



$B_d \rightarrow K^{*0} \mu \mu$ with ATLAS

BEAUTY 2013

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For the
ATLAS collaboration

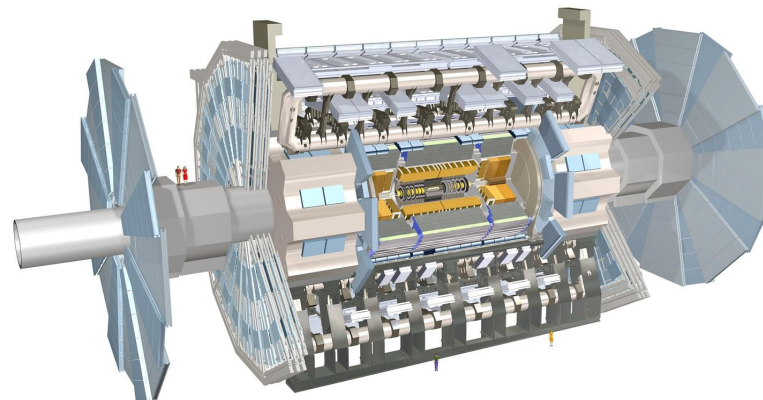
*ATLAS-CONF-2013-038 “Angular Analysis of $B_d \rightarrow K^{*0} \mu \mu$ with the ATLAS Experiment”*

Outline

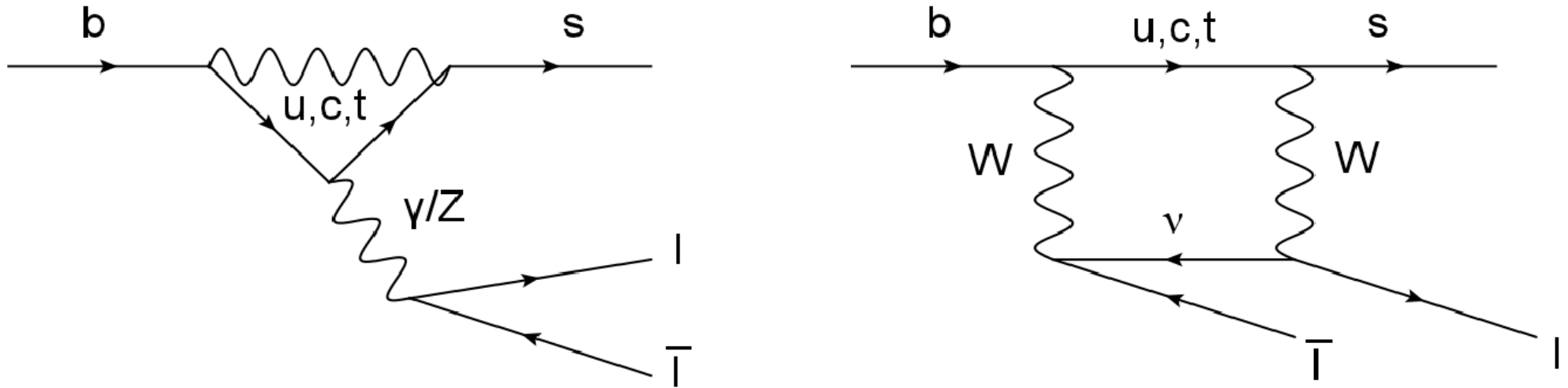
- Motivation
- Introduction
- Details of the analysis:
 - Data
 - Analysis strategy
 - Sources of systematic uncertainties
- Results, comparison
- Conclusions, outlook

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Motivation

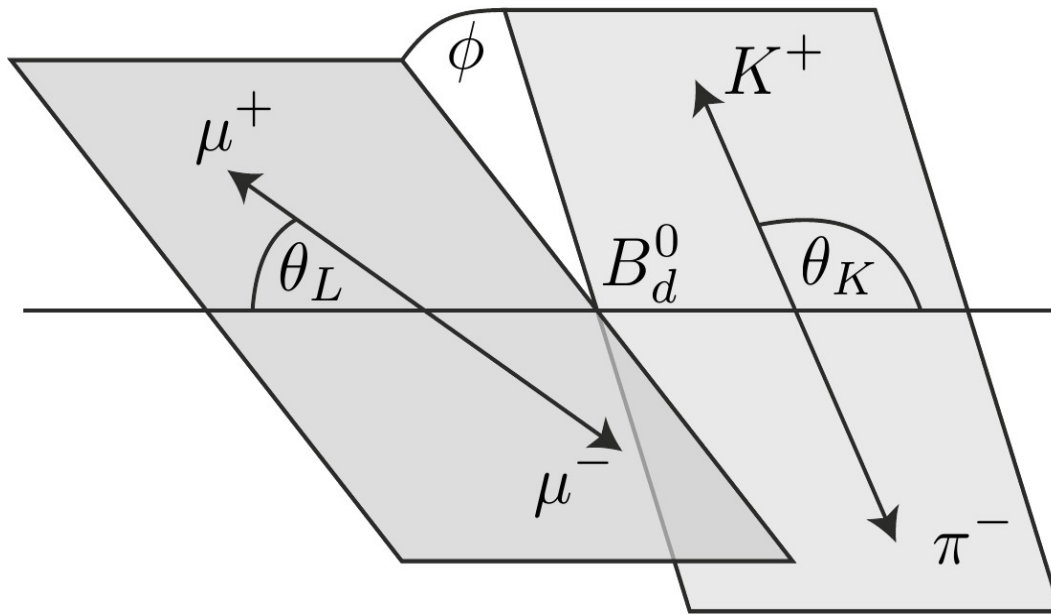


- $B_d \rightarrow K^{*0}(\rightarrow K^+\pi^-)\mu^+\mu^-$ is one of the exclusive final states for $b \rightarrow sl^+l^-$
- Rare decay with a relatively small branching fraction

$$Br(B_d \rightarrow K^{*0}\mu^+\mu^-) = (1.06 \pm 0.1) \cdot 10^{-6}$$
<http://pdg.lbl.gov>
- Can occur only on the loop level, as SM has no FCNCs on the tree level
- The angular distributions in these decays as a function of dilepton mass squared $q^2 = m^2(l^+l^-)$ are sensitive to many possible scenarios of physics beyond the SM

C. Bobeth et al. "Angular analysis of $B \rightarrow V(\rightarrow P_1P_2)l^+l^-$ decays" arXiv:1105.2659v1

Introduction



4 kinematic variables:
 q^2 – invariant mass of the leptons
 angles ϕ, θ_K, θ_L

F_L – fraction of longitudinally polarized K^*

A_{FB} – forward-backward asymmetry of muons

$$\frac{1}{\Gamma} \frac{d^2\Gamma}{dq^2 d \cos \theta_L} = \frac{3}{4} F_L(q^2) (1 - \cos^2 \theta_L) + \frac{3}{8} (1 - F_L(q^2)) (1 + \cos^2 \theta_L) + A_{FB}(q^2) \cos \theta_L$$

$$\frac{1}{\Gamma} \frac{d^2\Gamma}{dq^2 d \cos \theta_K} = \frac{3}{2} F_L(q^2) \cos^2 \theta_K + \frac{3}{4} (1 - F_L(q^2)) (1 - \cos^2 \theta_K)$$

Data and MC used

- 4.9 fb⁻¹ collected with ATLAS in 2011 at $\sqrt{s} = 7$ TeV
 - Single- and dimuon triggers
- MC event samples (PythiaB) used for selection optimization:
 - $B_d \rightarrow K^{0*} \mu \mu$ (signal)
 - $bb \rightarrow \mu \mu X$
 - $cc \rightarrow \mu \mu X$
 - Drell-Yan
 - $B_d \rightarrow J/\psi K^*$

Event selection

- Based on cuts

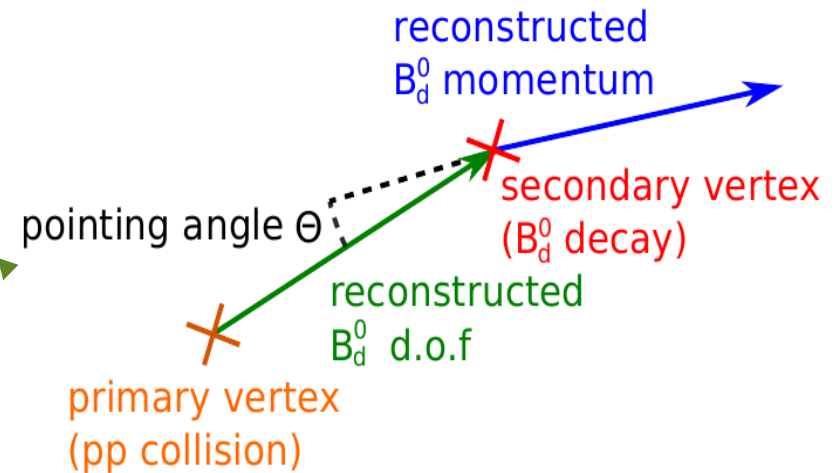
- Baseline:

- $p_T(\mu) > 3.5 \text{ GeV}$
- $|\eta| < 2.5$ for all tracks
- $\chi^2/\text{n.d.f}(\mu\mu) < 10$
- $846 < M(K^{*0}) < 946 \text{ MeV}$
- $p_T(K) > 0.5 \text{ GeV}$
- $p_T(\pi) > 0.5 \text{ GeV}$

