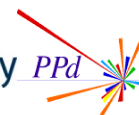


Properties of b-hadrons with ATLAS: B_s^0 rare decays and Λ_b^0 decay properties

John Baines

for the ATLAS Collaboration



Overview

- $B_s^0 \rightarrow \mu^+ \mu^-$ Branching Ratio
 - Update with full 2011 dataset

NEW

- Λ_b^0 mass and lifetime

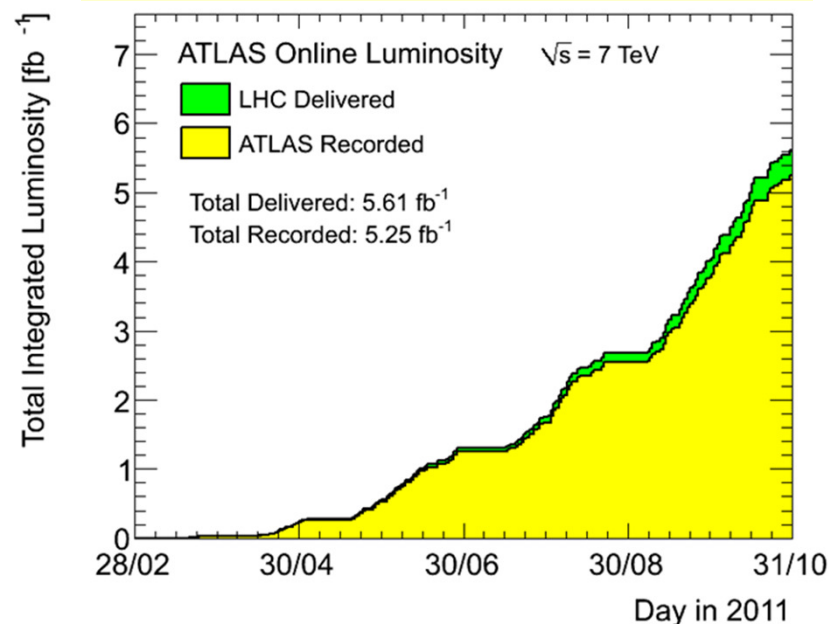
- Parity violation asymmetry parameter α_b and helicity amplitudes in $\Lambda_b^0 \rightarrow \Lambda^0 J/\psi$

NEW

See also other B-physics talks in this conference:

- QCD session: *Review of ATLAS Heavy-Quark and Quarkonium results*: Miriam Watson
- This session: *Studies of rare and suppressed processes in B mesons decays and of mixing/CP violation in the Bs system with the ATLAS detector*: Jochen Schieck

Measurements based on 2011 Dataset



ATLAS Detector & B-Physics Triggers

Precision Muon Detectors: $|\eta| < 2.7$:

- Resolution $\sim 40 \mu\text{m}$

Inner Detector: $|\eta| < 2.5$

- d_0 resolution $\sim 10 \mu\text{m}$

Combined tracks (ID+Muon):

- $\sigma(m_{J/\psi}) = 60 \text{ MeV}$

B-Physics Triggers:

• First Level Trigger (L1):

- Single muon & Dimuon Triggers

- Thresholds 4 – 40 GeV p_T

• High Level Trigger (L2&L3):

- Single muon & dimuon triggers

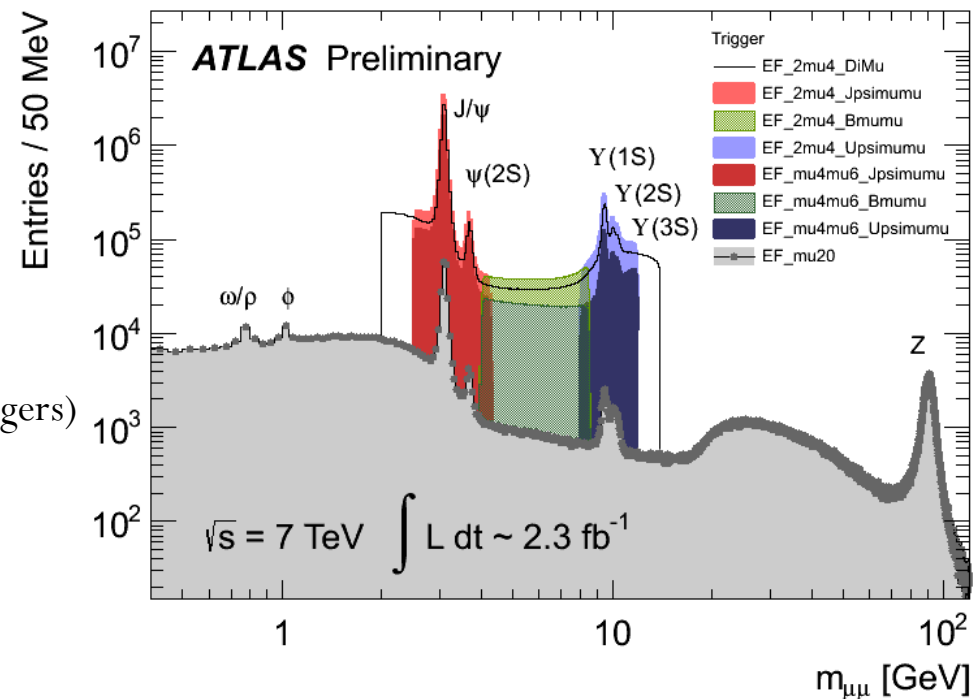
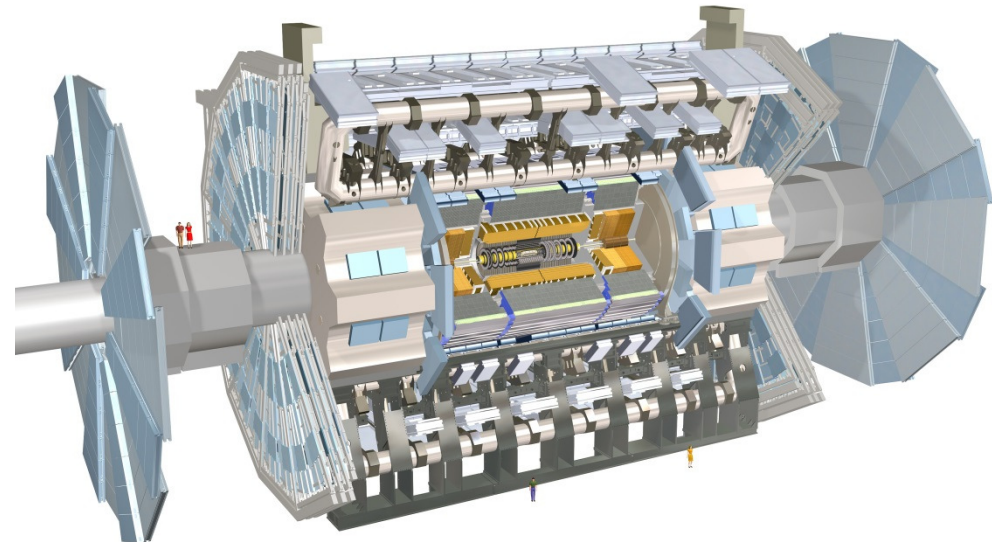
- B-physics triggers:

- Muons from common vertex
- Opposite charge (except some control triggers)

• Loose mass cuts:

$$J/\psi: 2.5 < M(\mu\mu) < 4.3 \text{ GeV}$$

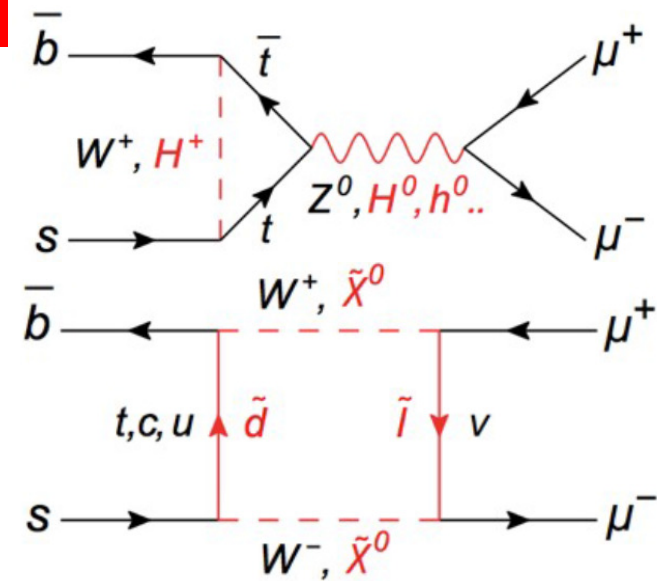
$$B: 4.0 < M(\mu\mu) < 8.5 \text{ GeV}$$



$B_s^0 \rightarrow \mu^+ \mu^-$ Branching Ratio NEW

ATLAS-CONF-2013-076

- Flavour Changing Neutral Current processes:
 - Strongly suppressed in SM¹: $BR = (3.23 \pm 0.27) \times 10^{-9}$
 - Can be enhanced by new physics
 - First measurement made by LHCb²: $BR = (3.2_{-1.2}^{+1.5}) \times 10^{-9}$
- Previous ATLAS³ limit used half 2011 data (2.4 fb^{-1}).
- Now updated with full 2011 dataset: 4.9 fb^{-1}
 - Including improved event reconstruction & analysis improvements



- Blind analysis - Blinded Region: 5066–5666 MeV
- BR measured w.r.t. reference channel:

$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = \underbrace{\mathcal{B}(B^\pm \rightarrow J/\psi K^\pm \rightarrow \mu^+ \mu^- K^\pm)}_{\text{PDG value}} \times \underbrace{\frac{f_u}{f_s}}_{\text{LHCb}^4 \text{ measurement}} \times \frac{N_{\mu^+ \mu^-}}{N_{J/\psi K^\pm}} \times R_{A\epsilon}$$

$B_s^0 \rightarrow \mu^+ \mu^-$ observed in data after S.B. subtraction



LHCb⁴ measurement



Reference Channel Yield from Data

$$R_{A\epsilon} = \frac{A_{J/\psi K^\pm}}{A_{\mu^+ \mu^-}} \frac{\epsilon_{J/\psi K^\pm}}{\epsilon_{\mu^+ \mu^-}} \quad \text{Acceptance} \times \text{Efficiency Ratio from MC}$$

