

Transverse Momentum Resummation in Top Quark Pair Production

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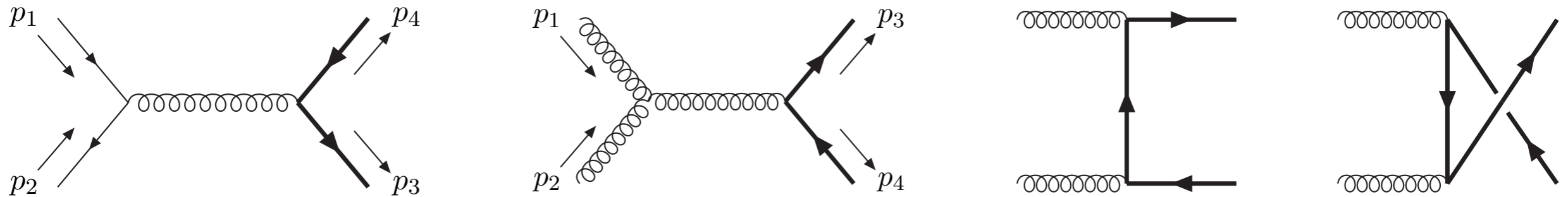
In collaboration with C. S. Li, H. T. Li, D. Y. Shao, H. X. Zhu

The first three years of the LHC, Mainz, March 2013

Outline

- Introduction: top quark pair production
- Introduction: Q_T resummation
- Q_T resummation in top quark pair production
- Summary

Top quark pair production



- Main production mechanism of top quarks at hadron colliders
- NNLO results for **total cross section** emerging Bärnreuther, Czakon, Mitov: 1204.5201
Czakon, Mitov: 1207.0236 & 1210.6832
waiting for the *gg* channel...
- Pair differential distributions interesting
 - Searching for new resonances in the **invariant mass** distribution
 - Forward-backward asymmetry shows intriguing dependence on the **invariant mass** and the **transverse momentum** of the pair

