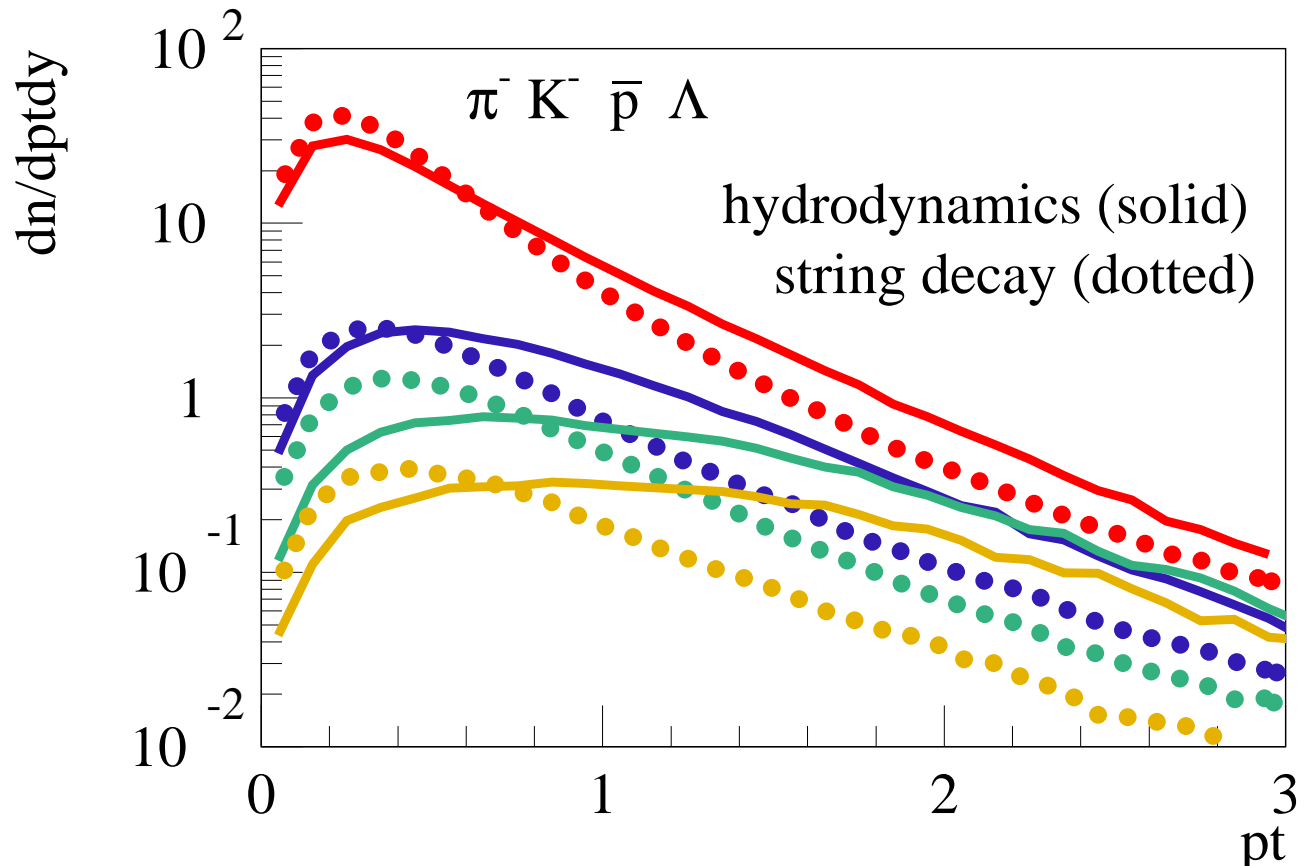


# Flow in proton-nucleus collisions at 5 TeV

# Manifestation of flow:

## Particle spectra affected by radial flow



**=> mass ordering of  $\langle p_t \rangle$ ,      lambda/K increase**

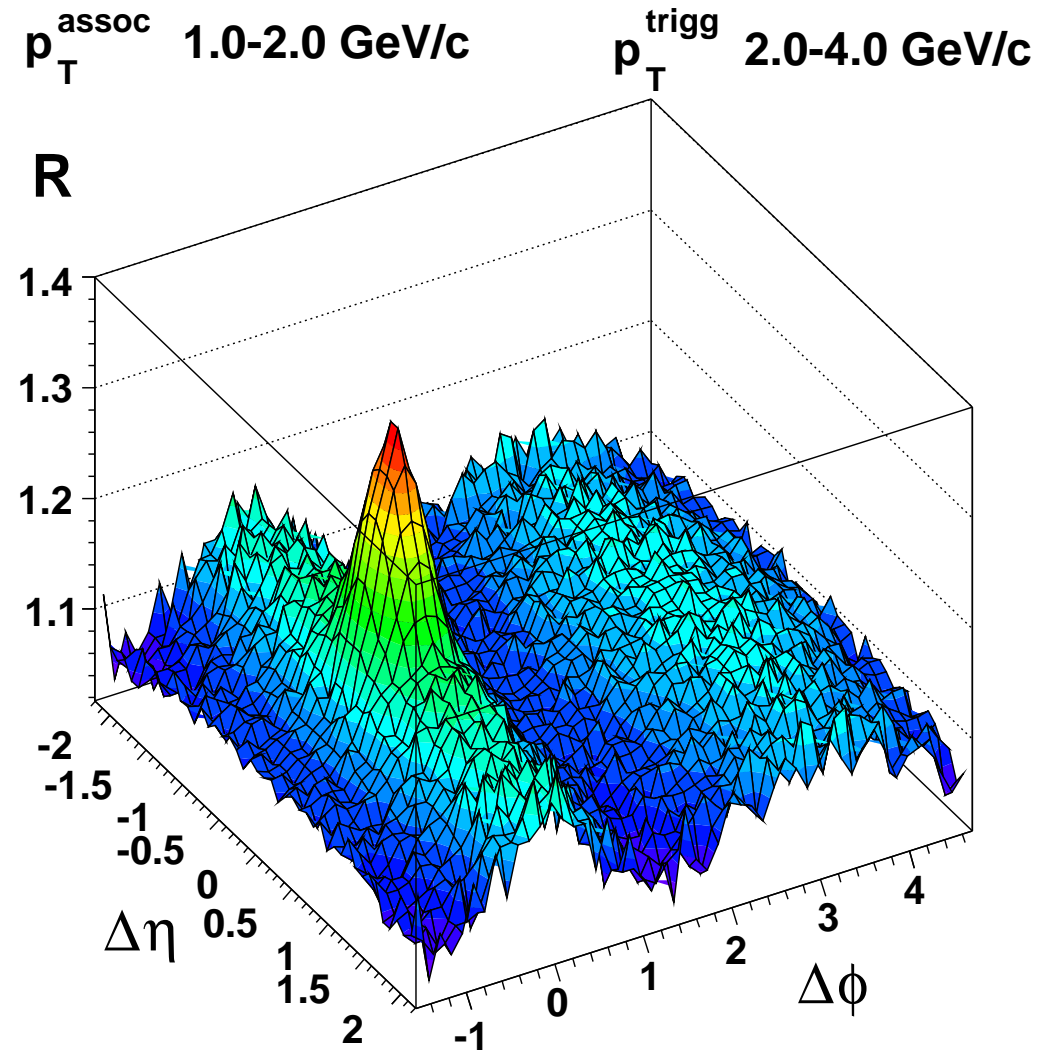
## Ridges & flow harmonics

Ridges appear in

$$R = \frac{1}{N_{\text{trigg}}} \frac{dn}{d\Delta\phi\Delta\eta}$$

**due to initial  
azimuthal  
anisotropies**

(longitudinally  
invariant)



EPOS3.074

# **pPb data, interpreted in terms of hydrodynamic flow**

Models:

**P. Bozek, W. Broniowski**, arXiv:1304.3044

analysis of pPb@5TeV

- Glauber model (wounded nucleon model) initial conditions
- Viscous hydrodynamic expansion,  $\eta/s = 0.08$  or  $0.16$
- Statistical hadronization using “Terminator”

**A. Bzdak, B. Schenke, P. Tribedy, R. Venugopalan,**

arXiv:1304.3403

- Theoretical study of flow in pp, pA, dA
- Glauber model or Color Glass Condensate initial conditions
- Viscous hydrodynamic expansion,  $\eta/s = 0.08$

## **EPOS3, B. Guiot, Y. Karpenko, T. Pierog, K. Werner**

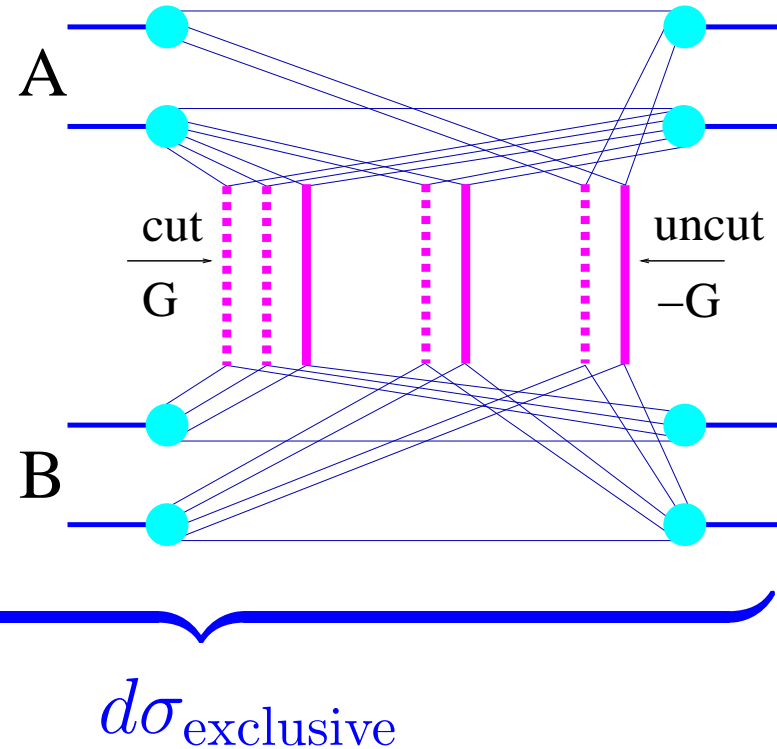
- Initial conditions:  
Gribov-Regge multiple scattering approach,  
elementary object = Pomeron = parton ladder,  
using saturation scale  $Q_s \propto N_{part} \hat{s}^\lambda$
- Core-corona approach  
to separate fluid and jet hadrons
- Viscous hydrodynamic expansion,  $\eta/s = 0.08$
- Statistical hadronization, final state hadronic cascade

