

# Centrality and $p_t$ dependence of $J/\psi$ suppression in $pA$ from induced gluon radiation

François Arleo<sup>1</sup>, Rodion Kolevatov<sup>2</sup>, Stephane Peigné<sup>2</sup>, Maryam Rustamova<sup>2</sup>

<sup>1</sup>LAPTh Annecy & LLR Palaiseau

<sup>2</sup>SUBATECH, Nantes

Workshop on  $pA$  collisions at the LHC  
6–10 May 2013, Trento, Italy

# Outline

## • Motivations

- $J/\psi$  suppression data in p A collisions
- Energy loss parametrization of suppression data

## • Revisiting energy loss

- New scaling properties from medium-induced coherent radiation

## • Phenomenology

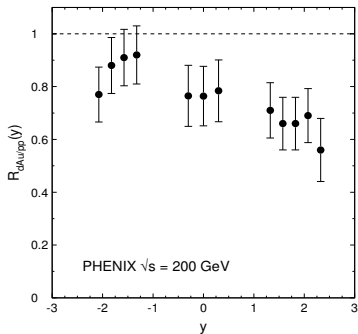
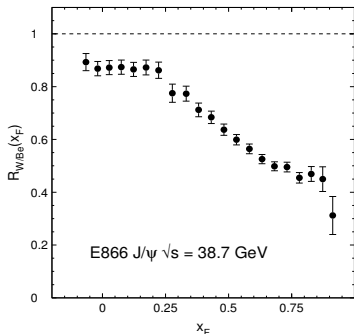
- Model for  $J/\psi$  and  $\Upsilon$  suppression in p A collisions
- Comparison with data and LHC predictions

## References

- F. Arleo, S. Peigné, PRL 109 (2012) 122301 [1204.4609] & JHEP 1303 (2013) 122 [1212.0434]
- F. Arleo, RK, S. Peigné, M. Rostamova, arXiv:1304.0901

$J/\psi$  suppression in  $pA$  collisions at forward rapidities

- $J/\psi$  suppression due to dissociation in QGP suggested as a probe of temperature in  $AA$  [ Matsui, Satz '86 ]
- A strong suppression is seen already in  $pA$  at large  $x_F$  at various  $\sqrt{s}$



- Weaker suppression in the Drell-Yan process

# $J/\psi$ suppression in p A collisions

Many mechanisms suggested as a source of the suppression...

- Nuclear absorption
  - requires unrealistically large cross section
- nPDF effects and saturation
  - constrained by Drell-Yan
- Intrinsic charm
  - assuming a large amount of charm in the proton
- Parton energy loss
  - requires  $\Delta E \propto E$ , ruled out for incoherent IS and FS radiation

... their relative importance is still debated

# $J/\psi$ suppression in p A collisions

Many mechanisms suggested as a source of the suppression...

- Nuclear absorption
  - requires unrealistically large cross section
- nPDF effects and saturation
  - constrained by Drell-Yan
- Intrinsic charm
  - assuming a large amount of charm in the proton
- Parton energy loss
  - requires  $\Delta E \propto E$ , ruled out for incoherent IS and FS radiation

... their relative importance is still debated

**This talk:** the  $J/\psi$  suppression from *coherent* parton energy loss

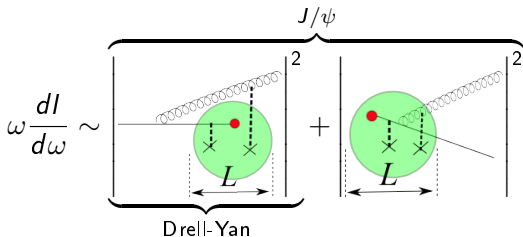
# Gavin–Milana model

Simple model assuming (mean) energy loss via the induced initial and final state radiation

$$\Delta E \propto E L M^{-2}$$

allows for description of both Drell-Yan and  $J/\psi$  suppression at high  $x_F$

[ Gavin Milana 1992 ]



## Gavin–Milana model

Simple model assuming (mean) energy loss via the induced initial and final state radiation

$$\Delta E \propto E L M^{-2}$$

allows for description of both Drell-Yan and  $J/\psi$  suppression at high  $x_F$

[ Gavin Milana 1992 ]

## Caveats

- Based on ad hoc assumption  $\Delta E \propto E$  for the scaling properties of IS and FS induced radiation
- Failure to describe  $\Upsilon$  suppression
- $\Delta E \propto E$  claimed to be incorrect in the high energy limit due to uncertainty principle