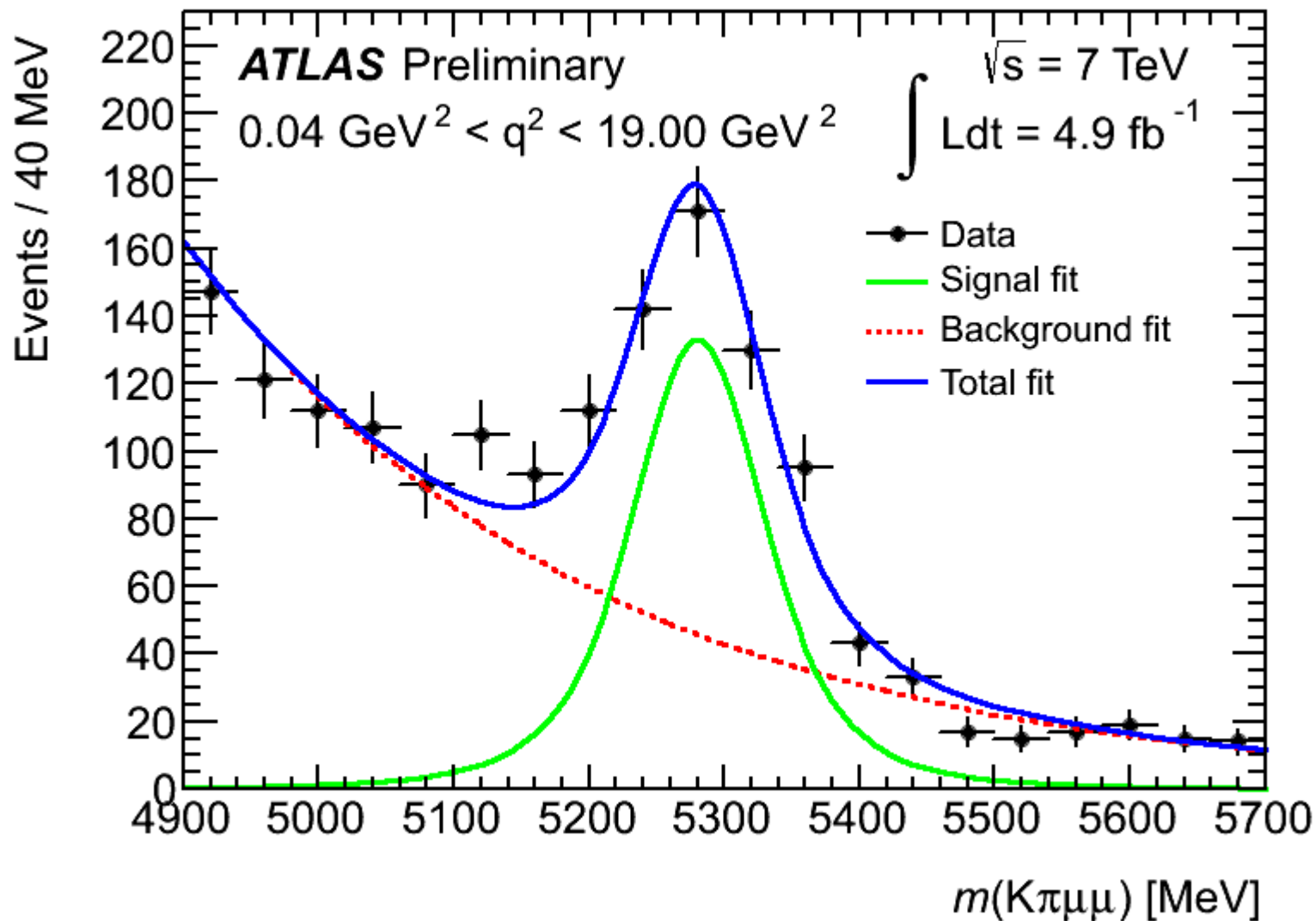
- $J/\psi, \Psi'(2S)$ regions are excluded

- Selection (cut values are optimized):

- $\tau/\Delta\tau(B_d) > 12.75$
- $\cos(\theta) > 0.999$
- $\chi^2/\text{n.d.f.}(B_d) < 2.0$
- $p_T(K^*) > 3 \text{ GeV}$
- $|(M(B^0)_{\text{rec}} - M(B^0)_{\text{PDG}})| - |(M(\mu\mu)_{\text{rec}} - M(J/\psi)_{\text{PDG}})| > 130 \text{ MeV}$



Signal observation



In full range of dimuon mass, with J/ψ , $\Psi'(2S)$ regions excluded

q^2 bins

Data is separated into 9 regions of dimuon mass [GeV^2] – binning identical to Belle

- $0.04 < q^2 < 2.00$ No angular analysis performed due to low number of events
- $2.00 < q^2 < 4.30$
- $4.30 < q^2 < 8.68$
- $8.68 < q^2 < 10.09$ J/ψ
- $10.09 < q^2 < 12.86$
- $12.86 < q^2 < 14.18$ $\Psi'(2S)$
- $14.18 < q^2 < 16.00$
- $16.00 < q^2 < 19.00$
- $1.00 < q^2 < 6.00$

Fit strategy

- Extended unbinned maximum likelihood fit

$$\mathcal{L} = \prod_{i=1}^N \left[N_{\text{sig}}^{\text{fix}} \cdot \mathcal{M}_{\text{sig}}(m_i, \delta_{m_i}) \cdot \mathcal{A}_{L,\text{sig}}(\cos \theta_{L,i}) \cdot \alpha_L(\cos \theta_{L,i}) \cdot \mathcal{A}_{K,\text{sig}}(\cos \theta_{K,i}) \cdot \alpha_K(\cos \theta_{K,i}) + N_{\text{bckg}}^{\text{fix}} \cdot \mathcal{M}_{\text{bckg}}(m_i) \cdot \mathcal{A}_{L,\text{bckg}}(\cos \theta_{L,i}) \cdot \mathcal{A}_{K,\text{bckg}}(\cos \theta_{K,i}) \right]$$

Mass term Angular terms

- Sequential fit approach: first mass distribution is fitted, then a multidimensional dataset is fitted with fixed parameters of the mass PDF

$$\mathcal{L} = \prod_{i=1}^N \left[N_{\text{sig}} \cdot \mathcal{M}_{\text{sig}}(m_i, \delta_{m_i}) + N_{\text{bckg}} \cdot \mathcal{M}_{\text{bckg}}(m_i) \right]$$

Performed individually in each q^2 bin

- Mass distribution: signal \rightarrow gaussian with per-event errors, background \rightarrow exponential

$$\mathcal{M}_{\text{sig}}(m_i, \delta_{m_i}) = \frac{1}{\sqrt{2\pi} s_m \delta_{m_i}} \exp\left(\frac{-(m_i - m_{B^0})^2}{2(s_m \delta_{m_i})^2}\right) \quad \mathcal{M}_{\text{bckg}}(m_i) = e^{-\lambda \cdot m_i}$$

Acceptance functions, taking into account detector and cuts effects on angular shape. Polynomials obtained from fit to signal MC sample

Fit strategy

- Angular terms

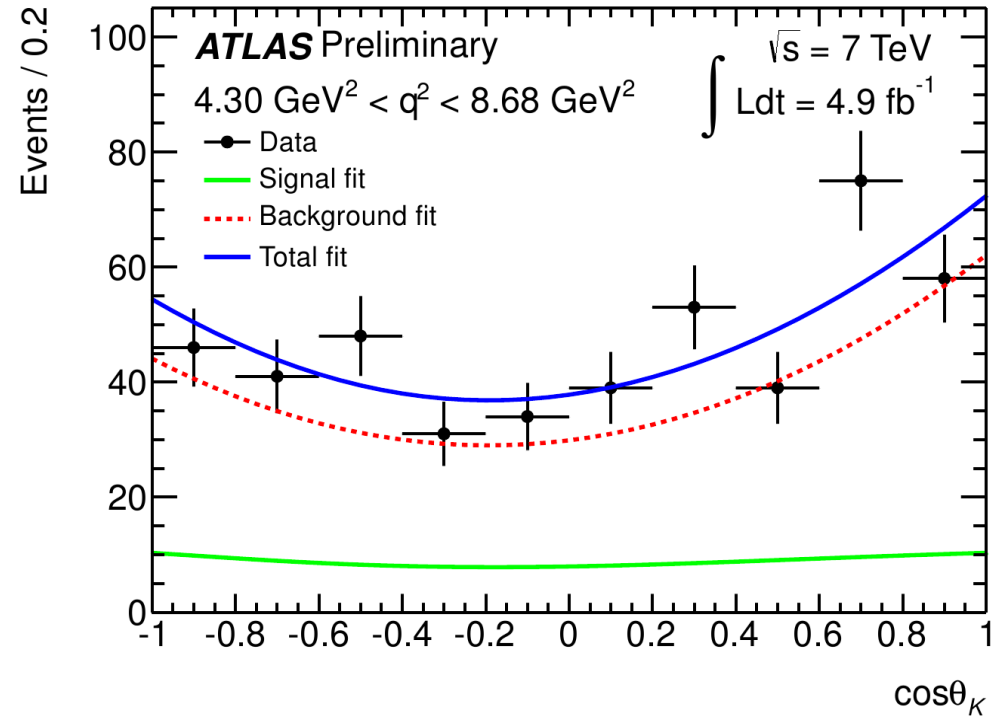
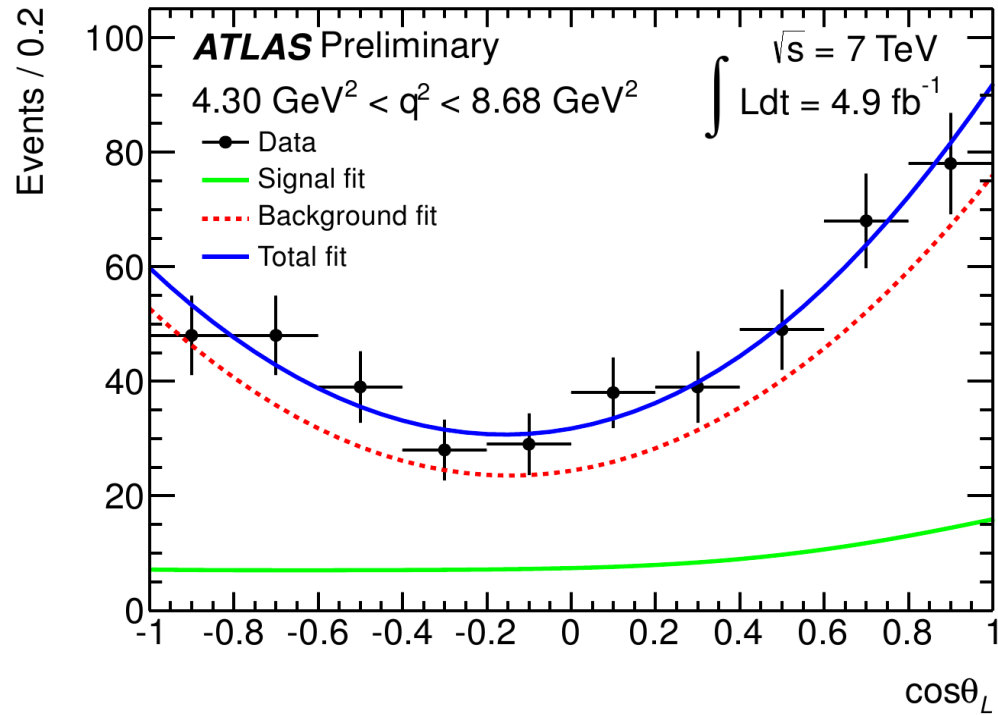
- Signal

$$\begin{aligned}\mathcal{A}_{L,\text{sig}}(\cos \theta_{L,i}) &= \left(\frac{3}{4} F_L (1 - (\cos \theta_{L,i})^2) \right. \\ &\quad \left. + \frac{3}{8} (1 - F_L) (1 + (\cos \theta_{L,i})^2) + A_{FB} \cos \theta_{L,i} \right) \\ \mathcal{A}_{K,\text{sig}}(\cos \theta_{K,i}) &= \frac{3}{2} F_L (\cos \theta_{K,i})^2 + \frac{3}{4} (1 - F_L) (1 - (\cos \theta_{K,i})^2)\end{aligned}$$

