

Status of $B \rightarrow D^{(*)} \tau \nu$ decays in two-Higgs-doublet models

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work in collaboration with A. Pich, M. Jung and Xin-Qiang Li

[arXiv:1302.5992](https://arxiv.org/abs/1302.5992)

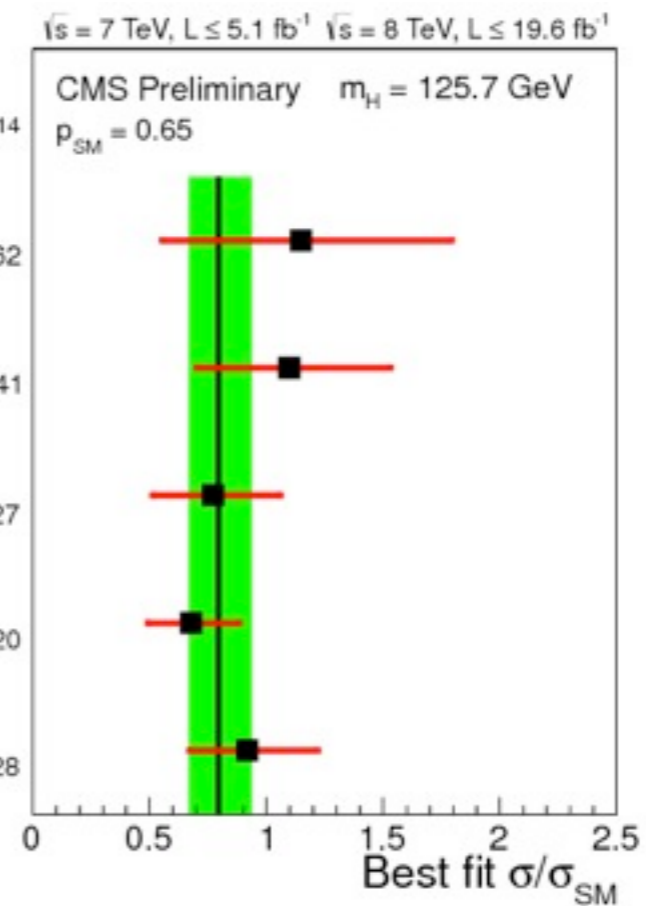
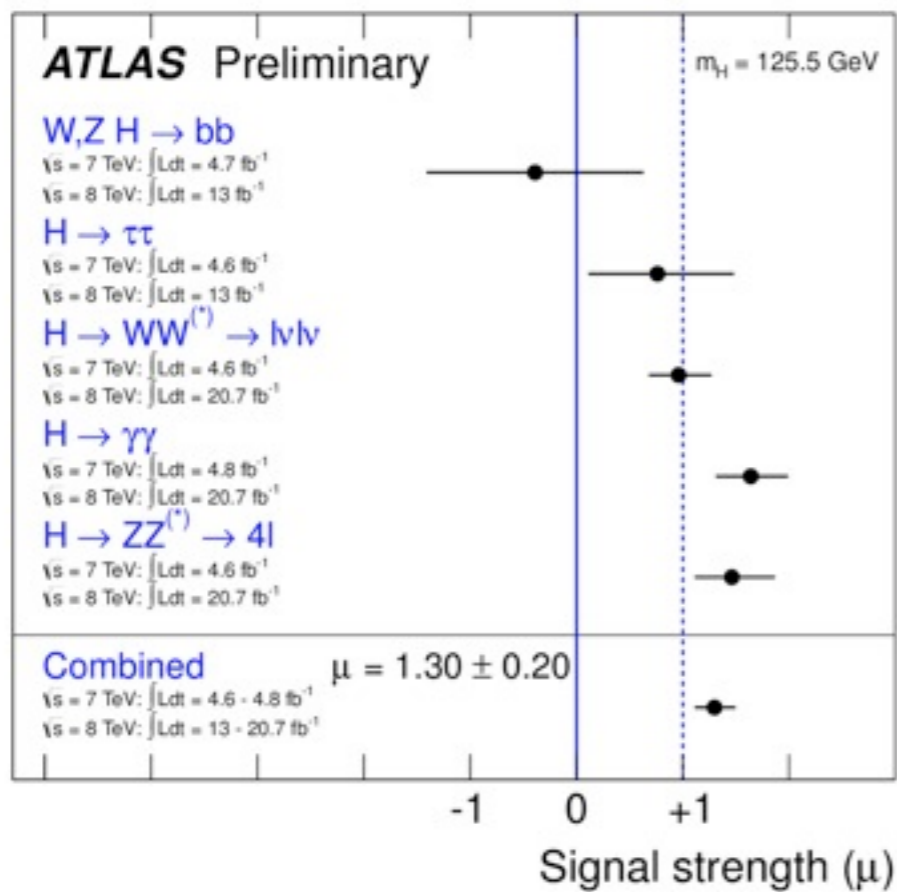
[arXiv:1210.8443](https://arxiv.org/abs/1210.8443)

IFIC, Universitat de Valencia-CSIC



HEP 2013
Stockholm
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A new boson around 126 GeV

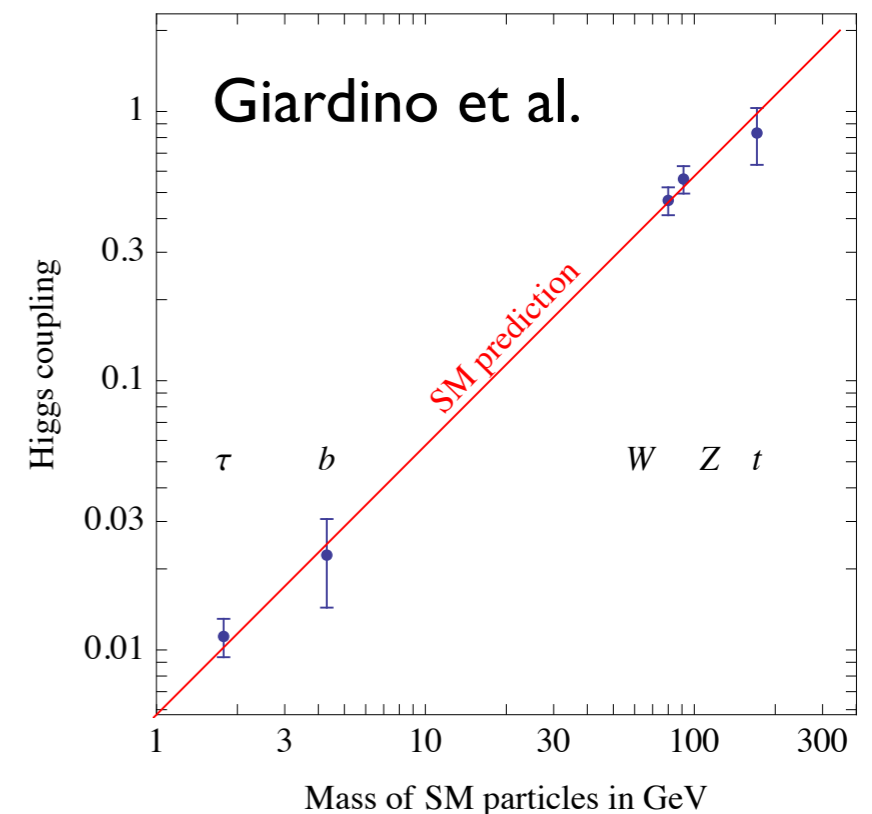
Consistent with SM Higgs



Why does the muon weigh?

R. Feynman

Fit to Higgs couplings



Adding a second Higgs doublet to the SM

Scalar spectrum $\rightarrow \{h, H, A, H^\pm\}$

3 Goldstone bosons
+
3 neutral Higgs
+
a charged scalar

Aligned 2HDM

Pich, Tuzon '09

no tree-level FCNCs

$$\mathcal{L}_Y \supset -\frac{\sqrt{2}}{v} H^+ \left\{ \bar{u} \left[\varsigma_d V M_d \mathcal{P}_R - \varsigma_u M_u^\dagger V \mathcal{P}_L \right] d + \varsigma_l \bar{\nu} M_l \mathcal{P}_R l \right\}$$

$\varsigma_f \rightarrow$ new sources of CP violation
Flavor Universal (the same for each family)

