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Implications of $Br(\mu \rightarrow e\gamma)$ and Δa_μ on Muonic Lepton Flavor Violating Processes

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Motivation

- Charged lepton flavor violation decays are prohibited in the SM
- MEG recently set a tight bound on $Br(\mu \rightarrow e \gamma)$

$$Br(\mu^+ \rightarrow e^+ \gamma) < 5.7 \times 10^{-13}$$

- Muon g-2 remains an unsolved puzzle ($3.x\sigma$) (since 2001)

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (287 \pm 63 \pm 49) \times 10^{-11}$$

- Bounds on $\mu \rightarrow e \gamma$, $3e$, muon to electron conversions ($\mu N \rightarrow e N$) are constantly improved

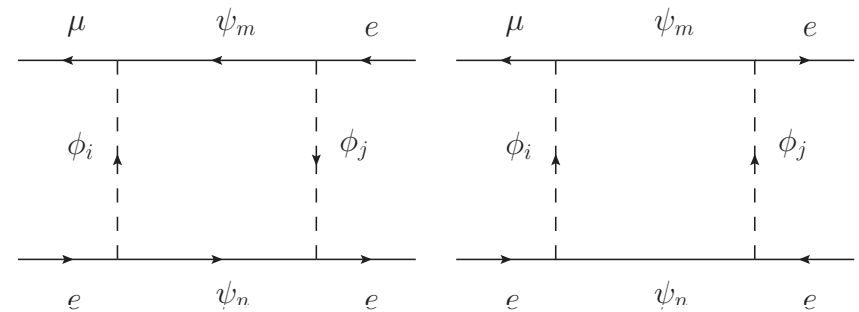
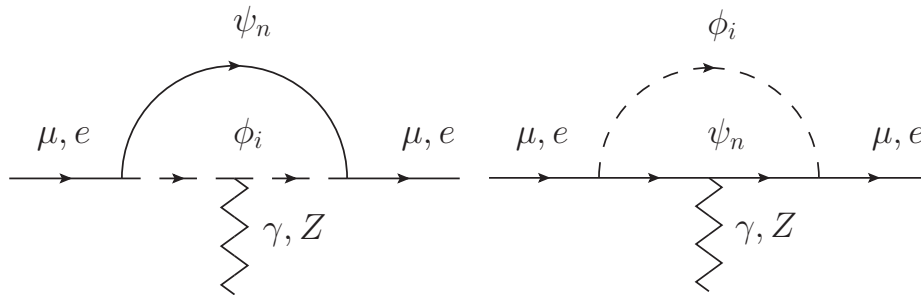
Current limits and future sensitivities

	current limit	future sensitivity
$\mathcal{B}(\mu^+ \rightarrow e^+ \gamma)$	$< 5.7 \times 10^{-13}$	10^{-13}
$\mathcal{B}(\mu^+ \rightarrow e^+ e^+ e^-)$	$< 1.0 \times 10^{-12}$	$10^{-14} - 10^{-16}$
$\mathcal{B}(\mu^- \text{Ti} \rightarrow e^- \text{Ti})$	$< 4.3 \times 10^{-12}$	10^{-18}
$\mathcal{B}(\mu^- \text{Au} \rightarrow e^- \text{Au})$	$< 7 \times 10^{-13}$	$10^{-14} - 10^{-16}$
$\mathcal{B}(\mu^- \text{Al} \rightarrow e^- \text{Al})$...	10^{-16}

- “Ratios of current bounds” $\sim O(1\sim 10)$.
- Sensitivities will be improved by 1-6 orders of magnitudes in future

We consider...

- Muon g-2 and LFV generated by ϕ - ψ one-loop dig.s:



$$\Delta a_\mu, \mu \rightarrow e\gamma, 3e, \mu N \rightarrow eN$$

$$\mu \rightarrow 3e$$

- Use a bottom up approach:
data \rightarrow couplings, masses
- Study the correlations among these processes

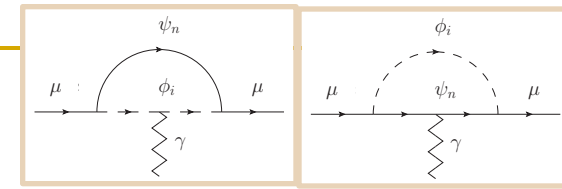
Investigate Two Cases:

- Case I: Cancellations among diagrams are not effective (\sim order of magnitudes)
- Case II: Have some built-in cancellations, e.g. SGIM.

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Muon $g-2$ (case I)



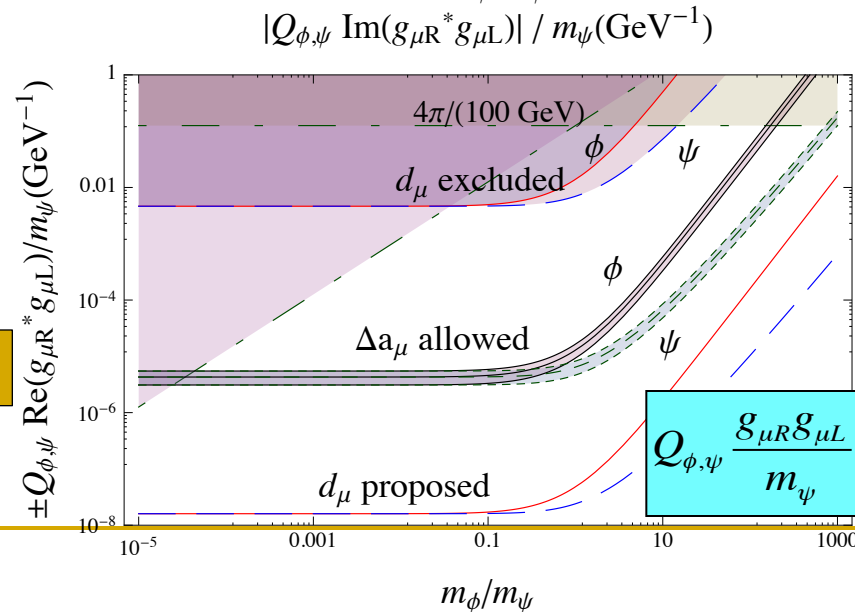
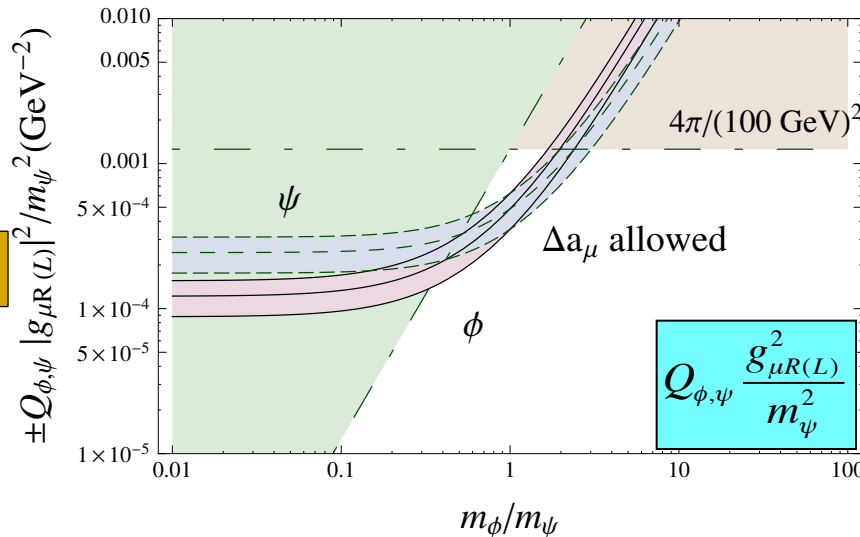
- $g_{R(L)}$: couplings of $\mu_{R(L)}-\psi-\phi$ int.

- $g_R g_R$ ($g_L g_L$) term:

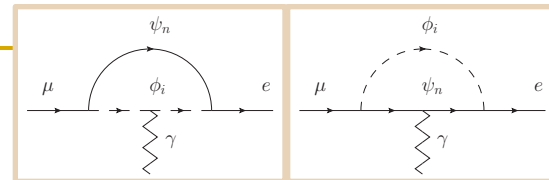
- From $g^2 < 4\pi$ and $m_{\psi,\phi} > 100\text{GeV}$:
 $m_{\psi,\phi} < 300(200)\text{GeV}$ (tight)
- $g \sim e$: $m_{\psi,\phi} = 10-30\text{GeV}$ (disfavored)

- $g_R g_L$ term: (chiral enh.)

