

Optimizing the basis of $B \rightarrow K^* l^+ l^-$ in the full kinematic range

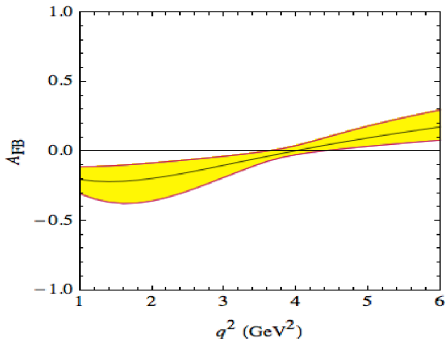
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Based on: S. Descotes, T. Hurth, JM, J. Virto, [arXiv: 1303.5794](#)

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For a long time huge efforts were devoted (still now) to measure the position of the zero of the forward-backward asymmetry A_{FB} of $B \rightarrow K^* \mu^+ \mu^-$.



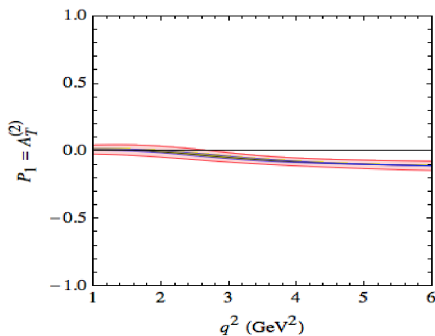
Reason:

- At LO the soft form factor dependence cancels exactly at q_0^2 (dependence appears at NLO).
- A relation among $\mathbf{C}_9^{\text{eff}}$ and $\mathbf{C}_7^{\text{eff}}$ arises at the zero:

$$\mathbf{C}_9^{\text{eff}}(q_0^2) + 2 \frac{m_b M_B}{q_0^2} \mathbf{C}_7^{\text{eff}} = 0$$

A similar idea was incorporated in the construction of the transverse asymmetry

$$A_T^{(2)}(q^2) = \frac{|A_{\perp}|^2 - |A_{\parallel}|^2}{|A_{\perp}|^2 + |A_{\parallel}|^2} \quad [\text{Kruger, J.M'05}]$$



where $A_{\perp, \parallel}$ correspond to two transversity amplitudes of the K^* .

- **Big advantage with respect to A_{FB} :** Cancellation of soft form factors at LO happens for all low- q^2 range ($0.1 - 6 \text{ GeV}^2$) and not only at one point. **First example of a clean observable.**
- $A_{\perp} \sim -A_{\parallel}$ in the SM ($A_T^{(2)} \sim 0$) due to its LH structure.
- $P_2 = -\frac{2A_{FB}}{3F_T} = \frac{1}{2}A_T^{re}$ is a clean version of A_{FB} with same information.

[Egede, Hurth, JM, Ramon, Reece'08, and '10]

- Later on a set of **transverse asymmetries** called $\mathbf{A}_T^{(3,4,5)}$ were proposed

$$\mathbf{A}_T^{(3)} = \frac{|A_0^L A_{\parallel}^{L*} + A_0^{R*} A_{\parallel}^R|}{\sqrt{|A_0|^2 |A_{\perp}|^2}} \quad \mathbf{A}_T^{(4)} = \frac{|A_0^L A_{\perp}^{L*} - A_0^{R*} A_{\perp}^R|}{|A_0^L A_{\parallel}^{L*} + A_0^{R*} A_{\parallel}^R|} \quad \mathbf{A}_T^{(5)} = \frac{|A_{\perp}^L A_{\parallel}^{R*} + A_{\perp}^R A_{\parallel}^L|}{|A_{\perp}|^2 + |A_{\parallel}|^2}$$

[Bobeth, Hiller, Dyk, '10]

- Also at the low-recoil a set of clean observables called $\mathbf{H}_T^{(1,2,3)}$ were proposed that correspond to $P_{4,5,6}$ at large-recoil.

$$\mathbf{H}_T^{(1)} = \frac{\text{Re}(A_0^L A_{\parallel}^{L*} + A_0^{R*} A_{\parallel}^R)}{\sqrt{|A_0|^2 |A_{\parallel}|^2}}, \quad \mathbf{H}_T^{(2)} = \frac{\text{Re}(A_0^L A_{\perp}^{L*} - A_0^{R*} A_{\perp}^R)}{\sqrt{|A_0|^2 |A_{\perp}|^2}}, \quad \mathbf{H}_T^{(3)} = \frac{\text{Re}(A_{\parallel}^L A_{\perp}^{L*} - A_{\parallel}^{R*} A_{\perp}^R)}{\sqrt{|A_{\parallel}|^2 |A_{\perp}|^2}}$$

[Altmannshofer, Ball, Bharucha, Buras, Straub, Wick'09]

- Finally, a set of CP-conserving and CP-violating observables \mathbf{S}_i and \mathbf{A}_i were constructed directly from the coefficients of the distribution, easy to measure

$$\mathbf{S}_i = \frac{\int_{bin} dq^2 [J_i + \bar{J}_i]}{d\Gamma/dq^2 + d\bar{\Gamma}/dq^2}, \quad \mathbf{A}_i = \frac{\int_{bin} dq^2 [J_i - \bar{J}_i]}{d\Gamma/dq^2 + d\bar{\Gamma}/dq^2}.$$

but sensitive already at LO to hadronic form factor uncertainties.

All those observables comes from the decay $\bar{B}_d \rightarrow \bar{K}^{*0}(\rightarrow K^- \pi^+) l^+ l^-$ with the K^{*0} on the mass shell. It is described by $s = q^2$ and three angles θ_l , θ_K and ϕ

$$\frac{d^4\Gamma(\bar{B}_d)}{dq^2 d\cos\theta_l d\cos\theta_K d\phi} = \frac{9}{32\pi} J(q^2, \theta_l, \theta_K, \phi)$$

The differential distribution splits in J_i coefficients:

$$J(q^2, \theta_l, \theta_K, \phi) = J_{1s} \sin^2 \theta_K + J_{1c} \cos^2 \theta_K + (J_{2s} \sin^2 \theta_K + J_{2c} \cos^2 \theta_K) \cos 2\theta_l + J_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi + J_4 \sin 2\theta_K \sin 2\theta_l \cos \phi + J_5 \sin 2\theta_K \sin \theta_l \cos \phi + (J_{6s} \sin^2 \theta_K + J_{6c} \cos^2 \theta_K) \cos \theta_l + J_7 \sin 2\theta_K \sin \theta_l \sin \phi + J_8 \sin 2\theta_K \sin 2\theta_l \sin \phi + J_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi.$$

The decay rate $\bar{\Gamma}(B_d)$ is obtained replacing within our conventions:

[Bobeth, Hiller, Piranishvili'08]

$$J_{1,2,3,4,7} \rightarrow \bar{J}_{1,2,3,4,7} \quad \text{and} \quad J_{5,6,8,9} \rightarrow -\bar{J}_{5,6,8,9}$$

The information on

- the helicity/transversity amplitudes of the K^* ($H_{\pm 1,0}$ or $A_{\perp, \parallel, 0}$) is inside the coefficients J_i .
- short distance physics C_i is encoded in ($H_{\pm 1,0}$ or $A_{\perp, \parallel, 0}$)

$$\begin{aligned}
J_{1s} &= \frac{(2 + \beta_\ell^2)}{4} \left[|A_\perp^L|^2 + |A_\parallel^L|^2 + (L \rightarrow R) \right] + \frac{4m_\ell^2}{q^2} \operatorname{Re} \left(A_\perp^L A_\perp^{R*} + A_\parallel^L A_\parallel^{R*} \right), \\
J_{1c} &= |A_0^L|^2 + |A_0^R|^2 + \frac{4m_\ell^2}{q^2} \left[|A_t|^2 + 2\operatorname{Re}(A_0^L A_0^{R*}) \right] + \beta_\ell^2 |A_S|^2, \\
J_{2s} &= \frac{\beta_\ell^2}{4} \left[|A_\perp^L|^2 + |A_\parallel^L|^2 + (L \rightarrow R) \right], \quad J_{2c} = -\beta_\ell^2 \left[|A_0^L|^2 + (L \rightarrow R) \right], \\
J_3 &= \frac{1}{2} \beta_\ell^2 \left[|A_\perp^L|^2 - |A_\parallel^L|^2 + (L \rightarrow R) \right], \quad J_4 = \frac{1}{\sqrt{2}} \beta_\ell^2 \left[\operatorname{Re}(A_0^L A_\parallel^{L*}) + (L \rightarrow R) \right], \\
J_5 &= \sqrt{2} \beta_\ell \left[\operatorname{Re}(A_0^L A_\perp^{L*}) - (L \rightarrow R) - \frac{m_\ell}{\sqrt{q^2}} \operatorname{Re}(A_\parallel^L A_S^* + A_\parallel^R A_S^*) \right], \\
J_{6s} &= 2\beta_\ell \left[\operatorname{Re}(A_\parallel^L A_\perp^{L*}) - (L \rightarrow R) \right], \quad J_{6c} = 4\beta_\ell \frac{m_\ell}{\sqrt{q^2}} \operatorname{Re} \left[A_0^L A_S^* + (L \rightarrow R) \right], \\
J_7 &= \sqrt{2} \beta_\ell \left[\operatorname{Im}(A_0^L A_\parallel^{L*}) - (L \rightarrow R) + \frac{m_\ell}{\sqrt{q^2}} \operatorname{Im}(A_\perp^L A_S^* + A_\perp^R A_S^*) \right], \\
J_8 &= \frac{1}{\sqrt{2}} \beta_\ell^2 \left[\operatorname{Im}(A_0^L A_\perp^{L*}) + (L \rightarrow R) \right], \quad J_9 = \beta_\ell^2 \left[\operatorname{Im}(A_\parallel^{L*} A_\perp^L) + (L \rightarrow R) \right]
\end{aligned}$$

In red lepton mass terms.

