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**Flavor-changing Higgs Effects  
in the MSSM and 2HDMs**

# Outline:

- Introductions: Flavor violation in 2HDMs
- Matching on the MSSM on the 2HDM of type III
  - Resummation of chirally enhanced effects
  - 2-loop corrections to Higgs-quark-quark vertices
- Flavor-phenomenology of 2HDMs with generic flavour-structure
  - Constraints from FCNC processes
  - Tauonic B decays
  - Direct CP asymmetry in  $D \rightarrow KK, \pi\pi$
  - LFV processes
- Conclusions

# Introduction

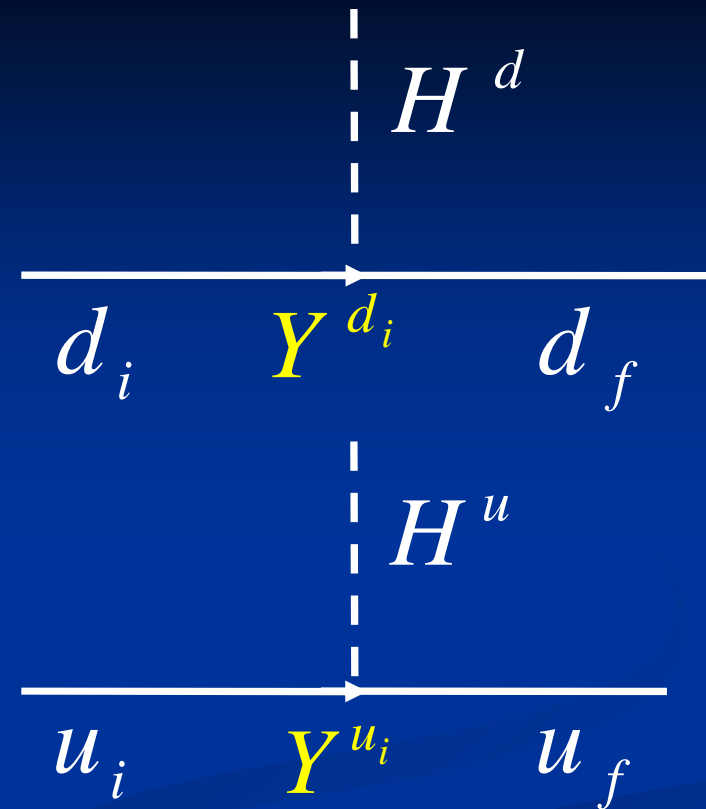
## Flavor-violation in 2HDMs

# 2HDM of type II (MSSM at tree-level)

- One Higgs doublet couples only to down-quarks (and charged leptons), the other Higgs doublet couples only to up-quarks.
- 2 additional free parameters:  $\tan(\beta)=v_u/v_d$  and the heavy Higgs mass

$$m_H \approx m_{A^0} \approx m_{H^\pm} \approx m_{H^0}$$

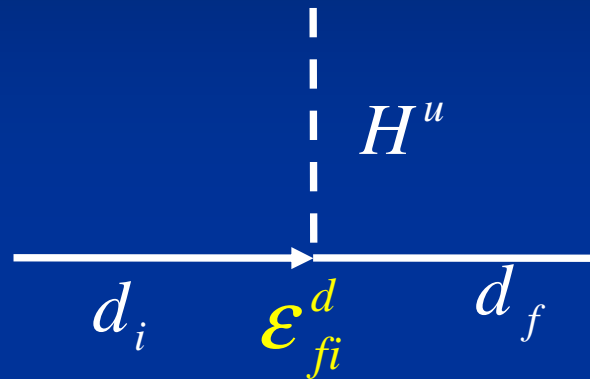
- All flavor-violations is due to the CKM matrix: neutral Higgs-quark couplings are flavor-conserving.



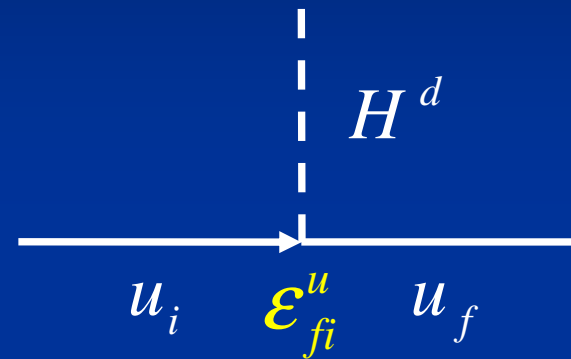
$$m_{q_i} = v_q Y^{q_i}$$

# 2HDM of type III

- Both Higgs doublets couple simultaneously to up and down quarks.



$$m_{ij}^d = v_d Y_{ij}^d + v_u \epsilon_{ij}^d$$



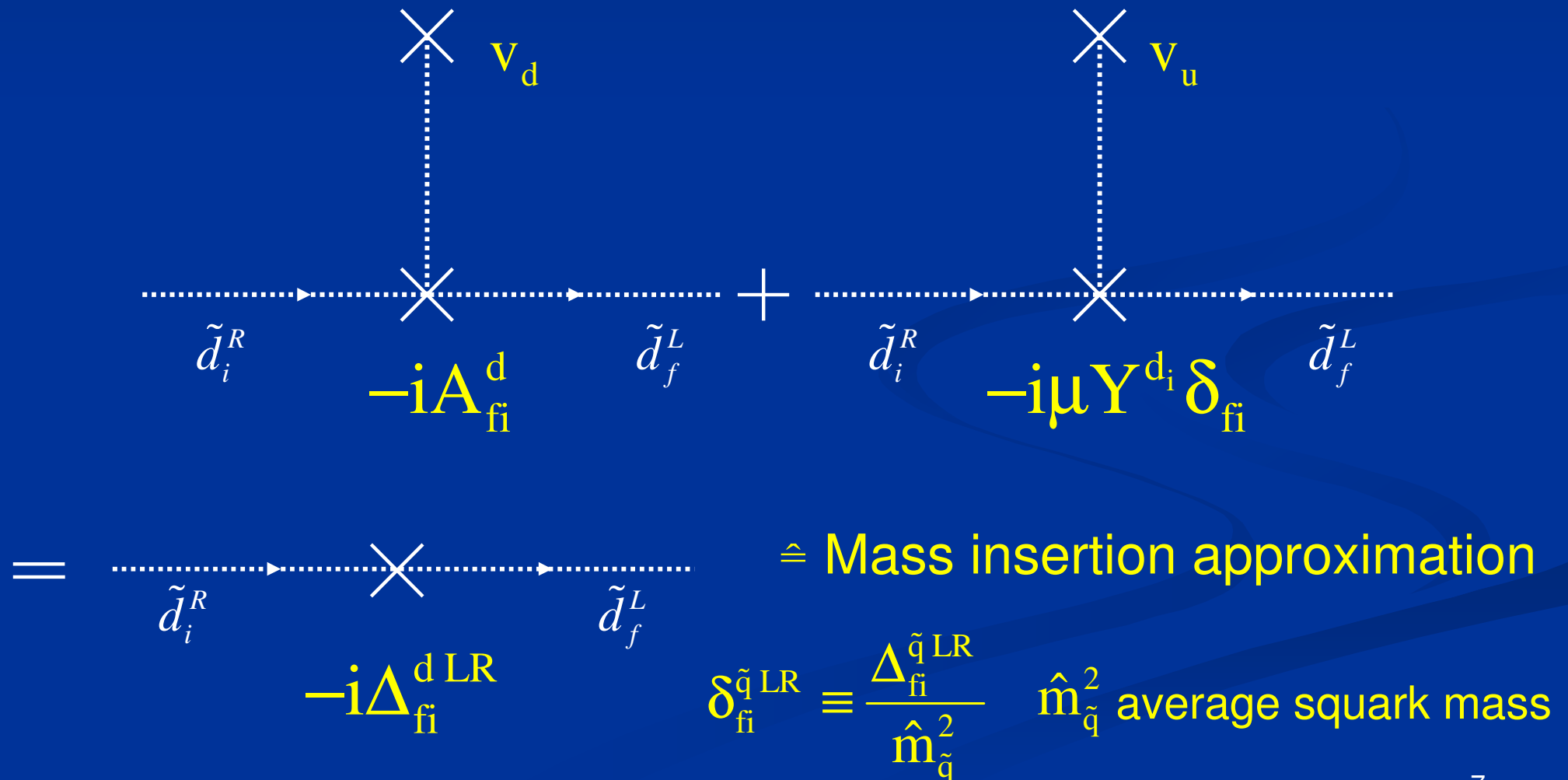
$$m_{ij}^u = v_u Y_{ij}^u + v_d \epsilon_{ij}^u$$