$B_S^0 \rightarrow \mu^+ \mu^-$ Branching Ratio Measurement

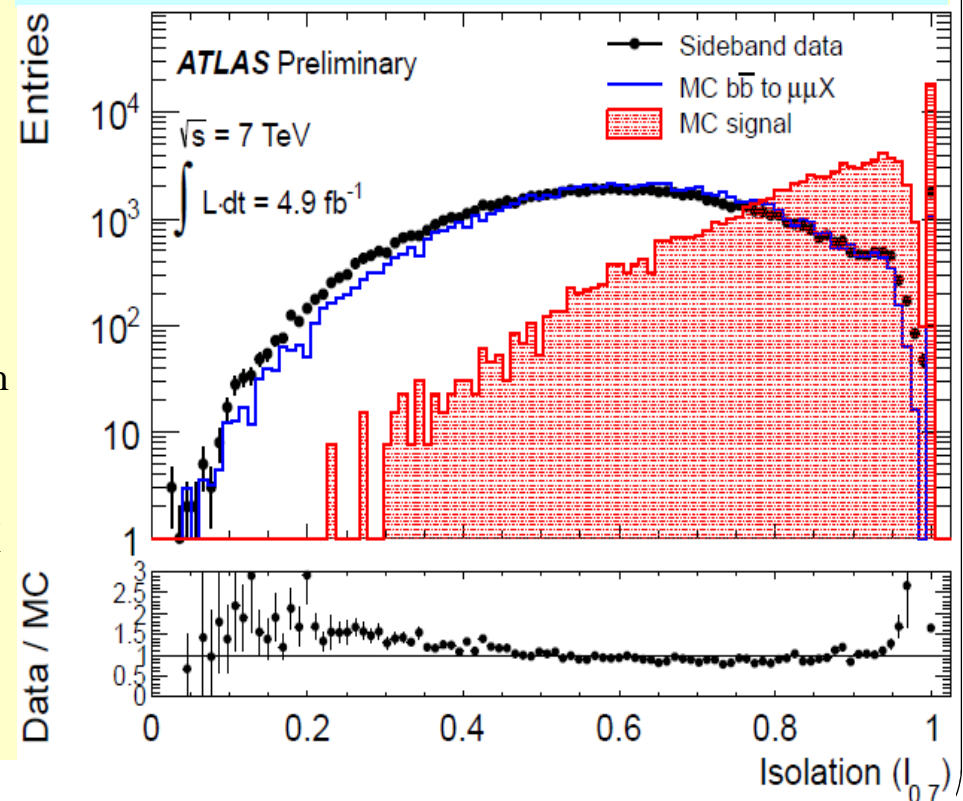
Data Selection:

- Trigger: L1: dimuon $p_T > 4$ GeV; HLT: dimuon, Loose B & J/ψ mass cuts
- Pre-selection to select good quality reconstructed tracks & vertices
- Reference Channel Data divided into two parts to avoid bias of yield extraction:
 - Odd-#: odd event numbers used for data-driven reweighting of MC
 - Even-#: even event numbers used to extract reference channel yield and background estimate

Monte-Carlo tuning:

- J/ψ polarization correction
 - MC generated without decay polarization
- Binned (p_T^B, η^B) re-weighting of MC:
 - **Generator Level (GL) re-weighting:**
 - Applied to signal & reference MC
 - Corrects for GL filter biases
 - Derived from MC samples generated with a loose GL filter
 - **Data Driven re-weighting :**
 - Applied to signal, reference & $b\bar{b} \rightarrow \mu\mu X$
 - Derived from differences between MC and odd-# reference channel data
- Small residual diff.s \Rightarrow Syst. error on R_{Ae}

Side-band data c.f. MC for Isolation parameter $I_{0.7}$



Background Modelling & Selection Optimization

Combinatorial Background:

- Suppressed by BDT Discriminant
 - 13 discriminating variables inputs
 - Training using MC datasets
 - Selection Optimization using MC & data:
 - 2D optimization (Δm , BDT output)
 - Signal MC & odd-# sideband data

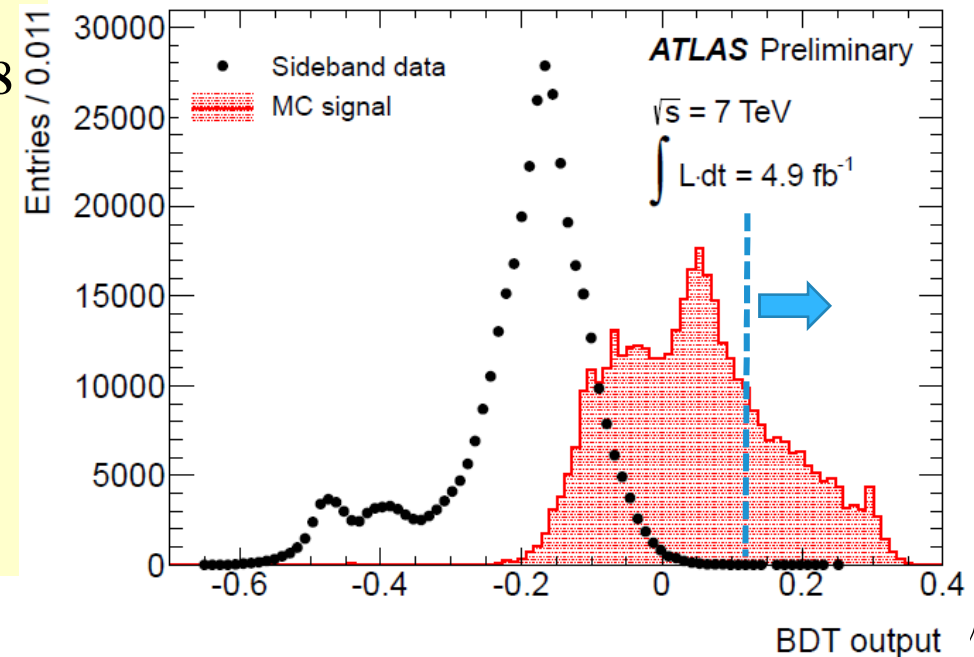
$$\text{Maximize : } \mathcal{P} = \frac{\epsilon}{1 + \sqrt{B}}$$

$\Rightarrow \Delta m < 121 \text{ GeV}; \text{ BDT output} > 0.118$

- Residual background, after Δm & BDT cuts, determined by interpolation:
 - using even even-# side-band data

Peaking background:

- B candidates with 1 or 2 misidentified μ
- Misidentification prob. from MC:
 - π^\pm : 2.1‰; K^+ : 4.1‰; K^- : 3.3‰
- Estimate yield for $B \rightarrow hh'$ from luminosity, measured branching fractions, acceptance & effic.



Single Event Sensitivity

SES: BR corresponding a single observed signal event:

$$B(B_s^0 \rightarrow \mu^+ \mu^-) = SES \times N_{\mu^+ \mu^-}$$

$$SES = B(B^\pm \rightarrow J/\psi K^\pm \rightarrow \mu^- \mu^+ K^\pm) \times \frac{f_u}{f_s} \times \frac{R_{A\epsilon}}{N_{J/\psi K^\pm}}$$

- Acceptance \times Efficiency Ratio, $R_{A\epsilon}$:

- Evaluated from MC sample:

$$A \times \epsilon \text{ for } B^+: 1.317 \pm 0.008\%(\text{stat.})$$

$$A \times \epsilon \text{ for } B_s^0: 4.929 \pm 0.084\%(\text{stat.})$$

$$R_{A\epsilon} = 0.267 \pm 1.8\%(\text{stat.}) \pm 6.9\%(\text{syst.})$$

- Yield for Reference Channel, $N_{J/\psi K^\pm}$:

- Unbinned extended max. likelihood fits to mass & mass uncertainty ($m, \delta m$)

- Using even-# data in mass range: 4930-5630 MeV

$$N_{J/\psi K^\pm} = 15\,214 \text{ even-no. events } \pm 1.1\%(\text{stat.}) \pm 2.4\%(\text{syst.})$$

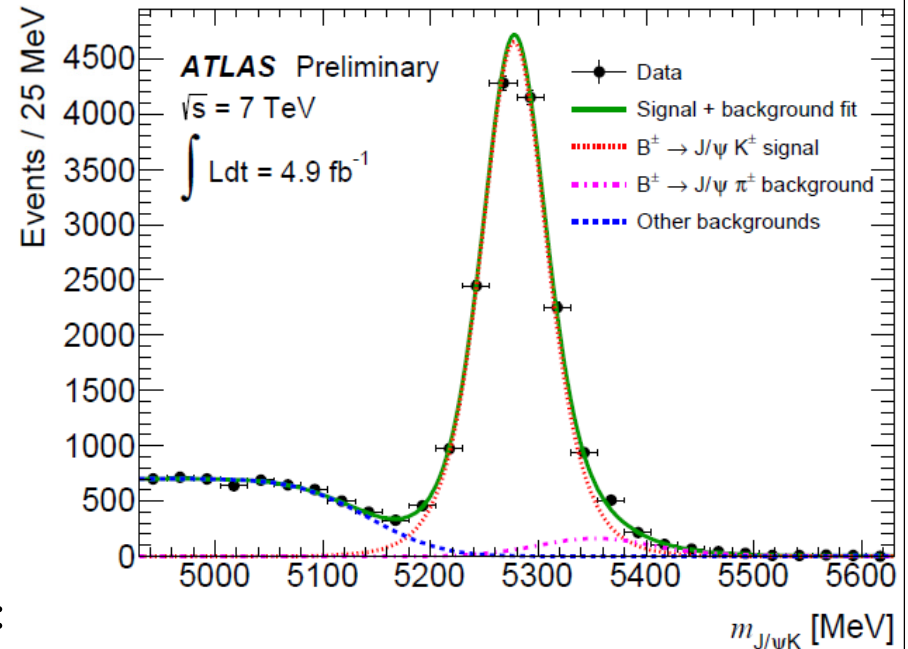
- Single Event Sensitivity: $SES = (2.065 \pm 0.262) \times 10^{-9}$

- Dominant Syst. : Ref. Chan. BR & f_u/f_s : 8.5%; $R_{A\epsilon}$: 6.9%

$$B(B^\pm \rightarrow J/\psi K^\pm): 1.016 \pm 0.033 \times 10^{-3} \text{ (PDG)}^a$$

$$B(B^\pm \rightarrow \mu^+ \mu^-): 5.93 \pm 0.06 \times 10^{-2} \text{ (PDG)}^a$$

$$f_u/f_s: 0.256 \pm 0.020 \text{ (LHCb)}^b$$



Stat. error (2.1%) plus syst. error (12.5%) in quadrature.