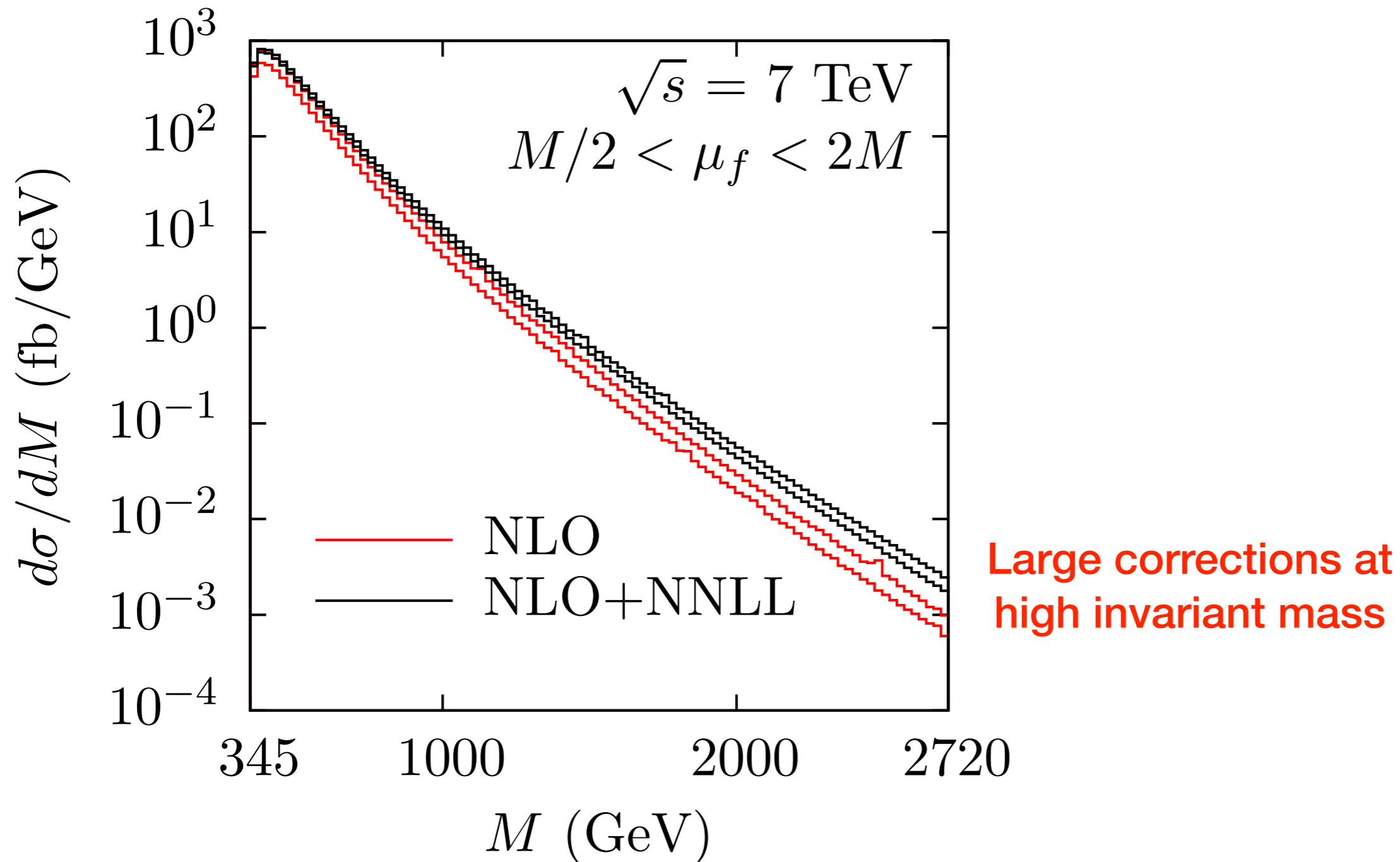
M

Q_T

Invariant mass distribution

Ahrens, Ferroglia, Neubert, Pecjak, LLY: 1003.5827

- NLO+NNLL threshold resummed prediction



Invariant mass distribution in the boosted regime

- For M much larger than m_t , may simultaneously resum threshold logs and mass logs
- Framework set up **Ferrogia, Pecjak, LLY: 1205.3662**

$$C_{ij}(z, M, m_t, \cos \theta, \mu_f) = C_D^2(m_t, \mu_f) \text{Tr} \left[\mathbf{H}_{ij}(M, t_1, \mu_f) \mathbf{S}_{ij}(\sqrt{\hat{s}}(1-z), t_1, \mu_f) \right]$$

partonic cross section

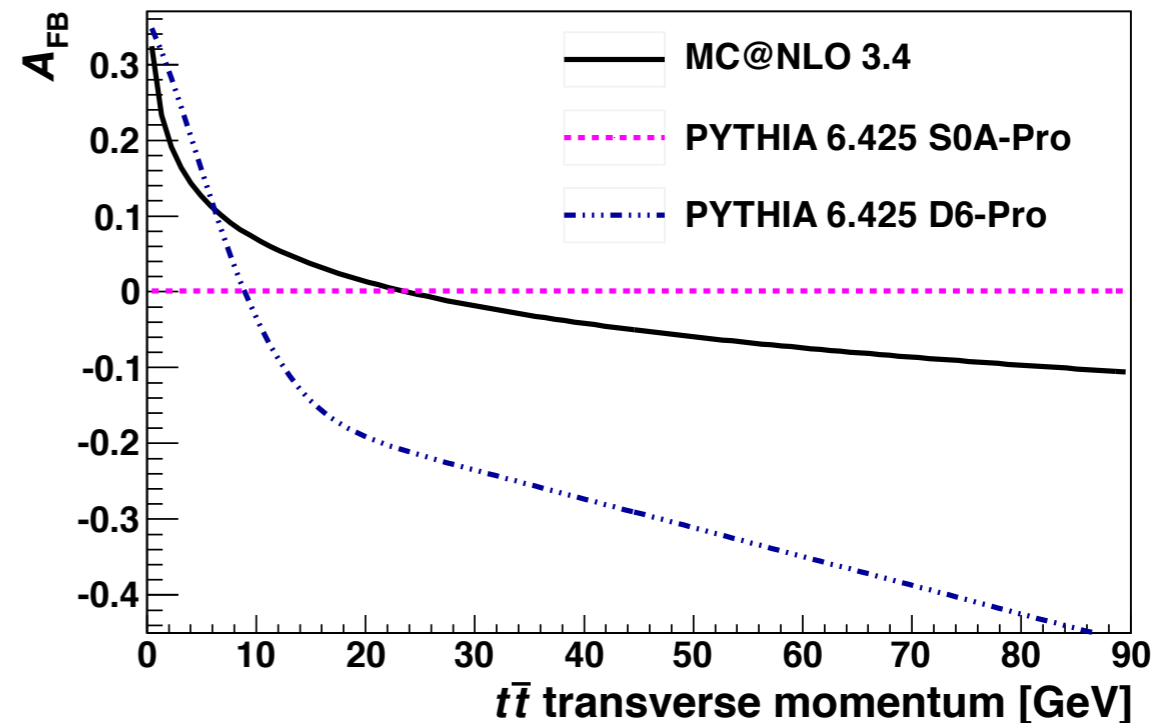
$$\otimes C_{ff}^{ij}(z, m_t, \mu_f) \otimes C_{t/t}(z, m_t, \mu_f) \otimes C_{t/t}(z, m_t, \mu_f)$$

$$\otimes S_D(m_t(1-z), \mu_f) \otimes S_D(m_t(1-z), \mu_f) + \mathcal{O}(1-z) + \mathcal{O}\left(\frac{m_t}{M}\right)$$

