

# Rare Decays from Flavor to QCD and Back

- 1)  $B \rightarrow K^* \mu^+ \mu^-$  @ Low Recoil
- 2) SU(3)-ing 2-body decays of charm and CPX

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based on works with Christoph Bobeth, Danny van Dyk, Christian Hambrock, Martin Jung, Stefan Schacht, Roman Zwicky

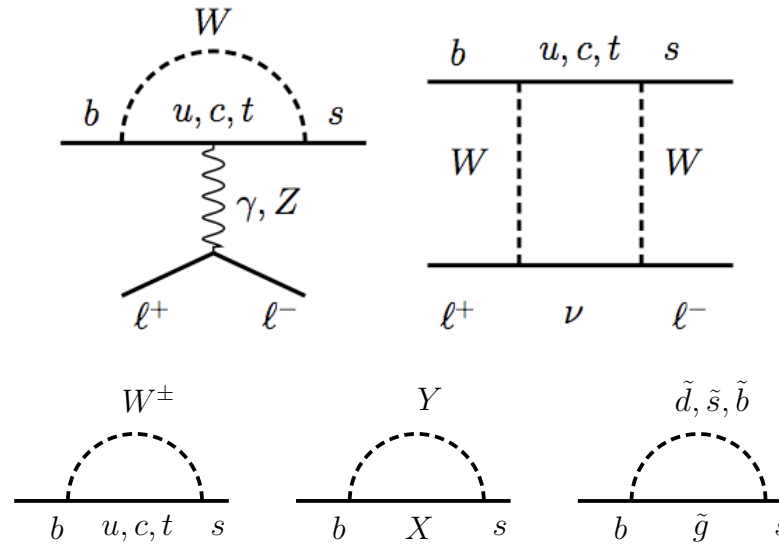
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1)

# Exclusive semileptonic FCNC $b \rightarrow s \mu^+ \mu^-$ decays

$\Delta F = 1$  FCNC; sensitive to flavor in and beyond the SM.

$$Br_{\text{SM}} \sim 10^{-6} - 10^{-7}$$



observed (at SM level):

$B \rightarrow K^{(*)} \mu^+ \mu^-$  BaBar, Belle, CDF  $6.8 \text{ fb}^{-1}$  and LHCb  $1 \text{ fb}^{-1}$  [LHCb-CONF-2012-008](#)

$B_s \rightarrow \Phi \mu^+ \mu^-$  CDF 2011 [1101.1028 \[hep-ex\]](#) LHCb 2012 [LHCb-CONF-2012-008](#)

$\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$  CDF 2011 [1107.3753 \[hep-ex\]](#)

distributions measured. precision physics started.

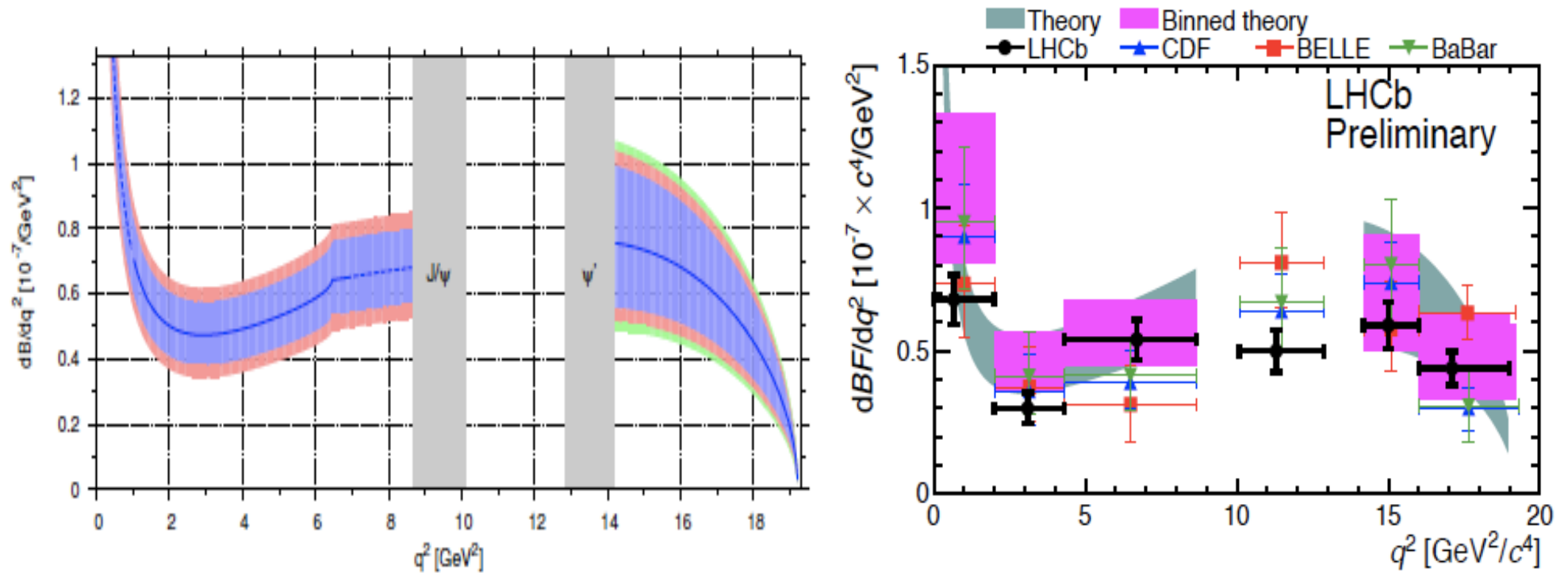
Different theory in both regions – binned data needed.

- Small dilepton mass  $q^2 \leftrightarrow$  large hadronic recoil  $E_{K^*} \gg \Lambda$   
QCD Factorization BBNS, Beneke, Feldmann, Seidel'01,04
- Large  $q^2 \sim \mathcal{O}(m_b^2) \leftrightarrow$  low hadronic recoil  $E_{K^*} \sim \Lambda$   
Operator product expansion in  $1/m_b$  Grinstein,Pirjol '04, Beylich, Buchalla,Feldmann'11

## THIS TALK:

- Low recoil  $B \rightarrow K^{(*)} \mu^+ \mu^-$  predictions, pheno & implications  
Bobeth,GH, vanDyk, Wacker '10,11,12
- Extractions of hadronic form factor ratios at low recoil from data  
GH, Hambrock '12, and in preparation together with Schacht, Zwicky

# Situation: Dilepton Mass Spectrum in $B \rightarrow K^* \mu^+ \mu^-$



left-hand Fig. from 1006.5013 [hep-ph] Blue band: form factor uncertainties, red:  $1/m_b$  right-hand Fig. from LHCb-CONF-2012-008

Biggest source of theory uncertainty: the  $B \rightarrow K^*$  form factors.

# Opportunity: Angular Analysis $B \rightarrow K^*(\rightarrow K\pi)\mu^+\mu^-$

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$$d\Gamma^4 \sim J dq^2 d \cos \Theta_l d \cos \Theta_{K^*} d\Phi \quad \text{Krüger, Sehgal, Sinha, Sinha hep-ph/9907386}$$

$$\begin{aligned} J(q^2, \theta_l, \theta_{K^*}, \phi) = & J_1^s \sin^2 \theta_{K^*} + J_1^c \cos^2 \theta_{K^*} + (J_2^s \sin^2 \theta_{K^*} + J_2^c \cos^2 \theta_{K^*}) \cos 2\theta_l \\ & + J_3 \sin^2 \theta_{K^*} \sin^2 \theta_l \cos 2\phi + J_4 \sin 2\theta_{K^*} \sin 2\theta_l \cos \phi + J_5 \sin 2\theta_{K^*} \sin \theta_l \cos \phi \\ & + J_6 \sin^2 \theta_{K^*} \cos \theta_l + J_7 \sin 2\theta_{K^*} \sin \theta_l \sin \phi \\ & + J_8 \sin 2\theta_{K^*} \sin 2\theta_l \sin \phi + J_9 \sin^2 \theta_{K^*} \sin^2 \theta_l \sin 2\phi, \end{aligned} \quad (2.3)$$

