

ADVANCED *U&A* NUCLEON EM STRUCTURE MODEL AND ITS PREDICTABILITY

C.Adamuscin¹, E.Bartos¹, **S. Dubnička**¹, A.-Z. Dubničková²

¹Institute of Physics SAS, Bratislava, Slovakia

²Department of Theoretical Physics, Comenius University, Bratislava, Slovakia

20. July 2013

EPS HEP'13



1 INTRODUCTION

- Today's experimental situation

2 NUCLEON EM FFs *U&A* MODEL RESPECTING $SU(3)$ SYMMETRY AND OZI RULE VIOLATION

3 VECTOR AND TENSOR POLARIZATIONS IN $e^+e^- \rightarrow p\bar{p}$ PROCESS

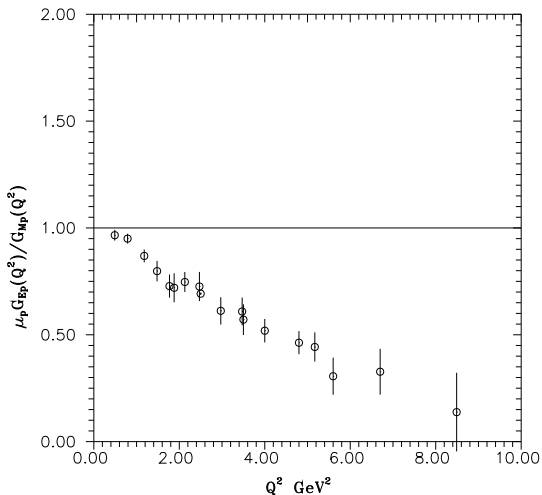
4 $1/2^+$ OCTET HYPERONS EM STRUCTURE

5 CONCLUSIONS



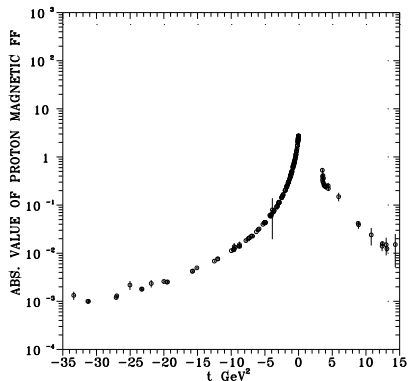
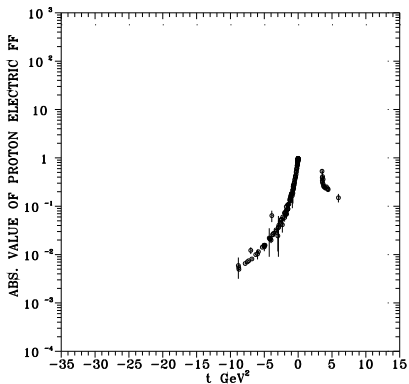
Today's experimental situation on the nucleon EM FFs $G_E^p(t)$ $G_M^p(t)$, $G_E^n(t)$, $G_M^n(t)$ is presented in the following Figs.



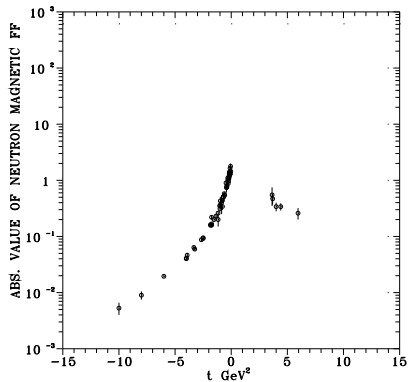
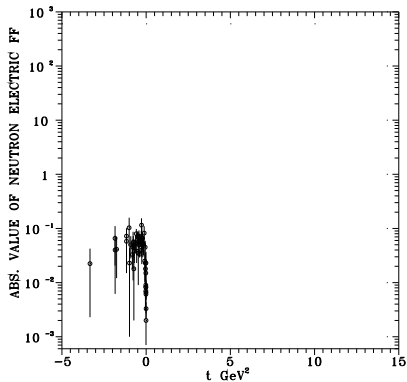


New JLab proton polarization data on the ratio $\mu_p G_{Ep}(t)/G_{Mp}(t)$ from polarization transfer $\vec{e}p \rightarrow e\vec{p}$ process.

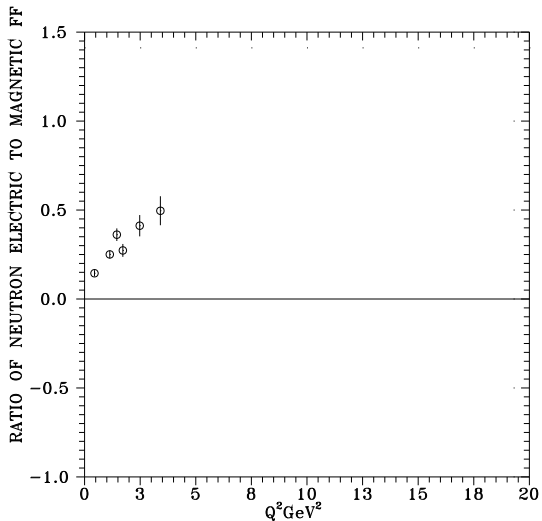




Experimental data on proton electric and magnetic form factors.



Experimental data on neutron electric and magnetic form factors.



Neutron polarization data on the ratio $\mu_n G_{En}(t)/G_{Mn}(t)$.



For a description of data **we shall apply the U&A approach**, which already appeared to be **very powerful in a description of the EM structure of the complete nonet** ($\pi^-, \pi^0, \pi^+, K^-, K^0, \bar{K}^0, K^+, \eta, \eta'$) **of pseudoscalar mesons.**

S.Dubnicka and A.Z.Dubnickova: Eur. Phys. J. Web of Conference 37 (2012) 01003



U&A MODEL OF NUCLEON EM STRUCTURE

Electric and magnetic FFs, $G_E(t)$ and $G_M(t)$, are **very suitable for extraction of experimental data** from the measured cross-sections.

However, for construction of various nucleon EM structure models the flavor-independent **iso-scalar and iso-vector parts of the Dirac and Pauli FFs** are more suitable.

Both sets are related

$$G_E^p(t) = [F_{1N}^s(t) + F_{1N}^v(t)] + \frac{t}{4m_p^2} [F_{2N}^s(t) + F_{2N}^v(t)]$$

$$G_M^p(t) = [F_{1N}^s(t) + F_{1N}^v(t)] + [F_{2N}^s(t) + F_{2N}^v(t)]$$

$$G_E^n(t) = [F_{1N}^s(t) - F_{1N}^v(t)] + \frac{t}{4m_n^2} [F_{2N}^s(t) - F_{2N}^v(t)]$$

$$G_M^n(t) = [F_{1N}^s(t) - F_{1N}^v(t)] + [F_{2N}^s(t) - F_{2N}^v(t)]$$



Consideration of the $SU(3)$ symmetry in EM structure model means
- **always complete trinity of vector-mesons ($\rho, \omega, \phi; \rho', \omega', \phi';$ etc.)**
has to be taken into account !