[Egede, Hurth, JM, Ramon, Reece'10]

An important step forward was the identification of the **symmetries** of the distribution:

Transformation of amplitudes leaving distribution invariant.

Symmetries determine the minimal # observables for each scenario:

$$n_{obs} = 2n_A - n_S$$

Case	Coefficients	Amplitudes	Symmetries	Observables
$m_\ell = 0, A_S = 0$	11	6	4	8
$m_\ell = 0$	11	7	5	9
$m_\ell > 0, A_S = 0$	11	7	4	10
$m_\ell > 0$	12	8	4	12

All symmetries (massive and scalars) were found explicitly later on.

[JM, Mescia, Ramon, Virto'12]

Symmetries \Rightarrow # of observables \Rightarrow determine a **basis**: each angular observable constructed can be expressed in terms of this basis.

Optimal basis of observables, a compromise between:

- *Excellent experimental accessibility and simplicity of the fit.*
- *Reduced FF dependence (in the low- q^2 (or large-recoil) region).*

Our proposal for **CP-conserving basis**:

$$\left\{ \frac{d\Gamma}{dq^2}, \mathbf{F}_L, \mathbf{P}_1, \mathbf{P}_2, \mathbf{P}_3, \mathbf{P}'_4, \mathbf{P}'_5, \mathbf{P}'_6 \right\}$$

where $P_1 = A_7^2$ [Kruger, J.M'05], $P_2 = \frac{1}{2}A_7^{\text{re}}$, $P_3 = -\frac{1}{2}A_7^{\text{im}}$ [Becirevic, Schneider'12] and $P'_{4,5,6}$ [Descotes, JM, Ramon, Virto'13]

and the corresponding **CP-violating basis**:

$$\left\{ \mathbf{A}_{\text{CP}}, \mathbf{F}_L^{\text{CP}}, \mathbf{P}_1^{\text{CP}}, \mathbf{P}_2^{\text{CP}}, \mathbf{P}_3^{\text{CP}}, \mathbf{P}'_4^{\text{CP}}, \mathbf{P}'_5^{\text{CP}}, \mathbf{P}'_6^{\text{CP}} \right\}$$

Besides one may include a redundant observable (in absence of scalars) $P'_8 = Q'$ and a corresponding P_8^{CP} .

There is a correspondence between $\mathbf{P}_i^{(\prime)}$ and \mathbf{J}_k (β_ℓ^2 absorbed here in $F_{L,T}$)

$$\begin{aligned}
 (\mathbf{J}_{2s} + \bar{\mathbf{J}}_{2s}) &= \frac{1}{4} \mathbf{F}_T \frac{d\Gamma + d\bar{\Gamma}}{dq^2} & (\mathbf{J}_{2c} + \bar{\mathbf{J}}_{2c}) &= -\mathbf{F}_L \frac{d\Gamma + d\bar{\Gamma}}{dq^2} \\
 \mathbf{J}_3 + \bar{\mathbf{J}}_3 &= \frac{1}{2} \mathbf{P}_1 \mathbf{F}_T \frac{d\Gamma + d\bar{\Gamma}}{dq^2} & \mathbf{J}_3 - \bar{\mathbf{J}}_3 &= \frac{1}{2} \mathbf{P}_1^{\text{CP}} \mathbf{F}_T \frac{d\Gamma + d\bar{\Gamma}}{dq^2} \\
 \mathbf{J}_{6s} + \bar{\mathbf{J}}_{6s} &= 2 \mathbf{P}_2 \mathbf{F}_T \frac{d\Gamma + d\bar{\Gamma}}{dq^2} & \mathbf{J}_{6s} - \bar{\mathbf{J}}_{6s} &= 2 \mathbf{P}_2^{\text{CP}} \mathbf{F}_T \frac{d\Gamma + d\bar{\Gamma}}{dq^2} \\
 \mathbf{J}_9 + \bar{\mathbf{J}}_9 &= -\mathbf{P}_3 \mathbf{F}_T \frac{d\Gamma + d\bar{\Gamma}}{dq^2} & \mathbf{J}_9 - \bar{\mathbf{J}}_9 &= -\mathbf{P}_3^{\text{CP}} \mathbf{F}_T \frac{d\Gamma + d\bar{\Gamma}}{dq^2} \\
 \mathbf{J}_4 + \bar{\mathbf{J}}_4 &= \frac{1}{2} \mathbf{P}'_4 \sqrt{\mathbf{F}_T \mathbf{F}_L} \frac{d\Gamma + d\bar{\Gamma}}{dq^2} & \mathbf{J}_4 - \bar{\mathbf{J}}_4 &= \frac{1}{2} \mathbf{P}'_4{}^{\text{CP}} \sqrt{\mathbf{F}_T \mathbf{F}_L} \frac{d\Gamma + d\bar{\Gamma}}{dq^2} \\
 \mathbf{J}_5 + \bar{\mathbf{J}}_5 &= \mathbf{P}'_5 \sqrt{\mathbf{F}_T \mathbf{F}_L} \frac{d\Gamma + d\bar{\Gamma}}{dq^2} & \mathbf{J}_5 - \bar{\mathbf{J}}_5 &= \mathbf{P}'_5{}^{\text{CP}} \sqrt{\mathbf{F}_T \mathbf{F}_L} \frac{d\Gamma + d\bar{\Gamma}}{dq^2} \\
 \mathbf{J}_7 + \bar{\mathbf{J}}_7 &= -\mathbf{P}'_6 \sqrt{\mathbf{F}_T \mathbf{F}_L} \frac{d\Gamma + d\bar{\Gamma}}{dq^2} & \mathbf{J}_7 - \bar{\mathbf{J}}_7 &= -\mathbf{P}'_6{}^{\text{CP}} \sqrt{\mathbf{F}_T \mathbf{F}_L} \frac{d\Gamma + d\bar{\Gamma}}{dq^2}
 \end{aligned}$$

where each $\mathbf{P}_i^{(\prime)}$ and $\mathbf{P}_i^{(\prime)\text{CP}}$ encodes the information that can be extracted *cleanly* at large-recoil inside each \mathbf{J}_k and define the simplest possible fit besides S_i, A_i . The **brown** and **blue** pieces are strongly FF-dependent pieces.

Massive observables

- In the construction of the $P_{1,2,3}, P'_{4,5,6}$ *all m_ℓ corrections* are included.
- Still from the first couple of J 's: \mathbf{J}_{1c} and \mathbf{J}_{1s} it is possible to construct a couple more of observables (and CP) to take into account their m_ℓ terms.
- The simplest way to do it is to define an extra $\hat{\mathbf{F}}_T$ and $\hat{\mathbf{F}}_L$ (FF dependent)

$$(\mathbf{J}_{1s} + \bar{\mathbf{J}}_{1s}) = \frac{3}{4} \hat{\mathbf{F}}_T \frac{d\Gamma + d\bar{\Gamma}}{dq^2} \quad (\mathbf{J}_{1c} + \bar{\mathbf{J}}_{1c}) = \hat{\mathbf{F}}_L \frac{d\Gamma + d\bar{\Gamma}}{dq^2}$$

such that $\hat{\mathbf{F}}_L/\mathbf{F}_L = \frac{1}{\beta_\ell^2}(1 + \mathbf{M}_2)$ and $\hat{\mathbf{F}}_T/\mathbf{F}_T = \frac{1}{3\beta_\ell^2}(2 + (1 + 4\mathbf{M}_1)\beta_\ell^2)$.

Those $\mathbf{M}_{1,2}$ can be added to the basis.