$\Theta_l$ : angle between  $l^-$  and  $\bar{B}$  in dilepton-CMS

$\Theta_{K^*}$ : angle between K and  $\bar{B}$  in  $K^*$ -CMS

$\Phi$ : angle between normals of the  $K\pi$  and  $l^+l^-$  planes

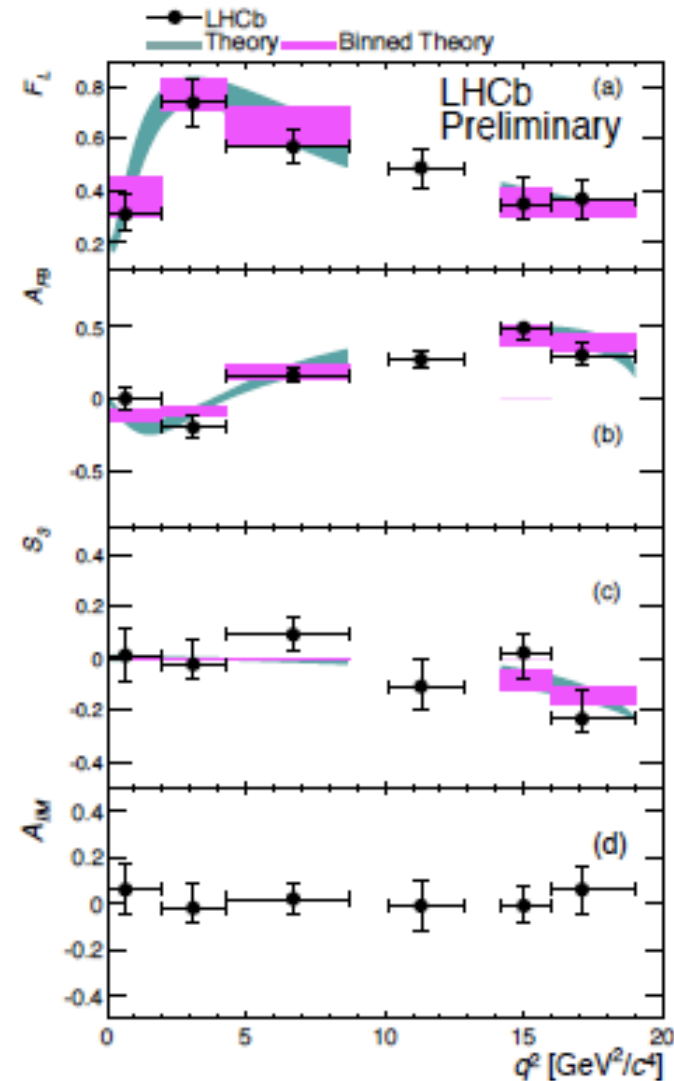
complex structure, plenty of observables, not all need full  $d^4\Gamma$ .

$$\Gamma \sim J_1 - J_2/3, \quad A_{\text{FB}} \sim J_6, \quad A_T^{(2)} \sim J_3 \quad \text{Krüger, Matias hep-ph/0502060}$$

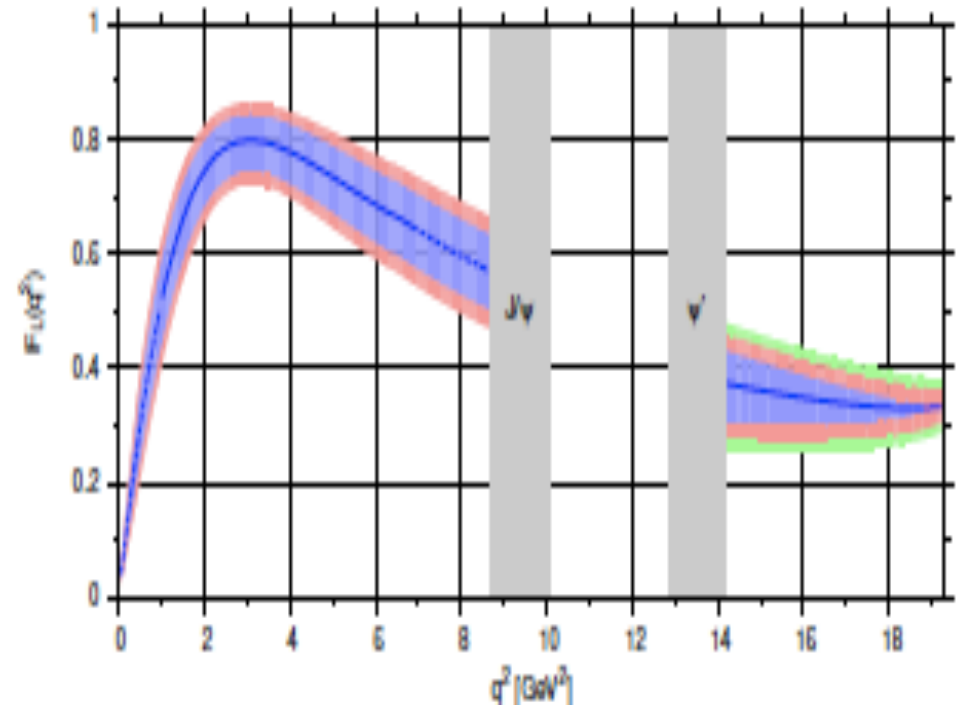
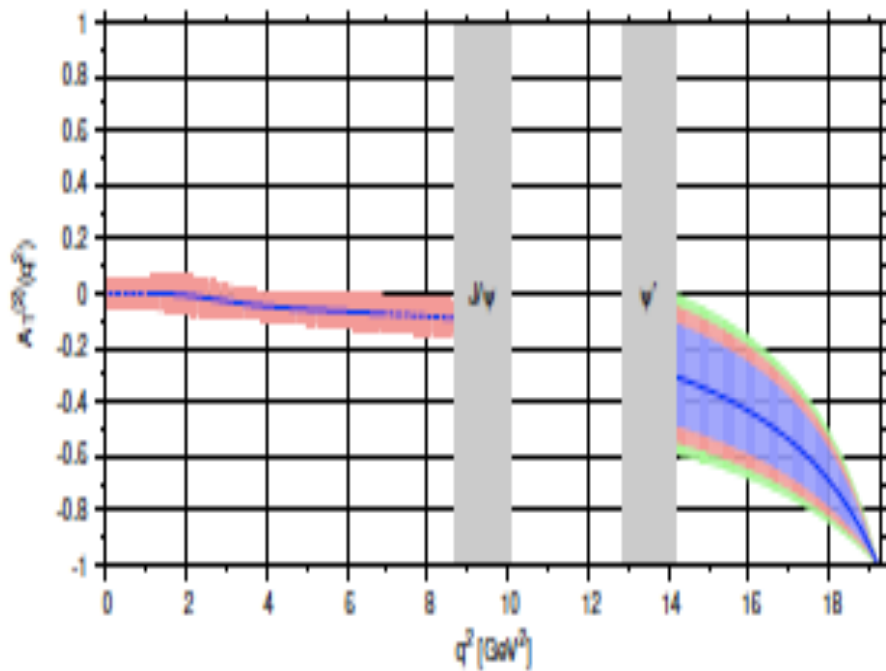
With full  $\Delta B = 1$  dimension six operators: [Bobeth et al, 1212.2321 \[hep-ph\]](#)

## $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ Angular Analysis Results

- 4D fit to 3 angles and mass
- Larger data sample enables measurements of  $S_3$  and  $A_{IM}$
- Error bars include systematic uncertainties
- Data points at average  $q^2$  of signal candidates in data
- These are the **most precise measurements** to-date [preliminary]
- The results are consistent with the SM prediction [1]



# $A_T^2$ and $F_L$ in $B \rightarrow K^* \mu^+ \mu^-$



Figs. from 1006.5013 [hep-ph] Blue band: form factor uncertainties, red:  $1/m_b A_T^{(2)} = 2S_3/(1 - F_L)$

$F_L$ : fraction of longitudinally polarized  $K^*$

$A_T^{(2)}$ : transverse Asymmetry; Null test of SM at low  $q^2$

Both probe form factor ratios at low recoil! pollution from BSM right-handed currents can be

controlled by e.g.  $A_T^{(2)}$  @large recoil; currently  $\lesssim 30\%$  Bobeth et al '12



# $A_T^2$ and $F_L$ in $B \rightarrow K^* \mu^+ \mu^-$ data 2012

| $q^2$ [GeV <sup>2</sup> ] | BaBar                  | CDF                    |                         | LHCb                   |                         |
|---------------------------|------------------------|------------------------|-------------------------|------------------------|-------------------------|
|                           | $F_L$                  | $F_L$                  | $A_T^{(2)}$             | $F_L$                  | $A_T^{(2)}$             |
| [14.18, 16]               | $0.43^{+0.13}_{-0.16}$ | $0.40^{+0.12}_{-0.12}$ | $0.11^{+0.65}_{-0.65}$  | $0.35^{+0.10}_{-0.06}$ | $0.06^{+0.24}_{-0.29}$  |
| [16, 19.xx]               | $0.55^{+0.15}_{-0.17}$ | $0.19^{+0.14}_{-0.13}$ | $-0.57^{+0.60}_{-0.57}$ | $0.37^{+0.07}_{-0.08}$ | $-0.75^{+0.35}_{-0.20}$ |

# Benefits of $B \rightarrow K^*$ at low recoil

At low hadronic recoil transversity amplitudes  $A_i^{L,R}$ ,  $i = \perp, \parallel, 0$  related:

$$A_i^{L,R} \propto C^{L,R} \cdot f_i$$

$C^{L,R}$ : universal short-dist.-physics;  $C^{L,R} = (C_9^{\text{eff}} \mp C_{10}) + \kappa \frac{2\hat{m}_b}{\hat{s}} C_7^{\text{eff}}$