The **newest Review of Particle Physics**

J.Beringer et al (Particle Data Group), Phys. Rev. D86 (2012) 010001.

provides **just 3 complete trinities of such vector-meson resonances**

$\rho(770), \omega(782), \phi(1020)$

$\omega'(1420), \rho'(1450), \phi'(1680)$

$\omega''(1650), \rho''(1700), \phi''(2170).$

then also **OZI rule violation is fulfilled.**

As a result the 9-resonance (**3 iso-vectors and 6 iso-scalars**)

zero-width VMD parametrization of $F_{1N}^S(t), F_{1N}^V(t), F_{2N}^S(t), F_{2N}^V(t)$

can be written down.



U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 F_{1N}^s(t) = & \frac{1}{2} \frac{m_\omega^2 m_\phi^2}{(m_\omega^2 - t)(m_\phi^2 - t)} + \\
 + & \left\{ \frac{m_\phi^2 m_{\omega'}^2}{(m_\phi^2 - t)(m_{\omega'}^2 - t)} \frac{(m_\phi^2 - m_{\omega'}^2)}{(m_\phi^2 - m_\omega^2)} + \frac{m_\omega^2 m_{\omega'}^2}{(m_\omega^2 - t)(m_{\omega'}^2 - t)} \frac{(m_\omega^2 - m_{\omega'}^2)}{(m_\omega^2 - m_\phi^2)} - \right. \\
 & \left. - \frac{m_\omega^2 m_\phi^2}{(m_\omega^2 - t)(m_\phi^2 - t)} \right\} (f_{\omega' NN}^{(1)} / f_{\omega'}) + \\
 + & \left\{ \frac{m_\phi^2 m_{\phi'}^2}{(m_\phi^2 - t)(m_{\phi'}^2 - t)} \frac{(m_\phi^2 - m_{\phi'}^2)}{(m_\phi^2 - m_\omega^2)} + \frac{m_\omega^2 m_{\phi'}^2}{(m_\omega^2 - t)(m_{\phi'}^2 - t)} \frac{(m_\omega^2 - m_{\phi'}^2)}{(m_\omega^2 - m_\phi^2)} - \right. \\
 & \left. - \frac{m_\omega^2 m_\phi^2}{(m_\omega^2 - t)(m_\phi^2 - t)} \right\} (f_{\phi' NN}^{(1)} / f_{\phi'}) +
 \end{aligned}$$



U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 & + \left\{ \frac{m_\phi^2 m_{\omega''}^2}{(m_\phi^2 - t)(m_{\omega''}^2 - t)} \frac{(m_\phi^2 - m_{\omega''}^2)}{(m_\phi^2 - m_\omega^2)} + \frac{m_\omega^2 m_{\omega''}^2}{(m_\omega^2 - t)(m_{\omega''}^2 - t)} \frac{(m_\omega^2 - m_{\omega''}^2)}{(m_\omega^2 - m_\phi^2)} - \right. \\
 & \qquad \qquad \qquad \left. - \frac{m_\omega^2 m_\phi^2}{(m_\omega^2 - t)(m_\phi^2 - t)} \right\} (f_{\omega'' NN}^{(1)} / f_{\omega''}) + \\
 & + \left\{ \frac{m_\phi^2 m_{\phi''}^2}{(m_\phi^2 - t)(m_{\phi''}^2 - t)} \frac{(m_\phi^2 - m_{\phi''}^2)}{(m_\phi^2 - m_\omega^2)} + \frac{m_\omega^2 m_{\phi''}^2}{(m_\omega^2 - t)(m_{\phi''}^2 - t)} \frac{(m_\omega^2 - m_{\phi''}^2)}{(m_\omega^2 - m_\phi^2)} - \right. \\
 & \qquad \qquad \qquad \left. - \frac{m_\omega^2 m_\phi^2}{(m_\omega^2 - t)(m_\phi^2 - t)} \right\} (f_{\phi'' NN}^{(1)} / f_{\phi''}).
 \end{aligned}$$



$$\begin{aligned}
 F_{1N}^{\nu}(t) = & \frac{1}{2} \frac{m_{\rho}^2 m_{\rho'}^2}{(m_{\rho}^2 - t)(m_{\rho'}^2 - t)} + \\
 + & \left\{ \frac{m_{\rho'}^2 m_{\rho''}^2}{(m_{\rho'}^2 - t)(m_{\rho''}^2 - t)} \frac{(m_{\rho'}^2 - m_{\rho''}^2)}{(m_{\rho'}^2 - m_{\rho}^2)} + \frac{m_{\rho}^2 m_{\rho''}^2}{(m_{\rho}^2 - t)(m_{\rho''}^2 - t)} \frac{(m_{\rho}^2 - m_{\rho''}^2)}{(m_{\rho}^2 - m_{\rho'}^2)} - \right. \\
 & \left. - \frac{m_{\rho}^2 m_{\rho'}^2}{(m_{\rho}^2 - t)(m_{\rho'}^2 - t)} \right\} (f_{\rho'' NN}^{(1)} / f_{\rho''}).
 \end{aligned}$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 F_{2N}^s(t) = & \frac{1}{2}(\mu_p + \mu_n) \frac{m_\omega^2 m_\phi^2 m_{\omega'}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\omega'}^2 - t)} + \\
 & + \left\{ \frac{m_\phi^2 m_{\omega'}^2 m_{\phi'}^2}{(m_\phi^2 - t)(m_{\omega'}^2 - t)(m_{\phi'}^2 - t)} \frac{(m_\phi^2 - m_{\phi'}^2)(m_{\omega'}^2 - m_{\phi'}^2)}{(m_\phi^2 - m_\omega^2)(m_{\omega'}^2 - m_\omega^2)} + \right. \\
 & + \frac{m_\omega^2 m_{\omega'}^2 m_{\phi'}^2}{(m_\omega^2 - t)(m_{\omega'}^2 - t)(m_{\phi'}^2 - t)} \frac{(m_\omega^2 - m_{\phi'}^2)(m_{\omega'}^2 - m_{\phi'}^2)}{(m_\omega^2 - m_\phi^2)(m_{\omega'}^2 - m_\phi^2)} + \\
 & + \frac{m_\omega^2 m_\phi^2 m_{\phi'}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\phi'}^2 - t)} \frac{(m_\omega^2 - m_{\phi'}^2)(m_\phi^2 - m_{\phi'}^2)}{(m_\omega^2 - m_{\omega'}^2)(m_\phi^2 - m_{\omega'}^2)} - \\
 & \left. - \frac{m_\omega^2 m_\phi^2 m_{\omega'}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\omega'}^2 - t)} \right\} (f_{\phi' NN}^{(2)} / f_{\phi'}) +
 \end{aligned}$$