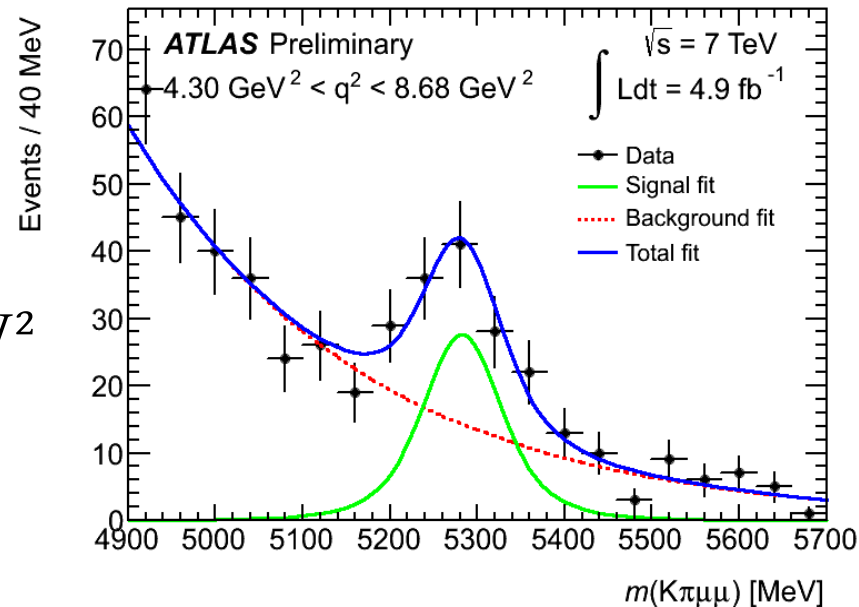
- Background – 2nd order Chebyshev polynomials

$$\begin{aligned}\mathcal{A}_{L,\text{bckg}}(\cos \theta_{L,i}) &= 1 + p_1 \cos \theta_{L,i} + p_2 (2(\cos \theta_{L,i})^2 - 1) \\ \mathcal{A}_{K,\text{bckg}}(\cos \theta_{K,i}) &= 1 + p_1 \cos \theta_{K,i} + p_2 (2(\cos \theta_{K,i})^2 - 1)\end{aligned}$$

Example of the fit



$4.30 \text{ GeV}^2 < q^2 < 8.68 \text{ GeV}^2$



Systematic uncertainties

- Mass fit region
- Angular background shape
- Contribution of $B^+ \rightarrow \mu^+\mu^-K^+$ events
- Acceptance effects
- Fit mode (sequential fit approach)
- Sources that were studied but found negligible:
 - S-wave contribution
 - $B_s \rightarrow \phi\mu^+\mu^-$ contribution
 - Bias due to the fit model (linearity, 1D-2D)

Systematic uncertainties

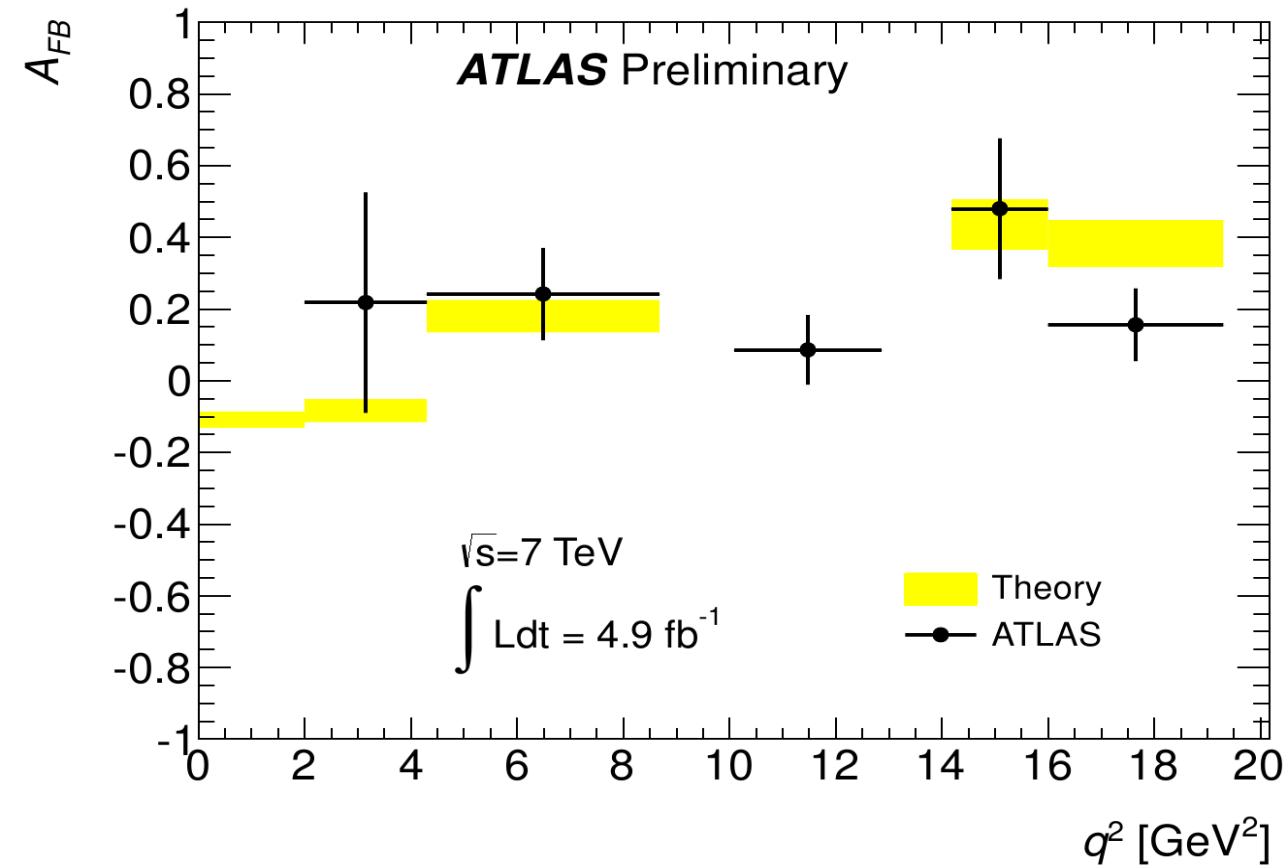
A_{FB}

q^2 range (GeV ²)	fit region	ang. fit	$B^\pm \rightarrow K^\pm \mu^+ \mu^-$	acc. maps	fit	SUM
$2.00 < q^2 < 4.30$	0.02	0.01	0.08	0.01	0.10	0.136
$4.30 < q^2 < 8.68$	0.00	0.01	0.01	0.01		0.013
$10.09 < q^2 < 12.86$	0.03	0.01	0.02	0.00		0.031
$14.18 < q^2 < 16.00$	0.03	0.01	0.03	0.02		0.050
$16.00 < q^2 < 19.00$	0.02	0.01	0.02	0.01		0.026
$1.00 < q^2 < 6.00$	0.05	0.01	0.02	0.04		0.069

F_L

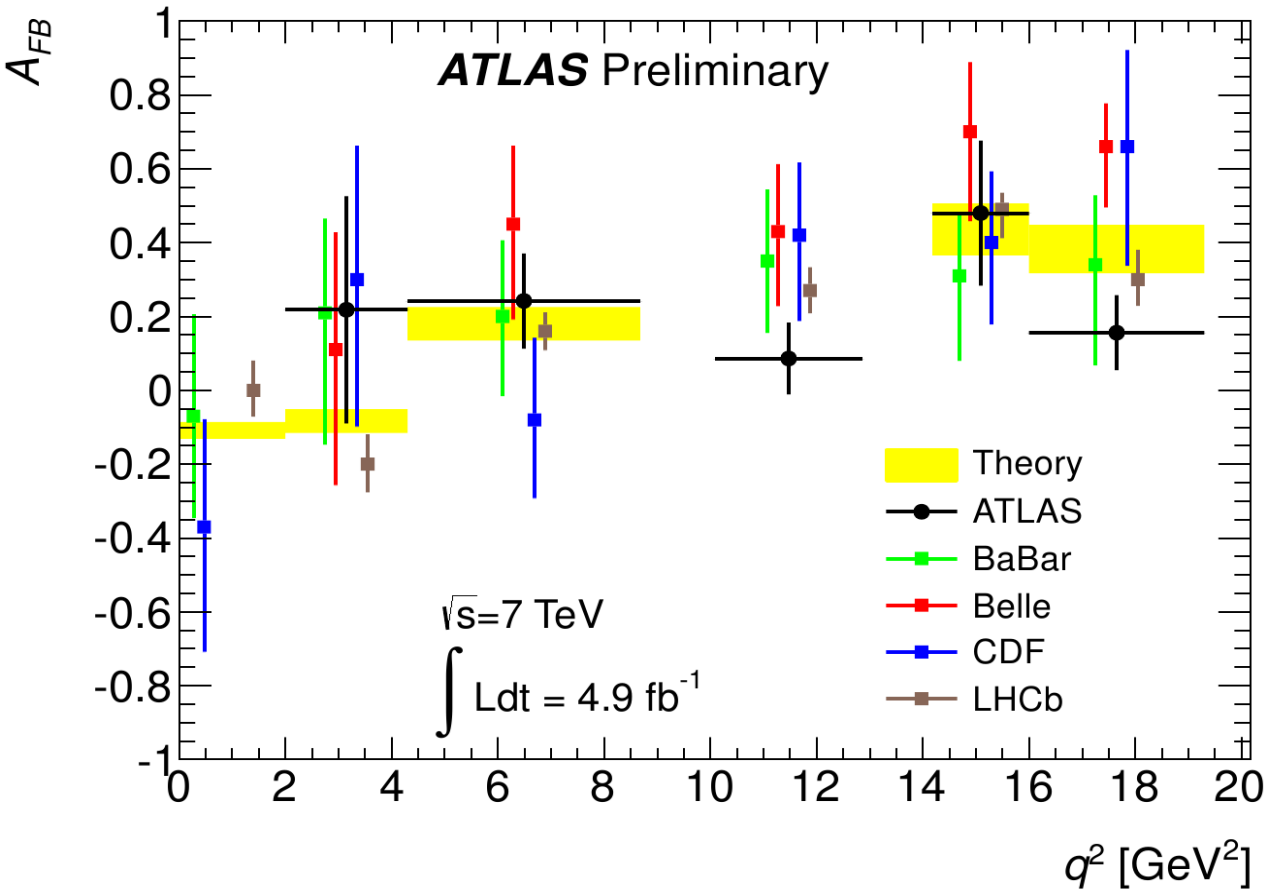
q^2 range (GeV ²)	fit region	ang. fit	$B^\pm \rightarrow K^\pm \mu^+ \mu^-$	acc. maps	fit	SUM
$2.00 < q^2 < 4.30$	0.01	0.01	0.02	0.01	0.05	0.058
$4.30 < q^2 < 8.68$	0.01	0.01	0.00	0.02		0.021
$10.09 < q^2 < 12.86$	0.04	0.01	0.00	0.02		0.042
$14.18 < q^2 < 16.00$	0.01	0.01	0.02	0.01		0.025
$16.00 < q^2 < 19.00$	0.02	0.01	0.01	0.00		0.023
$1.00 < q^2 < 6.00$	0.02	0.01	0.00	0.03		0.034

