

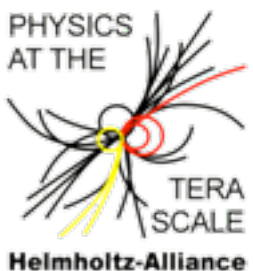


LHC top pair cross section combination

ATLAS-CONF-2012-134

CMS PAS TOP-12-003

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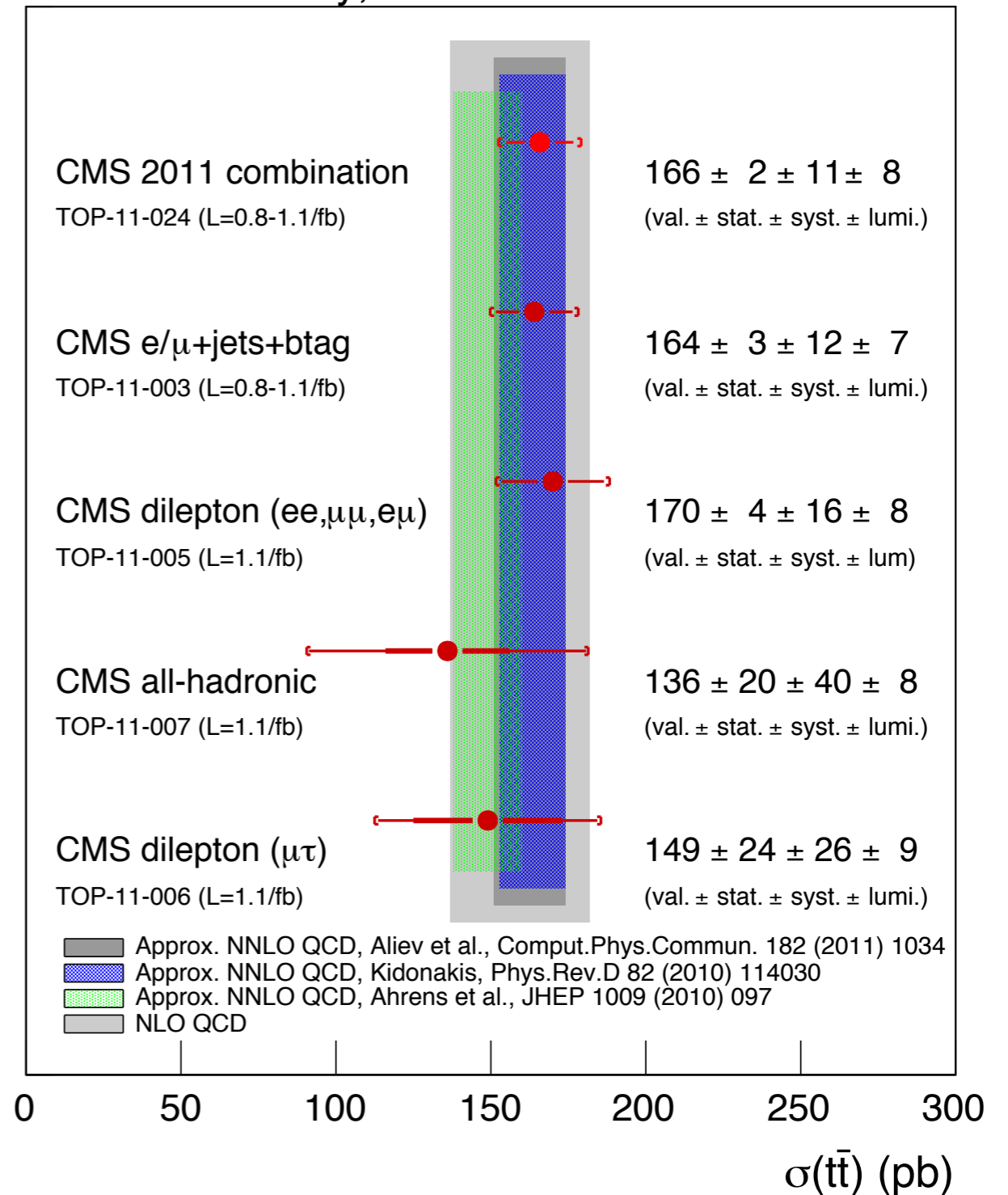


- Goal: combine CMS and ATLAS top pair cross section measurements
- What is included in the combination?
- Combination strategy and method
 - ▶ BLUE vs full likelihood
- Breakdown of systematic uncertainties
 - ▶ correlations of systematic uncertainties
- New measurements and future combination

- up to 1.1/fb
- 4 channels
- relative uncertainty 8%
- dominated by l+jets - 8.6% uncertainty

$$\sigma = 166 \pm 2(\text{stat}) \pm 11(\text{syst}) \pm 8(\text{lumi})$$

CMS Preliminary, $\sqrt{s}=7$ TeV

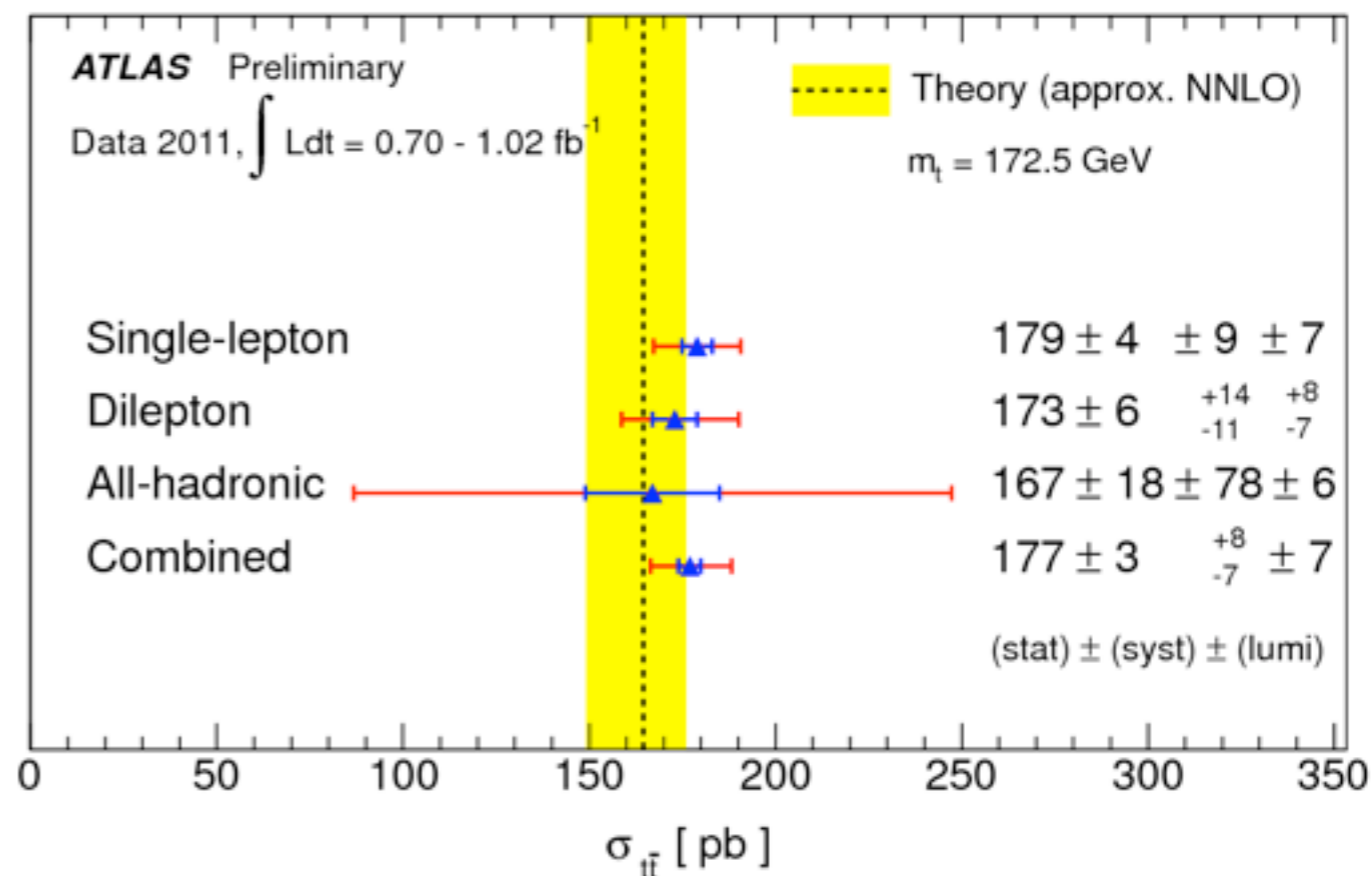


CMS-PAS-TOP-11-024

- Techniques in individual channels
 - ▶ l+jets: binned profile likelihood fit
 - ▶ dilepton and $\mu+\tau$: cut and count
 - ▶ all hadronic: unbinned maximum likelihood fit to reconstructed m_{top}
- Combination: fitter used in l+jets extended to include other channels
 - ▶ channels using counting methods are modeled by histograms with one bin
 - ▶ results of unbinned LH fit are parameterized to be represented as a single bin in combined likelihood
 - ▶ not straightforward to extend to include ATLAS measurements
- **B**est **L**inear **U**nbiased **E**stimate method used as a cross check
 - ▶ results agree very well
 - ▶ central value differs by 0.7%
 - ▶ relative uncertainty is the same