- NNLO massless soft function calculated — allows soft+virtual at NNLO
Ferrogia, Pecjak, LLY: 1207.4798
- Phenomenological studies in progress

Small Q_T region

- Suppress the gluon channel — enhance the forward-backward asymmetry
- Theoretically challenging — fixed-order divergent, **resummation** necessary
- Existing parton shower tools need to be validated in this region by analytic calculations



D0 Collaboration: 1107.4995

Q_T resummation

- Originally developed by Collins, Soper, Sterman (CSS)
Collins, Soper, Sterman: Nucl. Phys. B 250, 199 (1985)
- Refinement by Catani, de Florian, Grazzini
Catani, de Florian, Grazzini: hep-ph/0008014
- New SCET based approaches
 - Becher, Neubert: 1007.4005
 - Chiu, Jain, Neill, Rothstein: 1104.0881
 - Echevarria, Idilbi, Scimemi: 1111.4996

Applied to color-neutral final states so far!

Q_T resummation in Higgs production

Becher, Neubert, Wilhelm: 1212.2621

$$d\sigma = \sigma_0(\mu) C_t^2(m_t^2, \mu) |C_S(-m_H^2, \mu)|^2 \frac{m_H^2}{\tau_S} dy \frac{d^2 q_\perp}{(2\pi)^2} \int d^2 x_\perp e^{-iq_\perp \cdot x_\perp} \\ \times 2\mathcal{B}_c^{\mu\nu}(\xi_1, x_\perp, \mu) \mathcal{B}_{\bar{c}\mu\nu}(\xi_2, x_\perp, \mu) \mathcal{S}(x_\perp, \mu),$$

transverse PDFs

**transverse soft function
trivial with analytic regulator**

$$\bar{C}_{gg\leftarrow ij}(z_1, z_2, q_T^2, m_H^2, \mu) = \frac{1}{2} \int_0^\infty dx_T x_T J_0(x_T q_T) \exp[g_A(\eta, L_\perp, a_s)] \\ \times \sum_{n=1,2} \bar{I}_{g\leftarrow i}^{(n)}(z_1, L_\perp, a_s) \bar{I}_{g\leftarrow j}^{(n)}(z_2, L_\perp, a_s),$$

See Becher's talk for details

Q_T subtraction

Catani, Grazzini: hep-ph/0703012

- Closely related to Q_T resummation
- Exploits behavior at small Q_T to subtract IR divergences
- Works in principle for any process where Q_T resummation is available
- One of the first subtraction methods applied successfully at NNLO

$$d\sigma_{(N)NLO}^F = \mathcal{H}_{(N)NLO}^F \otimes d\sigma_{LO}^F + \left[d\sigma_{(N)LO}^{F+jets} - d\sigma_{(N)LO}^{CT} \right]$$

Q_T resummation in $t\bar{t}$ production

- Early attempts — naively supplementing the CSS formalism with final state interactions

Berger, Meng: hep-ph/9310341

Mrenna, Yuan: hep-ph/9606361

- Results don't agree between the two works!

- (Partial) NLL only. No initial-final interference.

- New SCET based systematic factorization/resummation framework

Li, Li, Shao, LLY, Zhu: 1208.5774

- Works in principle to all orders

Rest of this talk!

- NNLL numerical results

Factorization formula

- An all-order factorization formula is proposed

$$\frac{d^4\sigma}{dQ_T^2 dy dM d\cos\theta} = \frac{\pi\beta_t}{sM} \int \frac{d^2x_\perp}{4\pi} e^{-iQ_\perp \cdot x_\perp} \\ \times \text{Tr} \left[\mathbf{H}(M, \cos\theta, m_t, \mu) \mathbf{S}(L_\perp, M, \cos\theta, m_t, \mu) \right] \\ \times \mathcal{B}(\xi_1, L_\perp, \mu) \bar{\mathcal{B}}(\xi_2, L_\perp, \mu)$$