$B_s^0 \rightarrow \mu^+ \mu^-$ BR Limit

$$B(B_s^0 \rightarrow \mu^+ \mu^-) = \text{SES} \times N_{\mu^+ \mu^-}$$

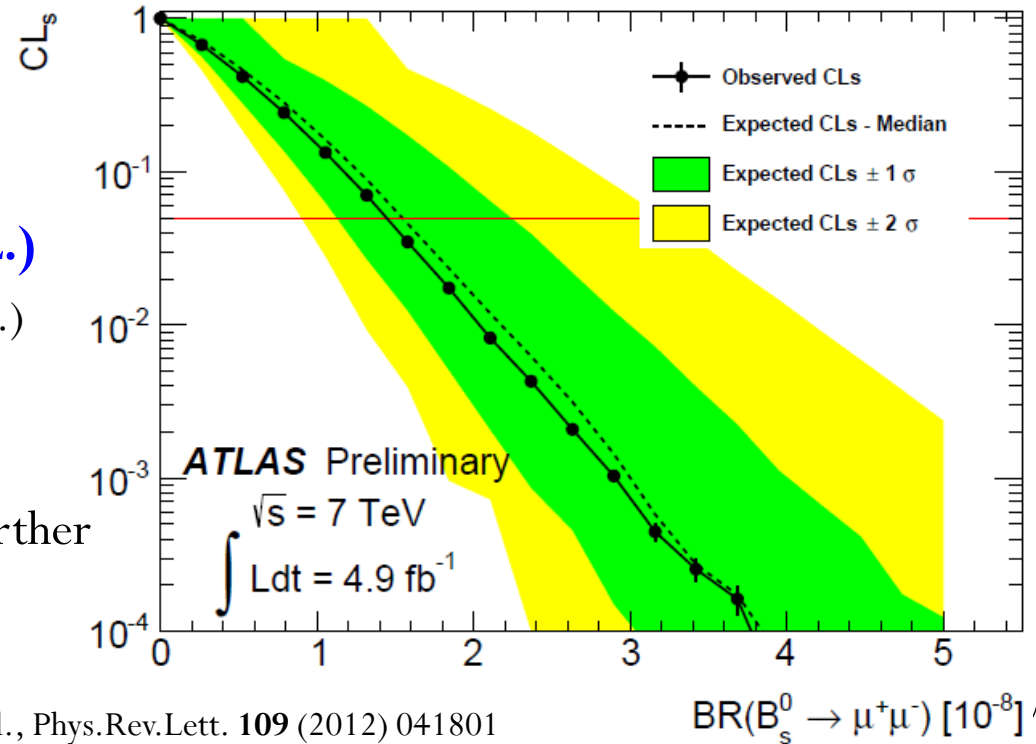
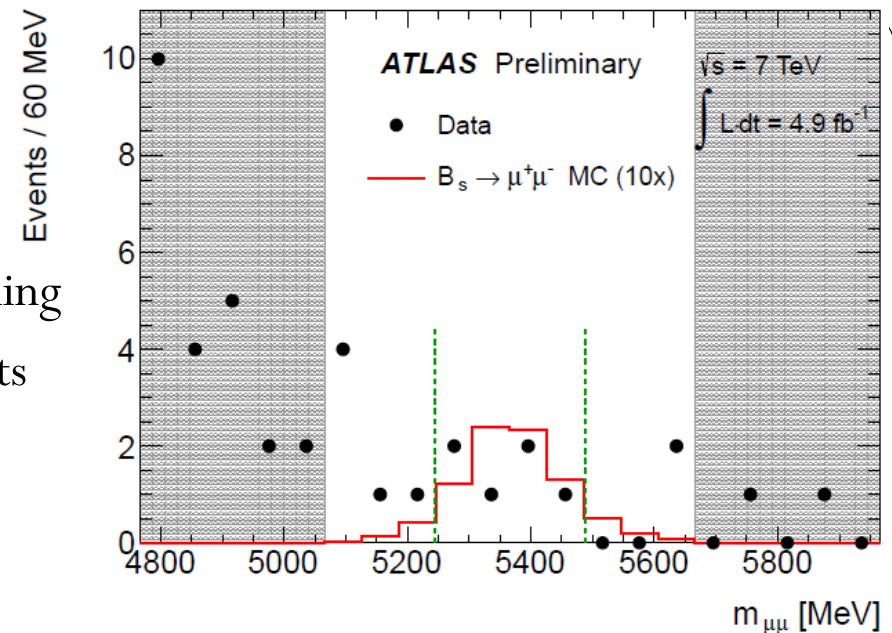
- 6 events observed in mass region after un-blinding
- Estimated background contribution: 6.75 events
 - From SB interpolation using even-# events
 - Includes estimated 0.295 $B \rightarrow hh'$ events

SM prediction: 1.7 ± 0.2
signal events in mass window

- Upper limit from CLs method:

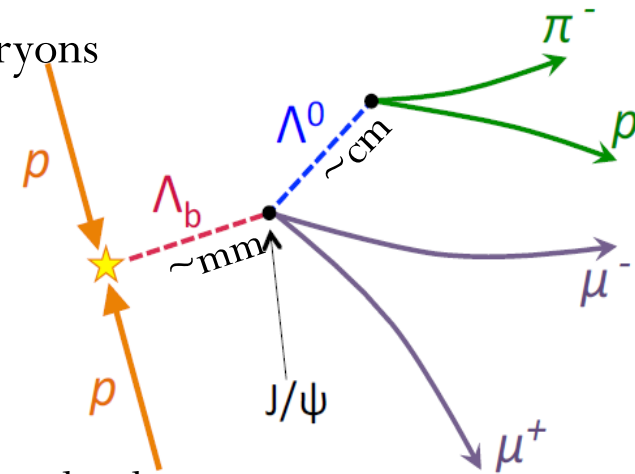
$$B(B_s^0 \rightarrow \mu^+ \mu^-) < 1.5 \times 10^{-8} \text{ (95\% C.L.)}$$

- Expected limit: $1.6_{-0.4}^{+0.7} \times 10^{-8}$ (95% C.L.)
- Time integrated SM¹ prediction:
 - $\text{BR} = (3.54 \pm 0.30) \times 10^{-9}$
- Will update with 2012 data including further analysis improvements



Λ_b Properties

- Hadron colliders are currently the only place to study b baryons
- Provides means to test theory:
 - How heavy quarks are produced; how they hadronize
 - Whether polarization is preserved in the process
- Use decay: $\Lambda_b^0 \rightarrow J/\psi(\mu^+\mu^-)\Lambda^0(p^+\pi^-)$ to measure:
 - Λ_b^0 mass & lifetime
 - Parity violating decay asymmetry parameter, α_b , & helicity amplitudes
 - Compare Lifetime Ratio $\tau(\Lambda_b)/\tau(B_d)$ and α_b with theory predictions



• Data Pre-selection:

- J/ψ & Λ^0 pre-selection:
 - J/ψ : $2.8 \text{ GeV} < M(\mu\mu) < 3.4 \text{ GeV}$
 - Λ^0 : $1.08 < M(hh) < 1.15 \text{ GeV}$
- $\Lambda_b^0 \rightarrow J/\psi(\mu^+\mu^-)\Lambda^0(p^+p^-)$ pre-selection:
 - Cascade topology fit – constrain:
 - J/ψ & Λ^0 masses
 - \vec{p}_{V^0} points to $\mu\mu$ vertex

Cascade topology fit requirements:

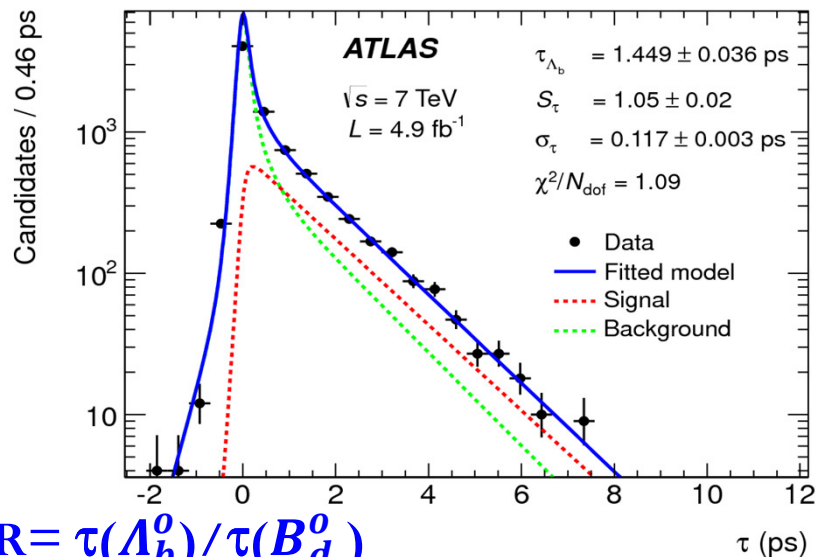
- Fit $\chi^2/N_{\text{dof}} < 3$ ($N_{\text{dof}} = 6$)
- V^0 : $p_T > 3.5 \text{ GeV}$; $L_{xy} > 10 \text{ mm}$
- $5.38 < M(J/\psi \Lambda^0) < 5.90 \text{ GeV}$
- If also B_d^0 : $\mathcal{P}(\Lambda_b^0) - \mathcal{P}(B_d^0) > 0.05$

Λ_b mass & lifetime

[Phys. Rev. D87 \(2013\) 032002](#)

- Unbinned maximum likelihood fit:

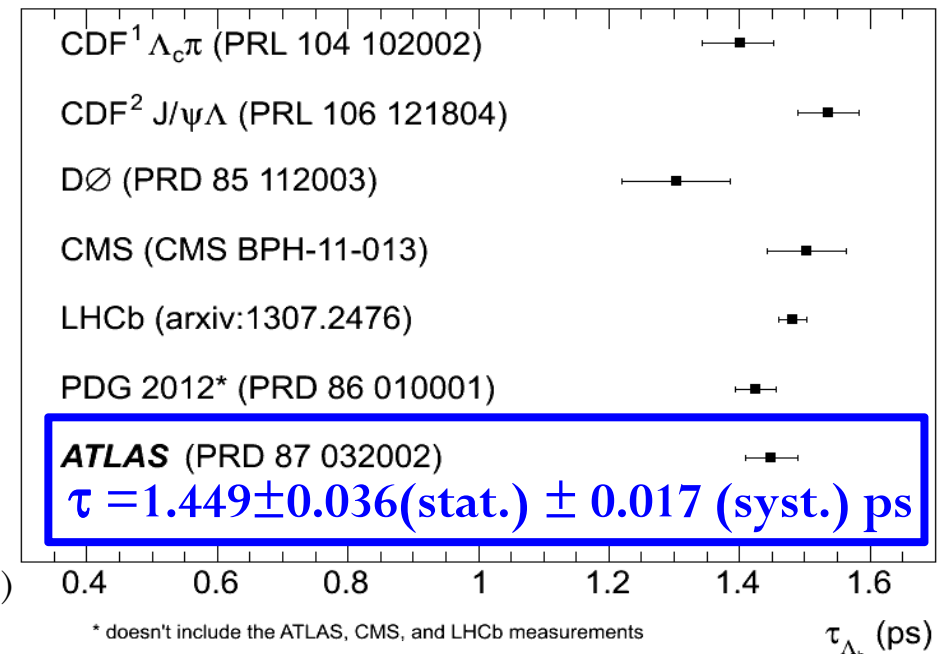
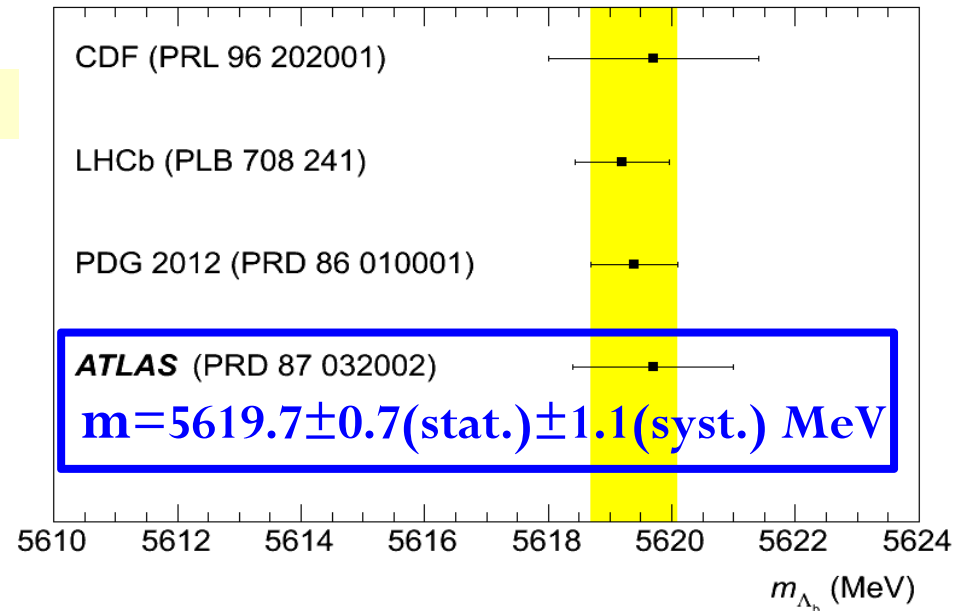
$$L = \prod_{i=1}^N \left[f_{\text{sig}} \mathcal{M}_s(m_i | \delta m_i) \mathcal{T}_s(\tau_i | \delta \tau_i) w_s(\delta m_i, \delta \tau_i) + (1 - f_{\text{sig}}) \mathcal{M}_b(m_i | \delta m_i) \mathcal{T}_b(\tau_i | \delta \tau_i) w_b(\delta m_i, \delta \tau_i) \right]$$



$$R = \tau(\Lambda_b^0) / \tau(B_d^0) = 0.960 \pm 0.025(\text{stat.}) \pm 0.016(\text{syst.})$$

c.f. 0.976 ± 0.013 (LHCb); 0.864 ± 0.052 (D0);
 1.020 ± 0.030 (CDF²)

$0.88-0.97$ (HQE^a); $0.86^b-0.88^c(\pm 0.05)$ (NLO pQCD^b)



* doesn't include the ATLAS, CMS, and LHCb measurements

α_b Measurement

NEW

ATLAS-CONF-2013-071

Amplitude	λ_Λ	$\lambda_{J/\psi}$
a_+	$+1/2$	0
a_-	$-1/2$	0
b_+	$-1/2$	-1
b_-	$+1/2$	+1

- $\Lambda_b^0 \rightarrow J/\psi(\mu^+\mu^-)\Lambda^0(p^+\pi^-)$ decay described by:

- 4 helicity amplitudes \Rightarrow
- Dynamics described by 5 angles - sensitive to squared amplitudes
- Parity violating decay asymmetry parameter:

$$\alpha_b = |a_+|^2 - |a_-|^2 + |b_+|^2 - |b_-|^2$$

$$|a_+|^2 + |a_-|^2 + |b_+|^2 + |b_-|^2 = 1$$

- Full angular PDF:

$$W(\vec{\Omega}, \vec{A}, P) = \frac{1}{(4\pi)^3} \sum_{i=0}^{19} f_{1i}(\vec{A}) f_{2i}(P\alpha_\Lambda) F_i(\vec{\Omega})$$

- $f_{1i}(\vec{A})$: bilinear combination of helicity amplitudes

$$\vec{A} \equiv (a_+, a_-, b_+, b_-) \quad \begin{aligned} a_+ &= |a_+| e^{i\rho_+}, & a_- &= |a_-| e^{i\rho_-}, \\ b_+ &= |b_+| e^{i\omega_+}, & b_- &= |b_-| e^{i\omega_-} \end{aligned}$$

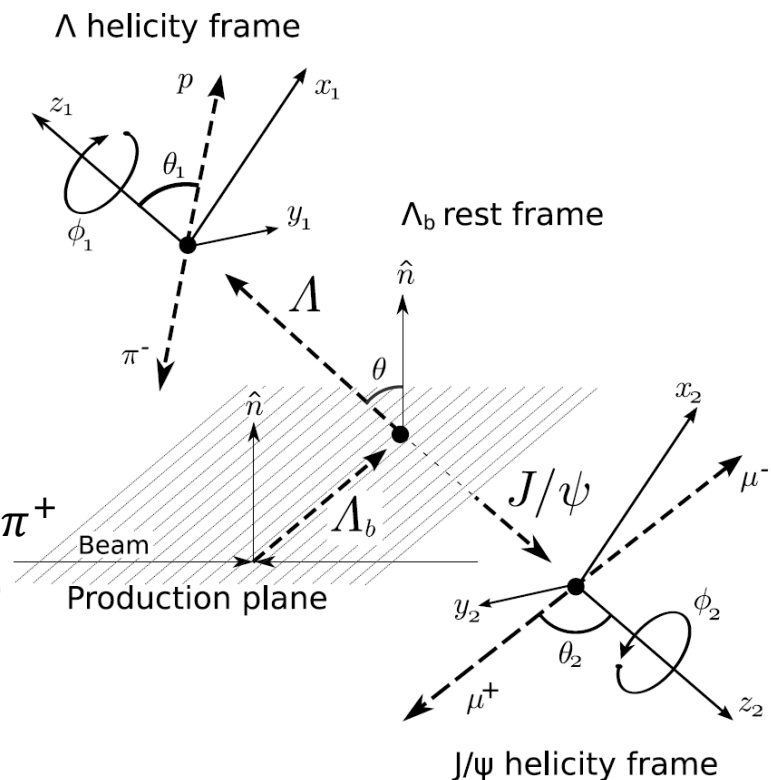
- $f_{2i}(P\alpha_\Lambda)$: has a values of $P\alpha_\Lambda, P, \alpha_\Lambda$ or 1

- Assym. param. $\alpha_\Lambda = -0.642 \pm 0.013^{[1]}$ for $\Lambda^0 \rightarrow p\pi^+$
- Exploit ATLAS symmetry in $\eta \Rightarrow$ Polarization = 0

- $F_i(\vec{\Omega})$: orthogonal functions of decay angles

- Analysis uses method of moments:

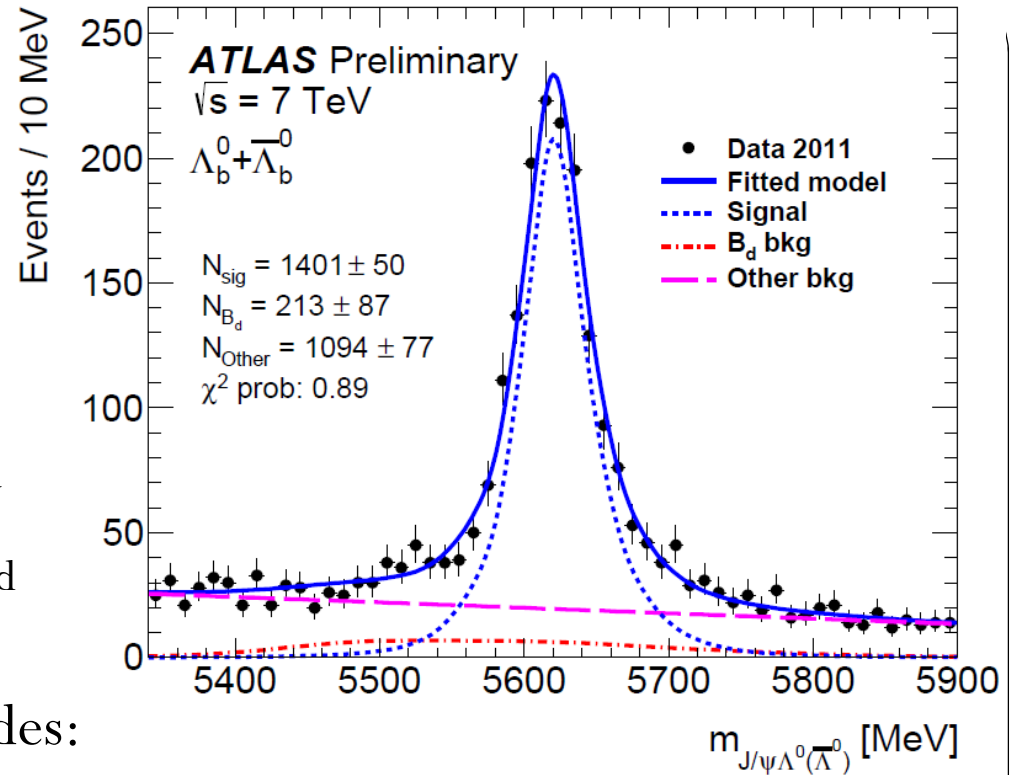
- Extract α_b and helicity amplitudes from measured averages of each F_i (moments).