## A bound on energy loss

Purely initial/final state induced radiation comes from short formation times while large formation times cancel out [ Brodsky Hoyer 93 ]

$$t_f \sim \frac{\omega}{k_{\perp}^2} \lesssim L \Rightarrow \Delta E \sim \omega \lesssim k_{\perp}^2 L \sim \hat{q} L^2$$

- Bound independent of the parton energy
- Energy loss cannot be arbitrarily large in a finite medium
- Gavin–Milana model is apparently ruled out





## A bound on energy loss

Purely **initial/final state** induced radiation comes from **short formation times** while **large formation times cancel out** [ Brodsky Hoyer 93 ]

$$t_f \sim \frac{\omega}{k_{\perp}^2} \lesssim L \quad \Rightarrow \quad \Delta E \sim \omega \lesssim k_{\perp}^2 L \sim \hat{q} L^2$$

- Bound independent of the parton energy
- Energy loss cannot be arbitrarily large in a finite medium
- Gavin–Milana model is apparently ruled out

The bound applies to:

- Hadron production in nuclear DIS and Drell-Yan in p A collisions
- Jets and hadrons produced in hadronic collisions at large angle

## A bound on energy loss

Purely **initial/final state** induced radiation comes from **short formation times** while **large formation times cancel out** [ Brodsky Hoyer 93 ]

$$t_f \sim \frac{\omega}{k_{\perp}^2} \lesssim L \quad \Rightarrow \quad \Delta E \sim \omega \lesssim k_{\perp}^2 L \sim \hat{q} L^2$$

- Bound independent of the parton energy
- Energy loss cannot be arbitrarily large in a finite medium
- Gavin–Milana model is apparently ruled out

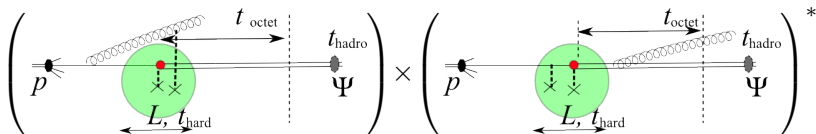
### However

- In certain situations induced radiation has different scaling properties [ Arleo Peigné Sami 10 ]

## Revisiting energy loss scaling properties

Induced gluon radiation dominated by **large formation times**

$$\max(L, t_{\text{hard}}) \ll t_f \sim \frac{\omega}{k_{\perp}^2} \ll t_{\text{octet}} \sim \frac{E}{M} \tau_{\psi} \sim \frac{E}{M k_{\perp}} \Rightarrow \Delta E \propto \frac{\sqrt{\hat{q}L}}{M} E$$



- Requires **small angle scattering** of energetic **color** charge in the medium rest frame
- Comes from **interference** between gluon emissions in the initial and final state

## Revisiting energy loss scaling properties

Induced gluon radiation dominated by **large formation times**

$$\max(L, t_{\text{hard}}) \ll t_f \sim \frac{\omega}{k_{\perp}^2} \ll t_{\text{octet}} \sim \frac{E}{M} \tau_{\psi} \sim \frac{E}{M k_{\perp}} \Rightarrow \Delta E \propto \frac{\sqrt{\hat{q}L}}{M} E$$

Applies to:

- Production of light and open heavy-flavour hadrons at forward rapidities in the medium rest frame (nuclear matter or QGP)
- Production of heavy-quarkonium if color neutralisation occurs on long time-scales  $t_{\text{octet}} \gg t_{\text{hard}}$

## Medium-induced gluon spectrum

Gluon spectrum  $dl/d\omega \sim$  Bethe-Heitler spectrum of massive (color) charge

$$\omega \frac{dl}{d\omega} \Big|_{\text{ind}} = \frac{N_c \alpha_s}{\pi} \left\{ \ln \left( 1 + \frac{E^2 \Delta q_{\perp}^2}{\omega^2 M_{\perp}^2} \right) - \ln \left( 1 + \frac{E^2 \Lambda_{\text{QCD}}^2}{\omega^2 M_{\perp}^2} \right) \right\}$$

$$\Delta E = \int d\omega \omega \frac{dl}{d\omega} \Big|_{\text{ind}} = N_c \alpha_s \frac{\sqrt{\Delta q_{\perp}^2} - \Lambda_{\text{QCD}}}{M_{\perp}} E$$