Result: A_{FB}



q^2 range (GeV^2)	N_{sig}	A_{FB}	F_L
$2.00 < q^2 < 4.30$	19 ± 8	$0.22 \pm 0.28 \pm 0.14$	$0.26 \pm 0.18 \pm 0.06$
$4.30 < q^2 < 8.68$	88 ± 17	$0.24 \pm 0.13 \pm 0.01$	$0.37 \pm 0.11 \pm 0.02$
$10.09 < q^2 < 12.86$	138 ± 31	$0.09 \pm 0.09 \pm 0.03$	$0.50 \pm 0.09 \pm 0.04$
$14.18 < q^2 < 16.00$	32 ± 14	$0.48 \pm 0.19 \pm 0.05$	$0.28 \pm 0.16 \pm 0.03$
$16.00 < q^2 < 19.00$	149 ± 24	$0.16 \pm 0.10 \pm 0.03$	$0.35 \pm 0.08 \pm 0.02$
$1.00 < q^2 < 6.00$	42 ± 11	$0.07 \pm 0.20 \pm 0.07$	$0.18 \pm 0.15 \pm 0.03$

Result: A_{FB}



BaBar: arXiv:0804.4412

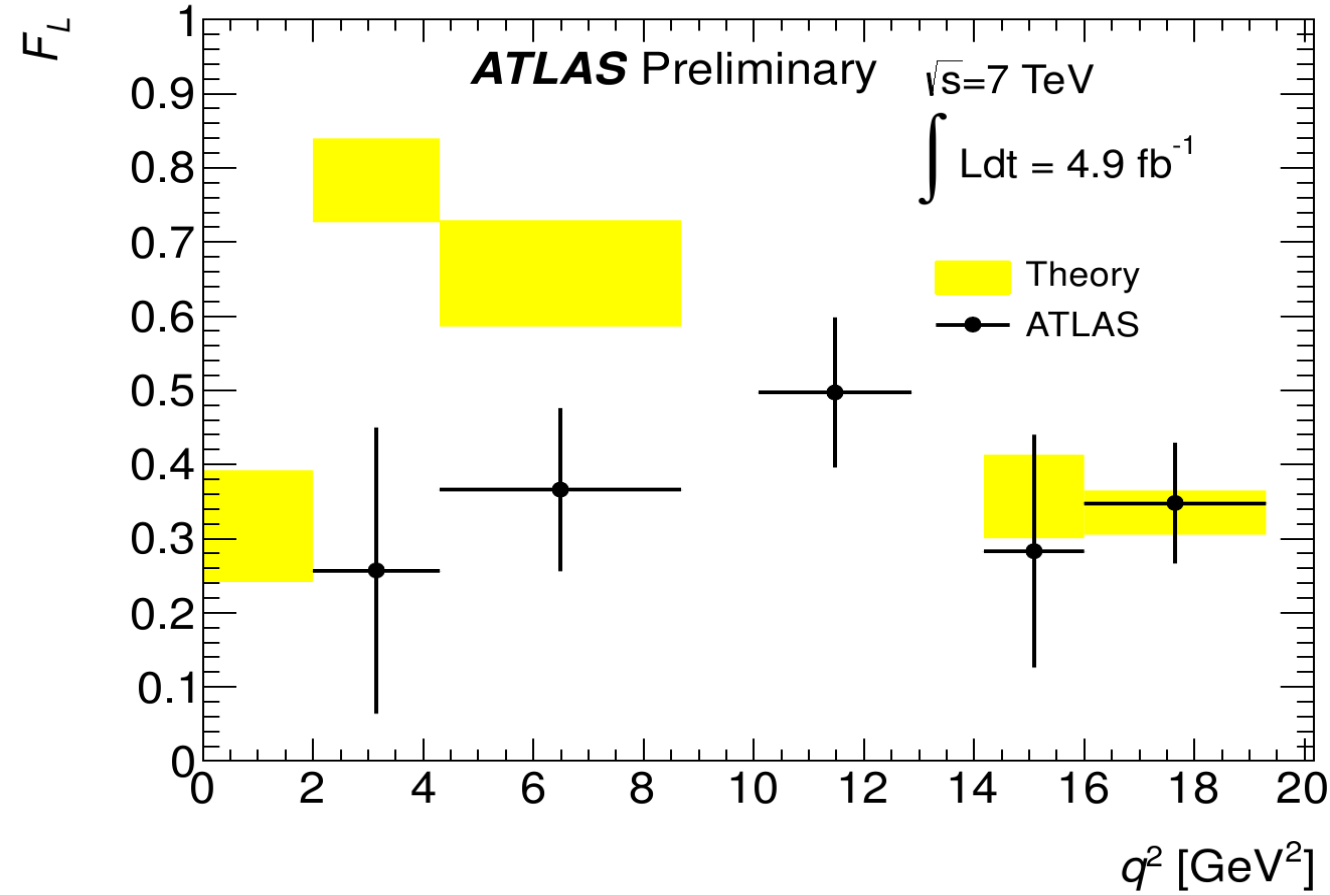
Belle: arXiv:0904.0770

CDF: arXiv:1108.0695

LHCb: <http://cds.cern.ch/record/1427691>

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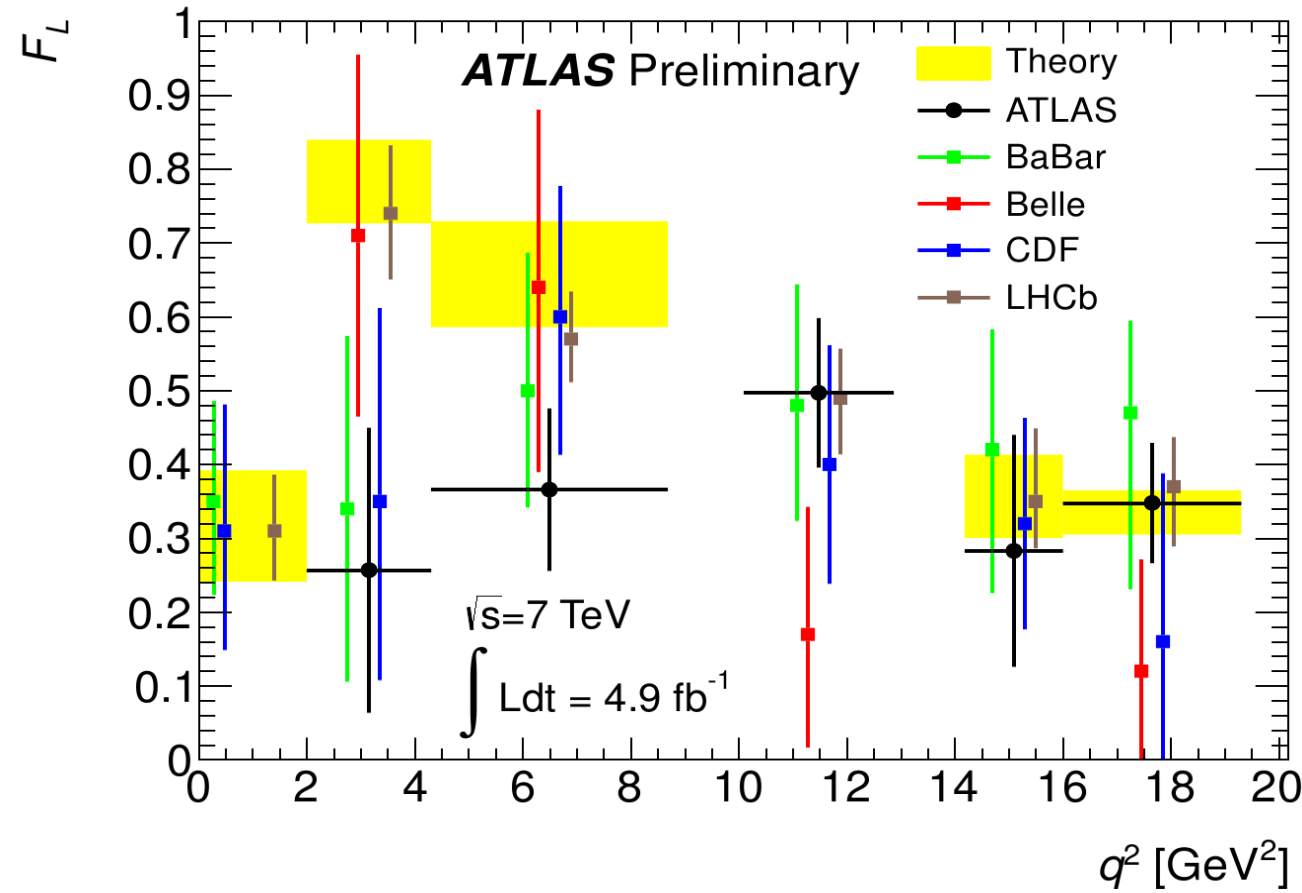
Result: F_L



