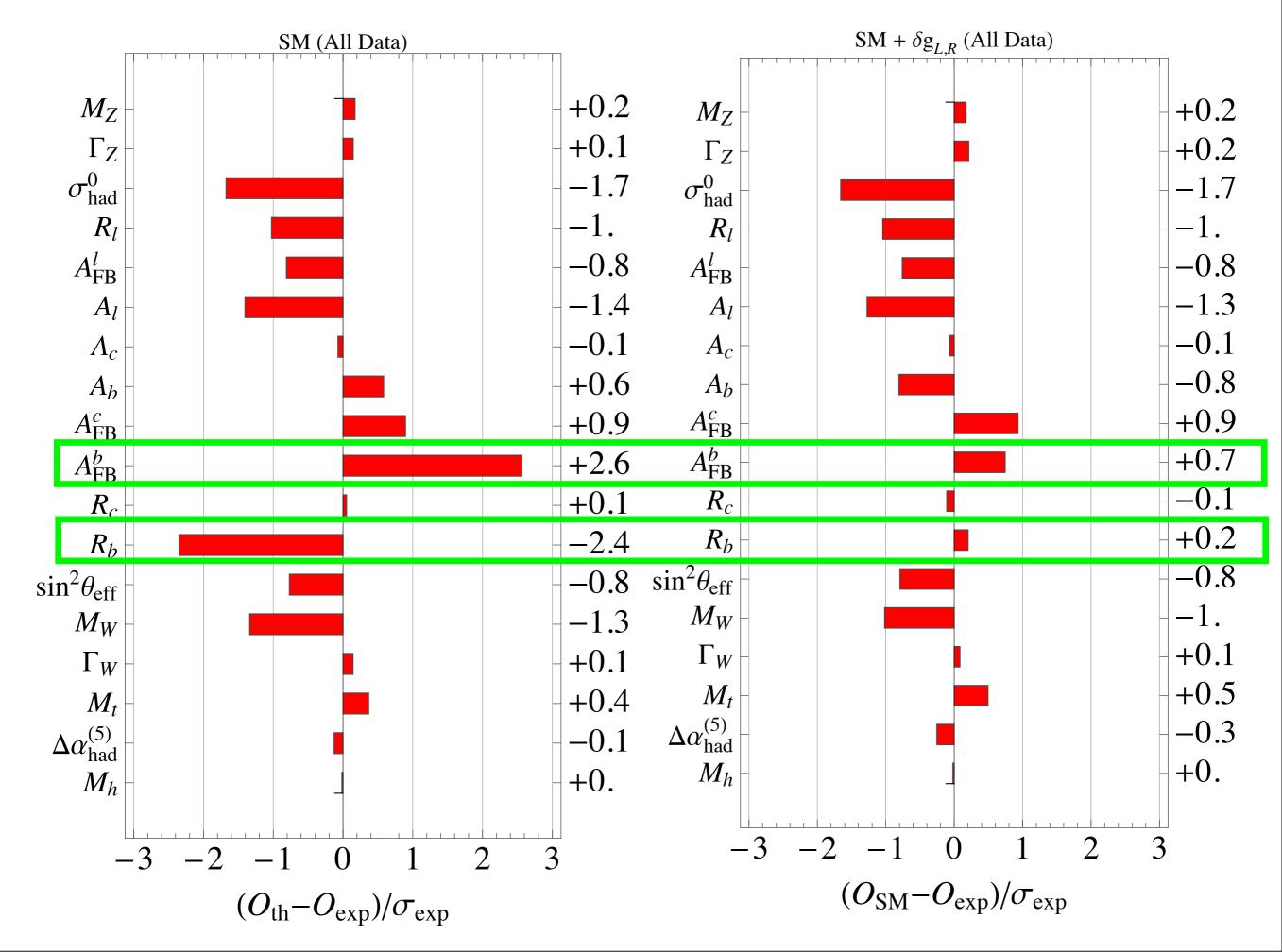
$$\delta g_{Rb} \sim -0.17 \pm 0.005$$



Always $|\delta g_{Rb}| \gg |\delta g_{Lb}|$

See also:

[Choudhury, Tait, Wagner '01] [Kumar, Shepard, Tait, Vega-Morales '10]



Putting in New Physics

Adding new ingredients

Basic idea: Mix new vector-like quark B'_{L,R} with bottom quark

$$\mathcal{L} \supset -(\bar{b}'_L \ \bar{B}'_L) \begin{pmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{pmatrix} \begin{pmatrix} b'_R \\ B'_R \end{pmatrix} + \text{h.c.}$$

Diagonalize mass matrix via rotations of $b_{i(L,R)}$, with angles $heta_{L,R}$

Shifts in couplings sensitive to mixing angles and $SU(2)_L$ representation of new B' (in particular its $T_{3L,R}$)

$$\delta g_{Lb} = \left(t_{3L} + \frac{1}{2}\right) s_L^2, \qquad \delta g_{Rb} = t_{3R} s_R^2,$$

Higgs physics

Main effects in Higgs production and decay:

- 1. Rotations shift in the $hb\bar{b}$ vertex: $\mathcal{L}_{hbb}\simeq -c_R^2\frac{m_b}{v}h\bar{b}b$ Partial width $h\to b\bar{b}$ suppressed by c_R^4
- **2.** Heavy quark B contributes to $h \to gg$ and $h \to \gamma\gamma$

can be characterized in terms of ratios

$$r_b, r_g, r_\gamma, ~~ r_i \equiv rac{\Gamma(h
ightarrow i)}{\Gamma(h
ightarrow i)_{
m SM}}$$

also define:

$$\mu_i = \frac{\sigma(pp \to h \to i)}{\sigma_{\rm SM}(pp \to h \to i)}$$

What does the signal strength data say?