- $\Delta E \propto E$  neither initial nor final state effect nor 'parton' energy loss: **arises from coherent radiation**
- Physical origin: broad  $t_f$  interval :  $L, t_{\text{hard}} \ll t_f \ll t_{\text{octet}}$  for medium-induced radiation

## Model for heavy-quarkonium suppression

[ Arleo Peigné 1212.0434 ]

$$\frac{1}{A} \frac{d\sigma_{pA}^{\psi}}{dE}(E, \sqrt{s}) = \int_0^{\varepsilon_{\max}} d\varepsilon \mathcal{P}(\varepsilon, E | \Delta q_{\perp}^2) \frac{d\sigma_{pp}^{\psi}}{dE}(E + \varepsilon, \sqrt{s})$$

- pp cross section fitted from experimental data

$$E \frac{d\sigma_{pp}^{\psi}}{dE} = \frac{d\sigma_{pp}^{\psi}}{dy} \propto \left(1 - \frac{2M_{\perp}}{\sqrt{s}} \cosh y\right)^{n(\sqrt{s})}$$

- $\mathcal{P}(\varepsilon)$ : quenching weight, scaling function of  $\hat{w} = \sqrt{\hat{q}L}/M_{\perp} \times E$
- Effective length  $L_{\text{eff}}$  is given by Glauber model,  $L_{pp} = 1.5$  fm

$$\hat{q}(L_{\text{eff}} - L_{pp}) = \left( \langle N_A^{\text{part}} \rangle_{\psi} - 1 \right) \frac{\sigma_{\text{broad}} \mu_{\perp}^2}{\sigma_{\text{inel}}} = \hat{q} \frac{\langle N_A^{\text{part}} \rangle_{\psi} - 1}{\sigma_{\text{inel}} \rho_0}$$

## Transport coefficient

- $\hat{q}$  related to gluon distribution in a target nucleon [ [BDMPS 1997](#) ]

$$\hat{q}(x) = \frac{4\pi^2\alpha_s C_R}{N_c^2 - 1} \rho x G(x, \hat{q}L)$$

- Typical value for  $x$  depends on  $t_{\text{hard}} \sim \frac{1}{M} \frac{E}{M} \sim 1/(m_p x_2)$ :
  - $t_{\text{hard}} \lesssim L \Rightarrow x = x_0 \simeq (m_N L)^{-1}$ ;
  - $t_{\text{hard}} > L \Rightarrow x \simeq x_2$ ;

Using  $xG(x) \sim x^{-0.3}$  for  $x \ll 1$ ,

$$\hat{q}(x) = \hat{q}_0 \left( \frac{10^{-2}}{x} \right)^{0.3} \quad x = \min(x_0, x_2)$$

$\hat{q}_0$  only free parameter of the model

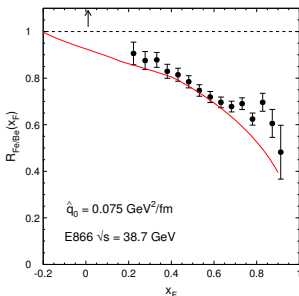
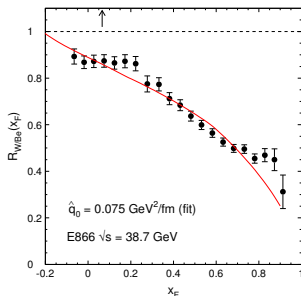
## Procedure

- 1 Fit  $\hat{q}_0$  from  $J/\psi$  E866 data in p W collisions:  
 $\hat{q}_0 = 0.075 \text{ GeV}^2/\text{fm}$
- 2 Predict  $J/\psi$  and  $\Upsilon$  suppression for all nuclei and c.m. energies



## Procedure

- 1 Fit  $\hat{q}_0$  from  $J/\psi$  E866 data in p W collisions:  
 $\hat{q}_0 = 0.075 \text{ GeV}^2/\text{fm}$
- 2 Predict  $J/\psi$  and  $\Upsilon$  suppression for all nuclei and c.m. energies



- Fe/Be ratio well described, supporting the  $L$  dependence of the model

## Extrapolating to other energies

Two competing mechanisms might alter heavy-quarkonium suppression

- Nuclear absorption if hadron formation occurs inside the medium

$$t_{\text{form}} = \gamma \tau_{\text{form}} \lesssim L$$

- Low  $\sqrt{s}$  and/or negative  $x_F$ , indicated later assuming  $\tau_{\text{form}} = 0.3$  fm

