



# Gluon saturation in dijet production in p-Pb collisions at Large Hadron Collider

#### Krzysztof Kutak



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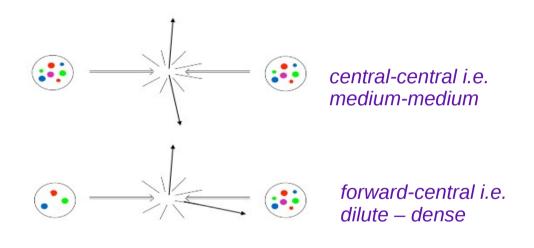
Based on:

arXiv:1205.5035 K.K, Sebastian Sapeta.

Paper accepted to PRD

## LHC as a scaner of gluon

$$S = 2P_1 \cdot P_2$$



dense medium

dilute

0.0001 0.001 0.001

 $\phi(x,k)$ 

From C. Marquet

$$x_1 = \frac{1}{\sqrt{S}} \left( p_{t1} e^{y_1} + p_{t2} e^{y_2} \right) \qquad \underset{y_1 \sim 0, y_2 \gg 0}{\underbrace{\qquad \qquad }} \sim 1$$

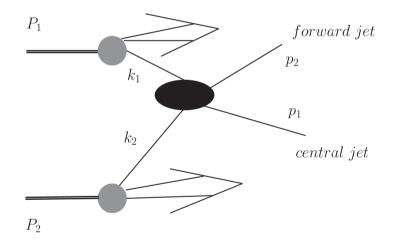
$$x_2 = \frac{1}{\sqrt{S}} \left( p_{t1} e^{-y_1} + p_{t2} e^{-y_2} \right) \qquad \ll 1$$

## High energy prescription and forward-central dijets

Deak, Jung, Hautmann Kutak JHEP 0909:121.2009

$$\frac{d\sigma}{dy_1 dy_2 dp_{1t} dp_{2t} d\phi} = \sum_{a,c,d} \frac{p_{t1} p_{t2}}{8\pi^2 (x_1 x_2 S)^2} \overline{|\mathcal{M}_{ag \to cd}|}^2 x_1 f_{a/A}(x_1,\mu^2) \, \phi_{g/B}(x_2,k_t^2,\mu^2) \frac{1}{1+\delta_{cd}}$$

$$S = 2P_1 \cdot P_2$$



$$x_1 = \frac{1}{\sqrt{S}} (p_{t1}e^{y_1} + p_{t2}e^{y_2})$$

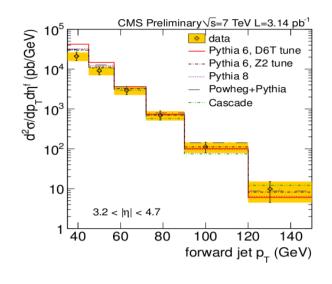
$$x_2 = \frac{1}{\sqrt{S}} (p_{t1}e^{-y_1} + p_{t2}e^{-y_2})$$

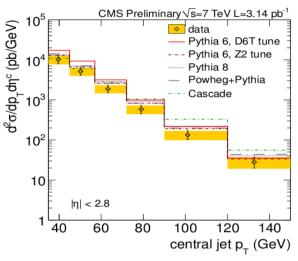
Gauge inv. ME with off shell initial state gluons. More on this P. Kotko and A. van Mameren

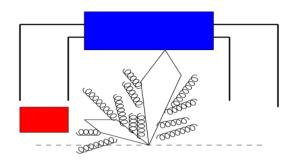
- Resummation of logs of x and logs of hard scale
- Knowing well parton densities at largr x one can get information about low x physics
- Framework goes recently under name de framework"

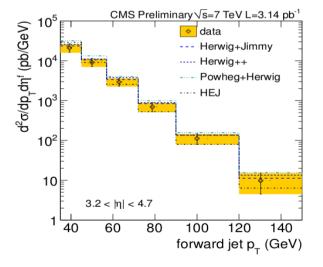
$$\sim 1$$
  $k_1^\mu = x_1 P_1^\mu$   $\ll 1$   $k_2^\mu = x_2 P_2^\mu + k_t^\mu$  3

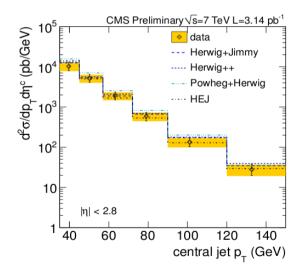
## Forward central – jet production











- •HEJ and Cascade based on unordered in k<sub>t</sub> emissions but use different parton densities
- •Herwig and PYTHIA use  $k_t$  odered shower but differ in approximations in ME and ordering conditions in shower

Deak, Jung, Hautmann, Kutak, '10

## High energy factorization and saturation

ln(1/x)

 $Q_s(x)$ 

Saturation – state where number of gluons stops growing due to high occupation number.