ATLAS-CONF-2012-024

- up to 1.1/fb
- 3 final channels
 - ▶ 4th channel was available (l+tau) but not included into combination due to overlap with l+jets
- relative uncertainty - 6.2%
- dominated by l+jets - 6.7%



$$\sigma = 177 \pm 3 \text{ (stat)} \begin{matrix} +8 \\ -7 \end{matrix} \text{ (syst)} \pm 7 \text{ (lumi)}$$

- 6 channel combination is implemented as a product of individual likelihoods
 - ▶ approximation for the LH of l+jets channel

$$L_{\text{comb}}(\sigma_{t\bar{t}}, \mathcal{L}, \vec{\alpha}) = L_{l+\text{jets}}(\sigma_{t\bar{t}}, \mathcal{L}, \vec{\alpha}) \prod_{i \in \{ee, \mu\mu, e\mu\}} \text{Pois}(N_i^{\text{obs}} | N_{i,\text{tot}}^{\text{exp}}(\vec{\alpha})) \\ \times \prod_{k \in \text{all-had bins}} \text{Pois}(n_k | s_k(\vec{\alpha}) + b_k(\vec{\alpha})) \prod_{j \notin l+\text{jets sys}} \text{Gaus}(0 | \alpha_j, 1).$$

- 89 parameters total
- 26 shared between l+jets and dilepton LH
- 12 common to all three channels

BLUE combination

- much simpler
- more approximations
 - symmetrized uncertainties
- excellent agreement with LH

$$\sigma = 177.4^{+11.1}_{-10.2} \text{ (total)}$$

$$\sigma = 177.7 \pm 11.4 \text{ (total)}$$

- Performing combination of all individual channels from two experiments using likelihood technique is very complicated
- **BLUE = Best Linear Unbiased Estimate**
 - L.Lyons, D.Gibaut, P.Clifford, NIM A270 (1988), A.Valassi, NIM A500 (2003)
 - ▶ calculates linear weighted sum of individual results with weights determined such that they minimize the total uncertainty on the combined result
 - ▶ takes into account statistical and systematic uncertainties and their correlations
- **Advantages**
 - ▶ allows combination of correlated measurements of one or more parameters
 - ▶ produces a fit χ^2 to evaluate consistency of inputs
 - ▶ fast and simple
 - ▶ well established technique used recently for the LHC top quark mass combination

- Split in categories according to
 - ▶ physics origin
 - ▶ correlation between experiments
- Try to follow as close as possible
 - ▶ LHC top quark mass combination
 - ▶ ATLAS-CONF-2012-095
 - ▶ CMS PAS TOP-12-001

- Signal modelling uncertainties
- ATLAS
 - ▶ generator: MC@NLO vs Powheg (vs Alpgen for the recent results)
 - ▶ shower model: Powheg+Pythia vs Powheg+Herwig
 - ▶ ISR/FSR: ACER+Pythia with more/less radiation
 - ▶ PDF
- CMS
 - ▶ Q^2 variation in Madgraph
 - ▶ ME-PS matching
 - ▶ MC tune (for some analysis)
 - ▶ PDF

Mapping of uncertainties

Table 2: Mapping of the ATLAS and CMS systematic uncertainties

Category	ATLAS systematics	CMS systematics	correlation
Statistical			0
Detector simulation			0
	muon, electron identification jeteff, JER, MET btag-allHad trigger allHad	lepton efficiency, lepton selection pileup b-tagging trigger allHad τ fake, τ identification	
JES	JES	JES, bJES	0
Signal model			
MC	Generator	Generator, MC tune Jet and MET model, τ decay model	1
PS	Parton shower	ME-PS matching	1
Radiation	ISR/FSR	$t\bar{t}$ Q^2	1
PDF			1
	added for ATLAS	W branching	1
Background (data)			0
	QCD shape fake background multijet background Z pT model, DY normalization	QCD normalization DY normalization	
Background (MC)			1
	theoretical cross-sections W shape	cross sections of MC backgrounds W+jets Q^2	
Method	Monte Carlo statistics		
Luminosity			
	Bunch current Detector	Bunch current Detector	1 0

- keep separate components as in LHC top mass combination
- test sensitivity to correlation

Top mass uncertainty is not considered

	ATLAS	CMS	Correlation	LHC combination
Cross-section	177.0	165.8		173.3
Uncertainty				
Statistical	3.2	2.2	0	2.3
Jet Energy Scale	2.7	3.5	0	2.1
Detector model	5.3	8.8	0	4.6
Signal model				
Monte Carlo	4.2	1.1	1	3.1
Parton shower	1.3	2.2	1	1.6
Radiation	0.8	4.1	1	1.9
PDF	1.9	4.1	1	2.6
Background from data	1.5	3.4	0	1.6
Background from MC	1.6	1.6	1	1.6
Method	2.4	n/e	0	1.6
W leptonic branching ratio	1.0	1.0	1	1.0
Luminosity				
Bunch current	5.3	5.1	1	5.3
Luminosity measurement	4.3	5.9	0	3.4
Total systematic	10.8	14.2		9.8
Total	11.3	14.4		10.1

ATLAS: 60% of total
CMS: 54% of total

$\sigma = 173.3 \pm 2.3$ (stat) ± 9.8 (syst+lumi)
weights: 67% ATLAS, 33% CMS
probability - 47%, correlation - 30%

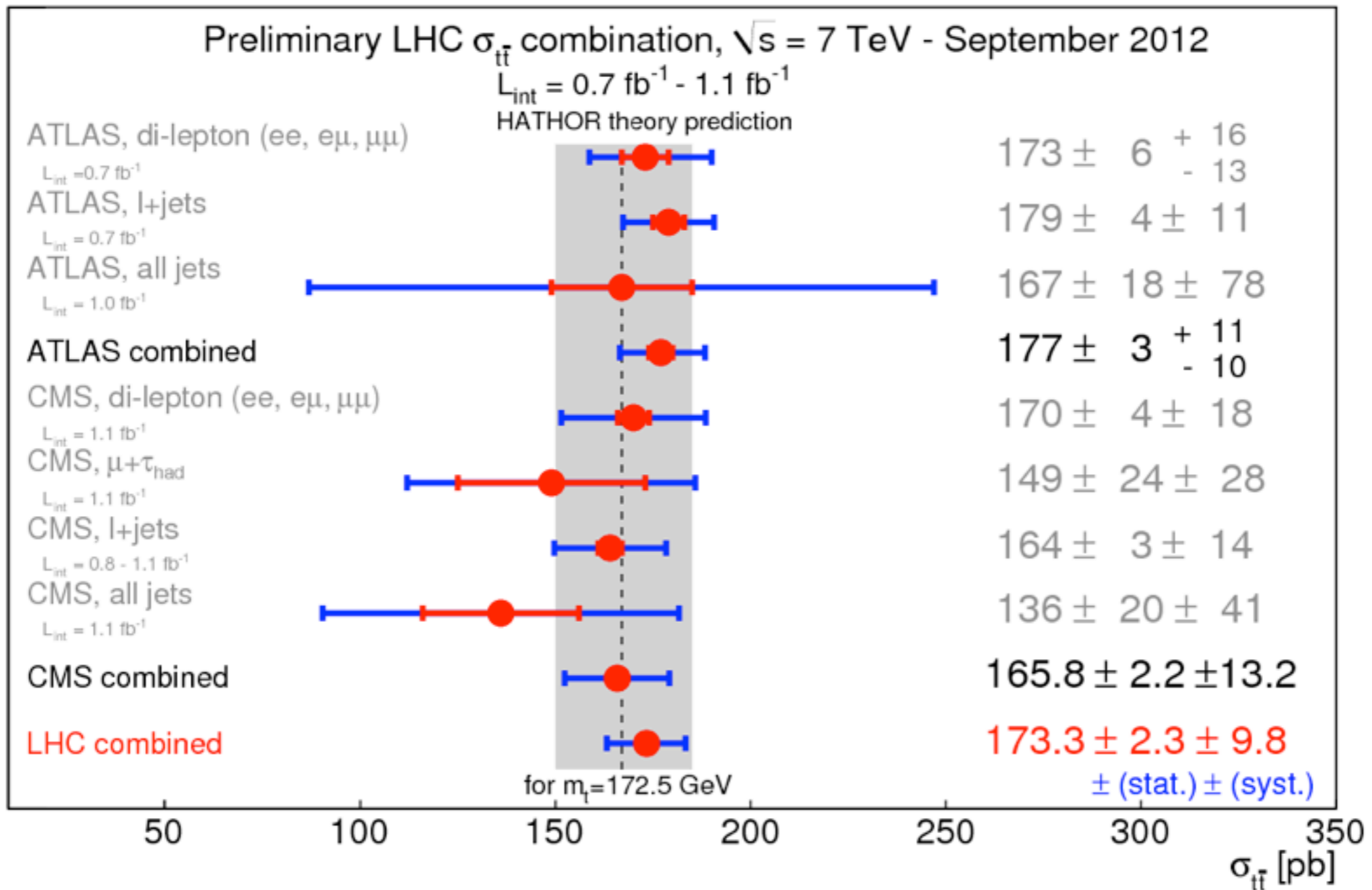
5.8% relative uncertainty,
7% improvement relative
to the most precise result