same as in
threshold resummation

Ahrens, Ferroglia, Neubert,
Pecjak, LLY: 1003.5827

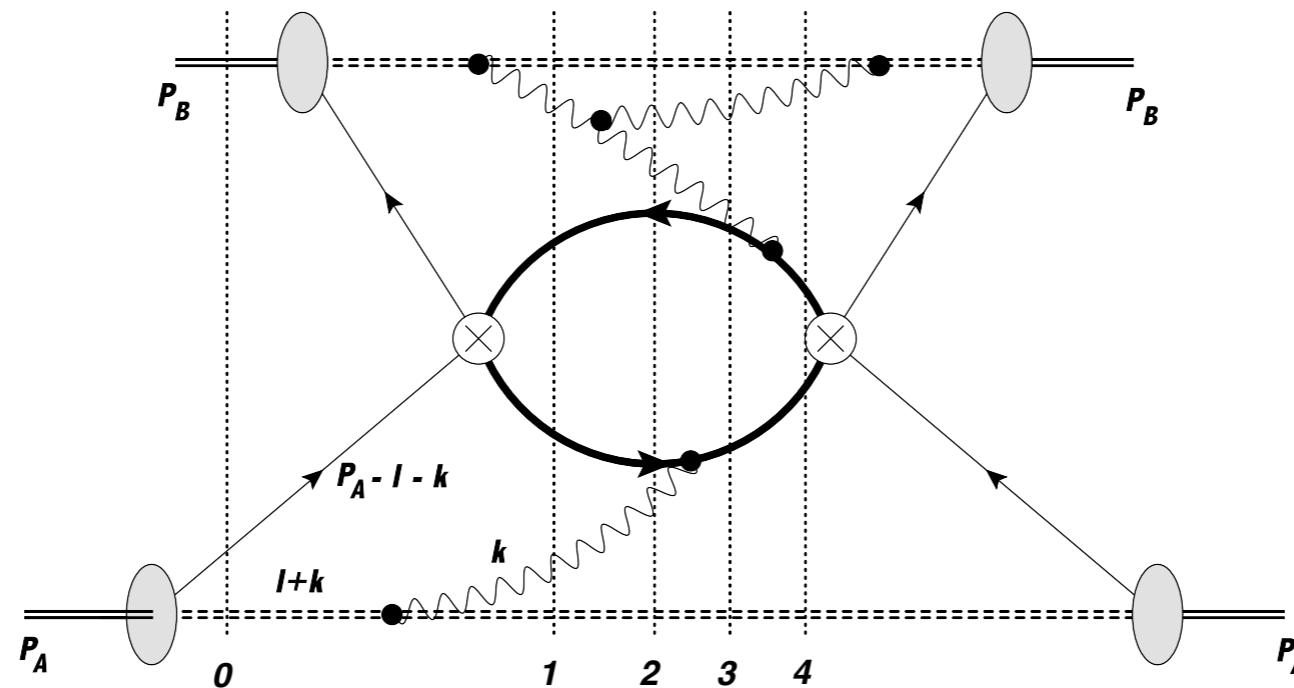
same as in
DY and Higgs

Becher, Neubert, Wilhelm:
1109.6027 & 1212.2621

new transverse soft function
matrix in color space

Possible factorization breaking effects

Mitov, Sterman: 1209.5798



See also

Collins, Qiu: 0705.2141

Rogers, Mulders: 1001.2977

- Due to interactions among top quarks and spectators
- Numerical impacts unclear
- We focus on the partonic cross section (neglecting spectators)

The transverse soft function

$$\mathcal{S}(L_{\perp}, M, \cos \theta, m_t, \mu) = \frac{1}{d_R} \sum_{X_s} \int \frac{d\phi_t}{2\pi} d^2 Q_{\perp} e^{i Q_{\perp} \cdot x_{\perp}} \\ \times \langle 0 | Y_n^{\dagger} Y_{\bar{n}}^{\dagger} Y_t^{\dagger} Y_{\bar{t}}^{\dagger} | X_s \rangle \delta^{(2)}(Q_{\perp} + \hat{P}_{\perp}) \langle X_s | Y_n Y_{\bar{n}} Y_t Y_{\bar{t}} | 0 \rangle$$

- Definition similar to the threshold one, but calculation much more complicated due to the presence of the transverse vector
- We had to integrate over the azimuthal angle — calculation for the more exclusive case failed **ideas?**