α_b Measurement

Selection of Λ_b^0 dataset:

- As for the mass & lifetime analysis plus specific requirements for this analysis:
 - B_d^0 veto: $\mathcal{P}(\Lambda_b^0) > \mathcal{P}(B_d^0)$ if both
 - Λ_b proper decay time $\tau > 0.35$ ps
 - Sig. Reg.: $5560 < M(J/\psi \Lambda^0) < 5680$ MeV
- $N_{sig}, N_{B_d}, N_{other}$ determined from extended binned maximum likelihood fit



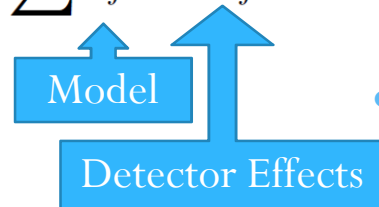
Extraction of α_b and helicity amplitudes:

- Perform χ^2 fit to measured moments $\langle F_i \rangle$:

$$\chi^2 = \sum_{i=1}^5 \sum_{j=1}^5 (\langle F_i \rangle^{\text{expected}} - \langle F_i \rangle) V_{ij}^{-1} (\langle F_j \rangle^{\text{expected}} - \langle F_j \rangle)$$

V_{ij} : Covariance matrix of measured $\langle F_i \rangle$

$$\langle F_i \rangle^{\text{expected}} = \sum f_j(\vec{A}) C_{ij}$$



- Model defined in terms of 5 free parameters:

$$\alpha_b, k_0 = \frac{|a_+|}{\sqrt{|a_-|^2 + |b_+|^2}}, k_1 = \frac{|b_-|}{\sqrt{|a_-|^2 + |b_-|^2}}, \Delta_+ = \rho_+ - \omega_+, \Delta_- = \rho_- - \omega_-$$

- Detector accept. and effic. encoded by C_{ij} :

- No dependence on helicity parameters
- Determined from MC samples generated with flat angular distributions

Fit Result

- Fit Result:

$$\alpha_b = 0.28 \pm 0.16 \pm 0.06$$

$$|a_+| = 0.17_{-0.17}^{+0.12} \text{ (stat.)} \pm 0.06 \text{ (syst.)}$$

$$|a_-| = 0.59_{-0.07}^{+0.06} \text{ (stat.)} \pm 0.04 \text{ (syst.)}$$

$$|b_+| = 0.78_{-0.05}^{+0.04} \text{ (stat.)} \pm 0.02 \text{ (syst.)}$$

$$|b_-| = 0.08_{-0.08}^{+0.13} \text{ (stat.)} \pm 0.05 \text{ (syst.)}$$

- Systematics mainly from:

- Uncertainties in background contrib. to measured $\langle F_i \rangle$
- Calculation of correction matrix

- Λ^0 and J/ψ from Λ_b^0 decay are highly polarized in the direction of their momenta

- Large $|a_-|$ and $|b_+| \Rightarrow$ negative-helicity states for Λ^0 preferred

- α_b value:

- consistent with LHCb measurement: $0.05 \pm 0.17 \text{ (stat.)} \pm 0.07 \text{ (syst.)}$ (Physics Letters **B 724** (2013) 27)

- Intermediate between pQCD and HQET predictions:

$\sim 2.5\sigma$ c.f. pQCD expectation $\sim (-0.14 \rightarrow -0.18)$ Chou et. al. Phys. Rev. D65 (2002) 074030

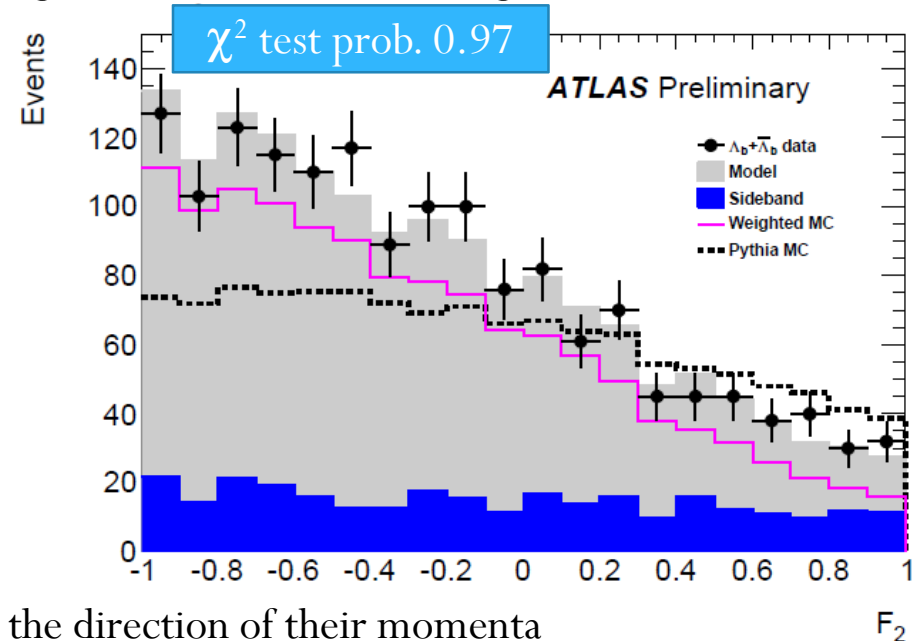
Leitner et al. Nucl. Phys. A755 (2005) 435,

$\sim 2.9\sigma$ c.f. HQET expectation (0.78)

Ajaltouni et al. Phys. Let. B614 (2005) 165

Check of fit results:

- MC events weighted with signal PDF and parameters resulting from fit
- Compare F_i distribution for data with weighted signal MC plus sideband b.g.



Summary

NEW • $B(B_s^0 \rightarrow \mu^+ \mu^-)$ measurement updated with full 2011 dataset (4.9 fb⁻¹):

- $B(B_s^0 \rightarrow \mu^+ \mu^-) < 1.5$ (95% C.L.)

ATLAS-CONF-2013-076

- Consistent with SM expectation, LHCb measurement and other experimental limits

• Λ_b^0 mass & lifetime have been measured:

$$\tau = 1.449 \pm 0.036(\text{stat.}) \pm 0.017(\text{syst.}) \text{ (ps)}$$

[Phys. Rev. D87 \(2013\) 032002](#)

$$m = 5619.7 \pm 0.7(\text{stat.}) \pm 1.1(\text{syst.}) \text{ MeV}$$

$$R = \tau(\Lambda_b^0) / \tau(B_d^0) = 0.960 \pm 0.025(\text{stat.}) \pm 0.016(\text{syst.})$$

- Consistent with both pQCD and HQET predictions and other experimental measurements

NEW • Λ_b^0 parity violating parameter, α_b , and helicity amplitudes have been measured:

ATLAS-CONF-2013-071

$$\alpha_b = 0.28 \pm 0.16 \pm 0.06$$

$$|a_+| = 0.17_{-0.17}^{+0.12}(\text{stat.}) \pm 0.06(\text{syst.}); |a_-| = 0.59_{-0.07}^{+0.06}(\text{stat.}) \pm 0.04(\text{syst.})$$

$$|b_+| = 0.78_{-0.05}^{+0.04}(\text{stat.}) \pm 0.02(\text{syst.}); |b_-| = 0.08_{-0.08}^{+0.13}(\text{stat.}) \pm 0.05(\text{syst.})$$

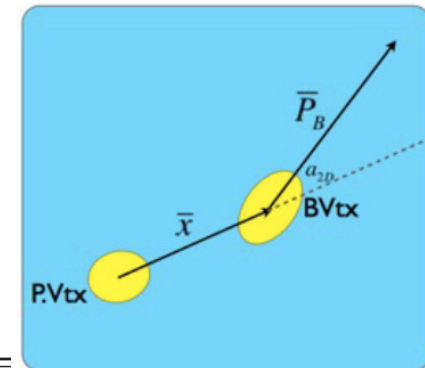
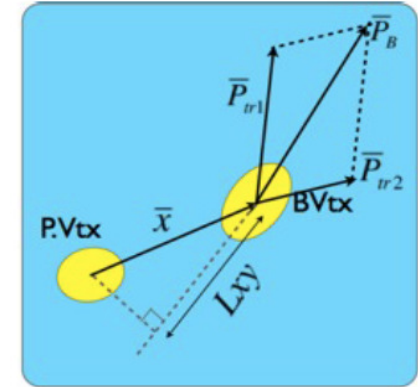
- α_b differs from pQCD expectation $-(0.14 \sim 0.18)$ by $\sim 2.5\sigma$ and HQET expectation (0.78) by 2.9σ

• More accurate measurements will be made with 2012 data (21.7 fb⁻¹ rec.)

Backup

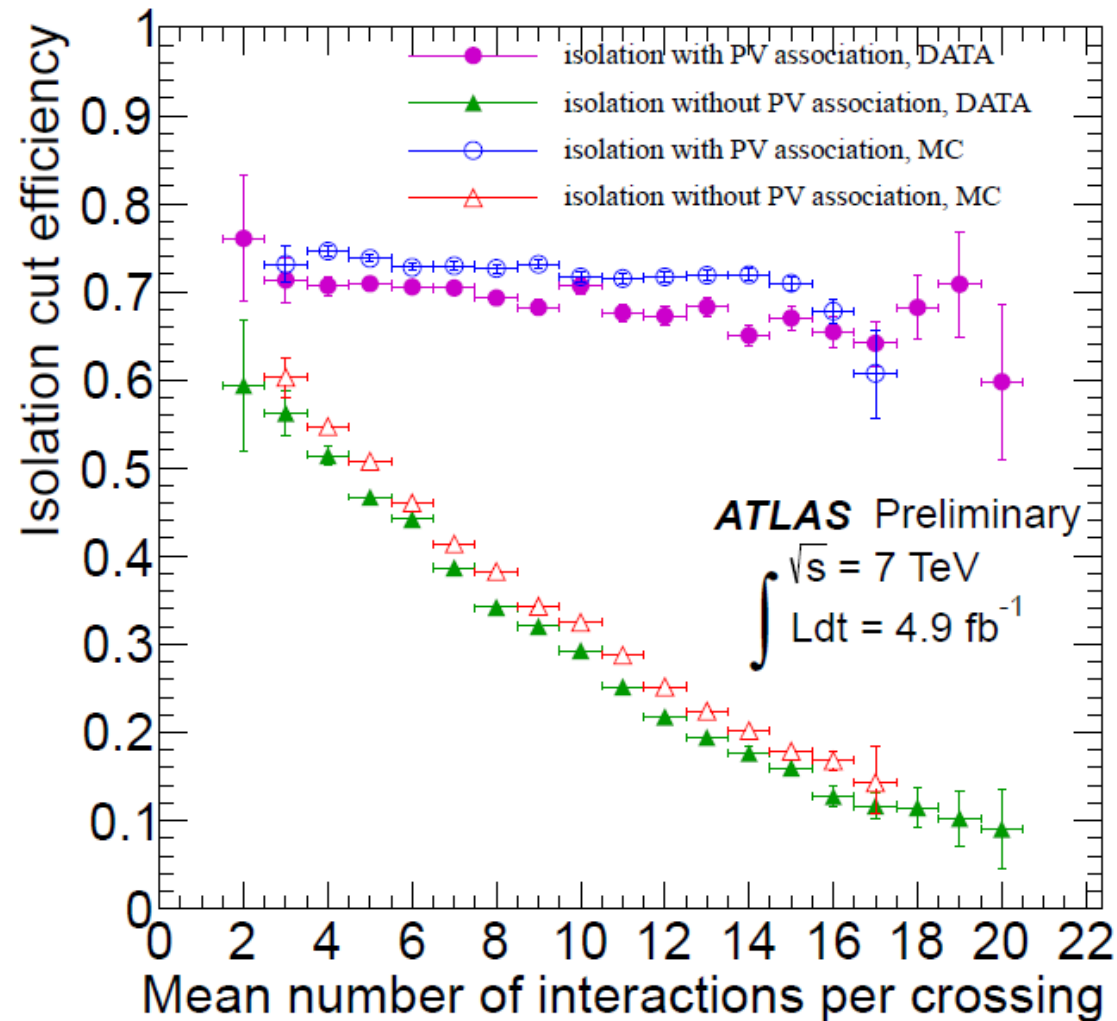
Discriminating Variables for $B_S^0 \rightarrow \mu^+ \mu^-$