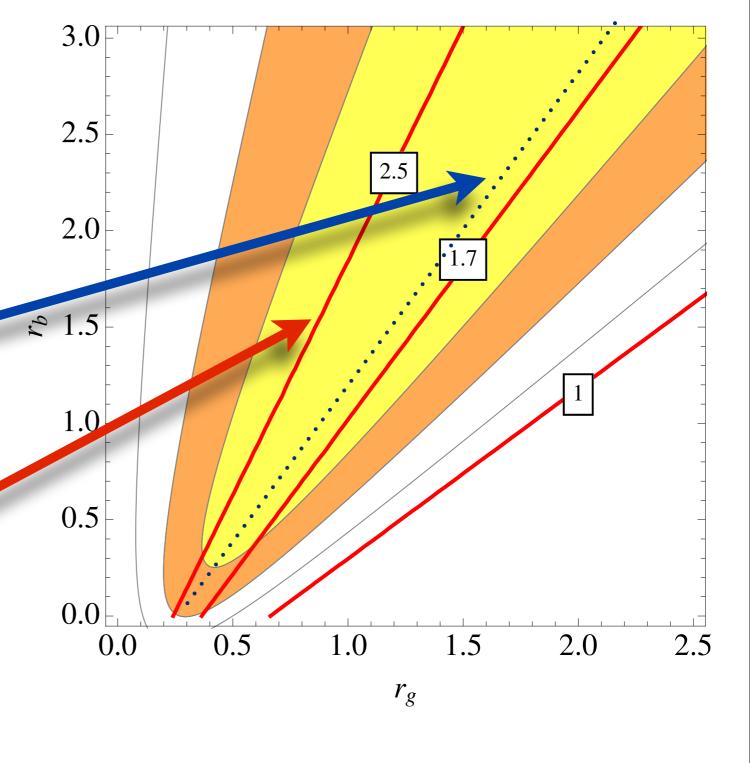
$$\mu_{i} = \frac{\sigma(pp \to h \to i)}{\sigma_{\rm SM}(pp \to h \to i)}$$

$$\mu_{\gamma\gamma} \simeq \frac{r_g r_{\gamma}}{1 + \operatorname{Br}_b(r_b - 1) + \operatorname{Br}_g(r_g - 1)},$$

$$\mu_{VV} \simeq \frac{r_g}{1 + \operatorname{Br}_b(r_b - 1) + \operatorname{Br}_g(r_g - 1)},$$

$$\mu_{b\bar{b}} \simeq \frac{r_b}{1 + \operatorname{Br}_b(r_b - 1) + \operatorname{Br}_g(r_g - 1)}$$

Shallow direction in $r_g - r_b$ plane



Minimal models.

"beautiful mirrors" [Choudhury, Tait, Wagner '01]

Shifts in $Z\bar{b}b$ couplings:

$$\delta g_{Lb} = \left(t_{3L} + \frac{1}{2}\right) s_L^2, \qquad \delta g_{Rb} = t_{3R} s_R^2,$$

Single out 3 possible vector-like representations:

$$\Psi_{L,R} \sim (3,2,1/6), (3,2,-5/6), (3,3,2/3)$$

Minimal models.

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$$\frac{1}{\sqrt{\delta_{\text{QLb}} > \delta_{\text{QRb}}, \text{ not useful}}}$$

Minimal models.

"beautiful mirrors" [Choudhury, Tait, Wagner '01]

Shifts in $Z\bar{b}b$ couplings:

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Single out 3 possible vector-like representations:

$$\Psi_{L,R} \sim (3,2,1/6), (3,2,-5/6), (3,3,2/3)$$

Only consider these

$$\delta g_{Lb} > \delta g_{Rb}$$
, not useful

$$\Psi_{L,R} \sim (T,B) \sim (3,2,1/6) \quad \begin{array}{l} \text{Choudhury, Tait, Wagner '0 I} \\ \text{Morrissey, Wagner '0 3} \end{array}$$

$$\delta g_{Lb} = \left(t_{3L} + \frac{1}{2}\right) s_L^2, \qquad \delta g_{Rb} = t_{3R} s_R^2, \quad {\sf T_{3R}(B)} = -1/2 \ {\sf Want to have } \delta g_{\sf Rb} \approx -0.17$$

Mixing between T and top quark \Rightarrow Wt_Rb_R coupling Ruled out by $b \rightarrow s \gamma$.

$$\Psi_{L,R} \sim (T,B) \sim (3,2,1/6) \quad {\hbox{Choudhury, Tait, Wagner '0 I} \atop \hbox{Morrissey, Wagner '03}}$$

$$\delta g_{Lb} = \left(t_{3L} + \frac{1}{2}\right) s_L^2, \qquad \delta g_{Rb} = t_{3R} s_R^2, \quad {\sf T_{3R}(B) = -1/2} {\sf Want to have } \delta g_{\sf Rb} \approx -0.17$$

Mixing between T and top quark \Rightarrow Wt_Rb_R coupling Ruled out by $b \rightarrow s \gamma$.