**EPOS3 will be used in the following**

EPOS IC: Marriage pQCD+GRT+energy sharing

(Drescher, Hladik, Ostapchenko, Pierog, and Werner, Phys. Rept. 350, 2001)

$$\sigma^{\text{tot}} = \sum_{\text{cut P}} \int \sum_{\text{uncut P}} \int$$



$$\text{cut Pom} : G = \frac{1}{2\hat{s}} 2\text{Im} \{ \mathcal{FT} \{ T \} \} (\hat{s}, b), T = i\hat{s} \sigma_{\text{hard}}(\hat{s}) \exp(R_{\text{hard}}^2 t)$$

Nonlinear effects considered via saturation scale  $Q_s \propto N_{\text{part}} \hat{s}^\lambda$

$$\begin{aligned}
 \sigma^{\text{tot}} = & \int d^2b \int \prod_{i=1}^A d^2b_i^A dz_i^A \rho_A(\sqrt{(b_i^A)^2 + (z_i^A)^2}) \\
 & \prod_{j=1}^B d^2b_j^B dz_j^B \rho_B(\sqrt{(b_j^B)^2 + (z_j^B)^2}) \\
 & \sum_{m_1 l_1} \dots \sum_{m_{AB} l_{AB}} (1 - \delta_{0 \Sigma m_k}) \int \prod_{k=1}^{AB} \left( \prod_{\mu=1}^{m_k} dx_{k,\mu}^+ dx_{k,\mu}^- \prod_{\lambda=1}^{l_k} d\tilde{x}_{k,\lambda}^+ d\tilde{x}_{k,\lambda}^- \right) \left\{ \right. \\
 & \prod_{k=1}^{AB} \left( \frac{1}{m_k!} \frac{1}{l_k!} \prod_{\mu=1}^{m_k} G(x_{k,\mu}^+, x_{k,\mu}^-, s, |\vec{b} + \vec{b}_{\pi(k)}^A - \vec{b}_{\tau(k)}^B|) \right. \\
 & \left. \left. \prod_{\lambda=1}^{l_k} -G(\tilde{x}_{k,\lambda}^+, \tilde{x}_{k,\lambda}^-, s, |\vec{b} + \vec{b}_{\pi(k)}^A - \vec{b}_{\tau(k)}^B|) \right) \right\} \\
 & \prod_{i=1}^A \left( 1 - \sum_{\pi(k)=i} x_{k,\mu}^+ - \sum_{\pi(k)=i} \tilde{x}_{k,\lambda}^+ \right)^\alpha \prod_{j=1}^B \left( 1 - \sum_{\tau(k)=j} x_{k,\mu}^- - \sum_{\tau(k)=j} \tilde{x}_{k,\lambda}^- \right)^\alpha \left. \right\}
 \end{aligned}$$



The hydrodynamic equations (Israel-Stewart formulation) in arbitrary coordinate system (implemented/solved by Yuri Karpenko), always  $\eta/S = 0.08$ ,  $\zeta/S = 0$

$$\begin{aligned} \partial_{;\nu} T^{\mu\nu} &= \partial_\nu T^{\mu\nu} + \Gamma_{\nu\lambda}^\mu T^{\nu\lambda} + \Gamma_{\nu\lambda}^\nu T^{\mu\lambda} = 0 \\ \gamma (\partial_t + v_i \partial_i) \pi^{\mu\nu} &= -\frac{\pi^{\mu\nu} - \pi_{\text{NS}}^{\mu\nu}}{\tau_\pi} + I_\pi^{\mu\nu} \\ \gamma (\partial_t + v_i \partial_i) \Pi &= -\frac{\Pi - \Pi_{\text{NS}}}{\tau_\Pi} + I_\Pi \end{aligned}$$

$T^{\mu\nu} = \epsilon u^\mu u^\nu - (p + \Pi) \Delta^{\mu\nu} + \pi^{\mu\nu}$ ,

$\partial_{;\nu}$  denotes a covariant derivative,

$\Delta^{\mu\nu} = g^{\mu\nu} - u^\mu u^\nu$  is the projector orthogonal to  $u^\mu$ ,

$\pi^{\mu\nu}$  and  $\Pi$  are the shear stress tensor and bulk pressure, respectively.

$\pi_{\text{NS}}^{\mu\nu} = \eta(\Delta^{\mu\lambda} \partial_{;\lambda} u^\nu + \Delta^{\nu\lambda} \partial_{;\lambda} u^\mu) - \frac{2}{3} \eta \Delta^{\mu\nu} \partial_{;\lambda} u^\lambda$

$\Pi_{\text{NS}} = -\zeta \partial_{;\lambda} u^\lambda$

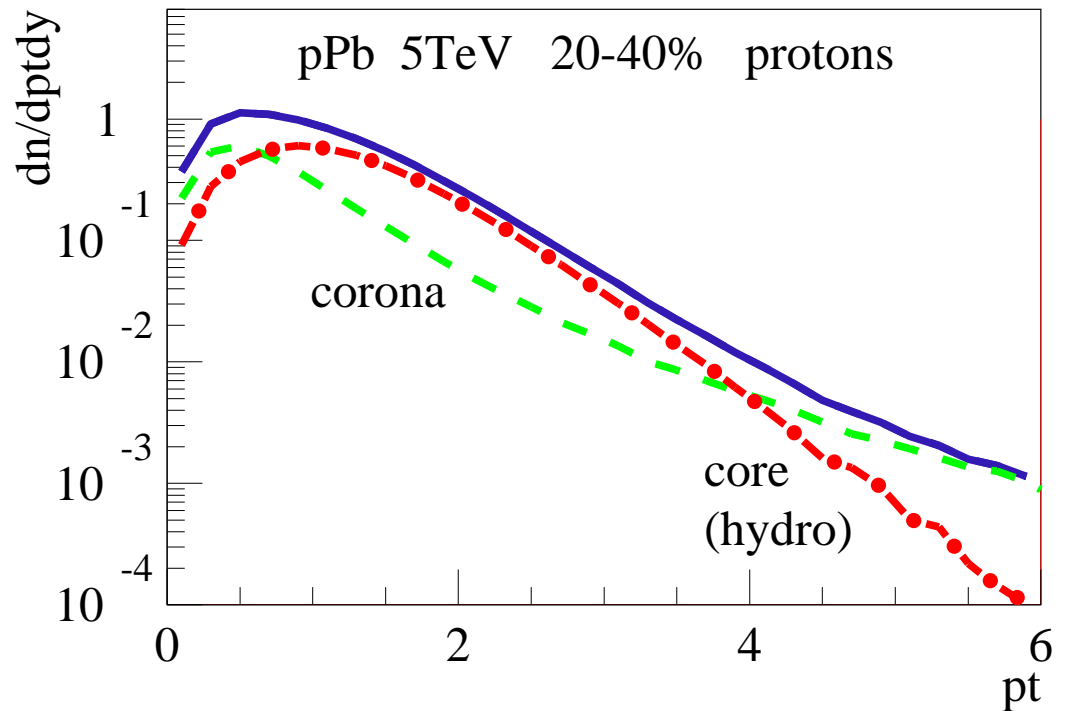
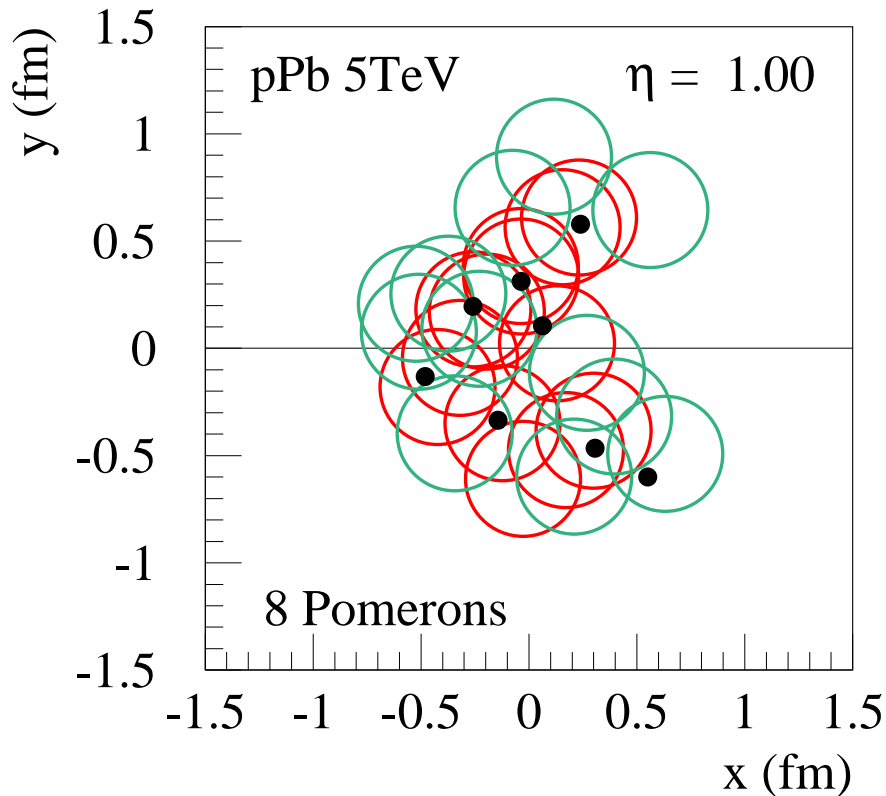
$I_\pi^{\mu\nu} = -\frac{4}{3} \pi^{\mu\nu} \partial_{;\gamma} u^\gamma - [u^\nu \pi^{\mu\beta} + u^\mu \pi^{\nu\beta}] u^\lambda \partial_{;\lambda} u_\beta$

$I_\Pi = -\frac{4}{3} \Pi \partial_{;\gamma} u^\gamma$

**EPOS3:**

**Pomeron => parton ladder => flux tube (kinky string)**

String segments with high  $p_t$  escape => **corona**,  
 the others form the **core** = initial condition for hydro  
 depending on the local string density