Redundancy

- If no scalars are present there is one redundant observable ($P'_8 = Q', P_8^{CP}$)

$$\mathbf{J}_8 + \bar{\mathbf{J}}_8 = -\frac{1}{2} \mathbf{P}'_8 \sqrt{\mathbf{F}_T \mathbf{F}_L} \frac{d\Gamma + d\bar{\Gamma}}{dq^2}$$

$$P'_8 = \frac{2}{\sqrt{1 - P_1}} \left\{ (P_2 P_6 - P_3 P_4) + \eta [(P_2 P_6 - P_3 P_4)^2 + P_5 (P_2 P_4 + P_3 P_6)] \sqrt{1 - P_1^2} \right. \\ \left. + \frac{1}{4} (1 - \sum_{i=4}^6 P_i^2) (1 - P_1^2) - P_2^2 - P_3^2 \right\}^{\frac{1}{2}}$$

Folded distributions

BIG STEP: Substitute *uniangular distributions* \rightarrow *folded distributions*

The **identification** of $\phi \leftrightarrow \phi + \pi$ ($\phi < 0$) produces a “**folded**” angle $\hat{\phi} \in [0, \pi]$ in terms of which a (folded) differential rate $d\hat{\Gamma}(\hat{\phi}) = d\Gamma(\phi) + d\Gamma(\phi - \pi)$ is:

$$\frac{d^4\hat{\Gamma}}{dq^2 d\cos\theta_K d\cos\theta_l d\hat{\phi}} = \frac{9}{16\pi} \left[\mathbf{J}_{1c} \cos^2\theta_K + \mathbf{J}_{1s}(1 - \cos^2\theta_K) + \mathbf{J}_{2c} \cos^2\theta_K \cos 2\theta_\ell + \mathbf{J}_{2s}(1 - \cos^2\theta_K)(2\cos^2\theta_\ell - 1) + \mathbf{J}_3 \sin^2\theta_K(1 - \cos^2\theta_\ell) \cos 2\hat{\phi} + \mathbf{J}_{6s}(1 - \cos^2\theta_K) \cos\theta_\ell + \mathbf{J}_9(1 - \cos^2\theta_K)(1 - \cos^2\theta_\ell) \sin 2\hat{\phi} \right] \mathbf{X} + \mathbf{W}_1$$

with

$$\mathbf{X} = \int dm_{K\pi}^2 |BW_{K^*}(m_{K\pi}^2)|^2$$

being a correction to consider the width of the resonance. **Advantages:**

- Folding reduces the # of coefficients to a manageable experimentally subset. In this case: $11 J + 8 \tilde{J} \rightarrow 7 J + 4 \tilde{J}$
- Unwanted S-wave pollution has a distinct angular dependence:

$$\mathbf{W}_1 = \frac{1}{2\pi} \left[\tilde{\mathbf{J}}_{1a}^c + \tilde{\mathbf{J}}_{1b}^c \cos\theta_K + \left(\tilde{\mathbf{J}}_{2a}^c + \tilde{\mathbf{J}}_{2b}^c \cos\theta_K \right) (2\cos^2\theta_\ell - 1) \right]$$

Or in terms of observables generalizing LHCb note (CONF-2012-008) to include lepton mass corrections and the S-wave pollution in a minimal form [JM'12]

$$\begin{aligned} \frac{d^4\Gamma}{dq^2 d\cos\theta_K d\cos\theta_\ell d\hat{\phi}} &= \frac{9}{16\pi} \left[\hat{F}_L \cos^2\theta_K + \frac{3}{4} \hat{F}_T (1 - \cos^2\theta_K) - F_L \cos^2\theta_K \cos 2\theta_\ell \right. \\ &+ \frac{1}{4} F_T (1 - \cos^2\theta_K) (2 \cos^2\theta_\ell - 1) + \frac{1}{2} P_1 F_T (1 - \cos^2\theta_K) (1 - \cos^2\theta_\ell) \cos 2\hat{\phi} \\ &\left. + 2P_2 F_T (1 - \cos^2\theta_K) \cos\theta_\ell - P_3 F_T (1 - \cos^2\theta_K) (1 - \cos^2\theta_\ell) \sin 2\hat{\phi} \right] \frac{d\Gamma_{K^*}}{dq^2} + W_1 \end{aligned}$$

where

$$\frac{d\Gamma_{K^*}}{dq^2} = \frac{1}{4} (3J_{1c} + 6J_{1s} - J_{2c} - 2J_{2s}) \mathbf{X}$$

Notation: β_ℓ^2 is included inside $F_{L,T}$ ($F_{L,T} = \beta_\ell^2 \tilde{F}_{L,T}$ as compared to notation [JM'12]) and the P_i are the massive versions defined previously (for instance P_2 corresponds to $P_2^{m_\ell \neq 0}$ in [JM'12]).

- An intermediate massless-improved limit can be easily defined by

$$\hat{F}_T \rightarrow \frac{F_T}{\beta_\ell^2}, \quad \hat{F}_L \rightarrow 1 - \frac{F_T}{\beta_\ell^2}$$

where the error induced by this approximation is below 2%.

In this improved limit 6 observables (one less): $\{ F_{L,T}, P_{1,2,3}, \frac{d\Gamma_{K^*}}{dq^2} \} + 4 \tilde{J}$

Other double folded distributions can be **more selective** and allow to extract other sets of observables of the optimal basis. For examples: [JM'12]

Identify $\phi \leftrightarrow -\phi$ ($\phi < 0$) and $\theta_\ell \leftrightarrow \theta_\ell - \frac{\pi}{2}$ ($\theta_\ell > \frac{\pi}{2}$) with $\hat{\phi} \in [0, \pi]$, $\hat{\theta}_\ell \in [0, \pi/2]$ and the corresponding folded distribution is:

$$d\hat{\Gamma} = d\Gamma(\hat{\phi}, \hat{\theta}_\ell, \theta_K) + d\Gamma(\hat{\phi}, \hat{\theta}_\ell + \frac{\pi}{2}, \theta_K) + d\Gamma(-\hat{\phi}, \hat{\theta}_\ell, \theta_K) + d\Gamma(-\hat{\phi}, \hat{\theta}_\ell + \frac{\pi}{2}, \theta_K)$$

$$\frac{d^4\hat{\Gamma}}{dq^2 d\cos\theta_K d\cos\hat{\theta}_\ell d\hat{\phi}} = \frac{9}{32\pi} \left[\frac{1}{2}(4\hat{\mathbf{F}}_L + 3\hat{\mathbf{F}}_T + (4\hat{\mathbf{F}}_L - 3\hat{\mathbf{F}}_T) \cos 2\theta_K) + \right.$$

$$+ 2\sqrt{\mathbf{F}_L\mathbf{F}_T}\mathbf{P}'_5 \cos \hat{\phi} \sin 2\theta_K (\sin \hat{\theta}_\ell + \cos \hat{\theta}_\ell) +$$

$$\left. + \mathbf{F}_T \sin^2 \theta_K (\mathbf{P}_1 \cos 2\hat{\phi} + 4\mathbf{P}_2 (\cos \hat{\theta}_\ell - \sin \hat{\theta}_\ell)) \right] \frac{d\Gamma_{K^*}}{dq^2} + \mathbf{W}_{13}$$

where $\mathbf{W}_{13} = \frac{1}{2\pi} \left[2\tilde{J}_{1a}^c + 2\tilde{J}_{1b}^c \cos \theta_K + \tilde{J}_5 \cos \hat{\phi} \sin \theta_K (\cos \hat{\theta}_\ell + \sin \hat{\theta}_\ell) \right]$

Again $\mathbf{F}_{L,T}$ absorbed a β_ℓ^2 piece and \mathbf{P}_2 and \mathbf{P}'_5 are the massive version.

Large-recoil

- ET: QCDF/SCET. Soft form factors $\xi_{\perp,\parallel}(q^2)$ from

$$\begin{aligned}\xi_{\perp}(q^2) &= \frac{m_B}{m_B + m_{K^*}} \mathbf{V}(q^2), \\ \xi_{\parallel}(q^2) &= \frac{m_B + m_{K^*}}{2E} \mathbf{A}_1(q^2) - \frac{m_B - m_{K^*}}{m_B} \mathbf{A}_2(q^2)\end{aligned}$$

- q^2 -dependence of form factors is reproduced using a SE with single pole.
- FF at $q^2 = 0$ and slope parameters are computed by [Khodjamirian et al.'10] (KMPW) using light-cone sum rules.

The wide spread of different errors in literature associated to FF:

$$V(0) = 0.31 \pm 0.04 \text{ and } A(0) = 0.33 \pm 0.03 \text{ [W. Altmannshofer et al.'09]}$$

$$V(0) = 0.36 \pm 0.17 \text{ and } A(0) = 0.29 \pm 0.10 \text{ [A. Khodjamirian et al. '10].}$$

Even central values have shifted significantly, for instance $V(0) = 0.41 \pm 0.05$ [P. Ball and R. Zwicky,'05] (BZ).

It is essential to be conservative: We choose KMPW in our analysis since all other parametrizations for $V, A_{1,2}(q^2)$ always fall inside error bars of KMPW.