## Extrapolating to other energies

Two competing mechanisms might alter heavy-quarkonium suppression

- **Nuclear absorption** if hadron formation occurs inside the medium

$$t_{\text{form}} = \gamma \tau_{\text{form}} \lesssim L$$

- Low  $\sqrt{s}$  and/or negative  $x_F$ , indicated later assuming  $\tau_{\text{form}} = 0.3$  fm
- **nPDF/saturation effects** when  $Q_s^2 \sim m_c^2$

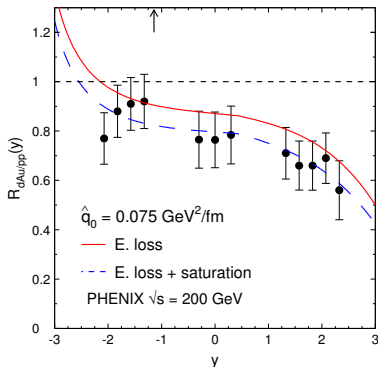
$$R_{\text{pA}} = R_{\text{pA}}^{\text{E.loss}}(\hat{q}) \times \mathcal{S}_{\text{A}}^{\text{sat}}(Q_s) / \mathcal{S}_{\text{p}}^{\text{sat}}(Q_s)$$

$\mathcal{S}_{\text{A}}^{\text{sat}}(Q_s)$  taken from CGC calculations [Fujii Gelis Venugopalan 2006]

- No additional parameter:  $Q_s^2(x, L) = \hat{q}(x)L$  [Mueller 1999]
- $Q_s^2(x = 10^{-2}) = 0.11 - 0.14 \text{ GeV}^2$  consistent with fits to DIS data

[Albacete et al AAMQS 2011]

# RHIC predictions



- Good agreement at all rapidity
- Saturation effects improve the agreement, but taken alone reproduce neither shape nor the magnitude of the suppression

## $p_{\perp}$ dependence

Most general case. The  $p_t$  broadening:  $|\Delta\vec{p}_{\perp}| = \hat{q}L_{\text{eff}}$

$$\frac{1}{A} \frac{d\sigma_{pA}^{\psi}}{dE d^2\vec{p}_{\perp}} = \int_{\varepsilon} \int_{\varphi} \mathcal{P}(\varepsilon, E) \frac{d\sigma_{pp}^{\psi}}{dE d^2\vec{p}_{\perp}} (E+\varepsilon, \vec{p}_{\perp} - \Delta\vec{p}_{\perp})$$

- Parametrization consistent with  $pp$  experimental data

$$\frac{d\sigma_{pp}^{\psi}}{dy d^2\vec{p}_{\perp}} \propto \left( \frac{p_0^2}{p_0^2 + p_{\perp}^2} \right)^m \times \left( 1 - \frac{2M_{\perp}}{\sqrt{s}} \cosh y \right)^n \equiv \mathcal{N} \times \mu(p_{\perp}) \times \nu(y, p_{\perp})$$

- For  $\mathcal{P}(\varepsilon, E)$  peaked at small  $\varepsilon$

$$R_{pA}^{\psi}(y, p_{\perp}) \simeq R_{pA}^{\text{loss}}(y, p_{\perp}) \cdot R_{pA}^{\text{broad}}(p_{\perp})$$

## $p_{\perp}$ dependence

Most general case. The  $p_t$  broadening:  $|\Delta\vec{p}_{\perp}| = \hat{q}L_{\text{eff}}$

$$\frac{1}{A} \frac{d\sigma_{\text{pA}}^{\psi}}{dE d^2\vec{p}_{\perp}} = \int_{\varepsilon} \int_{\varphi} \mathcal{P}(\varepsilon, E) \frac{d\sigma_{\text{pp}}^{\psi}}{dE d^2\vec{p}_{\perp}} (E+\varepsilon, \vec{p}_{\perp} - \Delta\vec{p}_{\perp})$$