## **CMS: Multiplicity dependence of pion, kaon, proton pt spectra**

CMS, arXiv:1307.3442

**We plot 4 “centrality” classes:**

$$\langle N_{\text{tracks}} \rangle = 8, 84, 160, 235 \text{ (in } |\eta| < 2.4 \text{)}$$

**Multiplicity = centrality measure**

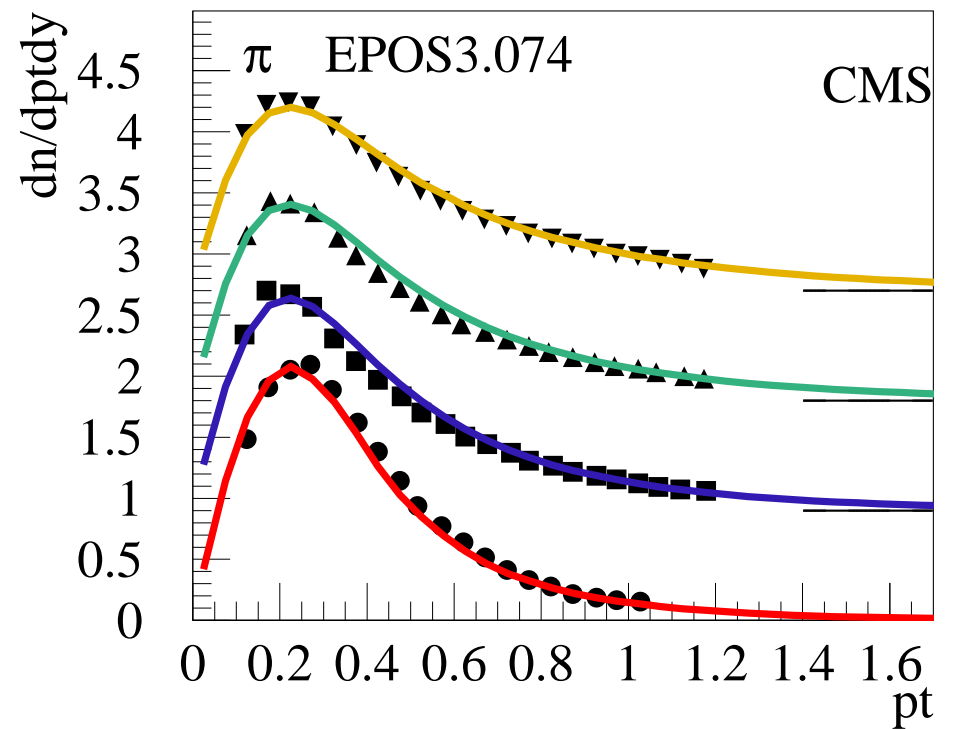
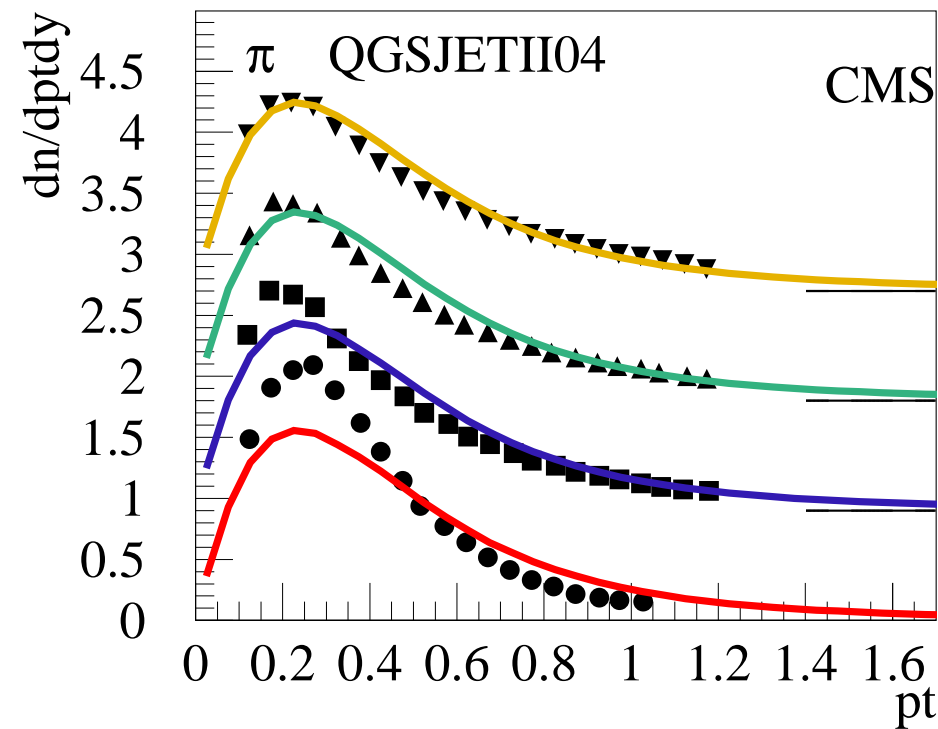
**in EPOS: high multiplicity = many Pomerons**

**Data compared to**

- EPOS3 (hydrodynamic expansion, flow)**
- QGSJETII (no flow effects, only string decay)**

## Pions

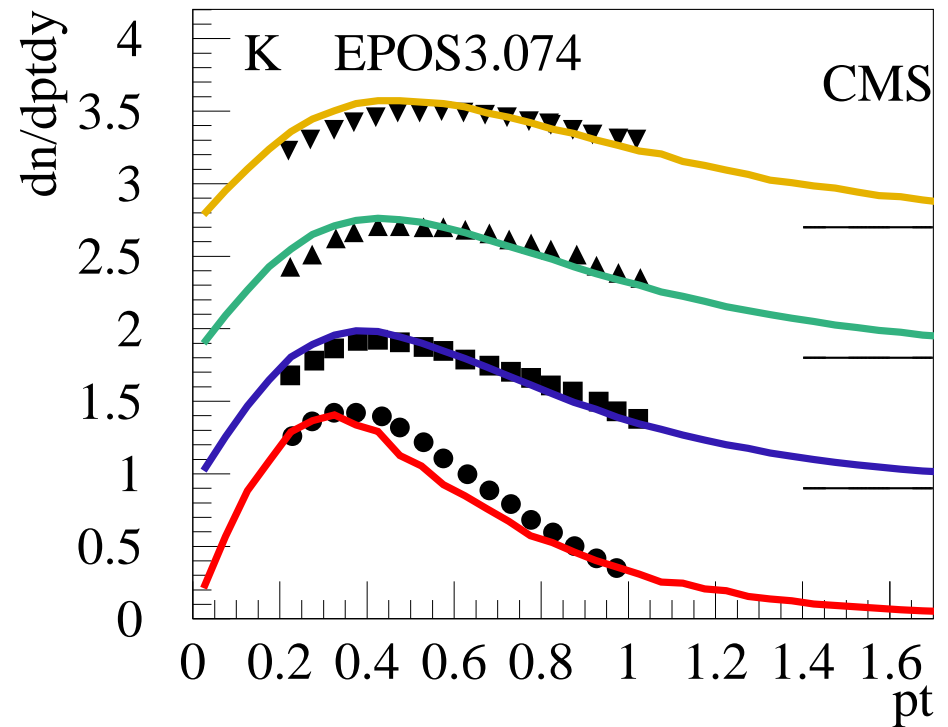
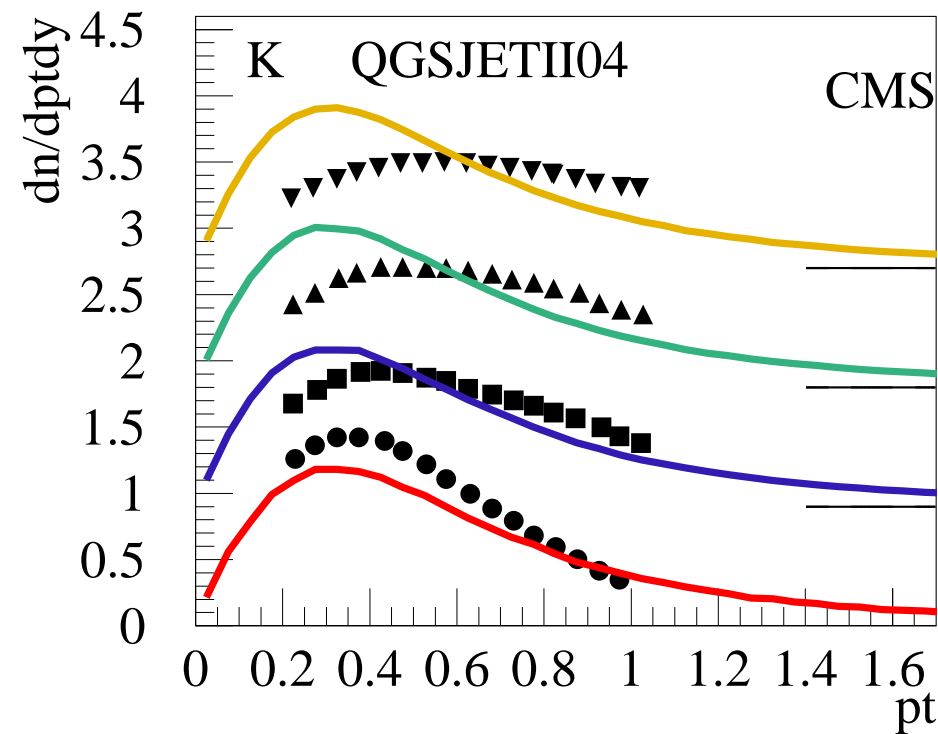
$\langle N_{\text{tracks}} \rangle = 8, 84, 160, 235$ , from bottom to top, curves shifted by 0.9  
 spectra normalized to unity, lines = theory



**Little change with  $\langle N_{\text{tracks}} \rangle$  for pions**

## Kaons

$\langle N_{\text{tracks}} \rangle = 8, 84, 160, 235$ , from bottom to top, curves shifted by 0.9  
 spectra normalized to unity, lines = theory