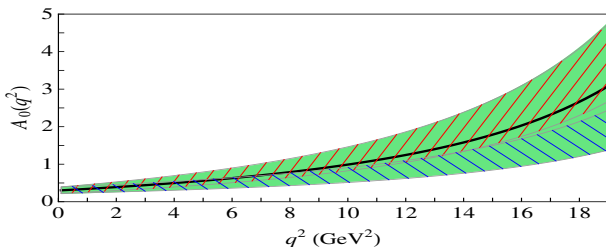
Once $\xi_{\perp}(q^2)$ and $\xi_{\parallel}(q^2)$ are defined all form factors follow

$$A_1(q^2) = \frac{2E}{m_B + m_{K^*}} \xi_{\perp}(q^2) + \Delta A_1 + \mathcal{O}(\Lambda/m_b)$$

$$A_2(q^2) = \frac{m_B}{m_B - m_{K^*}} [\xi_{\perp}(q^2) - \xi_{\parallel}(q^2)] + \frac{m_B}{2E} \frac{m_B + m_{K^*}}{m_B - m_{K^*}} \Delta A_1 + \mathcal{O}(\Lambda/m_b)$$

$$A_0(q^2) = \frac{E}{m_{K^*}} \frac{\xi_{\parallel}(q^2)}{\Delta_{\parallel}(q^2)} + \mathcal{O}(\Lambda/m_b)$$

$A_{1,2}(q^2)$ have good agreement with KMPW. But $A_0(q^2)$ require an enlarged error bar to get agreement between both determinations (enters only A_t).



Tensor form factors $T_{\perp,\parallel}$ are computed in QCDF following [Beneke, Feldmann, Seidel'01,'05] including factorizable and non-factorizable contributions.

Low-recoil

- LCSR are valid up to $q \leq 14 \text{ GeV}^2$. We extend FF determination [Bobeth & Hiller & Dyk'10] till 19 GeV^2 and cross check the consistency with **lattice** QCD. In HQET one expects the ratios to be near one

$$R_1 = \frac{T_1(q^2)}{V(q^2)}, \quad R_2 = \frac{T_2(q^2)}{A_1(q^2)}, \quad R_3 = \frac{q^2}{m_B^2} \frac{T_3(q^2)}{A_2(q^2)}.$$

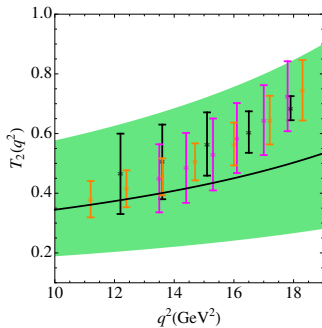
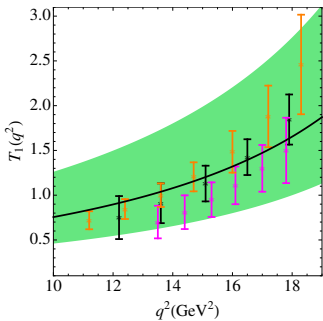
- BZ was problematic with R_3 .

Indeed R_3 originates from the scaling laws of form factors [Grinstein, Pirjol'04] and it is a bit more complicated:

$$R_3^{GP} = \frac{q^2}{m_B^2} \frac{T_3}{2 \frac{m_V}{m_B} A_0(q^2) - \left(1 + \frac{m_V}{m_B}\right) A_1(q^2) + \left(1 - \frac{m_V}{m_B}\right) A_2(q^2)}.$$

If one applies strictly the different order in m_b of FF in the denominator then $R_3^{GP} \rightarrow R_3$. However effectively the three terms are numerically competing. For this reason we prefer **not to use** nor R_3 neither R_3^{GP} to get T_3 from A_2 .

Our approach: we determine $T_{1,2}$ by exploiting the ratios $R_{1,2}$ allowing for up to a 20% breaking, i.e., $R_{1,2} = 1 + \delta_{1,2}$. All other form factors extrapolated from KMPW.

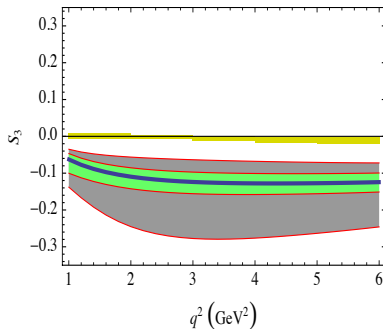
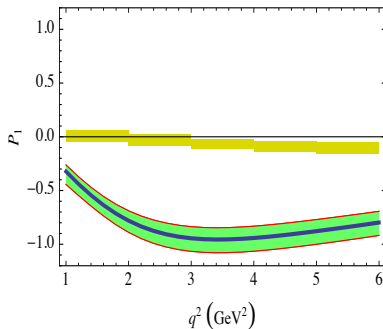


- We find excellent agreement between our determination of $T_{1,2}$ using $R_{1,2}$ and lattice data.
- This serves as a test of validity of the extrapolation of KMPW for $V(q^2)$ and $A_1(q^2)$.
- T_3 only in $A_0^{L,R}$ and multiplied by $\lambda(q^2)$ such that vanishes at the no-recoil endpoint $\rightarrow T_3$ plays only a marginal role.

The benefit of using clean observables: The case of S_3 vs P_1

The choice at large-recoil of FF (KMPW or BZ) has a marginal impact on clean observables, but an important one (in presence of NP) for LO-FF dependent observables (like S_3).

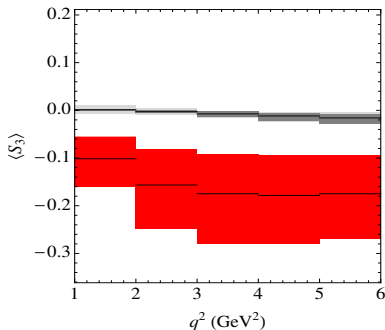
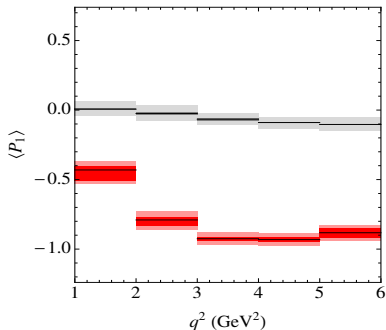
- The SM prediction for P_1 is insensitive to the choice of form factors. Also S_3 is insensitive due to the fact that $S_3 \sim 0$.
- The NP predictions for P_1 is insensitive to the choice of form factors. S_3 is very sensitive and the hadronic form factors x3, reducing the ability of S_3 to disentangle among different NP curves. FF code: **BZ**, **KMPW**:



The benefit of using clean observables: The case of S_3 vs P_1

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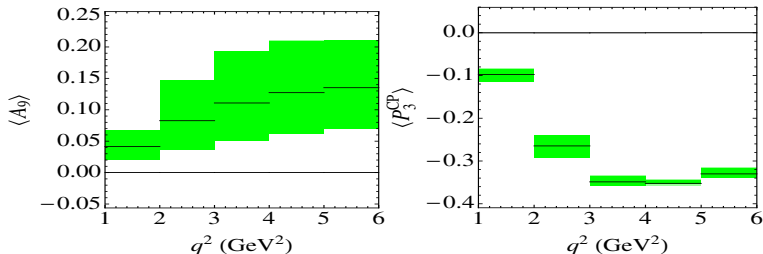
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Similar conclusion arises in CP violating observables. Let's focus on J_9 in the **large-recoil region**. We can construct:

$$A_9 = \frac{[J_i - \bar{J}_i]}{d\Gamma/dq^2 + d\bar{\Gamma}/dq^2} \quad P_3^{\text{CP}} = -\frac{1}{4} \frac{[J_9 - \bar{J}_9]}{[J_{2s} + \bar{J}_{2s}]}$$

where P_3^{CP} is clean and A_9 is sensitive to FF at LO. Take a point of NP $\delta C'_{10} = -1.5 + 2i$ and compute the binned observables with KMPW.

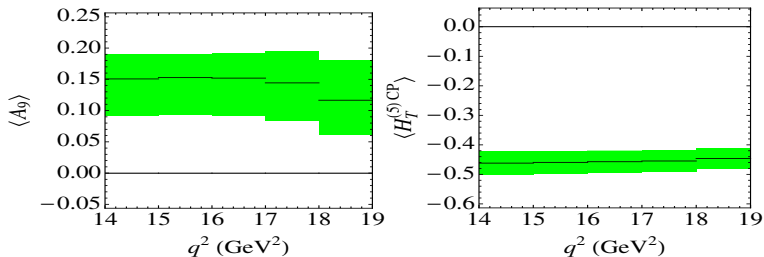


The difference in sensitivity to NP for the same point of NP is self-evident in favor of P_3^{CP}

Similar conclusion arises in CP violating observables. Let's focus on J_9 in the **low-recoil region**. We can construct:

$$A_9 = \frac{[J_i - \bar{J}_i]}{d\Gamma/dq^2 + d\bar{\Gamma}/dq^2} \quad H_T^{(5)\text{CP}} = -\frac{[J_9 - \bar{J}_9]}{\sqrt{4([J_{2s} + \bar{J}_{2s}]^2 - ([J_3 + \bar{J}_3])^2)}}$$

where P_3^{CP} is clean and A_9 is sensitive to FF at LO. Take a point of NP $\delta C'_{10} = -1.5 + 2i$ and compute the binned observables with KMPW.