Variable	Description	Ranking
L_{xy}	Scalar product in the transverse plane of $(\Delta\vec{x} \cdot \vec{p}^B)/ \vec{p}_T^B $	1
$I_{0.7}$ isolation	Ratio of $ \vec{p}_T^B $ to the sum of $ \vec{p}_T^B $ and the transverse momenta of all tracks with $p_T > 0.5$ GeV within a cone $\Delta R < 0.7$ from the B direction, excluding B decay products	2
$ \alpha_{2D} $	Absolute value of the angle in the transverse plane between $\Delta\vec{x}$ and \vec{p}^B	3
p_L^{\min}	Minimum momentum of the two muon candidates along the B direction	4
p_T^B	B transverse momentum	5
ct significance	Proper decay length $ct = L_{xy} \times m_B/p_T^B$ divided by its uncertainty	6
χ_z^2, χ_{xy}^2	Significance of the separation between production (PV) and decay vertex (SV) $\Delta\vec{x}^T \cdot (\sigma_{\Delta\vec{x}}^2)^{-1} \cdot \Delta\vec{x}$, in z and (x, y) , respectively	7, 13
$ D_{xy} ^{\min}, D_z ^{\min}$	Absolute values of the minimum distance of closest approach in the xy plane or along z of tracks in the event to the B vertex	8, 11
ΔR	Angle $\sqrt{(\Delta\phi)^2 + (\Delta\eta)^2}$ between $\Delta\vec{x}$ and \vec{p}^B	9
$ d_0 ^{\max}, d_0 ^{\min}$	Absolute values of the maximum and minimum impact parameter in the transverse plane of the B decay products relative to the primary vertex	10, 12



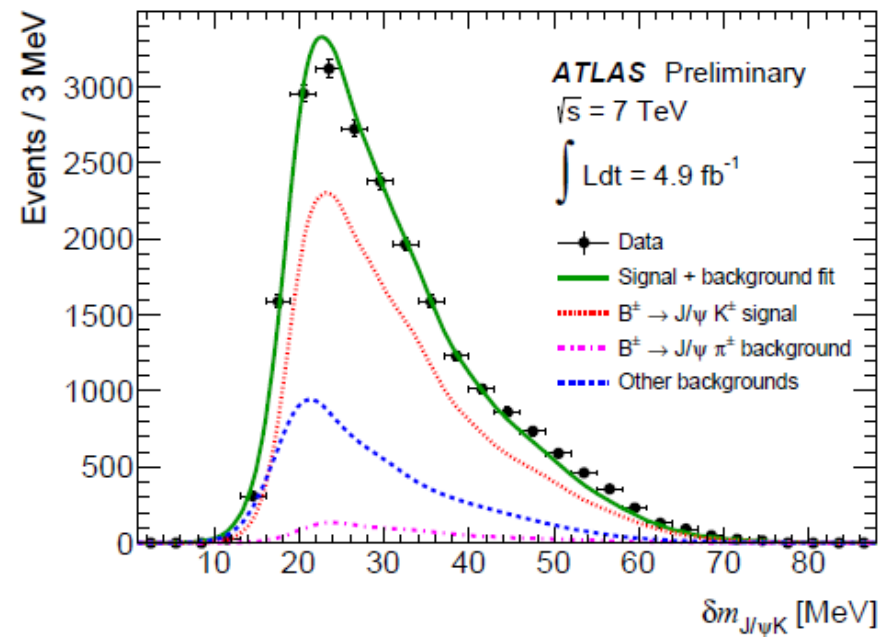
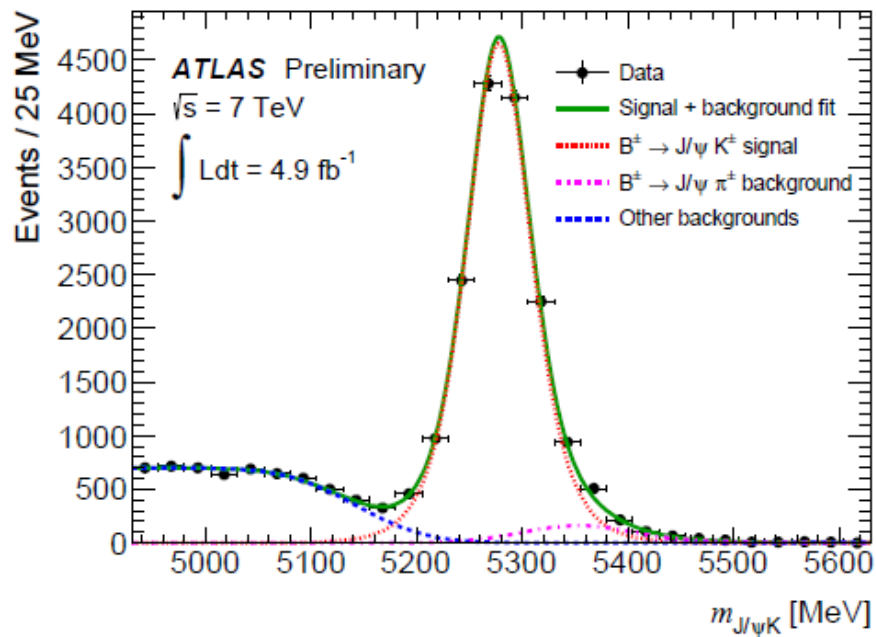
BDT input variables for $B(B_s^0 \rightarrow \mu^+ \mu^-)$ measurement

- Stability of Isolation parameter w.r.t. pile-up



B- \rightarrow J/ ψ K yield

Fit results



CLs limit extraction

$$\mathcal{L} = \text{Poisson}(N_{SR}^{obs} | \epsilon \mathcal{B} + N_{bkg} + N_{B \rightarrow hh'}) \text{Poisson}(N_{bkg, SB}^{obs} | R_{bkg} N_{bkg}) \times \\ \text{Gauss}(\epsilon^{obs} | \epsilon, \sigma_\epsilon) \text{Gauss}(R_{bkg}^{obs} | R_{bkg}, \sigma_{R_{bkg}})$$

\mathcal{B} Branching fraction to be measured

ϵ Inverse of the SES constrained to ϵ^{obs}

N_{bkg} No. Continuum background events in signal region

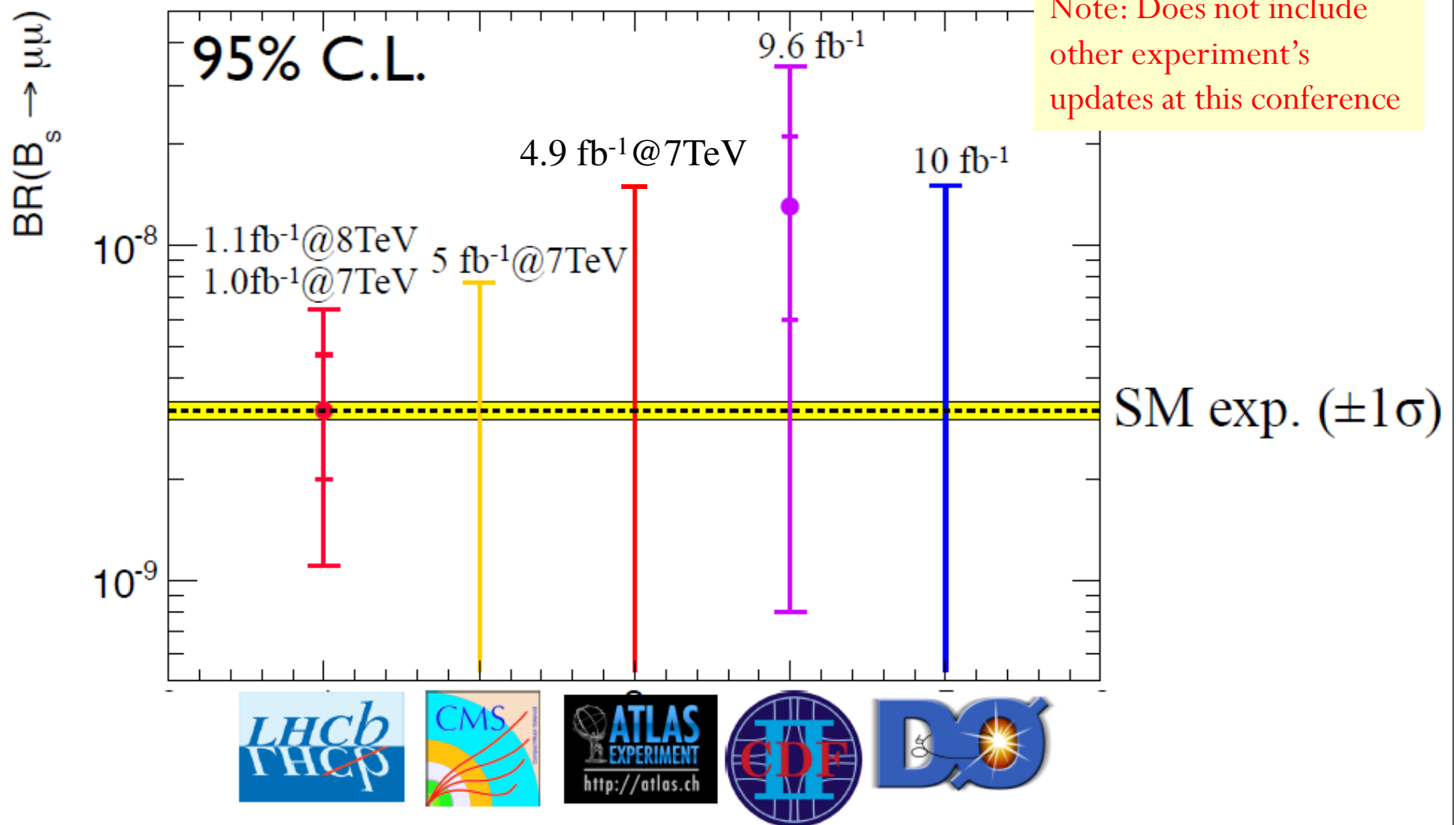
N_{SR}^{obs} No. even and odd numbered events observed in the signal region








$N_{bkg, SB}^{obs}$ No. even no. events observed in sidebands

$N_{B \rightarrow hh'}$ Contribution from irreducible resonant $B \rightarrow hh'$ background