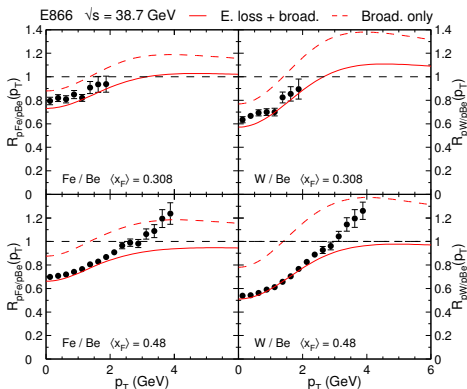
$$R_{\text{pA}}^{\psi}(y, p_{\perp}) \simeq R_{\text{pA}}^{\text{loss}}(y, p_{\perp}) \cdot R_{\text{pA}}^{\text{broad}}(y, p_{\perp})$$

- Overall depletion due to **parton energy loss**
- Possible Cronin peak due to **momentum broadening**

$$R_{\text{pA}}^{\text{broad}}(y, p_{\perp}) \equiv \int_{\varphi} \frac{\mu(|\vec{p}_{\perp} - \Delta\vec{p}_{\perp}|)}{\mu(p_{\perp})} \frac{\nu(E, \vec{p}_{\perp} - \Delta\vec{p}_{\perp})}{\nu(E, p_{\perp})};$$

$$R_{\text{pA}}^{\text{loss}}(y, p_{\perp}) \equiv \int_{\varepsilon} \mathcal{P}(\varepsilon, E) \left[ \frac{E}{E+\varepsilon} \right] \frac{\nu(E+\varepsilon, p_{\perp})}{\nu(E, p_{\perp})}$$

# E866 $p_t$ dependence



- Good description of  $R_{pA/pB}$  for  $p_t \lesssim 3$  GeV
- Possible reasons for discrepancy at  $p_t > 3$  GeV:
  - Model calculations at fixed  $x_F$  rather than averaging
  - $p_t$  dependence from fit to E789  $pp$  data at  $x_F = 0$ .

# Centrality

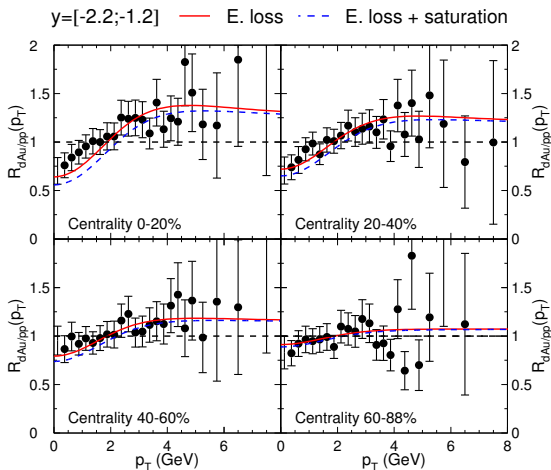
Centrality dependence is given by  $L_{\text{eff}}$

- Experimental situation [ PHENIX 08, ALICE 12 ]
  - Centrality selection via multiplicity in target fragmentation region  $N_A^{\text{ch}}$
  - $N_A^{\text{ch}}$  is strongly correlated with  $N_A^{\text{part}}$
- The model
  - $L_{\text{eff}} = L_{pp} + \frac{\langle N_A^{\text{part}} \rangle_{\psi} - 1}{\sigma_{\text{inel}} \rho_0}$
  - Glauber model estimates of  $\langle N_A^{\text{part}} \rangle_{\psi}$  with constraints on  $N_A^{\text{part}}$ 
    - for  $dAu$  – estimate of  $\langle N_{\text{coll}}^{\text{tagged}N} \rangle_{\psi}$  with constraints on the overall  $N_A^{\text{part}}$

[ Arleo, RK, Peigné, Rustamova 1304.0901 ]