U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 & + \left\{ \frac{m_\phi^2 m_\omega^2 m_{\omega'}^2}{(m_\phi^2 - t)(m_\omega^2 - t)(m_{\omega'}^2 - t)} \frac{(m_\phi^2 - m_{\omega'}^2)(m_\omega^2 - m_{\omega'}^2)}{(m_\phi^2 - m_\omega^2)(m_\omega^2 - m_\omega^2)} + \right. \\
 & + \frac{m_\omega^2 m_\phi^2 m_{\omega'}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\omega'}^2 - t)} \frac{(m_\omega^2 - m_{\omega'}^2)(m_\phi^2 - m_{\omega'}^2)}{(m_\omega^2 - m_\phi^2)(m_\phi^2 - m_\phi^2)} + \\
 & + \frac{m_\omega^2 m_\phi^2 m_{\omega'}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\omega'}^2 - t)} \frac{(m_\omega^2 - m_{\omega'}^2)(m_\phi^2 - m_{\omega'}^2)}{(m_\omega^2 - m_{\omega'}^2)(m_\phi^2 - m_{\omega'}^2)} - \\
 & \left. - \frac{m_\omega^2 m_\phi^2 m_{\omega'}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\omega'}^2 - t)} \right\} (f_{\omega' NN}^{(2)} / f_{\omega'}) +
 \end{aligned}$$



U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 & + \left\{ \frac{m_\phi^2 m_\omega^2 m_{\phi''}^2}{(m_\phi^2 - t)(m_\omega^2 - t)(m_{\phi''}^2 - t)} \frac{(m_\phi^2 - m_{\phi''}^2)(m_\omega^2 - m_{\phi''}^2)}{(m_\phi^2 - m_\omega^2)(m_\omega^2 - m_{\phi''}^2)} + \right. \\
 & + \frac{m_\omega^2 m_\phi^2 m_{\phi''}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\phi''}^2 - t)} \frac{(m_\omega^2 - m_{\phi''}^2)(m_\phi^2 - m_{\phi''}^2)}{(m_\omega^2 - m_\phi^2)(m_\phi^2 - m_{\phi''}^2)} + \\
 & + \frac{m_\omega^2 m_\phi^2 m_{\phi''}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\phi''}^2 - t)} \frac{(m_\omega^2 - m_{\phi''}^2)(m_\phi^2 - m_{\phi''}^2)}{(m_\omega^2 - m_{\phi''}^2)(m_\phi^2 - m_{\phi''}^2)} - \\
 & \left. - \frac{m_\omega^2 m_\phi^2 m_{\phi''}^2}{(m_\omega^2 - t)(m_\phi^2 - t)(m_{\phi''}^2 - t)} \right\} (f_{\phi'' NN}^{(2)} / f_{\phi''})
 \end{aligned}$$



$$F_{2N}^V(t) = \frac{1}{2} \frac{m_\rho^2 m_{\rho'}^2 m_{\rho''}^2}{(m_\rho^2 - t)(m_{\rho'}^2 - t)(m_{\rho''}^2 - t)}$$

to be **automatically normalized** and governing the **asymptotic behaviors** as predicted by the quark model of hadrons.

By the non-linear transformations

$$t = t_0^S + \frac{4(t_{in}^{1S} - t_0^S)}{[1/V(t) - V(t)]^2}; \quad t = t_0^V + \frac{4(t_{in}^{1V} - t_0^V)}{[1/W(t) - W(t)]^2};$$

$$t = t_0^S + \frac{4(t_{in}^{2S} - t_0^S)}{[1/U(t) - U(t)]^2}; \quad t = t_0^V + \frac{4(t_{in}^{2V} - t_0^V)}{[1/X(t) - X(t)]^2}.$$

and a subsequent **inclusion of the nonzero values of vector-meson widths**, for every iso-scalar and iso-vector Dirac and Pauli FF, one obtains just **one analytic and smooth from $-\infty$ to $+\infty$ function** in the forms

U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 F_{1N}^s[V(t)] = & \left(\frac{1 - V^2}{1 - V_N^2} \right)^4 \left\{ \frac{1}{2} L_\omega(V) L_\phi(V) + \right. \\
 & + \left[L_\phi(V) L_{\omega'}(V) \frac{(C_\phi^{1s} - C_{\omega'}^{1s})}{(C_\phi^{1s} - C_\omega^{1s})} + L_\omega(V) L_{\omega'}(V) \frac{(C_\omega^{1s} - C_{\omega'}^{1s})}{(C_\omega^{1s} - C_\phi^{1s})} - \right. \\
 & \quad \left. - L_\omega(V) L_\phi(V) \right] (f_{\omega' NN}^{(1)} / f_{\omega'}) + \\
 & + \left[L_\phi(V) H_{\phi'}(V) \frac{(C_\phi^{1s} - C_{\phi'}^{1s})}{(C_\phi^{1s} - C_\omega^{1s})} + L_\omega(V) H_{\phi'}(V) \frac{(C_\omega^{1s} - C_{\phi'}^{1s})}{(C_\omega^{1s} - C_\phi^{1s})} - \right. \\
 & \quad \left. - L_\omega(V) L_\phi(V) \right] (f_{\phi' NN}^{(1)} / f_{\phi'}) + \\
 & + \left[L_\phi(V) H_{\omega''}(V) \frac{(C_\phi^{1s} - C_{\omega''}^{1s})}{(C_\phi^{1s} - C_\omega^{1s})} + L_\omega(V) H_{\omega''}(V) \frac{(C_\omega^{1s} - C_{\omega''}^{1s})}{(C_\omega^{1s} - C_\phi^{1s})} - \right. \\
 & \quad \left. - L_\omega(V) L_\phi(V) \right] (f_{\omega'' NN}^{(1)} / f_{\omega''}) + \\
 & + \left[L_\phi(V) H_{\phi''}(V) \frac{(C_\phi^{1s} - C_{\phi''}^{1s})}{(C_\phi^{1s} - C_\omega^{1s})} + L_\omega(V) H_{\phi''}(V) \frac{(C_\omega^{1s} - C_{\phi''}^{1s})}{(C_\omega^{1s} - C_\phi^{1s})} - \right. \\
 & \quad \left. - L_\omega(V) L_\phi(V) \right] (f_{\phi'' NN}^{(1)} / f_{\phi''}) \left. \right\}
 \end{aligned}$$



$$\begin{aligned}
 F_{1N}^v[W(t)] = & \left(\frac{1 - W^2}{1 - W_N^2} \right)^4 \left\{ \frac{1}{2} L_\rho(W) L_{\rho'}(W) + \right. \\
 + & \left[L_{\rho'}(W) H_{\rho''}(W) \frac{(C_{\rho'}^{1v} - C_{\rho''}^{1v})}{(C_{\rho'}^{1v} - C_\rho^{1v})} + L_\rho(W) H_{\rho''}(W) \frac{(C_\rho^{1v} - C_{\rho''}^{1v})}{(C_\rho^{1v} - C_{\rho'}^{1v})} - \right. \\
 & \left. \left. - L_\rho(W) L_{\rho'}(W) \right] (f_{\rho''NN}^{(1)} / f_{\rho''}) \right\}
 \end{aligned}$$