NLO soft function

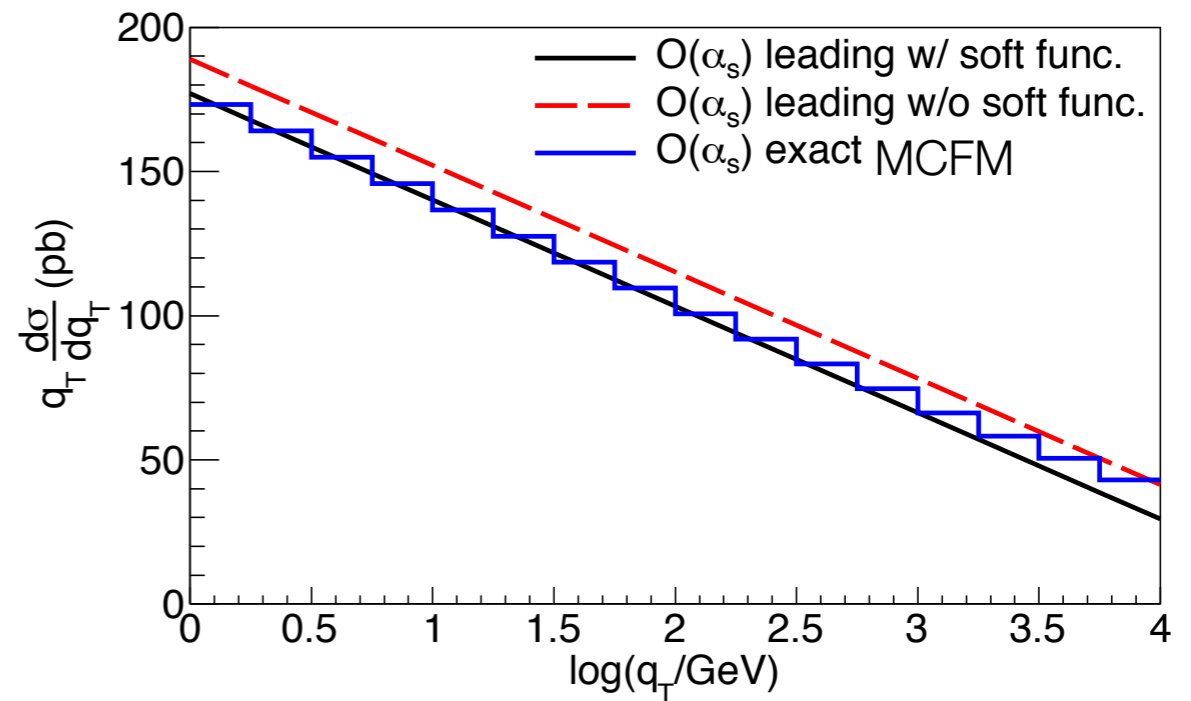
$$\begin{aligned}
 \mathcal{S}_{i\bar{i}}^{(1)} = & 4L_{\perp} \left(2w_{i\bar{i}}^{13} \ln \frac{-t_1}{m_t M} + 2w_{i\bar{i}}^{23} \ln \frac{-u_1}{m_t M} + w_{i\bar{i}}^{33} \right) \\
 & - 4 \left(w_{i\bar{i}}^{13} + w_{i\bar{i}}^{23} \right) \text{Li}_2 \left(1 - \frac{t_1 u_1}{m_t^2 M^2} \right) + 4w_{i\bar{i}}^{33} \ln \frac{t_1 u_1}{m_t^2 M^2} \\
 & - 2w_{i\bar{i}}^{34} \frac{1 + \beta_t^2}{\beta_t} [L_{\perp} \ln x_s + f_{34}],
 \end{aligned}$$

$$\begin{aligned}
 f_{34} = & -\text{Li}_2 \left(-x_s \tan^2 \frac{\theta}{2} \right) + \text{Li}_2 \left(-\frac{1}{x_s} \tan^2 \frac{\theta}{2} \right) \\
 & + 4 \ln x_s \ln \cos \frac{\theta}{2}.
 \end{aligned}$$

- Rapidity divergence in intermediate steps regularized using method in **Becher, Bell: 1112.3907**
- No rapidity divergence in the final soft function (as expected)
- Dependence on the scattering angle cannot be written as simple functions of the invariants t_1 and u_1 (unlike the threshold soft function)

Consistency checks

- NLO expansion compared with exact result at small Q_T
- Soft function important for the nice agreement
- Constant term checked by reproducing the NLO total cross section
- Would be great to compare the NNLO expansion with the NLO $t\bar{t}$ +jet code



