

1 or 2?



COMPOSITE 2 HIGGS DOUBLET MODELS

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S U M M A R Y

WHY (NOT) 2HDM?

3 MAIN ISSUES

(COMPOSITE 1HDM)

COMPOSITE 2HDM

2 CASE STUDIES

SUMMARY TABLE

E. BERTUZZO, T. S. RAY, H. DE SANDES, CAS

WHY 2HDM ?

(“ELUSIVE”) SUSY

2 HD's but MUCH MORE!!
Here: only non-susy models

EW-BARYOGENESIS

more phases, more scalars, but
w/ 125GeV Higgs, looks marginal

FLAVOUR MODELS

2 vev's: $\tan\beta = v_I / v_{II}$ can help in
accounting for m_t / m_b ratio...

RARE DECAYS

strongly constrain 2HDM, not
quite the reverse (by now)

IMO: no really sound reason!

WHY NOT 2HDM ?

+parameters...

+constraints...

+ symmetries (discrete,...) !

$\Delta T = 0$

tree level anomalous T-parameter
in composite/effective models

solution: custodial symmetry

FCNC

at tree-level from two Higgs exchange

solution: Weinberg-Glashow

$Zb\bar{b}$ coupling

corrections from compositeness

solution: custodial symmetry for bL

T - PARAMETER

COUPLINGS OF HIGGS(ES) TO GAUGE BOSONS

$$\mathcal{L} = D_\mu \phi_i^\dagger D^\mu \phi^i + \frac{\kappa}{f^2} (\phi_i^\dagger D^\mu \phi^j)^2$$

$O(3)_C$: $\Delta I = 0$ $\Delta I = 2$

$$\rho = 1 \Leftrightarrow \Delta I_C = 0 \Leftrightarrow \text{custodial symmetry}$$

2 Higgses must align in vacuum: $\phi_I \propto \phi_{II}$ (or $\phi_{II}=0$)

PNGB Higgs(es): composite sector must have more symmetry

I both $SU(2)_L$ and $O(3)_C \Rightarrow O(4) = SU(2)_L \times SU(2)_R$

II 2 Higgs vev's must align to preserve $O(3)_C \Rightarrow$
more symmetry: another $SU(2)$, parities

FCNC

COUPLINGS OF HIGGS(ES) TO SM FERMIONS

GLASHOW-WEINBERG PRESCRIPTION

$$Q = -1/3$$

$$Q = 2/3$$

Type I

$$b,s,d \text{ --- } \phi_I \text{ --- } u,d,t \quad \phi_{II}$$

Type II

$$b,s,d \text{ --- } \phi_I \quad u,d,t \text{ --- } \phi_{II}$$

⇒ symmetry to discriminate between ϕ_I and ϕ_{II} , extended to fermions

&

⇒ symmetry might also impose $\langle \phi_{II} \rangle = 0$ and save T, $\rho = 1$

Zb \bar{b}

COUPLING OF Z TO b $_L$

m_t and radiative EWSB
in (CW) $V(\phi)$ suggest
more composite $q_L=(t_L, b_L)$

measured b $_L$ coupling to Z,
close to SM value, suggests
more elementary, SM, b $_L$

custodial symmetry for b $_L$:

$$\mathbf{I}_C = \mathbf{I}_L + \mathbf{I}_R \text{ conserved}$$

$$\& \mathbf{I}_{L3}(b_L) = \mathbf{I}_{R3}(b_L) = -1/2$$

$$\Rightarrow b_L \in (2,2)$$

$$\left. \begin{array}{cc} ++ & +- \\ -+ & -- \end{array} \right\} \begin{array}{l} \leftarrow t_L \\ \leftarrow b_L \end{array}$$

$$O(4) \times U(1)_X$$

QUARK HYPERCHARGE

$$Y = T_R^3 + X$$

$$X(\phi) = 0$$

quark masses $\Rightarrow X(q_L) = X(q_R)$

$X(t)$	$X(b)$	$T_R^3(t_R)$	$T_R^3(b_R)$	$O(4)$!
$2/3$	$-1/3$	0	0	(1,1)	need brane mass
$2/3$	$2/3$	0	-1	(1,3)	$X=2B$