U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 F_{2N}^s[U(t)] = & \left(\frac{1 - U^2}{1 - U_N^2} \right)^6 \left\{ \frac{1}{2} (\mu_p + \mu_n) L_\omega(U) L_\phi(U) L_{\omega'}(U) + \right. \\
 & + \left[L_\phi(U) L_{\omega'}(U) H_{\phi'}(U) \frac{(C_\phi^{2s} - C_{\phi'}^{2s})(C_{\omega'}^{2s} - C_\omega^{2s})}{(C_\phi^{2s} - C_\omega^{2s})(C_{\omega'}^{2s} - C_\omega^{2s})} + \right. \\
 & + L_\omega(U) L_{\omega'}(U) H_{\phi'}(U) \frac{(C_\omega^{2s} - C_{\phi'}^{2s})(C_{\omega'}^{2s} - C_\phi^{2s})}{(C_\omega^{2s} - C_\phi^{2s})(C_{\omega'}^{2s} - C_\phi^{2s})} + \\
 & + L_\omega(U) L_\phi(U) H_{\phi'}(U) \frac{(C_\omega^{2s} - C_{\phi'}^{2s})(C_\phi^{2s} - C_{\omega'}^{2s})}{(C_\omega^{2s} - C_{\omega'}^{2s})(C_\phi^{2s} - C_{\omega'}^{2s})} - \\
 & \left. \left. - L_\omega(U) L_\phi(U) L_{\omega'}(U) \right] (f_{\phi' NN}^{(2)} / f_{\phi'}) + \right. \\
 & + \left[L_\phi(U) L_{\omega'}(U) H_{\omega''}(U) \frac{(C_\phi^{2s} - C_{\omega''}^{2s})(C_{\omega'}^{2s} - C_\omega^{2s})}{(C_\phi^{2s} - C_\omega^{2s})(C_{\omega'}^{2s} - C_\omega^{2s})} + \right. \\
 & + L_\omega(U) L_{\omega'}(U) H_{\omega''}(U) \frac{(C_\omega^{2s} - C_{\omega''}^{2s})(C_{\omega'}^{2s} - C_\omega^{2s})}{(C_\omega^{2s} - C_\phi^{2s})(C_{\omega'}^{2s} - C_\phi^{2s})} + \\
 & + L_\omega(U) L_\phi(U) H_{\omega''}(U) \frac{(C_\omega^{2s} - C_{\omega''}^{2s})(C_\phi^{2s} - C_{\omega'}^{2s})}{(C_\omega^{2s} - C_{\omega'}^{2s})(C_\phi^{2s} - C_{\omega'}^{2s})} - \\
 & \left. \left. - L_\omega(U) L_\phi(U) L_{\omega'}(U) \right] (f_{\omega'' NN}^{(2)} / f_{\omega''}) + \right. \\
 & \left. - L_\omega(U) L_\phi(U) L_{\omega'}(U) \right\}
 \end{aligned}$$



U&A MODEL OF NUCLEON EM STRUCTURE

$$\begin{aligned}
 & + \left[L_\phi(U)L_{\omega'}(U)H_{\phi''}(U) \frac{(C_\phi^{2s} - C_{\phi''}^{2s})(C_{\omega'}^{2s} - C_{\phi''}^{2s})}{(C_\phi^{2s} - C_\omega^{2s})(C_{\omega'}^{2s} - C_\omega^{2s})} + \right. \\
 & + L_\omega(U)L_{\omega'}(U)H_{\phi''}(U) \frac{(C_\omega^{2s} - C_{\phi''}^{2s})(C_{\omega'}^{2s} - C_{\phi''}^{2s})}{(C_\omega^{2s} - C_\phi^{2s})(C_{\omega'}^{2s} - C_\phi^{2s})} + \\
 & + L_\omega(U)L_\phi(U)H_{\phi''}(U) \frac{(C_\omega^{2s} - C_{\phi''}^{2s})(C_\phi^{2s} - C_{\phi''}^{2s})}{(C_\omega^{2s} - C_{\omega'}^{2s})(C_\phi^{2s} - C_{\omega'}^{2s})} - \\
 & \left. - L_\omega(U)L_\phi(U)L_{\omega'}(U) \right] (f_{\phi'' NN}^{(2)} / f_{\phi''}) \}
 \end{aligned}$$



U&A MODEL OF NUCLEON EM STRUCTURE

$$F_{2N}^V[X(t)] = \left(\frac{1 - X^2}{1 - X_N^2} \right)^6 \left\{ \frac{1}{2} (\mu_p - \mu_n) L_\rho(U) L_{\rho'}(U) H_{\rho''}(U) \right\}$$

where

$$L_r(V) = \frac{(V_N - V_r)(V_N - V_r^*)(V_N - 1/V_r)(V_N - 1/V_r^*)}{(V - V_r)(V - V_r^*)(V - 1/V_r)(V - 1/V_r^*)},$$

$$C_r^{1s} = \frac{(V_N - V_r)(V_N - V_r^*)(V_N - 1/V_r)(V_N - 1/V_r^*)}{-(V_r - 1/V_r)(V_r - 1/V_r^*)}, \quad r = \omega, \phi, \omega'$$

$$H_l(V) = \frac{(V_N - V_l)(V_N - V_l^*)(V_N + V_l)(V_N + V_l^*)}{(V - V_l)(V - V_l^*)(V + V_l)(V + V_l^*)},$$

$$C_l^{1s} = \frac{(V_N - V_l)(V_N - V_l^*)(V_N + V_l)(V_N + V_l^*)}{-(V_l - 1/V_l)(V_l - 1/V_l^*)}, \quad l = \phi', \omega'' \phi''$$

$$L_k(W) = \frac{(W_N - W_k)(W_N - W_k^*)(W_N - 1/W_k)(W_N - 1/W_k^*)}{(W - W_k)(W - W_k^*)(W - 1/W_k)(W - 1/W_k^*)},$$

$$C_k^{1v} = \frac{(W_N - W_k)(W_N - W_k^*)(W_N - 1/W_k)(W_N - 1/W_k^*)}{-(W_k - 1/W_k)(W_k - 1/W_k^*)}, \quad k = \rho, \rho'$$