$1/m_b$ - corrections parametrically suppressed  $\sim \alpha_s/m_b, C_7/C_9 1/m_b$

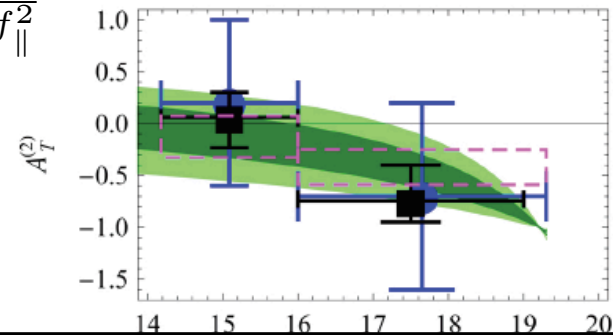
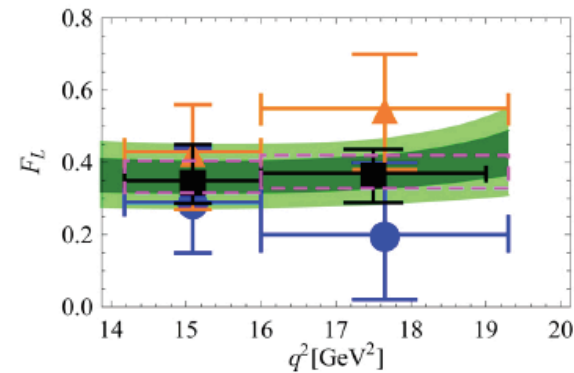
$f_i$ : form factors

$C^{L,R}$  drops

out in ratios:

$$F_L = \frac{|A_0^L|^2 + |A_0^R|^2}{\sum_{X=L,R} (|A_0^X|^2 + |A_\perp^X|^2 + |A_\parallel^X|^2)} = \frac{f_0^2}{f_0^2 + f_\perp^2 + f_\parallel^2}$$

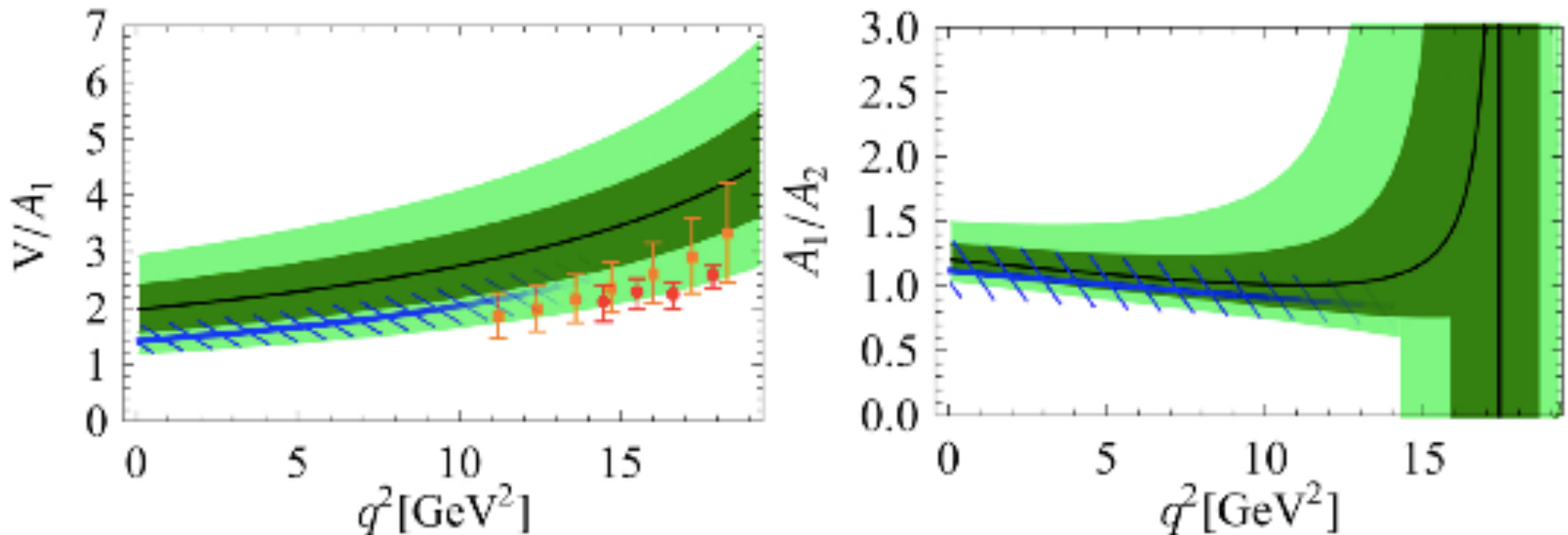
$$A_T^{(2)} = \frac{|A_\perp^L|^2 + |A_\perp^R|^2 - |A_\parallel^L|^2 - |A_\parallel^R|^2}{|A_\perp^L|^2 + |A_\perp^R|^2 + |A_\parallel^L|^2 + |A_\parallel^R|^2} = \frac{f_\perp^2 - f_\parallel^2}{f_\perp^2 + f_\parallel^2}$$



# Extracting $B \rightarrow K^*$ form factors from data

Using series expansion  $\hat{f}_i(t) = \frac{(\sqrt{-z(t,0)})^m (\sqrt{z(t,t_-)})^l}{B(t) \varphi_f(t)} \sum_k \alpha_{i,k} z^k(t)$

best-fit results:  $\alpha_{\parallel}/\alpha_{\perp} = 0.43_{-0.08}^{+0.11}$ ,  $\alpha_0/\alpha_{\perp} = 0.15_{-0.02}^{+0.03}$



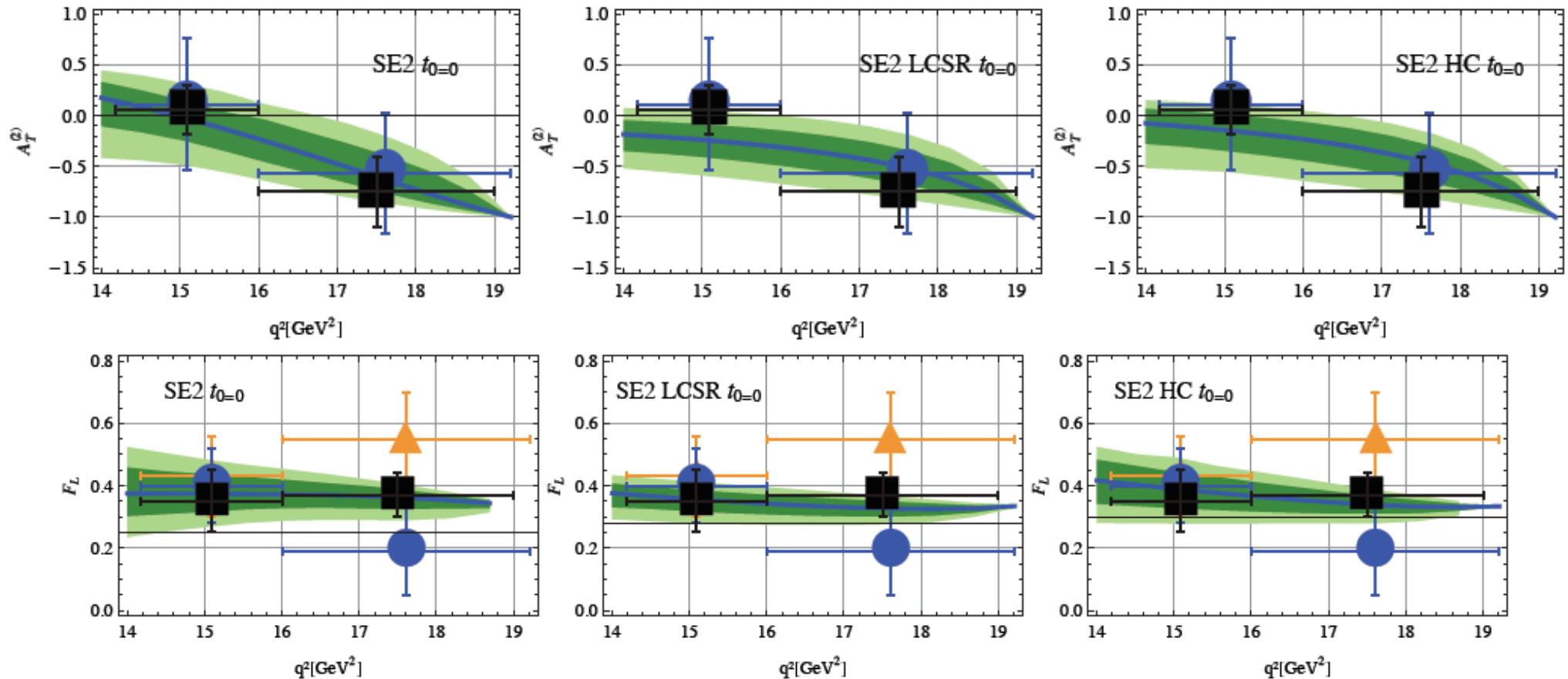
Yellow, red points; lattice QCD; blue bands: QCD sum rules Ball, Zwicky '05; green bands: 1, 2 $\sigma$  fit [1204.4444 \[hep-ph\]](https://arxiv.org/abs/1204.4444)

Consistency between data (loreco-OPE), LCSR (small  $q^2$ ) and lattice (large  $q^2$ )!