O(5) / O(4)

MINIMAL COMPOSITE 'SM' HIGGS

global $O(5) \rightarrow O(4)$ @ $\Lambda \sim f$

PNGB HIGGS $(\mathbf{2}, \mathbf{2}) \longleftrightarrow O(5)/O(4) = \mathbf{4}$ of $O(4)$ 5d sphere

NON-LINEAR REALIZATION

$$U(\phi^a) = \exp\left(i \sum_a \frac{\phi^a}{f} M_{a5}\right)$$

$$M_{a5} \in O(5)/O(4)$$

$$u = U(\phi^a) u_0$$

$$u_0^T = (00001)$$

$$u^T u = 1$$

$$u^T \partial^\mu u = 0$$

5-vector

5d sphere

$$\mathcal{L} = f^2 \partial_\mu u^T \partial^\mu u$$

σ -model Lagrangian

$O(5) / O(4)$

COUPLINGS TO SM GAUGE BOSONS

$$\mathcal{L} = f^2 D_\mu u^\top D^\mu u$$

non-linear Higgs Lagrangian

$$D_\mu = \partial_\mu - igW_\mu^i T_\mu^i - ig'B_\mu Y$$

$$\rho_{\text{tree}} = 1 \iff \Delta T_{\text{tree}} = 0$$

$$O(4) \rightarrow O(3)_c$$

$O(5) / O(4)$

COUPLINGS TO SM FERMIONS

$$\begin{array}{l} O(5) \\ \text{(vector)} \quad \mathbf{5} = \mathbf{(2,2)} + \mathbf{(1,1)} \\ \text{(symm.)} \quad \mathbf{10} = \mathbf{(2,2)} + \mathbf{(1,3)} + \mathbf{(3,1)} \end{array}$$

$\begin{array}{c} \uparrow \\ \mathbf{t}_L \\ \mathbf{b}_L \end{array}$ $\begin{array}{c} \uparrow \\ \mathbf{t}_R, \mathbf{b}_R \end{array}$

$$Z_{bb_{\text{tree}}} = Z_{bb_{\text{SM}}}$$

2HDM

CANDIDATES

YANG-MILLS QUANTUM

1HDM

$$\frac{O(5)}{O(4)} = \frac{Sp(4)}{Sp(2) \times Sp(2)}$$

2HDM

$$\frac{O(6)}{O(4) \times O(2)}$$

$$\frac{SU(5)}{SU(4) \times U(1)}$$

$$\frac{Sp(6)}{Sp(4) \times Sp(2)}$$

$$\frac{O(9)}{O(8)}$$

2 (2,2)

1 complex

1 complex

2 quaternions

2 real

NB: many extensions with $O(4)$ singlet PNGB = axion-like, disregarded because not easy to make the axion invisible

$O(9) / O(8)$

COUPLINGS TO GAUGE BOSONS

global $O(9) \rightarrow O(8)$ @ $\Lambda \sim f$

PNGB HIGGS $2 \times (\mathbf{2}, \mathbf{2}) \longleftrightarrow O(9)/O(8) = \mathbf{8}_s$ of $O(8) \supset O(4) [\times U(1)]$