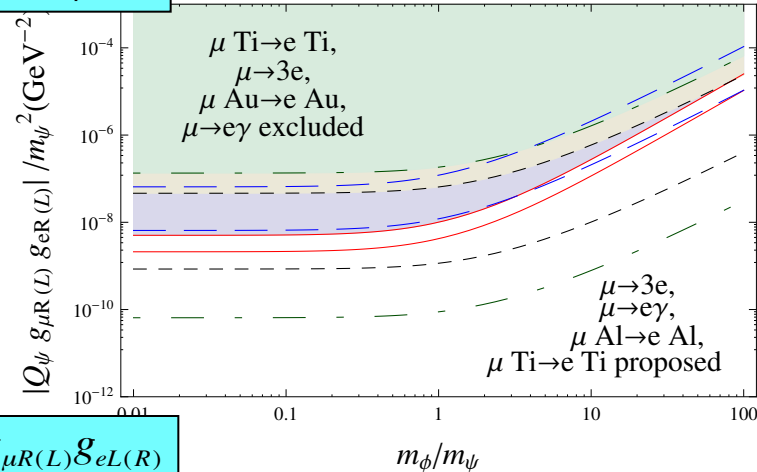
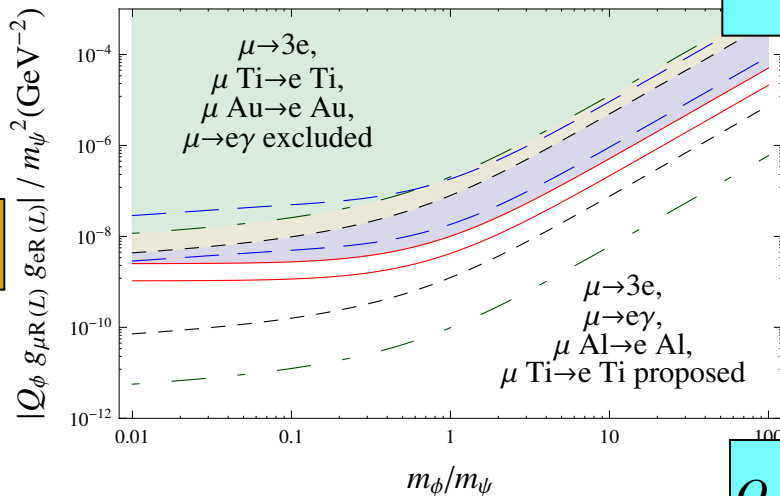
- From $g^2 < 4\pi$ and $m_{\psi,\phi} > 100\text{GeV}$:
 $m_\phi < 100\text{TeV}$, $m_\psi < 3000\text{TeV}$
- $g \sim e$: $m_\psi \sim 20\text{TeV}$
- More sensitive than the RR case



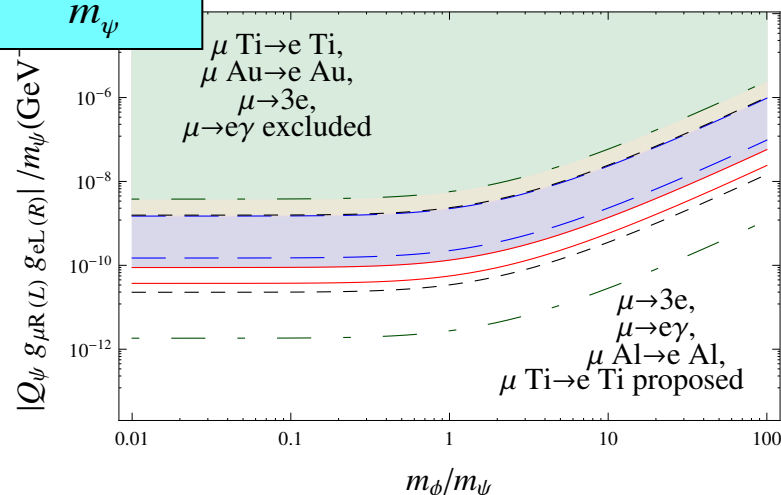
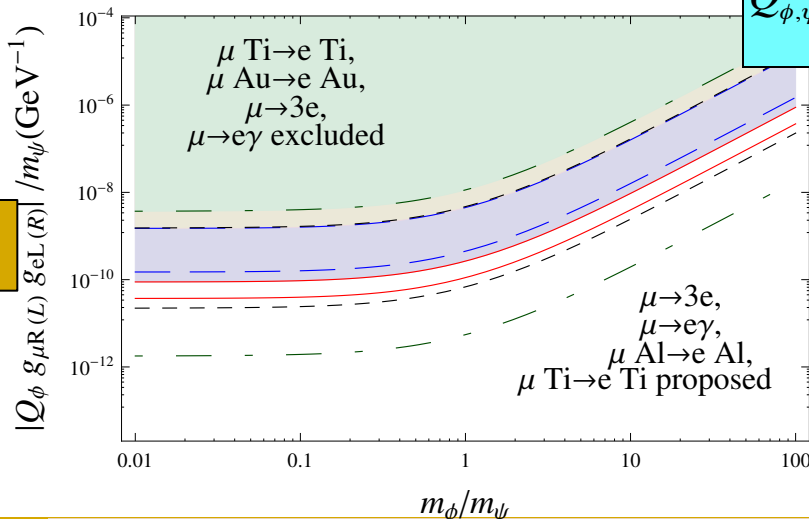
μ LFV (penguins) (case I)



$$Q_{\phi,\psi} \frac{g_{\mu R(L)} g_{e R(L)}}{m_\psi^2}$$



$$Q_{\phi,\psi} \frac{g_{\mu R(L)} g_{e L(R)}}{m_\psi}$$



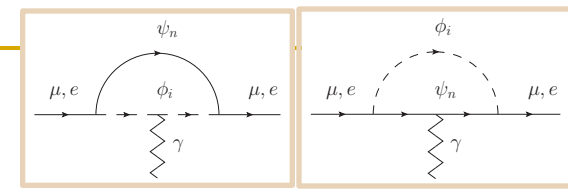
10^{-8}

10^{-9}

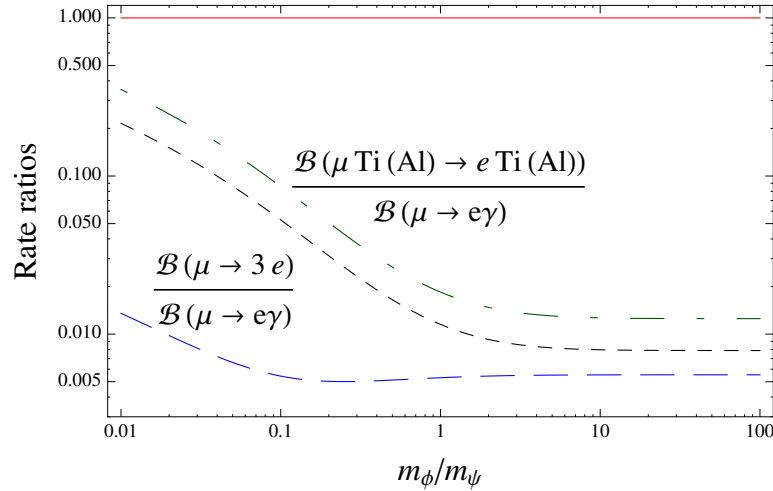
Sensitive in RL is more than 3 orders of mag. better than the RR case

$\mu \rightarrow e \gamma$ bound is most severe

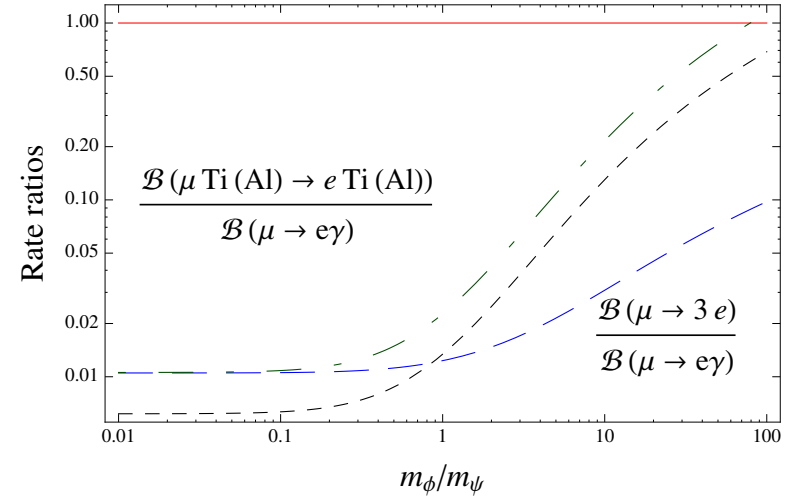
μ LFV (penguins) (case I)