- The parameters  $\epsilon_{ij}^{u,d}$  describe flavor-changing neutral Higgs interactions
- In the MSSM,  $\epsilon_{ij}^{u,d}$  are induced via loops

# Matching of the MSSM on the 2HDM

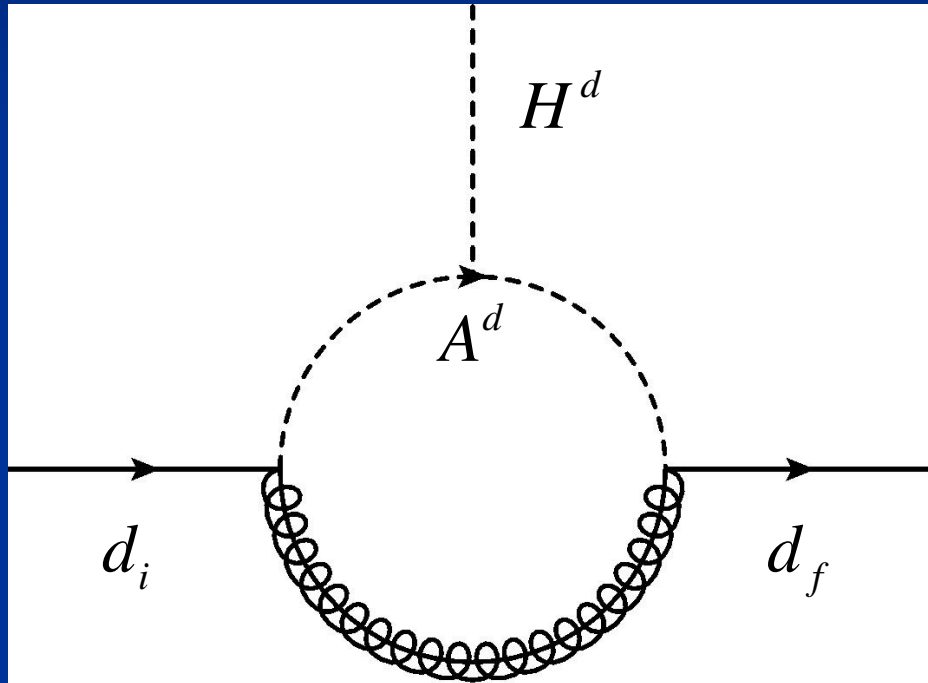
# Squark-Higgs couplings

- The off-diagonal elements  $\Delta_{ij}^{qLR}$  of the squark mass matrices originate from squark-Higgs couplings