- Use Asymmetric Iterative BLUE (AIB):
 - ▶ <http://home.fnal.gov/cplager/log/AIB>
 - ▶ Important if combining the measurements where the magnitude of the uncertainty depends on the measurement itself
 - ▶ true for the cross section
 - ▶ uses the starting combined value to calculate the uncertainty
 - ▶ iterates until the starting value and the output are the same
 - ▶ Result of AIB and BLUE turned out to be identical within rounding

- Vary correlation between 0 and 1 and check the effect on combined cross section
 - ▶ Variation for JES and components of the signal model evaluated differently by CMS and ATLAS has negligible effect on the result
 - ▶ For luminosity uncertainty breakdown into correlated and uncorrelated part is critical
 - ▶ for extreme variation of correlation of total luminosity uncertainty between 0 and 1 cross section changes by 0.8 pb, uncertainty by 1.1% absolute, 12% relative

summary talk by W. Kozanecki at “LHC Lumi Days 2012 workshop”

- ATLAS luminosity uncertainty on the combined cross section - 3.8%
 - ▶ 3% comes from bunch current and taken as fully correlated with CMS
 - ▶ 2.3% uncorrelated
- CMS luminosity uncertainty on the combined cross section - 4.7%
 - ▶ 3.1% comes from bunch current and taken fully correlated with ATLAS
 - ▶ 3.5% uncorrelated





Recent measurements at 7 TeV

□ counting using soft muon tag

single lepton

□ ≥ 3 jets

ATLAS-CONF-2012-131

$$\sigma_{t\bar{t}} = 165 \pm 2(\text{stat}) \pm 17(\text{syst}) \pm 3(\text{lumi}) \text{ pb}$$

total uncertainty $\sim 10.5\%$



□ τ +jets, 1.7/fb, 23%

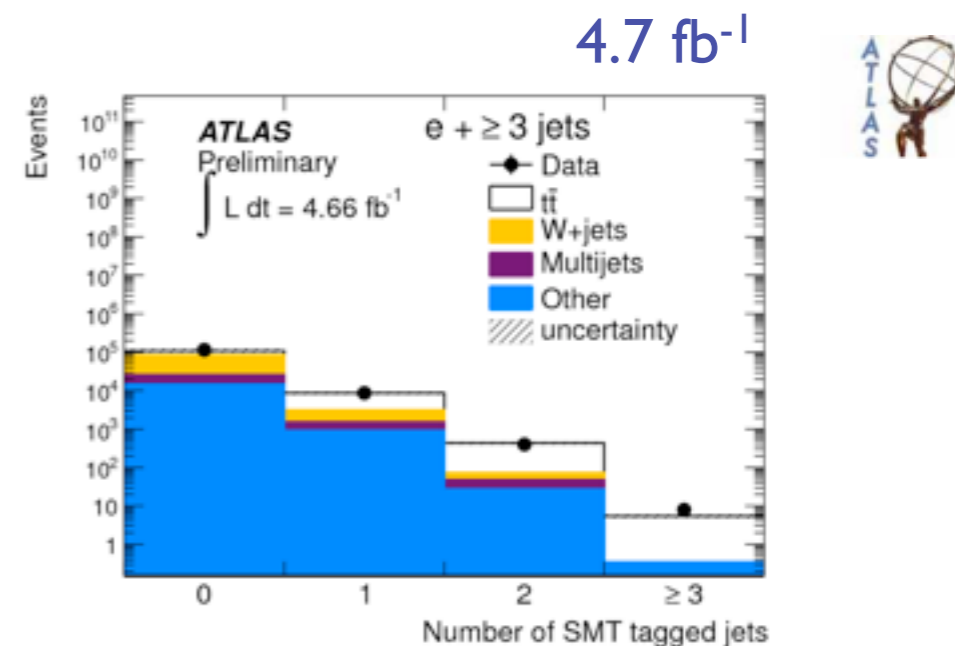
ATLAS-CONF-2012-032

□ all hadronic, 4.7/fb, 37%

ATLAS-CONF-2012-031

□ l + τ , 2/fb, 13.4%

[Phys. Lett. B 717 \(2012\) 89-108](#)



statistical correlation?

□ count with b-tagging

dilepton 2.3 fb⁻¹



□ cross section extracted from the profile likelihood fit to N_{jets} vs N_{btags} distribution

$$\sigma_{t\bar{t}} = 161.9 \pm 2.5(\text{stat})^{+5.1}_{-5.0}(\text{syst}) \pm 3.6(\text{lumi}) \text{ pb}$$

[arXiv:1208.2671](#)

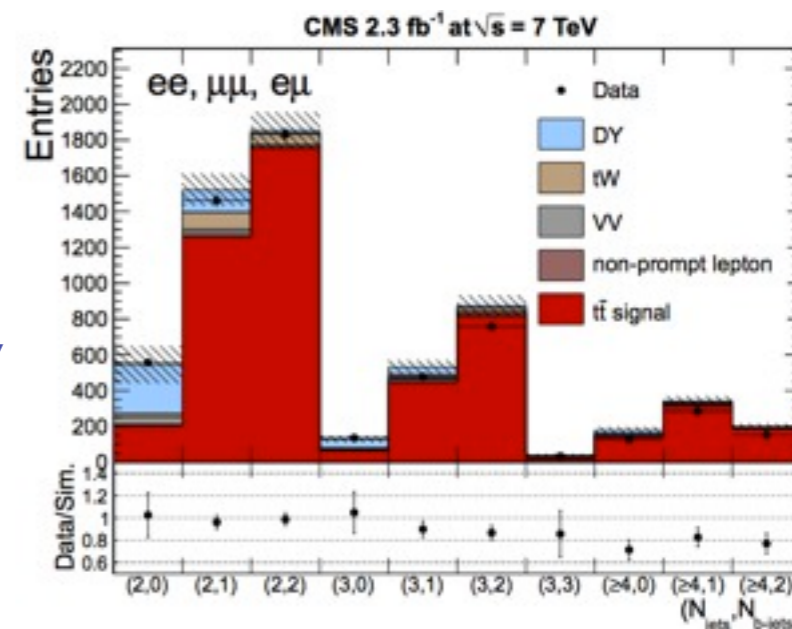
total uncertainty $\sim 5\%$

□ τ +jets, 3.9/fb, 23%

CMS PAS TOP-11-004

□ l + τ , 2.1/fb, 18%

[Phys. Rev. D 85 \(2012\) 112007](#)



The most precise single measurement



single lepton

Source	Combined
Statistical Uncertainty	± 1.0
<i>Object selection</i>	
Lepton energy resolution	+0.2 /-0.1
Lepton reco, ID, trigger	+1.7 /-1.8
Jet energy scale	+3.5 /-3.8
Jet energy resolution	± 0.2
Jet reconstruction efficiency	± 0.06
Jet vertex fraction	+1.2 /-1.4
E_T^{miss} uncertainty	± 0.07
SMT muon reco, ID	± 1.3
SMT muon χ^2_{match} efficiency	± 0.6
<i>Background estimates</i>	
Multijet normalisation	± 4.4
W+jet normalisation	± 5.5
Other bkg normalisation	± 0.1
Other bkg systematics	+2.2 /-1.8
<i>Signal simulation</i>	
$b \rightarrow \mu X$ Branching ratio	+2.9 /-3.1
ISR/FSR	± 1.5
PDF	± 3.1
NLO generator	± 3.2
Parton shower	± 2.2
Total systematics	± 10.5
Integrated luminosity	± 1.8



dilepton

arXiv:1208.2671

Uncertainty on $t\bar{t}$ signal

Source	Without b tagging
Luminosity	2.2
Lepton efficiencies	1.7 (ee) / 1.7 ($\mu\mu$) / 1.0 ($e\mu$)
Lepton energy scale	0.3
Jet energy scale	1.8
Jet energy resolution	0.5
\cancel{E}_T efficiency	1.4
b tagging	-
Pileup	0.5
Scale of QCD (μ)	0.6
Matching partons to showers	0.6
W branching fraction	1.7