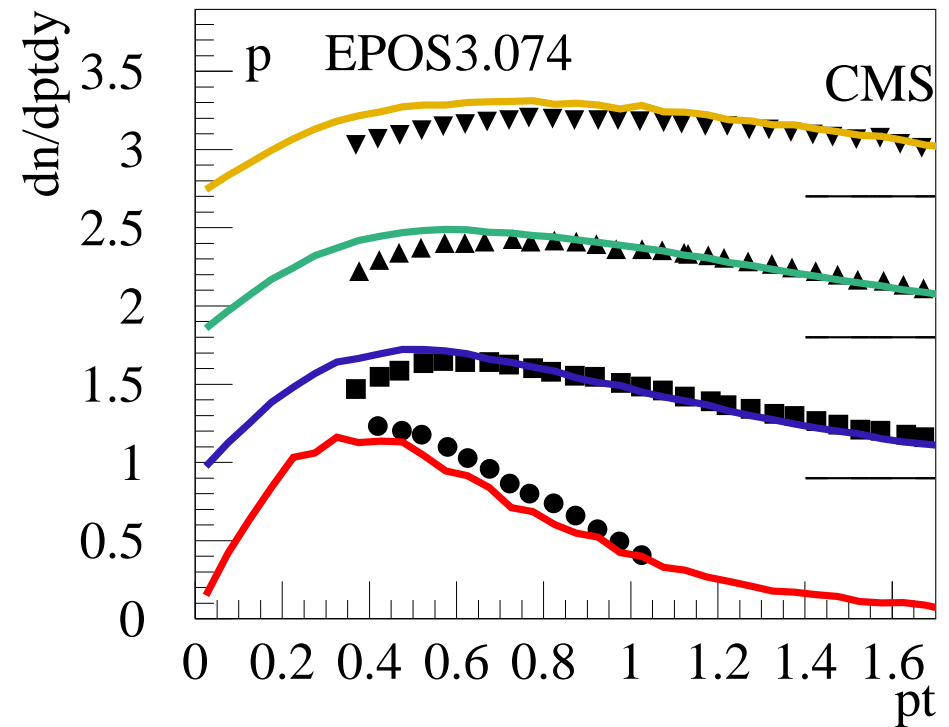
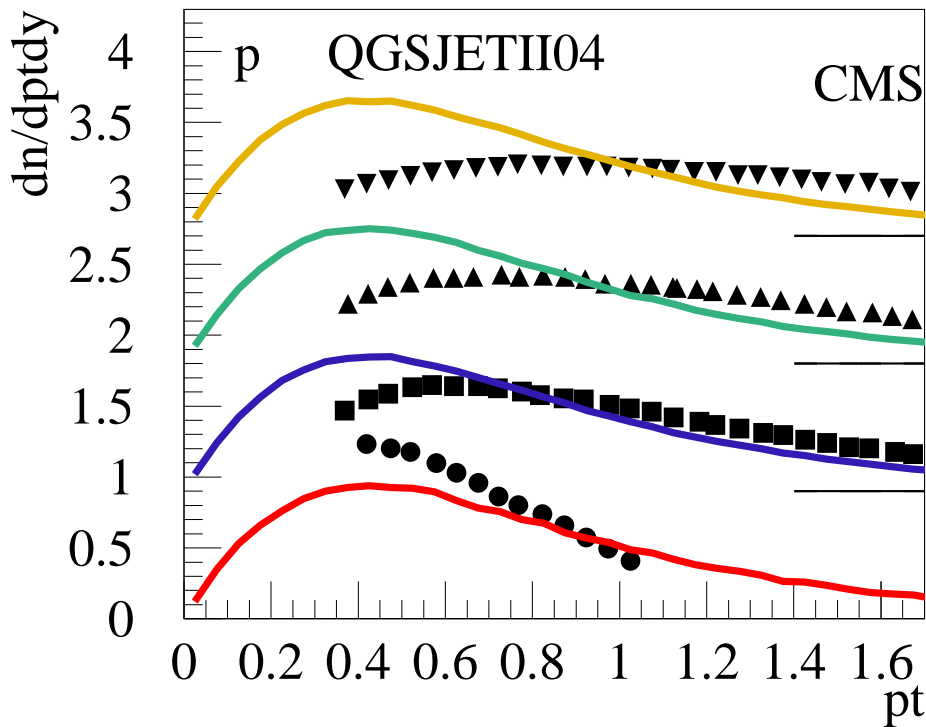


**Kaon spectra change significantly with  $\langle N_{\text{tracks}} \rangle$**

**in EPOS3: more and more flow contribution**

## Protons

$\langle N_{\text{tracks}} \rangle = 8, 84, 160, 235$ , from bottom to top, curves shifted by 0.9  
 spectra normalized to unity, lines = theory



**Strong variation of proton spectra**

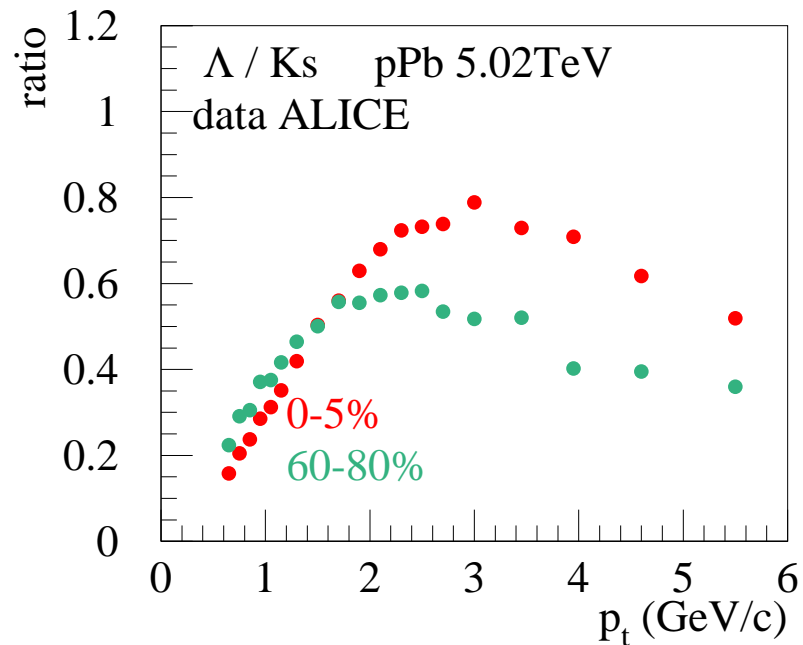
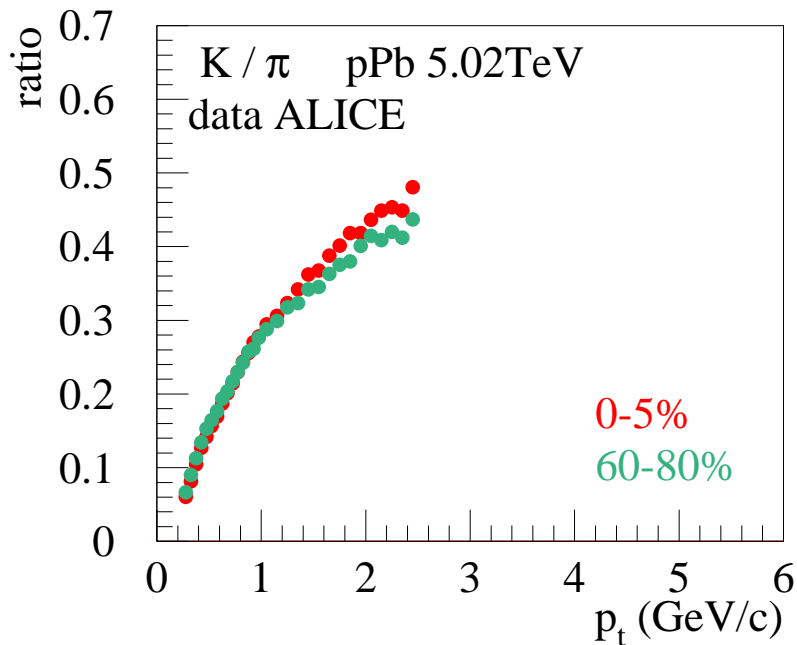
**=> flow helps**

**ALICE: compare pt spectra for identified particles in different multiplicity classes: 0-5%,...,60-80%**

(in  $2.8 < \eta_{lab} < 5.1$ )

R. Preghenella, ALICE, talk Trento workshop 2013

**Useful : ratios (K/pi, p/pi...)**

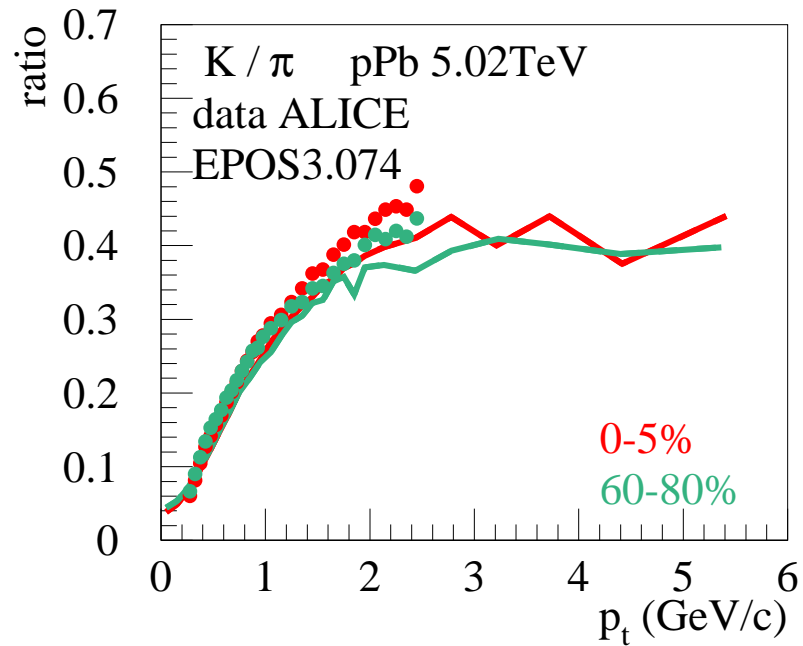
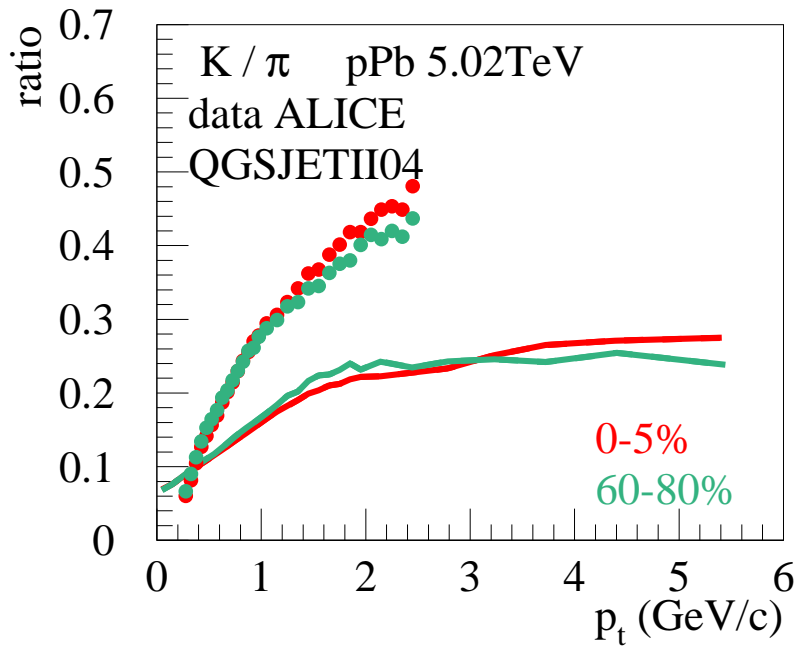