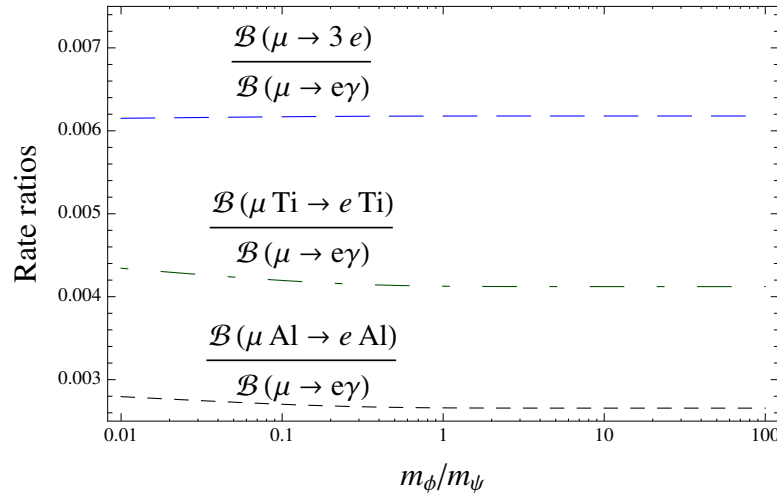
$$Q_\phi g_{\mu R(L)} g_{eR(L)}$$



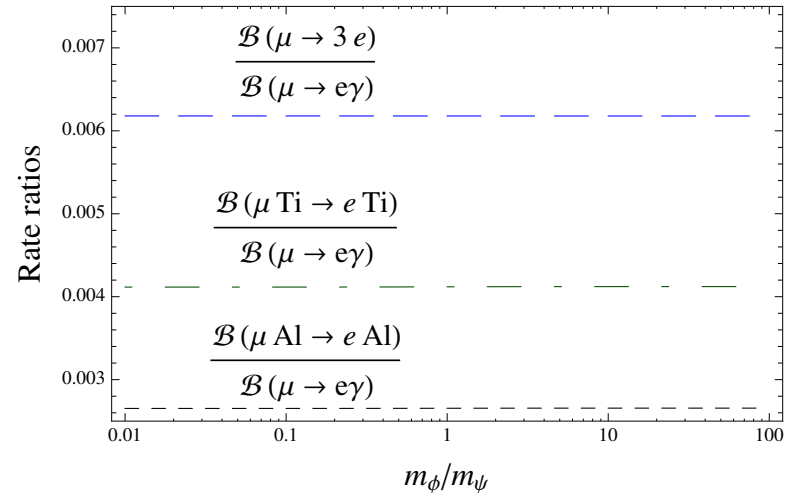
$$Q_\psi g_{\mu R(L)} g_{eR(L)}$$



$$Q_\phi g_{\mu R(L)} g_{eL(R)}$$



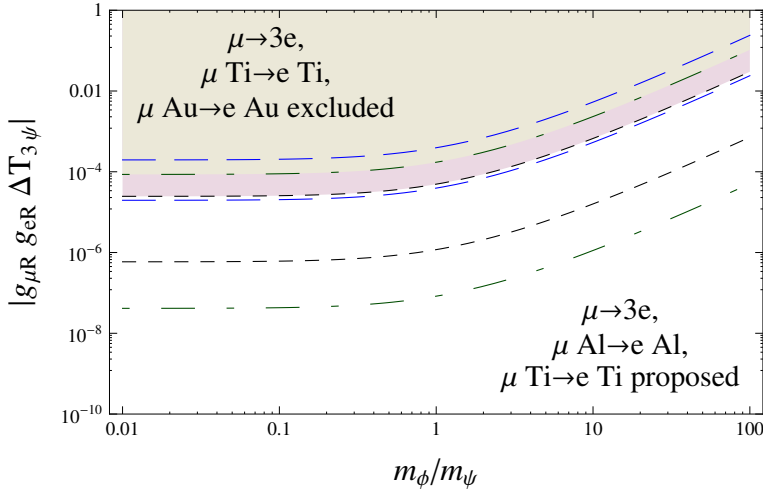
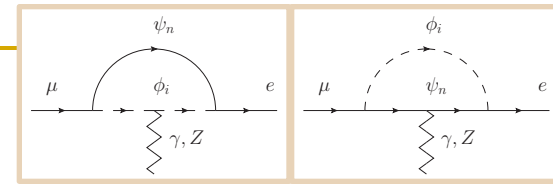
$$Q_\psi g_{\mu R(L)} g_{eL(R)}$$



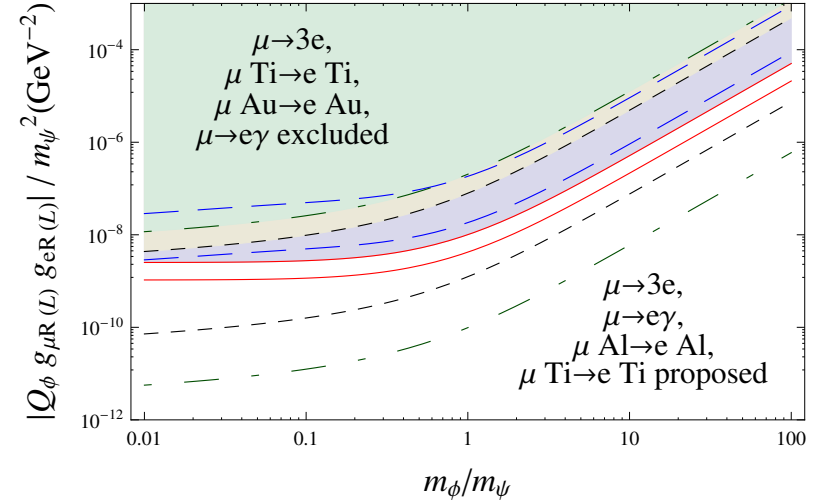
Exp. bound ratios $\sim O(1\sim 10)$

$\mu \rightarrow e\gamma$ constrains other processes

μ LFV (Z-penguins) (case I)



Z-peg.

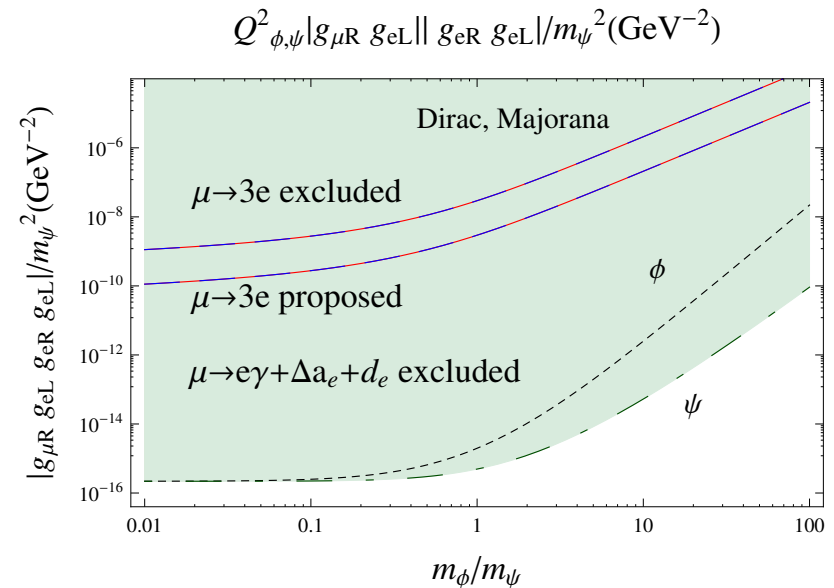
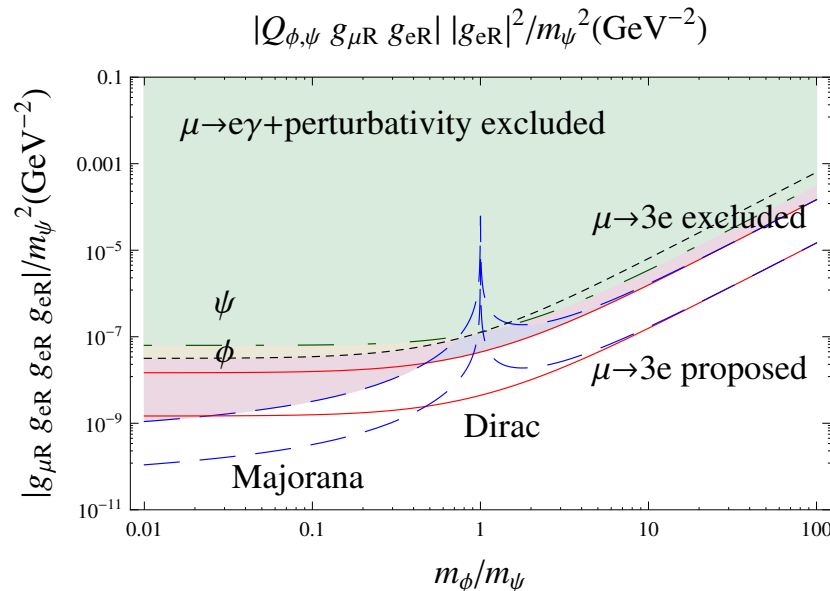
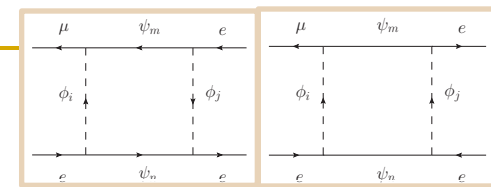


γ -peg.

- For $m_\psi = (>) O(100) \text{ GeV}$, Z-peng. has similar (better) sensitivity as the RR γ -peng.
- Z-peng is less sensitive than the RL γ -peng. unless m_ψ is as heavy as $O(100) \text{ TeV}$
- $\text{Br}(Z \rightarrow \mu e) < 10^{-13 \sim 15}$ [$\text{Br}_{UL}(Z \rightarrow \mu e) \sim 10^{-6}$]