Theory prediction:
 arXiv:1105.2659v1

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Result: F_L



BaBar: arXiv:0804.4412
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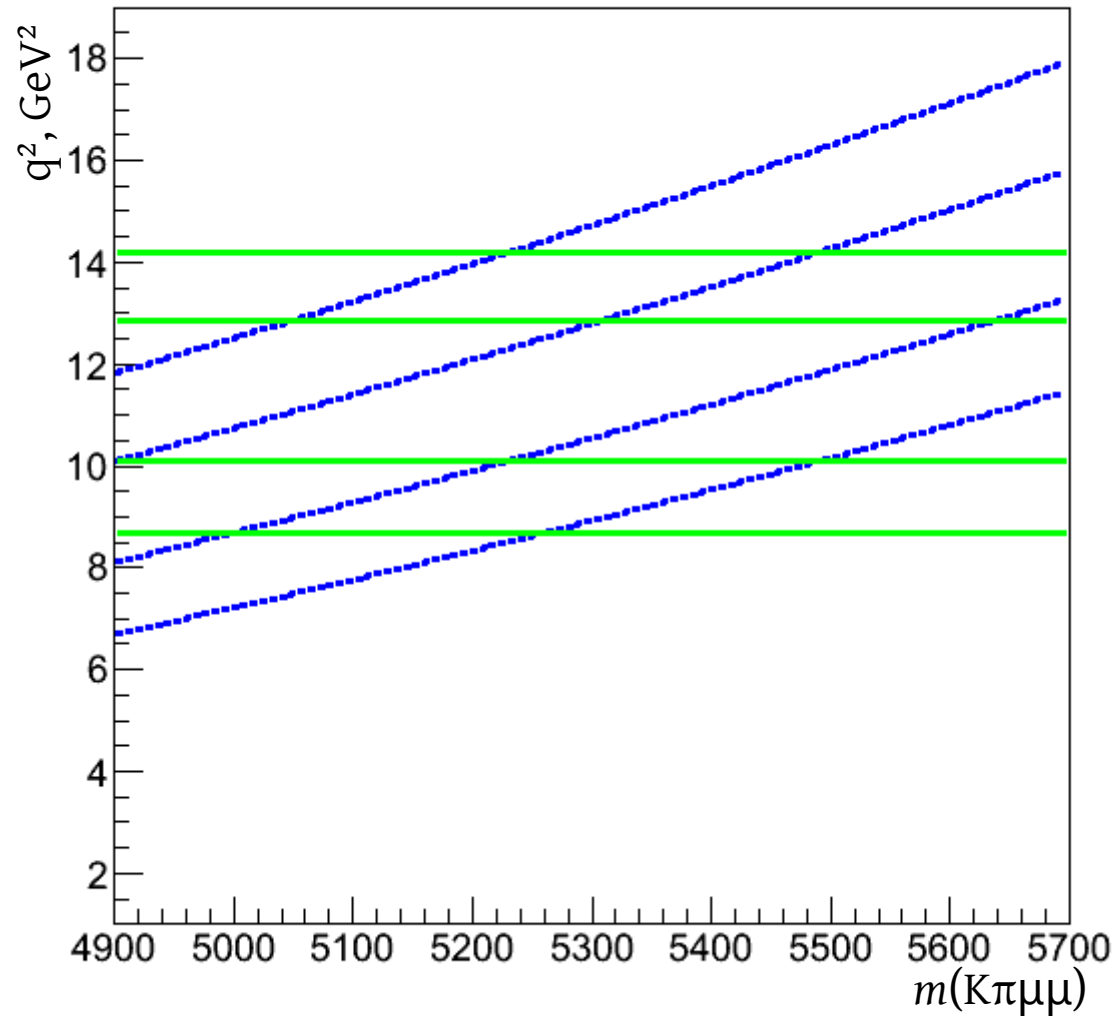
Conclusions, outlook

- We performed an analysis of 2011 data to study the angular distribution of $B_d \rightarrow K^* \mu^+ \mu^-$ decay
- 466 signal events were observed, A_{FB} and F_L values measured
- We have looked at various sources of possible systematic uncertainties; statistical errors dominate
- Our result is consistent with the other experiments
- We are looking forward to the analysis of the data collected with ATLAS in 2012
- There is a lot of space for improvement

Backup slides

Fits in other q^2 bins

2D plot



Theoretical distributions

$$\begin{aligned} \frac{8\pi}{3} \frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_K d\phi} &= (J_{1s} + J_{2s} \cos 2\theta_\ell + J_{6s} \cos \theta_\ell) \sin^2\theta_K \\ &+ (J_{1c} + J_{2c} \cos 2\theta_\ell + J_{6c} \cos \theta_\ell) \cos^2\theta_K \\ &+ (J_3 \cos 2\phi + J_9 \sin 2\phi) \sin^2\theta_K \sin^2\theta_\ell \\ &+ (J_4 \cos \phi + J_8 \sin \phi) \sin 2\theta_K \sin 2\theta_\ell \\ &+ (J_5 \cos \phi + J_7 \sin \phi) \sin 2\theta_K \sin \theta_\ell \end{aligned}$$

3D →

$$\begin{aligned} 4m_\mu^2 \leq q^2 \leq (m_{B_d^0} - m_{K^{*0}})^2, \quad -1 \leq \cos\theta_L \leq 1, \\ -1 \leq \cos\theta_K \leq 1, \quad 0 \leq \phi \leq 2\pi \end{aligned}$$

$$\begin{aligned} \frac{1}{\langle\Gamma\rangle} \frac{d^2\langle\Gamma\rangle}{d\cos\theta_\ell d\cos\theta_K} &= \frac{9}{32} \left[2\langle F_L \rangle \cos^2\theta_K + (1 - \langle F_L \rangle)(1 - \cos^2\theta_K) \right. \\ &- 2\langle F_L \rangle \cos^2\theta_K (2\cos^2\theta_\ell - 1) \\ &+ (1 - \langle F_L \rangle)(1 - \cos^2\theta_K) \cos^2\theta_\ell \\ &\left. + \frac{8}{3} \langle A_{FB} \rangle \cos\theta_\ell (1 - \cos^2\theta_K) \right] \end{aligned}$$

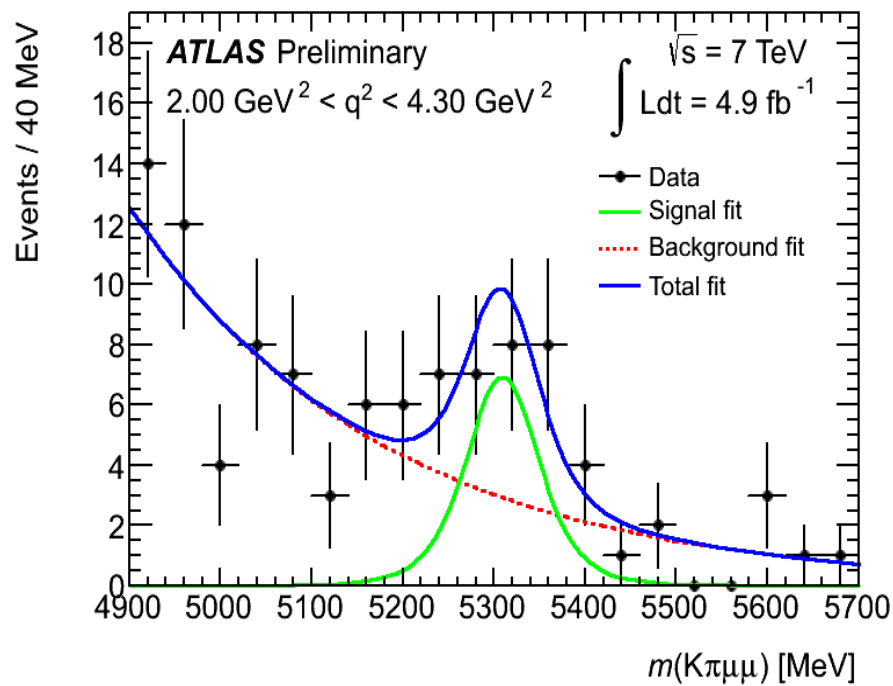
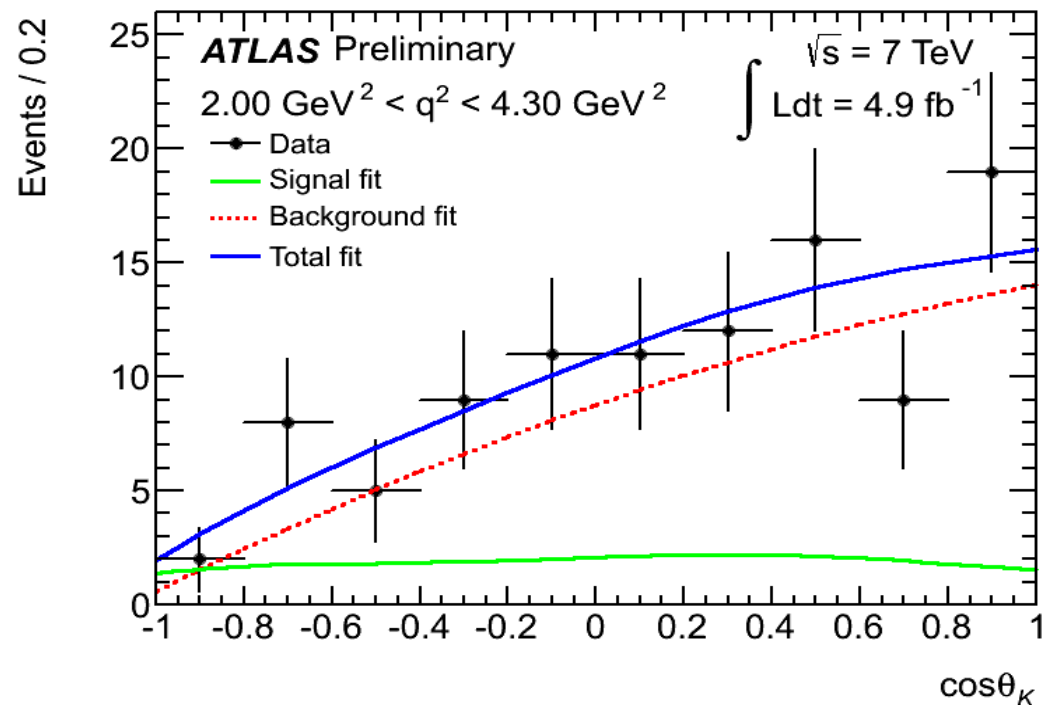
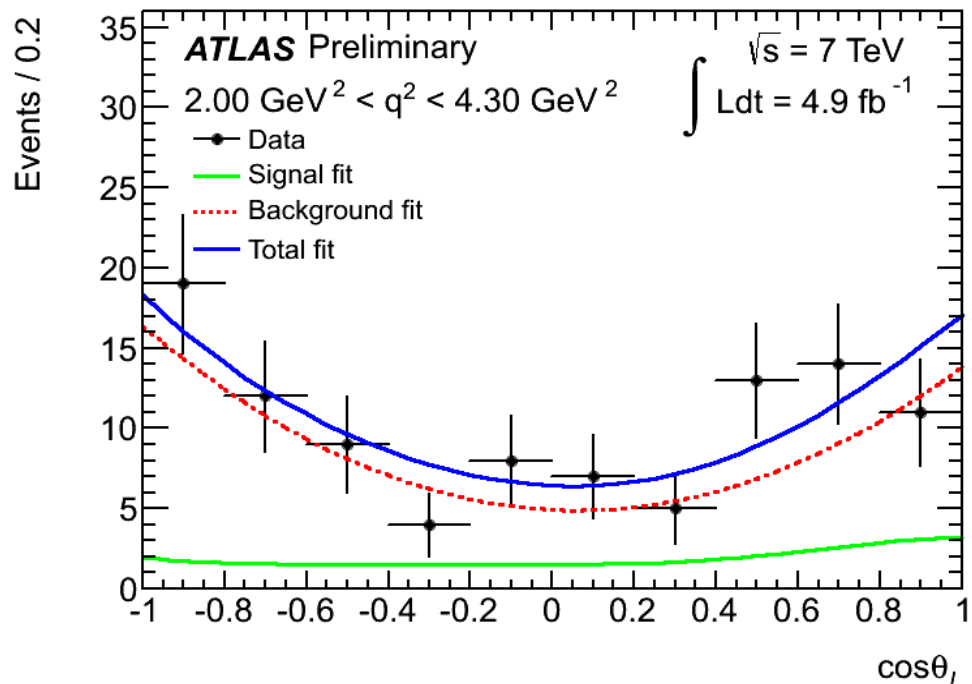
2D →