U&A MODEL OF NUCLEON EM STRUCTURE

$$H_{\rho''}(W) = \frac{(W_N - W_{\rho''})(W_N - W_{\rho''}^*)(W_N + W_{\rho''})(W_N + W_{\rho''}^*)}{(W - W_{\rho''})(W - W_{\rho''}^*)(W + W_{\rho''})(W + W_{\rho''}^*)},$$

$$C_{\rho''}^{1v} = \frac{(W_N - W_{\rho''})(W_N - W_{\rho''}^*)(W_N + W_{\rho''})(W_N + W_{\rho''}^*)}{-(W_{\rho''} - 1/W_{\rho''})(W_{\rho''} - 1/W_{\rho''}^*)},$$

$$L_r(U) = \frac{(U_N - U_r)(U_N - U_r^*)(U_N - 1/U_r)(U_N - 1/U_r^*)}{(U - U_r)(U - U_r^*)(U - 1/U_r)(U - 1/U_r^*)},$$

$$C_r^{2s} = \frac{(U_N - U_r)(U_N - U_r^*)(U_N - 1/U_r)(U_N - 1/U_r^*)}{-(U_r - 1/U_r)(U_r - 1/U_r^*)}, r = \omega, \phi, \omega'$$

$$H_l(U) = \frac{(U_N - U_l)(U_N - U_l^*)(U_N + U_l)(U_N + U_l^*)}{(U - U_l)(U - U_l^*)(U + U_l)(U + U_l^*)},$$

$$C_l^{2s} = \frac{(U_N - U_l)(U_N - U_l^*)(U_N + U_l)(U_N + U_l^*)}{-(U_l - 1/U_l)(U_l - 1/U_l^*)}, l = \phi', \omega'' \phi''$$



$$L_k(X) = \frac{(X_N - X_k)(X_N - X_k^*)(X_N - 1/X_k)(X_N - 1/X_k^*)}{(X - X_k)(X - X_k^*)(X - 1/X_k)(X - 1/X_k^*)},$$

$$C_k^{2v} = \frac{(X_N - X_k)(X_N - X_k^*)(X_N - 1/X_k)(X_N - 1/X_k^*)}{-(X_k - 1/X_k)(X_k - 1/X_k^*)}, \quad k = \rho, \rho'$$

$$H_{\rho''}(X) = \frac{(X_N - X_{\rho''})(X_N - X_{\rho''}^*)(X_N + X_{\rho''})(X_N + X_{\rho''}^*)}{(X - X_{\rho''})(X - X_{\rho''}^*)(X + X_{\rho''})(X + X_{\rho''}^*)},$$

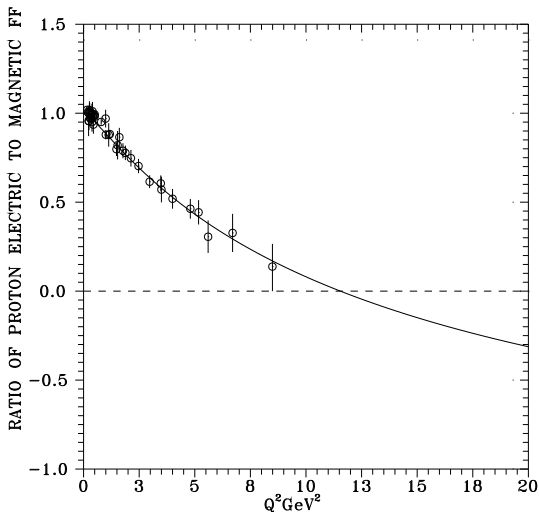
$$C_{\rho''}^{2v} = \frac{(X_N - X_{\rho''})(X_N - X_{\rho''}^*)(X_N + X_{\rho''})(X_N + X_{\rho''}^*)}{-(X_{\rho''} - 1/X_{\rho''})(X_{\rho''} - 1/X_{\rho''}^*)}.$$

This advanced model is **defined on four-sheeted Riemann surface** and includes all required properties like

- **experimental fact of a creation of unstable vector-meson resonances** in e^+e^- annihilation processes into hadrons
- the **analytic properties** of FFs
- the **reality conditions**
- **unitarity conditions** of FFs
- **normalizations** of FFs
- **asymptotic behaviors** of FFs

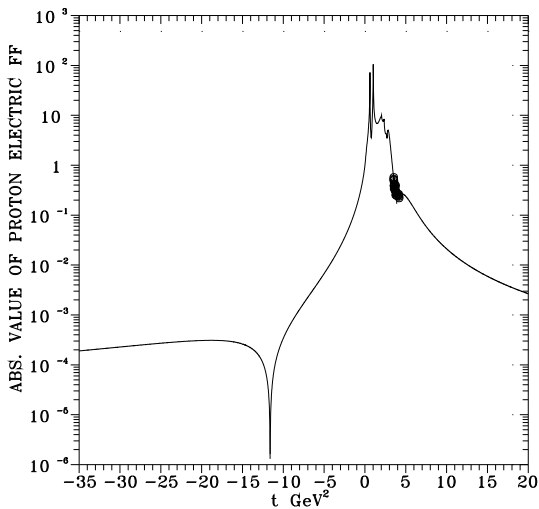
and moreover, **describes all today's nucleon EM FFs data in space-like and time-like regions simultaneously.**





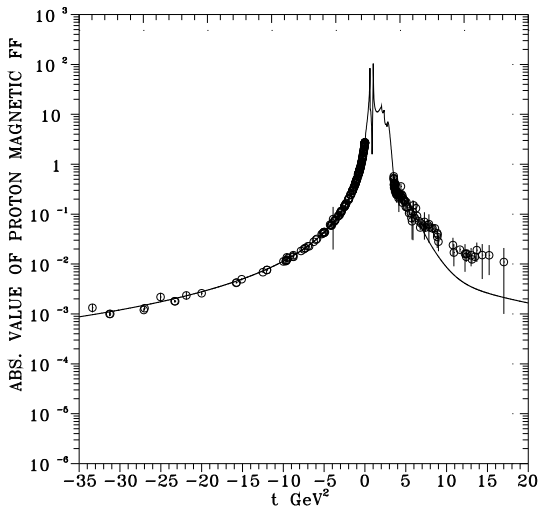
Prediction of proton electric to magnetic FFs ratio behavior by *U&A* model respecting *SU(3)* symmetry and OZI rule violation





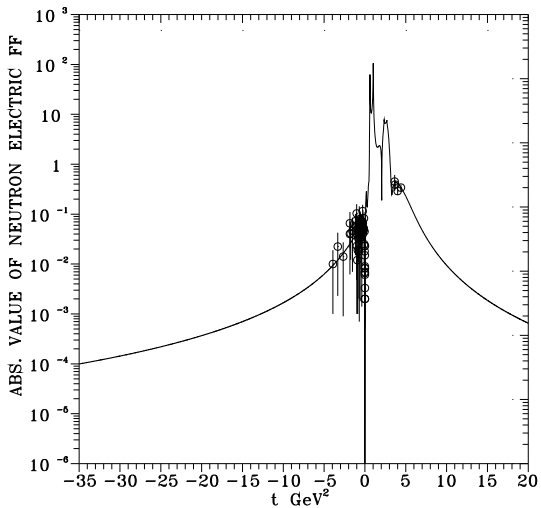
Prediction of proton electric FF behavior by $U&A$ model respecting $SU(3)$ symmetry and OZI rule violation