In conclusion P_3^{CP} and $H_T^{(5)\text{CP}}$ are much more sensitive to NP than A_9 due to their reduced hadronic uncertainties.

Integrated observables

Contact theory and experiment:

Indeed the observables are measured in bins.

Present bins: [0.1,2], [2,4.3], [4.3,8.68], [1,6], [14.18,16], [16,19] GeV^2 .

Comments on the bins:

- Ultralow bin region [0.1,1] including light-resonances analyzed in [S. Jager, JM Camalich]'12. Binning tends to wash out the resonances.
- The region $q^2 \sim 6 - 8.68 \text{ GeV}^2$ can be affected by charm-loop effects. [Khodjamirian, Mannel, Pivovarov, Wang'10]
- The middle bin [10.09, 12.89] GeV^2 between J/ψ and $\psi(2s)$. Charm-loop effects lead to a destructive interference (raw estimate). We treat it as a simple interpolation.
- Suggestion to experimentalists on binning: [1,2], [2,4.3], [4.3,6]

Integrated observables

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This requires a **redefinition** of observables in **bins**:

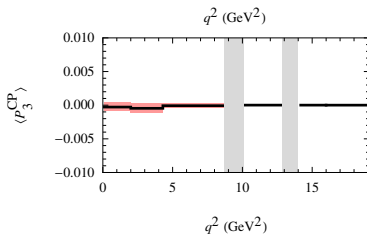
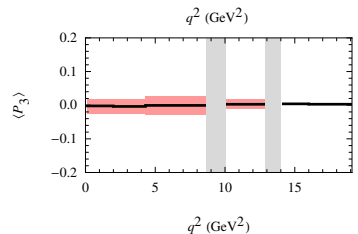
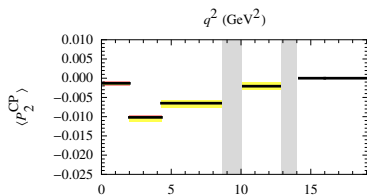
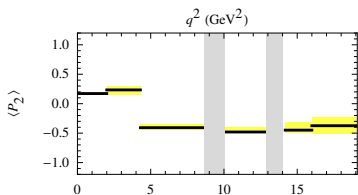
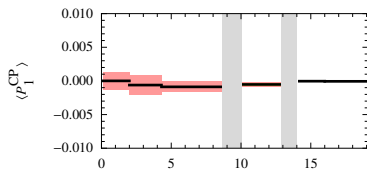
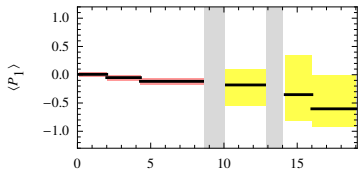
$$\begin{aligned}\langle A_T^{(2)} \rangle_{\text{bin}} &\equiv \langle P_1 \rangle_{\text{bin}} = \frac{\int_{\text{bin}} dq^2 [J_3 + \bar{J}_3]}{2 \int_{\text{bin}} dq^2 [J_{2s} + \bar{J}_{2s}]} = \frac{\int_{\text{bin}} dq^2 F_T \mathbf{P}_1 \frac{d\Gamma + \bar{d}\Gamma}{dq^2}}{\int_{\text{bin}} dq^2 F_T \frac{d\Gamma + \bar{d}\Gamma}{dq^2}}, \\ \langle P_2 \rangle_{\text{bin}} &= \frac{\int_{\text{bin}} dq^2 [J_{6s} + \bar{J}_{6s}]}{8 \int_{\text{bin}} dq^2 [J_{2s} + \bar{J}_{2s}]} = \frac{\int_{\text{bin}} dq^2 F_T \mathbf{P}_2 \frac{d\Gamma + \bar{d}\Gamma}{dq^2}}{\int_{\text{bin}} dq^2 F_T \frac{d\Gamma + \bar{d}\Gamma}{dq^2}}, \\ \langle P_3 \rangle_{\text{bin}} &= -\frac{\int_{\text{bin}} dq^2 [J_9 + \bar{J}_9]}{4 \int_{\text{bin}} dq^2 [J_{2s} + \bar{J}_{2s}]} = \frac{\int_{\text{bin}} dq^2 F_T \mathbf{P}_3 \frac{d\Gamma + \bar{d}\Gamma}{dq^2}}{\int_{\text{bin}} dq^2 F_T \frac{d\Gamma + \bar{d}\Gamma}{dq^2}}.\end{aligned}$$

where β_ℓ^2 is included in F_T . Similar definitions for $\langle P_i^{CP} \rangle_{\text{bin}}$ with $J_i - \bar{J}_i$.

They are indirectly measured via S_3, A_{im}, A_{FB}, F_L

(and already provide constraints).

BUT it is urgent to get direct experimental measurements of $P_{1,2,3}$ (preliminary results on $P_{1,2}$ last week)



The integrated version of observables $P'_{4,5,6}$ are defined by

$$\begin{aligned} \langle P'_4 \rangle_{\text{bin}} &= \frac{1}{\mathcal{N}'_{\text{bin}}} \int_{\text{bin}} dq^2 [J_4 + \bar{J}_4], & \langle P'^{CP}_4 \rangle_{\text{bin}} &= \frac{1}{\mathcal{N}'_{\text{bin}}} \int_{\text{bin}} dq^2 [J_4 - \bar{J}_4], \\ \langle P'_5 \rangle_{\text{bin}} &= \frac{1}{2\mathcal{N}'_{\text{bin}}} \int_{\text{bin}} dq^2 [J_5 + \bar{J}_5], & \langle P'^{CP}_5 \rangle_{\text{bin}} &= \frac{1}{2\mathcal{N}'_{\text{bin}}} \int_{\text{bin}} dq^2 [J_5 - \bar{J}_5], \\ \langle P'_6 \rangle_{\text{bin}} &= \frac{-1}{2\mathcal{N}'_{\text{bin}}} \int_{\text{bin}} dq^2 [J_7 + \bar{J}_7], & \langle P'^{CP}_6 \rangle_{\text{bin}} &= \frac{-1}{2\mathcal{N}'_{\text{bin}}} \int_{\text{bin}} dq^2 [J_7 - \bar{J}_7], \end{aligned}$$

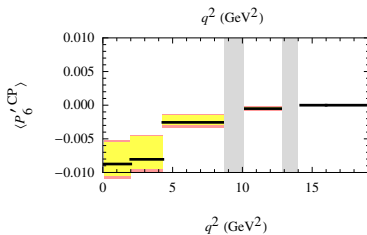
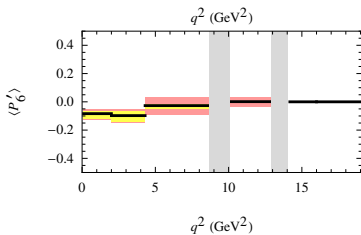
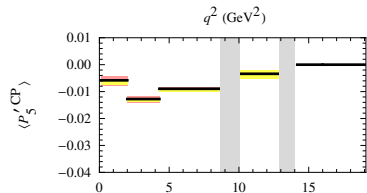
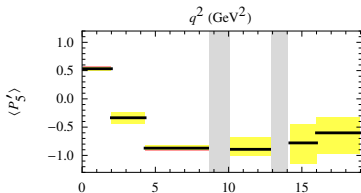
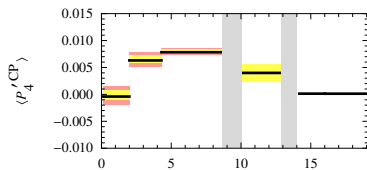
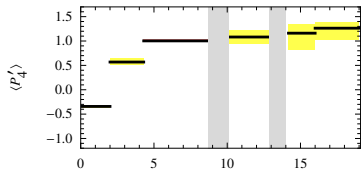
where the normalization $\mathcal{N}'_{\text{bin}}$ is defined as

$$\mathcal{N}'_{\text{bin}} = \sqrt{- \int_{\text{bin}} dq^2 [J_{2s} + \bar{J}_{2s}] \int_{\text{bin}} dq^2 [J_{2c} + \bar{J}_{2c}]}.$$