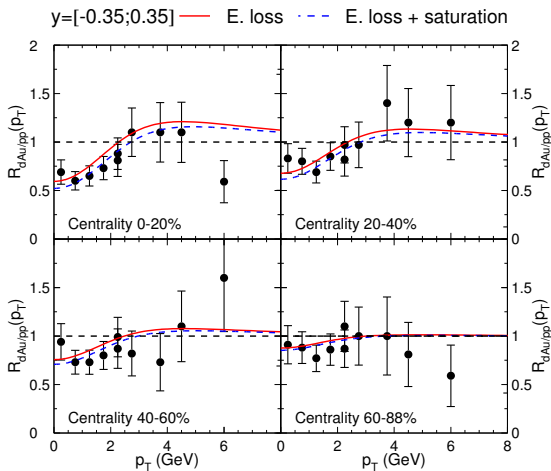


# RHIC predictions



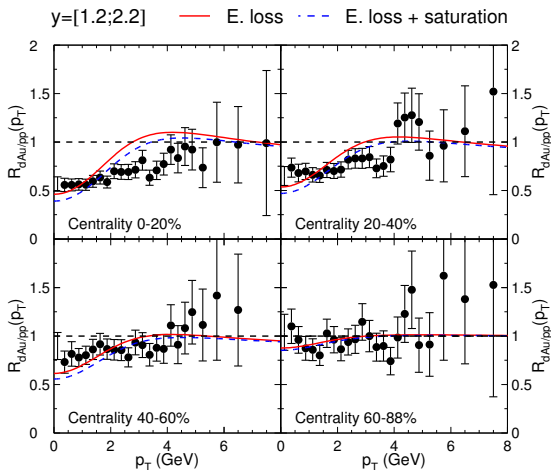
- Good description of  $p_{\perp}$  and centrality dependence at  $y = -1.7$

# RHIC predictions



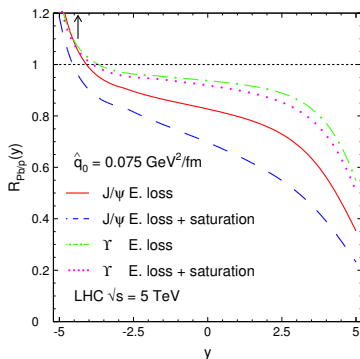
- Good description of  $p_{\perp}$  and centrality dependence at  $y = 0$

# RHIC predictions



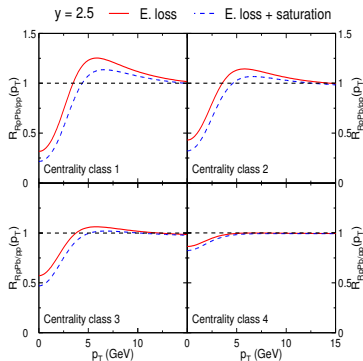
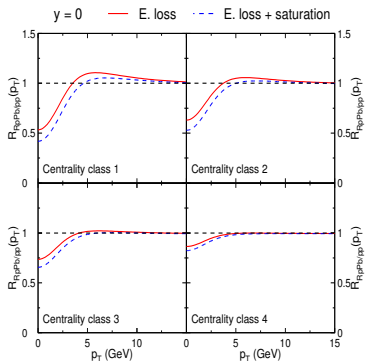
- Good description of  $p_{\perp}$  and centrality dependence at  $y = 1.7$

# LHC predictions



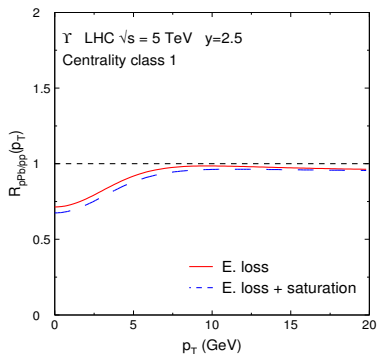
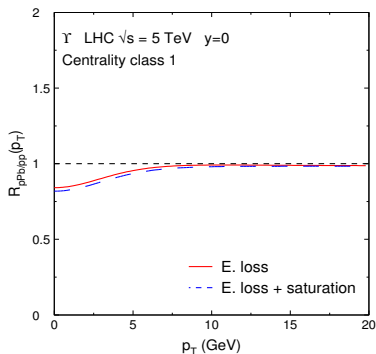
- Moderate effects ( $\sim 20\%$ ) around mid-rapidity, smaller at  $y < 0$
- Large effects above  $y \gtrsim 2 - 3$
- Slightly smaller suppression expected in the  $\Upsilon$  channel

# LHC predictions



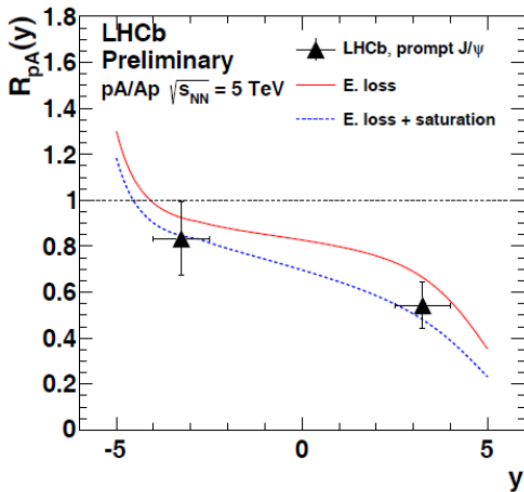
- Suppression expected up to  $p_{\perp} \simeq 3-4$  GeV
- Possible enhancement in most central collisions