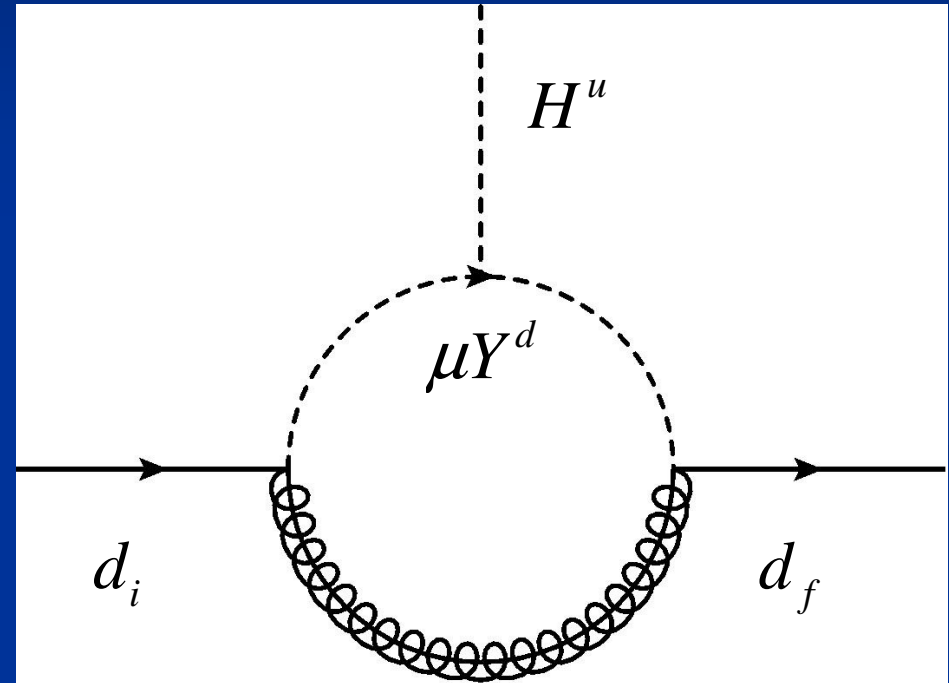


# Loop corrections to Higgs quark couplings

- Before electroweak symmetry breaking



$$\Gamma_{d_f d_i}^{H^d}$$

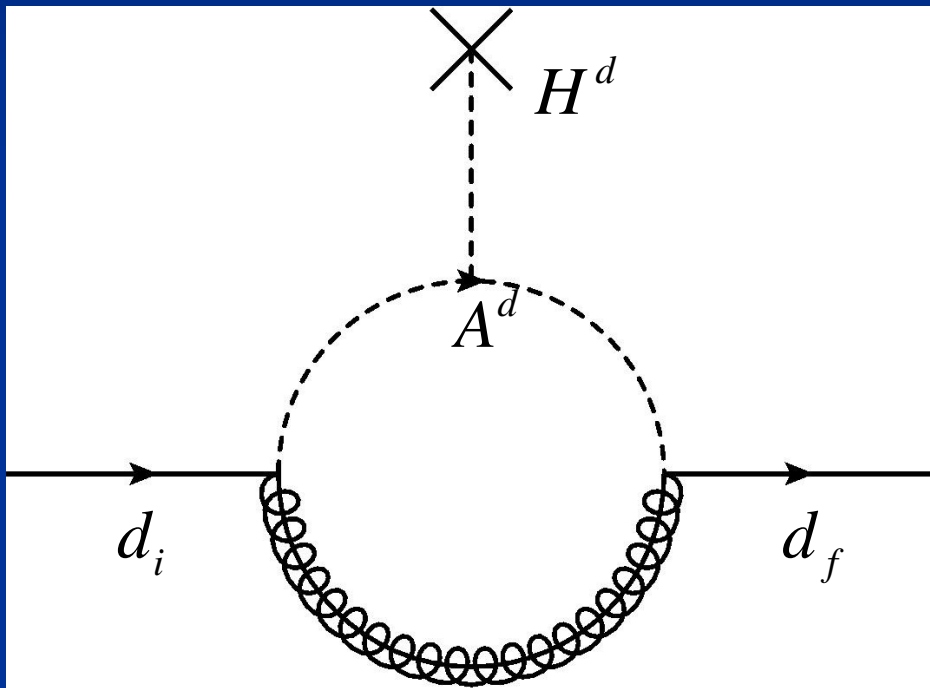


$$\Gamma_{d_f d_i}^{H^u}$$

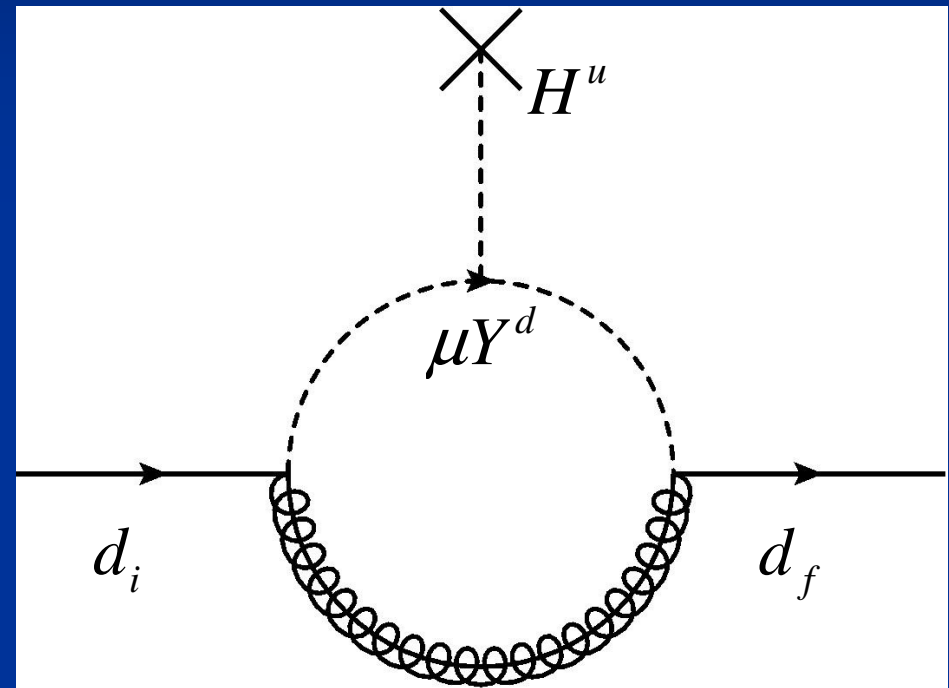


# Loop corrections to Higgs quark couplings

- After electroweak symmetry breaking



$$\sum_{fi A}^{d LR} = v_d \Gamma_{d_f d_i}^{H^d}$$



$$\sum_{fi Y}^{d LR} = v_u \Gamma_{d_f d_i}^{H^u}$$


➔ One-to-one correspondence between Higgs-quark couplings and chirality changing self-energies. (In the decoupling limit)

# Determination of the MSSM Yukawa coupling

- All corrections are finite and are non-decoupling

## Matching condition:

$$\begin{aligned} m_{d_i} &= v_d Y^{d_i} + \sum_{ii}^{d LR} \\ &= v_d Y^{d_i} + \sum_{ii A}^{q LR} + v_d \tan(\beta) Y^{d_i} \epsilon_{d_i} \end{aligned}$$


$$Y^{d_i} = \frac{m_{d_i} - \sum_{ii A}^{q LR}}{v_d (1 + \tan(\beta) \epsilon_i^d)}$$

- $\tan(\beta)$  is automatically resummed to all orders

Carena et al, hep-ph/9912516

# Complete resummation of all chirally enhanced corrections

A.C., L. Hofer and J. Rosiek, 1103.4272

Including:

- Most general MSSM flavor structure
- SQCD and electroweak contributions
- Threshold corrections to the CKM matrix
- Effective Higgs-quark-quark vertices
- Effective quark-squark-gaugino vertices

Using these vertices, all chirally enhanced corrections can be automatically included.

Implemented in `SUSY_FLAVOR 2.0`

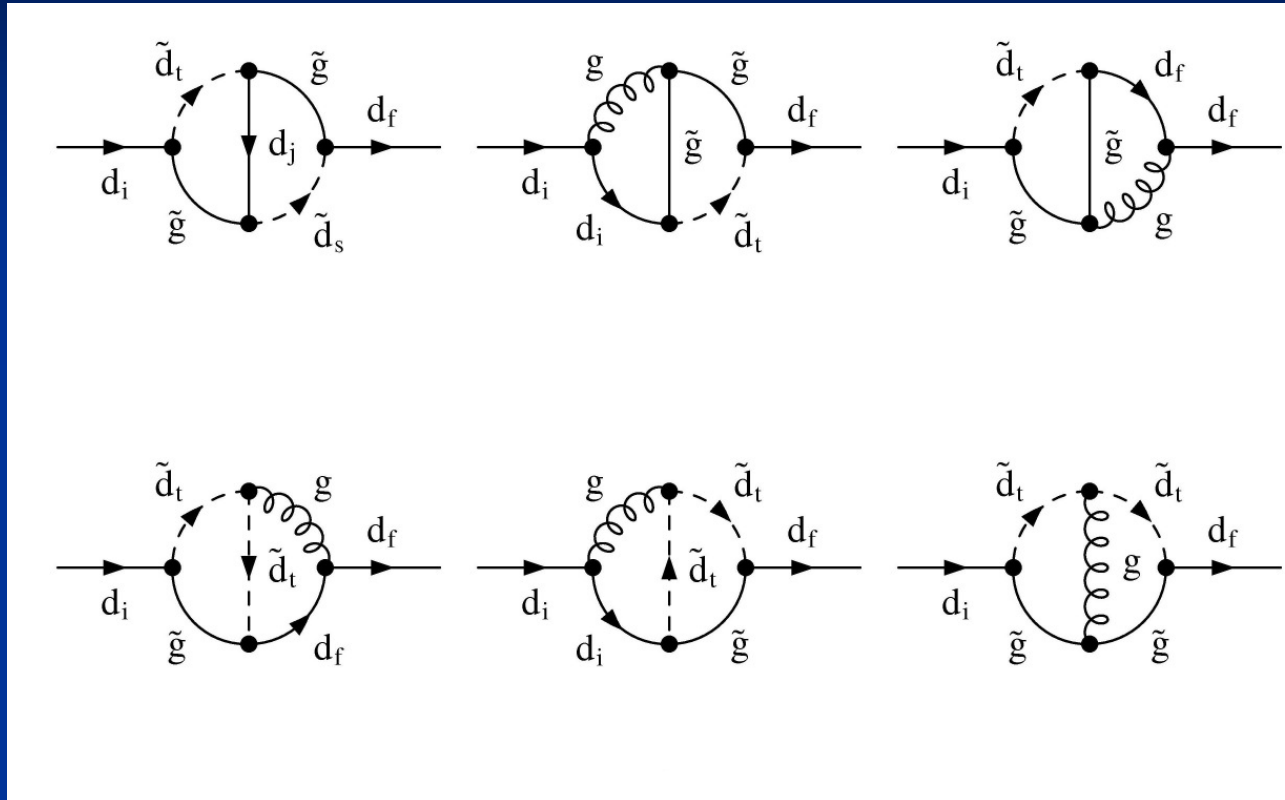
# NLO calculation of the quark self-energies

NLO calculation is important for:

- Computation of effective Higgs-quark vertices.
- Determination of the Yukawa couplings of the MSSM superpotential (needed for the study of Yukawa unification in GUTs).
- NLO calculation of FCNC processes in the MSSM at large  $\tan(\beta)$ .