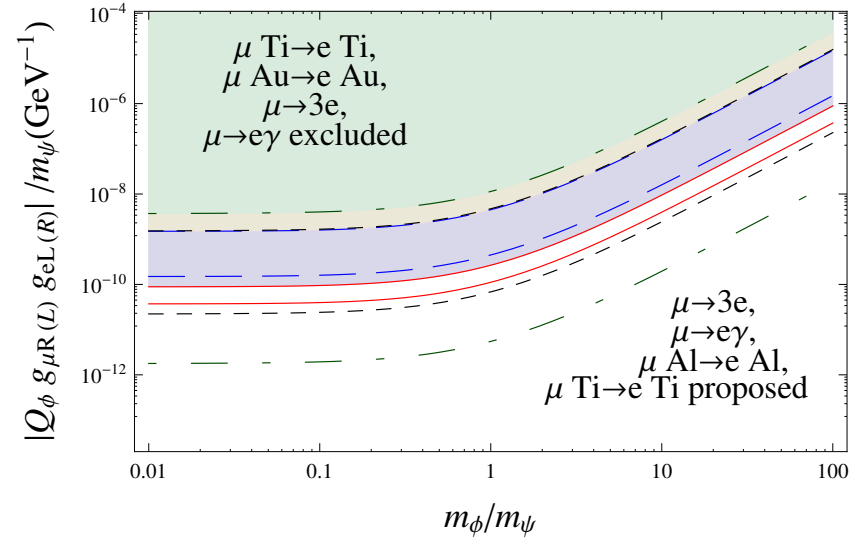
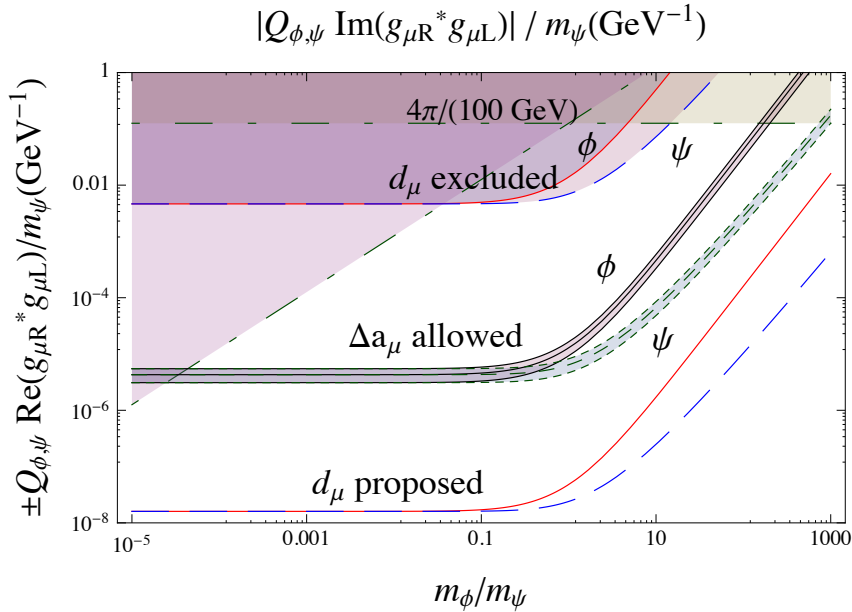
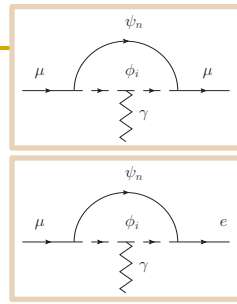
$$\Delta T_{3\psi mn} \equiv V_{mp}^R T_{3\psi RP} V_{pn}^{\dagger L} - V_{mp}^L T_{3\psi LP} V_{pn}^{\dagger R}$$

μ LFV (boxes) (case I)



- Dirac and Majorana cases have different sensitivities
- $\mu \rightarrow e \gamma + \text{perturbativity} (+\Delta a_\mu + \text{edm})$ exclude some (most) parameter space.

Comparing $Br(\mu \rightarrow e \gamma)$ and Δa_μ



$$\frac{g_{\mu R(L)} g_{e L(R)}}{g_{\mu R} g_{\mu L}} = \frac{g_{e L(R)}}{g_{\mu L(R)}} \leq 2.1 \times 10^{-5} \simeq \lambda^7$$

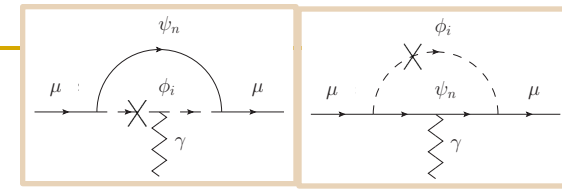
- The ratio is smaller than any known coupling ratio among 1st and 2nd generations. $\frac{g_e}{g_\mu} \approx \frac{m_e}{m_\mu} \approx \lambda^{3\sim 4}$

Investigate Two Cases:

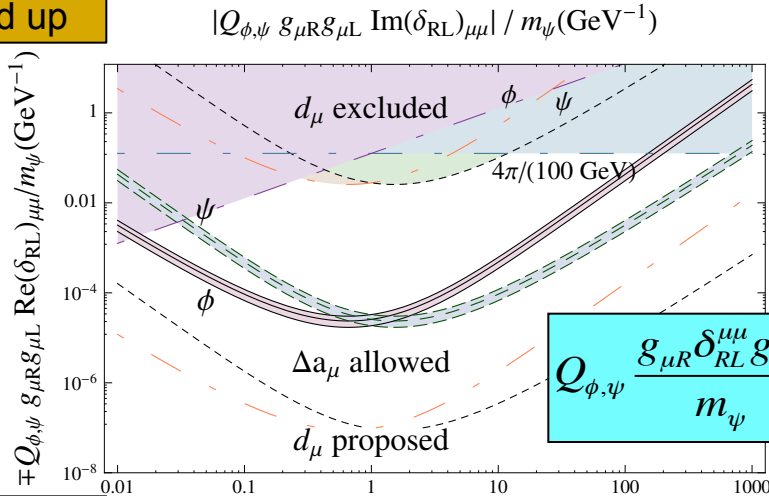
- Case I: Cancellations among diagrams are not effective (\sim order of magnitudes)

- ⇒ ■ Case II: Have some built-in cancellations, e.g. SGIM.

Muon g-2 (case II)



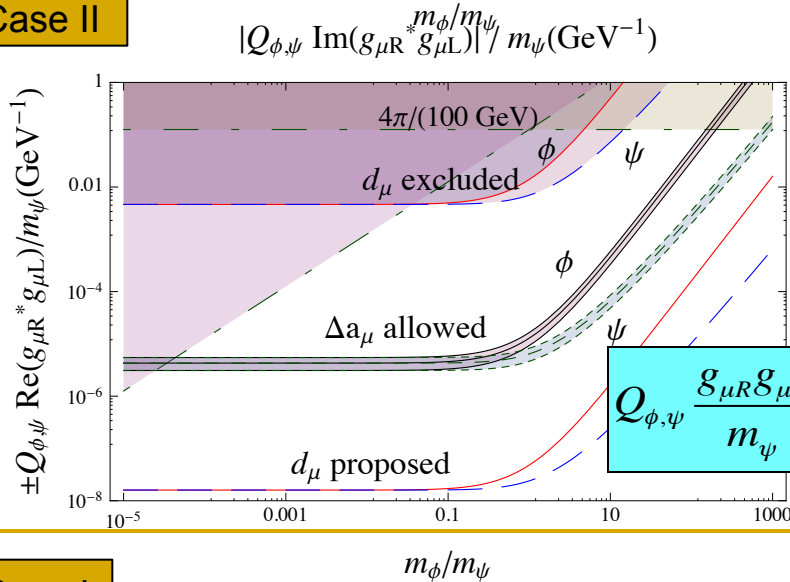
Bend up



- $\delta = (\delta m^2 / m^2)_\phi$: mixing angle
- $g_{R(L)} g_{R(L)}$ term same as case I

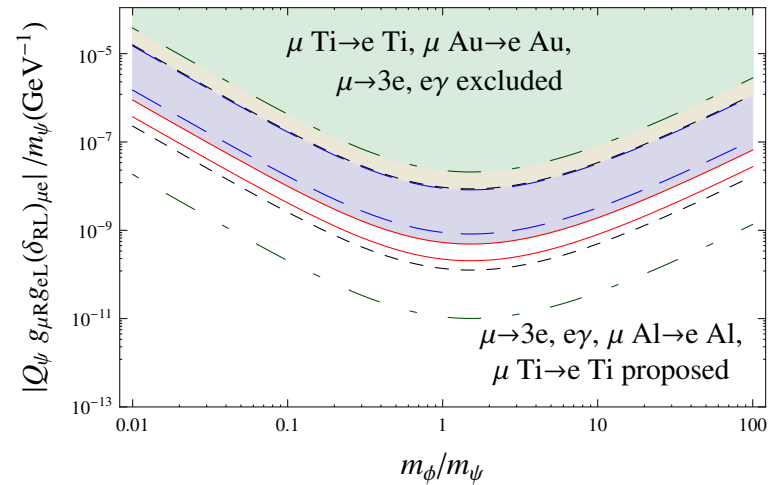
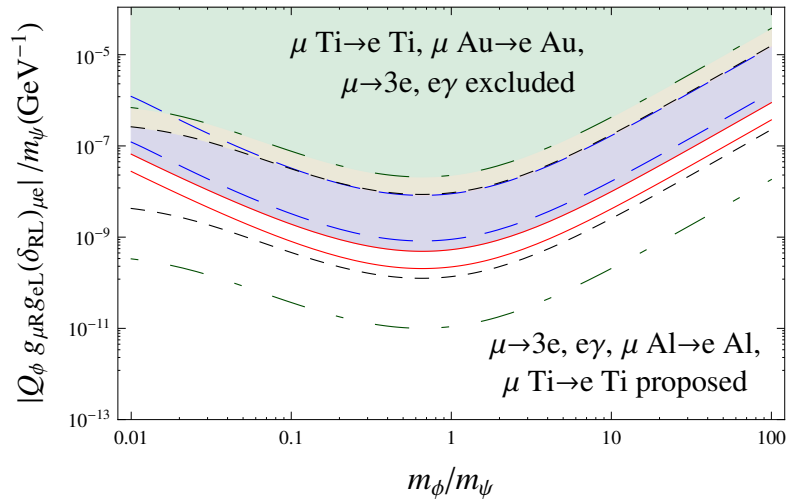
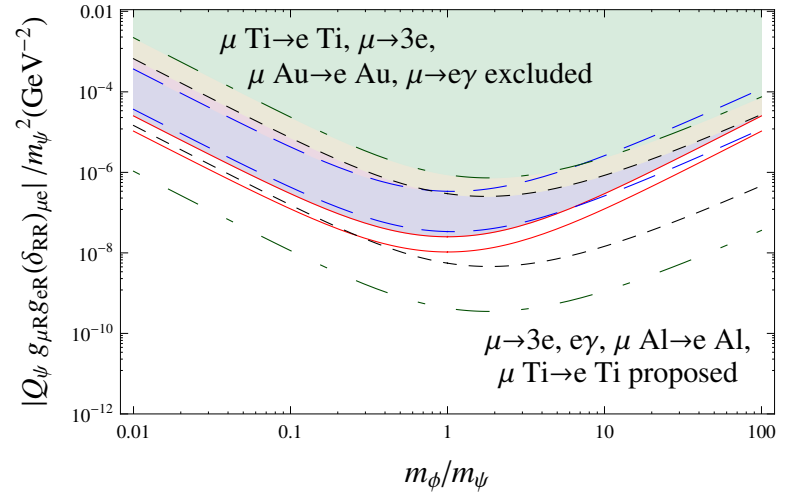
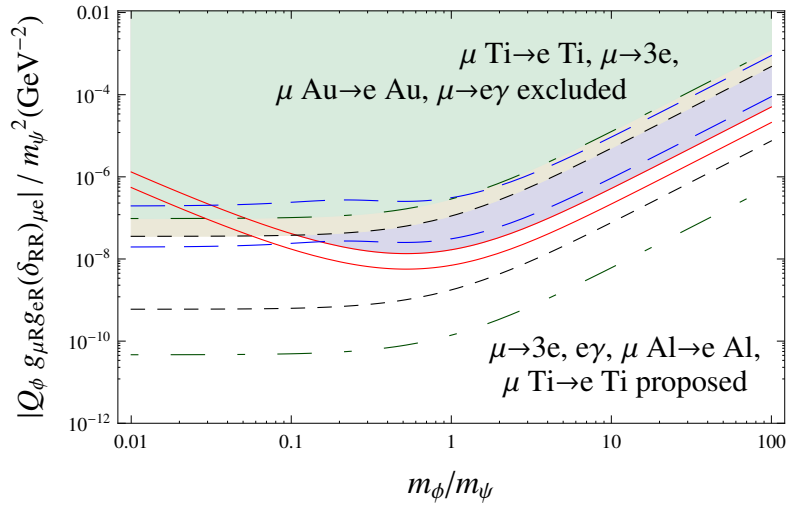
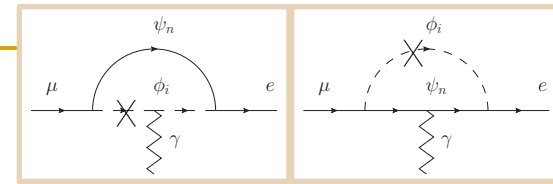
- $g_R g_L$ term: (chiral enh.)
- Cancellation is working at the low m_ϕ / m_ψ mass ratio region
- need larger couplings, smaller mass
- From $g^2 < 4\pi$ and $m_{\psi,\phi} > 100 \text{ GeV}$:
 $m_\phi < 100 \text{ TeV}$, $m_\psi < \text{few TeV}$
 $[m_\phi < 100 \text{ TeV}, m_\psi < 3000 \text{ TeV (case I)]$
- For $g \sim e$, $\delta = 1$, $m_\phi = m_\psi \sim 3 \text{ TeV}$
 $[m_\psi = 20 \text{ TeV (case I)]$