No T-t mixing ⇒ Large custodial breaking.

Precision data: $M_{T.B}$ 100-200 GeV, very heavy Higgs. Inconsistent with $m_h = 126$ GeV!

$$\Psi_{L,R} \sim (T,B) \sim (3,2,1/6) \quad \begin{array}{l} \text{Choudhury, Tait, Wagner '0 I} \\ \text{Morrissey, Wagner '03} \end{array}$$

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Precision data: $M_{T.B}$ 100-200 GeV, very heavy Higgs. Inconsistent with $m_h = 126$ GeV!

Even if this can be fixed. Sizable negative $\delta g_{bR} \Rightarrow large\ HB_Rb_R$ coupling.

 $M_{T.B}$ 100-200 GeV $\Rightarrow \mu_{VV} \sim 2.4$, in conflict with Higgs data!

$$\Psi_{L,R} \sim (B,X) \sim (3,2,-5/6)$$

$$\delta g_{Lb} = \left(t_{3L} + \frac{1}{2}\right)s_L^2, \qquad \delta g_{Rb} = t_{3R}s_R^2, \quad \text{Want to have } \delta g_{Rb} \approx 0.016$$

X charge -4/3. No mixing with top quark. Only need smaller mixing angle: $s_R \approx 0.2$

Good fit to precision data.

Consistent with Higgs data.

Deviation from SM very small.

Explore more variations

Adding singlet exotic fermions:

$$\Psi_{L,R}^T = (B,X) \sim (3,2,-5/6),$$

 $\hat{B}_{L,R} \sim (3,1,-1/3),$
 $\hat{X}_{L,R} \sim (3,1,-4/3).$

• Quantum numbers under $SU(2)_L \times SU(2)_R \times U(1)_X$

$$\Psi_{L,R}^T = (B, X) \sim (2, 1)_{-5/6}$$

 $\hat{\Psi}_{L,R}^T = (\hat{B}, \hat{X}) \sim (1, 2)_{-5/6}$

 Such representations can find motivation in composite Higgs models
 [Agashe, Contino, Da Rold, Pomarol '06]

Lagrangian

$$-\mathcal{L} \supset M_{1}\bar{\Psi}'_{L}\Psi'_{R} + M_{2}\bar{\hat{B}}'_{L}\hat{B}'_{R} + M_{3}\bar{\hat{X}}'_{L}\hat{X}'_{R} + y_{1}\bar{Q}'_{L}Hb'_{R} + y_{2}\bar{Q}'_{L}H\hat{B}'_{R} + y_{3}\bar{\Psi}'_{L}\tilde{H}b'_{R} + y_{4}\bar{\Psi}'_{L}\tilde{H}\hat{B}'_{R} + y_{5}\bar{\hat{B}}'_{L}\tilde{H}^{\dagger}\Psi'_{R} + y_{6}\bar{\Psi}'_{L}H\hat{X}'_{R} + y_{7}\bar{\hat{X}}'_{L}H^{\dagger}\Psi'_{R}$$

- Custodial limit: $M_2 = M_3, \ y_4 = y_6, \ y_5 = y_7$
- Note that y_1 , y_2 , y_3 explicitly break custodial symmetry, but only small values required to obtain required shifts δg_{Lb} , δg_{Rb} ,

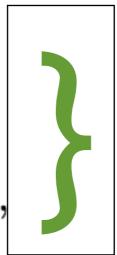
Yukawa contributions small, suggested by collider limits

$$Y_i = y_i v / \sqrt{2} \ll M_{1,2,3}$$

Integrate out heavy fermions to obtain effective theory

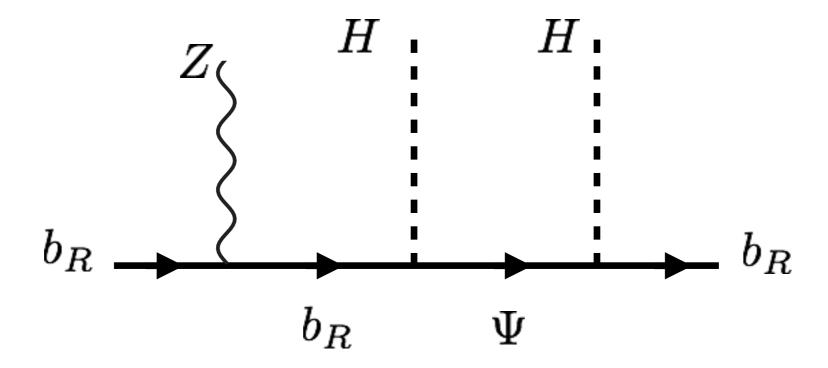
$$\mathcal{L} = \sum_i a_i \mathcal{O}_i$$