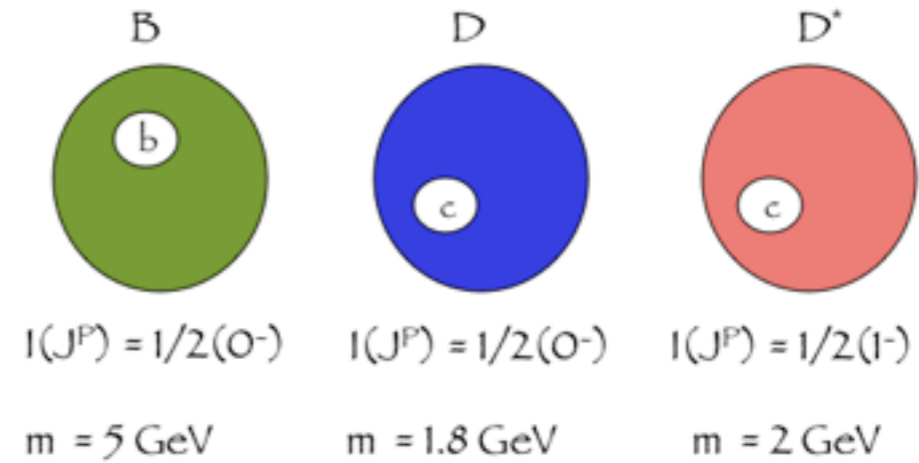
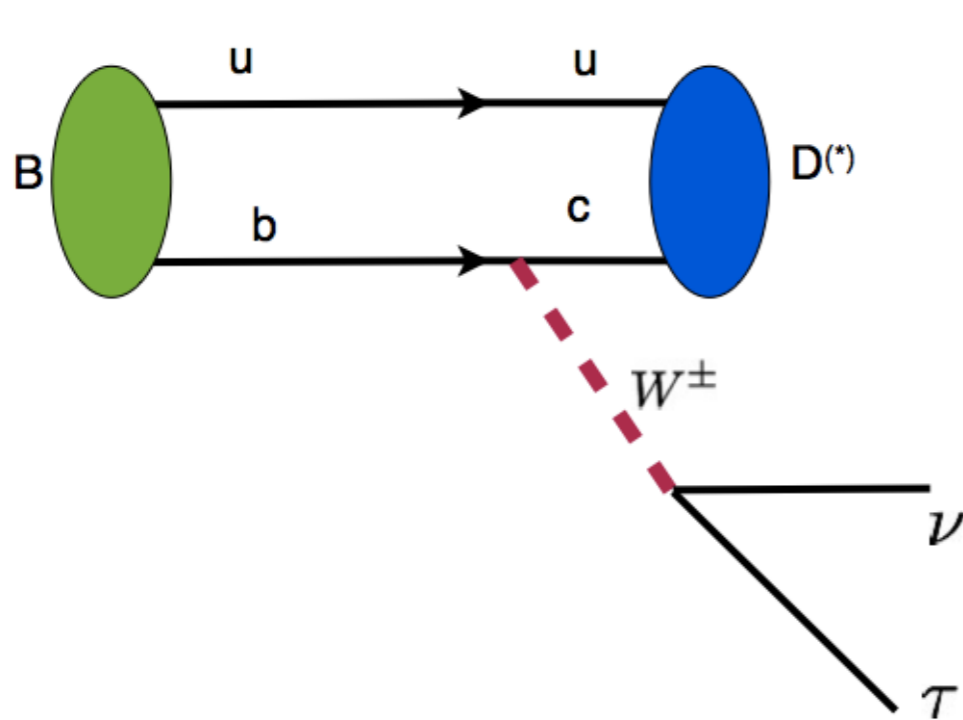
2HDMs with natural flavor conservation

Model	ς_d	ς_u	ς_l
Type I	$\cot \beta$	$\cot \beta$	$\cot \beta$
Type II	$-\tan \beta$	$\cot \beta$	$-\tan \beta$
Type X	$\cot \beta$	$\cot \beta$	$-\tan \beta$
Type Y	$-\tan \beta$	$\cot \beta$	$\cot \beta$
Inert	0	0	0

★ See A. Crivellin talk for the Type III 2HDM

Flavor physics tests indirectly the mechanism of EWSB.

b, c, τ : heaviest fermions produced at flavor factories



BaBar [Phys. Rev. D86 (2012) 032001]



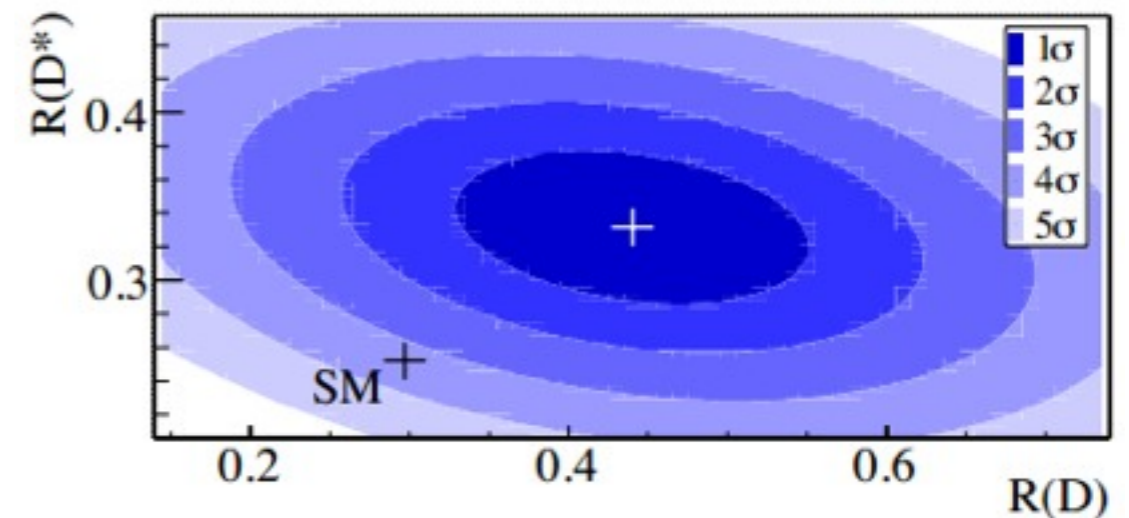
Charged Higgs enters at tree level

$$R(D^{(*)}) = \frac{\Gamma(B \rightarrow D^{(*)} \tau \nu)}{\Gamma(B \rightarrow D^{(*)} l \nu)}$$

SM predictions

Kamenik, Mescia [Phys.Rev. D78 (2008) 014003]

Fajfer, Kamenik, Nisandzic [Phys.Rev. D85 (2012) 094025]

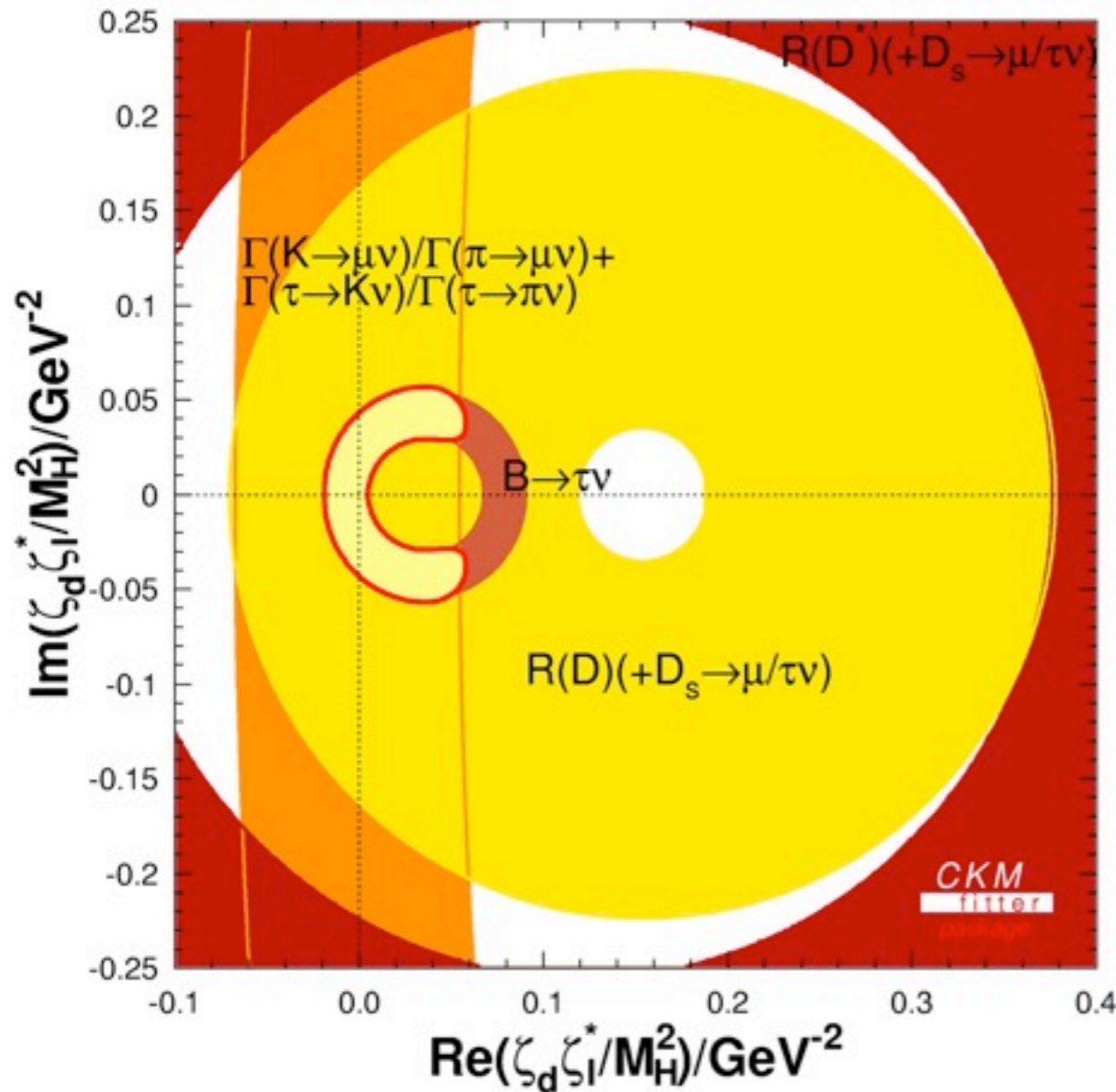


$$R(D) = \left\{ \begin{array}{ll} 0.440 \pm 0.072 & \text{BABAR} \\ 0.297 \pm 0.017 & \text{SM} \end{array} \right\} \left. \begin{array}{l} 2.0\sigma \\ \\ \end{array} \right\} 3.4\sigma$$