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1. Its great to have (even more) data.
  2. With (even one) more bins the sensitivity in the fits to the  $q^2$ -shape increases.
  3. If you (lattice, sum rules,..) calculate form factors, please provide also ratios (with uncertainties).
  4. Data-extracted form factor ratios constitute benchmarks for lattice form factor estimations at low recoil.

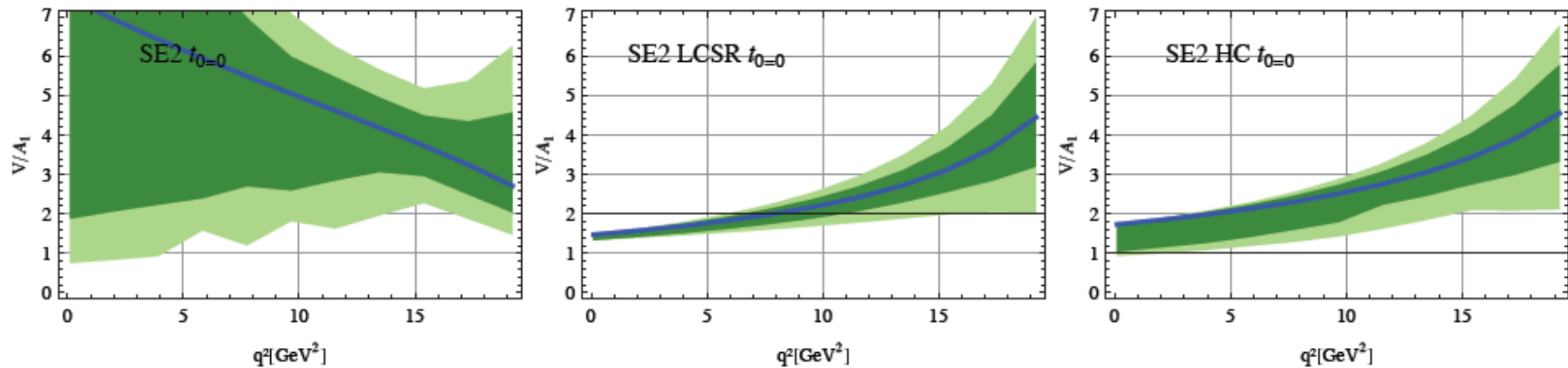
# Advances in ... Extracting $B \rightarrow K^*$ form factors

Higher order Series Expansion; use theory input from low  $q^2$ : LCSR  
(sum rules) or  $V(0)/A_1(0) = (m_B + m_{K^*})^2 / (2m_B E_{K^*}) + \mathcal{O}(1/m_b) = 1.33 \pm 0.4$  (HC)



Fit ok with (mid: LCSR, right: HC) or without (left) low  $q^2$ -input.

# Advances in ... Extracting $B \rightarrow K^*$ form factors



Predictivity at low  $q^2$  is obtained from low  $q^2$  input. (Required at higher order) Preliminary – Hambrock, GH, Schacht, Zwicky '13 in preparation

Data-extracted form factor ratios constitute benchmark for lattice form factor estimations at low recoil.

# Exploiting $B \rightarrow K^* l^+ l^-$ at low recoil further

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OPE in  $1/Q$ ,  $Q = \{m_b, \sqrt{q^2}\}$  by Grinstein, Pirjol '04 with heavy quark FF relations  $T_{1,2,3} \leftrightarrow V, A_{1,2}$  leads to simply transversity structure with universal short-distance  $C$  and form factor coefficients  $f_i$

$$A_i^{L,R} \propto C^{L,R} \cdot f_i$$

up to corrections of order  $\alpha_s \Lambda/m_b$  and  $(C_7/C_9)\Lambda/m_b$  (few percent).

Allows to design new observables which are Bobeth, GH, vanDyk 1006.5013, and '11,'12

– independent of form factors ( $H_T^{(2,3,4,5)}$ )

– independent of short-distance coefficients and test the form factors

– independent of either ones and test the theoretical low recoil

framework  $H_T^{(1)}, H_T^{(2)} / H_T^{(3)}, H_T^{(4)} / H_T^{(5)}$

# Exploiting $B \rightarrow K^* l^+ l^-$ at low recoil further

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$$H_T^{(1)} = \frac{\text{Re}(A_0^L A_{\parallel}^{L*} + A_0^{R*} A_{\parallel}^R)}{\sqrt{(|A_0^L|^2 + |A_0^R|^2)(|A_{\parallel}^L|^2 + |A_{\parallel}^R|^2)}} = \frac{\sqrt{2}J_4}{\sqrt{-J_2^c(2J_2^s - J_3)}},$$
$$H_T^{(2)} = \frac{\text{Re}(A_0^L A_{\perp}^{L*} - A_0^{R*} A_{\perp}^R)}{\sqrt{(|A_0^L|^2 + |A_0^R|^2)(|A_{\perp}^L|^2 + |A_{\perp}^R|^2)}} = \frac{\beta_l J_5}{\sqrt{-2J_2^c(2J_2^s + J_3)}},$$
$$H_T^{(3)} = \frac{\text{Re}(A_{\parallel}^L A_{\perp}^{L*} - A_{\parallel}^{R*} A_{\perp}^R)}{\sqrt{(|A_{\parallel}^L|^2 + |A_{\parallel}^R|^2)(|A_{\perp}^L|^2 + |A_{\perp}^R|^2)}} = \frac{\beta_l J_6}{2\sqrt{(2J_2^s)^2 - J_3^2}}.$$

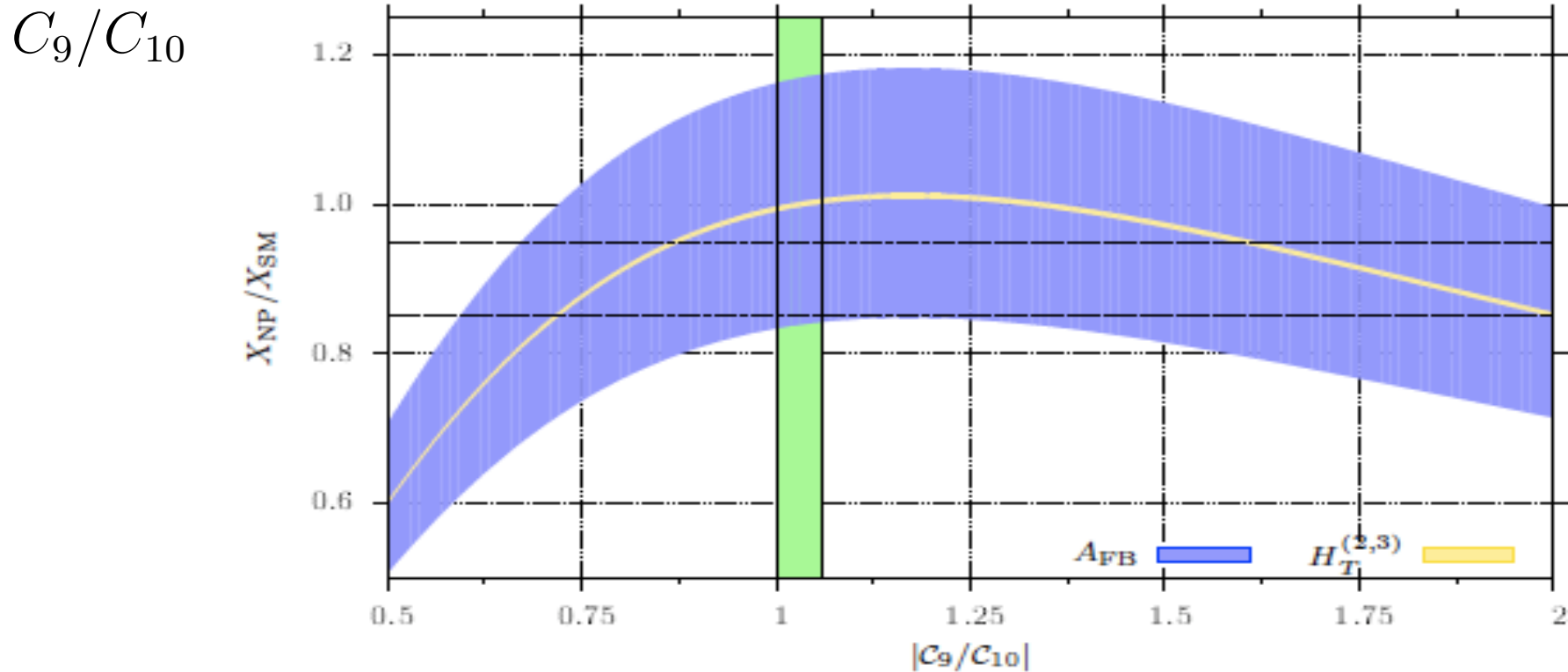
Low recoil Heavy-quark-OPE:  $H_T^{(1)} = 1$ ,  $H_T^{(2)} / H_T^{(3)} = 1$ .