$$\begin{aligned} \frac{1}{\langle\Gamma\rangle} \frac{d\langle\Gamma\rangle}{d\cos\theta_\ell} &= \frac{1}{\langle\Gamma\rangle} \int_{-1}^1 d\cos\theta_K \frac{d^2\langle\Gamma\rangle}{d\cos\theta_\ell d\cos\theta_K} = \\ &\frac{9}{16} \left[\left(1 - \frac{1}{3}\langle F_L \rangle\right) + \left(\frac{1}{3} - \langle F_L \rangle\right) (2\cos^2\theta_\ell - 1) \right. \\ &\left. + \frac{16}{9} \langle A_{FB} \rangle \cos\theta_\ell \right] \\ &= \frac{3}{4} \langle F_L \rangle (1 - \cos^2\theta_\ell) + \frac{3}{8} (1 - \langle F_L \rangle) (1 + \cos^2\theta_\ell) + \langle A_{FB} \rangle \cos\theta_\ell \end{aligned}$$

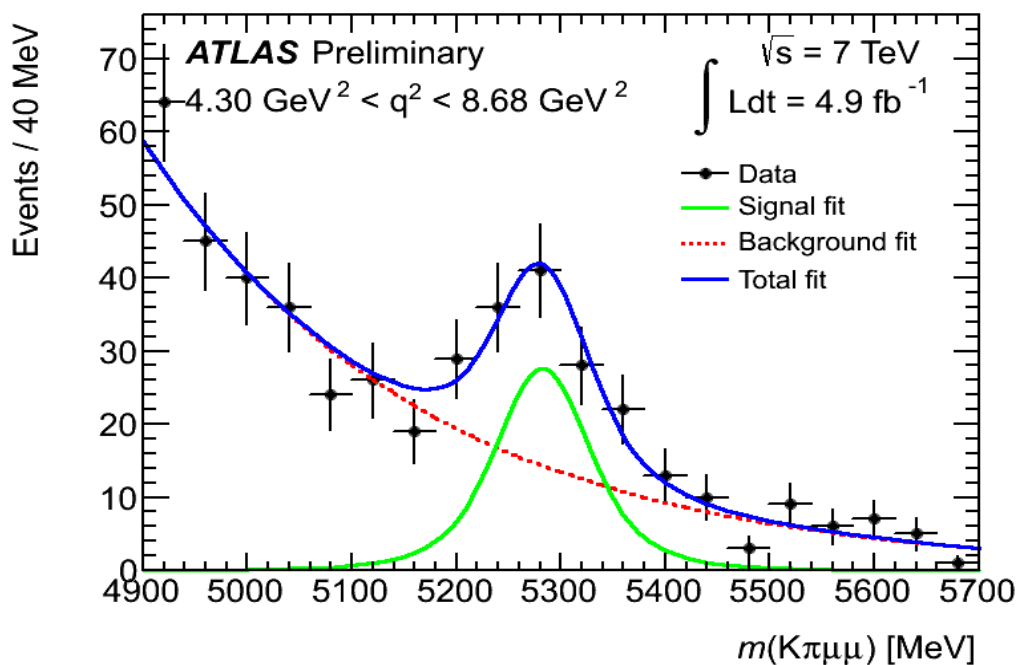
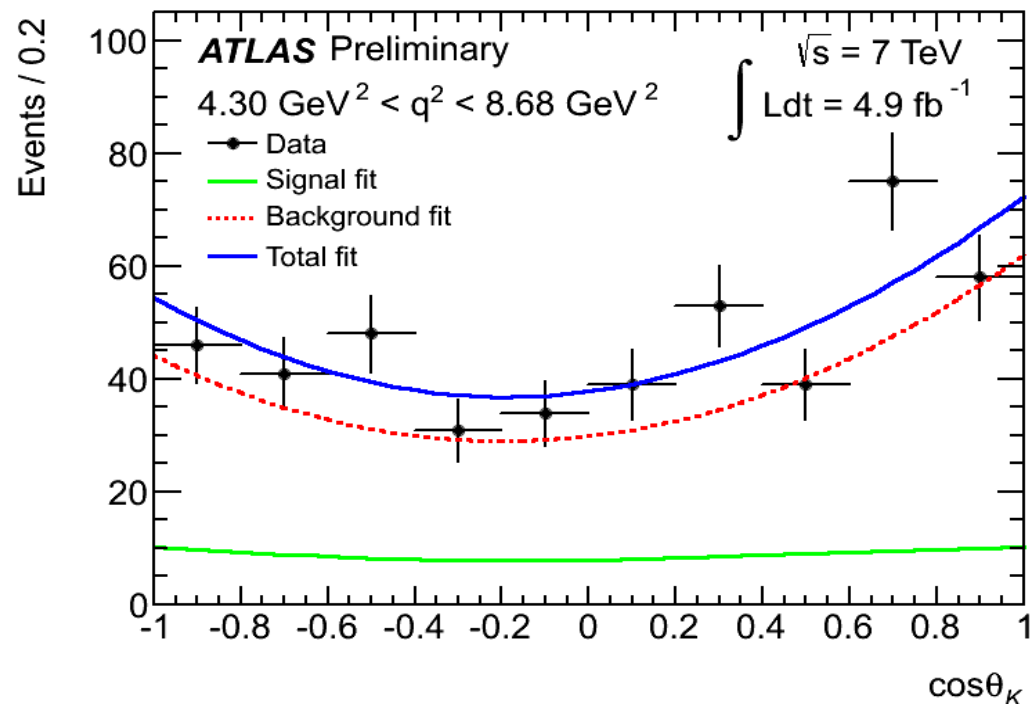
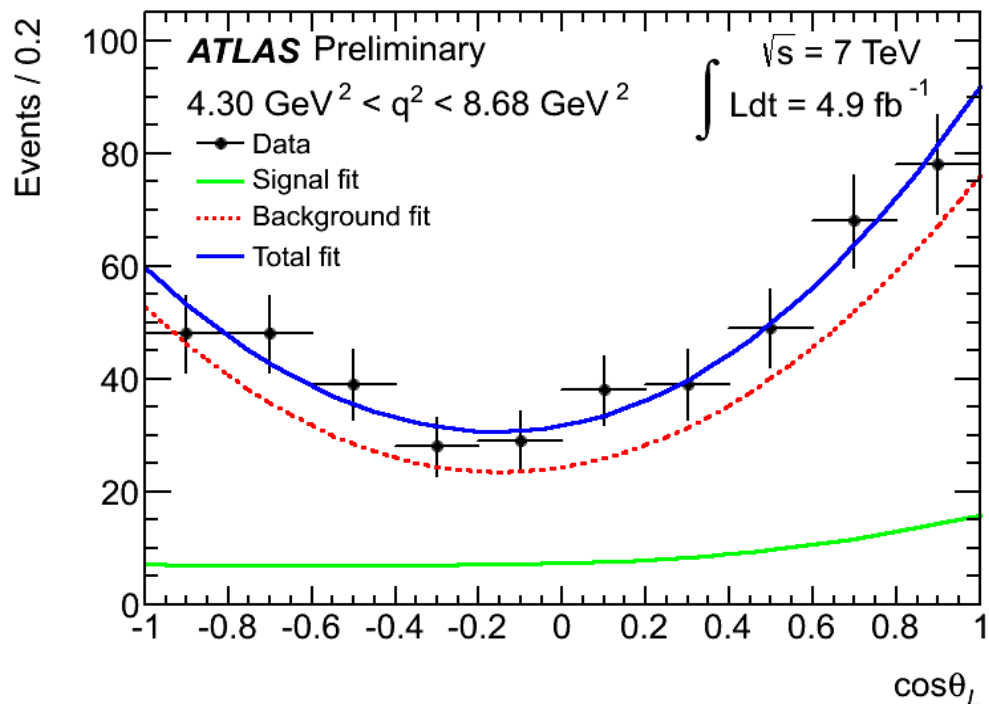
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1D