Very small modelling uncertainties

Only combined uncertainty on each background source is provided

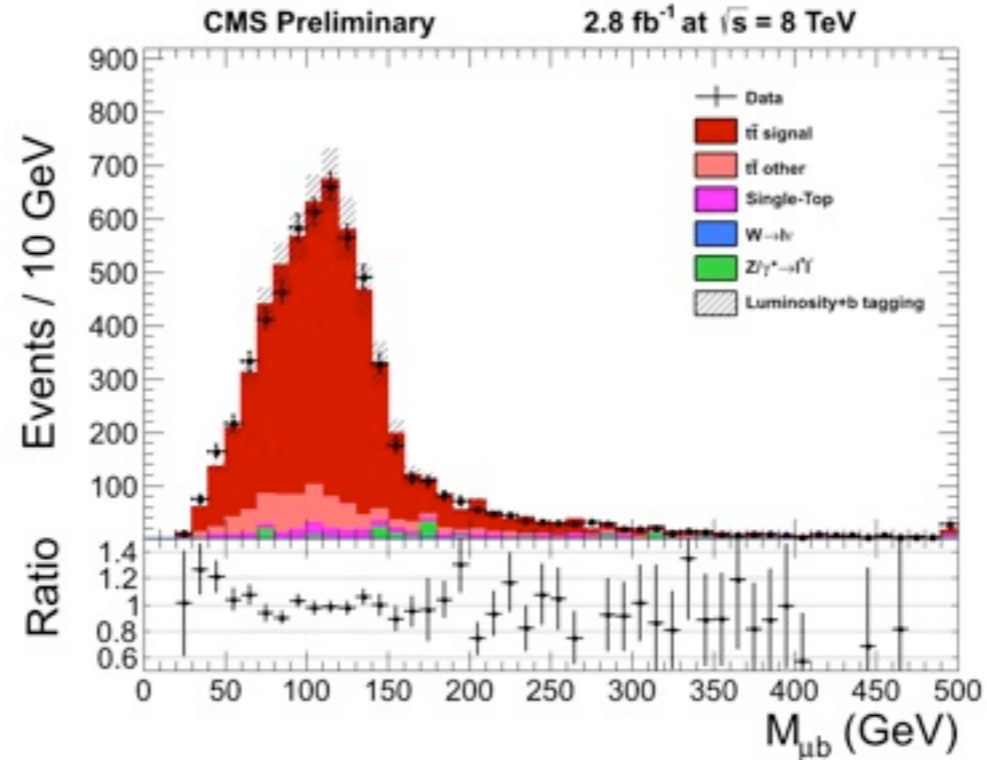
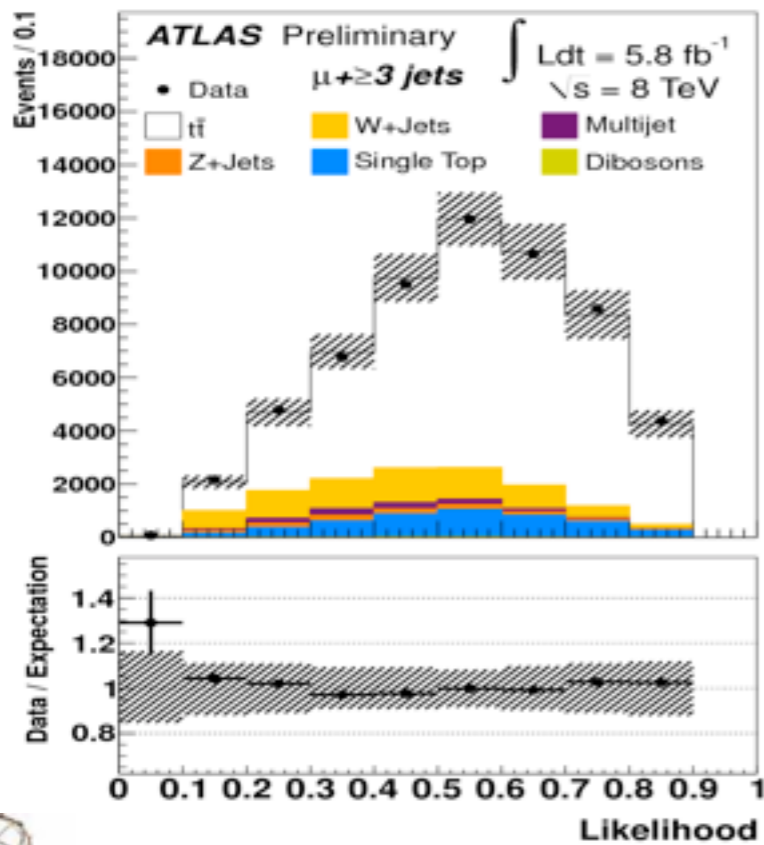
PDF uncertainty ?

No breakdown of uncertainties after the fit

A complete table is given for the counting cross check analysis



New measurements at 8 TeV



- ≥ 4 jets, ≥ 1 b-tag
- fit to $M(lb)$

CMS PAS TOP-12-006

$$\sigma_{t\bar{t}} \text{ (combined)} = 228.4 \pm 9.0 \text{ (stat.) } {}^{+29.0}_{-26.0} \text{ (syst.) } \pm 10.0 \text{ (lumi.) pb}$$

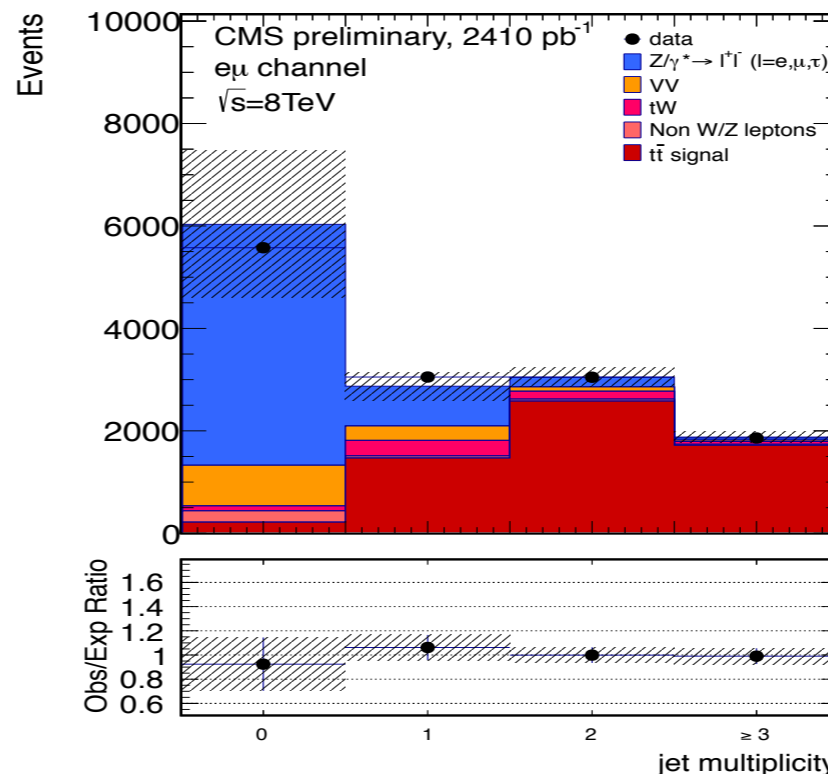


- ≥ 3 jets, ≥ 1 b-tag
- multivariate discriminant
 - lepton η , aplanarity

ATLAS-CONF-2012-149

$$\sigma_{t\bar{t}} = 241 \pm 2 \text{ (stat.) } \pm 31 \text{ (syst.) } \pm 9 \text{ (lumi.) pb}$$

in $l+jets$ comparable uncertainty between ATLAS and CMS



CMS PAS TOP-12-007



dilepton

- ≥ 2 jets, ≥ 1 b-tag
- counting

$$\sigma = 227 \pm 3 \text{ (stat.) } \pm 11 \text{ (syst.) } \pm 10 \text{ (lumi.) pb}$$



8 TeV measurements: systematics

ATLAS-CONF-2012-149



Source	$e+ \geq 3 \text{ jets}$	$\mu+ \geq 3 \text{ jets}$	combined
Jet/MET reconstruction, calibration	6.7, -6.3	5.4, -4.6	5.9, -5.2
Lepton trigger, identification and reconstruction	2.4, -2.7	4.7, -4.2	2.7, -2.8
Background normalization and composition	1.9, -2.2	1.6, -1.5	1.8, -1.9
b-tagging efficiency	1.7, -1.3	1.9, -1.1	1.8, -1.2
MC modelling of the signal	± 12	± 11	± 11
Total	± 14	± 13	± 13

single lepton	
generator	6%
shower	6%
ISR/FSR	4%
PDF	6%



TABLE 1. Overview of the systematic uncertainties on the cross section measurement. Uncertainties marked with (*) are obtained from 7 TeV.