# LHC predictions



- Weaker suppression in the  $\Upsilon$  channel, which however extend to slightly larger  $p_{\perp}$

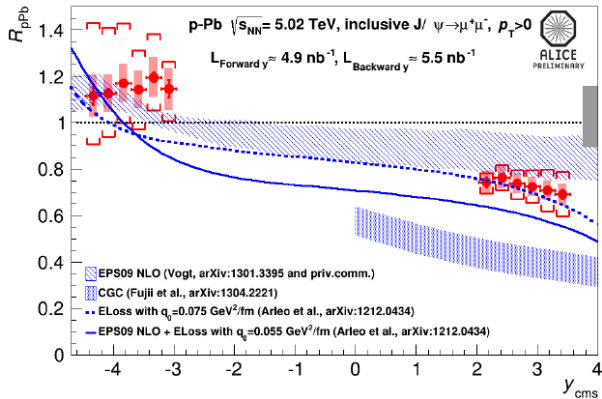
# Comparison with LHCb



Theoretical predictions:  
JHEP 1303 (2013) 122  
[ arXiv:1212.0434 ]

From Fanfan Jing's talk on Monday

# Comparison with ALICE



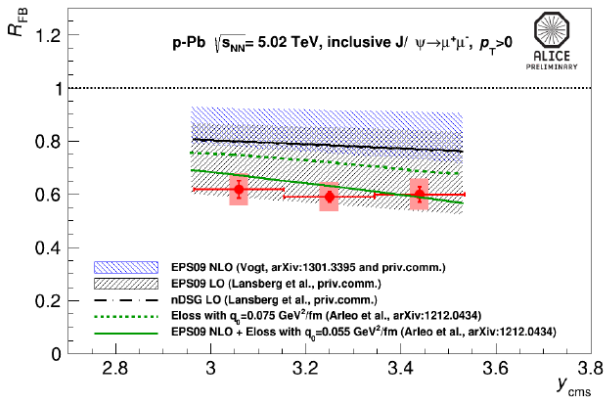
### Uncertainties:

- uncorrelated (box around points)
- partially correlated ([ ])
- 100% correlated (grey box)

From Roberta Arnaldi's talk

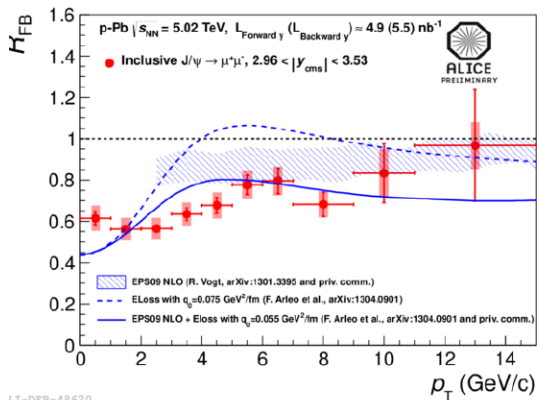


# Comparison with ALICE



From Roberta Arnaldi's talk

# Comparison with ALICE



➔ The  $R_{FB}$  ratio shows a  $p_T$  dependence with a stronger suppression at low  $p_T$

➔ theoretical predictions including energy loss show strong nuclear effects at low  $p_T$ , in fair agreement with the data

LI-DER-48620

From Roberta Arnaldi's talk

## Summary

- Energy loss  $\Delta E \propto E$  due to coherent radiation
  - Neither initial nor final state effect
  - Parametric dependence of  $dI/d\omega$  and  $\Delta E$  predicted
- Heavy-quarkonium suppression predicted for wide range of  $\sqrt{s}$ 
  - Good agreement with all existing data vs.  $x_F(y)$  and  $p_\perp$
  - Natural explanation for the large  $x_F$   $J/\psi$  suppression
  - Model supplemented consistently by saturation effects
  - Supports the assumption of long-lived color octet  $Q\bar{Q}$  pairs
  - Fair agreement with the LHC  $p\text{Pb}$  data on  $J/\psi$