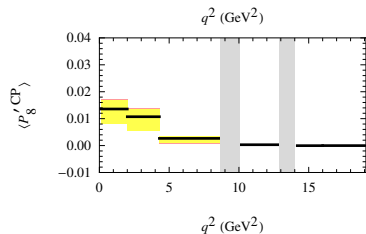
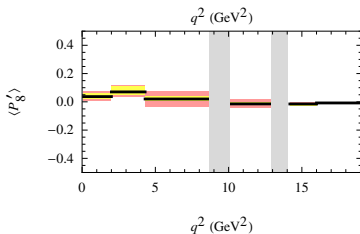
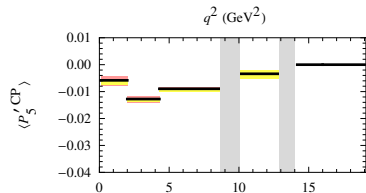
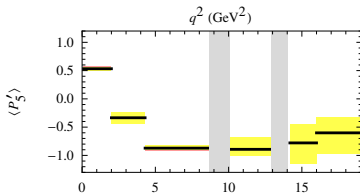
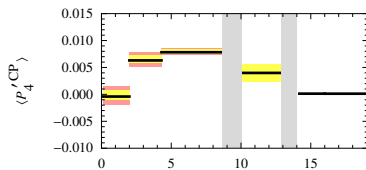
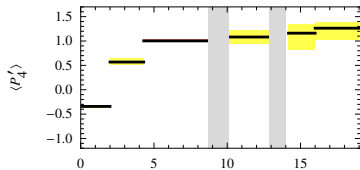
- They are **not yet measured** but the **double-folded distributions** give access to these observables.
- There is also a **redundant** clean observable $P'_8 = Q'$ (if there are no scalars) associated to J_8 that can be introduced for practical reasons:

$$\langle P'_8 = Q' \rangle_{\text{bin}} = \frac{-1}{\mathcal{N}'_{\text{bin}}} \int_{\text{bin}} dq^2 [J_8 + \bar{J}_8], \quad \langle P'^{CP}_8 \rangle_{\text{bin}} = \frac{-1}{\mathcal{N}'_{\text{bin}}} \int_{\text{bin}} dq^2 [J_8 - \bar{J}_8].$$

Notice that $Q' = f(P_i)$ **but** $\langle Q' \rangle_{\text{bin}} \neq f(\langle P_i \rangle_{\text{bin}})$.



Binned SM predictions for $\langle P'_{4,5,8} \rangle$ and $\langle P'^{(CP)}_{4,5,8} \rangle$ [arXiv:1303.5794](https://arxiv.org/abs/1303.5794)



[S. Descotes, T. Hurth, JM, J. Virto'13], [J.M'12]

- Another possible source of uncertainty is the **S-wave contribution** coming from $B \rightarrow K_0^* l^+ l^-$ decay. [Becirevic, Tayduganov '13], [Blake et al.'13]
- We will assume that both P and S waves are described by q^2 -dependent FF times a Breit-Wigner function.
- The **distinct** angular dependence of the S-wave terms in **folded** distributions allow to disentangle the signal of the P-wave from the S-wave: $P_i^{(\prime)}$ can be **disentangled** from S-wave pollution [JM'12].

Problem: Changing the normalization used for the distribution from

$$\frac{d\Gamma_K^*}{dq^2} \equiv \Gamma'_{K^*} \rightarrow \Gamma'_{full}$$

introduces a $(1 - \mathbf{F}_S)$ in front of the P-wave.

$$\Gamma'_{full} = \Gamma'_{K^*} + \Gamma'_S$$

and the longitudinal polarization fraction associated to Γ'_S is

$$\mathbf{F}_S = \frac{\Gamma'_S}{\Gamma'_{full}} \quad \text{and} \quad 1 - \mathbf{F}_S = \frac{\Gamma'_{K^*}}{\Gamma'_{full}}$$

The modified distribution including the **S-wave** and new normalization Γ'_{full} :

$$\begin{aligned} \frac{1}{\Gamma'_{full}} \frac{d^4\Gamma}{dq^2 d\cos\theta_K d\cos\theta_l d\phi} &= \frac{9}{32\pi} \left[\frac{3}{4} \mathbf{F}_T \sin^2\theta_K + \mathbf{F}_L \cos^2\theta_K \right. \\ &+ \left(\frac{1}{4} \mathbf{F}_T \sin^2\theta_K - \mathbf{F}_L \cos^2\theta_K \right) \cos 2\theta_l + \frac{1}{2} \mathbf{P}_1 \mathbf{F}_T \sin^2\theta_K \sin^2\theta_l \cos 2\phi \\ &+ \sqrt{\mathbf{F}_T \mathbf{F}_L} \left(\frac{1}{2} \mathbf{P}'_4 \sin 2\theta_K \sin 2\theta_l \cos \phi + \mathbf{P}'_5 \sin 2\theta_K \sin \theta_l \cos \phi \right) \\ &- \sqrt{\mathbf{F}_T \mathbf{F}_L} \left(\mathbf{P}'_6 \sin 2\theta_K \sin \theta_l \sin \phi - \frac{1}{2} \mathbf{Q}' \sin 2\theta_K \sin 2\theta_l \sin \phi \right) \\ &\left. + 2\mathbf{P}_2 \mathbf{F}_T \sin^2\theta_K \cos\theta_l - \mathbf{P}_3 \mathbf{F}_T \sin^2\theta_K \sin^2\theta_l \sin 2\phi \right] (1 - \mathbf{F}_S) + \frac{1}{\Gamma'_{full}} \mathbf{W}_S \end{aligned}$$

in the massless case and where the polluting terms are

$$\begin{aligned} \frac{\mathbf{W}_S}{\Gamma'_{full}} &= \frac{3}{16\pi} \left[\mathbf{F}_S \sin^2\theta_\ell + \mathbf{A}_S \sin^2\theta_\ell \cos\theta_K + \mathbf{A}_S^4 \sin\theta_K \sin 2\theta_\ell \cos\phi \right. \\ &\left. + \mathbf{A}_S^5 \sin\theta_K \sin\theta_\ell \cos\phi + \mathbf{A}_S^7 \sin\theta_K \sin\theta_\ell \sin\phi + \mathbf{A}_S^8 \sin\theta_K \sin 2\theta_\ell \sin\phi \right] \end{aligned}$$

We can get **bounds** on the size of the S-wave polluting terms.
 Let's take for instance A_S

$$A_S = 2\sqrt{3} \frac{1}{\Gamma'_{full}} \int \text{Re} \left[(A_0^L A_0^{L*} + A_0^R A_0^{R*}) BW_{K_0^*}(m_{K\pi}^2) BW_{K^*}^\dagger(m_{K\pi}^2) \right] dm_{K\pi}^2$$

where

$$F_S = \frac{8}{3} \frac{\tilde{j}_{1a}^c}{\Gamma'_{full}} = \frac{|A_0^L|^2 + |A_0^R|^2}{\Gamma'_{full}} \mathbf{Y} \quad \mathbf{Y} = \int dm_{K\pi}^2 |BW_{K_0^*}(m_{K\pi}^2)|^2$$

\mathbf{Y} factor included to take into account the width of scalar resonance K_0^*

A bound is obtained once we define the $S - P$ interference integral

$$\mathbf{Z} = \int \left| BW_{K_0^*}(m_{K\pi}^2) BW_{K^*}^\dagger(m_{K\pi}^2) \right| dm_{K\pi}^2$$

and use the bound from the Cauchy-Schwartz inequality

$$\begin{aligned} & \left| \int (\text{Re}, \text{Im}) \left[(A_0^L A_j^{L*} \pm A_0^R A_j^{R*}) BW_{K_0^*}(m_{K\pi}^2) BW_{K^*}^\dagger(m_{K\pi}^2) \right] dm_{K\pi}^2 \right| \\ & \leq \mathbf{Z} \times \sqrt{[|A_0^L|^2 + |A_0^R|^2][|A_j^L|^2 + |A_j^R|^2]} \end{aligned}$$

From the definitions of F_S and F_L and P_1 one gets the following bound:

$$|A_S| \leq 2\sqrt{3}\sqrt{F_S(1-F_S)F_L} \frac{Z}{\sqrt{XY}}$$

the factor $(1 - F_S)$ in the bound arises due to the fact that F_L is defined with respect to Γ'_{K^*} rather than Γ'_{full} .

$$|A_S^4| \leq \sqrt{\frac{3}{2}} \sqrt{F_S(1-F_S)(1-F_L) \left(\frac{1-P_1}{2}\right)} \frac{Z}{\sqrt{XY}}$$

$$|A_S^5| \leq 2\sqrt{\frac{3}{2}} \sqrt{F_S(1-F_S)(1-F_L) \left(\frac{1+P_1}{2}\right)} \frac{Z}{\sqrt{XY}}$$

$$|A_S^7| \leq 2\sqrt{\frac{3}{2}} \sqrt{F_S(1-F_S)(1-F_L) \left(\frac{1-P_1}{2}\right)} \frac{Z}{\sqrt{XY}}$$

$$|A_S^8| \leq \sqrt{\frac{3}{2}} \sqrt{F_S(1-F_S)(1-F_L) \left(\frac{1+P_1}{2}\right)} \frac{Z}{\sqrt{XY}}$$

Coefficient	Large recoil ∞ Range	Low recoil ∞ Range	Large Recoil Finite Range	Low Recoil Finite Range
$ A_S $	0.33	0.25	0.67	0.49
$ A_S^4 $	0.05	0.10	0.11	0.19
$ A_S^5 $	0.11	0.11	0.22	0.23
$ A_S^7 $	0.11	0.19	0.22	0.38
$ A_S^8 $	0.05	0.06	0.11	0.11

Table : Illustrative values of the size of the bounds for the choices of F_S, F_L, P_1 and $\mathbf{F} = \mathbf{Z}/\sqrt{\mathbf{XY}}$

- **Large-recoil:** $F_S \sim 7\%$ (like $B^0 \rightarrow J/\psi K^+ \pi^-$), $F_L \sim 0.7$ and $P_1 \sim 0$
- **Low-recoil:** $F_S \sim 7\%$, $F_L \sim 0.38$ and $P_1 \sim -0.48$.