Case II



Case I

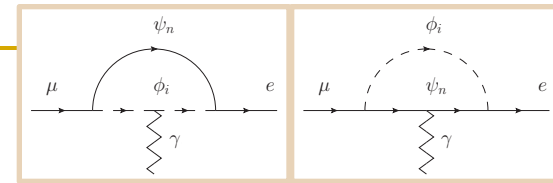
μ LFV (penguins) (case II)



Sensitivities are relaxed

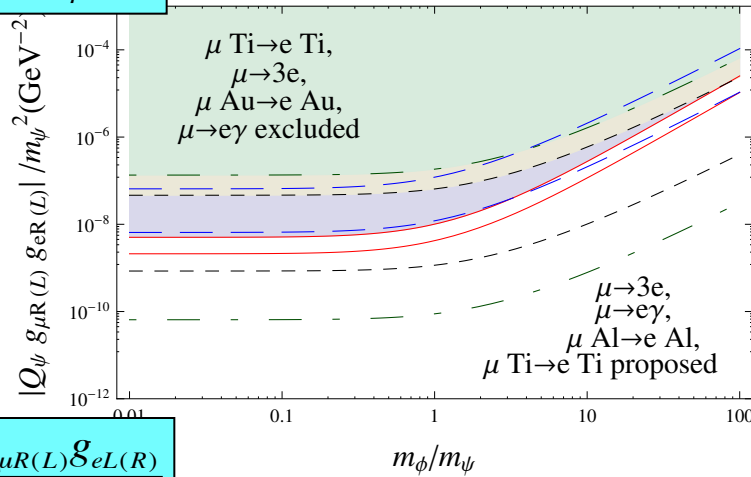
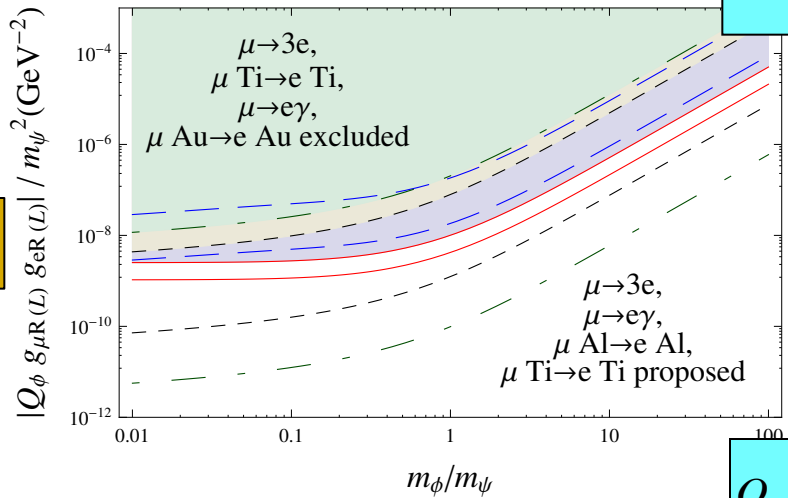
$\mu \rightarrow e\gamma$ bound is not always
the most stringent one

For comparison, recall...

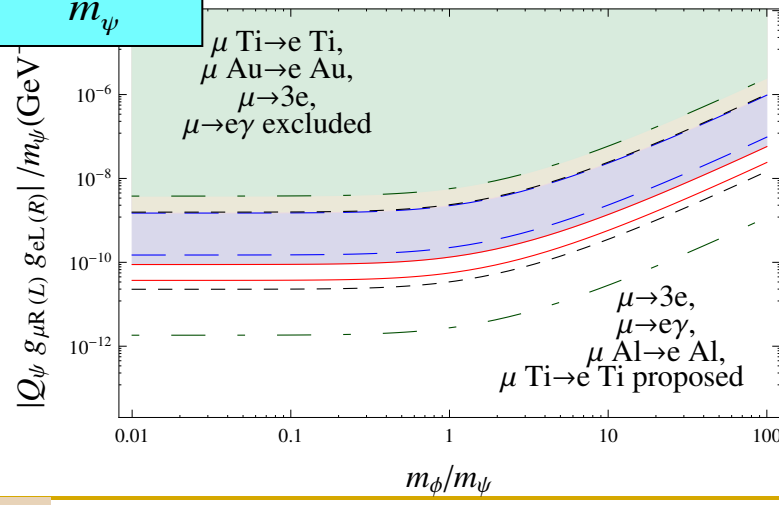
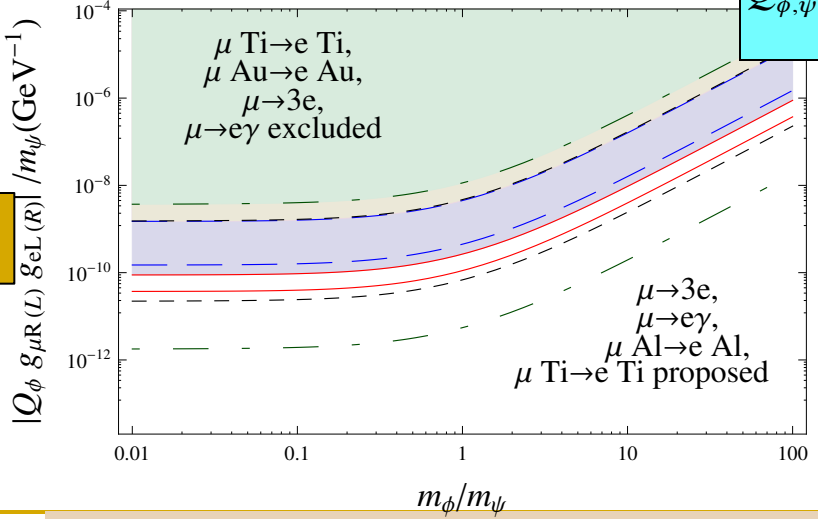