Reduction of the matching scale dependence

# NLO calculation

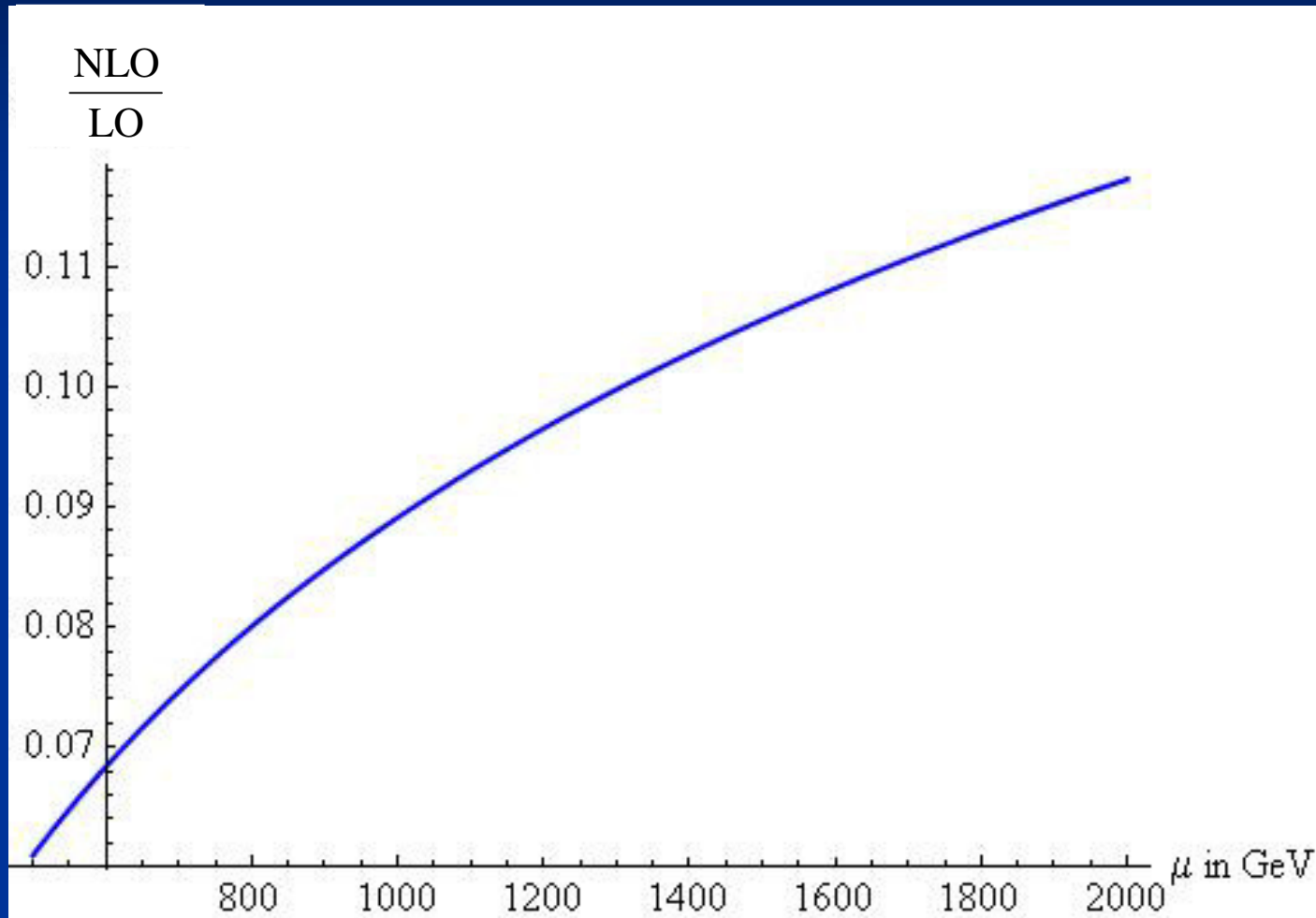


Examples of 2-loop diagrams

- NLO calculation includes analytic results and  $\tan(\beta)$  resummation in the generic MSSM.

$\Delta_b$  at order  $\alpha_s^2$

# NLO results

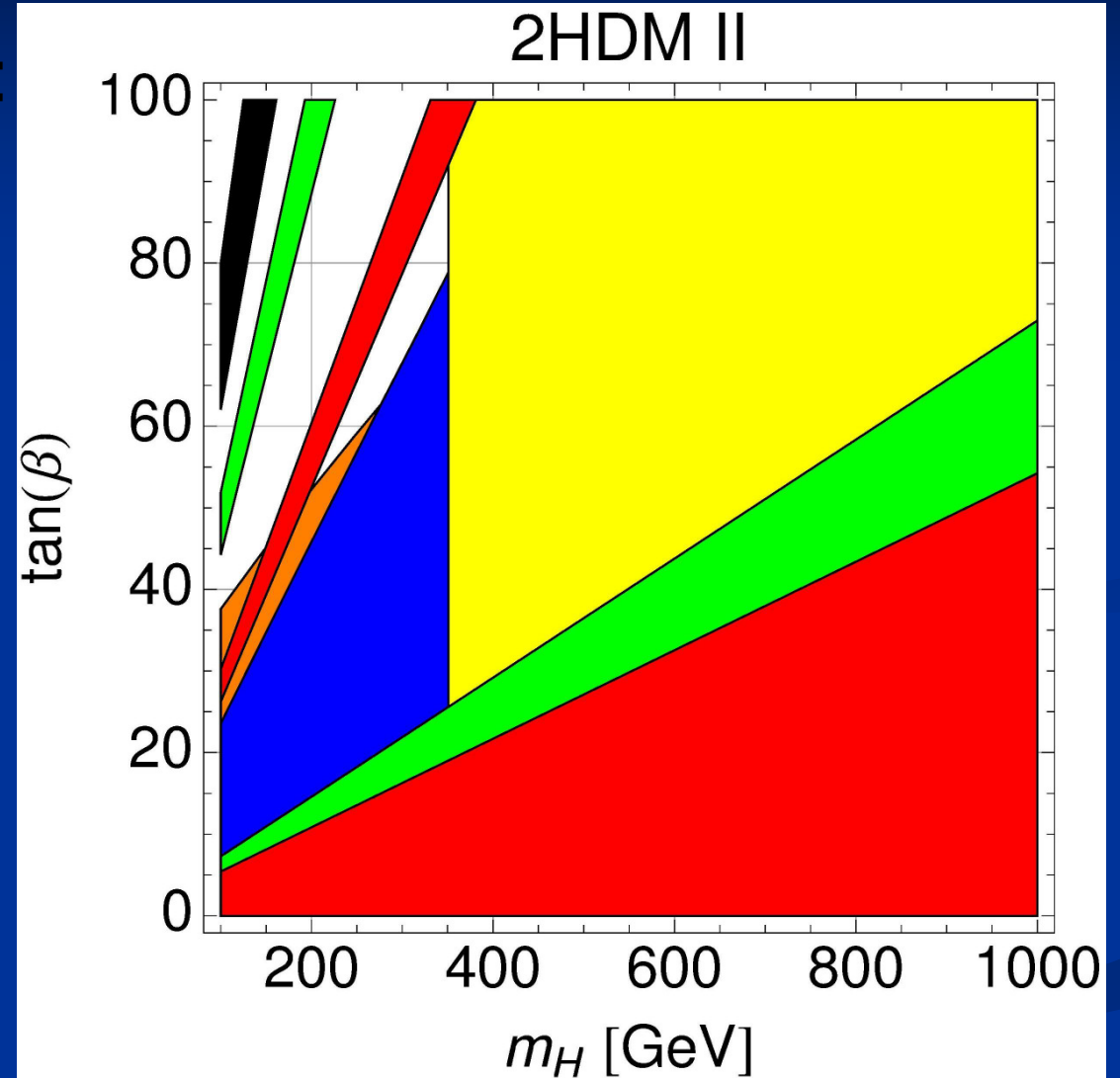
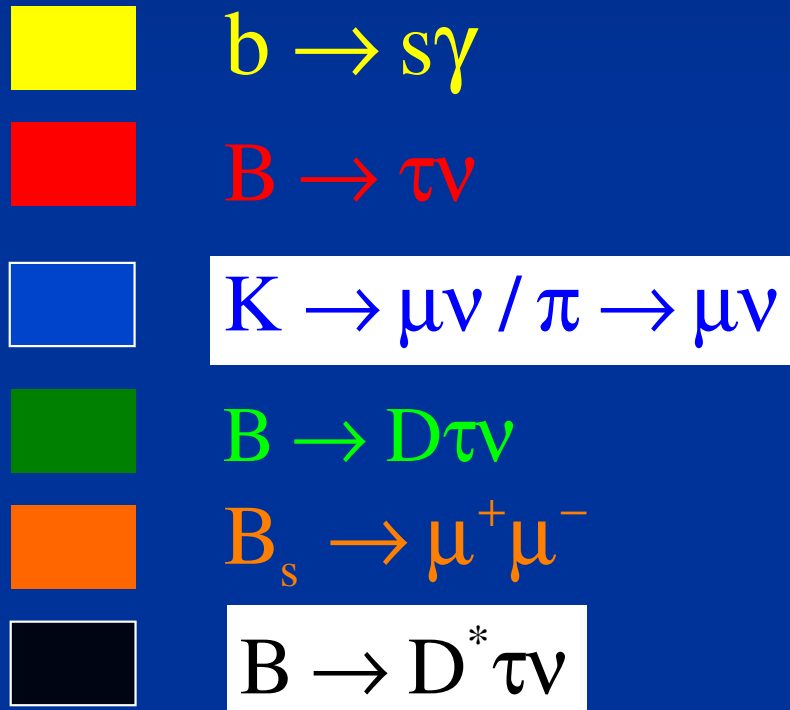


Relative importance of the 2-loop corrections  
approximately 9%

# Flavor- phenomenology of two-Higgs-doublet models

# Type-II 2HDM

- Allowed regions from:



 Tension from  $B \rightarrow D^*\tau\nu$



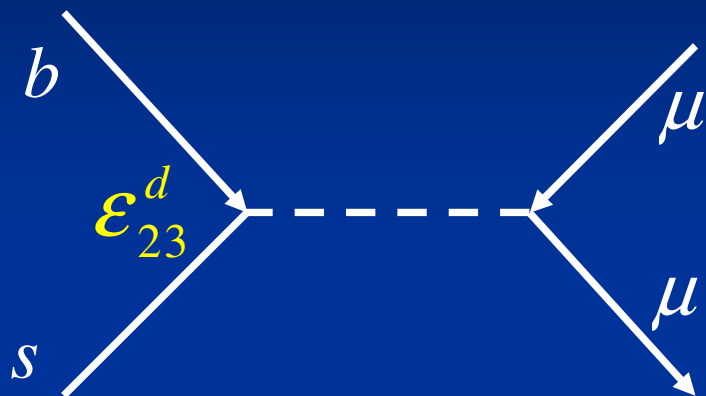
# Type-III: constraints from $M \rightarrow \mu^+ \mu^-$

$$\tan(\beta) = 50$$

  $m_H = 700 \text{ GeV}$

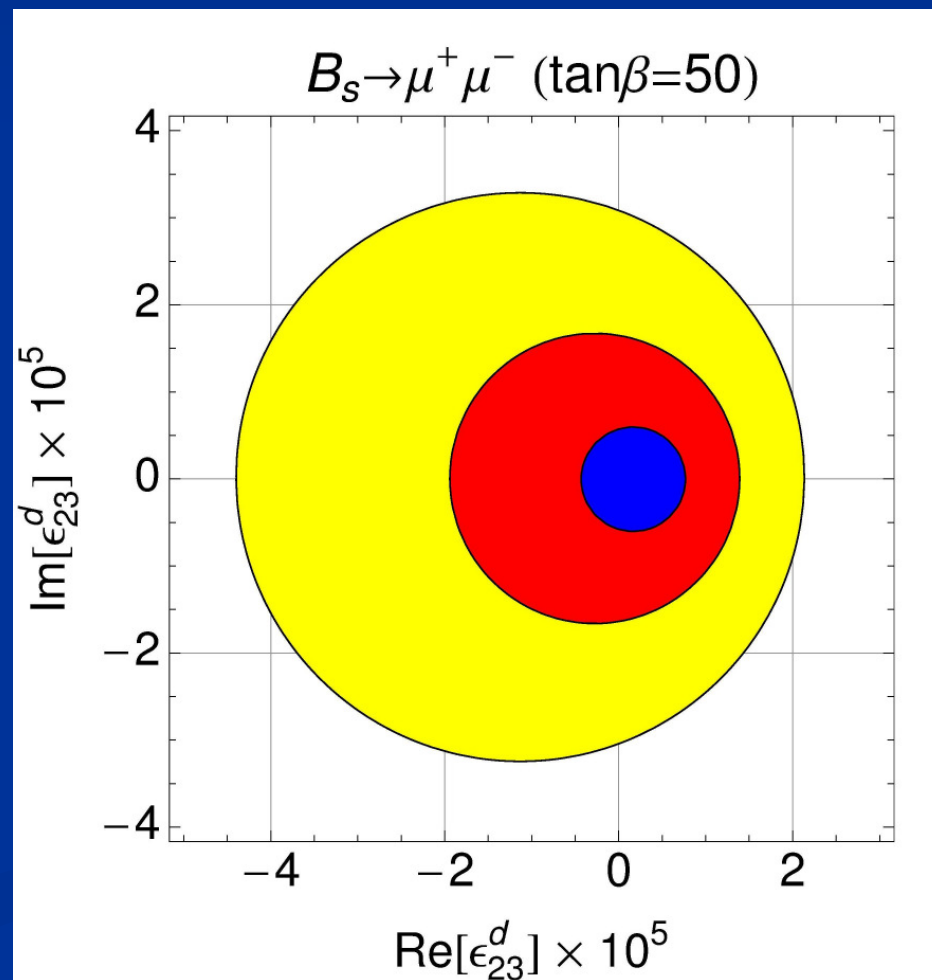
  $m_H = 500 \text{ GeV}$

  $m_H = 300 \text{ GeV}$



- $B \rightarrow \mu^+ \mu^-$  constrains  $\epsilon_{13,31}^d$
- $B_s \rightarrow \mu^+ \mu^-$  constrains  $\epsilon_{23,32}^d$
- $K_L \rightarrow \mu^+ \mu^-$  constrains  $\epsilon_{12,21}^d$
- $D \rightarrow \mu^+ \mu^-$  constrains  $\epsilon_{12,21}^u$

  $\epsilon_{32,23}^u$  and  $\epsilon_{13,31}^u$  unconstrained  
from tree-level FCNCs




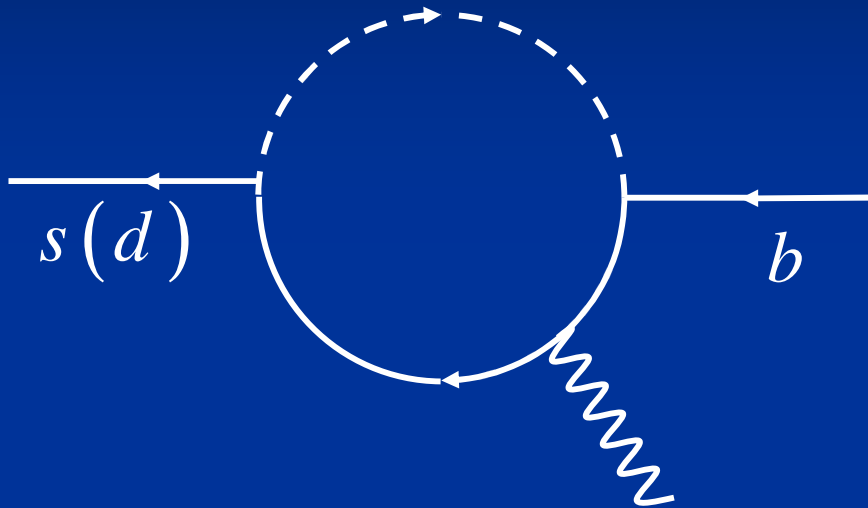
# Type-III: Constraints from $b \rightarrow s(d) \gamma$

$$\tan(\beta) = 50$$

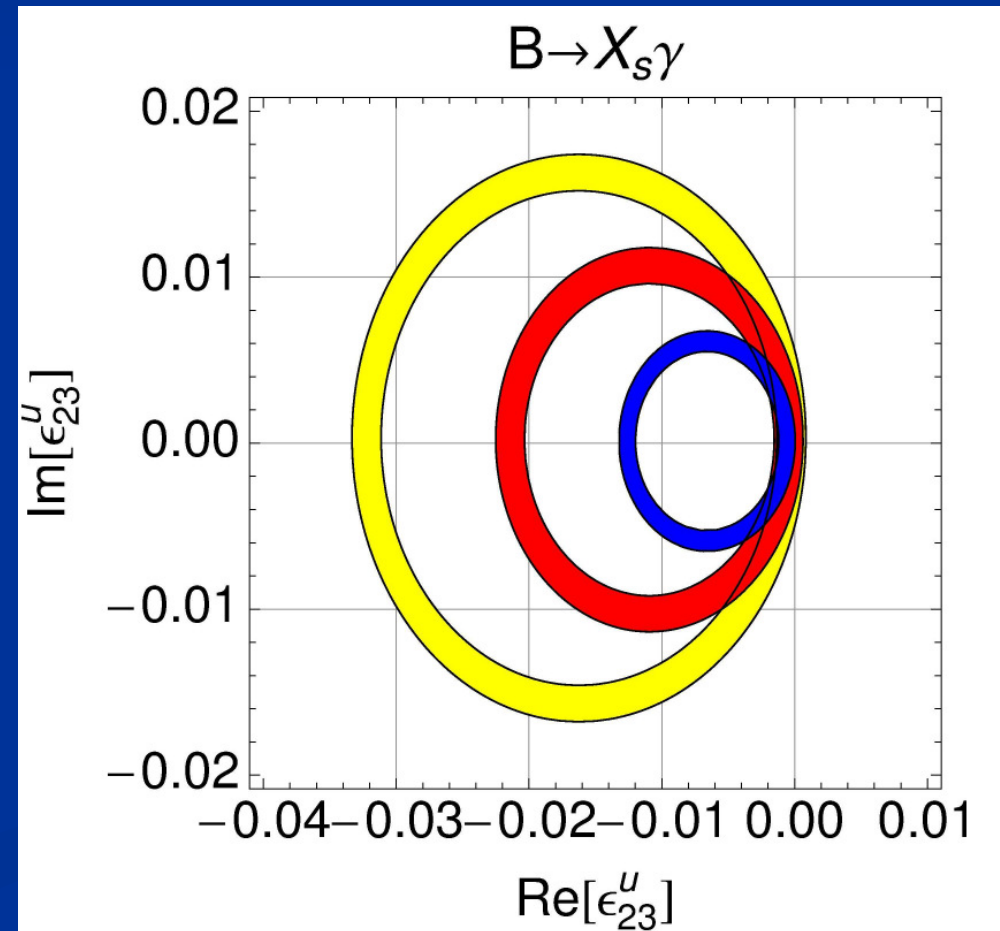
  $m_H = 700 \text{ GeV}$

  $m_H = 500 \text{ GeV}$

  $m_H = 300 \text{ GeV}$






- $b \rightarrow s\gamma$  constrains  $\epsilon_{23}^u$
- $b \rightarrow d\gamma$  constrains  $\epsilon_{13}^u$
- $\epsilon_{31,32}^u$  still unconstrained