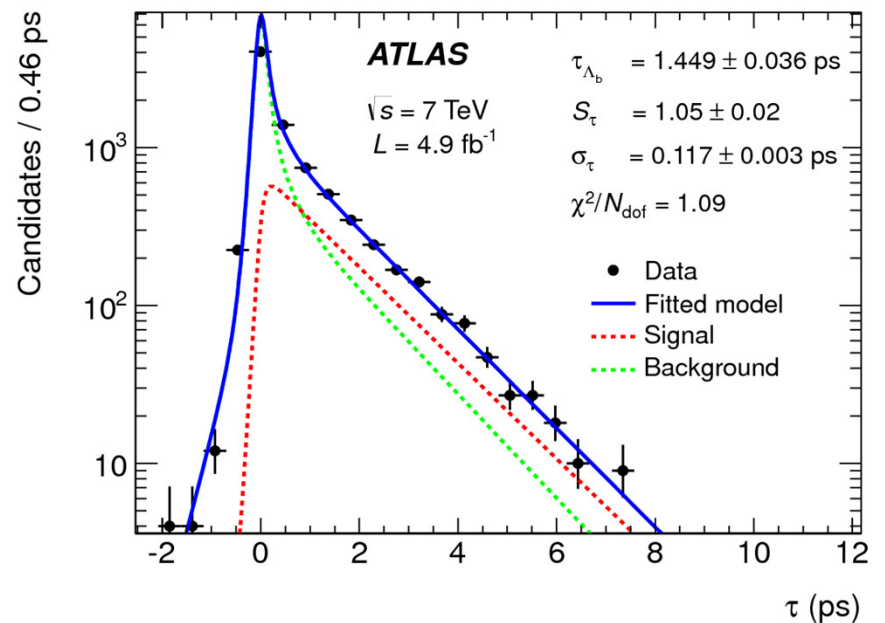
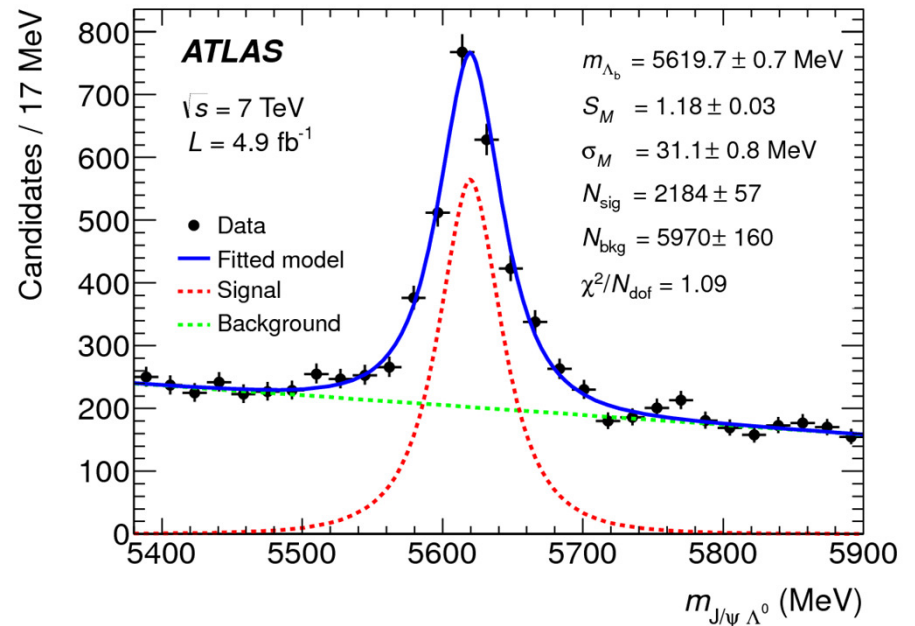
R_{bkg} Expected ration of background events in the SB to those in the SR
- constrained to R_{bkg}^{obs} the ratio of widths of the two regions

Comparison with other measurements

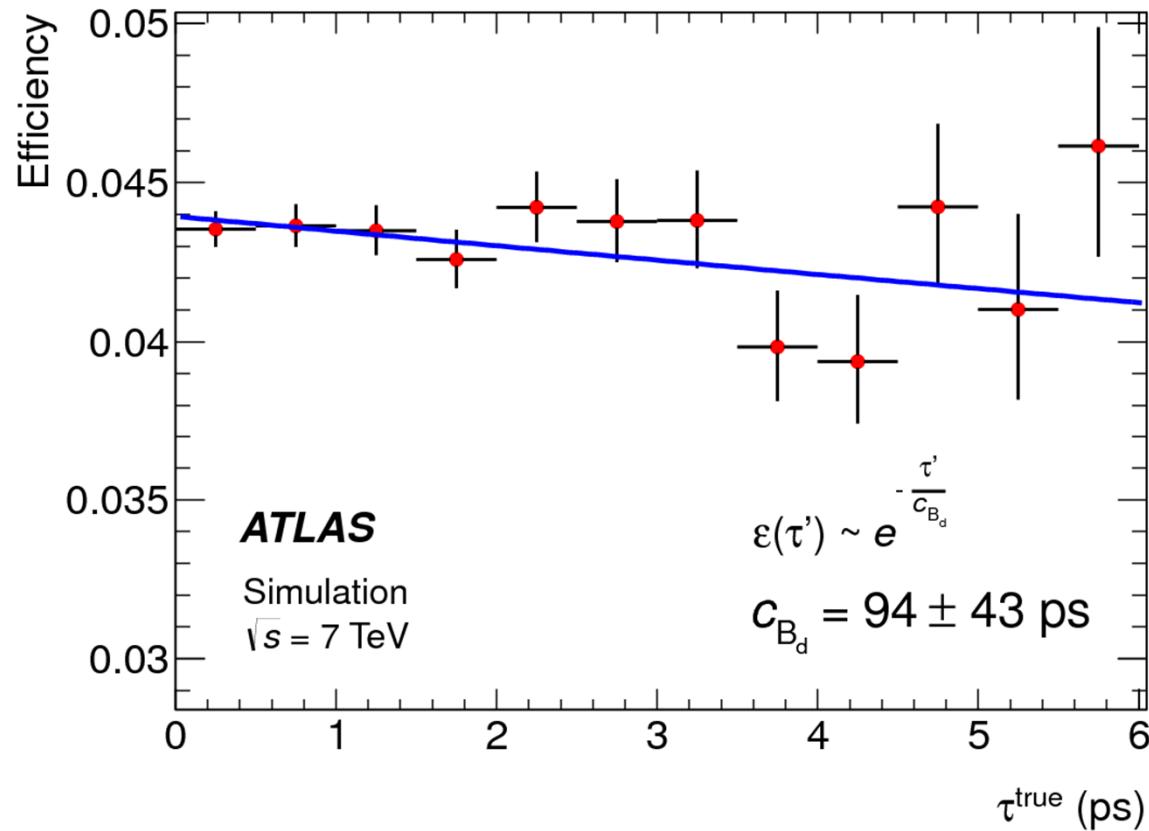


		$BR(B^0 \rightarrow \mu^+ \mu^-)$	$BR(B_s^0 \rightarrow \mu^+ \mu^-)$
	1.1 fb ⁻¹ (8TeV) 1.0 fb ⁻¹ (7TeV)	$<9.4 \times 10^{-10}$	$[1.1, 6.4] \times 10^{-9}$ ----- $(3.2^{+1.5}_{-1.2}) \times 10^{-9}$
	5 fb ⁻¹ (7TeV)	$<1.8 \times 10^{-9}$	$<7.7 \times 10^{-9}$
	4.9 fb ⁻¹ (7TeV)	-	$<1.5 \times 10^{-8}$
	9.6 fb ⁻¹	$<4.6 \times 10^{-9}$	$[0.8, 34] \times 10^{-9}$ ----- $(1.3^{+0.9}_{-0.7}) \times 10^{-8}$
	10 fb ⁻¹	-	$<1.5 \times 10^{-8}$
	78fb ⁻¹	$<1.6 \times 10^{-8}$	-
	347fb ⁻¹	$<8.3 \times 10^{-9}$	-

Mass & Lifetime Fit



Λ_b Lifetime measurement



Efficiency
correction as a
function of decay
length

Λ_b assymetry measurement

Full Angular PDF

$$w(\vec{\Omega}, \vec{A}, P) = \frac{1}{(4\pi)^3} \sum_{i=0}^{19} f_{1i}(\vec{A}) f_{2i}(P, \alpha_\Lambda) F_i(\vec{\Omega})$$

i	f_{1i}	f_{2i}	F_i
0	$a_+ a_+^* + a_- a_-^* + b_+ b_+^* + b_- b_-^*$	1	1
1	$a_+ a_+^* - a_- a_-^* + b_+ b_+^* - b_- b_-^*$	P	$\cos \theta$
2	$a_+ a_+^* - a_- a_-^* - b_+ b_+^* + b_- b_-^*$	α_Λ	$\cos \theta_1$
3	$a_+ a_+^* + a_- a_-^* - b_+ b_+^* - b_- b_-^*$	$P \alpha_\Lambda$	$\cos \theta \cos \theta_1$
4	$-a_+ a_+^* - a_- a_-^* + \frac{1}{2} b_+ b_+^* + \frac{1}{2} b_- b_-^*$	1	$\frac{1}{2} (3 \cos^2 \theta_2 - 1)$
5	$-a_+ a_+^* + a_- a_-^* + \frac{1}{2} b_+ b_+^* - \frac{1}{2} b_- b_-^*$	P	$\frac{1}{2} (3 \cos^2 \theta_2 - 1) \cos \theta$
6	$-a_+ a_+^* + a_- a_-^* - \frac{1}{2} b_+ b_+^* + \frac{1}{2} b_- b_-^*$	α_Λ	$\frac{1}{2} (3 \cos^2 \theta_2 - 1) \cos \theta_1$
7	$-a_+ a_+^* - a_- a_-^* - \frac{1}{2} b_+ b_+^* - \frac{1}{2} b_- b_-^*$	$P \alpha_\Lambda$	$\frac{1}{2} (3 \cos^2 \theta_2 - 1) \cos \theta \cos \theta_1$
8	$-3 \text{Re}(a_+ a_-^*)$	$P \alpha_\Lambda$	$\sin \theta \sin \theta_1 \sin^2 \theta_2 \cos \varphi_1$
9	$3 \text{Im}(a_+ a_-^*)$	$P \alpha_\Lambda$	$\sin \theta \sin \theta_1 \sin^2 \theta_2 \sin \varphi_1$
10	$-\frac{3}{2} \text{Re}(b_- b_+^*)$	$P \alpha_\Lambda$	$\sin \theta \sin \theta_1 \sin^2 \theta_2 \cos(\varphi_1 + 2\varphi_2)$
11	$\frac{3}{2} \text{Im}(b_- b_+^*)$	$P \alpha_\Lambda$	$\sin \theta \sin \theta_1 \sin^2 \theta_2 \sin(\varphi_1 + 2\varphi_2)$
12	$-\frac{3}{\sqrt{2}} \text{Re}(b_- a_+^* + a_- b_+^*)$	$P \alpha_\Lambda$	$\sin \theta \cos \theta_1 \sin \theta_2 \cos \theta_2 \cos \varphi_2$
13	$\frac{3}{\sqrt{2}} \text{Im}(b_- a_+^* + a_- b_+^*)$	$P \alpha_\Lambda$	$\sin \theta \cos \theta_1 \sin \theta_2 \cos \theta_2 \sin \varphi_2$
14	$-\frac{3}{\sqrt{2}} \text{Re}(b_- a_-^* + a_+ b_+^*)$	$P \alpha_\Lambda$	$\cos \theta \sin \theta_1 \sin \theta_2 \cos \theta_2 \cos(\varphi_1 + \varphi_2)$
15	$\frac{3}{\sqrt{2}} \text{Im}(b_- a_-^* + a_+ b_+^*)$	$P \alpha_\Lambda$	$\cos \theta \sin \theta_1 \sin \theta_2 \cos \theta_2 \sin(\varphi_1 + \varphi_2)$
16	$\frac{3}{\sqrt{2}} \text{Re}(a_- b_+^* - b_- a_+^*)$	P	$\sin \theta \sin \theta_2 \cos \theta_2 \cos \varphi_2$
17	$-\frac{3}{\sqrt{2}} \text{Im}(a_- b_+^* - b_- a_+^*)$	P	$\sin \theta \sin \theta_2 \cos \theta_2 \sin \varphi_2$
18	$\frac{3}{\sqrt{2}} \text{Re}(b_- a_-^* - a_+ b_+^*)$	α_Λ	$\sin \theta_1 \sin \theta_2 \cos \theta_2 \cos(\varphi_1 + \varphi_2)$
19	$-\frac{3}{\sqrt{2}} \text{Im}(b_- a_-^* - a_+ b_+^*)$	α_Λ	$\sin \theta_1 \sin \theta_2 \cos \theta_2 \sin(\varphi_1 + \varphi_2)$