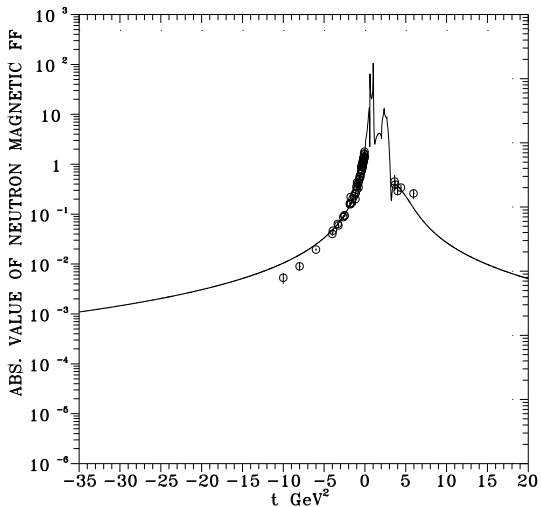
Prediction of proton magnetic FF behavior by $U&A$ model respecting $SU(3)$ symmetry and OZI rule violation





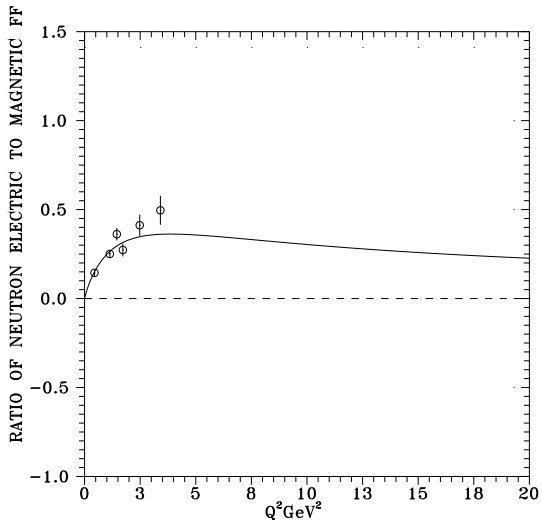
Prediction of neutron electric FF behavior by *U&A* model respecting *SU(3)* symmetry and OZI rule violation





Prediction of neutron magnetic FF behavior by *U&A* model respecting *SU(3)* symmetry and OZI rule violation





Prediction of neutron electric to magnetic FFs ratio behavior by *U&A* model respecting *SU(3)* symmetry and OZI rule violation



VECTOR AND TENSOR POLARIZATIONS IN $e^+e^- \rightarrow p\bar{p}$ PROCESS

The advanced *U&A* nucleon EM structure **model is analytic** - it **creates the nonzero imaginary parts of the FFs** in a natural way **starting from the lowest branch points** on the positive real axis - therefore, it **can be applied for the predictions of the vector and tensor polarizations** of the final protons and antiprotons in the $e^+e^- \rightarrow p\bar{p}$ process.



VECTOR AND TENSOR POLARIZATIONS IN

$e^+ e^- \rightarrow p \bar{p}$ PROCESS

In order to find an explicit forms of **single spin polarization observables** (either for p or for \bar{p}) one has to calculate the traces in the numerator and denominator of

$$\vec{P} = \frac{j_{ij} \text{Tr}[F_i F_j^\dagger \vec{\sigma}]}{j_{ij} \text{Tr}[F_i F_j^\dagger]}.$$

where,

$$\vec{F} = \sqrt{s} \left[G_{Mp}(s)(\vec{\sigma} - \vec{n}\vec{\sigma}\cdot\vec{n}) + \frac{2m_p}{\sqrt{s}} G_{Ep}(s)\vec{n}\vec{\sigma}\cdot\vec{n} \right]$$



VECTOR AND TENSOR POLARIZATIONS IN $e^+e^- \rightarrow p\bar{p}$ PROCESS

$$j_{ij} = 2s(\delta_{ij} - m_i m_j + \lambda i \epsilon_{ijl} m_l)$$

is the **lepton tensor with longitudinally polarized e^- or e^+**

$\vec{\sigma}$ are **Pauli matrices**, \vec{n} is the **unit vector** along the three momentum \vec{q} of p and \vec{m} is the **unit vector** of incoming longitudinally polarized e^- or e^+ .

As a result one gets



VECTOR AND TENSOR POLARIZATIONS IN

$e^+e^- \rightarrow p\bar{p}$ PROCESS

the components of the vector polarization \vec{P} of p or \bar{p} in the reaction $e^+e^- \rightarrow p\bar{p}$

$$P_x = -\frac{2 \sin \theta \cdot \text{Re}[G_{Ep}(s)G_{Mp}^*(s)]\tau}{|G_{Ep}(s)|^2 \sin^2 \theta / \tau + |G_{Mp}(s)|^2 (1 + \cos^2 \theta)} \quad (1)$$

$$P_y = -\frac{\frac{1}{\sqrt{\tau}} \text{Im}(G_{Ep}(s)G_{Mp}^*(s)) \sin 2\vartheta}{|G_{Ep}(s)|^2 \sin^2 \vartheta / \tau + |G_{Mp}(s)|^2 (1 + \cos^2 \vartheta)}; \quad (2)$$

$$P_z = \frac{2 \cos \theta |G_{Mp}(s)|^2}{|G_{Ep}(s)|^2 \sin^2 \theta / \tau + |G_{Mp}(s)|^2 (1 + \cos^2 \theta)}, \quad (3)$$

assuming 100% i.e. $\lambda = 1$ longitudinal polarization of e^- or e^+ .



VECTOR AND TENSOR POLARIZATIONS IN $e^+e^- \rightarrow p\bar{p}$ PROCESS

Similarly, one can calculate **explicit forms of double polarization observables** from

$$P_{kl} = \frac{j_{ij} \text{Tr}[F_i \sigma_k F_j^\dagger \sigma_l]}{j_{ij} \text{Tr}[F_i F_j^\dagger]}$$

with

$$k, l = x, y, z$$

Considering longitudinally polarized either e^- or e^+ and calculating the traces in numerator and denominator, respectively, one finds



VECTOR AND TENSOR POLARIZATIONS IN

$e^+ e^- \rightarrow p \bar{p}$ PROCESS

$$P_{xx} = \frac{|G_{Mp}(s)|^2 \cos^2 \vartheta - \frac{1}{\tau} |G_{Ep}(s)|^2 \sin^2 \vartheta}{\frac{1}{\tau} |G_{Ep}(s)|^2 \sin^2 \vartheta + |G_{Mp}(s)|^2 (1 + \cos^2 \vartheta)};$$

$$P_{yy} = \frac{|G_{Mp}(s)|^2 (1 + \sin^2 \vartheta) - \frac{1}{\tau} |G_{Ep}(s)|^2 \sin^2 \vartheta}{\frac{1}{\tau} |G_{Ep}(s)|^2 \sin^2 \vartheta + |G_{Mp}(s)|^2 (1 + \cos^2 \vartheta)};$$

$$P_{zz} = \frac{|G_{Mp}(s)|^2 \sin^2 \vartheta - \frac{1}{\tau} |G_{Ep}(s)|^2 \cos^2 \vartheta}{\frac{1}{\tau} |G_{Ep}(s)|^2 \sin^2 \vartheta + |G_{Mp}(s)|^2 (1 + \cos^2 \vartheta)};$$

$$P_{xy} = P_{yx} = 0;$$

$$P_{xz} = P_{zx} = \frac{\frac{1}{\sqrt{\tau}} \operatorname{Re}[G_{Mp}^*(s) G_{Ep}(s)] \sin 2\vartheta}{\frac{1}{\tau} |G_{Ep}(s)|^2 \sin^2 \vartheta + |G_{Mp}(s)|^2 (1 + \cos^2 \vartheta)};$$

$$P_{yz} = P_{zy} = -2 \frac{\frac{1}{\sqrt{\tau}} \operatorname{Im}[G_{Mp}^*(s) G_{Ep}(s)] \sin \vartheta}{\frac{1}{\tau} |G_{Ep}(s)|^2 \sin^2 \vartheta + |G_{Mp}(s)|^2 (1 + \cos^2 \vartheta)};$$