dilepton

CMS PAS TOP-12-007

CMS PAS TOP-12-006

Systematic	Combined fit $\delta\sigma_{t\bar{t}}$ (%)
Jet Energy Scale	$+4.3 -5.0$
Jet Energy Resolution	+0.5 -1.1
Pileup	-0.7 +0.7
Background Composition	-0.1 +0.1
W+Jets template shape from unweighted 7TeV	0.9
Normalisation of data-driven multijet shape	0.9
b tagging efficiency measurement	8.0
Trigger Efficiency	-2.8 +3.2
Lepton selection	-2.4 +2.8
Factorization scale (*)	$+6.2 -2.1$
ME-PS Matching threshold (*)	$+4.6 -3.1$
PDF uncertainties (*)	$+1.6 -2.0$
Top Quark Mass (*)	+0.3 +1.4
Luminosity	4.4
Total	$+12.7 -11.4$



Source	Cont. to the $\sigma_{t\bar{t}}$ (%)
VV	0.1
Single top - tW	1.0
Non W/Z leptons	1.4
Drell-Yan	0.7
Lepton efficiencies	1.8
LES	0.3
JES	2.5
JER	1.7
B-tagging	0.9
pileup	1.5
Branching ratio	1.7
Event Q^2 scale	0.7
Matching	0.7
Total Systematic	4.7
Luminosity	4.4
Statistics	1.4





Summary cross section of measurements

exp	\sqrt{s}	channel	cross section
CMS	7	combo	$166 \pm 2(\text{stat}) \pm 11(\text{syst}) \pm 8(\text{lumi})$
ATLAS	7	combo	$177 \pm 3(\text{stat})^{+8}_{-7}(\text{syst}) \pm 7(\text{lumi})$
LHC	7	combo	$173.3 \pm 2.3(\text{stat}) \pm 9.8(\text{syst+lumi})$
CMS	7	dilepton	$161.9 \pm 2.5(\text{stat})^{+5.1}_{-5.0}(\text{syst}) \pm 3.6(\text{lumi}) \text{ pb}$
CMS	7	tau+lep	$143 \pm 14(\text{stat.}) \pm 22(\text{syst}) \pm 3(\text{lumi})$
CMS	7	tau+jets	$156 \pm 12(\text{stat.}) \pm 33(\text{syst}) \pm 3(\text{lumi})$
ATLAS	7	l+jets	$165 \pm 2(\text{stat.}) \pm 17(\text{syst}) \pm 3(\text{lumi})$
ATLAS	7	tau+jets	$200 \pm 19(\text{stat}) \pm 43(\text{syst})$
ATLAS	7	tau+lep	$186 \pm 13(\text{stat.}) \pm 20(\text{syst}) \pm 7(\text{lumi})$
ATLAS	7	all hadron	$168 \pm 12(\text{stat.}) +60-57(\text{syst}) \pm 7(\text{lumi})$
ATLAS	8	l+jets	$241 \pm 2(\text{stat.}) \pm 31(\text{syst}) \pm 9(\text{lumi})$
CMS	8	l+jets	$228.4 \pm 9.0(\text{stat.}) +29.0-26.0(\text{syst}) \pm 10.(\text{lumi})$
CMS	8	dilepton	$227 \pm 3(\text{stat.}) \pm 11(\text{syst.}) \pm 10(\text{lumi.})$

- Performed the first combination of top pair production cross section measurements by CMS and ATLAS

$$\sigma = 173.3 \pm 2.3 \text{ (stat)} \pm 9.8 \text{ (syst+lumi)}$$

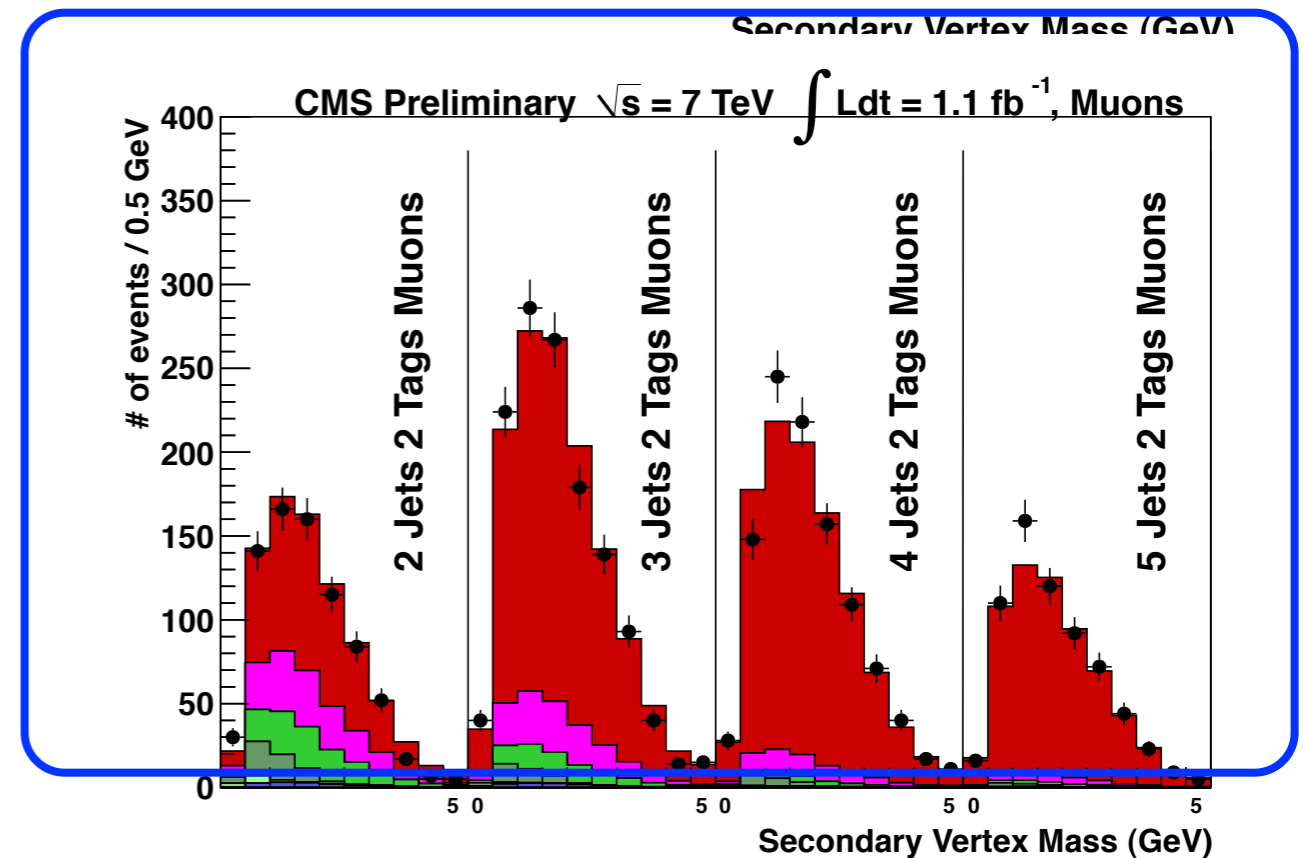
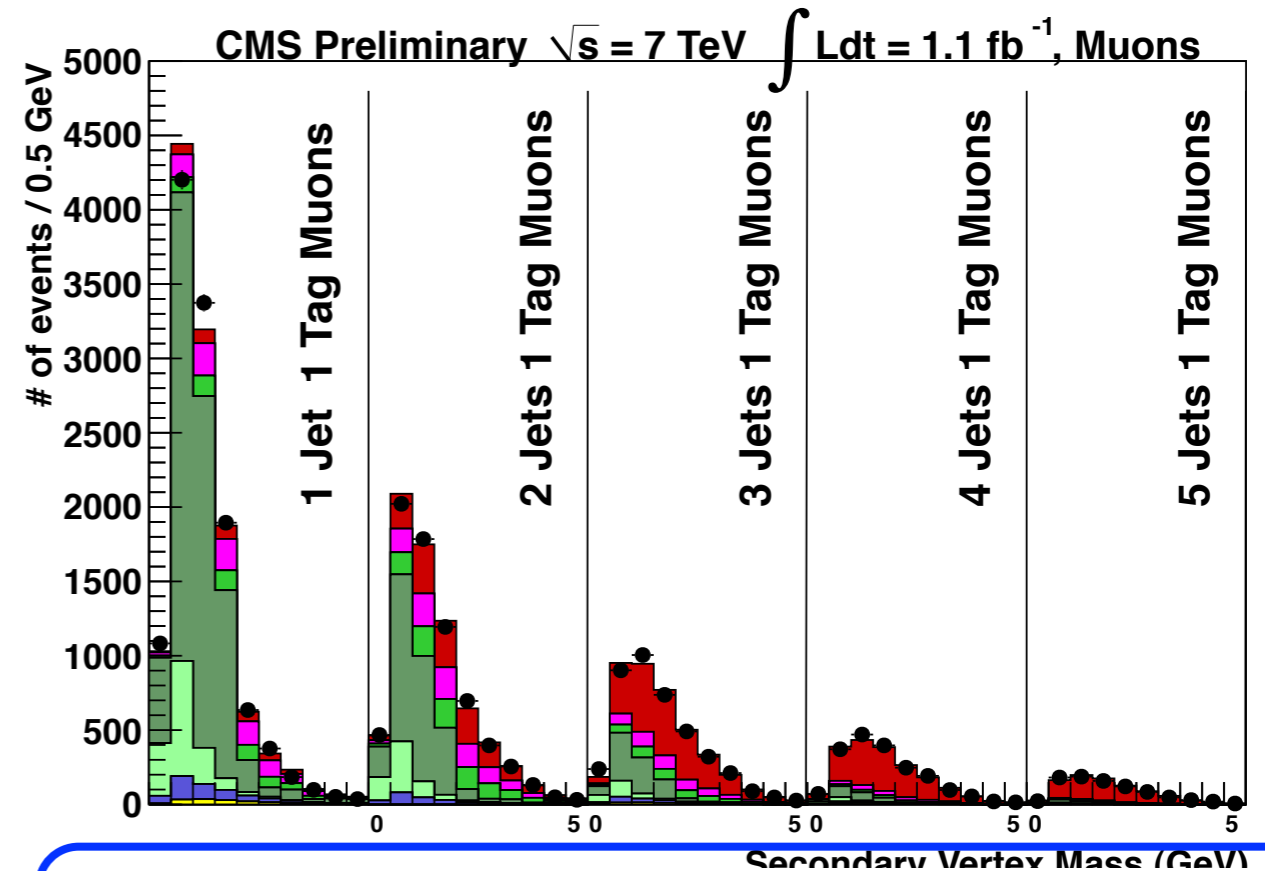
- Used BLUE method (as for top mass combinations)
- Luminosity correlation is of major importance in the current combination
 - ▶ luminosity uncertainty and correlation go down for full 2011 dataset
- **New combinations can be performed for 7 and 8 TeV results**
 - ▶ BLUE seems to be the best for practical reasons
 - ▶ it seems more practical to combine by channel
 - ▶ easier to update combination once new result is available
- Issues of future combinations
 - ▶ significant difference in treating modelling uncertainties by ATLAS and CMS
 - ▶ lack of information in public documents to perform combinations
 - ▶ some non-uniformity of quoting systematics even within the experiments