Extract them from the  $B \rightarrow K^*(\rightarrow K\pi)\mu^+\mu^-$  angular distribution.



# Further Benefits of $B \rightarrow K^* l^+ l^-$ at low recoil: BSM

Reach in low recoil-integrated observables vs Wilson coefficients



green: SM; blue:  $A_{FB}$  ( $f_i$ -dependent) gold:  $H_T^{(2)}$  ( $f_i$ -free)

Fig from 1212.2321

# Further Benefits of $B \rightarrow K^* l^+ l^-$ at low recoil: BSM-CP

Reach in low recoil-integrated CP-asymmetries vs Wilson coefficients  $C'_{10}$

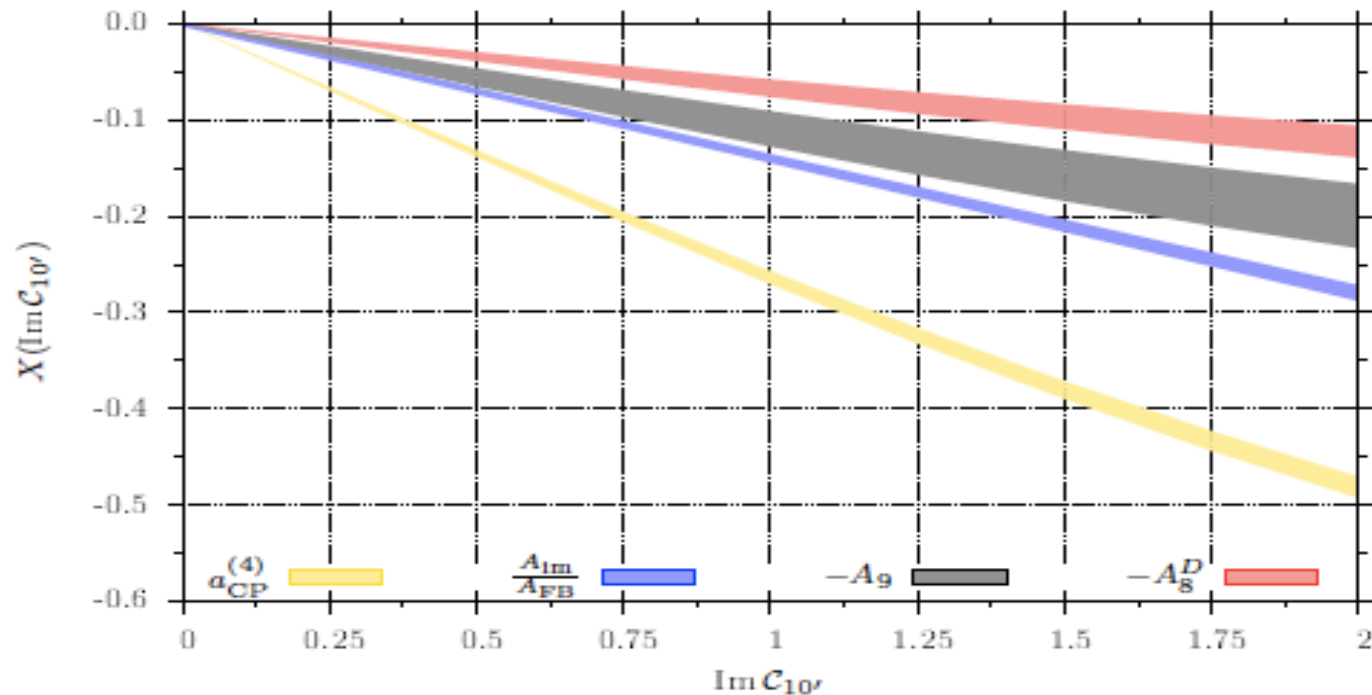


Fig from 1212.2321

gold: CP-asymmetry of  $H_T^{(4)}$ ; blue  $A_{im}/A_{FB} = J_9/J_{2s} \sim H_T^{(5)}/H_T^{(3)}$ : both  $f_i$ -free; other two  $A_{8,9}$  not

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2)

$$\Delta A_{CP} = A_{CP}(D^0 \rightarrow K^+ K^-) - A_{CP}(D^0 \rightarrow \pi^+ \pi^-)$$

$$\Delta A_{CP}^{wa} = -0.00678 \pm 0.00147 \text{ (pre-Moriond QCD 2013)}$$

$$\Delta A_{CP}^{SM} \sim \lambda^4 \times P/T \simeq 10^{-3} \times P/T; P/T \sim "0.x";$$

" $\Delta A_{CP}^{SM}$  is below permille " (traditional)

Are the data consistent with the SM? (large number of th papers)

# Many Modes Measured

TABLE II. The observables and the data for indirect  $CP$  violation used in this work; see Appendix A for removal of effects from charm and kaon mixing.

| Observable  | Measurement                         | References               |
|---|-------------------------------------|--------------------------|
| SCS $CP$ asymmetries  |                                     |                          |
| $\Delta a_{CP}^{\text{dir}}(K^+ K^-, \pi^+ \pi^-)$              | $-0.00678 \pm 0.00147$              | [1–4,28,29]              |
| $\Sigma a_{CP}^{\text{dir}}(K^+ K^-, \pi^+ \pi^-)$              | $+0.0014 \pm 0.0039$                | <sup>a</sup> [1–3,28,30] |
| $A_{CP}(D^0 \rightarrow K_S K_S)$                               | $-0.23 \pm 0.19$                    | [31]                     |
| $A_{CP}(D^0 \rightarrow \pi^0 \pi^0)$                           | $+0.001 \pm 0.048$                  | [31]                     |
| $A_{CP}(D^+ \rightarrow \pi^0 \pi^+)$                           | $+0.029 \pm 0.029$                  | [32]                     |
| $A_{CP}(D^+ \rightarrow K_S K^+)$                               | $-0.0011 \pm 0.0025$                | [32–35]                  |
| $A_{CP}(D_s \rightarrow K_S \pi^+)$                             | $+0.031 \pm 0.015$                  | <sup>a</sup> [32,33,36]  |
| $A_{CP}(D_s \rightarrow K^+ \pi^0)$                             | $+0.266 \pm 0.228$                  | [32]                     |
| Indirect $CP$ violation   |                                     |                          |
| $a_{CP}^{\text{ind}}$   | $(-0.027 \pm 0.163) \times 10^{-2}$ | [4]                      |
| $\delta_L \equiv 2\text{Re}(\varepsilon)/(1 +  \varepsilon ^2)$ | $(3.32 \pm 0.06) \times 10^{-3}$    | [37]                     |
| $K^+ \pi^-$ strong phase difference                             |                                     |                          |
| $\delta_{K\pi}$   | $21.4^\circ \pm 10.4^\circ$         | <sup>b</sup> [4]         |
| SCS branching ratios  |                                     |                          |
| $\mathcal{B}(D^0 \rightarrow K^+ K^-)$                          | $(3.96 \pm 0.08) \times 10^{-3}$    | [37]                     |
| $\mathcal{B}(D^0 \rightarrow \pi^+ \pi^-)$                      | $(1.401 \pm 0.027) \times 10^{-3}$  | [37]                     |
| $\mathcal{B}(D^0 \rightarrow K_S K_S)$                          | $(0.17 \pm 0.04) \times 10^{-3}$    | [37]                     |
| $\mathcal{B}(D^0 \rightarrow \pi^0 \pi^0)$                      | $(0.80 \pm 0.05) \times 10^{-3}$    | [37]                     |
| $\mathcal{B}(D^+ \rightarrow \pi^0 \pi^+)$                      | $(1.19 \pm 0.06) \times 10^{-3}$    | [37]                     |
| $\mathcal{B}(D^+ \rightarrow K_S K^+)$                          | $(2.83 \pm 0.16) \times 10^{-3}$    | [37]                     |
| $\mathcal{B}(D_s \rightarrow K_S \pi^+)$                        | $(1.21 \pm 0.08) \times 10^{-3}$    | [37]                     |
| $\mathcal{B}(D_s \rightarrow K^+ \pi^0)$                        | $(0.62 \pm 0.21) \times 10^{-3}$    | [37]                     |
| CF <sup>c</sup> branching ratios                                |                                     |                          |
| $\mathcal{B}(D^0 \rightarrow K^- \pi^+)$                        | $(3.88 \pm 0.05) \times 10^{-2}$    | [37]                     |
| $\mathcal{B}(D^0 \rightarrow K_S \pi^0)$                        | $(1.19 \pm 0.04) \times 10^{-2}$    | [37]                     |
| $\mathcal{B}(D^0 \rightarrow K_L \pi^0)$                        | $(1.00 \pm 0.07) \times 10^{-2}$    | [37]                     |
| $\mathcal{B}(D^+ \rightarrow K_S \pi^+)$                        | $(1.47 \pm 0.07) \times 10^{-2}$    | [37]                     |
| $\mathcal{B}(D^+ \rightarrow K_L \pi^+)$                        | $(1.46 \pm 0.05) \times 10^{-2}$    | [37]                     |
| $\mathcal{B}(D_s \rightarrow K_S K^+)$                          | $(1.45 \pm 0.05) \times 10^{-2}$    | <sup>a</sup> [37,38]     |
| DCS branching ratios  |                                     |                          |
| $\mathcal{B}(D^0 \rightarrow K^+ \pi^-)$                        | $(1.47 \pm 0.07) \times 10^{-4}$    | [37]                     |
| $\mathcal{B}(D^+ \rightarrow K^+ \pi^0)$                        | $(1.83 \pm 0.26) \times 10^{-4}$    | [37]                     |