$$= (\mathbf{2}, \mathbf{2})_{+1} + (\mathbf{2}, \mathbf{2})_{-1}$$

$\phi_I \quad \phi_{II}$

NON-LINEAR REALIZATION

$$u = U(\phi^a) u_0$$

real 9-vector

$$u_0^T = (0 \dots 01)$$

$$u^T u = 1$$

$$u^T \partial^\mu u = 0$$

9d sphere

$$\mathcal{L} = f^2 D_\mu u^T D^\mu u$$

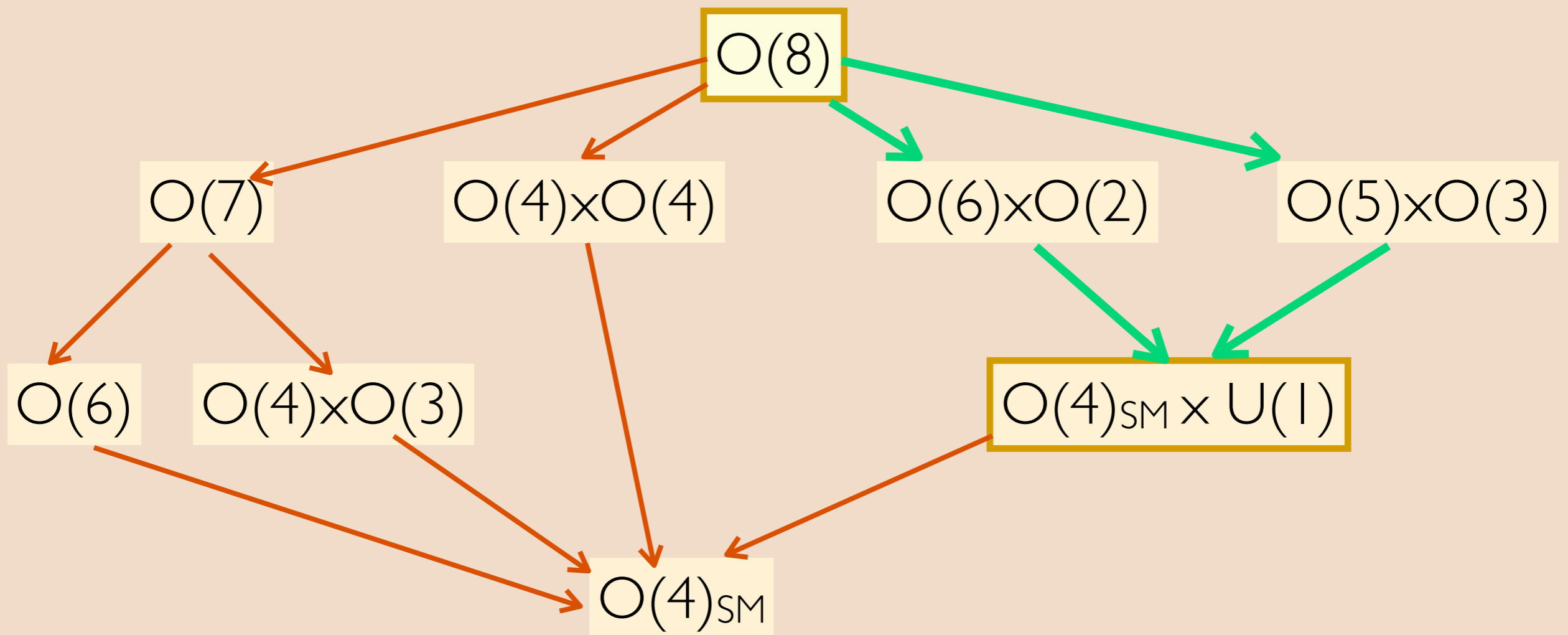
non-linear Higgs Lagrangian

$$\rho_{\text{tree}} = 1 \longleftrightarrow \Delta T_{\text{tree}} = 0$$

$O(9) / O(8)$

EMBEDDING $O(4)_{SM} \subset O(8)$

$$\begin{aligned} O(9)/O(8) &= \mathbf{8}_s \text{ of } O(8) \supset O(4) [xU(1)] \\ &= \underbrace{(2,2)_{+1}}_{\phi_I} + \underbrace{(2,2)_{-1}}_{\phi_{II}} \end{aligned}$$



$O(9) / O(8)$

EMBEDDING SM FERMIONS

$O(9)$	$O(8)$	$O(4) \times U(1)$
9	$\phi_{I,II} \in 8_s$	$(2, 2)_{+1} + (2, 2)_{-1}$
16	$\psi_L \in 8_c$	$(2, 2)_{-1} + (2, 2)_{+1}$
	$\psi_R \in 8_v$	$(1, 3)_0 + (3, 1)_0 + (1, 1)_{-2} + (1, 1)_{+2}$