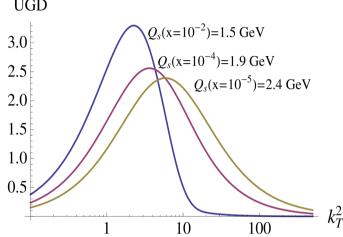
More generally saturation is an example of percolation which has to happen since partons have size  $1/k_t$  and hadron has finite size

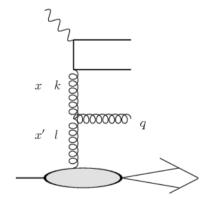
Cross sections change their behavior from power like to logarithmic like.

In Q On microscopic level it means that gluon apart splitting recombine Half" of triple pomeron recombination Bartels, Wusthoff splitting Z.Phys. C66 (1995) 157-180 Nonlinear evolution equations BK, JIMWLK Linear evolution Chirilli, Szymanowski, Wallon '10 **CGC** framework equation **DIPSY** 

## The BK equation for unintegrated gluon density in the momentum space

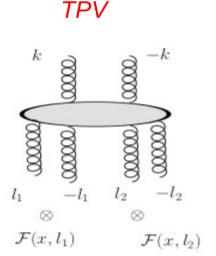
$$\begin{split} \frac{\partial \mathcal{F}_{BK}(x,k^2)}{\partial \ln 1/x} &= \frac{N_c \alpha_s}{\pi} \int_0^\infty \frac{dl^2}{l^2} \bigg[ \frac{l^2 \mathcal{F}_{BK}(x,l^2) - k^2 \mathcal{F}_{BK}(x,k^2)}{|k^2 - l^2|} + \frac{k^2 \mathcal{F}_{BK}(x,k^2)}{\sqrt{(4l^4 + k^4)}} \bigg] \\ &- \frac{\alpha_s^2}{R^2} \Bigg\{ \bigg[ \int_{k^2}^\infty \frac{dl^2}{l^2} \mathcal{F}_{BK}(x,l^2) \bigg]^2 + \mathcal{F}_{BK}(x,k^2) \int_{k^2}^\infty \frac{dl^2}{l^2} \ln \left( \frac{l^2}{k^2} \right) \mathcal{F}_{BK}(x,l^2) \Bigg\} \end{split}$$





Kutak, Kwiecinski '03; Nikolaev, Scheffer '04

$$\begin{split} \mathcal{V}(k,-k;l_1,-l_1,l_2,-l_2) &= \frac{\pi \alpha_s^2}{N_c R^2} \Bigg[ 2\theta(l_1^2-k^2)\theta(l_2^2-k^2) + k^2 \ln \frac{l_1^2}{l_2^2} \delta(l_1^2-k^2)\theta(l_2^2-l_1^2) \\ &\quad + k^2 \ln \frac{l_2^2}{l_1^2} \delta(l_2^2-k^2)\theta(l_1^2-l_2^2) \Bigg] \end{split}$$