## Backup – Quenching weight

- Poisson approximation assuming **independent** emission can be used for radiation with  $t_f \lesssim L$  [BDMS 2001]

$$\mathcal{P}(\epsilon) \propto \sum_{n=0}^{\infty} \frac{1}{n!} \left[ \prod_{i=1}^n \int d\omega_i \frac{dI(\omega_i)}{d\omega} \right] \delta \left( \epsilon - \sum_{i=1}^n \omega_i \right)$$

- $\Delta E \propto E$  comes from radiation with  $t_f(\omega_i) \sim \omega_i / \Delta q_{\perp}^2 \gg L$

For  $t_f(\omega_i) \sim t_f(\omega_j) \gg L \Rightarrow$  emissions  $i$  and  $j$  are not independent

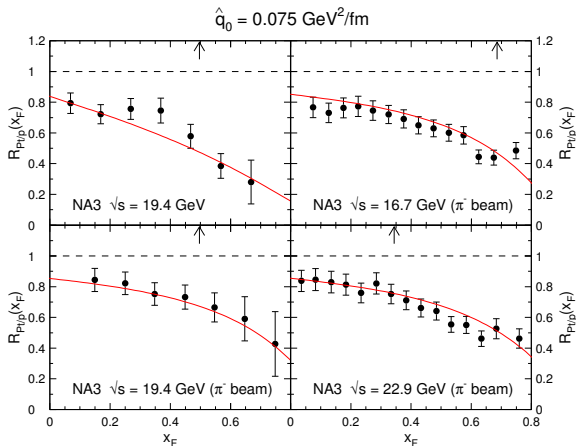
- For self-consistency, constrain  $\omega_1 \ll \omega_2 \ll \dots \ll \omega_n$

$$P(\epsilon) \simeq \frac{dI(\epsilon)}{d\omega} \exp \left\{ - \int_{\epsilon}^{\infty} d\omega \frac{dI}{d\omega} \right\}$$

## Backup – $L_{\text{eff}}$ vs centrality

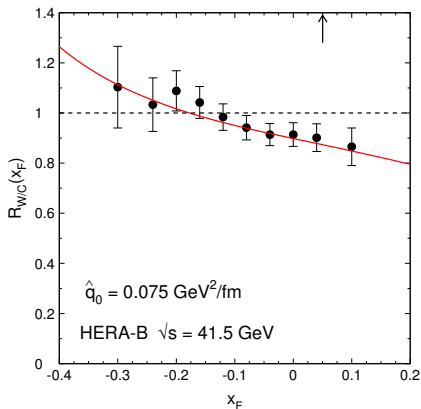
| Glauber, RHIC |                                      |                                       |                       |                 | Glauber, LHC |                                      |                                       |                       |                 |
|---------------|--------------------------------------|---------------------------------------|-----------------------|-----------------|--------------|--------------------------------------|---------------------------------------|-----------------------|-----------------|
| class         | $N_p^{\text{min}}; N_p^{\text{max}}$ | $\frac{P(\text{class})}{P(N \geq 1)}$ | $\langle N_c \rangle$ | $L_{\text{Au}}$ | class        | $N_p^{\text{min}}; N_p^{\text{max}}$ | $\frac{P(\text{class})}{P(N \geq 1)}$ | $\langle N_c \rangle$ | $L_{\text{Pb}}$ |
| A             | 11; 197                              | 0.28                                  | 15.9                  | 12.87           | 1            | 12; 208                              | 0.246                                 | 14.8                  | 13.46           |
| B             | 8; 12                                | 0.24                                  | 10.9                  | 9.62            | 2            | 9; 12                                | 0.215                                 | 10.5                  | 9.55            |
| C             | 5; 8                                 | 0.23                                  | 7.0                   | 7.17            | 3            | 5; 8                                 | 0.215                                 | 6.5                   | 6.29            |
| D             | 2; 4                                 | 0.29                                  | 3.6                   | 3.84            | 4            | 1; 5                                 | 0.428                                 | 2.4                   | 3.39            |

# Backup – SPS



- Agreement when  $x_F > x_F^{\text{min}}$  (and even below)
- Natural explanation from the different suppression in p A vs  $\pi$  A

## Backup – HERA-B



- Also good agreement in the nuclear fragmentation region ( $x_F < 0$ )
- Enhancement predicted at very negative  $x_F$