Resummation formula

$$\begin{aligned}
 C_{i\bar{i}\leftarrow ab}(z_1, z_2, q_T, M, \cos\theta, m_t, \mu) &= \frac{1}{2} \int_0^\infty db b J_0(bq_T) \\
 &\times \exp [g_i(\eta_i, L_\perp, \alpha_s)] \left[\bar{I}_{i/a}(z_1, L_\perp, \alpha_s) \bar{I}_{\bar{i}/b}(z_2, L_\perp, \alpha_s) \right. \\
 &\quad \left. + \delta_{gi} \bar{I}'_{g/a}(z_1, L_\perp, \alpha_s) \bar{I}'_{g/b}(z_2, L_\perp, \alpha_s) \right] \\
 &\times \text{Tr} \left[\mathbf{H}_{i\bar{i}}(M, \cos\theta, m_t, \mu_h, \mu) \mathbf{S}_{i\bar{i}}(L_\perp, M, \cos\theta, m_t, \mu) \right]
 \end{aligned}$$

- Scale choices follow **Becher, Neubert, Wilhelm** for DY and Higgs

$$\mu_i = q_i^* + Q_T$$

- Much weaker dependence on non-perturbative physics due to larger mass
— protected all the way down to $Q_T = 0$

$$q_q^* \gtrsim 3.0\text{GeV} \quad q_g^* \gtrsim 14.0\text{GeV}$$

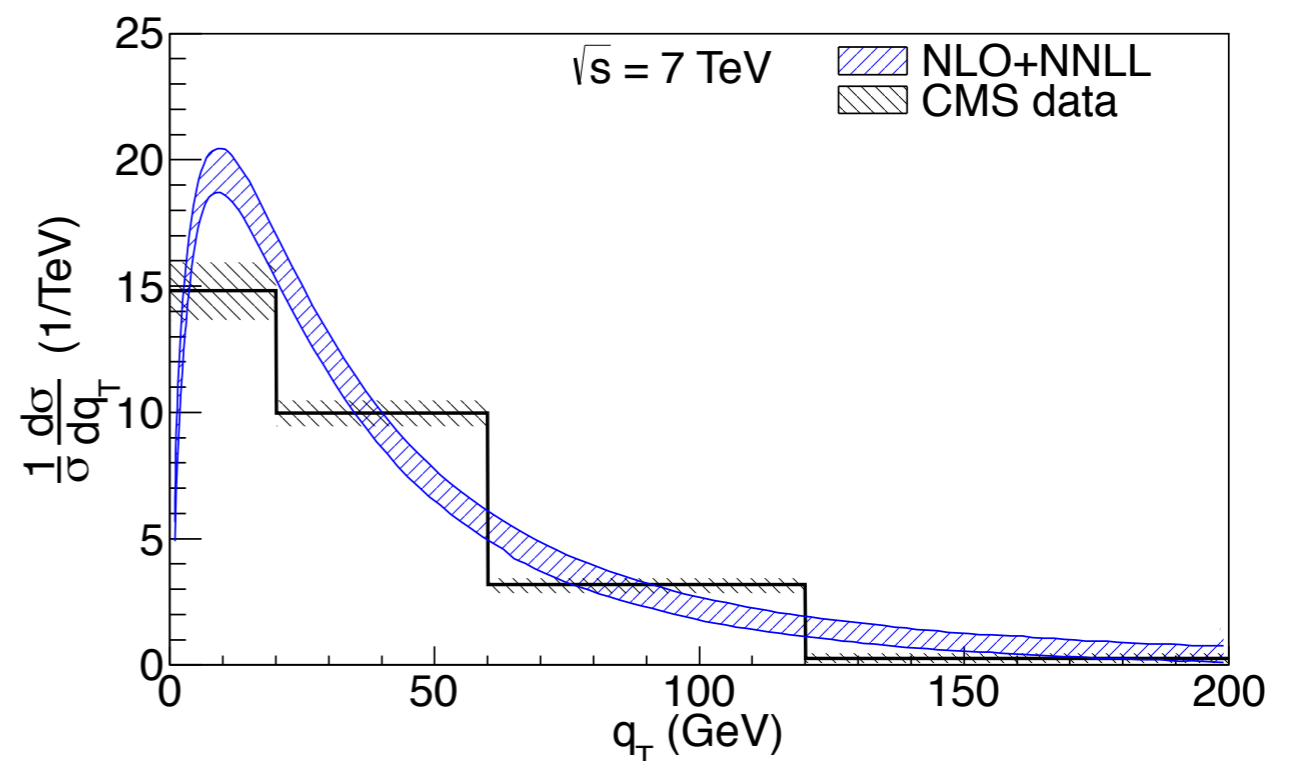
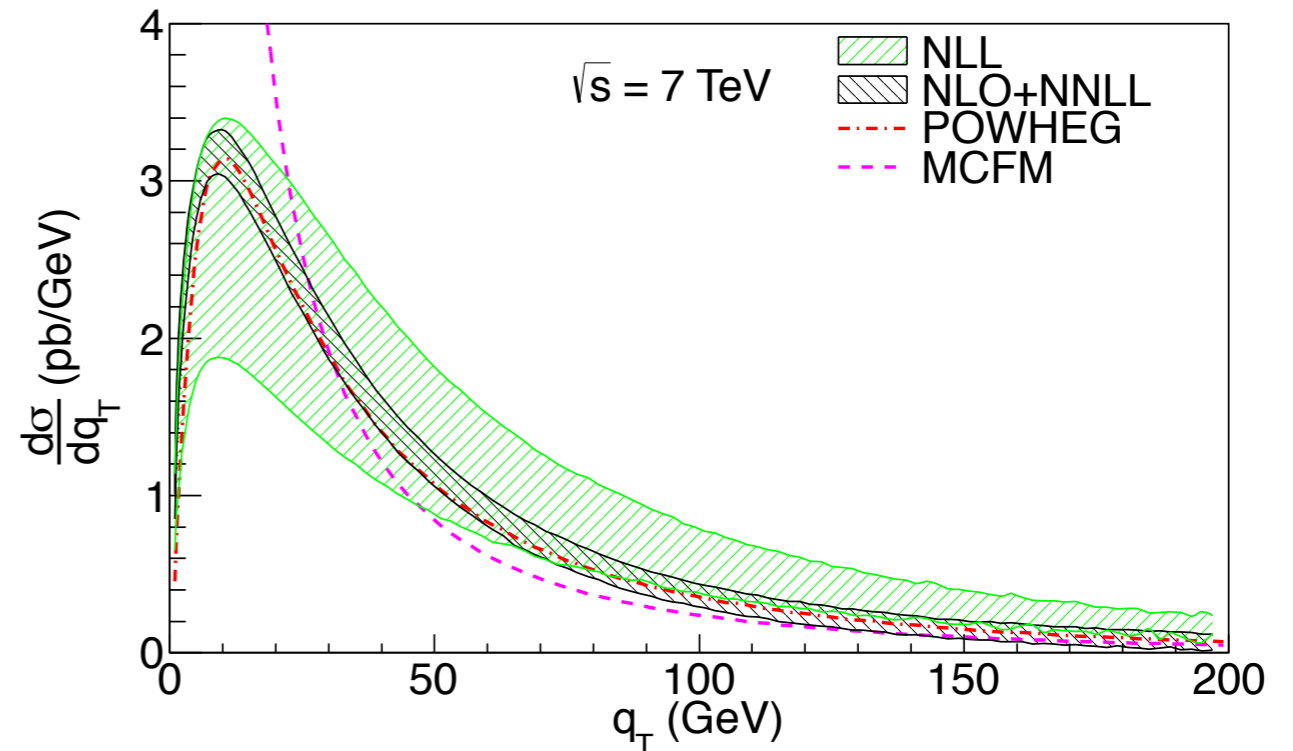
- Evolution of the hard function given in