μ LFV (penguins) (case I)

$$Q_{\phi,\psi} \frac{g_{\mu R(L)} g_{e R(L)}}{m_\psi^2}$$



$$Q_{\phi,\psi} \frac{g_{\mu R(L)} g_{e L(R)}}{m_\psi}$$



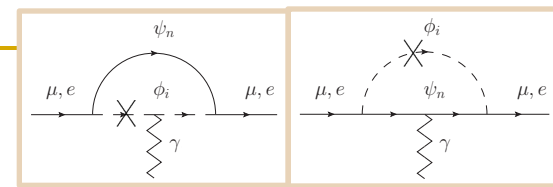
10^{-8}

10^{-9}

Sensitive in RL is more than 3 orders of mag. better than the RR case

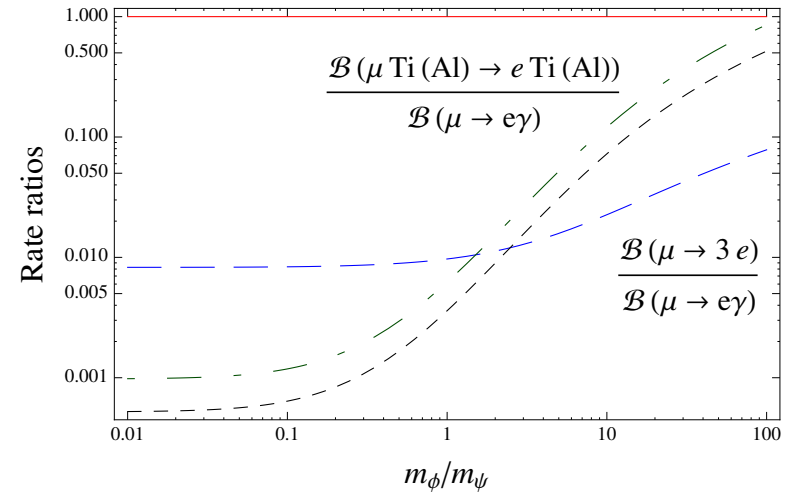
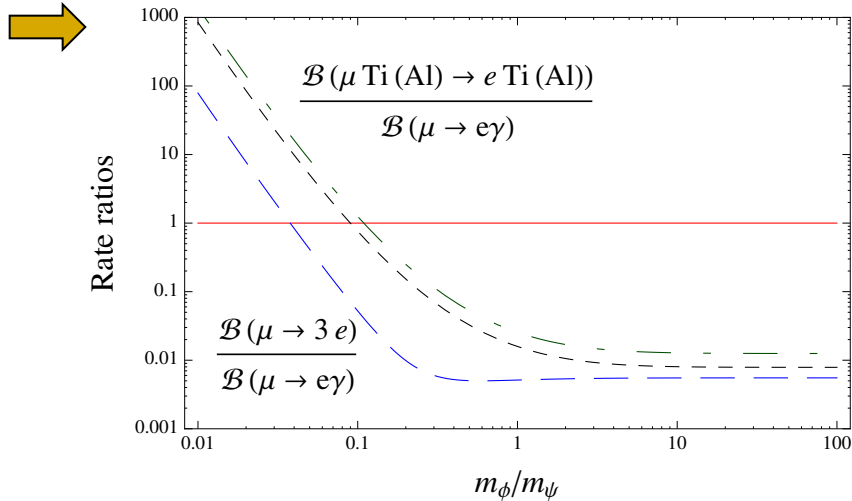
$\mu \rightarrow e \gamma$ bound is most severe

μ LFV (penguins) (case II)



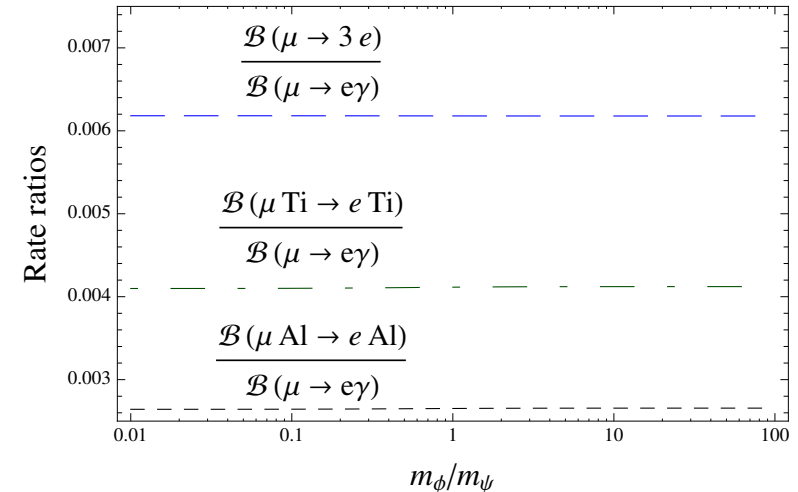
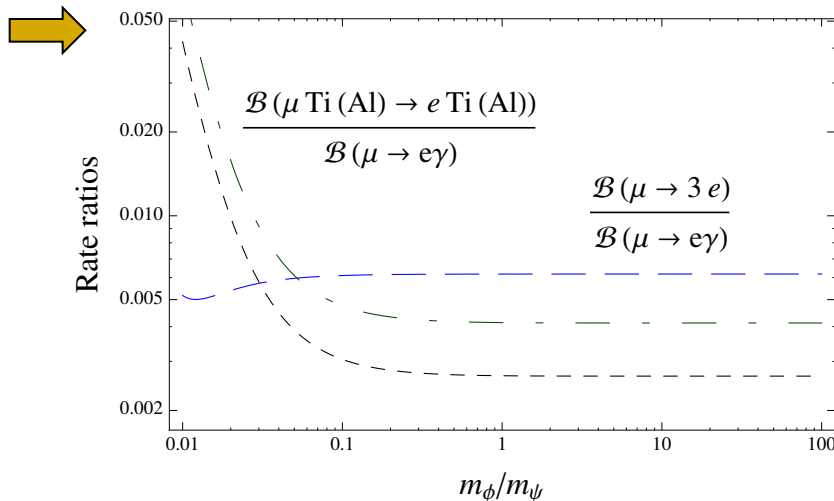
$Q_\phi g_{\mu R} g_{eR} (\delta_{RR})_{\mu e}$

$Q_\psi g_{\mu R} g_{eR} (\delta_{RR})_{\mu e}$



$Q_\phi g_{\mu R} g_{eL} (\delta_{RL})_{\mu e}$

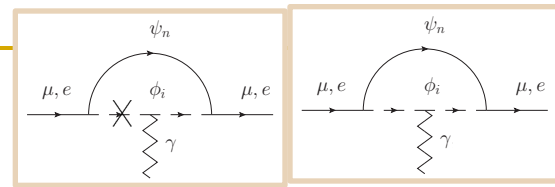
$Q_\psi g_{\mu R} g_{eL} (\delta_{RL})_{\mu e}$



$\mu N \rightarrow e N$ enhanced relatively ($B \sim 10^{-14}$)

$\mu \rightarrow e \gamma$ bound is not always the most stringent one

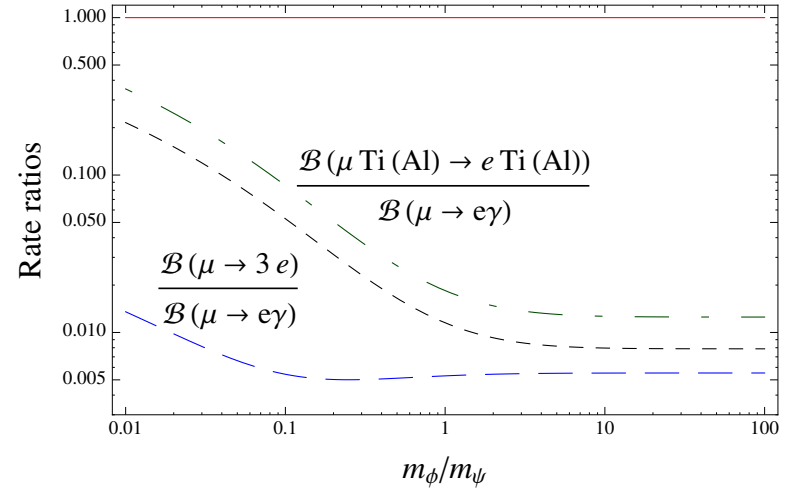
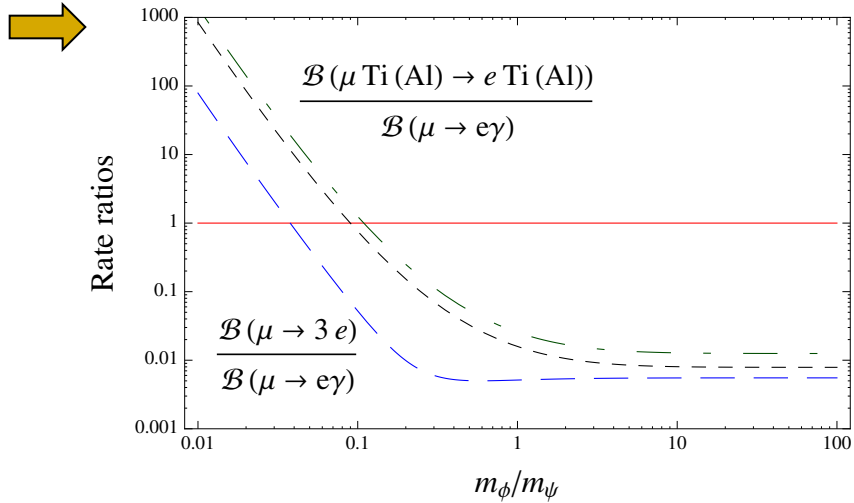
μ LFV (penguins) (comparing)