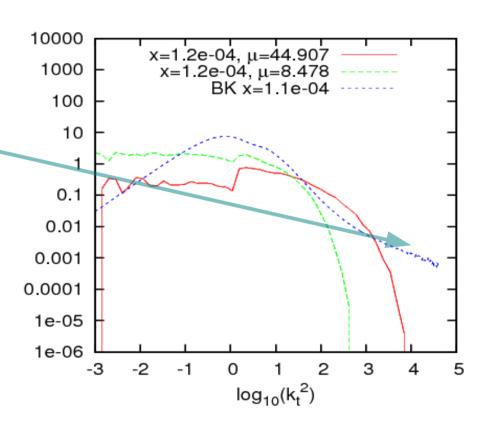


## Forward physics as the way to constrain gluon both at large and small pt



 Lack of saturation in CCFM small k<sub>t</sub>

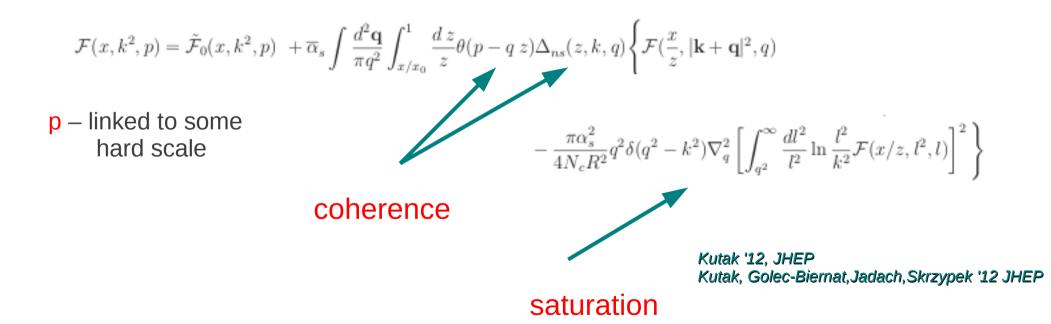
More on CCFM M. Slawinska's talk



Needed framework which unifies both correct behaviors

#### Final states and saturation

Original formulation of BK or BFKL- difficult to address final state problem. One of possible solutions is to combine physics of BK with CCFM



More on this on example of BK for WW gluon density: D. Toton's talk

#### Jets and saturation

S.Sapeta. KK PRD

- Another solution it to follow **Kwiecinski-Martin-Stasto** prescription to include corrections of higer order in In1/x
- ·High energy factorization is an approximation. More general framework given by: F. Dominguez, C. Marquet, F. Huan, Xiao

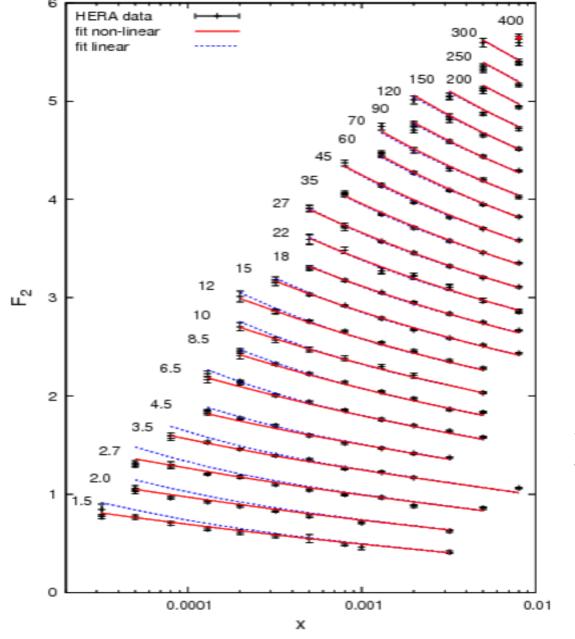
The equation for unintegrated gluon density with corrections reads:

$$\begin{split} \mathcal{F}_{p}(x,k^{2}) &= \mathcal{F}_{p}^{(0)}(x,k^{2}) \\ &+ \frac{\alpha_{s}(k^{2})N_{c}}{\pi} \int_{x}^{1} \frac{dz}{z} \int_{k_{0}^{2}}^{\infty} \frac{dl^{2}}{l^{2}} \left\{ \frac{l^{2}\mathcal{F}_{p}(\frac{x}{z},l^{2}) \, \theta(\frac{k^{2}}{z}-l^{2}) \, - \, k^{2}\mathcal{F}_{p}(\frac{x}{z},k^{2})}{|l^{2}-k^{2}|} + \frac{k^{2}\mathcal{F}_{p}(\frac{x}{z},k^{2})}{|4l^{4}+k^{4}|^{\frac{1}{2}}} \right\} \\ &+ \frac{\alpha_{s}(k^{2})}{2\pi k^{2}} \int_{x}^{1} dz \, \left( P_{gg}(z) - \frac{2N_{c}}{z} \right) \int_{k_{0}^{2}}^{k^{2}} dl^{2} \, \mathcal{F}_{p}(\frac{x}{z},l^{2}) \\ &- \frac{2\alpha_{s}^{2}(k^{2})}{R^{2}} \left[ \left( \int_{k^{2}}^{\infty} \frac{dl^{2}}{l^{2}} \mathcal{F}_{p}(x,l^{2}) \right)^{2} + \mathcal{F}_{p}(x,k^{2}) \int_{k^{2}}^{\infty} \frac{dl^{2}}{l^{2}} \ln \left( \frac{l^{2}}{k^{2}} \right) \mathcal{F}_{p}(x,l^{2}) \right] \end{split}$$
 Kwiecinski, Kutak '03

Corrections of higher orders Included.