<sup>a</sup>The measurement quoted corresponds to our average. Systematic and statistical uncertainties are added in quadrature.

<sup>b</sup>Our symmetrization of uncertainties.

<sup>c</sup>Modes into  $K_{S,L}$  assigned to CF decays.

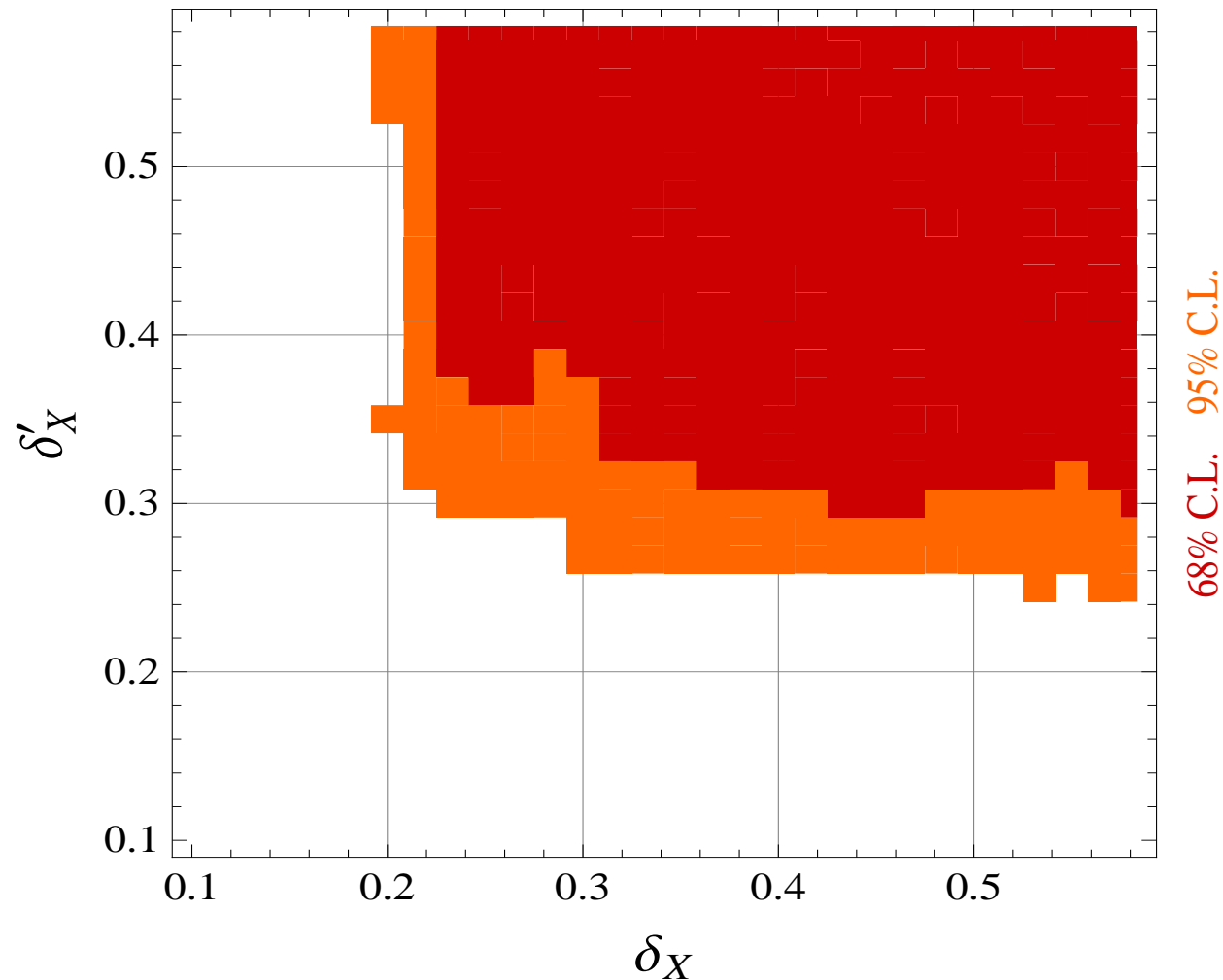
# SU(3)-ing Charm

| Decay $d$                         | $B_1^{3_1}$             | $B_1^{3_2}$            | $B_8^{3_1}$            | $B_8^{3_2}$             | $B_8^{0_1}$            | $B_8^{0_2}$             | $B_8^{15_1}$               | $B_8^{15_2}$             | $B_8^{15_3}$            | $B_{27}^{15_1}$                  | $B_{27}^{15_2}$                   | $B_{27}^{15_3}$        | $B_{27}^{24_1}$              | $B_{27}^{24_2}$         | $B_{27}^{42}$                 |
|-----------------------------------|-------------------------|------------------------|------------------------|-------------------------|------------------------|-------------------------|----------------------------|--------------------------|-------------------------|----------------------------------|-----------------------------------|------------------------|------------------------------|-------------------------|-------------------------------|
| SCS                               |                         |                        |                        |                         |                        |                         |                            |                          |                         |                                  |                                   |                        |                              |                         |                               |
| $D^0 \rightarrow K^+ K^-$         | $\frac{1}{4\sqrt{10}}$  | $\frac{1}{8}$          | $\frac{1}{10\sqrt{2}}$ | $\frac{1}{4\sqrt{5}}$   | $\frac{1}{10}$         | $-\frac{1}{10\sqrt{2}}$ | $-\frac{7}{10\sqrt{122}}$  | $\frac{\sqrt{3}}{5}$     | $-\frac{1}{20}$         | $-\frac{31}{20\sqrt{122}}$       | $-\frac{17}{20\sqrt{366}}$        | $\frac{7}{40}$         | $-\frac{1}{10\sqrt{6}}$      | $\frac{1}{10\sqrt{2}}$  | $-\frac{13}{20\sqrt{42}}$     |
| $D^0 \rightarrow \pi^+ \pi^-$     | $\frac{1}{4\sqrt{10}}$  | $\frac{1}{8}$          | $\frac{1}{10\sqrt{2}}$ | $\frac{1}{4\sqrt{5}}$   | $-\frac{1}{10}$        | $\frac{1}{10\sqrt{2}}$  | $-\frac{11}{10\sqrt{122}}$ | $-\frac{2\sqrt{2}}{5}$   | $\frac{3}{20}$          | $-\frac{23}{20\sqrt{122}}$       | $\frac{11}{20\sqrt{366}}$         | $-\frac{1}{40}$        | $\frac{1}{10\sqrt{6}}$       | $-\frac{1}{10\sqrt{2}}$ | $\frac{\sqrt{2}}{20}$         |
| $D^0 \rightarrow \bar{K}^0 K^0$   | $-\frac{1}{4\sqrt{10}}$ | $-\frac{1}{8}$         | $\frac{1}{5\sqrt{2}}$  | $\frac{1}{2\sqrt{5}}$   | 0                      | 0                       | $-\frac{9}{5\sqrt{122}}$   | $-\frac{1}{5\sqrt{366}}$ | $\frac{1}{10}$          | $-\frac{9}{20\sqrt{122}}$        | $-\frac{1}{20\sqrt{366}}$         | $\frac{1}{40}$         | $-\frac{1}{2\sqrt{6}}$       | $-\frac{1}{2\sqrt{2}}$  | $\frac{19}{20\sqrt{42}}$      |
| $D^0 \rightarrow \pi^0 \pi^0$     | $-\frac{1}{8\sqrt{5}}$  | $-\frac{1}{8\sqrt{2}}$ | $-\frac{1}{20}$        | $-\frac{1}{4\sqrt{10}}$ | $\frac{1}{10\sqrt{2}}$ | $-\frac{1}{20}$         | $\frac{11}{20\sqrt{61}}$   | $\frac{2}{5\sqrt{183}}$  | $-\frac{3}{20\sqrt{2}}$ | $-\frac{57}{40\sqrt{61}}$        | $\frac{7}{20\sqrt{183}}$          | $\frac{1}{40\sqrt{2}}$ | $\frac{1}{5\sqrt{3}}$        | $\frac{1}{20}$          | $-\frac{1}{20\sqrt{21}}$      |
| $D^+ \rightarrow \pi^0 \pi^+$     | 0                       | 0                      | 0                      | 0                       | 0                      | 0                       | 0                          | 0                        | 0                       | $-\frac{2(1-\Delta)}{\sqrt{61}}$ | $\frac{5(1-\Delta)}{8\sqrt{183}}$ | 0                      | $\frac{1-\Delta}{4\sqrt{3}}$ | 0                       | $\frac{1-\Delta}{8\sqrt{21}}$ |
| $D^+ \rightarrow \bar{K}^0 K^+$   | 0                       | 0                      | $\frac{3}{10\sqrt{2}}$ | $\frac{3}{4\sqrt{5}}$   | $\frac{1}{10}$         | $-\frac{1}{10\sqrt{2}}$ | $\frac{7}{10\sqrt{122}}$   | $-\frac{\sqrt{3}}{5}$    | $\frac{1}{20}$          | $-\frac{3\sqrt{2}}{5}$           | $-\frac{23}{20\sqrt{366}}$        | $\frac{1}{5}$          | $-\frac{1}{10\sqrt{6}}$      | $-\frac{\sqrt{2}}{5}$   | $-\frac{19}{20\sqrt{42}}$     |
| $D_s \rightarrow K^0 \pi^+$       | 0                       | 0                      | $\frac{3}{10\sqrt{2}}$ | $\frac{3}{4\sqrt{5}}$   | $-\frac{1}{10}$        | $\frac{1}{10\sqrt{2}}$  | $\frac{11}{10\sqrt{122}}$  | $\frac{2\sqrt{2}}{5}$    | $-\frac{3}{20}$         | $-\frac{3}{5\sqrt{122}}$         | $\frac{19}{20\sqrt{366}}$         | $-\frac{1}{10}$        | $-\frac{\sqrt{2}}{5}$        | $-\frac{1}{10\sqrt{2}}$ | $-\frac{19}{20\sqrt{42}}$     |
| $D_s \rightarrow K^+ \pi^0$       | 0                       | 0                      | $-\frac{3}{20}$        | $-\frac{3}{4\sqrt{10}}$ | $\frac{1}{10\sqrt{2}}$ | $-\frac{1}{20}$         | $-\frac{11}{20\sqrt{61}}$  | $-\frac{2}{5\sqrt{183}}$ | $\frac{3}{20\sqrt{2}}$  | $-\frac{17}{10\sqrt{61}}$        | $\frac{\sqrt{61}}{20}$            | $\frac{1}{10\sqrt{2}}$ | $-\frac{\sqrt{3}}{10}$       | $\frac{1}{20}$          | $-\frac{\sqrt{4}}{20}$        |