$Q_\phi g_{\mu R} g_{eR} (\delta_{RR})_{\mu e}$ **Case II**

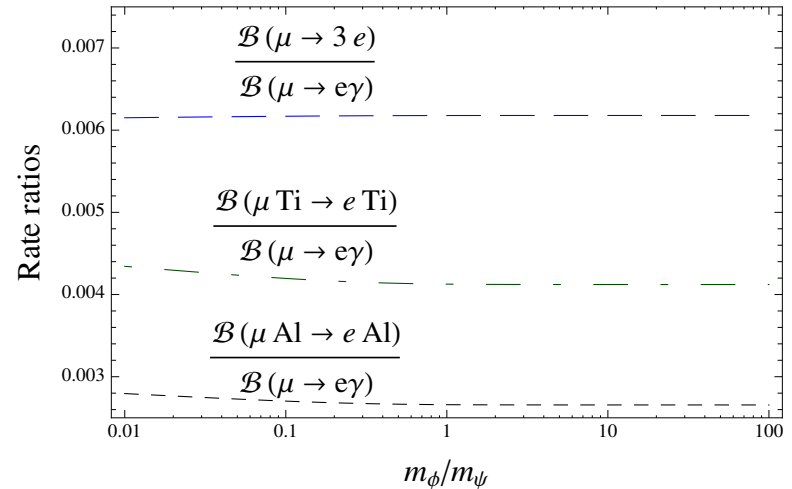
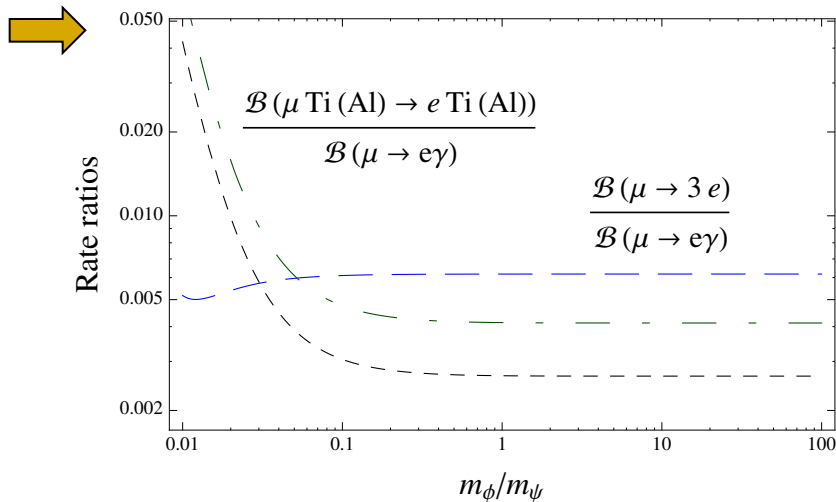
Case I

$Q_\phi g_{\mu R(L)} g_{eR(L)}$



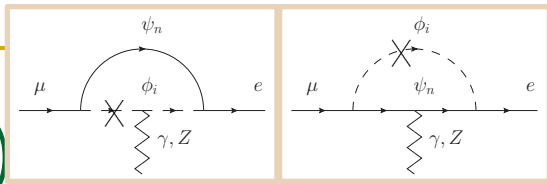
$Q_\phi g_{\mu R} g_{eL} (\delta_{RL})_{\mu e}$

$Q_\phi g_{\mu R(L)} g_{eL(R)}$

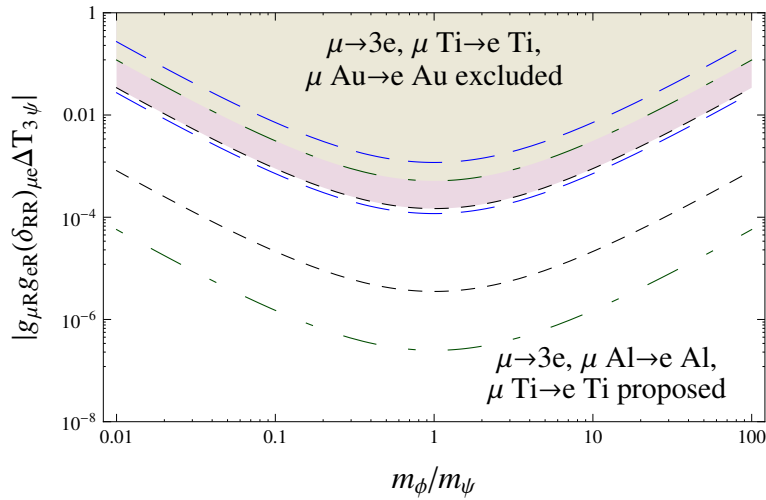


$\mu N \rightarrow e N$ is enhanced relatively in case II

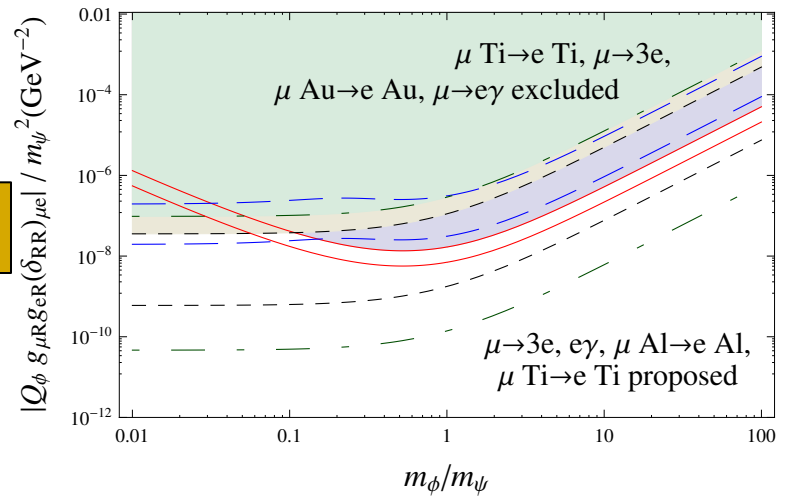
μ LFV (Z-penguins) (case II)



10⁻²



10⁻⁷

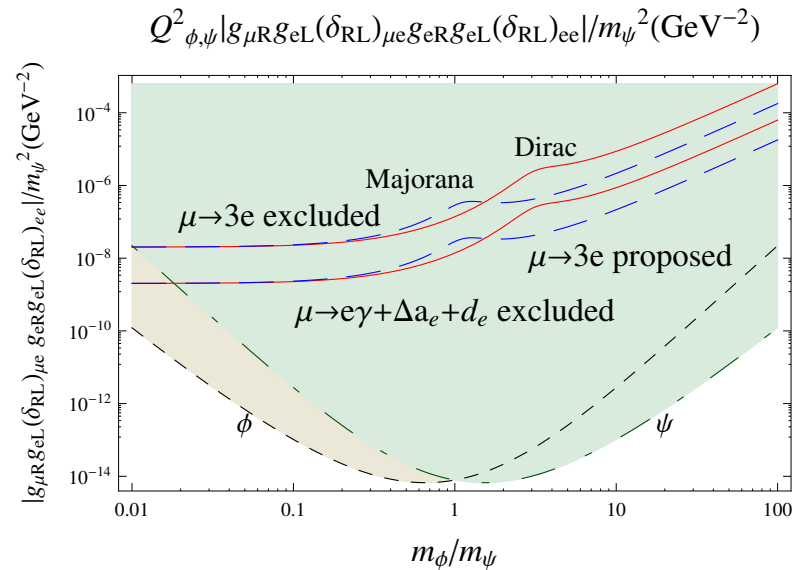
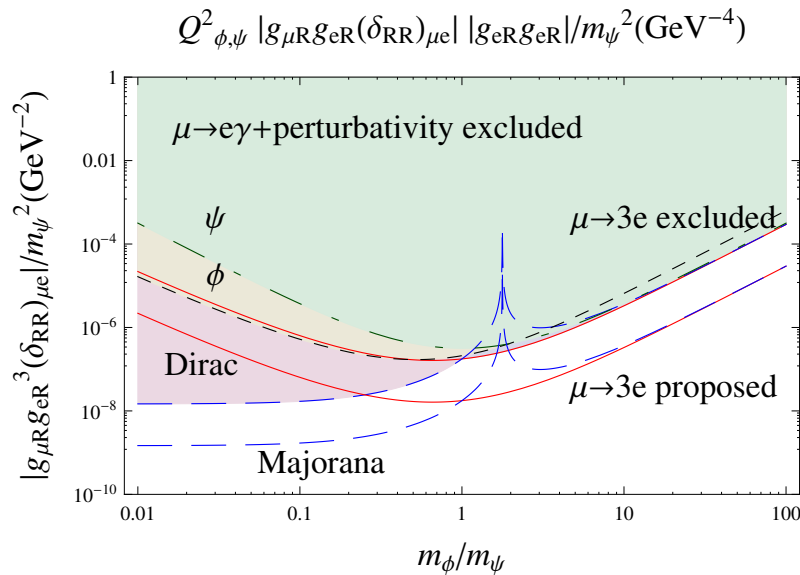
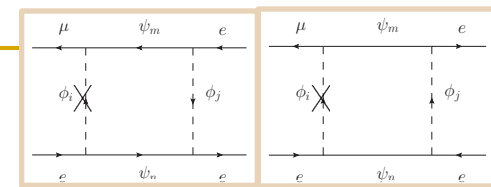


Z-peng.

γ -peng.