α_b Measurement

- Polarization $P=0$: due to symmetry of initial state & ATLAS symmetry in pseudo-rapidity
 - f_{1i}, f_{2i}, F_i reduced to 6 coefficients (from 20):

i	f_{1i}	f_{2i}	F_i
0	1	1	1
2	$(k_0^2 + k_1^2 - 1) + \alpha_b(k_0^2 - k_1^2)$	α_Λ	$\cos \theta_1$
4	$\frac{1}{4}[(3k_1^2 - 3k_0^2 - 1) + 3\alpha_b(1 - k_1^2 - k_0^2)]$	1	$\frac{1}{2}(3 \cos^2 \theta_2 - 1)$
6	$-\frac{1}{4}[(k_0^2 + k_1^2 - 1) + \alpha_b(3 + k_0^2 - k_1^2)]$	α_Λ	$\frac{1}{2}(3 \cos^2 \theta_2 - 1) \cos \theta_1$
18	$\frac{3}{\sqrt{2}}[\frac{1-\alpha_b}{2} \sqrt{k_1^2(1-k_1^2)} \cos(-\Delta_-) - \frac{1+\alpha_b}{2} \sqrt{k_0^2(1-k_0^2)} \cos(\Delta_+)]$	α_Λ	$\sin \theta_1 \sin \theta_2 \cos \theta_2 \cos(\varphi_1 + \varphi_2)$
19	$-\frac{3}{\sqrt{2}}[\frac{1-\alpha_b}{2} \sqrt{k_1^2(1-k_1^2)} \sin(-\Delta_-) - \frac{1+\alpha_b}{2} \sqrt{k_0^2(1-k_0^2)} \sin(\Delta_+)]$	α_Λ	$\sin \theta_1 \sin \theta_2 \cos \theta_2 \sin(\varphi_1 + \varphi_2)$

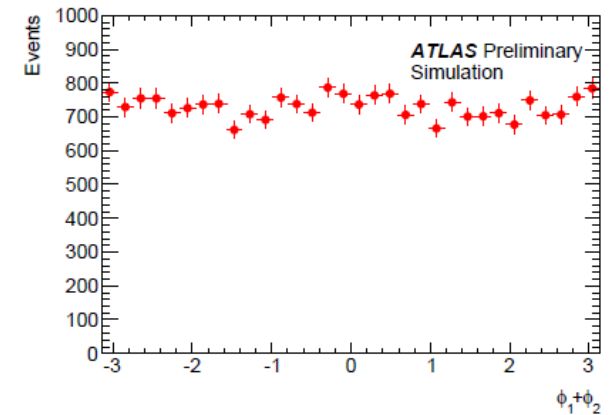
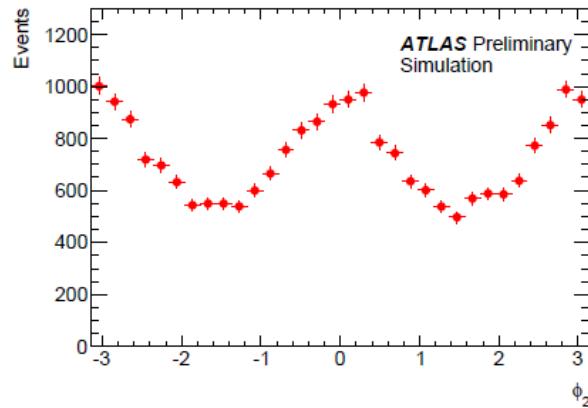
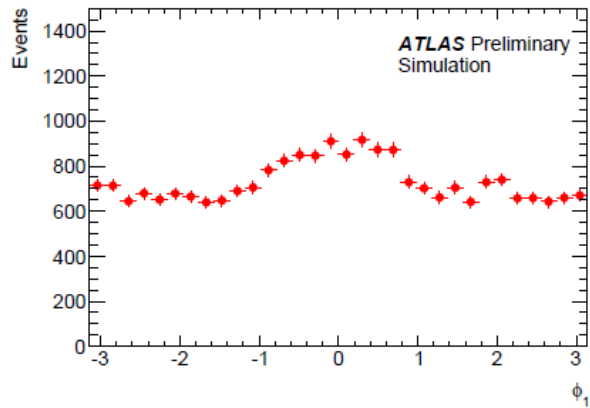
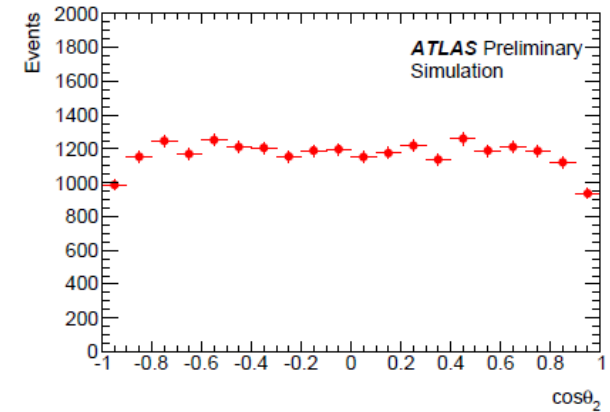
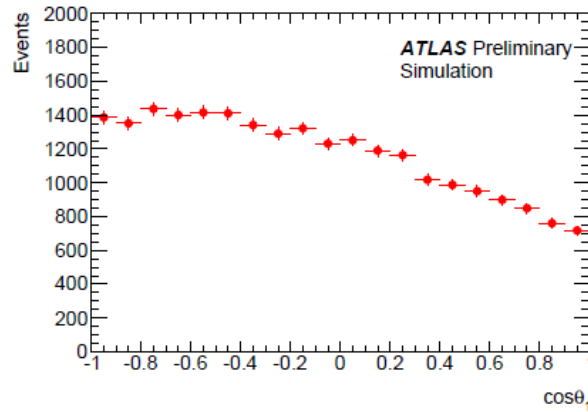
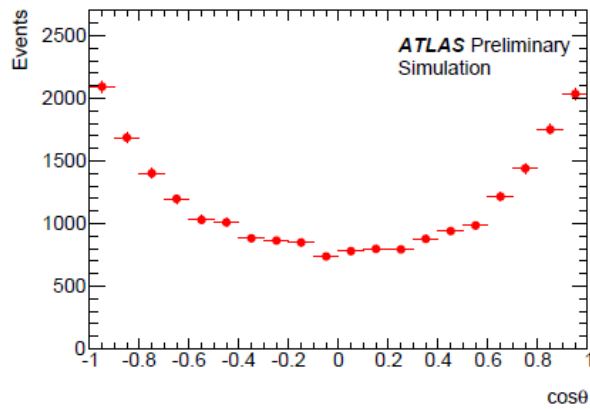
- Use following 5 parameters to define model:

$$\alpha_b = |a_+|^2 - |a_-|^2 + |b_+|^2 - |b_-|^2$$

$$k_0 = \frac{|a_+|}{\sqrt{|a_-|^2 + |b_+|^2}}, \quad k_1 = \frac{|b_-|}{\sqrt{|a_-|^2 + |b_-|^2}}$$

$$\Delta_+ = \rho_+ - \omega_+, \quad \Delta_- = \rho_- - \omega_-$$

Efficiency Correction



$$C = \begin{pmatrix} 1 & -0.114 & -0.030 & 0.0069 & 0.0220 & -0.0028 \\ -0.113 & 0.3093 & 0.0066 & -0.0125 & 0.0029 & -0.0009 \\ -0.030 & 0.0070 & 0.1782 & -0.0188 & 0.0040 & -0.0001 \\ 0.0066 & -0.0124 & -0.0188 & 0.0547 & 0.00012 & 0.00032 \\ 0.0219 & 0.0028 & 0.0039 & 0.00016 & 0.0465 & 0.0005 \\ -0.0032 & -0.0007 & -0.0003 & 0.00035 & 0.0005 & 0.0450 \end{pmatrix}$$

Ideal case, no detector effects:

$$D = \text{diag}\left\{1, \frac{1}{3}, \frac{1}{5}, \frac{1}{15}, \frac{2}{45}, \frac{2}{45}\right\}$$

Fit Results

- Measured $\langle F_i \rangle$ values:

- $\langle F_2 \rangle = -0.282 \pm 0.021$
- $\langle F_4 \rangle = -0.044 \pm 0.017$
- $\langle F_6 \rangle = 0.001 \pm 0.010$
- $\langle F_{18} \rangle = 0.019 \pm 0.009$
- $\langle F_{19} \rangle = -0.002 \pm 0.009$

$\langle F_i \rangle$	$\langle F_2 \rangle$	$\langle F_4 \rangle$	$\langle F_6 \rangle$	$\langle F_{18} \rangle$	$\langle F_{19} \rangle$
$\langle F_2 \rangle$	1	-0.066	-0.121	0.028	0.003
$\langle F_4 \rangle$		1	-0.503	0.088	0.000
$\langle F_6 \rangle$			1	-0.025	-0.008
$\langle F_{18} \rangle$				1	0.048
$\langle F_{19} \rangle$					1

Correlation matrix of $\langle F_i \rangle$ Measurements

- Values obtained from fit:

- $\alpha_b = 0.28 \pm 0.16$, $k_0 = 0.22_{-0.57}^{+0.14}$, $k_1 = 0.13_{-0.47}^{+0.20}$

Correlation matrix of the fitted parameters.

Parameter	α_b	k_0	k_1
α_b	1	0.41	-0.20
k_0		1	0.19
k_1			1