**Significant variation of lambda/K – like in PbPb**

$$K/\pi$$

**High multiplicity (0-5%, red),**  
**low multiplicity (60-80%, green)**

lines = theory  
 points = data



**No multiplicity dependence**

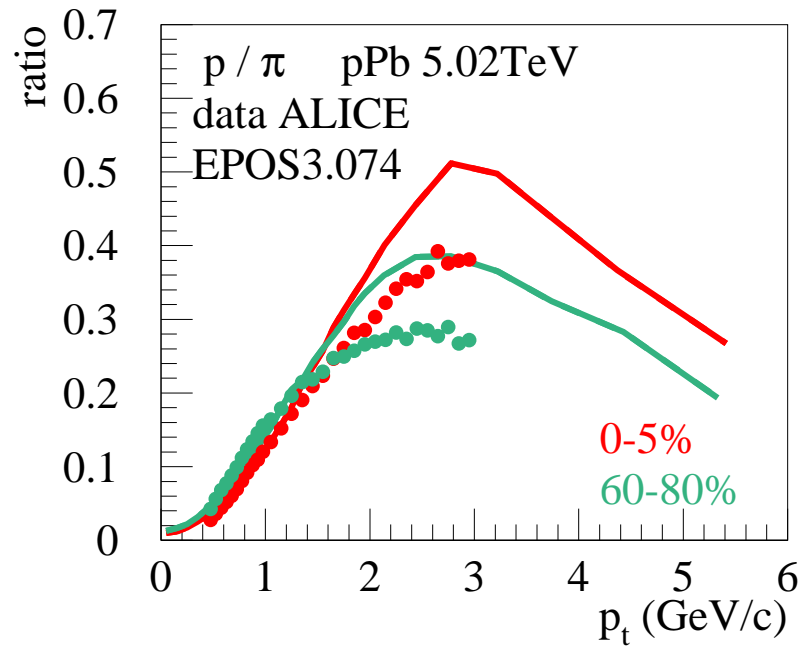
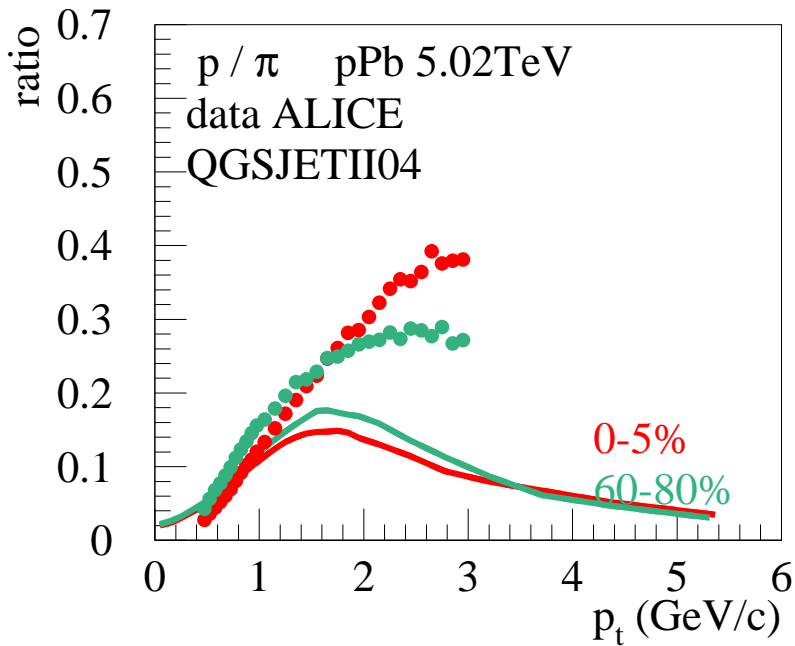
**not trivial to get the peripheral right !!**



$$p/\pi$$

**High multiplicity (0-5%, red),**  
**low multiplicity (60-80%, green)**

lines = theory  
 points = data



**Significant multiplicity dependence**

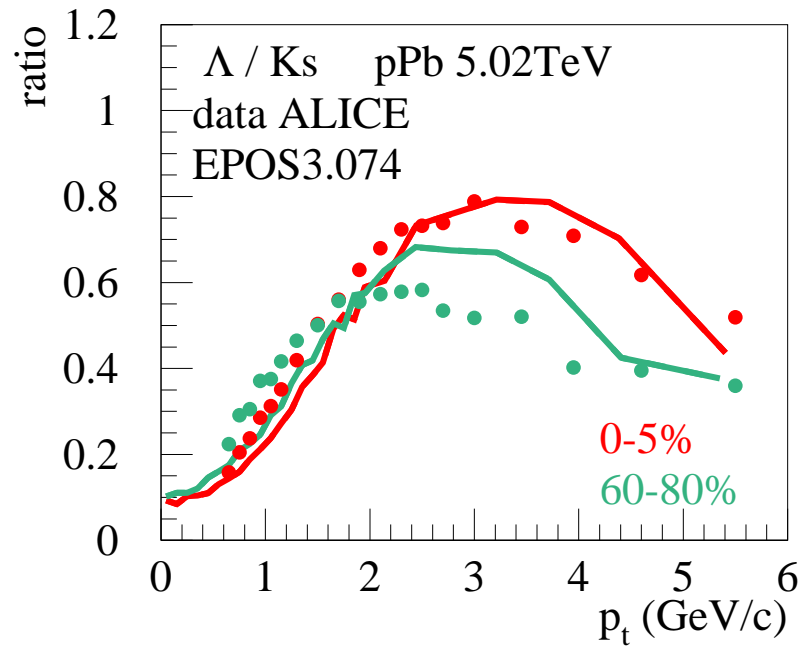
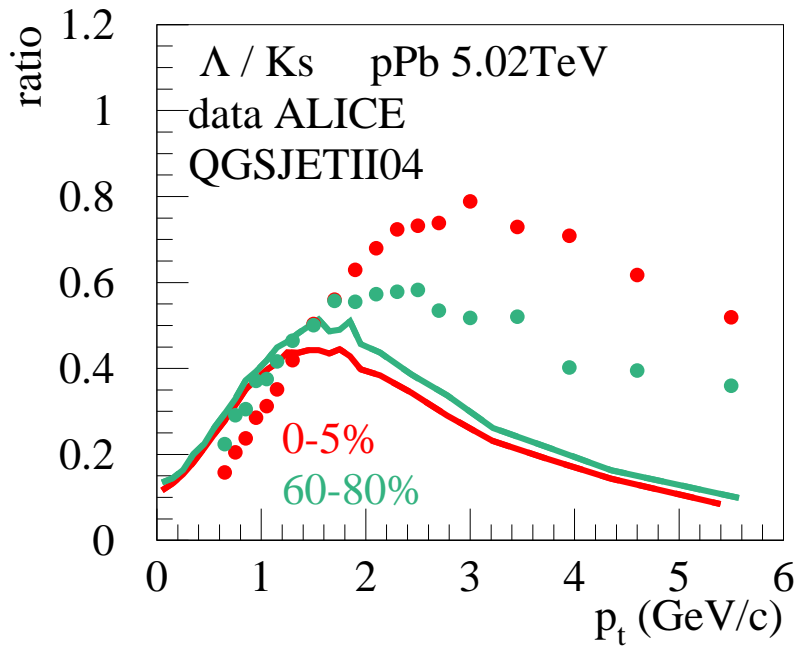
**in EPOS, flow already affects the low multiplicity case**