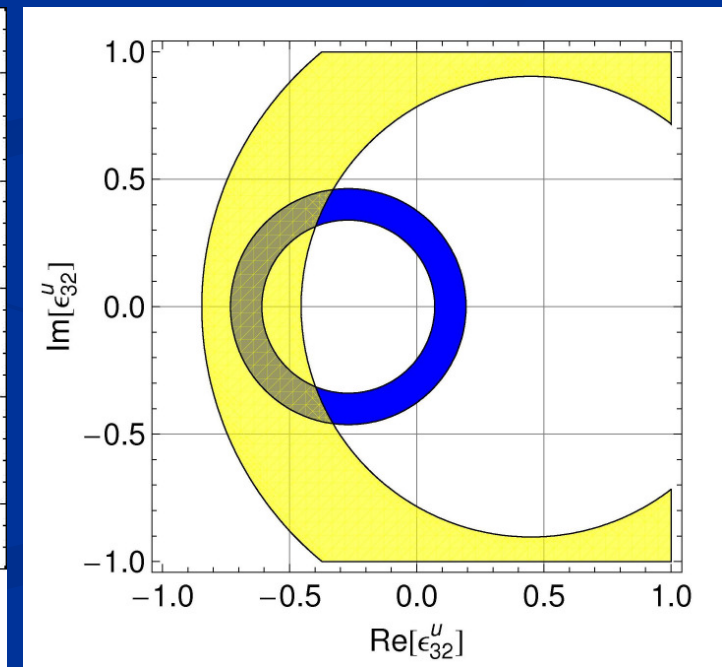
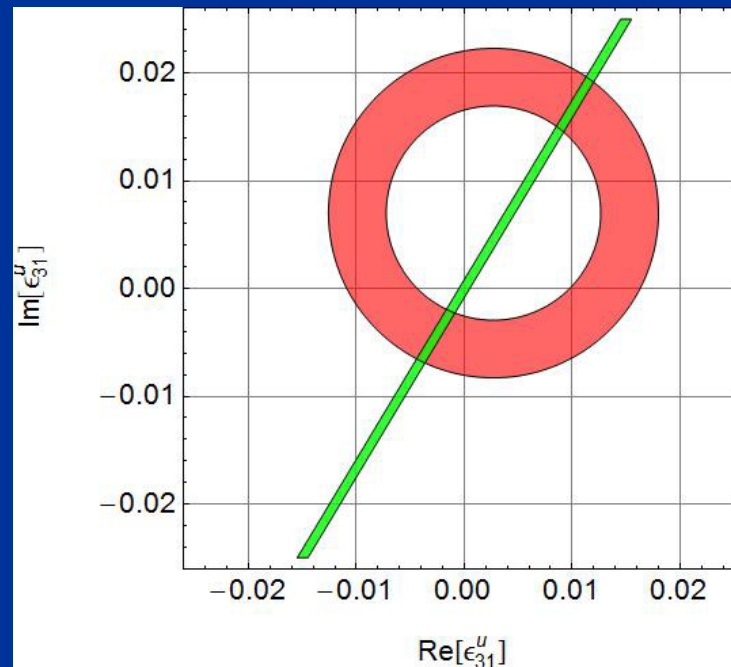


# Tauonic B decays

- Constructive contribution to  $B \rightarrow \tau \nu$  using  $\epsilon_{31}^u$  is possible.
- $B \rightarrow D^{(*)} \tau \nu$  and  $B \rightarrow D \tau \nu$  can be explained simultaneously using  $\epsilon_{32}^u$ . **→ Check model via  $H^0, A^0 \rightarrow \bar{t}c$**

Allowed regions from:

	$B \rightarrow D \tau \nu$
	$B \rightarrow D^* \tau \nu$
	$B \rightarrow \tau \nu$