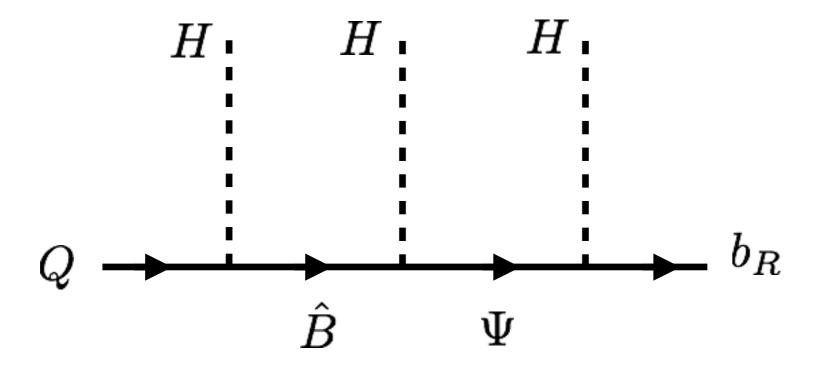
$$\begin{split} \mathcal{O}_{Hb} &= i(H^{\dagger}D_{\mu}H)(\bar{b}_{R}\gamma^{\mu}b_{R}) + \text{h.c.}, \\ \mathcal{O}_{HQ}^{s} &= i(H^{\dagger}D_{\mu}H)(\bar{Q}\gamma^{\mu}Q) + \text{h.c.}, \\ \mathcal{O}_{HQ}^{t} &= i(H^{\dagger}\sigma^{a}D_{\mu}H)(\bar{Q}\gamma^{\mu}\sigma^{a}Q) + \text{h.c.}, \end{split}$$



$$\mathcal{O}_{HY} = (H^\dagger H)(ar{Q}Hb_R) + ext{h.c..}$$
 | lead to shift in $m_b, y_{hbar{b}}$







$$\delta g_{Lb} = \frac{Y_2^2}{2M_2^2}, \quad \delta g_{Rb} = \frac{Y_3^2}{2M_1^2} \qquad Y_i = y_i v / \sqrt{2}$$

To fix Zbb, $\delta g_{Rb} \sim 0.015$, $\delta g_{Lb} \sim 0.001$,

$$Y_2 \simeq \pm 0.04 \, M_2 \quad Y_3 \simeq \pm 0.17 \, M_1$$

$$\delta g_{Lb} = \frac{Y_2^2}{2M_2^2}, \quad \delta g_{Rb} = \frac{Y_3^2}{2M_1^2} \qquad Y_i = y_i v / \sqrt{2}$$

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b-quark mass & hbb coupling

$$m_b = Y_1 \left(1 - \frac{Y_2^2}{2M_2^2} - \frac{Y_3^2}{2M_1^2} \right) + \frac{Y_2 Y_3 Y_5}{M_1 M_2}$$

$$y_{hbb} = \frac{1}{v} \left[Y_1 \left(1 - \frac{3Y_2^2}{2M_2^2} - \frac{3Y_3^2}{2M_1^2} \right) + \frac{3Y_2 Y_3 Y_5}{M_1 M_2} \right]$$

$$r_b = \left(\frac{y_{hbb}}{m_b/v}\right)^2 \approx 1 + 8\sqrt{\delta g_{Rb}\delta g_{Rb}} \frac{Y_5}{m_b}$$

Large corrections to h o b ar b possible if Y_5 large

h o gg and $h o \gamma\gamma$: Use low energy theorem

[Ellis, Gaillard, Nanopoulos `76] [Shifman, Vainshtein, Voloshin, Zakharov `79]