Ferrogia, Neubert, Pecjak, LLY: 0907.4791 & 0908.3676

Ahrens, Ferrogia, Neubert, Pecjak, LLY: 1003.5827

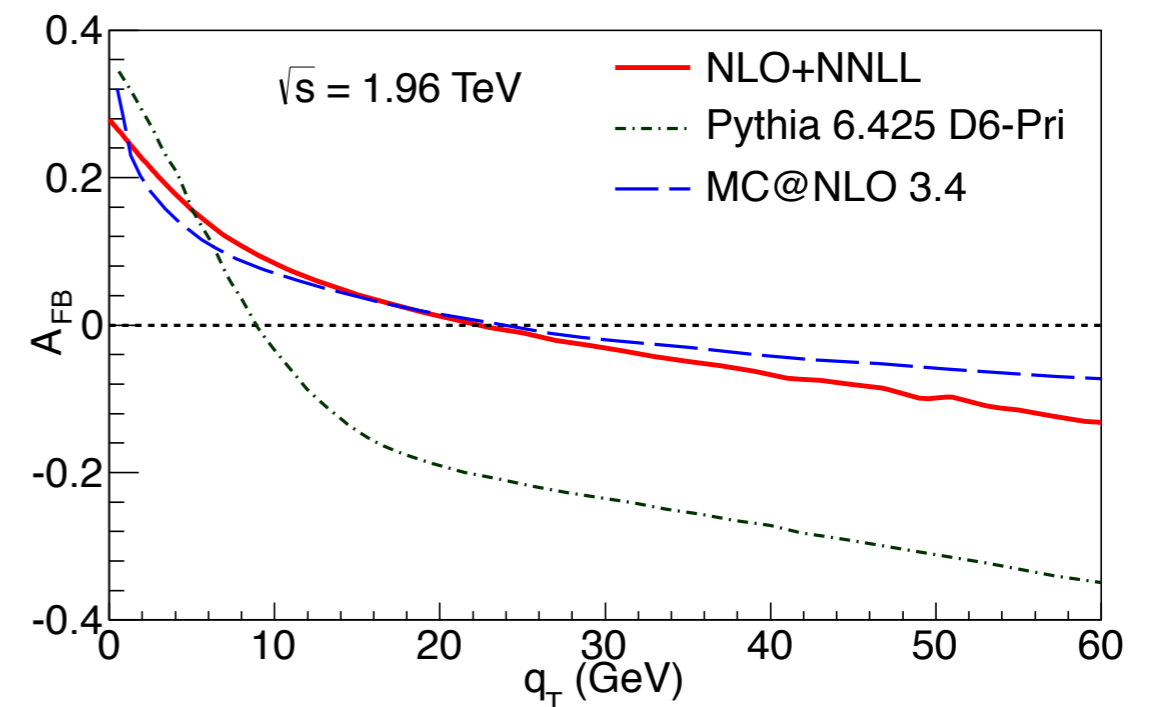
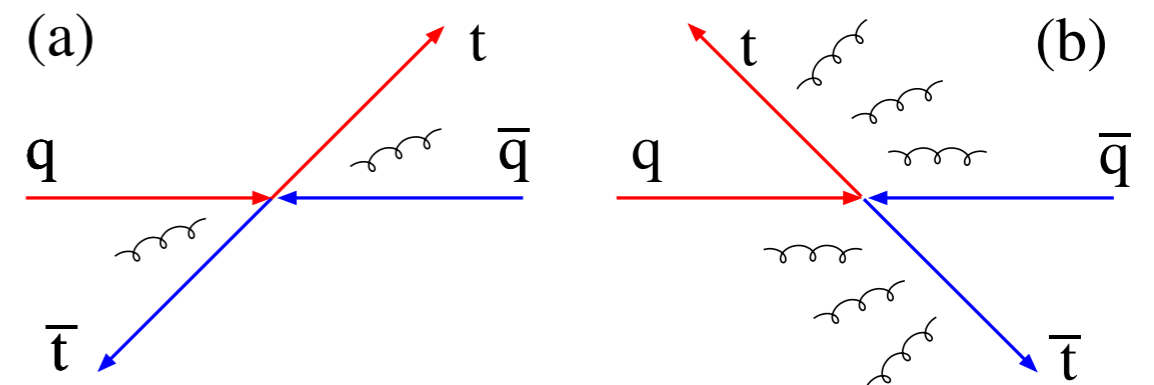
Resummed prediction

- Good perturbative convergence, significantly reduced scale dependence from NLL to NNLL
- Consistent with NLO parton shower results
- Agree well with existing data. More data required to check the shape in the low Q_T region!



Forward-backward asymmetry

- LO parton shower can generate non-zero asymmetry due to color coherence
Skands, Webber, Winter: 1205.1466
- In our framework, color coherence is built into the soft function
- Our prediction agrees well with NLO parton shower



NNLO Q_T subtraction in $t\bar{t}$ production?

$$\frac{d^4\sigma}{dQ_T^2 dy dM d\cos\theta} = \frac{\pi\beta_t}{sM} \int \frac{d^2x_\perp}{4\pi} e^{-iQ_\perp \cdot x_\perp}$$
$$\times \text{Tr} \left[\mathbf{H}(M, \cos\theta, m_t, \mu) \mathbf{S}(L_\perp, M, \cos\theta, m_t, \mu) \right]$$
$$\times \mathcal{B}(\xi_1, L_\perp, \mu) \bar{\mathcal{B}}(\xi_2, L_\perp, \mu)$$

???

Gehrmann, Lübbert, LLY
1209.0682 and work in progress

Summary

- An all-order Q_T resummation framework for top quark pair production is proposed for the first time
- Numerical results are given at NLO+NNLL accuracy
- Consistent with NLO parton shower tools and with experimental data
- May provide an alternative NNLO subtraction method for $t\bar{t}$ production
- Towards matching at NNLO

Thank you!