We take the maximal value for Z/\sqrt{XY} factor in two cases:

“infinite range” \rightarrow integrals in the whole $m_{K\pi}$ range

“finite range” \rightarrow integrals around $m_{K^*} \pm 0.1$ GeV.

This may help in estimating the **systematics** associated to S-wave.

All these analyses have a clear goal: To get tight constraints on the WC and/or discover NP.

Discussion on constraints on WC from radiative and leptonic B decays should be addressed in a given framework, specific scenarios & observables

S. Descotes, D. Ghosh, JM., M. Ramon, '11

- **Framework:** NP in C_7, C_9, C_{10} and $C_{7'}, C_{9'}, C_{10'}$ [chirally-flipped operators $\gamma_5 \rightarrow -\gamma_5$] as a real shift in the Wilson coefficients
- **Scenarios** (depending on the specific model)
 - A : NP in 7,7' only
 - B : NP in 7,7', 9,10 only
 - B' : NP in 7,7', 9',10' only
 - C : NP in 7,7',9,10,9',10' only
- **Classes within a Framework**
 - I: observables sensitive only to 7,7'
 - II: observables sensitive only to 7,7',9,9',10,10'
 - III: observables sensitive to 7,7',9,9',10,10' and more (scalars...)

Other model-independent analysis:

Bobeth, Hiller, van Dyk 1105.0376

Altmannshofer, Paradisi, Straub 1111.1257

Bobeth, Hiller, van Dyk, Wacker 1111.2558

Beaujean, Bobeth, van Dyk, Wacker 1205.1838

Altmannshofer, Straub 1206.0273

Becirevic, Kou, Le Yaouanc, Tayduganov 1206.1502

....

Also specific model analysis:

M. Blanke, B. Shakya, P. Tanedo, Y. Tsai, 1203.6650

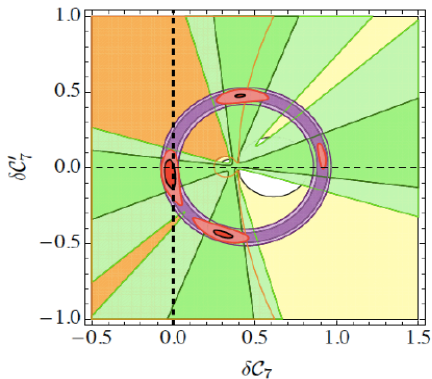
F. Mahmoudi, S. Neshatpour and J. Orloff, 1205.1845

Nejc Kosnik, 1206.2970

T. Hurth and F. Mahmoudi, 1207.0688

....

$\delta C_7 - \delta C_{7'}$ plane : constraints at 68.3% and 95.5% C.L.



S. Descotes, JM., J. Virto, M. Ramon '12

Class I observables (only $O_{7,7'}$)

dark 68.3%, light 95.5% CL

- A_l (yellow)
- $B(B \rightarrow X_s \gamma)$ (purple)
- $S_{K^* \gamma}$ (green)

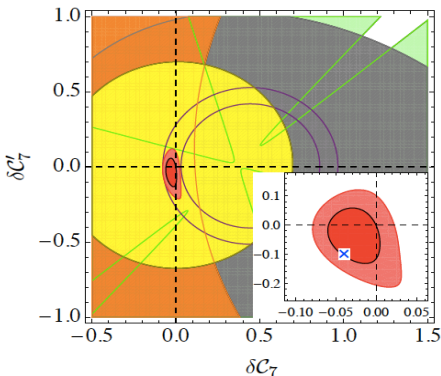
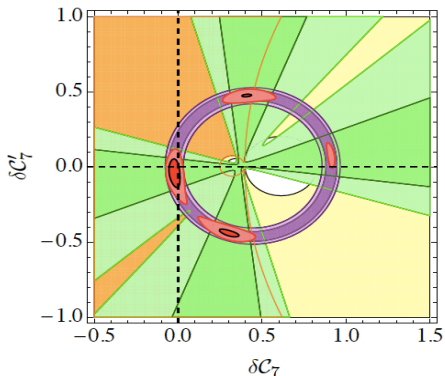
Overlap regions (red dark and light)

- Region around SM favoured: solid black contour red dark $(\delta C_7, \delta C_{7'}) \sim (0, 0)$.
- three non-SM solutions also allowed $(\delta C_7, \delta C_{7'}) \simeq (-C_7^{SM}, \pm 0.4), (0.9, 0)$

- A_l disfavors at 68.3% CL changed-sign solution $(C_7, C_{7'}) = (C_7^{SM} + 0.9, 0)$

\implies Same conclusion as [\[Gambino, Haisch, Misiak\]](#), without using Class-III $B \rightarrow X_s \ell^+ \ell^-$. Constraints independent of other WCs.

Scenario A ($C_{7,7'}$) : class I and class-III observables



⇒ class-III observables ($\langle A_{FB} \rangle_{[1,6]}$, $\langle F_L \rangle_{[1,6]}$, $BR(B \rightarrow X_s l^+ l^-)$) constrain further the shifts $\delta C_7, \delta C_{7'}$ (if all other NP WC to zero))

- $BR(B \rightarrow X_s \mu^+ \mu^-)$ favours SM-like region and two non-SM regions.
- $\langle A_{FB} \rangle_{[1,6]}$ selects SM region and one non-SM region. $\langle F_L \rangle_{[1,6]}$ does not discriminate any region.
- All combined observables disfavour changed sign solution at more than 95.5 % CL

What the $P_{1,2,3}, P'_{4,5,6}$ can do for you? Future Prospects

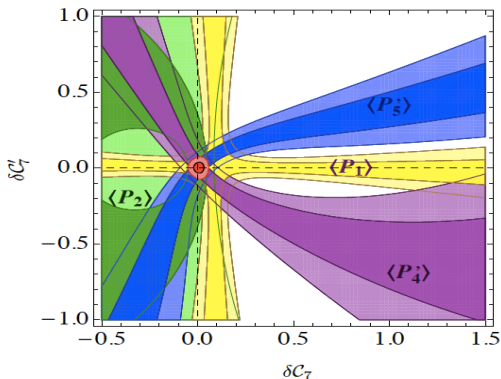


Figure : Individual constraints in the $\delta\mathcal{C}_7 - \delta\mathcal{C}'_7$ plane from hypothetical measurements of the observables $\langle P_1 \rangle_{[2,4,3]}$, $\langle P_2 \rangle_{[2,4,3]}$, $\langle P'_4 \rangle_{[2,4,3]}$ and $\langle P'_5 \rangle_{[2,4,3]}$, corresponding to central values equal to the SM predictions and an experimental uncertainty $\sigma_{exp} = 0.10$. The combined 68.3% (dark red) and 95.5% (light red) C.L. regions are also shown.

- We have presented an optimal basis of CP-conserving and CP-violating observables and computed their SM predictions in both large and low recoil regions:

$$\left\{ \frac{d\Gamma}{dq^2}, \mathbf{A}_{\text{FB}} \text{ or } \mathbf{F}_L, \mathbf{P}_1, \mathbf{P}_2, \mathbf{P}_3, \mathbf{P}'_4, \mathbf{P}'_5, \mathbf{P}'_6 \right\}$$

and the corresponding **CP-violating basis**:

$$\left\{ \mathbf{A}_{\text{CP}}, \mathbf{A}_{\text{FB}}^{\text{CP}} \text{ or } \mathbf{F}_L^{\text{CP}}, \mathbf{P}_1^{\text{CP}}, \mathbf{P}_2^{\text{CP}}, \mathbf{P}_3^{\text{CP}}, \mathbf{P}'_4{}^{\text{CP}}, \mathbf{P}'_5{}^{\text{CP}}, \mathbf{P}'_6{}^{\text{CP}} \right\}$$

where one can add also the massive $M_{1,2}$. They can be measured using folded distributions. **It is important to get them all measured!!**.