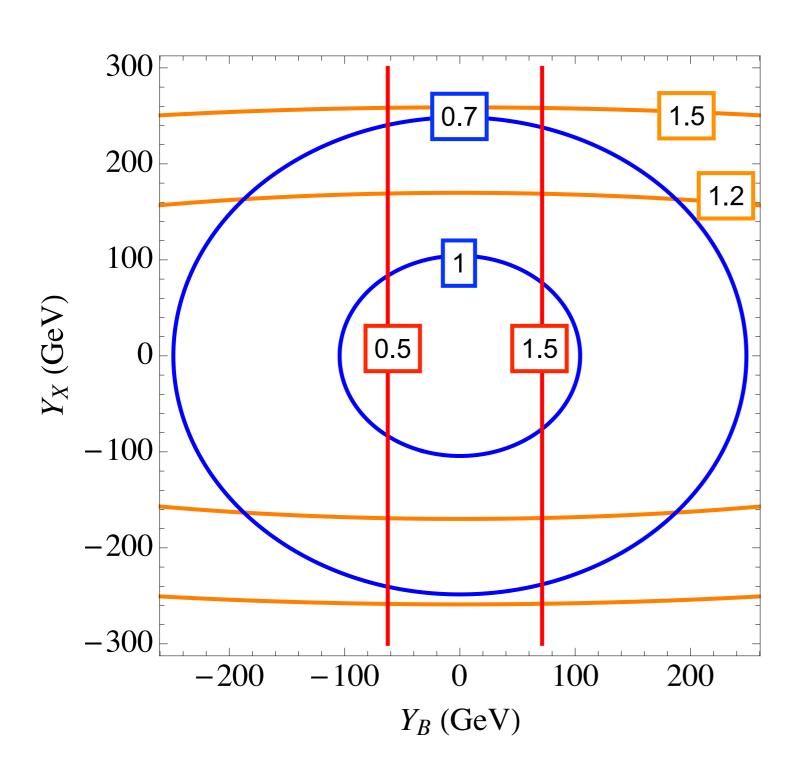
$$\mathcal{L} \supset rac{lpha}{16\pi v} \left[\sum_{f=B,X} b_f^{EM} z_f \, \right] h F_{\mu
u} F^{\mu
u} + rac{lpha_s}{16\pi v} \left[\sum_{f=B,X} b_f^c z_f \, \right] h G_{\mu
u}^a G^{\mu
u a},$$

$$b_B^{EM} = 4/9, \quad b_X^{EM} = 64/9, \quad b_B^c = b_X^c = 2/3.$$

$$z_f \equiv \frac{\partial}{\partial \log v} \left(\sum_i \log m_{f,i}^2(v) \right),$$

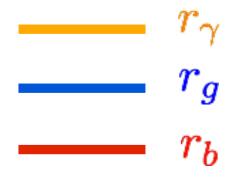
$$z_B \simeq -4 rac{Y_4 Y_5}{M_1 M_2} \qquad z_X \simeq -4 rac{Y_6 Y_7}{M_1 M_3}$$

$$r_{\gamma} \simeq \left| 1 + 0.13 \left(\frac{Y_4 Y_5}{M_1 M_2} + 16 \frac{Y_6 Y_7}{M_1 M_3} \right) \right|^2$$
 , $r_g \simeq \left| 1 - 2.1 \left(\frac{Y_4 Y_5}{M_1 M_2} + \frac{Y_6 Y_7}{M_1 M_3} \right) \right|^2$



$$Y_4 = Y_5 = Y_B$$

 $Y_6 = Y_7 = Y_X$
 $M_{1,2,3} = 800 \text{ GeV}$



Direct searches for Heavy Quarks

- Signatures similar to minimal (3,2,-5/6) model [Kumar, Shepard, Tait, Vega-Morales '10]
- Most robust limit comes from top prime searches

CMS search in dilepton channel [CMS-EXO-11-050]

$$pp \to t'\bar{t}' \to (W^+b)(W^-\bar{b}) \to \ell^+\ell^-\nu\nu\bar{b}\bar{b}$$

Bounds masses heavier than $m_{t'} > 557~{
m GeV}$

ullet These bounds apply since X decays via $X o bW^-$

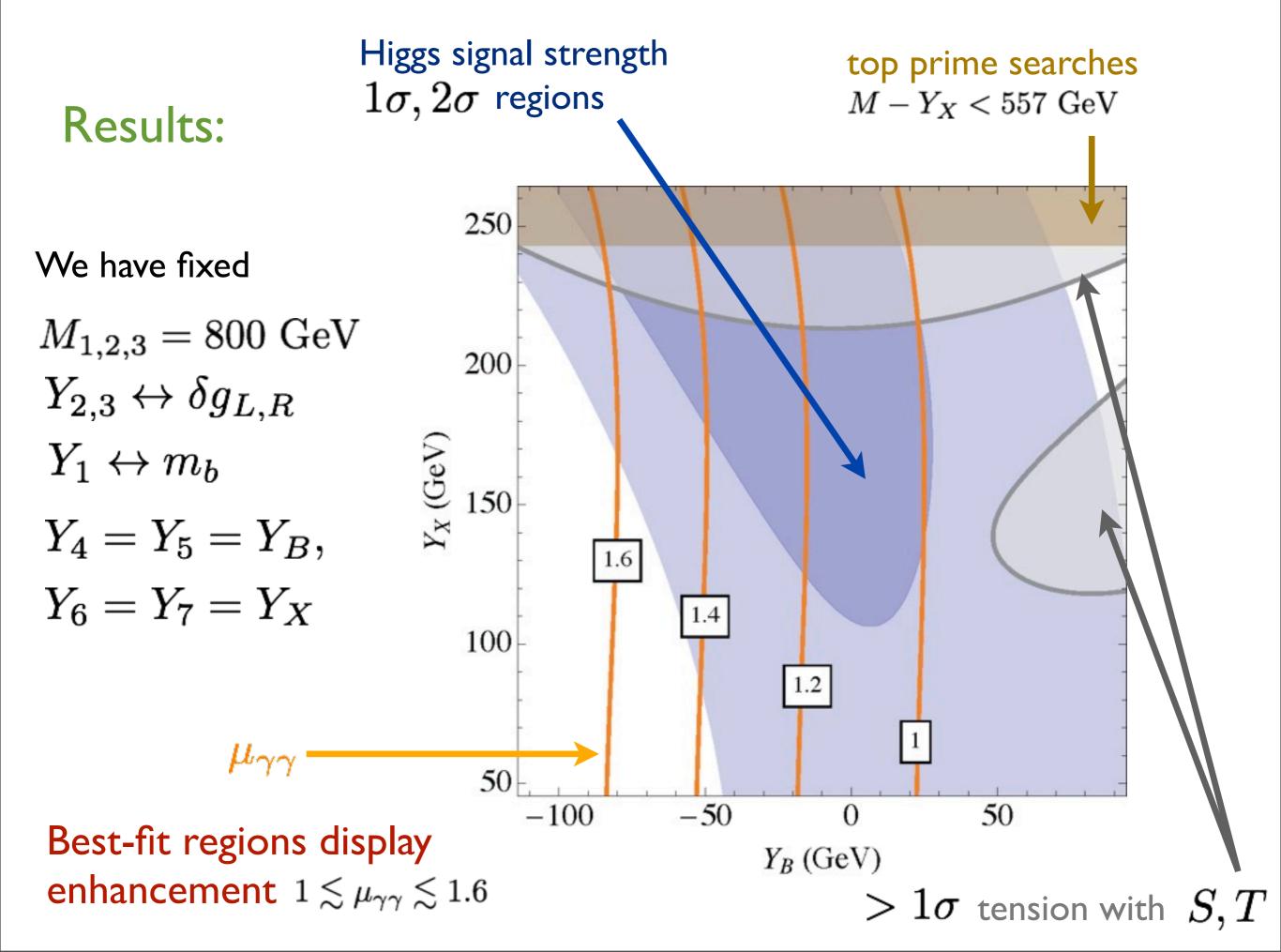
Other possible decay mode $X \to BW$ requires $m_X > m_B + m_W$, not favored by Higgs data (see shortly)