Kin. Constr DGLAP spf

### Hints for saturation in F2 data



S.Sapeta. KK PRD

Fit of BK-DGLAP and BFKL-DGLAP to combined H1-ZEUS data

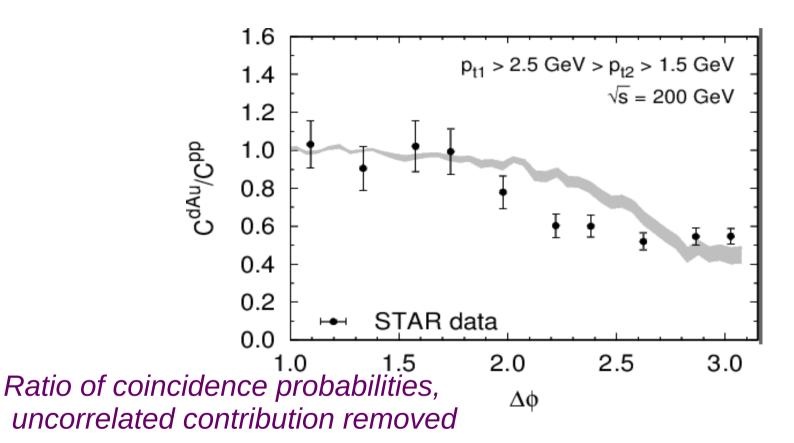
Very good description with BK-DGLAP in range  $Q^2 > 1.5 \text{ GeV}^2$ 

$$\chi^2 = 1.73$$

Very good description with BFKL-DGLAP in range  $Q^2 > 4.5 \text{ GeV}^2$ 

$$\chi^2 = 1.5$$

#### Hints for saturation in RHIC data



S.Sapeta. KK PRD

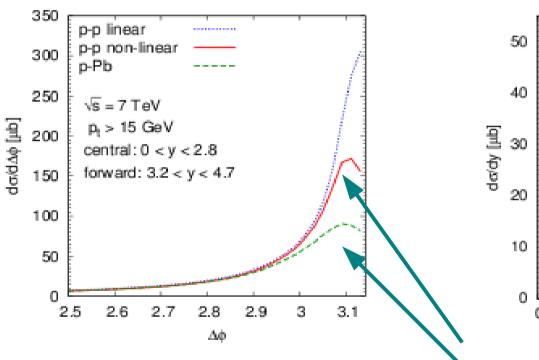
where  $C(\Delta \varphi) = N \text{ pair } (\Delta \varphi)/N \text{ incl}$ 

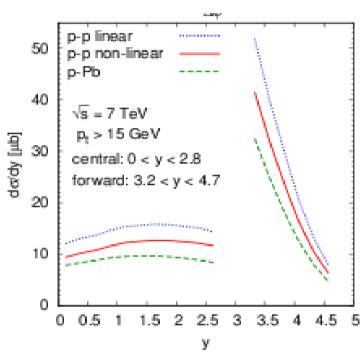
J. L. Albacete, C. Marquet, Phys. Rev. Lett. 105 (2010) 162301.

A. Stasto, B., Xaio, F. HuanPhys.Lett. B716 (2012) 430-434

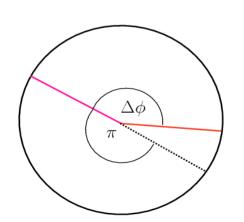
## Signatures of saturation in p-p and p-Pb

S.Sapeta. KK PRD



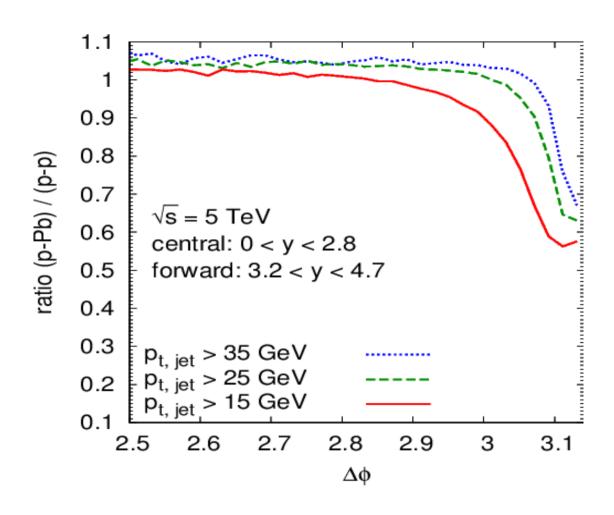


Observable suggested to study BFKL effects Sabio-Vera, Schwensen '06



Reflects~ k<sup>2</sup> behavior of gluon at small k<sup>2</sup>

## Signatures of saturation: p-Pb/p-p at 5 TeV







#### Conclusions and outlook

- •With help of LHC there comes opportunity to test parton densities both when the parton density is probed at low x and low enough kt.
- •HERA and RHIC data further gives some hints for saturation
- •Results based on BK/DGLAP approach predicts saturation in p-Pb and sugges tits presence in p-p