| CF                                |                         |                        |                        |                         |                        |                         |                            |                          |                         |                                  |                                   |                        |                              |                         |                               |
| $D^0 \rightarrow K^- \pi^+$       | 0                       | 0                      | 0                      | 0                       | $\frac{1}{5}$          | $\frac{1}{5\sqrt{2}}$   | $-\frac{\sqrt{61}}{5}$     | $-\frac{7}{5\sqrt{366}}$ | $-\frac{1}{5}$          | $\frac{\sqrt{61}}{5}$            | $\frac{7}{5\sqrt{366}}$           | $\frac{1}{5}$          | $\frac{1}{20\sqrt{6}}$       | $\frac{1}{20\sqrt{2}}$  | $-\frac{1}{2\sqrt{42}}$       |
| $D^0 \rightarrow \bar{K}^0 \pi^0$ | 0                       | 0                      | 0                      | 0                       | $-\frac{1}{5\sqrt{2}}$ | $-\frac{1}{10}$         | $\frac{1}{5\sqrt{61}}$     | $\frac{7}{10\sqrt{183}}$ | $\frac{1}{5\sqrt{2}}$   | $\frac{3}{10\sqrt{61}}$          | $\frac{7\sqrt{61}}{20}$           | $\frac{3}{10\sqrt{2}}$ | $-\frac{\sqrt{3}}{20}$       | $-\frac{3}{20}$         | 0                             |
| $D^+ \rightarrow \bar{K}^0 \pi^+$ | 0                       | 0                      | 0                      | 0                       | 0                      | 0                       | 0                          | 0                        | 0                       | $\frac{1}{\sqrt{122}}$           | $\frac{7}{2\sqrt{366}}$           | $\frac{1}{2}$          | $-\frac{1}{4\sqrt{6}}$       | $-\frac{1}{4\sqrt{2}}$  | $-\frac{1}{2\sqrt{42}}$       |
| $D_s \rightarrow \bar{K}^0 K^+$   | 0                       | 0                      | 0                      | 0                       | $-\frac{1}{5}$         | $-\frac{1}{5\sqrt{2}}$  | $-\frac{\sqrt{61}}{5}$     | $-\frac{7}{5\sqrt{366}}$ | $-\frac{1}{5}$          | $\frac{\sqrt{61}}{5}$            | $\frac{7}{5\sqrt{366}}$           | $\frac{1}{5}$          | $\frac{1}{5\sqrt{6}}$        | $\frac{1}{5\sqrt{2}}$   | $\frac{1}{\sqrt{42}}$         |
| DCS                               |                         |                        |                        |                         |                        |                         |                            |                          |                         |                                  |                                   |                        |                              |                         |                               |
| $D^0 \rightarrow K^+ \pi^-$       | 0                       | 0                      | 0                      | 0                       | 0                      | $-\frac{\sqrt{2}}{5}$   | $\frac{2\sqrt{61}}{5}$     | $\frac{7\sqrt{183}}{5}$  | 0                       | $-\frac{2\sqrt{2}}{5}$           | $-\frac{7\sqrt{183}}{5}$          | 0                      | $-\frac{1}{4\sqrt{6}}$       | $\frac{3}{20\sqrt{2}}$  | $-\frac{1}{2\sqrt{42}}$       |
| $D^0 \rightarrow K^0 \pi^0$       | 0                       | 0                      | 0                      | 0                       | 0                      | $\frac{1}{5}$           | $-\frac{2}{5\sqrt{61}}$    | $-\frac{7}{5\sqrt{183}}$ | 0                       | $-\frac{3}{5\sqrt{61}}$          | $-\frac{7\sqrt{61}}{10}$          | 0                      | $-\frac{\sqrt{3}}{8}$        | $-\frac{3}{40}$         | 0                             |
| $D^+ \rightarrow K^0 \pi^+$       | 0                       | 0                      | 0                      | 0                       | 0                      | $\frac{\sqrt{2}}{5}$    | $\frac{2\sqrt{61}}{5}$     | $\frac{7\sqrt{183}}{5}$  | 0                       | $-\frac{2\sqrt{2}}{5}$           | $-\frac{7\sqrt{183}}{5}$          | 0                      | $-\frac{1}{4\sqrt{6}}$       | $-\frac{3}{20\sqrt{2}}$ | $-\frac{1}{2\sqrt{42}}$       |
| $D^+ \rightarrow K^+ \pi^0$       | 0                       | 0                      | 0                      | 0                       | 0                      | $-\frac{1}{5}$          | $-\frac{2}{5\sqrt{61}}$    | $-\frac{7}{5\sqrt{183}}$ | 0                       | $-\frac{3}{5\sqrt{61}}$          | $-\frac{7\sqrt{61}}{10}$          | 0                      | $-\frac{\sqrt{3}}{8}$        | $\frac{3}{40}$          | 0                             |
| $D_s \rightarrow K^0 K^+$         | 0                       | 0                      | 0                      | 0                       | 0                      | 0                       | 0                          | 0                        | 0                       | $-\frac{\sqrt{2}}{5}$            | $-\frac{7}{\sqrt{366}}$           | 0                      | $\frac{1}{2\sqrt{6}}$        | 0                       | $\frac{1}{\sqrt{42}}$         |

To linear  $SU(3)$ -Xing, 13 complex matrix elements.