VECTOR AND TENSOR POLARIZATIONS IN $e^+e^- \rightarrow p\bar{p}$ PROCESS

Every of components P_{kl} characterizes
a **polarization of the proton p at the direction of k , if antiproton \bar{p}
is polarized at the direction l**
and
quantities P_{kl} are calculated for
100% longitudinally polarized of e^- or e^+ .

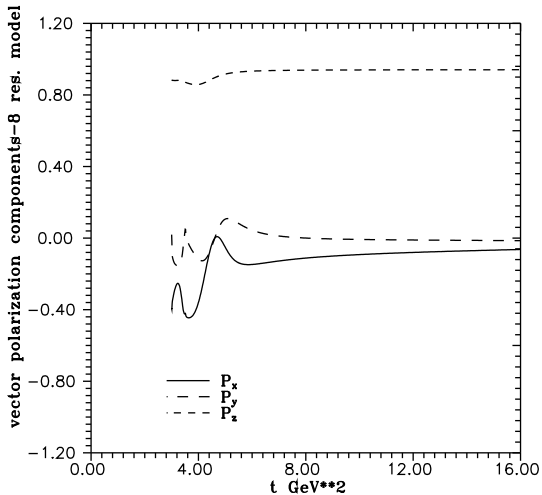


VECTOR AND TENSOR POLARIZATIONS IN $e^+e^- \rightarrow p\bar{p}$ PROCESS

By application of the **advanced 9 resonance *U&A* nucleon EM structure model** we are able to **predict vector and tensor polarizations** as a function of the energy.

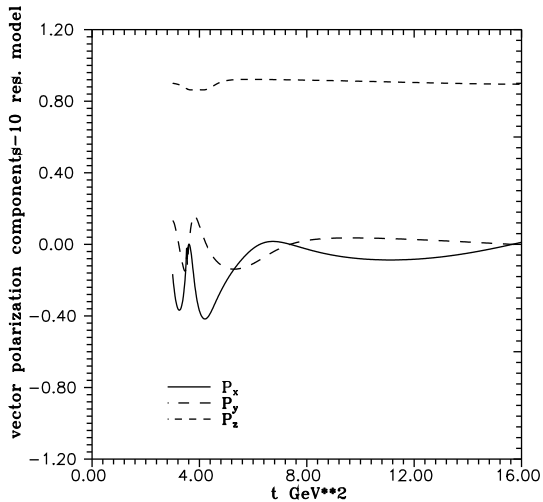
However, **in the past we have elaborated also 8 and 10 resonance *U&A* nucleon EM structure models** and we further present predictions by all of them for comparison.





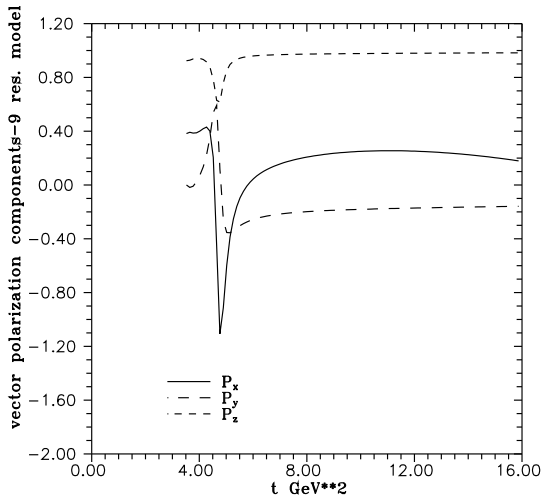
Vector polarization components - 8 resonance model





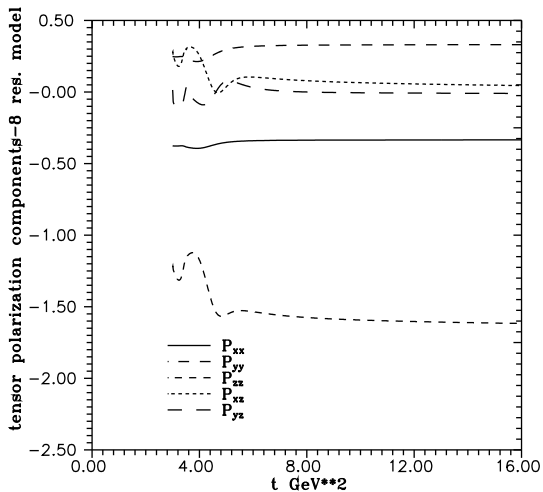
Vector polarization components - 10 resonance model





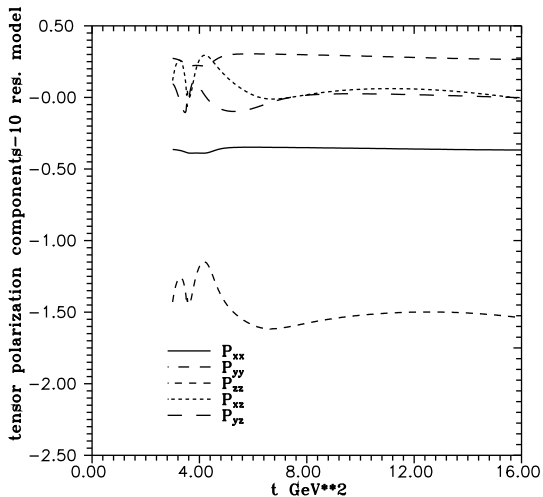
Vector polarization components - 9 resonance model



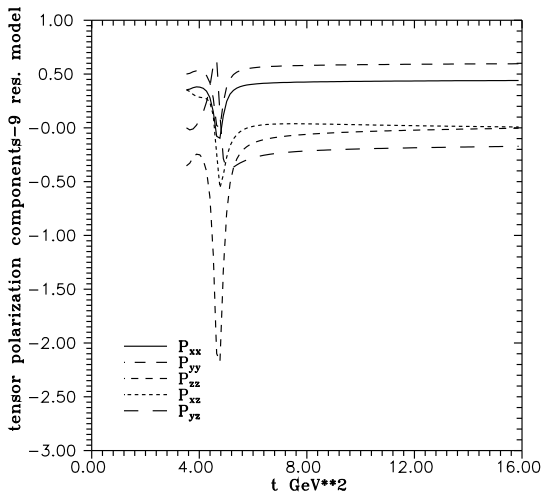


Tensor polarization components - 8 resonance model





Tensor polarization components - 10 resonance model



Tensor polarization components - 9 resonance model

One can use the **advanced $U&A$ nucleon EM structure model for a description of the complete $1/2^+$ octet hyperons EM structure**, to be represented by the Sachs electric $G_E^h(t)$ and magnetic $G_M^h(t)$ FFs of hyperons.