**”flow peak” around 2-3 GeV/c,  
 beyond 5GeV/c corona (minjets) dominate**

$$\Lambda / K_s$$

**High multiplicity (0-5%, red),**  
**low multiplicity (60-80%, green)**

lines = theory  
 points = data



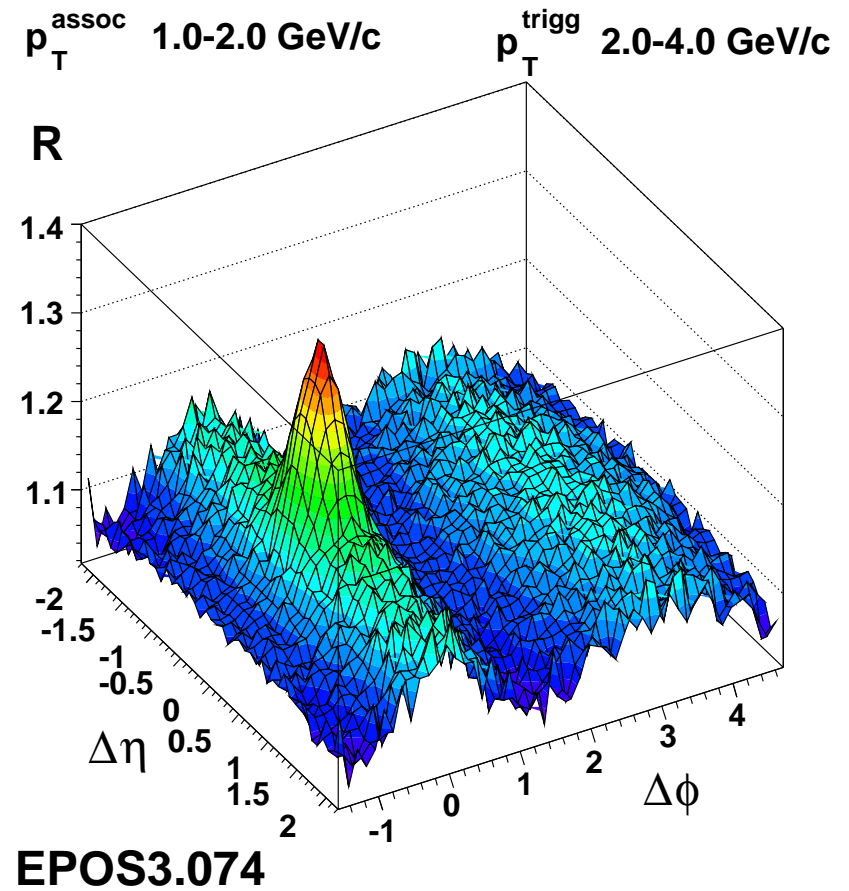
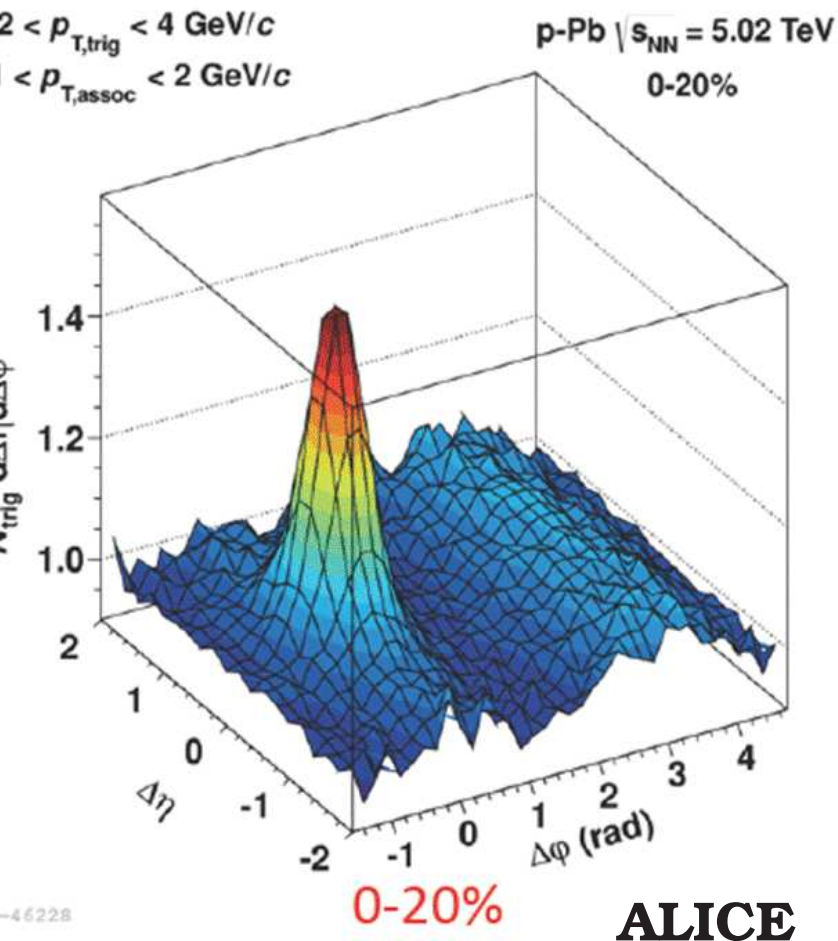
**Significant multiplicity dependence**

**again, flow already needed for low multiplicity (even in pp!)**

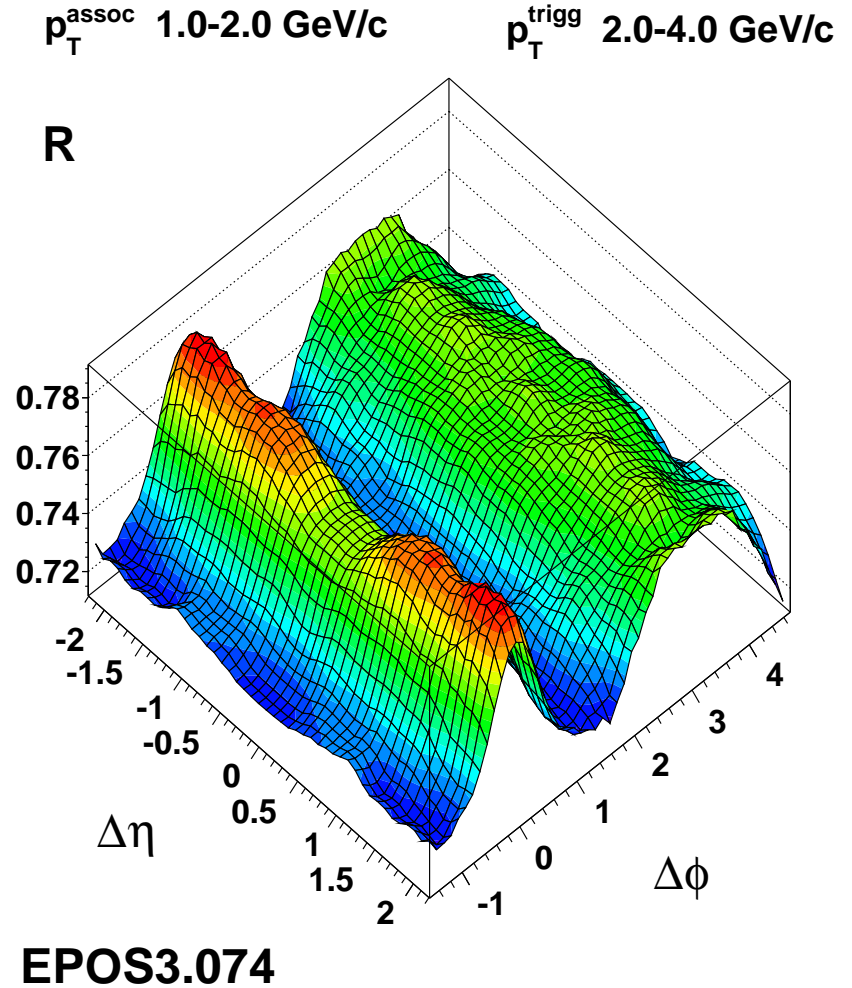
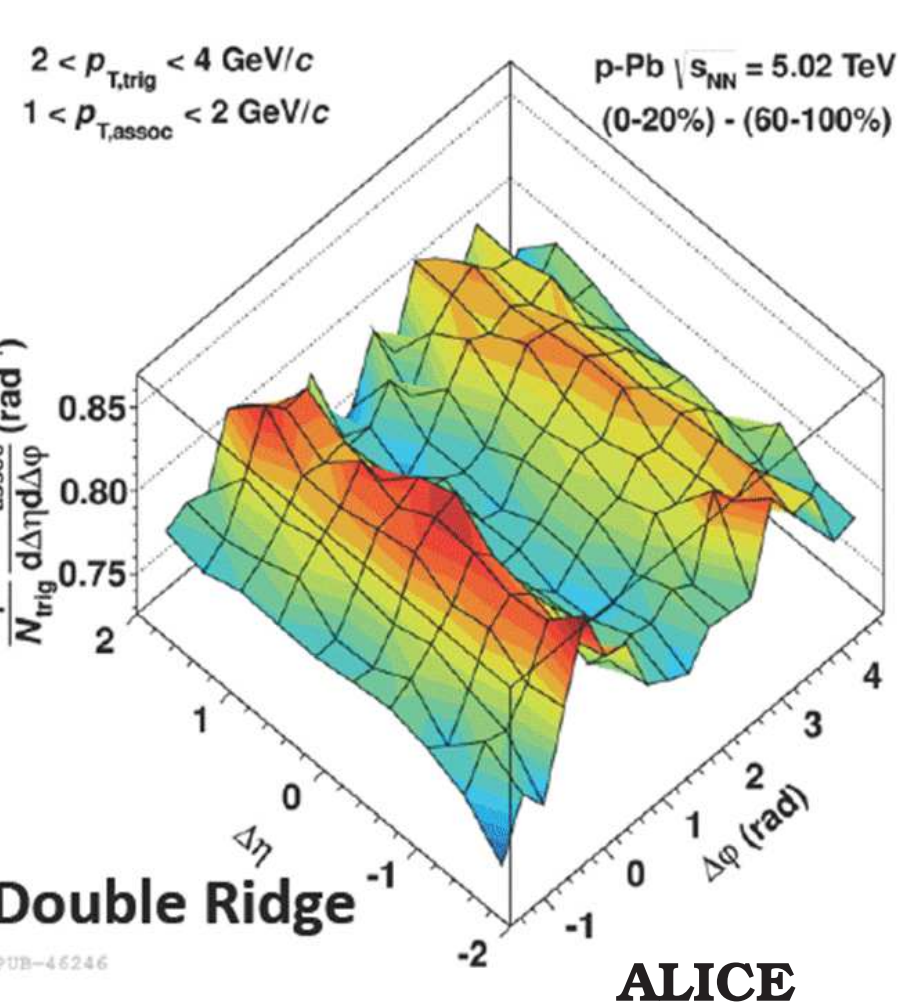
**flow dominates 2-5 GeV/c**