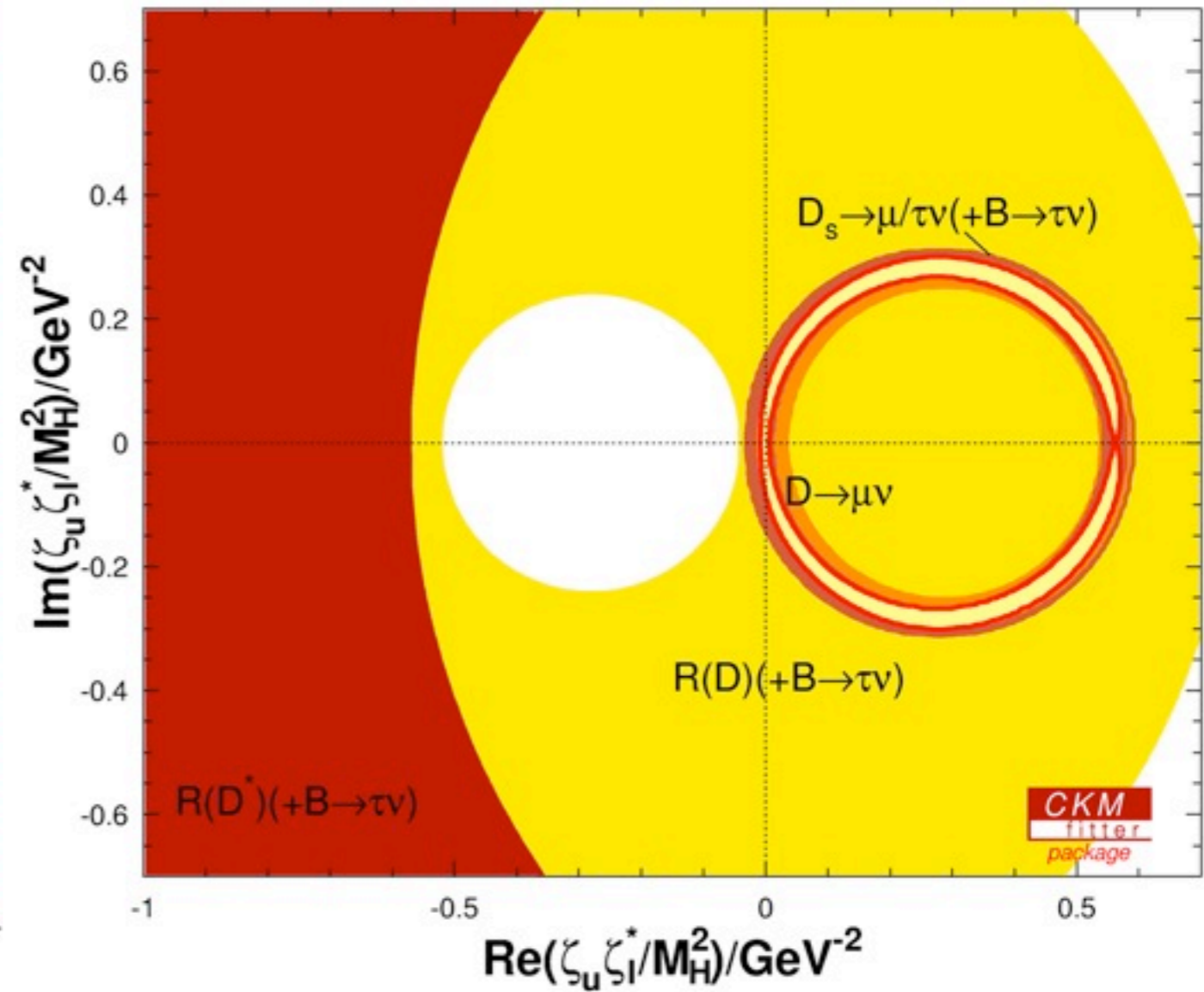
$$R(D^*) = \left\{ \begin{array}{ll} 0.332 \pm 0.030 & \text{BABAR} \\ 0.252 \pm 0.003 & \text{SM} \end{array} \right\} \left. \begin{array}{l} 2.7\sigma \\ \\ \end{array} \right\} 3.4\sigma$$

$$\mathcal{L}_Y \supset -\frac{\sqrt{2}}{v} H^+ \left\{ \bar{u} \left[\zeta_d V M_d \mathcal{P}_R - \zeta_u M_u^\dagger V \mathcal{P}_L \right] d + \zeta_l \bar{\nu} M_l \mathcal{P}_R \right\}$$

LEP limit: $M_{H^\pm} \gtrsim 80 \text{ GeV}$



95 % CL



★ A departure from family universality of the Yukawa couplings is needed

family universality of Yukawa couplings: $Y_f \sim \zeta_f M_f$

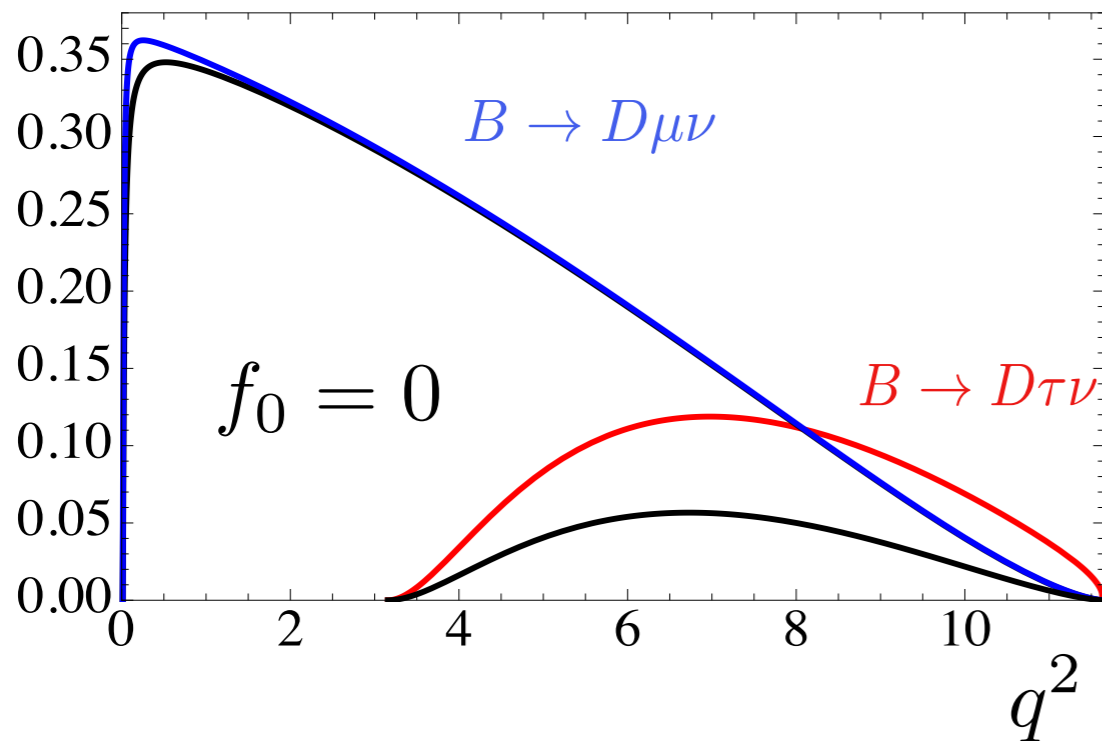
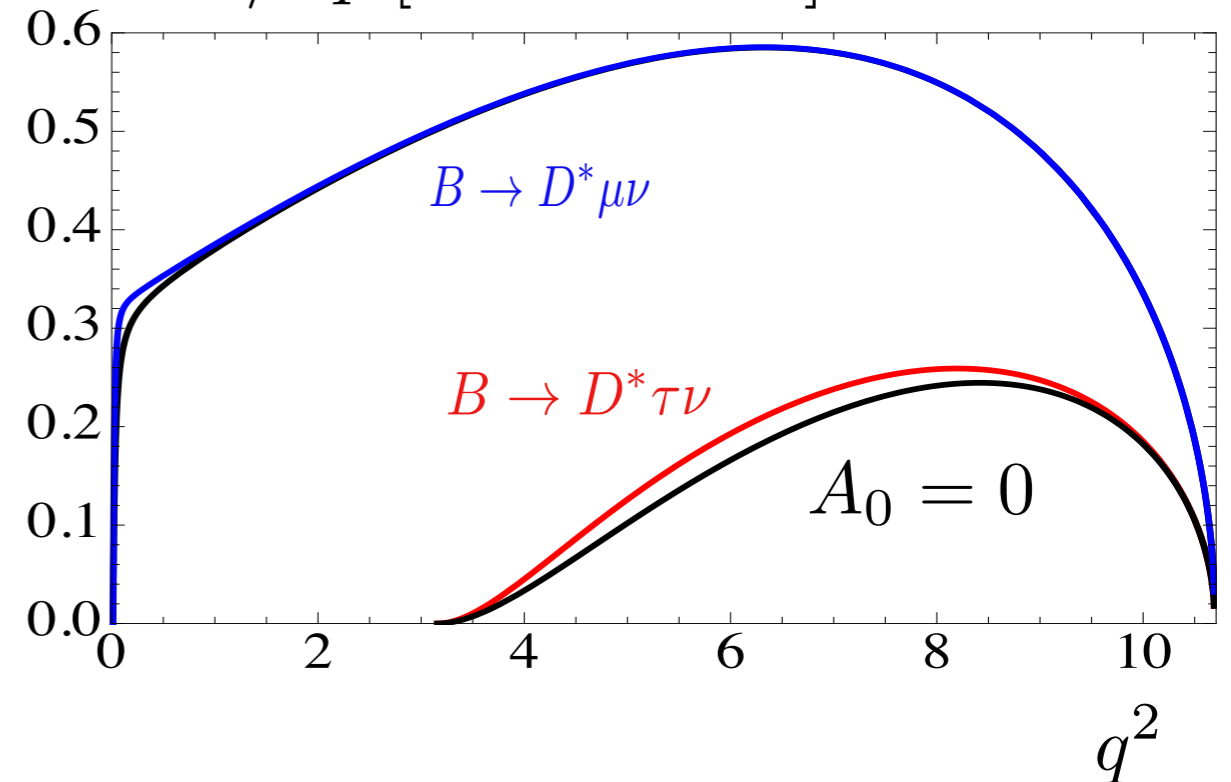
$B \rightarrow D$ $f_0(q^2), f_+(q^2)$ $B \rightarrow D^*$ $A_0(q^2), V(q^2), A_1(q^2), A_2(q^2)$