- We have discussed and show explicitly the benefits of using clean observables to disentangle possible NP (both for CP conserving and violating observables).
- We provide first bounds on the S-wave polluting terms coming from the interference between S and P waves originating from the companion decay $B \rightarrow K_0^* \mu^+ \mu^-$ important to evaluate the systematic errors.
- $P_{1,2,3}, P'_{4,5,6}$ can produce the strongest constraints on WC \rightarrow slice parameters space of models or signal New Physics in a clear way.

BACK-UP SLIDES

General Considerations for the Construction of Clean Observables

- J_i contain short distance Wilson coefficients ($C_{7,9,10}^{(\prime)}$) and long distances quantities (FF in particular).
- Effective Theories (QCDF/SCET or HQET) allow to relate FF and reduce inputs. Extra precision at low- q^2 including hard-gluon corrections.

*Construction of clean observables based on
cancellation of FF at LO in the relevant ET.*

$$A_{\perp}^{L,R} = \mathcal{N}_{\perp} \left[C_{9\mp 10}^+ \mathbf{V}(\mathbf{q}^2) + C_7^+ \mathbf{T}_1(\mathbf{q}^2) \right] + \mathcal{O}(\alpha_s, \Lambda/m_b \dots)$$

$$A_{\parallel}^{L,R} = \mathcal{N}_{\parallel} \left[C_{9\mp 10}^- \mathbf{A}_1(\mathbf{q}^2) + C_7^- \mathbf{T}_2(\mathbf{q}^2) \right] + \mathcal{O}(\alpha_s, \Lambda/m_b \dots)$$

$$A_0^{L,R} = \mathcal{N}_0 \left[C_{9\mp 10}^- \mathbf{A}_{12}(\mathbf{q}^2) + C_7^- \mathbf{T}_{23}(\mathbf{q}^2) \right] + \mathcal{O}(\alpha_s, \Lambda/m_b \dots)$$

where $C_{7,9\mp 10}^{\pm}$ contain the WC and $\mathbf{A}_{12} = f(A_1, A_2)$, $\mathbf{T}_{23} = f(T_2, T_3)$.

The key observation is that the ratios

$$\mathbf{R}_1 = \mathbf{T}_1/\mathbf{V} \quad \mathbf{R}_2 = \mathbf{T}_2/\mathbf{A}_1 \quad \tilde{\mathbf{R}}_3 = \mathbf{T}_{23}/\mathbf{A}_{12}$$

have well-defined limiting values in both regimes

$$\mathbf{R}_{1,2} = 1 + \text{corrections} \quad , \quad \tilde{\mathbf{R}}_3 = \frac{q^2}{m_B^2} + \text{corrections} \quad .$$

Using these ratios to eliminate T_1, T_2, T_{23} the transversity amplitudes turns out

$$A_{\perp}^{L,R} = X_{\perp}^{L,R}(C_i, R_1) \mathbf{V}(q^2) + \mathcal{O}(\alpha_s, \Lambda/m_b \dots)$$

$$A_{\parallel}^{L,R} = X_{\parallel}^{L,R}(C_i, R_2) \mathbf{A}_1(q^2) + \mathcal{O}(\alpha_s, \Lambda/m_b \dots)$$

$$A_0^{L,R} = X_0^{L,R}(C_i, \tilde{R}_3) \mathbf{A}_{12}(q^2) + \mathcal{O}(\alpha_s, \Lambda/m_b \dots)$$

Two consequences (case massless) from structure of J_i + symmetries:

- Low-recoil: 5 observables canceling FF at LO, 3 not canceling FF.
- Large-recoil: one extra relation

$$2E_{K^*} m_B \mathbf{V}(q^2) = (m_B + m_{K^*})^2 \mathbf{A}_1(q^2) + \mathcal{O}(\alpha_s, \Lambda/m_b \dots)$$

Additional clean observables at large recoil can be constructed (i.e., $P_1 = A_T^2$) not clean at low-recoil.

All observables that are clean at low-recoil are clean at large-recoil.

Limited sensitivity to hadronic inputs, or strong impact on analysis

- Class-I

- $\mathcal{B}(B \rightarrow X_s \gamma)$ with $E_\gamma > 1.6 \text{ GeV}$ [Misiak, Steinhauser, Haisch]
- exclusive time-dependent CP asymmetry $S_{K^* \gamma}$
- isospin asymmetry $A_I(B \rightarrow K^* \gamma)$ [Beneke, Feldman, Seidel]
[Kagan, Neubert, Feldman, J.M.]

- Class-II

- Integrated transverse asymmetries $\tilde{A}_T^2 = P_1, P_2$ and P_3 in $B \rightarrow K^* l^+ l^-$ over low- q^2 region in bins. [Kruger and J.M.]

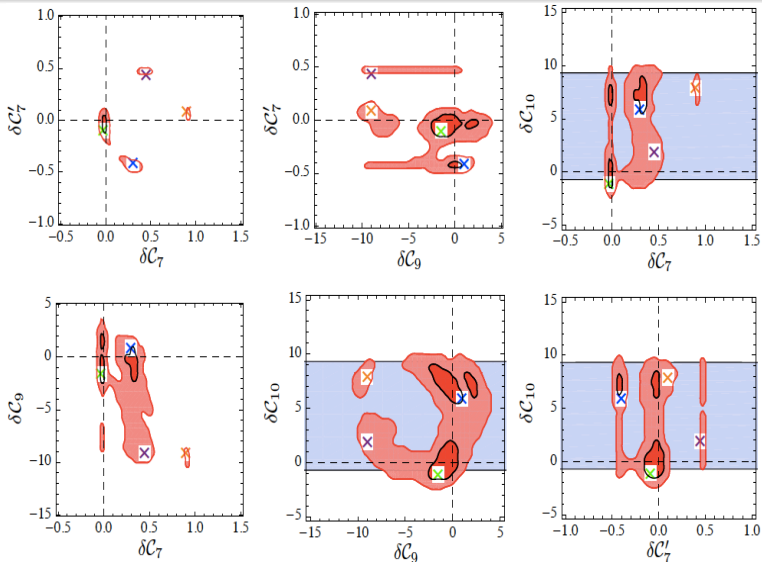
- Class-III

- $\mathcal{B}(B \rightarrow X_s l^+ l^-)$ [Bobeth et al., Huber, Lunghi et al.]
- Integrated \tilde{F}_L and \tilde{A}_{FB} in $B \rightarrow K^* l^+ l^-$ [1-6 GeV²]

Simple numerical parametrisation as $\delta C_i = C_i(\mu_b) - C_i^{SM}(\mu_b)$

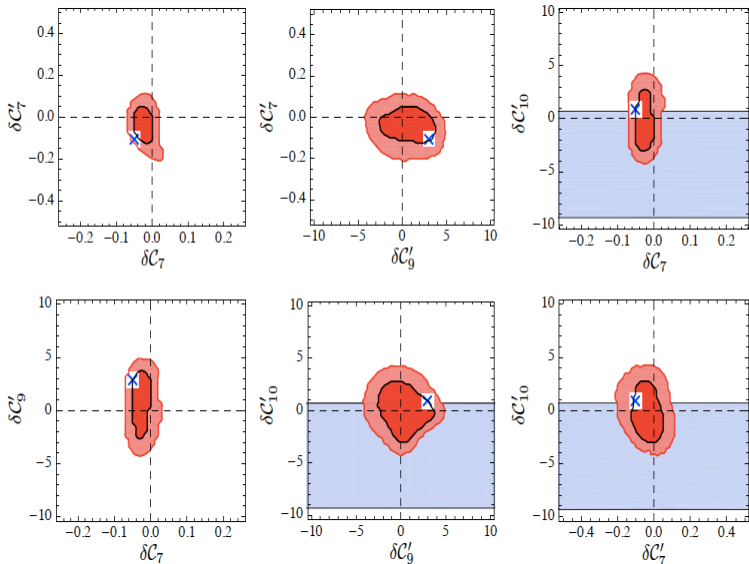
We provide the numerical expressions for the integrated observables $\langle A_{FB} \rangle, \langle F_L \rangle, \langle P_{1,2,3} \rangle$ and $\langle P_{4',5',6'} \rangle$ as a function of the NP Wilson coefficients, for different choices of the q^2 -binning. S. Descotes, J.M., J. Virto, M. Ramon '12

Scenario B ($C_{7,7',9,10}$) with all constraints



Four islands in the space of Wilson Coefficients ("four benchmark points" projected in all planes). Blue band is $BR(B_s \rightarrow \mu^+ \mu^-)$ constraint.

Scenario B' ($C_{7,7',9',10'}$) with all constraints



One island in the space of WCs. Blue band is $BR(B_s \rightarrow \mu^+ \mu^-)$ constraint. Changed-sign solution for C_7 reduce its statistical significance.

Scenario C ($C_{7,7',9,10,9',10'}$) with all constraints