# “Ridges” in pA

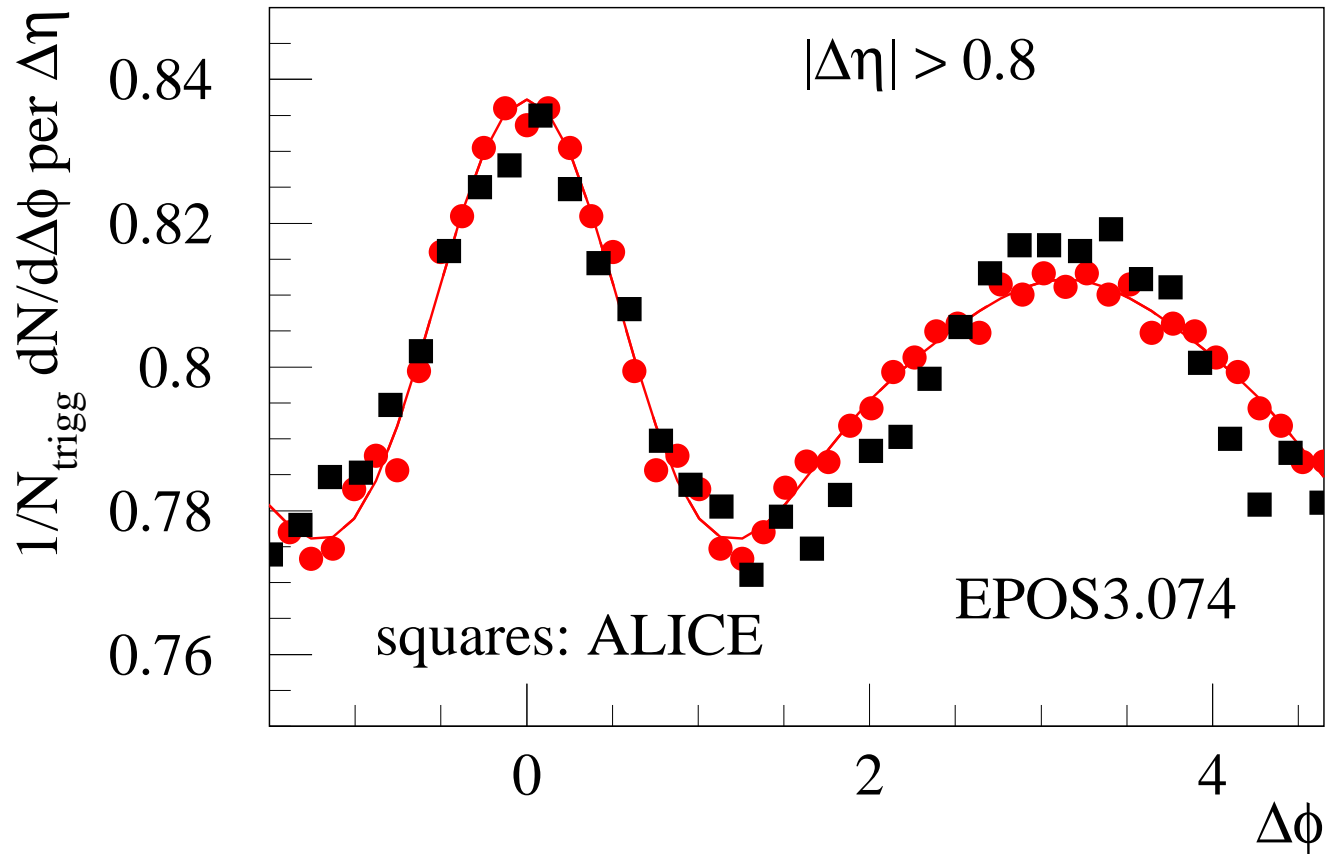
ALICE, arXiv:1212.2001, arXiv:1307.3237



# Central - peripheral (to get rid of jets)



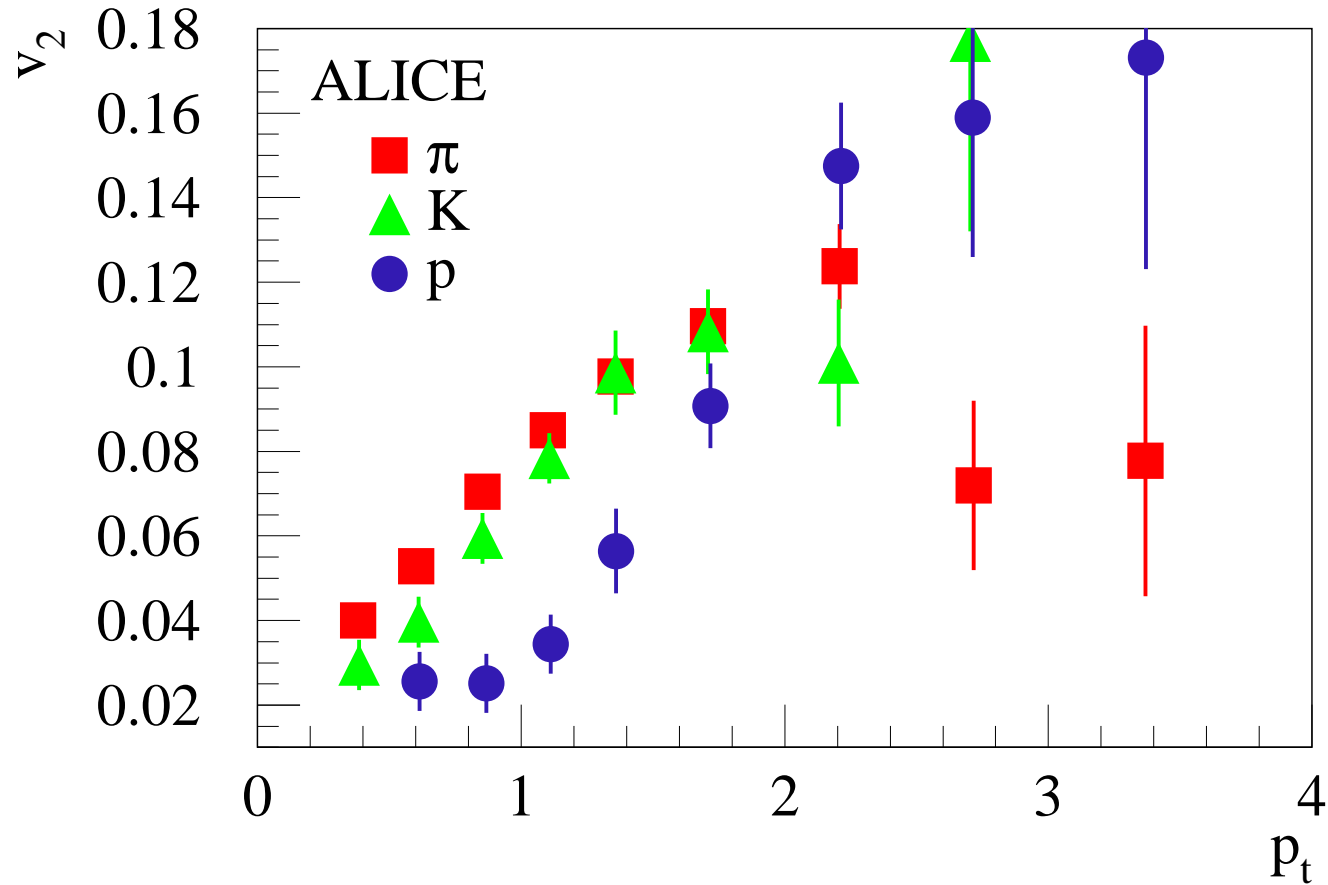
# Projection



red line :  $\sum 2a_n \cos(n\Delta\phi);$

$$\implies v_n = \sqrt{\frac{a_n}{b}}$$

# Identified particle $v_2$



**mass splitting, as in PbPb !!!**

# pPb in EPOS3

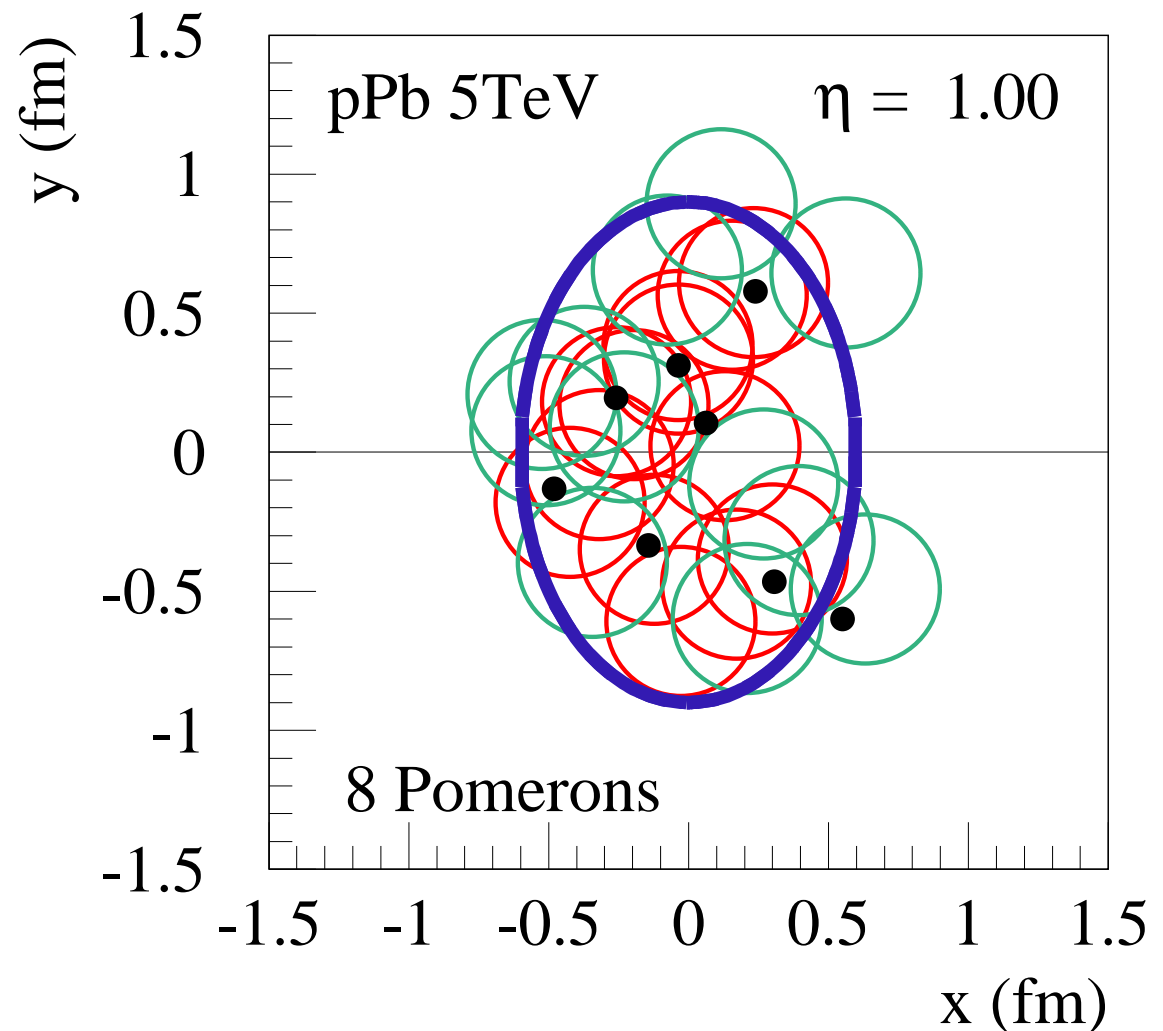
**Pomerons (number and positions) characterize geometry (P. number  $\propto$  multiplicity)**