Backup

- Fit to secondary mass distribution in
 - $n_{jets} = 1, 2, 3, 4$ and ≥ 5
 - $n_{btag} = 1, 2$
- Profile likelihood fit
- 8% relative uncertainty
- dominant uncertainties:
 - luminosity
 - PDF
 - pileup

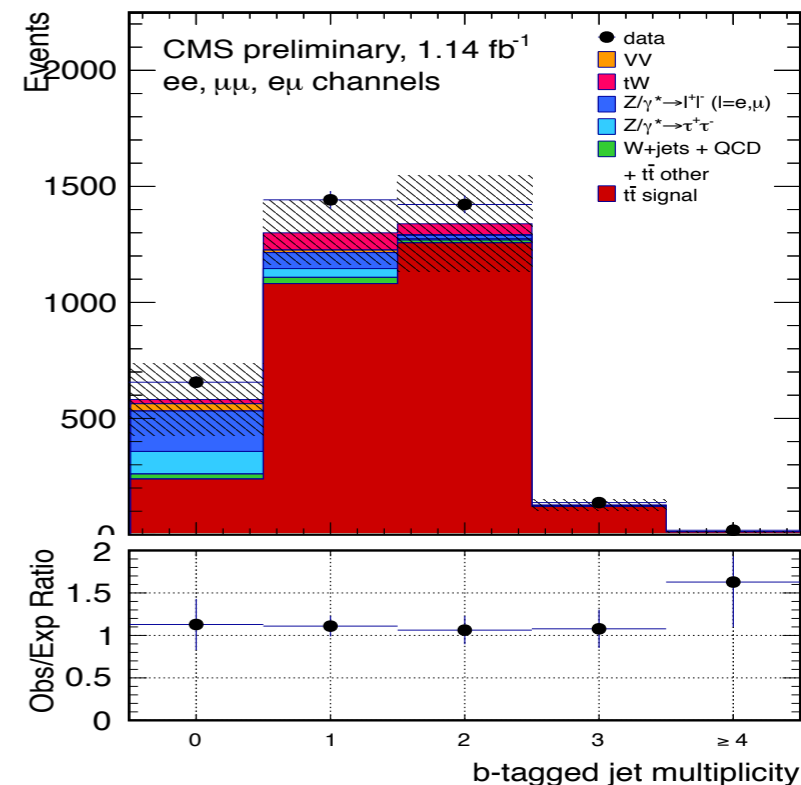
$$\sigma = 164 \pm 3(\text{stat}) \pm 12(\text{syst}) \pm 7(\text{lumi})$$



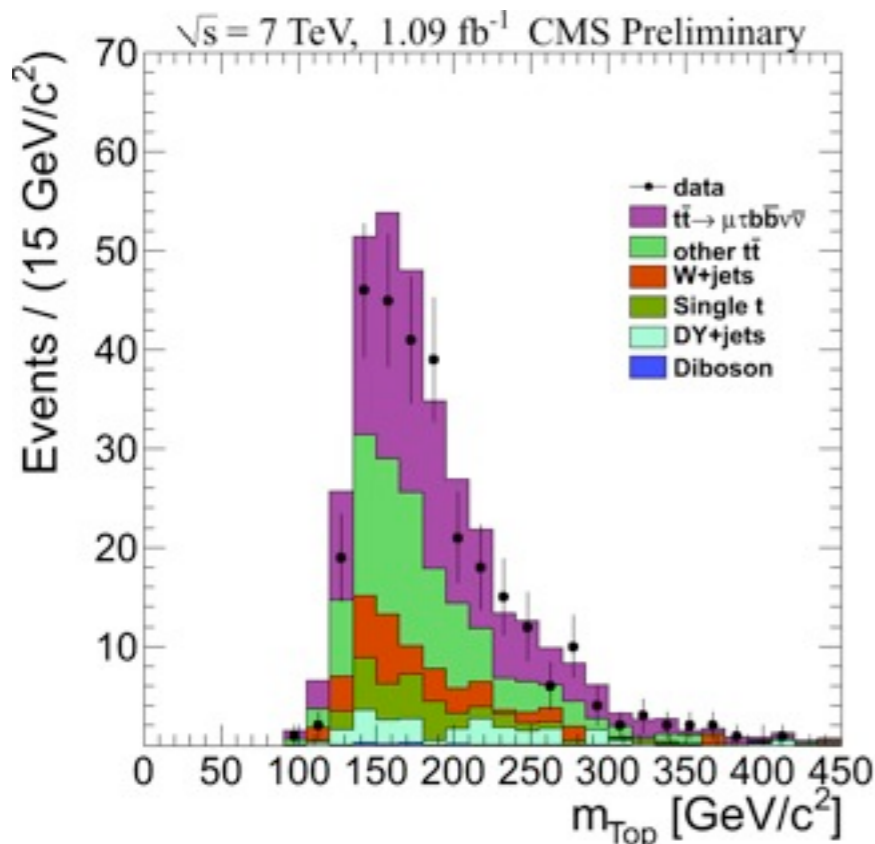
$ee, \mu\mu, e\mu$

- cut and count analysis
- dominant uncertainties:
 - b-tagging
 - pileup
 - lepton selection model