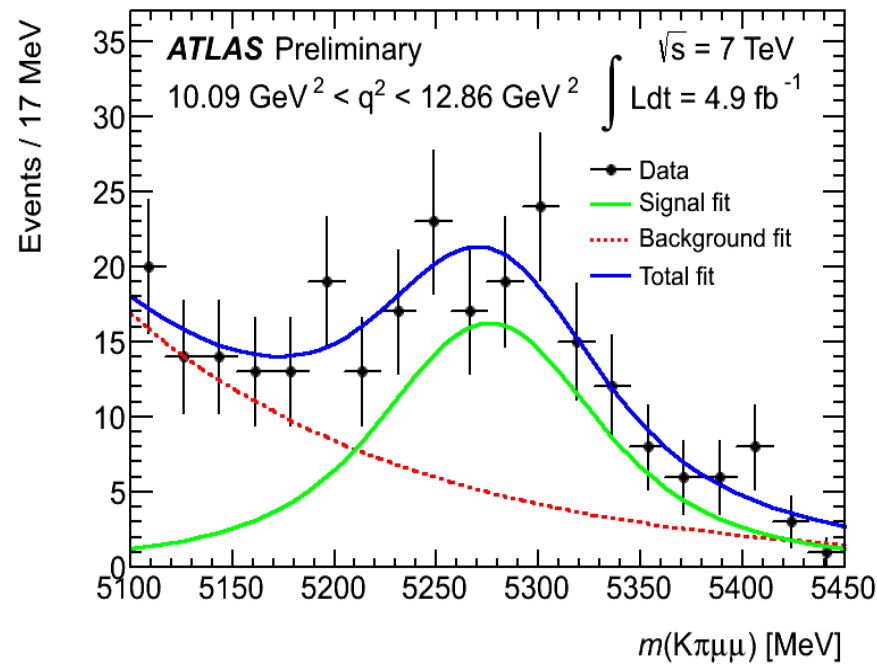
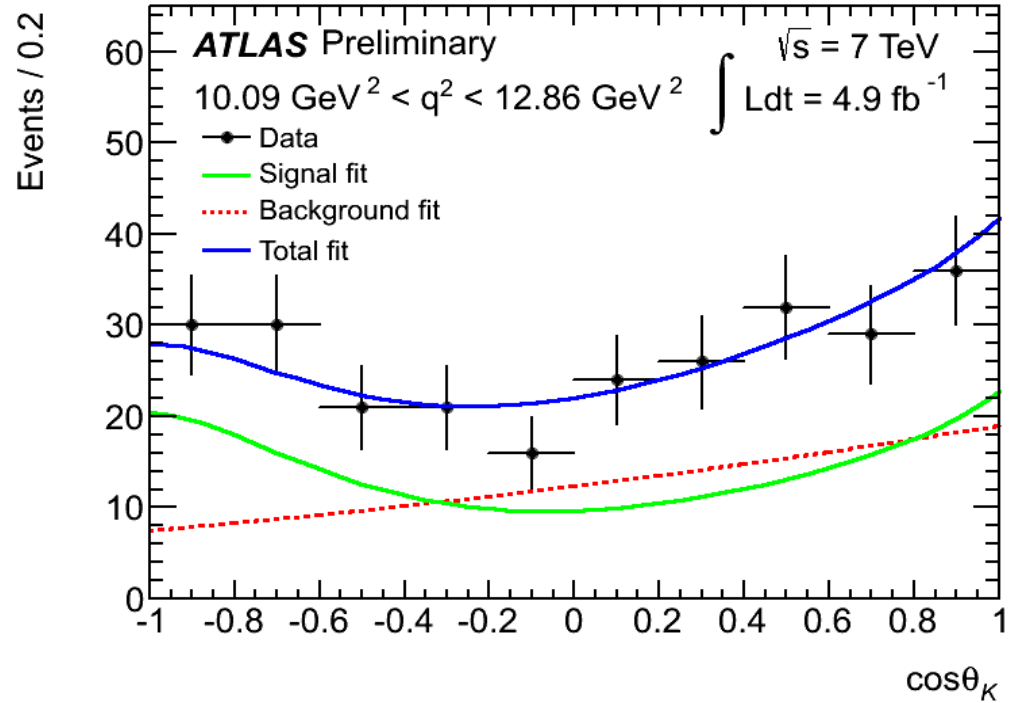
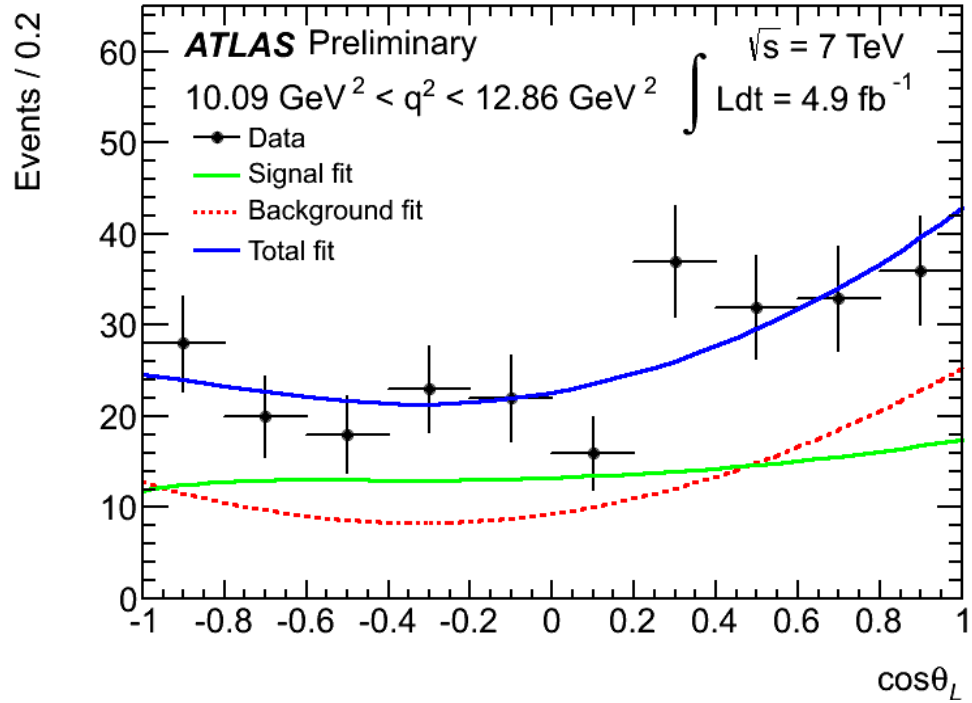
$2.00 < q^2 < 4.30$