They can be decomposed into the flavor independent iso-scalar and iso-vector parts of the Dirac and Pauli FFs



$$G_E^\Lambda(t) = F_{1s}^\Lambda(t) + \frac{t}{4m_\Lambda^2} F_{2s}^\Lambda(t)$$

$$G_M^\Lambda(t) = F_{1s}^\Lambda(t) + F_{2s}^\Lambda(t)$$

$$G_E^{\Sigma^0}(t) = F_{1s}^\Sigma(t) + \frac{t}{4m_\Sigma^2} F_{2s}^\Sigma(t)$$

$$G_M^{\Sigma^0}(t) = F_{1s}^\Sigma(t) + F_{2s}^\Sigma(t)$$

$$G_E^{\Sigma^+, \Sigma^-}(t) = [F_{1s}^\Sigma(t) \pm F_{1v}^\Sigma(t)] + \frac{t}{4m_\Sigma^2} [F_{2s}^\Sigma(t) \pm F_{2v}^\Sigma(t)]$$

$$G_M^{\Sigma^+, \Sigma^-}(t) = [F_{1s}^\Sigma(t) \pm F_{1v}^\Sigma(t)] + [F_{2s}^\Sigma(t) \pm F_{2v}^\Sigma(t)]$$

$$G_E^{\Xi^0, \Xi^-}(t) = [F_{1s}^\Xi(t) \pm F_{1v}^\Xi(t)] + \frac{t}{4m_\Xi^2} [F_{2s}^\Xi(t) \pm F_{2v}^\Xi(t)]$$

$$G_M^{\Xi^0, \Xi^-}(t) = [F_{1s}^\Xi(t) \pm F_{1v}^\Xi(t)] + [F_{2s}^\Xi(t) \pm F_{2v}^\Xi(t)]$$

HYPERONS EM STRUCTURE

Now, it is **sufficient to substitute for the iso-scalar and iso-vector parts of the Dirac and Pauli FFs** the expressions from nucleons, however, with the following change in the **corresponding coupling constant ratios**

$$N \Rightarrow \Lambda, \Sigma^0, \Sigma^\pm, \Xi^{0,-}$$

In a such way one has the *U&A* hyperons EM structure model, however dependent on **unknown coupling constat ratios**.

In nucleons we have **determined them in a fitting procedure of existing data**.

However, in the case of hyperons there are no sufficient data.

But also **in this case one finds the solution**.



The $SU(3)$ invariant Lagrangian

$$\begin{aligned} \text{Tr}(L_{VB\bar{B}}) = & \frac{i}{\sqrt{2}} f^F [\bar{B}_\beta^\alpha \gamma_\mu B_\gamma^\beta - \bar{B}_\gamma^\beta \gamma_\mu B_\beta^\alpha] (V_\mu)_\alpha^\gamma + \\ & \frac{i}{\sqrt{2}} f^D [\bar{B}_\gamma^\beta \gamma_\mu B_\beta^\alpha + \bar{B}_\gamma^\alpha \gamma_\mu B_\gamma^\beta] (V_\mu)_\alpha^\gamma + \\ & \frac{i}{\sqrt{2}} f^S \bar{B}_\beta^\alpha \gamma_\mu B_\alpha^\beta \omega_\mu^0 \end{aligned}$$

provides the relations



$$f_{\rho NN}^{1,2} = \frac{1}{2}(f_{1,2}^D + f_{1,2}^F)$$

$$f_{\omega NN}^{1,2} = \frac{1}{\sqrt{2}}\cos\theta f_{1,2}^S - \frac{1}{2\sqrt{3}}\sin\theta(3f_{1,2}^F - f_{1,2}^D)$$

$$f_{\phi NN}^{1,2} = \frac{1}{\sqrt{2}}\sin\theta f_{1,2}^S + \frac{1}{2\sqrt{3}}\cos\theta(3f_{1,2}^F - f_{1,2}^D)$$

$$\Gamma(V \rightarrow e^+e^-) = \frac{\alpha^2 m_V}{3} \left(\frac{f_V^2}{4\pi}\right)^{-1}$$

$$f_{\omega\Lambda\Lambda}^{1,2} = \frac{1}{\sqrt{2}} \cos\theta f_{1,2}^S + \frac{1}{\sqrt{3}} \sin\theta f_{1,2}^D$$

$$f_{\phi\Lambda\Lambda}^{1,2} = \frac{1}{\sqrt{2}} \sin\theta f_{1,2}^S - \frac{1}{\sqrt{3}} \cos\theta f_{1,2}^D$$

$$f_{\rho\Sigma\Sigma}^{1,2} = -f_{1,2}^F$$

$$f_{\omega\Sigma\Sigma}^{1,2} = \frac{1}{\sqrt{2}} \cos\theta f_{1,2}^S - \frac{1}{\sqrt{3}} \sin\theta f_{1,2}^D$$

$$f_{\phi\Sigma\Sigma}^{1,2} = \frac{1}{\sqrt{2}} \sin\theta f_{1,2}^S + \frac{1}{\sqrt{3}} \cos\theta f_{1,2}^D$$

$$f_{\rho\Xi\Xi}^{1,2} = \frac{1}{2} (f_{1,2}^D - f_{1,2}^F)$$

$$f_{\omega\Xi\Xi}^{1,2} = \frac{1}{\sqrt{2}} \cos\theta f_{1,2}^S + \frac{1}{2\sqrt{3}} \sin\theta (3f_{1,2}^F + f_{1,2}^D)$$

$$f_{\phi\Xi\Xi}^{1,2} = \frac{1}{\sqrt{2}} \sin\theta f_{1,2}^S - \frac{1}{2\sqrt{3}} \cos\theta (3f_{1,2}^F + f_{1,2}^D)$$



similarly for **excited states**

$\omega'(1420), \rho'(1450), \phi'(1680)$
 $\omega''(1650), \rho''(1700), \phi''(2170),$

where $\theta = 39.83^\circ$ is the **mixing angle** to be determined by the **Gell-Mann-Okubo quadratic mass formula**

$$m_\phi^2 \cos^2 \theta + m_\omega^2 \sin^2 \theta = \frac{4m_{K^*}^2 - m_\rho^2}{3}.$$



- The advanced *U&A nucleon EM structure model*, describing all today's experimental data in space-like and time-like regions simultaneously, has been elaborated
- The model **realistic vector and tensor polarizations in the $e^+e^- \rightarrow p\bar{p}$ process** predicts
- **A description of EM structure of the complete $1/2^+$ octet baryons** by means of the *U&A nucleon EM structure model* and *SU(3)* symmetry has been sketched.



Thank you