Also bounds exist from bottom prime searches:

$$pp \to b'\bar{b}' \to W^-tW^+\bar{t} \to 4W2b \to 3\ell + b \text{ or SS } \ell + b$$

Bounds masses heavier than $m_{b'} > 611 \; {\rm GeV}$

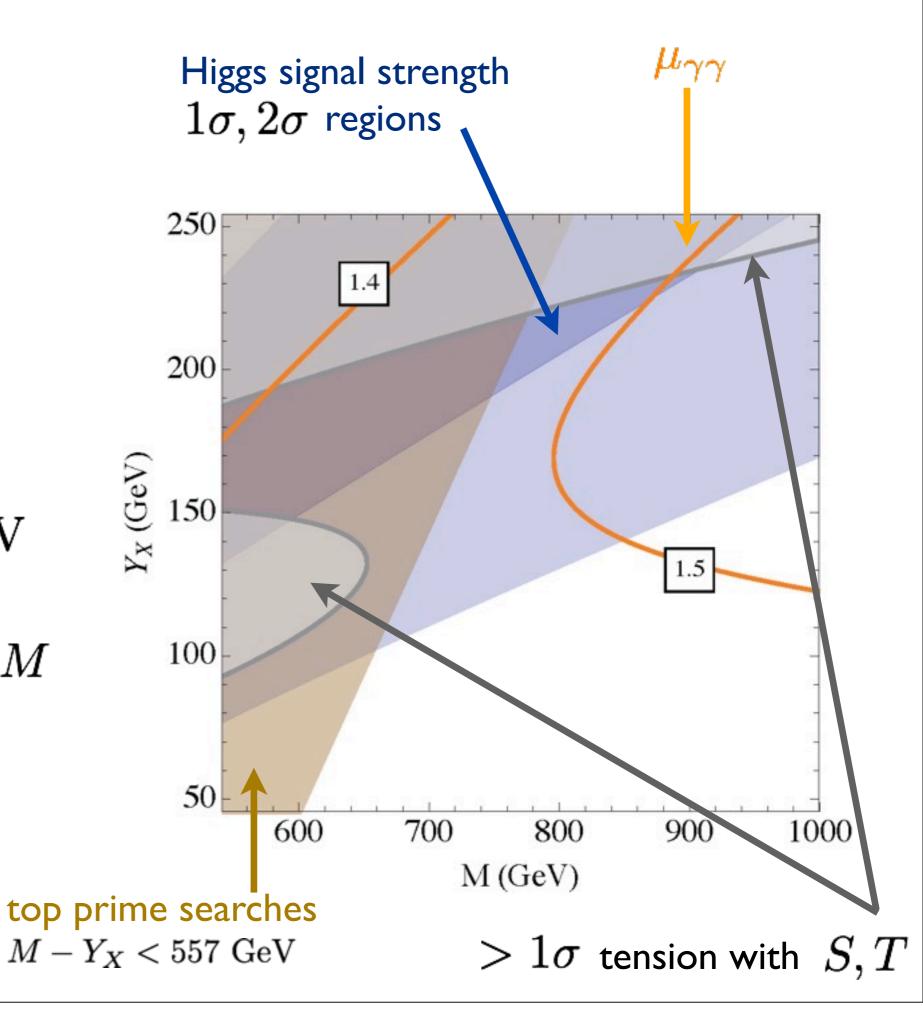
[CMS-EXO-11-036]