$$q^2 = (p_B - p_{D^{(*)}})^2$$

Type II: -1 $\tan^2 \beta$

$$\tilde{f}_0(q^2) = f_0(q^2) \left[1 + \frac{q^2}{m_{H^\pm}^2} \left(\frac{m_c \overline{\zeta_u \zeta_l^*} - m_b \overline{\zeta_d \zeta_l^*}}{m_b - m_c} \right) \right]$$

$$\tilde{A}_0(q^2) = A_0(q^2) \left[1 - \frac{q^2}{m_{H^\pm}^2} \left(\frac{m_c \overline{\zeta_u \zeta_l^*} + m_b \overline{\zeta_d \zeta_l^*}}{m_b + m_c} \right) \right]$$

 $d\text{Br}/dq^2 [10^{-2} \text{GeV}^{-2}]$  $d\text{Br}/dq^2 [10^{-2} \text{GeV}^{-2}]$ 

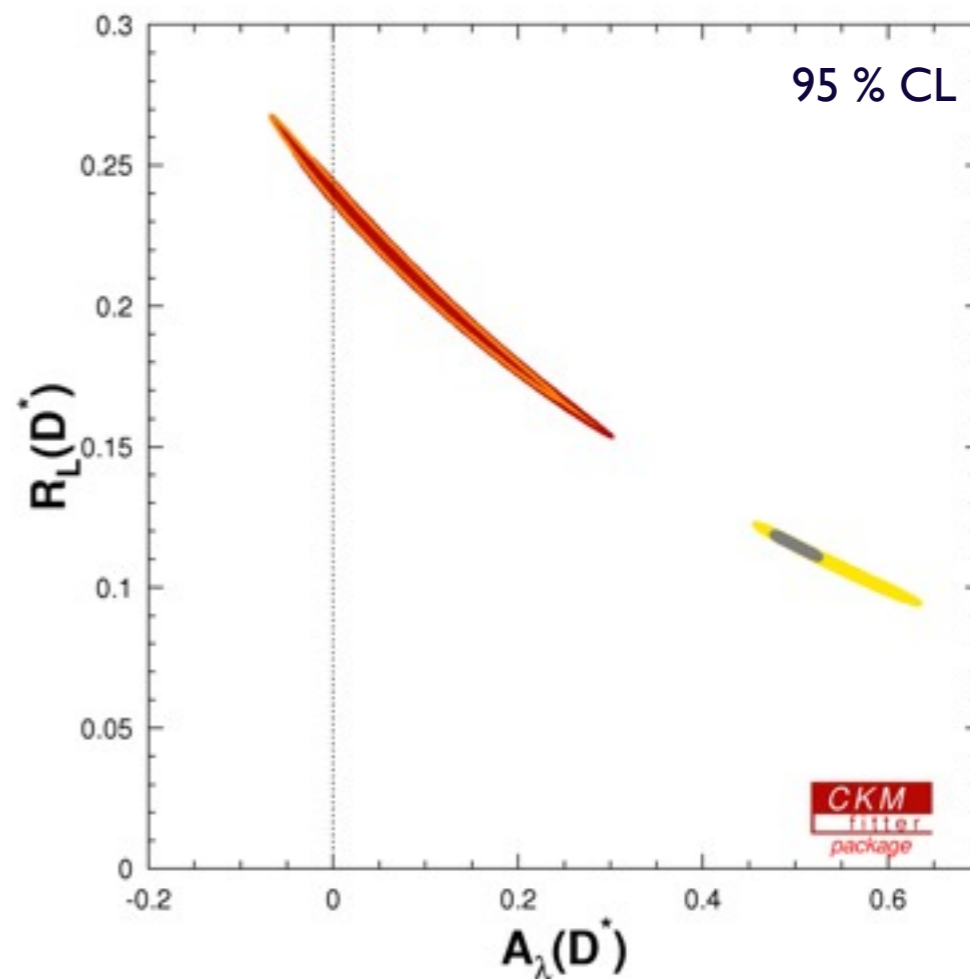
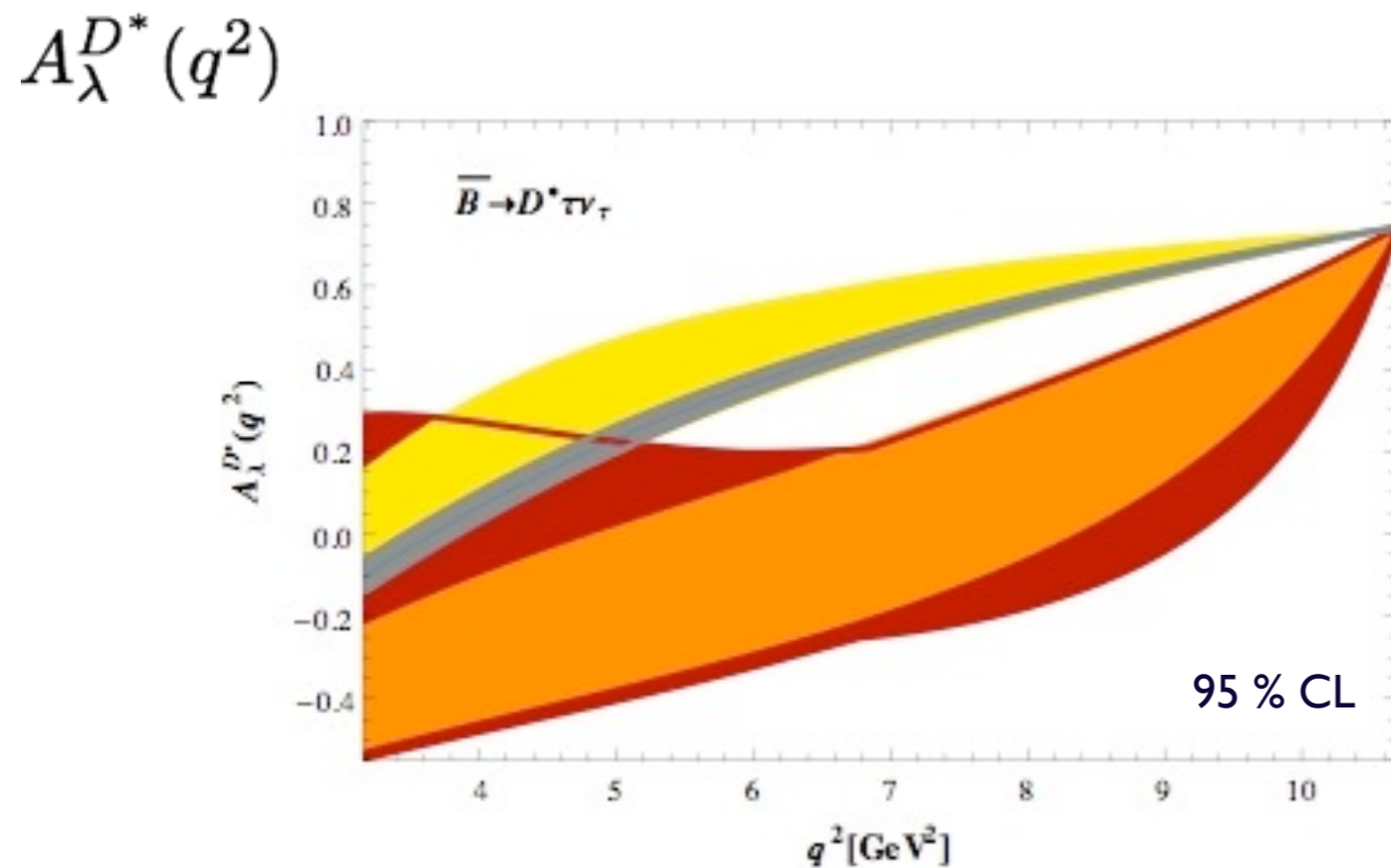
Is it a charged Higgs?