Table from 1211.3734; Previous  $SU(3)$  works: Quigg'80, Pirtskhalava,Uttayara

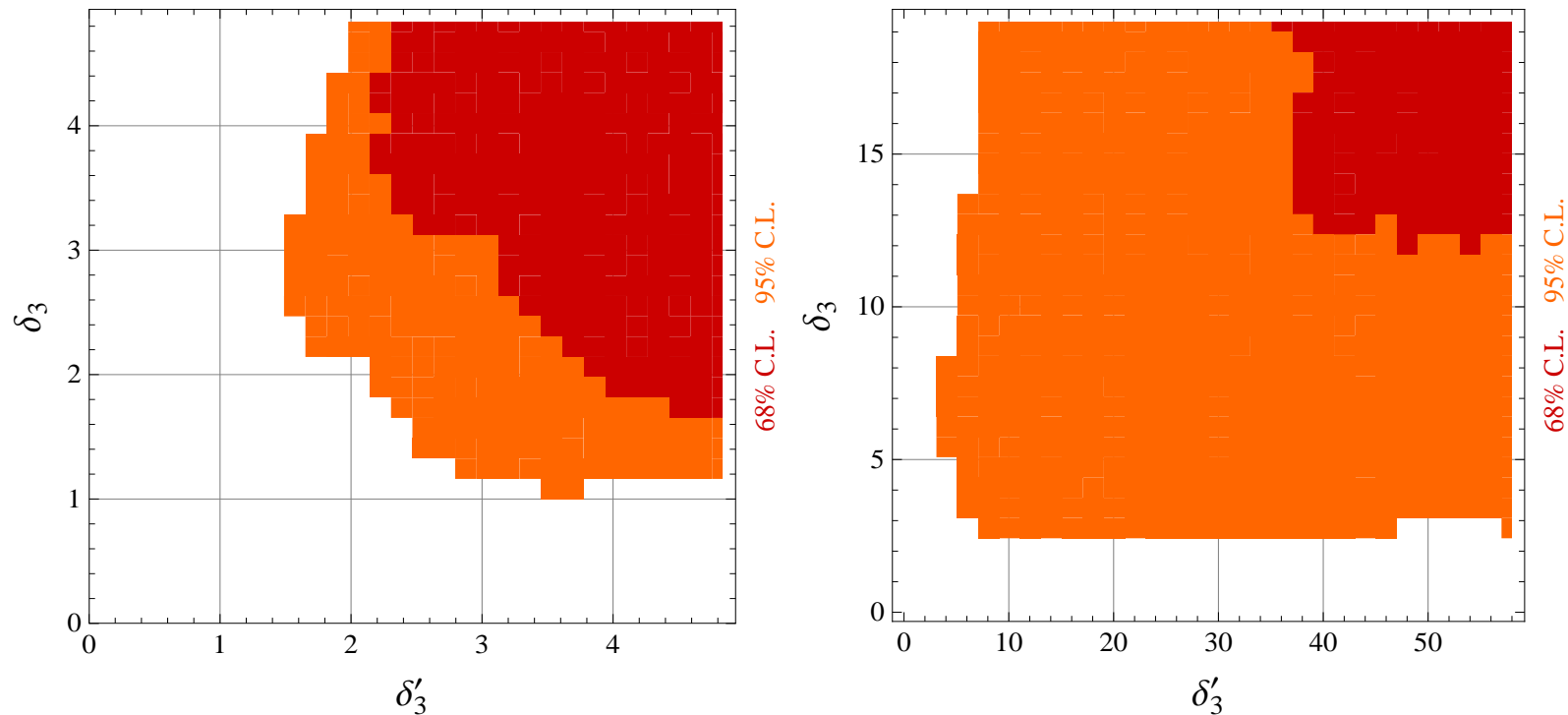
# Does the SU(3)-expansion makes sense in Charm?



Fit works with SU(3)-Xing of order 30 %. [Fig from 1211.3734](#)

$\delta_X$ : max ratio matrix elements;  $\delta'_X$ : max ratio decay amplitudes.

# Penguin enhancement?

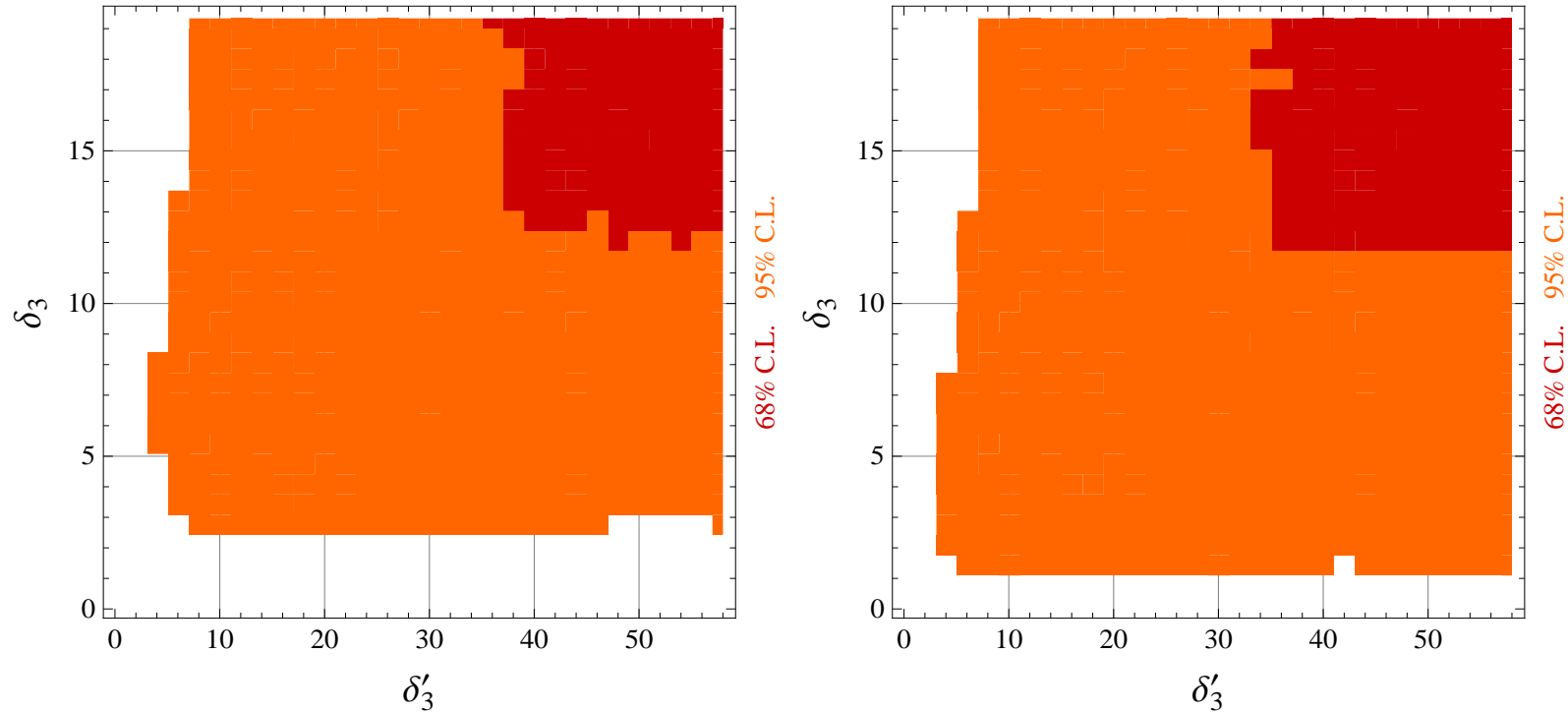


Left: without  $A_{CP}(D^0 \rightarrow K_S K_S), A_{CP}(D_s \rightarrow K_S \pi^+), A_{CP}(D_s \rightarrow K^+ \pi^0)$

Right: All data – penguins even more enhanced . [Figs from 1211.3734](#)



# Penguin enhancement?!



Left: All data from 1211.3734:  $\Delta A_{\text{CP}}^{wa} = -0.00678 \pm 0.00147$

Right: All data post Moriond QCD 2013:  $\Delta A_{\text{CP}}^{wa} = -0.0032 \pm 0.0012$   
(LHCb update/new) (Fig. courtesy of M.Jung/S.Schacht).

The penguins still need to be enhanced.

(0. This is the most comprehensive SU(3)-X-analysis without th bias; first full fit with 25 fit parameters.)

1.  $SU(3)$ -analysis predicts  $A_{CP}(D^0 \rightarrow K_S K_S)$  enhanced w.r.t  $A_{CP}(D^0 \rightarrow K^+ K^-)$  by  $\sim 1/\delta_X$ .

2. Future data can reveal pattern among BSM models with CPX due to operators with diff SU(3) representations:

-  $A_{CP}(D^+ \rightarrow \pi^+ \pi^0)$  characterizes  $\Delta I = 3/2$  in  $H_{eff}$ . [1204.3557 Grossman et al](#)

- U-spin change in  $K^+ K^- / \pi^+ \pi^-$  and  $D_s \rightarrow K_s \pi^+ / D^+ \rightarrow K_S K^+$ .

4. Fits sharpen with better data ..... and/or dynamical input.

**Stay Tuned**

- It is fantastic to witness great advances in FCNC physics and respective tests of SM and BSM physics.
- I reported on recent th advances in rare  $b \rightarrow s$  and  $c \rightarrow u$  decays.
- Cross talk between flavor and QCD allows for a sharper interpretation of data.
- Verdict still out.

Please see original papers for complete reference list.