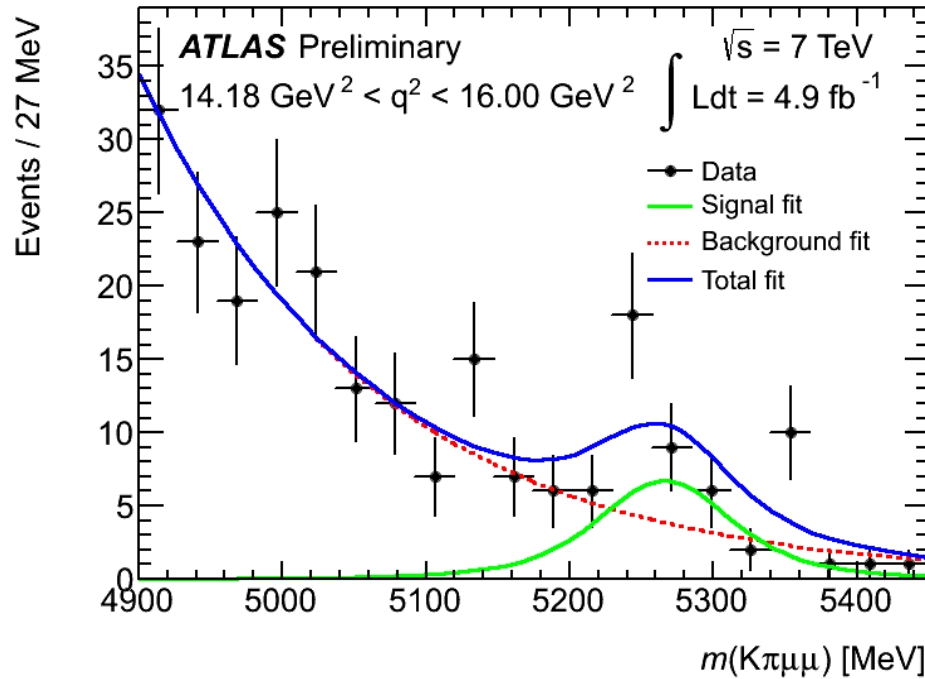
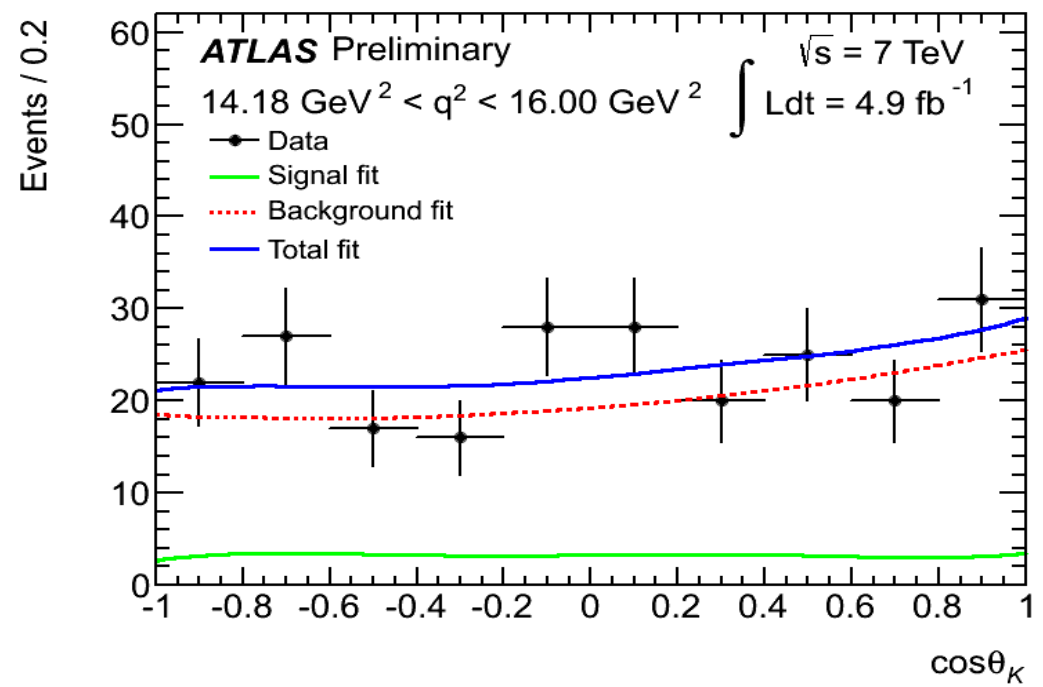
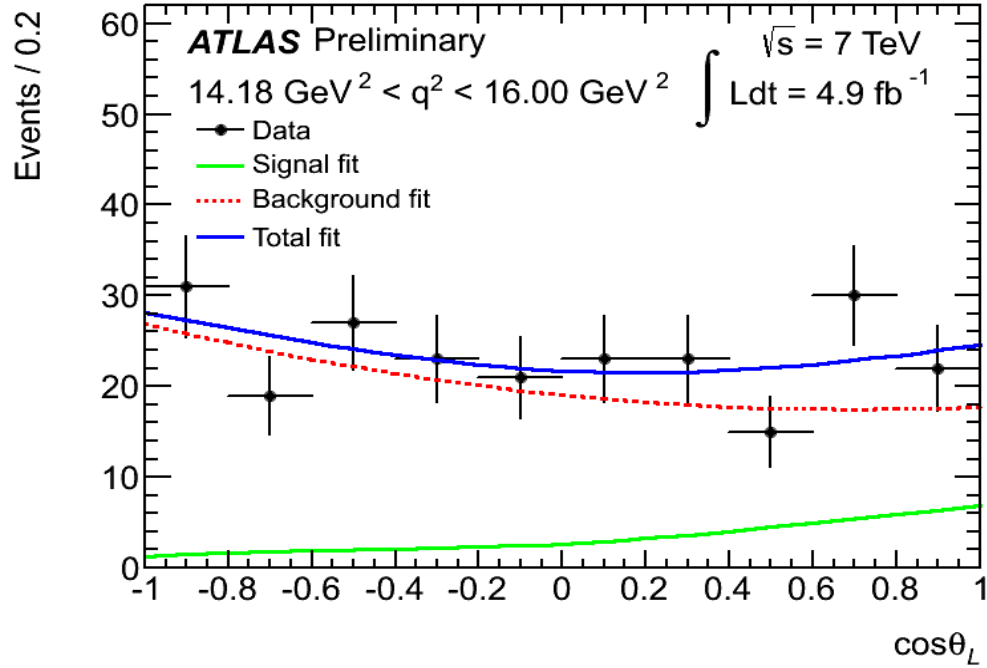
4.30 <math>q^2 < 8.68</math>



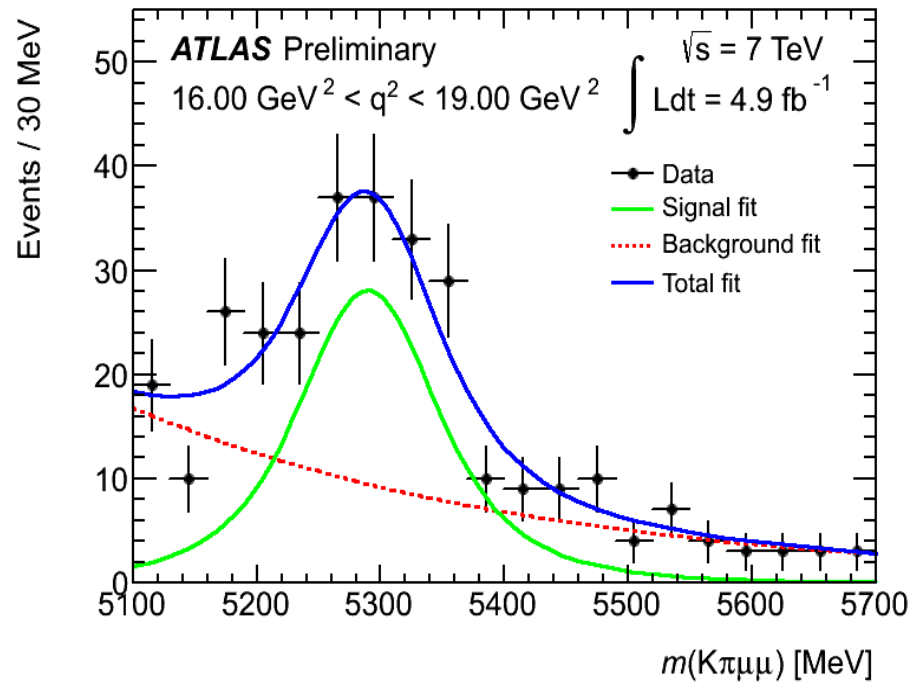
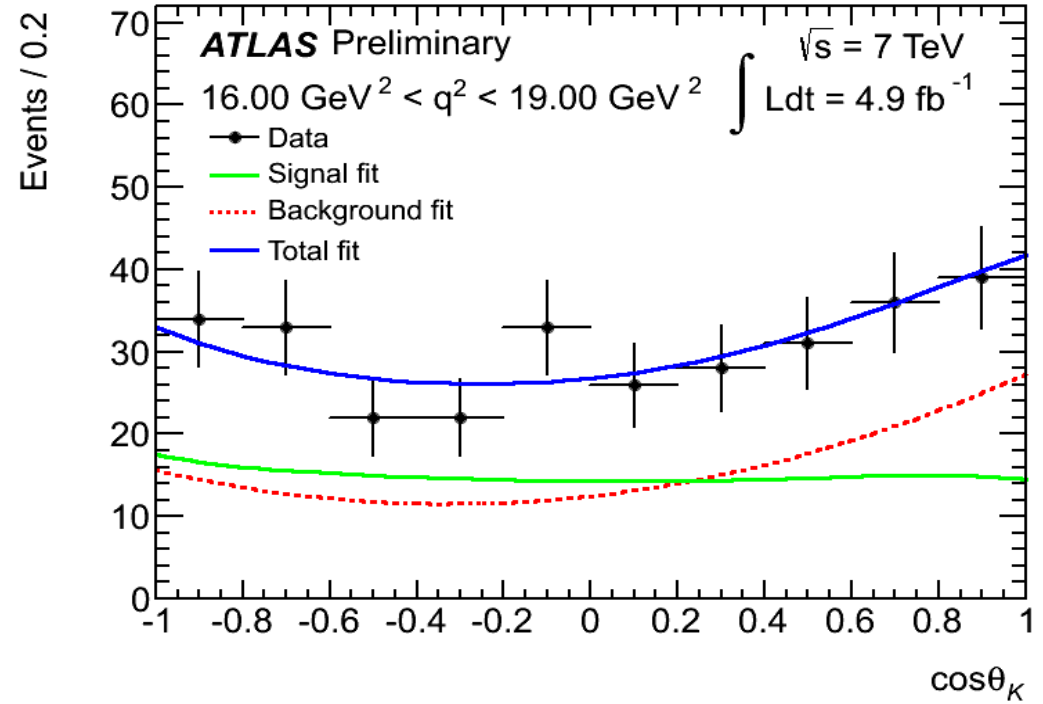
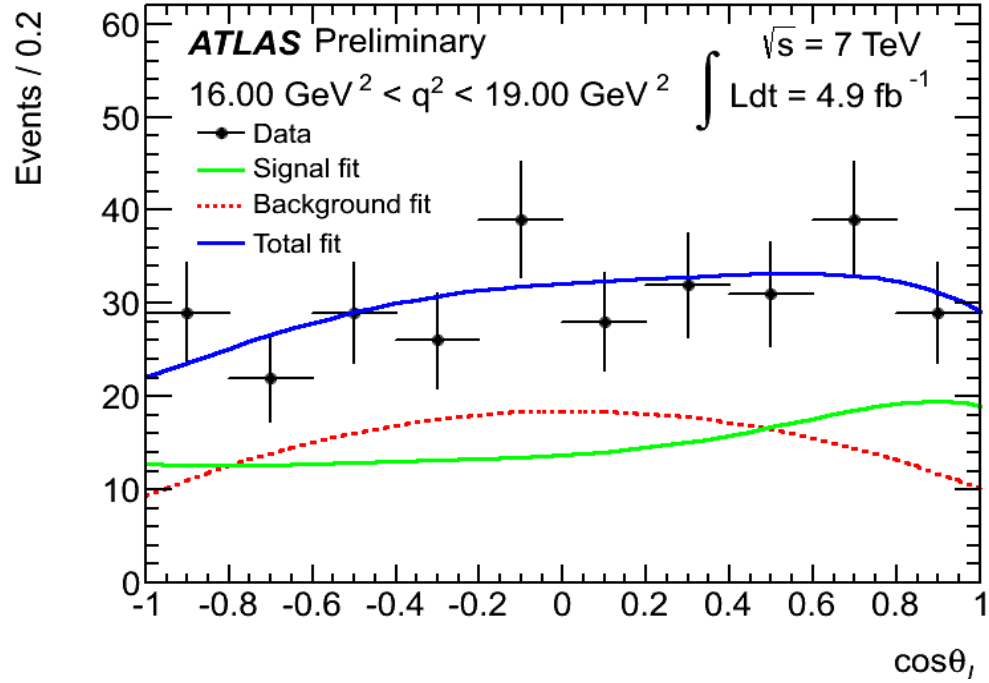
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14.18 < q² < 16.00



16.00 < q² < 19.00



$1.00 < q^2 < 6.00$