$O(9) / O(8)$

EMBEDDING SM FERMIONS

$O(9)$	$O(8)$	ϕ_I	ϕ_{II}	$O(4) \times U(1)$
9	$\phi_{I,II} \in 8_s$	$(2, 2)_{+1}$	$(2, 2)_{-1}$	
16	$\psi_L \in 8_c$	$(2, 2)_{-1}$	$(2, 2)_{+1}$	
	$\psi_R \in 8_v$	$(1, 3)_0$	$(3, 1)_{+1} + (1, 1)_{-2} + (1, 1)_{+2}$	

t_L, b_L (pointing to $(1, 3)_0$)
 t_R, b_R (pointing to $(3, 1)_{+1}$)

$U(1) \Rightarrow$ Type I \Rightarrow no FCNC & $b_L \in (2, 2) \Rightarrow Zbb_{tree} = Zbb_{SM}$

SU(5) / SU(4) × U(1)

COUPLINGS TO GAUGE BOSONS

$$\text{HIGGS} = 2 \times (\mathbf{2}, \mathbf{2}) \longleftrightarrow \text{SU}(5)/\text{U}(4) = \underline{\mathbf{4}^\dagger + \mathbf{4}} \text{ of } \text{U}(4) \supset \text{O}(4) [\times \text{U}(1)]$$

$$= (\mathbf{2}, \mathbf{2}) + i(\mathbf{2}, \mathbf{2}) \\ \phi_I + i\phi_{II}$$

NON-LINEAR REALIZATION

$$\mathbf{u} = \text{U}(\phi^a) \mathbf{u}_0$$

complex 5-vector

$$\mathbf{u}_0^T = (00001)$$

$$\mathbf{u}^\dagger \mathbf{u} = 1$$

$$\mathcal{L} = f^2 \text{D}_\mu \mathbf{u}^\dagger \text{D}^\mu \mathbf{u} + f^2 (\mathbf{u}^\dagger \text{D}^\mu \mathbf{u})^2$$

$$(\Delta I = 2)$$

non-linear Higgs
Lagrangian

$$\frac{(\Delta M_Z^2)_{I=2}}{M_Z^2} \leq \mathcal{O}(v^2/f^2)$$



$$\Delta T_{\text{tree}} \neq 0$$

(unnatural)

SU(5) / SU(4) x U(1)

EMBEDDING SM FERMIONS

SU(5)	U(4)	O(4) x U(1)	
	$\phi_I + i\phi_{II} \in 4$	$(2, 2) + i(2, 2)$	t and b couple to two orthogonal combinations of ϕ_I and ϕ_{II} of (Type II)
10	$\psi_L \in 4^*$	$(2, 2) + i(2, 2)$	
	$\psi_R \in 6$	$(1, 3) + (3, 1)$	

$\phi_I + i\phi_{II}$ (pointing to the top-right cell)
 t_L, b_L (pointing to the bottom-left cell)
 t_R, b_R (pointing to the bottom-right cell)

Type II \Rightarrow no FCNC & $b_L \in (2, 2) \Rightarrow Zbb_{\text{tree}} = Zbb_{\text{SM}}$

S U M M A R Y

G/H	T	$O(3)_c$	ψ_L ψ_R	Zbb	FCNC Type	Higgs- gauge unifictn
$O(6)/O(4) \times O(2)$	✗	✗	<u>6</u>	✓	✗	✗
$O(6)/O(4) \times O(2) \times Z_2$	✓	✗	<u>6</u>	✓	I	✗
$SU(5)/SU(4) \times U(1)$	✗	✗	<u>10</u>	✓	II	✓
$Sp(6)/Sp(4) \times Sp(2)$	✓	✓			I	
$O(9)/O(8)$	✓	✓	<u>16</u>	✓	I	✓