● SM

● $R(D) + R(D^*)$

● $R(D) + R(D^*) + B \rightarrow \tau\nu$

● $R(D) + B \rightarrow \tau\nu + D \rightarrow \ell\nu$



$$R_L(D^*) = \frac{\Gamma(B \rightarrow D_L^* \tau \nu)}{\Gamma(B \rightarrow D_L^* \ell \nu)}$$

$$A_\lambda^{D^{(*)}}(q^2) = \frac{d\Gamma^{D^{(*)}}[\lambda_\tau = -1/2]/dq^2 - d\Gamma^{D^{(*)}}[\lambda_\tau = +1/2]/dq^2}{d\Gamma^{D^{(*)}}/dq^2}$$



$B_c \rightarrow \tau\nu$

large enhancement expected

[arXiv:1302.5992](https://arxiv.org/abs/1302.5992)

Summary

$$B \rightarrow D^{(*)} \tau \nu$$

provide an interesting laboratory to look for NP effects related to the EWSB mechanism

To accommodate current measurements of $R(D^*)$ in 2HDMs, a departure from family universality of the Yukawa couplings is needed.

rich kinematics \longrightarrow interesting prospects for Belle II

Important to improve our understanding of hadronic matrix elements

- ★ Expected update from Belle.
Can it be measured at LHCb ?

Back-up slides

An incomplete list of
references on the
topic

apologies for those not included

Fajfer, Kamenik, Nisandzic, Zupan [Phys.Rev.Lett. 109 (2012) 161801]

Fajfer, Kamenik, Nisandzic [Phys.Rev. D85 (2012) 094025]

Kamenik, Mescia [Phys.Rev. D78 (2008) 014003]

Crivellin, Greub, Kokulu [Phys.Rev. D86 (2012) 054014]

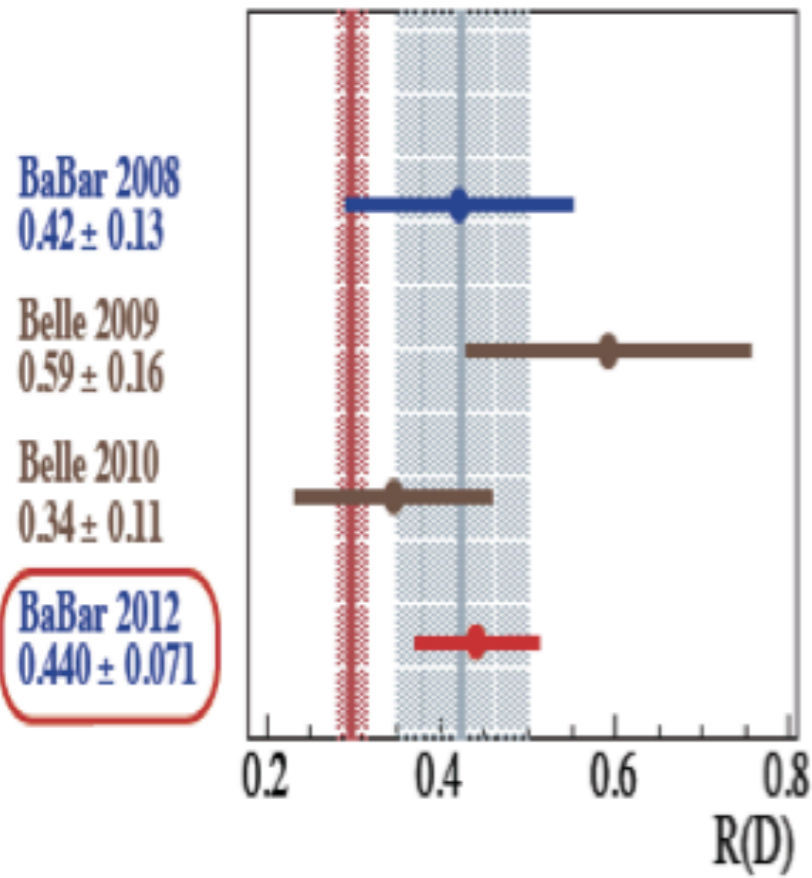
Datta, Duraisamy [Phys. Rev. D86 034027]

AC, Jung, X-Q. Li , Pich [JHEP 1301 (2013) 054]

Tanaka, Watanabe [Phys. Rev. D87 (2013) 034028]

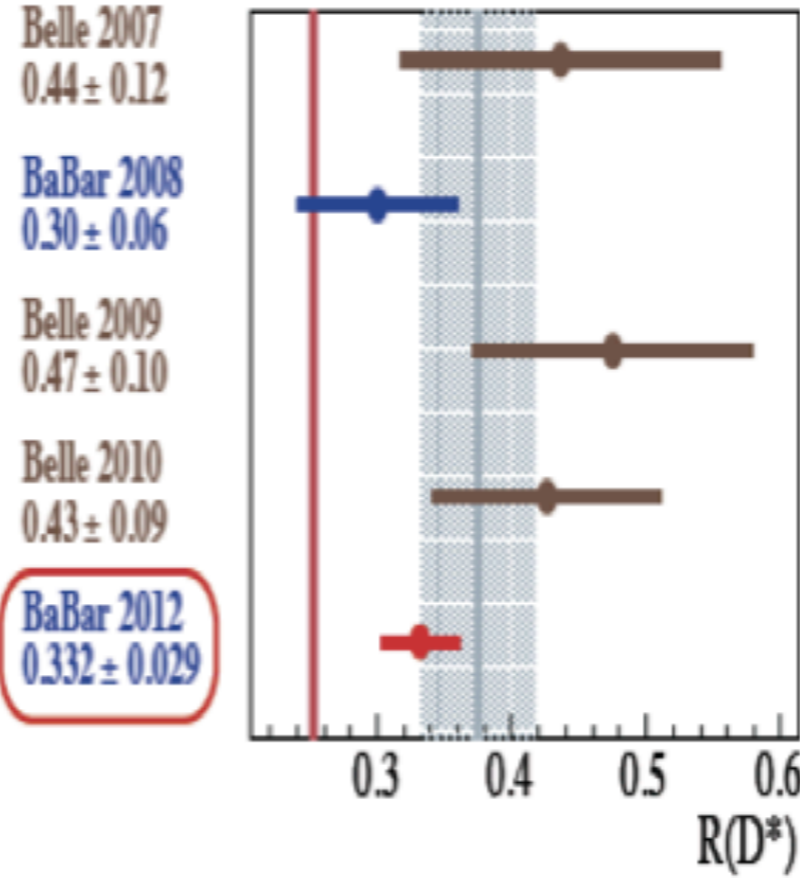
R(D)

SM



R(D*)