Results:

We have fixed

$$Y_{2,3} \leftrightarrow \delta g_{L,R}$$
 $Y_1 \leftrightarrow m_b$
 $Y_4 = Y_5 = -65 \text{ GeV}$
 $Y_6 = Y_7 = Y_X$
 $M_1 = M_2 = M_3 = M$



Outlook:

- 125 GeV Higgs discovered as suggested by EW data
- Higgs SM-like. Still plenty of room for deviation, such as in $\mu_{\gamma\gamma}$.
- Two discrepancies in EW data: A_{FB}^{b} (2.6 σ), R_{b} (2.4 σ)
- Can shift $Z \overline{b}_R b_R$ by b-B mixing
- Exotic B-quark can cause deviations in Higgs properties, interesting limits from Higgs data already.
- Model is directly testable at LHC via search for exotic ("beautiful mirror") quarks



Caveat: Vacuum stability

As emphasized recently in several works, new fermions with O(I) Yukawa's drive Higgs quartic negative at low scale

Jogelkar, Schwaller, Wagner `12 Arkani-Hamed, Blum, D'Agnolo, Fan `12 Reece `12

In our model,

- Model requires a UV completion to stabilize vacuum...
- Obvious candidate is a SUSY version (beyond scope here)

Ingredients going into the electroweak fit:

Observables

$$m_{Z}, \; \Gamma_{Z}, \; \sigma_{\mathrm{had}}^{0}, \; R_{\ell}, \; R_{c}, \; R_{b}, \ A_{FB}^{\ell}, \; A_{\ell}, \; A_{c}, \; A_{b}, \; A_{FB}^{c}, \; A_{FB}^{b}, \; \sin^{2}\theta_{\mathrm{eff}}, \ m_{W}, \; \Gamma_{W}, \; m_{t}, \; \Delta\alpha_{\mathrm{had}}^{(5)}, \; m_{h}$$

Vary SM + NP parameters in fit

$$m_H, m_Z, m_t, \Delta \alpha_{\rm had}^{(5)}, \alpha_s,$$

 $S, T, \delta g_{Lb}, \delta g_{Rb}$

• Theory predictions taken from various numerical parameterizations in literature...

$$A_{FB}^{b}$$

$$\mathcal{L} \supset rac{g}{c_W} Z_\mu ar{b} (g_{Lb} P_L + g_{Rb} P_R) b$$

Consider the process

$$e^+e^- \to \gamma, Z, \to b\bar{b}$$

Forward, backward cross sections:

$$\sigma_{F,B} = \mp \int_0^{\pm 1} \frac{d\sigma}{d\cos\theta} d\cos\theta$$

Polarized cross sections:

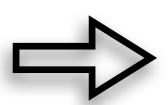
$$\sigma_{LL} \equiv \sigma(e_L^+ e_L^- \to b_L \bar{b}_L), \text{ etc.}$$

Forward-backward asymmetry:

$$A_{FB} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{3}{4} \frac{\sigma_{LL} + \sigma_{RR} - \sigma_{LR} - \sigma_{RL}}{\sigma_{LL} + \sigma_{RR} + \sigma_{LR} + \sigma_{RL}}$$

On Z-pole:

$$\sigma_{LL} \propto rac{g_{Le}g_{Lb}}{m_Z\Gamma_Z}$$
 , etc.



$$A_{FB} = \frac{3}{4} \frac{g_{Le}^2 - g_{Re}^2}{g_{Le}^2 + g_{Re}^2} \frac{g_{Lb}^2 - g_{Rb}^2}{g_{Lb}^2 + g_{Rb}^2}$$