$$\sigma = 170 \pm 4(\text{stat}) \pm 16(\text{syst}) \pm 8 (\text{lumi})$$



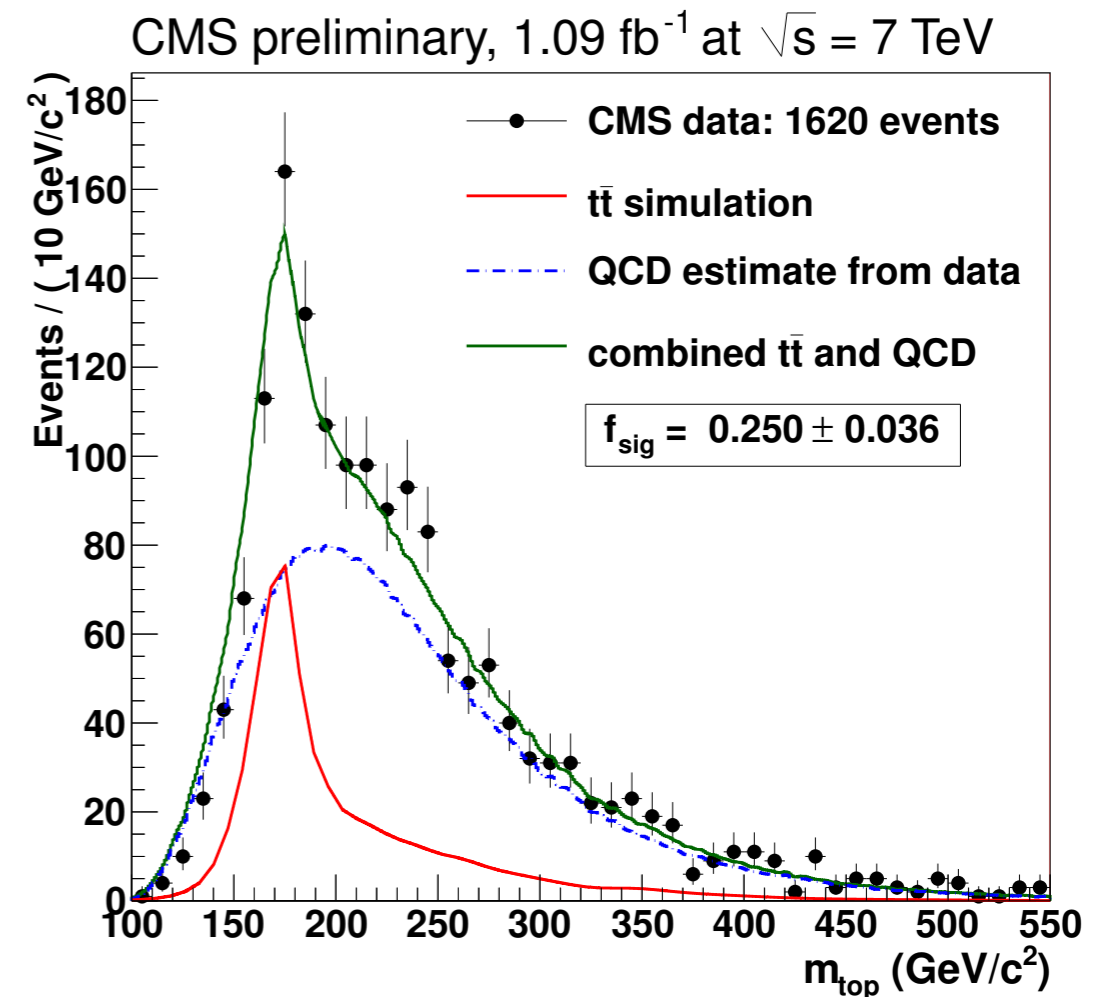
$\mu\tau_{\text{had}}$



- cut and count analysis
- dominant uncertainties:
 - τ fake background
 - τ identification
 - b-tagging
- overlap of events with l +jets channel has negligible effect on the combined result

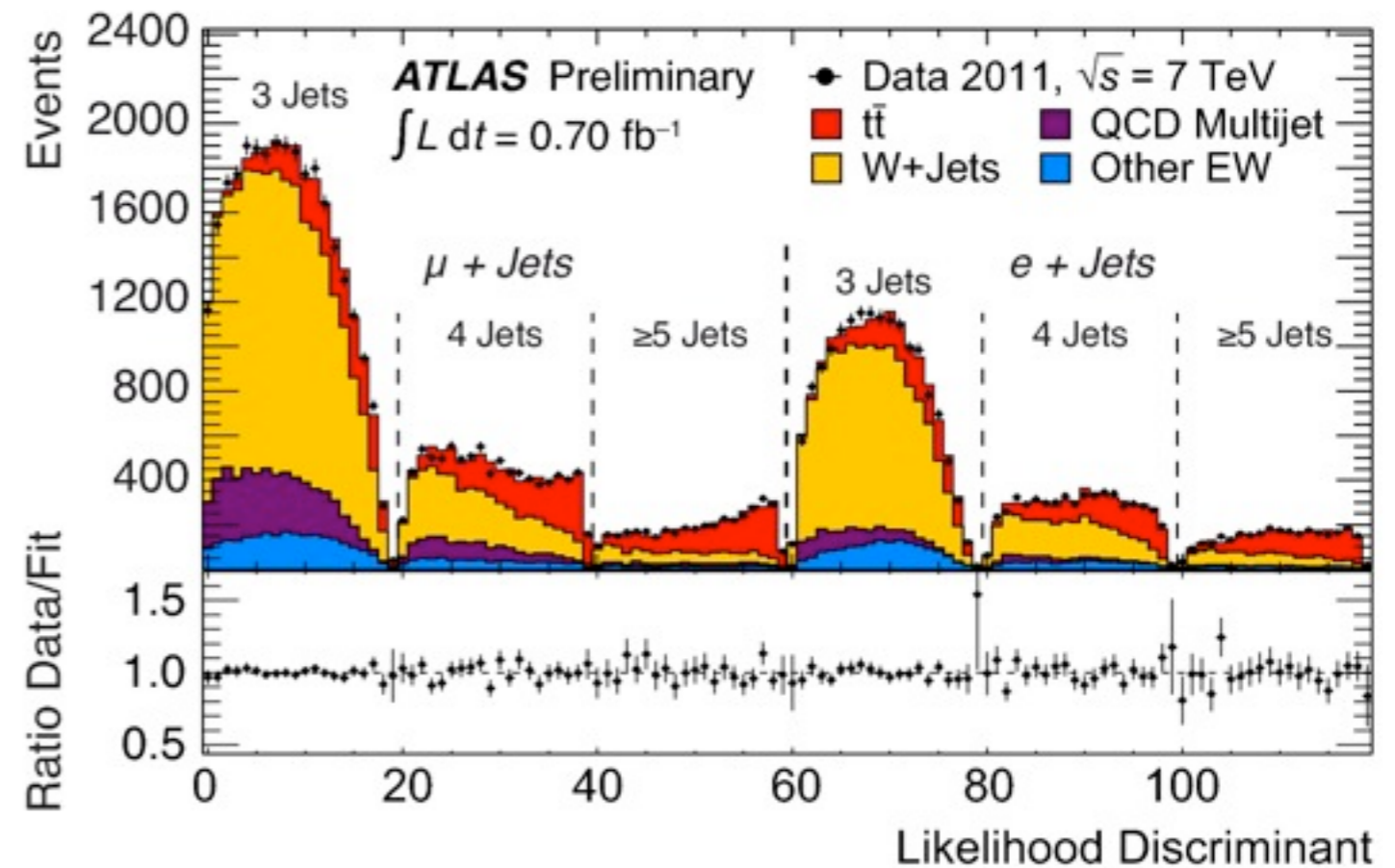
$$\sigma = 149 \pm 24(\text{stat}) \pm 26(\text{syst}) \pm 9 (\text{lumi})$$

- unbinned maximum likelihood fit to the reconstructed top quark mass
- dominant uncertainties
 - ▶ b-tagging
 - ▶ JES
 - ▶ background model



$$\sigma = 136 \pm 20(\text{stat}) \pm 40(\text{syst}) \pm 8 (\text{lumi})$$

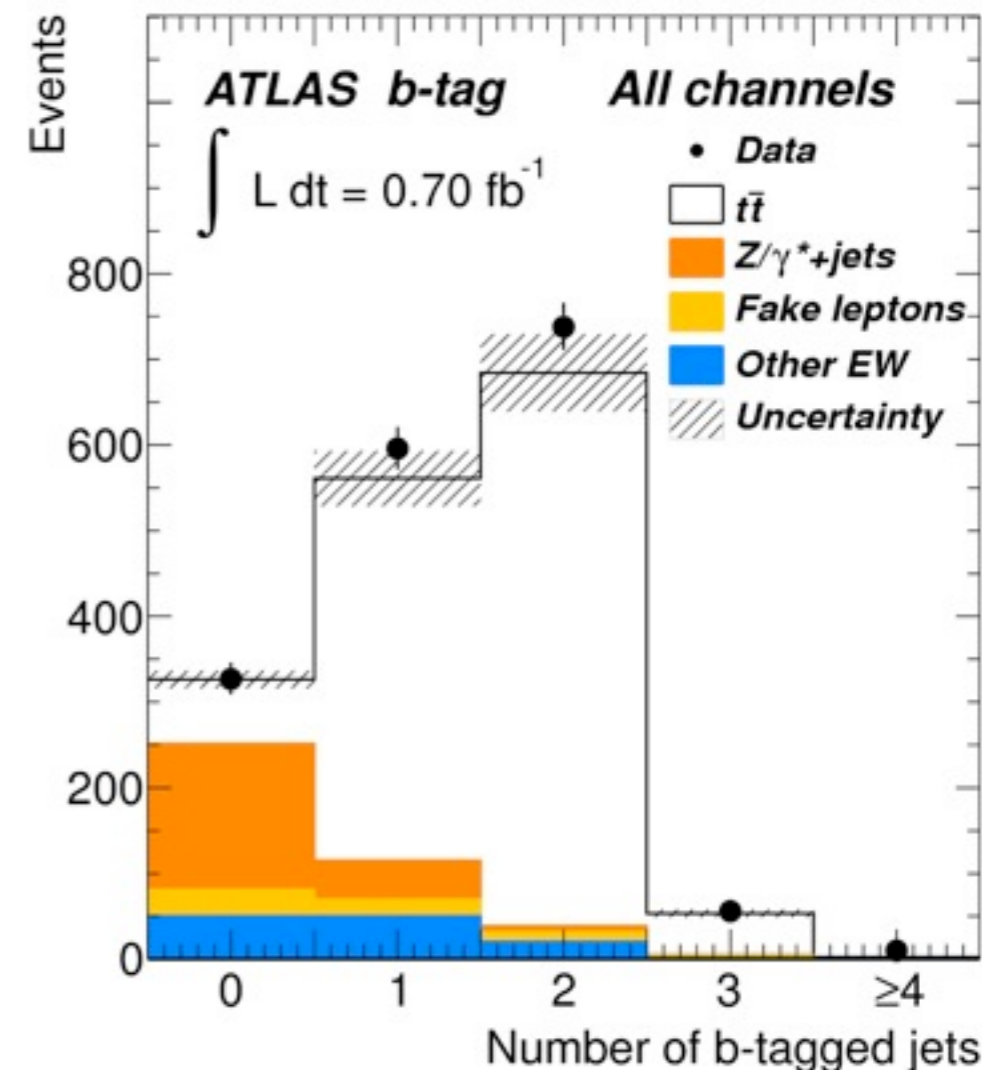
- discriminant built of 4 kinematic variables
- simultaneous fit in
 - njets = 3,4 and ≥ 5
 - no b-tag requirement
- profile likelihood fit
- dominant uncertainties
 - ▶ generator
 - ▶ JES
 - ▶ muon identification