SM



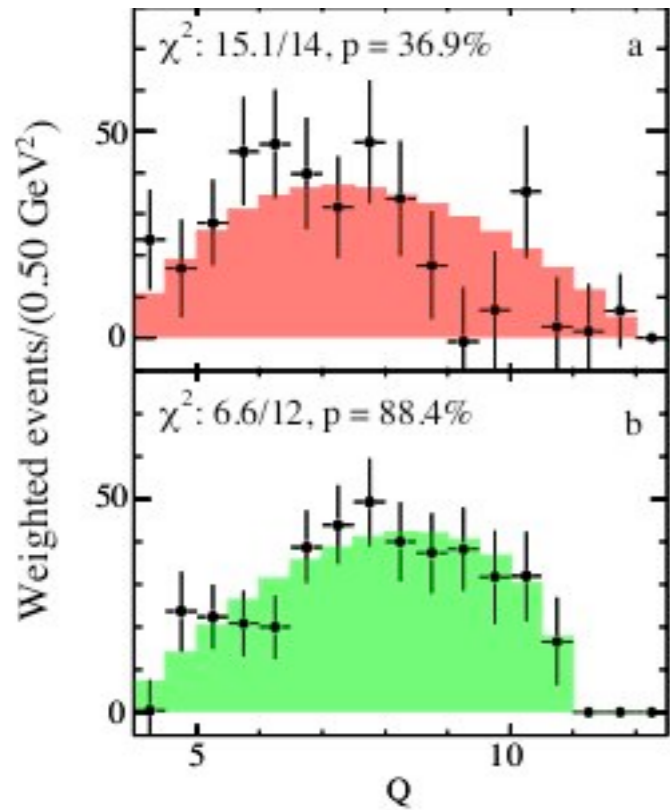
535M $B\bar{B}$

232M $B\bar{B}$

657M $B\bar{B}$

657M $B\bar{B}$

471M $B\bar{B}$

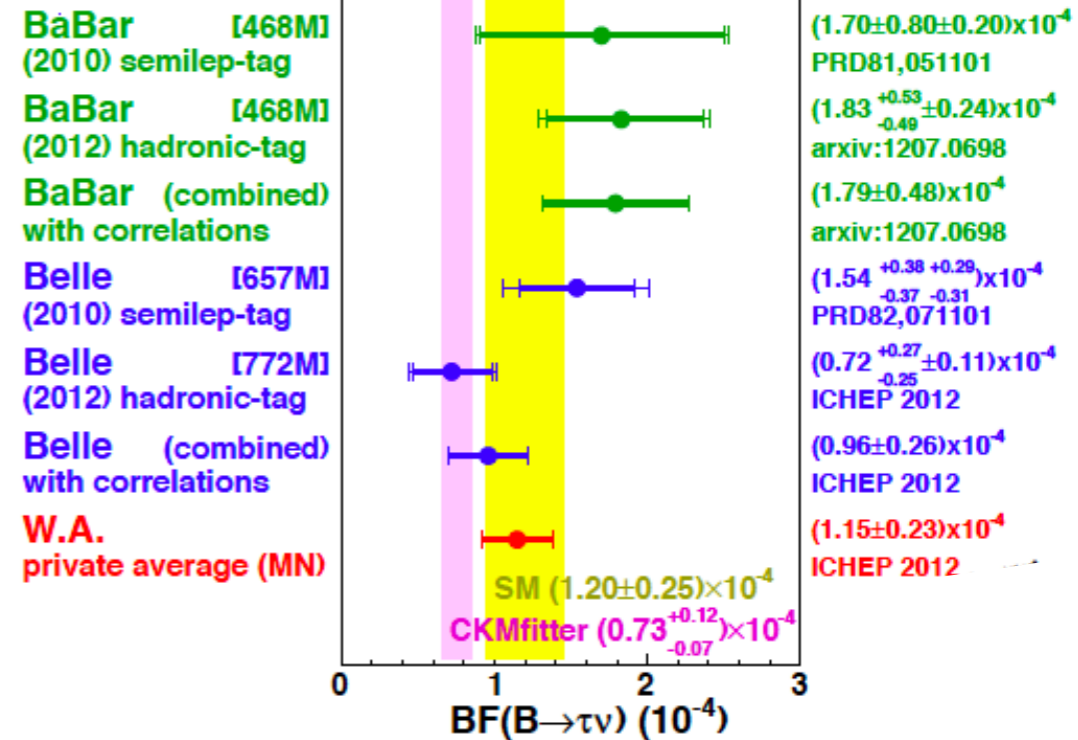


Distributions in momentum transfer

BaBar [arXiv:1303.0571]

BaBar [Phys. Rev. D86 (2012) 032001]

$B \rightarrow \tau \nu$



Two-Higgs-doublet model (2HDM)

$$\langle 0 | \phi_a^T(x) | 0 \rangle = \frac{1}{\sqrt{2}} (0, v_a e^{i\theta_a}) \quad , \quad \theta_1 = 0 \quad , \quad \theta \equiv \theta_2 - \theta_1$$

Higgs basis: $v \equiv \sqrt{v_1^2 + v_2^2} \quad , \quad \tan \beta \equiv v_2/v_1$

$$\begin{pmatrix} \Phi_1 \\ -\Phi_2 \end{pmatrix} \equiv \begin{bmatrix} \cos \beta & \sin \beta \\ \sin \beta & -\cos \beta \end{bmatrix} \begin{pmatrix} \phi_1 \\ e^{-i\theta} \phi_2 \end{pmatrix}$$

→ $\Phi_1 = \begin{bmatrix} G^+ \\ \frac{1}{\sqrt{2}} (v + S_1 + iG^0) \end{bmatrix} \quad , \quad \Phi_2 = \begin{bmatrix} H^+ \\ \frac{1}{\sqrt{2}} (S_2 + iS_3) \end{bmatrix}$

Mass eigenstates: H^\pm , $\varphi_i^0(x) \equiv \{h(x), H(x), A(x)\} = \mathcal{R}_{ij} S_j(x)$

Yukawa interactions in the 2HDM

$$\mathcal{L}_Y = -\bar{Q}'_L (\Gamma_1 \phi_1 + \Gamma_2 \phi_2) d'_R - \bar{Q}'_L (\Delta_1 \tilde{\phi}_1 + \Delta_2 \tilde{\phi}_2) u'_R \\ - \bar{L}'_L (\Pi_1 \phi_1 + \Pi_2 \phi_2) l'_R + \text{h.c.}$$

↓ **SSB**

$$\mathcal{L}_Y = -\frac{\sqrt{2}}{v} \left\{ \bar{Q}'_L (M'_d \Phi_1 + Y'_d \Phi_2) d'_R + \bar{Q}'_L (M'_u \tilde{\Phi}_1 + Y'_u \tilde{\Phi}_2) u'_R \right. \\ \left. + \bar{L}'_L (M'_l \Phi_1 + Y'_l \Phi_2) l'_R + \text{h.c.} \right\}$$

M'_f and Y'_f unrelated → **FCNCs**

$$\sqrt{2} M'_d = v_1 \Gamma_1 + v_2 \Gamma_2 e^{i\theta} \quad , \quad \sqrt{2} M'_u = v_1 \Delta_1 + v_2 \Delta_2 e^{-i\theta}$$

$$\sqrt{2} Y'_d = v_1 \Gamma_2 e^{i\theta} - v_2 \Gamma_1 \quad , \quad \sqrt{2} Y'_u = v_1 \Delta_2 e^{-i\theta} - v_2 \Delta_1$$

Avoiding large FCNC

- Very large scalar masses \rightarrow THDM irrelevant at low energies
- Very small scalar couplings

- Type III model: $(Y_f)_{ij} \propto \sqrt{m_i m_j}$ Yukawa textures
(Cheng - Sher '87)

- Discrete \mathcal{Z}_2 symmetries: only one $\phi_a(x)$ couples to a given $f_R(x)$
(Glashow - Weinberg '77)

$$\mathcal{Z}_2: \quad \phi_1 \rightarrow \phi_1 \quad , \quad \phi_2 \rightarrow -\phi_2 \quad , \quad Q_L \rightarrow Q_L \quad , \quad L_L \rightarrow L_L \quad , \quad f_R \rightarrow \pm f_R$$

\rightarrow CP conserved in the scalar sector

Aligned 2HDM

(Pich - Tuzón '09)

Require alignment in Flavour Space of Yukawa couplings:

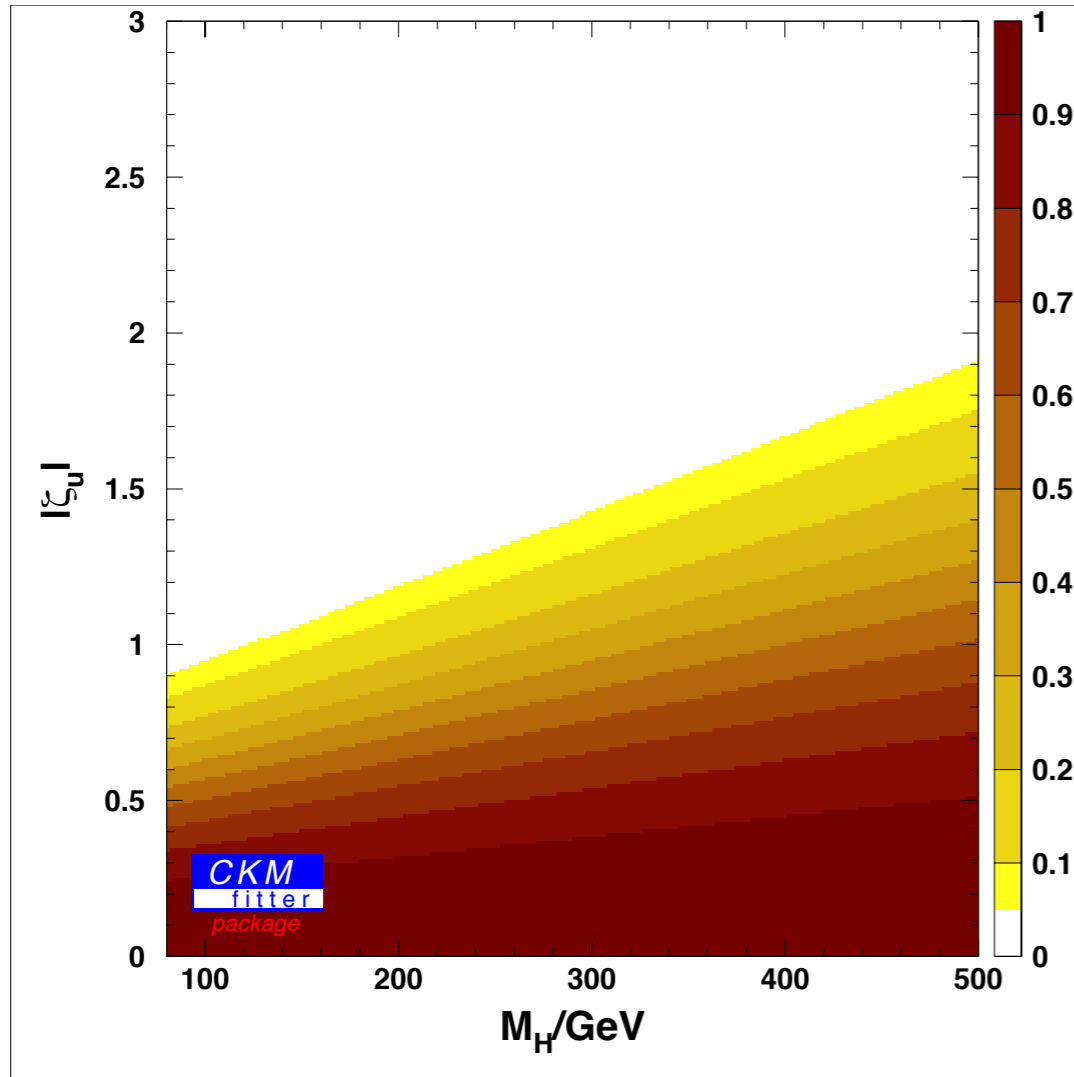
$$\Gamma_2 = \xi_d e^{-i\theta} \Gamma_1 \quad , \quad \Delta_2 = \xi_u^* e^{i\theta} \Delta_1 \quad , \quad \Pi_2 = \xi_l e^{-i\theta} \Pi_1$$