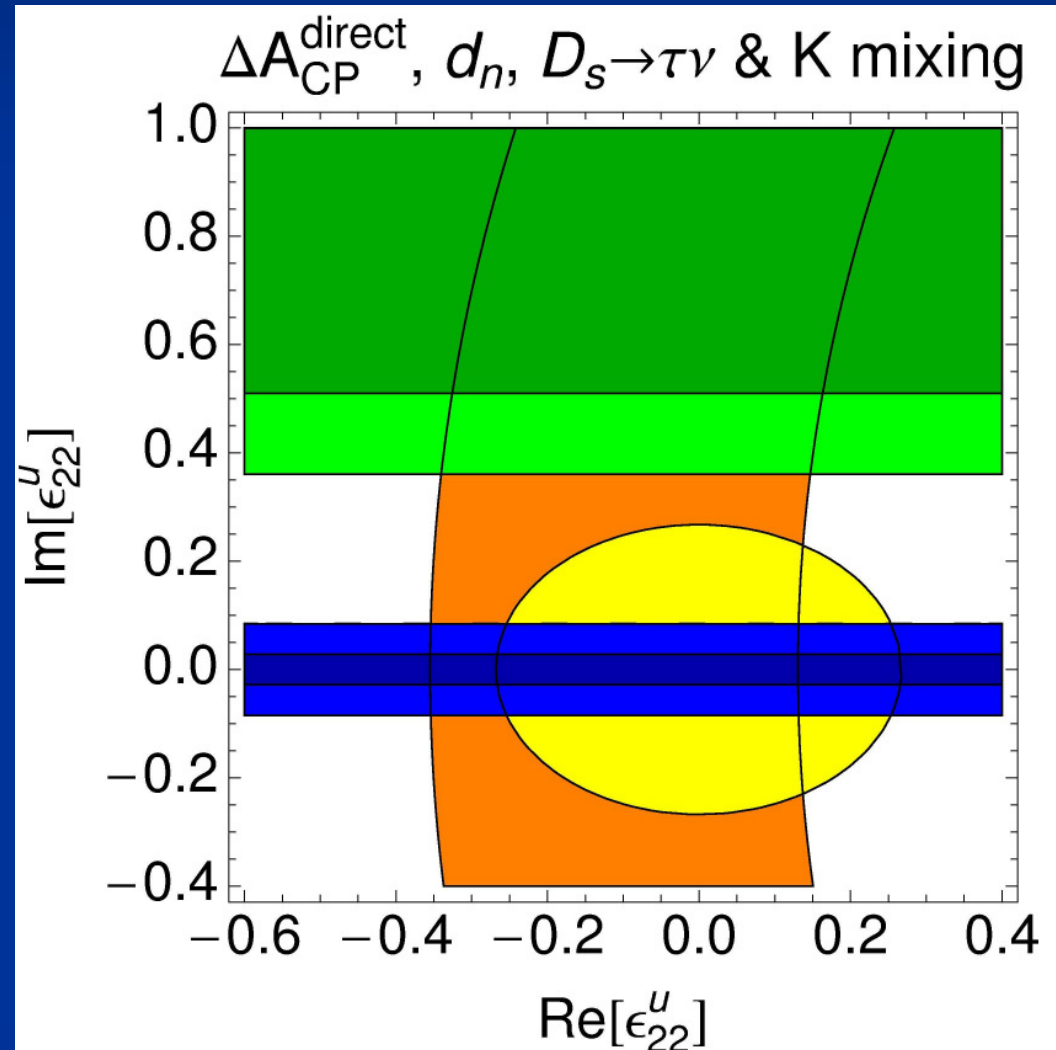
# Direct CP asymmetry in

$$\tan(\beta) = 50, m_H = 500 \text{ GeV}$$

- Cannot be explained in the 2HDM III

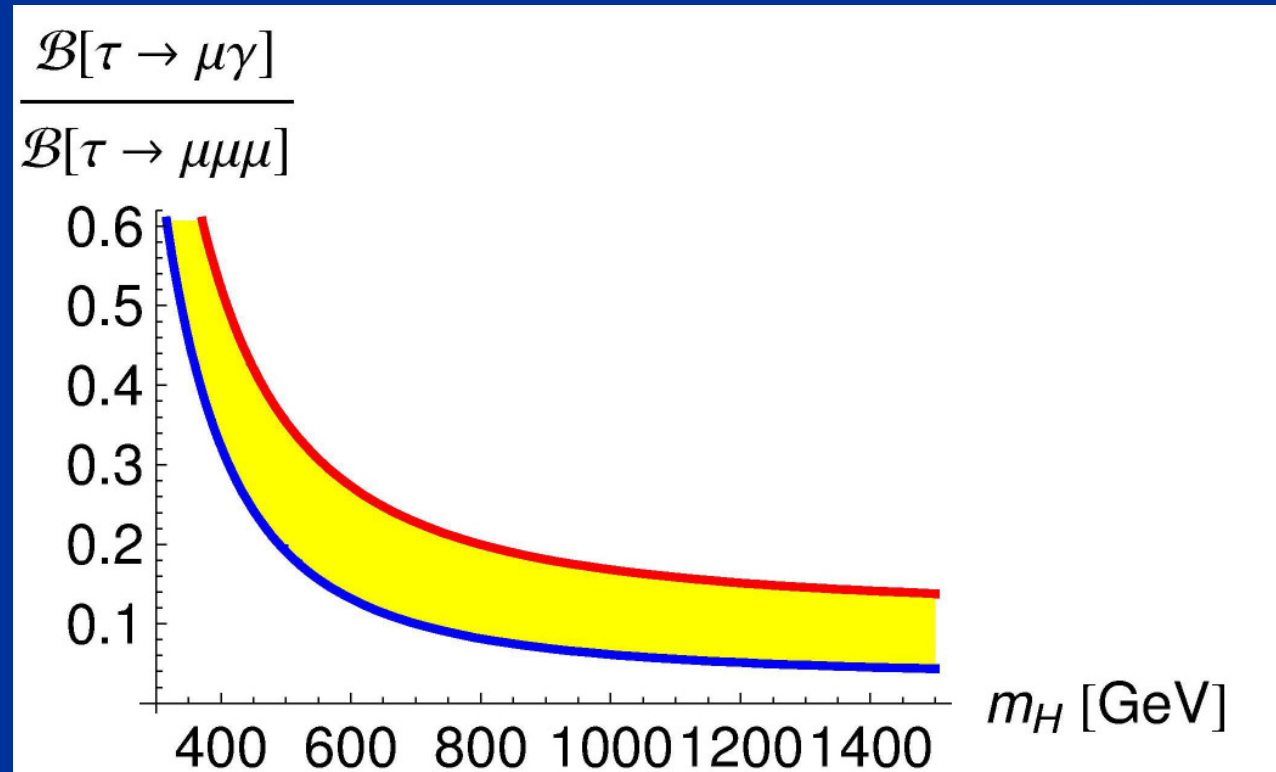
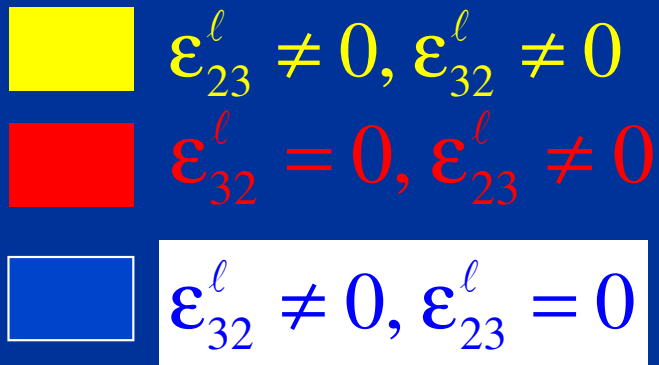
Allowed regions from:

-   $D \rightarrow KK, \pi\pi$
-  Neutron EDM
-   $K - \bar{K}$  mixing
-   $D_{(s)} \rightarrow \mu\nu$

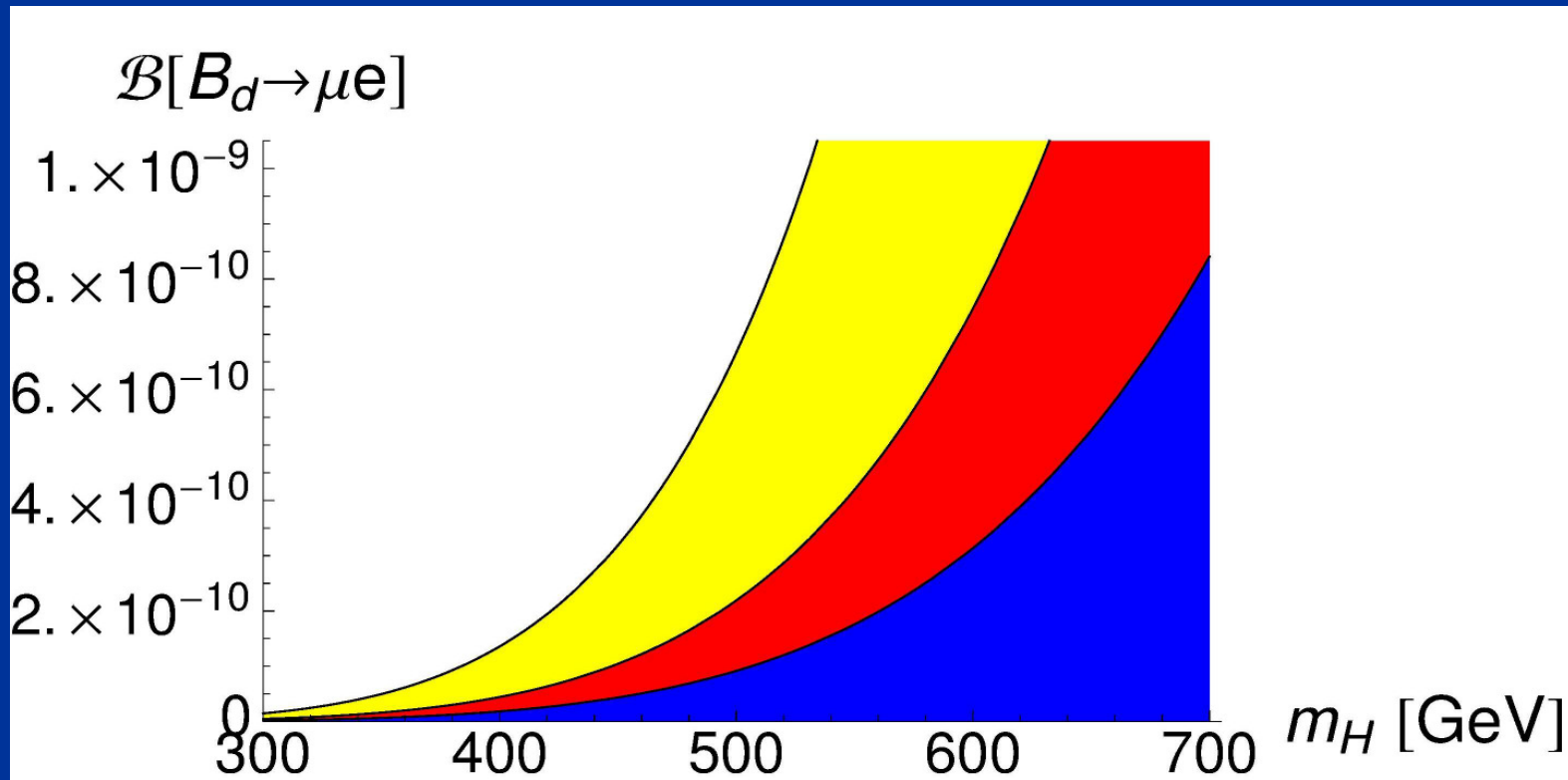
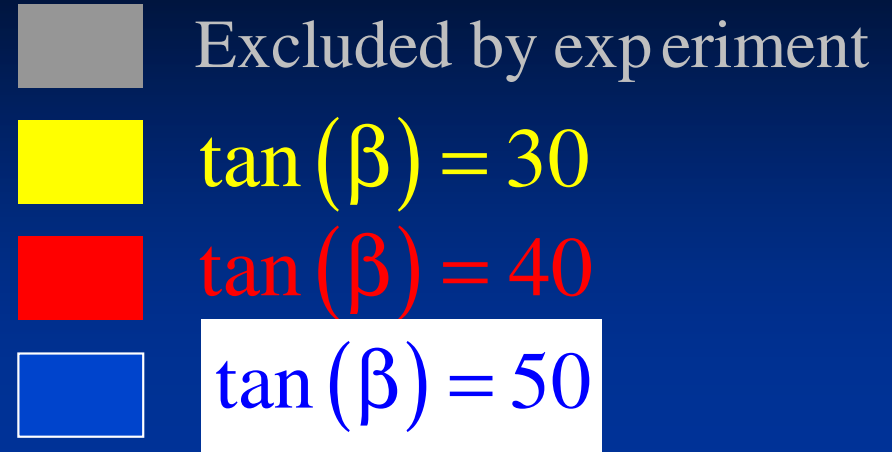