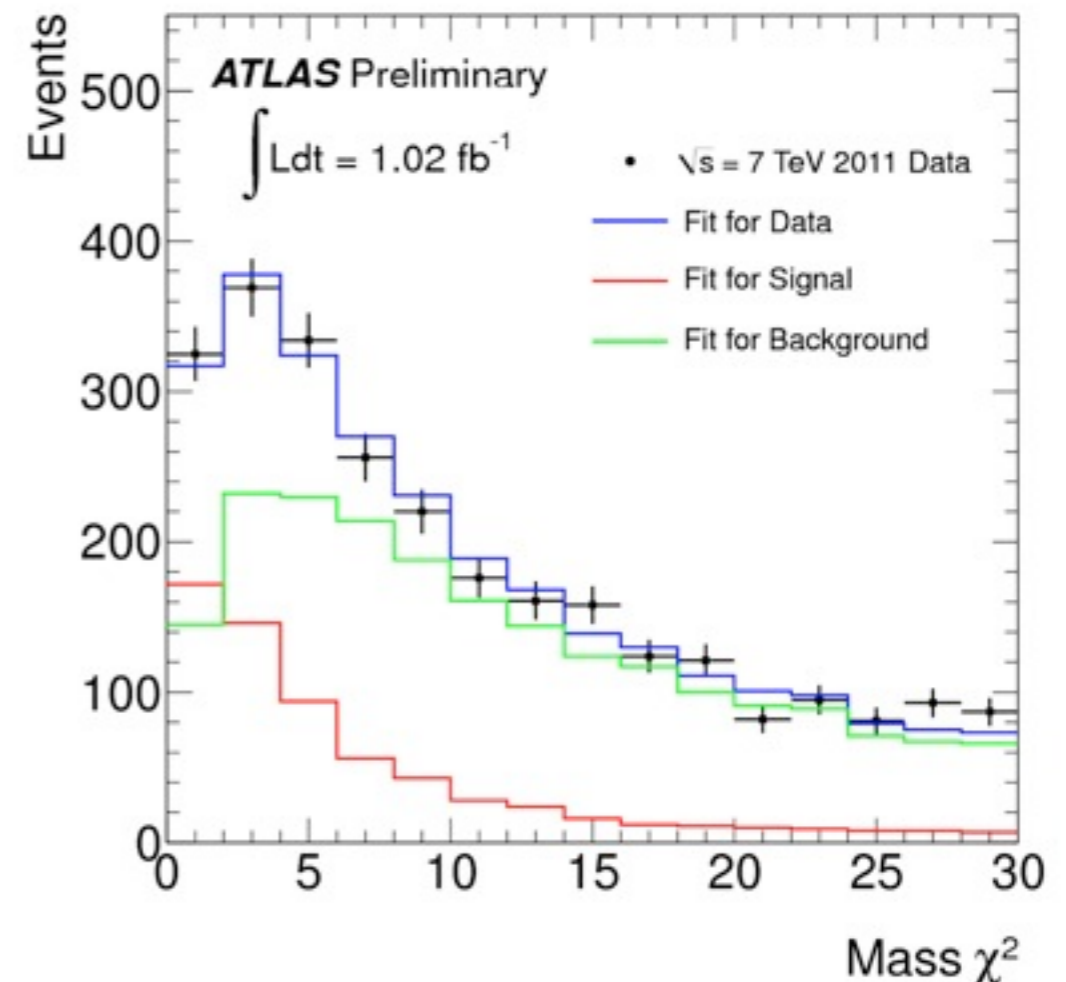
$$\sigma = 179 \pm 4 \text{ (stat)} \pm 9 \text{ (syst)} \pm 7 \text{ (lumi)}$$

- cut and count in 3 pretag samples
 - ▶ combination does not include l+track channels due to significant overlap with l+jets
- profile likelihood used to combine individual channels
- dominant uncertainties:
 - ▶ generator
 - ▶ JES
 - ▶ lepton identification

$$\sigma = 173 \pm 6 \text{ (stat)}^{+14}_{-11} \text{ (syst)}^{+8}_{-7} \text{ (lumi)}$$



- Binned likelihood fit to the reconstructed χ^2 top quark mass distribution
- Dominating uncertainties
 - ▶ JES
 - ▶ b-tagging
 - ▶ ISR/FSR



$$\sigma = 167 \pm 18 \text{ (stat)} \pm 78 \text{ (syst)} \pm 6 \text{ (lumi)}$$

What is the correlation?

summary talk by W. Kozanecki at “LHC Lumi Days 2012 workshop”

Systematic uncertainties on σ_{vis} (pp @ 7 TeV, vdM scans)

ATLAS
3.0%



CMS
3.1%

	ATLAS-CONF-2011-116 (2 fb ⁻¹) May 2011 vdM %	ATL Upd 2011 5 fb ⁻¹ , projected May 2011 vdM %	ATL est. 2012 for precision vdM scan	CMS 2011 pp 7 TeV May 2011 vdM %	ALICE 2011 pp 2.76 TeV Mar 2011 vdM %	LHCb 2011 pp 7 TeV Oct 2011 vdM %
DCCT calibration	2.73	0.23			0.4	0.23
FBCT bunch-by-bunch fractions	1.30	0.20			?	0.05
Ghost charge & satellites	0.18	0.18			0.4	0.39
<i>Subtotal, bunch-charge product</i>	3.0	0.35		3.10	0.64	0.46
Statistical	0.04	0.04		0?	0?	0.15
Beam centering	0.10	0.10		?	0	0
Beam position jitter	0.30	0.30	<i>depend</i>	?	?	?
ϵ growth & other non-reproducibility	0.40	0.77	<i>on</i>	1.34	0.64	1.06
Bunch-to-bunch σ_{vis} consistency	0.40	0.55		2 bunches	?	-> inflate stat err
Fit model	0.80	0.29		0	?	0.29
Background subtraction	N/A	0.31	<i>beam</i>	N/A	0.30	0
Reference \mathcal{L}_{int}	NC	0.30	<i>conditions</i>	only 1 det/alg	only 1 det/alg	only 1 det/alg
Dynamic beta	NC	0.80		?	1.00	0.80
Linear x-y coupling	negligible	negligible?		?	0.60	0.01
Non-linear transverse correlations	0.50	0.50		?	?	?
μ -dependence during vdM scan	0.50	0.50		?	negligible	no effect seen
Length scale calibration	0.30	0.30		0.50	1.41	0.14
ID length scale	0.30	0.30		?	?	?
Instrumental issues (e.g. BCM H/V)	0.70	0.70		-	-	-
<i>Subtotal, calibration-scan syst.</i>	1.5	1.75		1.43	1.96	1.38
Total syst. uncertainty on σ_{vis}	3.4	1.8		3.4 (1.5?)	2.1	1.5

The numbers are the systematic uncertainties (%) as reported by each experiment (and regrouped to fit roughly in the same descriptive scheme)

“?” reflect this speaker’s ignorance as to how this uncertainty was treated; it does not necessarily imply that it was ignored in the analysis – only that it was unclear where to find it.

<https://indico.cern.ch/conferenceOtherViews.py?view=standard&confId=162948>