$$Y_{d,l} = \varsigma_{d,l} M_{d,l} \quad , \quad Y_u = \varsigma_u^* M_u \quad , \quad \varsigma_f \equiv \frac{\xi_f - \tan \beta}{1 + \xi_f \tan \beta}$$

$$\mathcal{L}_Y = -\frac{\sqrt{2}}{v} H^+ \left\{ \bar{u} \left[\varsigma_d V_{\text{CKM}} M_d \mathcal{P}_R - \varsigma_u M_u^\dagger V_{\text{CKM}} \mathcal{P}_L \right] d + \varsigma_l (\bar{\nu} M_l \mathcal{P}_R l) \right\} \\ - \frac{1}{v} \sum_{\varphi_i^0, f} y_f^{\varphi_i^0} \varphi_i^0 (\bar{f} M_f \mathcal{P}_R f) + \text{h.c.}$$

$$R_b = \Gamma(Z \rightarrow \bar{b}b) / \Gamma(Z \rightarrow \text{hadrons})$$

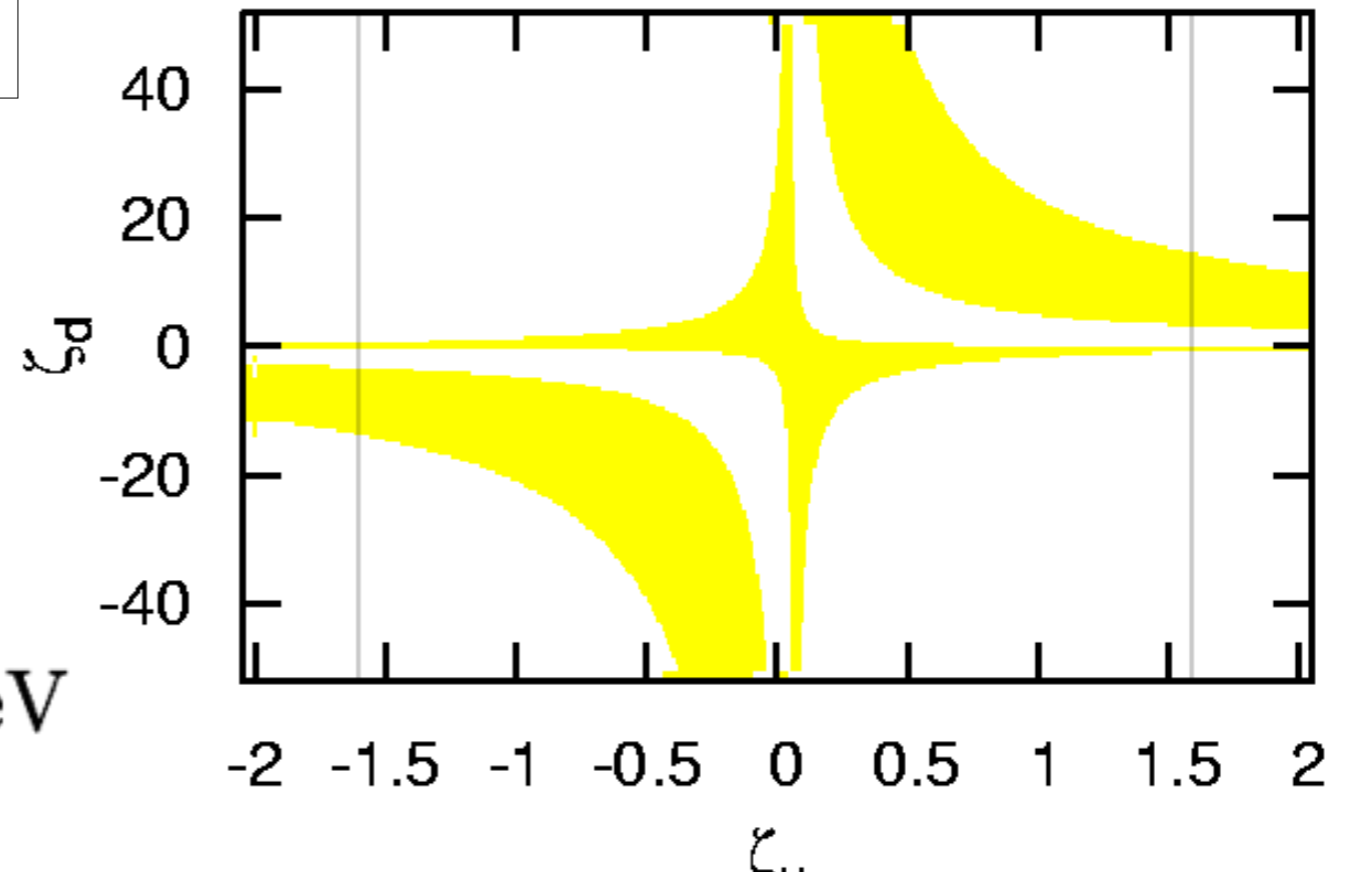


adding τ decays constraints

$$|\zeta_u \zeta_l^*| / M_{H^\pm}^2 < 0.005 \text{ GeV}^{-2}$$

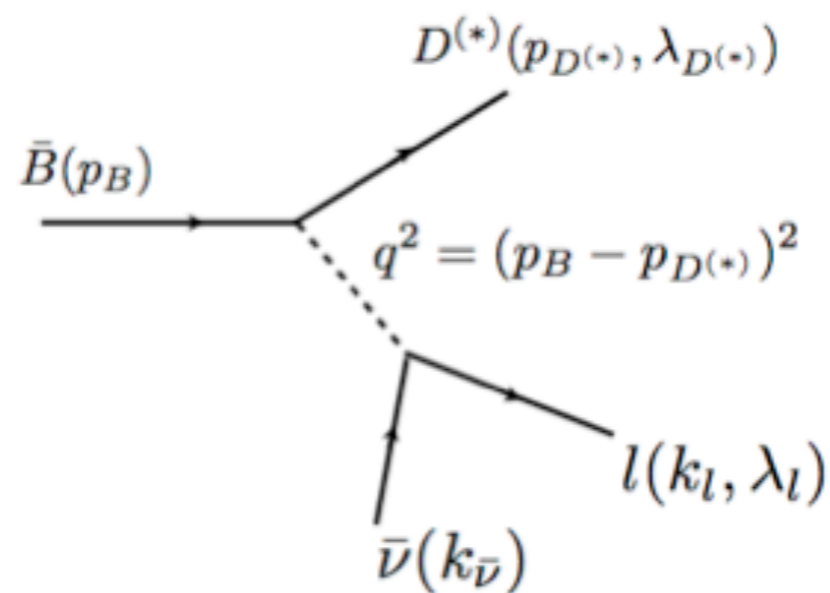
with $|\zeta_d| < 50$

$$\text{Br}(\bar{B} \rightarrow X_s \gamma)$$

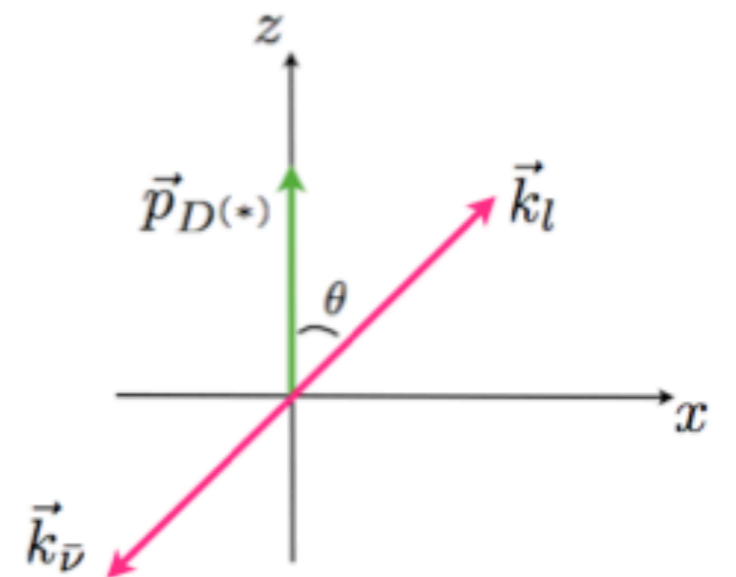


$$M_{H^\pm} \in [80, 500] \text{ GeV}$$

$\bar{B} \rightarrow D^{(*)} l \bar{\nu}$ Decays



$$m_l^2 \leq q^2 \leq (m_B - m_{D^{(*)}})^2$$



In the $l - \bar{\nu}$ rest frame

$$|\mathcal{M}(\bar{B} \rightarrow D^{(*)} l \bar{\nu})|^2 = |\langle D^{(*)} l \bar{\nu} | \mathcal{L}_{eff} | \bar{B} \rangle|^2 = L_{\mu\nu} H^{\mu\nu}$$

$$\frac{d^2\Gamma_l}{dq^2 d\cos\theta} = \frac{G_F^2 |V_{cb}|^2}{(2\pi)^3} \frac{|\vec{p}_B|}{2m_B^2} \left(1 - \frac{m_l^2}{q^2}\right) L_{\mu\nu} H^{\mu\nu}$$