# Lepton Flavor violation

- Correlations between  $\tau \rightarrow \mu\mu\mu$  and  $\tau \rightarrow \mu\gamma$



# Upper limits on lepton flavour violating B decays



# Conclusions

- The decoupling limit of the MSSM is the 2HDM of type III
- Sizable non-holomorphic Higgs couplings are generated via loops, 2-loop calculation of Higgs-quark couplings significantly reduces the matching scale dependence.
- In the 2HDM III all off-diagonal elements  $\mathcal{E}_{ij}^q$  except  $\mathcal{E}_{31,32}^u$  must be small.
- A 2HDM of type III with flavour violation in the up-sector can explain  $B \rightarrow \tau \nu$ ,  $B \rightarrow D \tau \nu$  and  $B \rightarrow D^* \tau \nu$  simultaneously.
- The direct CP asymmetry in  $D \rightarrow KK, \pi\pi$  cannot be explained
- Interesting correlations between among lepton flavor violating observables.

# SUSY\_FLAVOR 2.0

A.C., J. Rosiek et al, arXiv:1203.5023

Calculates a large set of  
flavour observables  
including the complete  
resummation of  
all chirally enhanced  
corrections and the  
effective Higgs vertices.

Observable	Most stringent constraints on	Experiment
$\Delta F = 0$		
$\frac{1}{2}(g-2)_e$	$\text{Re} \left[ \delta_{11}^{\ell LR, RL} \right]$	$(1159652188.4 \pm 4.3) \times 10^{-12}$
$\frac{1}{2}(g-2)_\mu$	$\text{Re} \left[ \delta_{22}^{\ell LR, RL} \right]$	$(11659208.7 \pm 8.7) \times 10^{-10}$
$\frac{1}{2}(g-2)_\tau$	$\text{Re} \left[ \delta_{33}^{\ell LR, RL} \right]$	$< 1.1 \times 10^{-3}$
$ d_e (\text{ecm})$	$\text{Im} \left[ \delta_{11}^{\ell LR, RL} \right]$	$< 1.6 \times 10^{-27}$
$ d_\mu (\text{ecm})$	$\text{Im} \left[ \delta_{22}^{\ell LR, RL} \right]$	$< 2.8 \times 10^{-19}$
$ d_\tau (\text{ecm})$	$\text{Im} \left[ \delta_{33}^{\ell LR, RL} \right]$	$< 1.1 \times 10^{-17}$
$ d_n (\text{ecm})$	$\text{Im} \left[ \delta_{11}^{d LR, RL} \right], \text{Im} \left[ \delta_{11}^{u LR, RL} \right]$	$< 2.9 \times 10^{-26}$
$\Delta F = 1$		
$\text{Br}(\mu \rightarrow e\gamma)$	$\delta_{12,21}^{\ell LR, RL}, \delta_{12}^{\ell LL, RR}$	$< 2.8 \times 10^{-11}$
$\text{Br}(\tau \rightarrow e\gamma)$	$\delta_{13,31}^{\ell LR, RL}, \delta_{13}^{\ell LL, RR}$	$< 3.3 \times 10^{-8}$
$\text{Br}(\tau \rightarrow \mu\gamma)$	$\delta_{23,32}^{\ell LR, RL}, \delta_{23}^{\ell LL, RR}$	$< 4.4 \times 10^{-8}$
$\text{Br}(K_L \rightarrow \pi^0 \nu\nu)$	$\delta_{23}^{u LR}, \delta_{13}^{u LR} \times \delta_{23}^{u LR}$	$< 6.7 \times 10^{-8}$
$\text{Br}(K^+ \rightarrow \pi^+ \nu\nu)$	sensitive to $\delta_{13}^{u LR} \times \delta_{23}^{u LR}$	$17.3_{-10.5}^{+11.5} \times 10^{-11}$
$\text{Br}(B_d \rightarrow ee)$	$\delta_{13}^{d LL, RR}$	$< 1.13 \times 10^{-7}$
$\text{Br}(B_d \rightarrow \mu\mu)$	$\delta_{13}^{d LL, RR}$	$< 1.8 \times 10^{-8}$
$\text{Br}(B_d \rightarrow \tau\tau)$	$\delta_{13}^{d LL, RR}$	$< 4.1 \times 10^{-3}$
$\text{Br}(B_s \rightarrow ee)$	$\delta_{23}^{d LL, RR}$	$< 7.0 \times 10^{-5}$
$\text{Br}(B_s \rightarrow \mu\mu)$	$\delta_{23}^{d LL, RR}$	$< 1.08 \times 10^{-8}$
$\text{Br}(B_s \rightarrow \tau\tau)$	$\delta_{23}^{d LL, RR}$	—
$\text{Br}(B_s \rightarrow \mu e)$	$\delta_{23}^{d LL, RR} \times \delta_{12}^{\ell LL, RR}$	$< 2.0 \times 10^{-7}$
$\text{Br}(B_s \rightarrow \tau e)$	$\delta_{23}^{d LL, RR} \times \delta_{13}^{\ell LL, RR}$	$< 2.8 \times 10^{-5}$
$\text{Br}(B_s \rightarrow \mu\tau)$	$\delta_{23}^{d LL, RR} \times \delta_{23}^{\ell LL, RR}$	$< 2.2 \times 10^{-5}$
$\text{Br}(B^+ \rightarrow \tau^+ \nu)$	—	$(1.65 \pm 0.34) \times 10^{-4}$
$\text{Br}(B_d \rightarrow D\tau\nu)/\text{Br}(B_d \rightarrow D\nu)$	—	$(0.407 \pm 0.12 \pm 0.049)$
$\text{Br}(B \rightarrow X_s \gamma)$	$\delta_{23}^{d LL, RR}$ for large $\tan\beta$ , $\delta_{23,32}^{d LR}$	$(3.52 \pm 0.25) \times 10^{-4}$
$\Delta F = 2$		
$ \epsilon_K $	$\text{Im} \left[ (\delta_{12}^{d LL, RR})^2 \right], \text{Im} \left[ (\delta_{12,21}^{d LR})^2 \right]$	$(2.229 \pm 0.010) \times 10^{-3}$
$\Delta M_K$	$\delta_{12}^{d LL, RR}, \delta_{12,21}^{d LR}$	$(5.292 \pm 0.009) \times 10^{-3} \text{ ps}^{-1}$
$\Delta M_D$	$\delta_{12}^{u LL, RR}, \delta_{12,21}^{u LR}$	$(2.37_{-0.71}^{+0.66}) \times 10^{-2} \text{ ps}^{-1}$
$\Delta M_{B_d}$	$\delta_{13}^{d LL, RR}, \delta_{13,31}^{d LR}$	$(0.507 \pm 0.005) \text{ ps}^{-1}$
$\Delta M_{B_s}$	$\delta_{23}^{d LL, RR}, \delta_{23,32}^{d LR}$	$(17.77 \pm 0.12) \text{ ps}^{-1}$