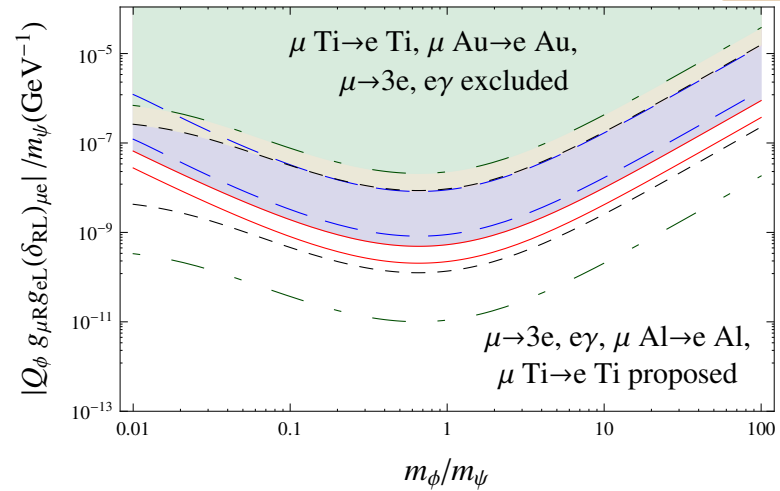
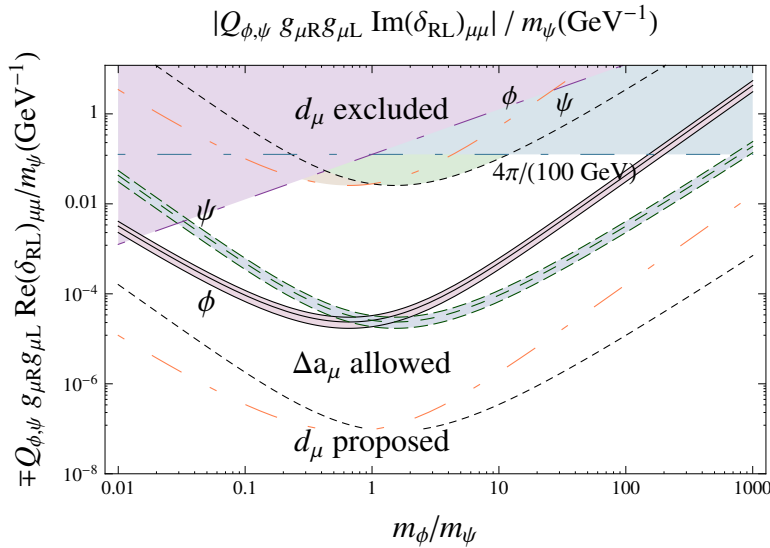
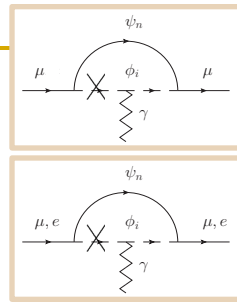
- Z-peng. sensitivity is relaxed in the low mass ratio region, for $m_\psi = (>)O(300\sim 1000)\text{GeV}$, Z-peng. has similar (better) sensitivity as the RR γ -peng.
- Z-peng. is less sensitive than the RL γ -peng. unless m_ψ is as heavy as $O(10^3)$ TeV (not supported by g-2 [$m_\psi < \text{few TeV}$])
- **Z-peng. is subdominant in this case.**
- $\text{Br}(Z \rightarrow \mu e) < 10^{-13\sim 15}$ [$\text{Br}_{\text{UL}}(Z \rightarrow \mu e) \sim 10^{-6}$]

μ LFV (boxes) (case II)



- Dirac and Majorana cases have different sensitivities
- $\mu \rightarrow e \gamma + \text{perturbativity} (+\Delta a_{\mu} + \text{edm})$ exclude some (most) parameter space.

Comparing $Br(\mu \rightarrow e\gamma)$ and Δa_μ



$$\frac{g_{\mu R(L)} g_{e L(R)} \text{Re}[(\delta_{RL(LR)})_{\mu e}]}{g_{\mu R} g_{\mu L} \text{Re}[(\delta_{RL})_{\mu\mu}]} = \frac{g_{e L(R)} \text{Re}[(\delta_{RL(LR)})_{\mu e}]}{g_{\mu L(R)} \text{Re}[(\delta_{RL})_{\mu\mu}]} \leq 2.1 \times 10^{-5} \simeq \lambda^7$$

■ Can be satisfied with

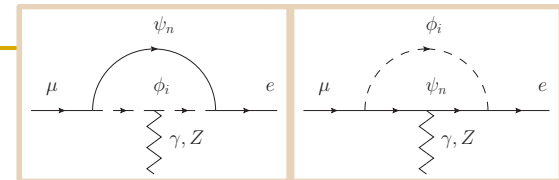
$$\frac{g_e}{g_\mu} \approx \frac{m_e}{m_\mu} \approx \lambda^{3\sim 4} \qquad \frac{\text{Re}[(\delta_{RL(LR)})_{\mu e}]}{\text{Re}[(\delta_{RL})_{\mu\mu}]} \leq \lambda^{3\sim 4}$$

Conclusion

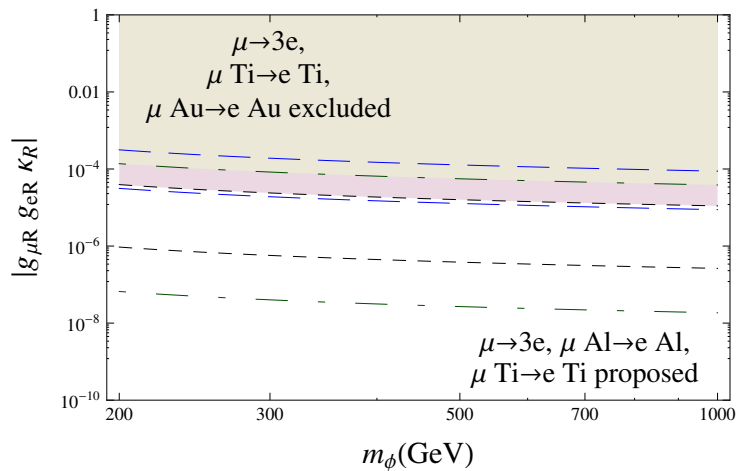
- Consider ψ - ϕ loop-induced LFV muon decays.
 - Bounds are translated to constraints on parameters (couplings and masses)
 - Muon $g-2$ favors non-chiral interaction
 - Z-penguin may play some role
- Box diagram contributions are highly constrained from other's
- Comparing different cases, we found that:
 - Case I (no cancellation):
 - Need fine-tune to satisfy $Br(\mu \rightarrow e \gamma)$ and Δa_μ
 - $\mu \rightarrow 3e$, $\mu N \rightarrow e N$ bounded by $\mu \rightarrow e \gamma$ (2~3 orders below expt.)
 - Case II (built-in cancellation):
 - Mixing angles soften the fine-tune in $Br(\mu \rightarrow e \gamma)$ and Δa_μ
 - $\mu \rightarrow 3e$ remains suppressed, but $\mu N \rightarrow e N$ is enhanced

Back up

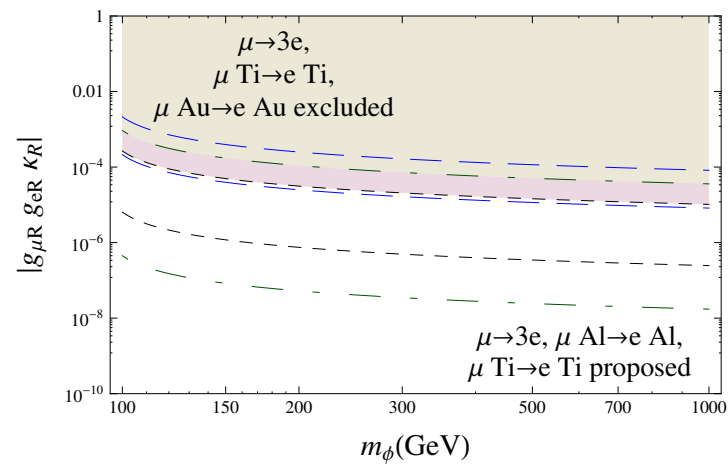
μ LFV (Z-penguins)



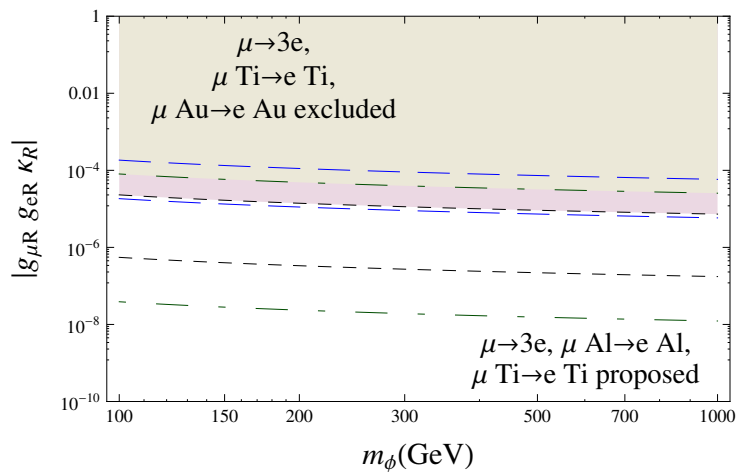
$m_\psi = 0.5m_\phi$



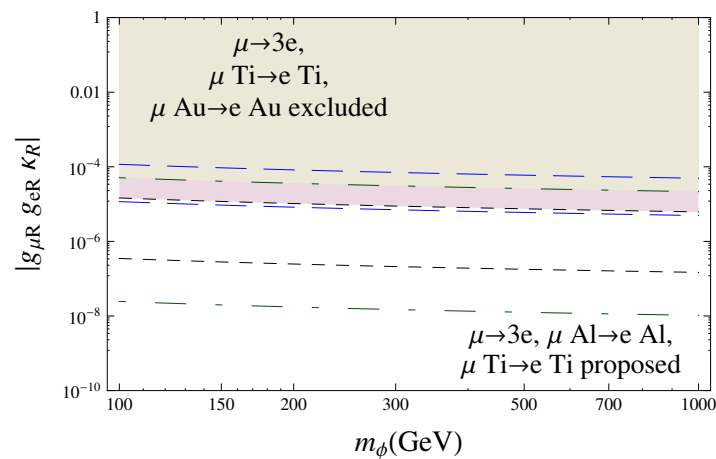
$m_\psi = m_\phi$



$m_\psi = 5m_\phi$



$m_\psi = 10m_\phi$



$$\kappa_{L(R)ijmn} \equiv \sin 2\theta_W (g_{L(R)}^Z \delta_{ij} \delta_{mn} - g_{\psi_{R(L)}}^Z \delta_{ij} - g_{\phi_{ij}}^Z \delta_{mn}) / e,$$