$\bar{B} \rightarrow D l \bar{\nu}$ hadronic matrix elements

- $\langle D(p_D) | \bar{c} \gamma^\mu b | \bar{B}(p_B) \rangle = f_+(q^2) \left[(p_B + p_D)^\mu - \frac{m_B^2 - m_D^2}{q^2} q^\mu \right]$
 $+ f_0(q^2) \frac{m_B^2 - m_D^2}{q^2} q^\mu$
- $\langle D(p_D) | \bar{c} \gamma^\mu \gamma_5 b | \bar{B}(p_B) \rangle = 0$

$B \rightarrow D$ form factors

$$f_+(q^2) = \frac{G_1(w)}{R_D}, \quad f_0(q^2) = R_D \frac{(1+w)}{2} G_1(w) \frac{1+r}{1-r} \Delta(w),$$

$$R_{D^{(*)}} = 2\sqrt{m_B m_{D^{(*)}}} / (m_B + m_{D^{(*)}}), \quad r = m_{D^{(*)}} / m_B \quad [\text{Falk, Neubert (1992)}]$$

$$w = v_B \cdot v_{D^{(*)}} = \frac{m_B^2 + m_{D^{(*)}}^2 - q^2}{2m_B m_{D^{(*)}}}$$

$$\Delta(w) = 0.46 \pm 0.02$$

de Divitiis, Petronzio, Tantalò [0707.0587]

Bailey et al. [1206.4992]

Becirevic, Kosnik, Tayduganov [1206.4977]

$$G_1(w) = G_1(1) [1 - 8\rho_1^2 z(w) + (51\rho_1^2 - 10) z(w)^2 - (252\rho_1^2 - 84) z(w)^3]$$

$$z(w) = (\sqrt{w+1} - \sqrt{2}) / (\sqrt{w+1} + \sqrt{2}) \quad \text{Caprini, Lellouch, Neubert [9712417]}$$

$G_1(1)$ and ρ values from $\bar{B} \rightarrow D\ell\bar{\nu}$ ($\ell = e, \mu$) ▶ Heavy Flavor Averaging Group (HFAG)

$\bar{B} \rightarrow D l \bar{\nu}$ differential decay width

$$H_0(q^2) = \frac{2m_B |\vec{\mathbf{p}}|}{\sqrt{q^2}} f_+(q^2), \quad H_t(q^2) = \frac{m_B^2 - m_D^2}{\sqrt{q^2}} f_0(q^2),$$

- $$\frac{d^2\Gamma^D[\lambda_l = -1/2]}{dq^2 d\cos\theta} = \frac{G_F^2 |V_{cb}|^2 q^2}{128\pi^3 m_B^2} \times \left(1 - \frac{m_l^2}{q^2}\right)^2 |\vec{\mathbf{p}}| |H_0(q^2)|^2 \sin^2\theta$$
- $$\frac{d^2\Gamma^D[\lambda_l = +1/2]}{dq^2 d\cos\theta} = \frac{G_F^2 |V_{cb}|^2 q^2}{128\pi^3 m_B^2} \times \left(1 - \frac{m_l^2}{q^2}\right)^2 |\vec{\mathbf{p}}| \frac{m_l^2}{q^2} |H_0(q^2) \cos\theta - H_t(q^2)|^2$$

Hagiwara, Martin, Wade [Phys. Lett. B 228 (1989) 144, Nucl. Phys. B 327 (1989) 569]

Korner, Schuler [Z. Phys. C 46 (1990) 93]

Kamenik, Mescia [0802.3790]

$\bar{B} \rightarrow D^* l \bar{\nu}$ hadronic matrix elements

- $\langle D^*(p_{D^*}, \epsilon^*) | \bar{c} \gamma_\mu b | \bar{B}(p_B) \rangle = \frac{2iV(q^2)}{m_B + m_{D^*}} \epsilon_{\mu\nu\alpha\beta} \epsilon^{*\nu} p_B^\alpha p_{D^*}^\beta,$
- $\langle D^*(p_{D^*}, \epsilon^*) | \bar{c} \gamma_\mu \gamma_5 b | \bar{B}(p_B) \rangle = 2m_{D^*} A_0(q^2) \frac{\epsilon^* \cdot q}{q^2} q_\mu$
 $+ (m_B + m_{D^*}) A_1(q^2) \left(\epsilon_\mu^* - \frac{\epsilon^* \cdot q}{q^2} q_\mu \right)$
 $- A_2(q^2) \frac{\epsilon^* \cdot q}{m_B + m_{D^*}} \left[(p_B + p_{D^*})_\mu - \frac{m_B^2 - m_{D^*}^2}{q^2} q_\mu \right].$

Hagiwara, Martin, Wade [Phys. Lett. B 228 (1989) 144, Nucl. Phys. B 327 (1989) 569]

Korner, Schuler [Z. Phys. C 46 (1990) 93]

Fajfer, Kamenik, Nisandzic [1203.2654]

$B \rightarrow D^*$ form factors

$$\begin{aligned} V(q^2) &= \frac{R_1(w)}{R_{D^*}} h_{A_1}(w) & A_0(q^2) &= \frac{R_0(w)}{R_{D^*}} h_{A_1}(w) \\ A_1(q^2) &= R_{D^*} \frac{w+1}{2} h_{A_1}(w) & A_2(q^2) &= \frac{R_2(w)}{R_{D^*}} h_{A_1}(w) \end{aligned}$$

$$h_{A_1}(w) = h_{A_1}(1) [1 - 8\rho^2 z(w) + (53\rho^2 - 15) z(w)^2 - (231\rho^2 - 91) z(w)^3]$$

$$R_0(w) = R_0(1) - 0.11(w-1) + 0.01(w-1)^2$$

$$R_1(w) = R_1(1) - 0.12(w-1) + 0.05(w-1)^2$$

$$R_2(w) = R_2(1) - 0.11(w-1) - 0.06(w-1)^2 \quad \text{Caprini, Lellouch, Neubert [9712417]}$$

$h_{A_1}(1)$, ρ^2 , $R_1(1)$ and $R_2(1)$ values from $\bar{B} \rightarrow D^* \ell \bar{\nu}$ ($\ell = e, \mu$) [HFAG](#)

$R_0(1)$ extracted from Heavy Quark Effective Theory [\[Falk, Neubert \(1992\)\]](#)

$$R_3(1) = \frac{R_2(1)(1-r) + r [R_0(1)(1+r) - 2]}{(1-r)^2} = 0.97 \pm 0.10$$

includes leading-order perturbative (in α_s) and power ($1/m_{b,c}$) corrections to the heavy-quark limit, plus 10% uncertainty to account for higher-order contributions.

$\bar{B} \rightarrow D^* l \bar{\nu}$ helicity amplitudes

- $H_{\pm\pm}(q^2) = (m_B + m_{D^*}) A_1(q^2) \mp \frac{2m_B}{m_B + m_{D^*}} |\vec{\mathbf{p}}| V(q^2)$
- $H_{00}(q^2) = \frac{1}{2m_{D^*} \sqrt{q^2}} [(m_B^2 - m_{D^*}^2 - q^2) (m_B + m_{D^*}) A_1(q^2) - \frac{4m_B^2 |\vec{\mathbf{p}}|^2}{m_B + m_{D^*}} A_2(q^2)]$
- $H_{0t}(q^2) = \frac{2m_B |\vec{\mathbf{p}}|}{\sqrt{q^2}} A_0(q^2)$

Hagiwara, Martin, Wade [Phys. Lett. B 228 (1989) 144, Nucl. Phys. B 327 (1989) 569]

Korner, Schuler [Z. Phys. C 46 (1990) 93]

Fajfer, Kamenik, Nisandzic [1203.2654]

$\bar{B} \rightarrow D^* l \bar{\nu}$ differential decay width

- $$\frac{d^2\Gamma^{D^*}[\lambda_l = -1/2]}{dq^2 d\cos\theta} = \frac{G_F^2 |V_{cb}|^2 |\vec{\mathbf{p}}| q^2}{256\pi^3 m_B^2} \left(1 - \frac{m_l^2}{q^2}\right)^2$$
$$\times \left[(1 - \cos\theta)^2 |H_{++}|^2 + (1 + \cos\theta)^2 |H_{--}|^2 + 2\sin^2\theta |H_{00}|^2 \right]$$
- $$\frac{d^2\Gamma^{D^*}[\lambda_l = +1/2]}{dq^2 d\cos\theta} = \frac{G_F^2 |V_{cb}|^2 |\vec{\mathbf{p}}| q^2}{256\pi^3 m_B^2} \left(1 - \frac{m_l^2}{q^2}\right)^2 \frac{m_l^2}{q^2}$$
$$\times \left[\sin^2\theta (|H_{++}|^2 + |H_{--}|^2) + 2 |H_{0t} - H_{00} \cos\theta|^2 \right]$$

Hagiwara, Martin, Wade [Phys. Lett. B 228 (1989) 144, Nucl. Phys. B 327 (1989) 569]

Korner, Schuler [Z. Phys. C 46 (1990) 93]

Fajfer, Kamenik, Nisandzic [1203.2654]