$$R_b$$

$$\mathcal{L} \supset rac{g}{c_W} Z_{\mu} ar{b} (g_{Lb} P_L + g_{Rb} P_R) b$$

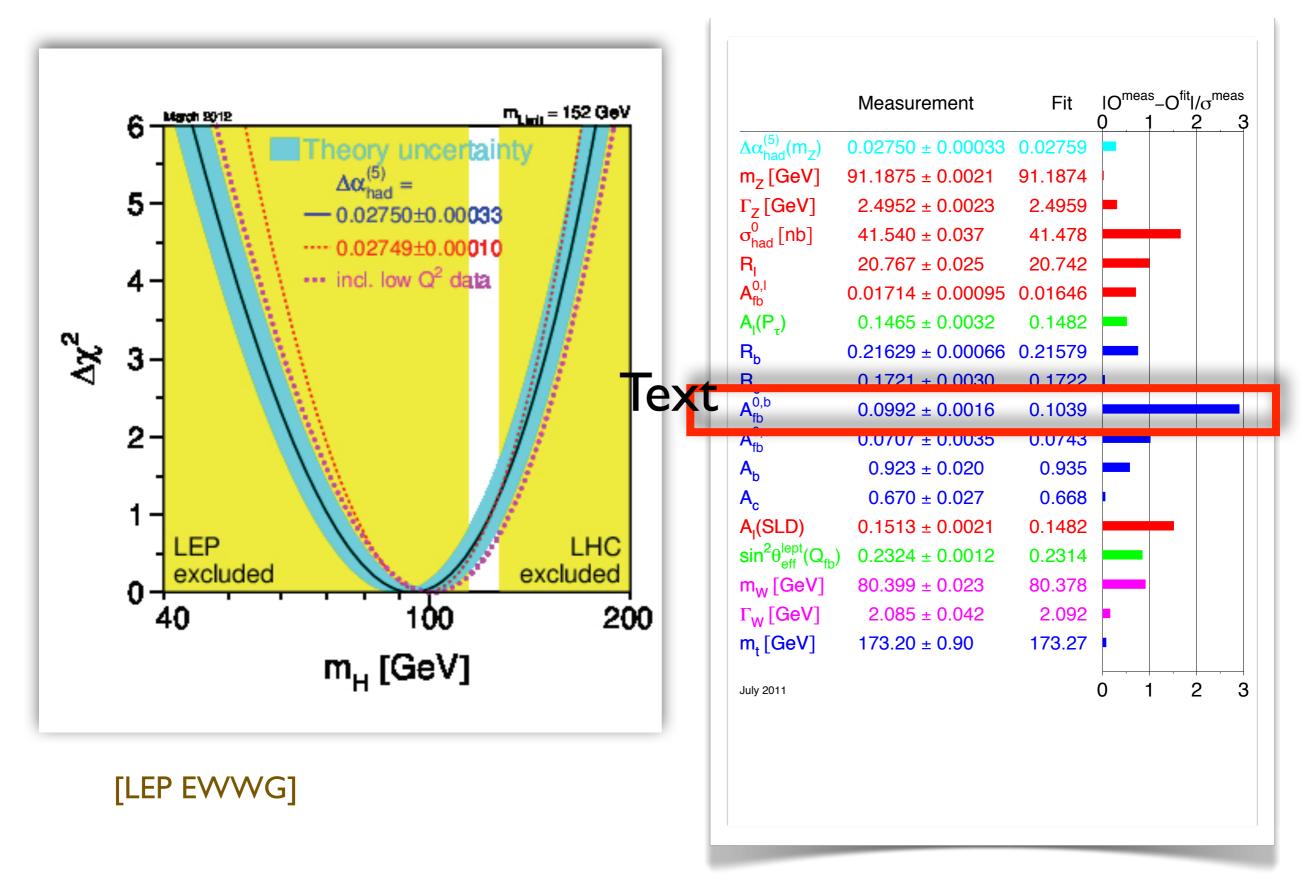
Z boson partial width: $\Gamma(Z o \psi_i ar{\psi}_i) \simeq rac{g^2}{24\pi c_W^2} (g_{Li}^2 + g_{Ri}^2) M_Z$

$$R_b \equiv \frac{\Gamma(Z \to b\bar{b})}{\Gamma(Z \to \text{hadrons})} \simeq \frac{g_{Lb}^2 + g_{Rb}^2}{\sum_a [g_{La}^2 + g_{Ra}^2]}$$

Note: both A_{FB}^b, R_b depend on couplings g_{Lb}, g_{Rb}

Suggests common resolution: tree-level shifts in $Zbar{b}$

Precision Electroweak Data (circa December 2011)



A_{FB}^{b}, R_{b} due to systematic effect

Including LHC Higgs mass measurement:

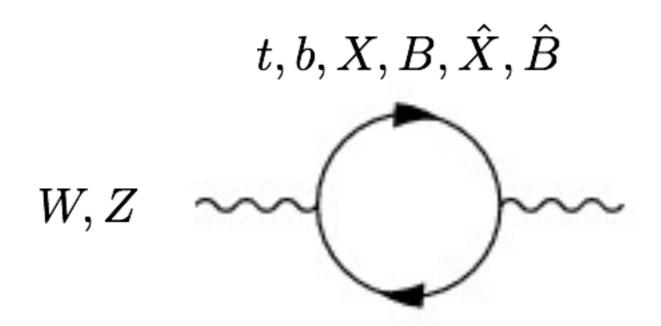
SM w/o
$$A_{FB}^b, R_b$$
 :
$$p = 0.67 \\ m_h = 125.7 \; \mathrm{GeV}$$

SM w/o
$$A_{FB}^b, R_b$$

$$S = -0.08 \pm 0.10$$

$$T = 0.0 \pm 0.08$$

- Marginal improvement with oblique parameters.
- No strong argument for new physics to pull up Higgs mass



- Contribution from new mirror quarks
- ullet $War{t}b,Zar{b}b$ vertices modified include t,b and subtract off SM
- ullet Restrict to 1σ regions determined by fit (including $\delta g_{L,R}$)

$$S = -0.02 \pm 0.09$$
, $T = 0.03 \pm 0.08$, $\rho \sim 0.90$