**random azimuthal asymmetry**

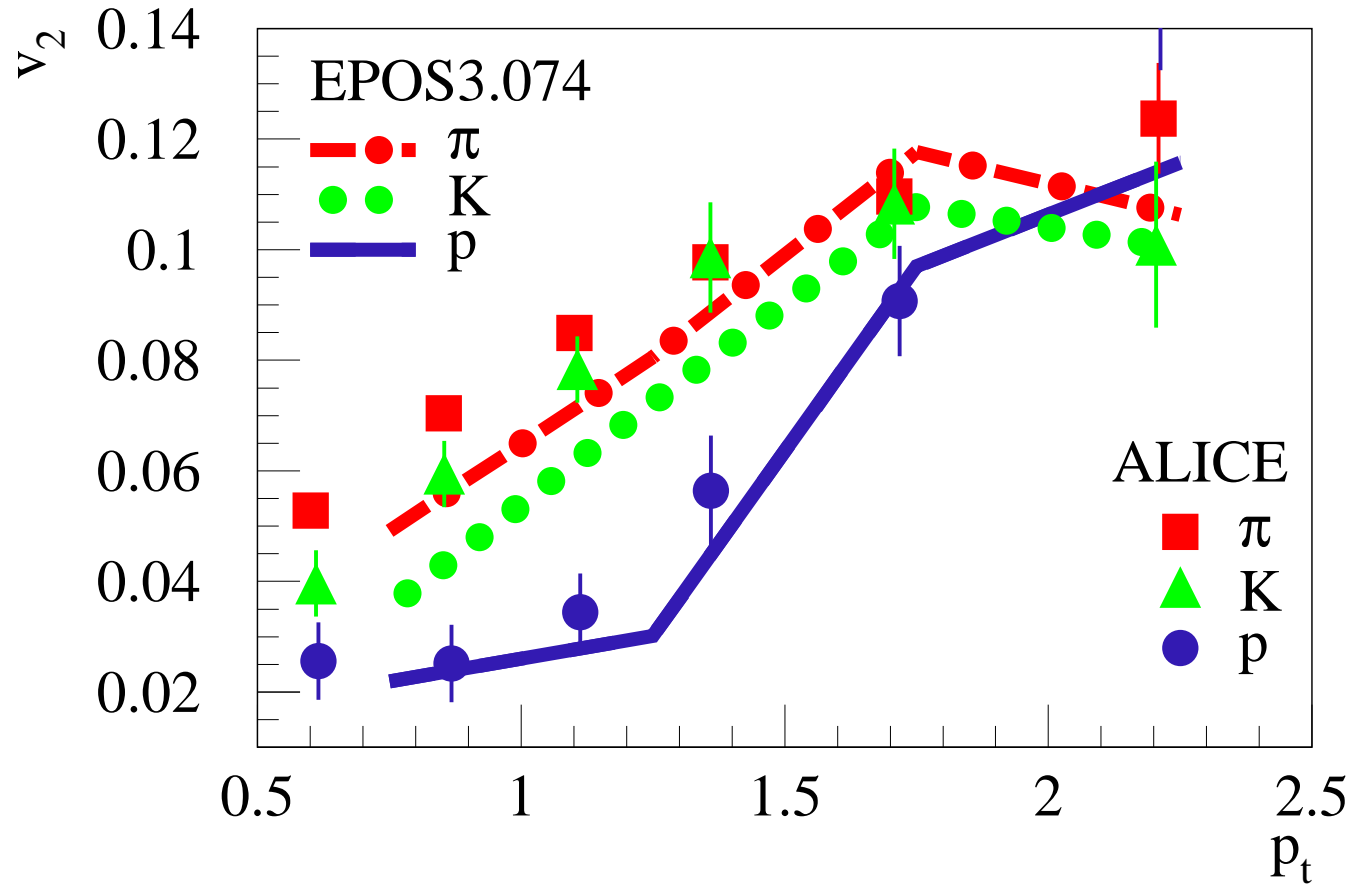
=>

**asymmetric flow seen at higher pt for heavier ptls**

**Robust results**



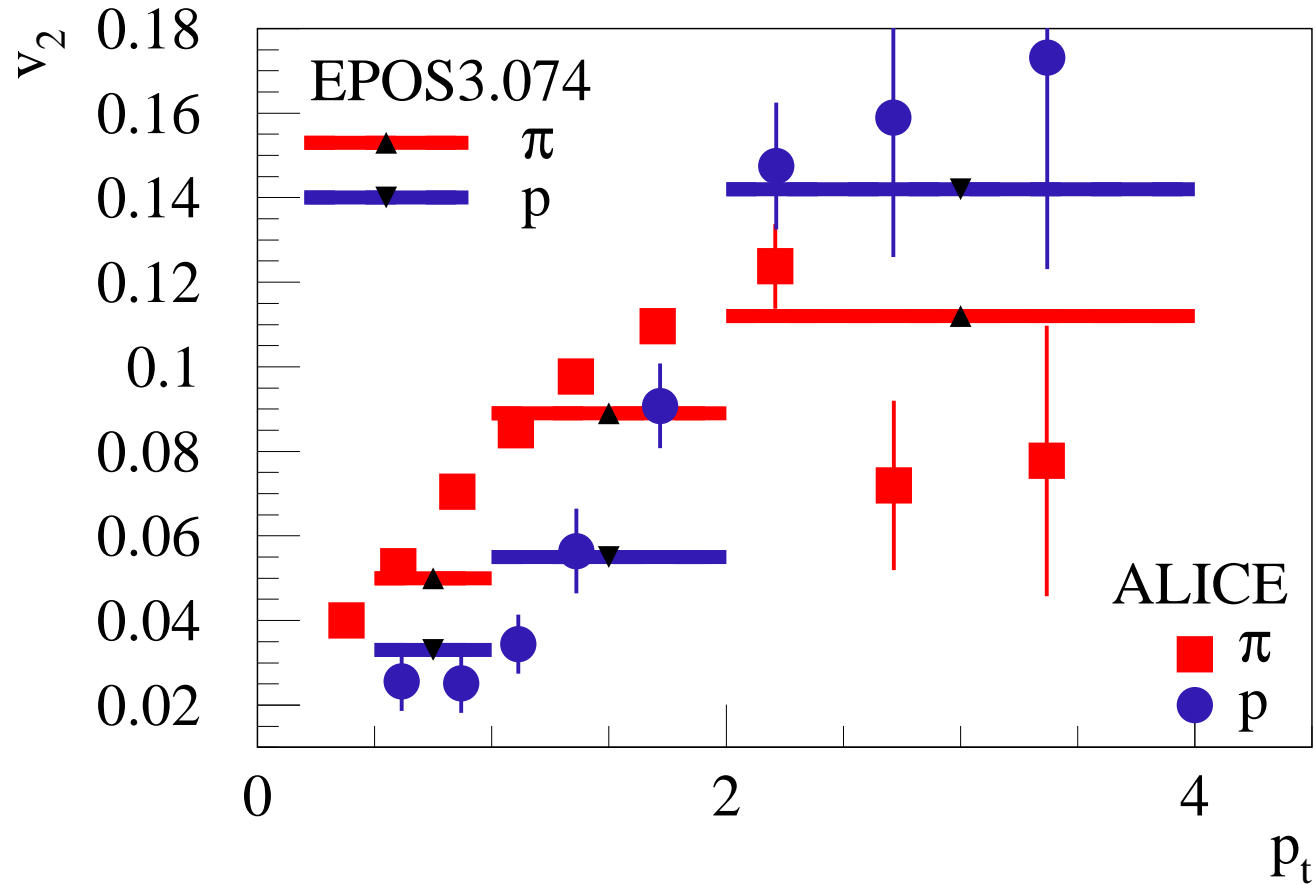
# $v_2$ for $\pi$ , K, p clearly differ



**mass splitting, due to flow**



# different binning:

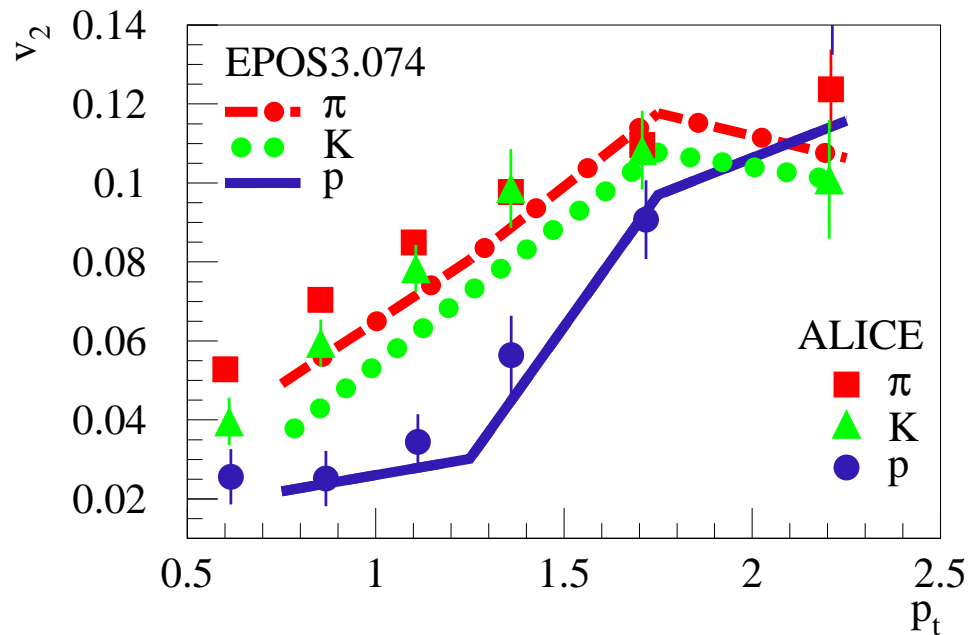


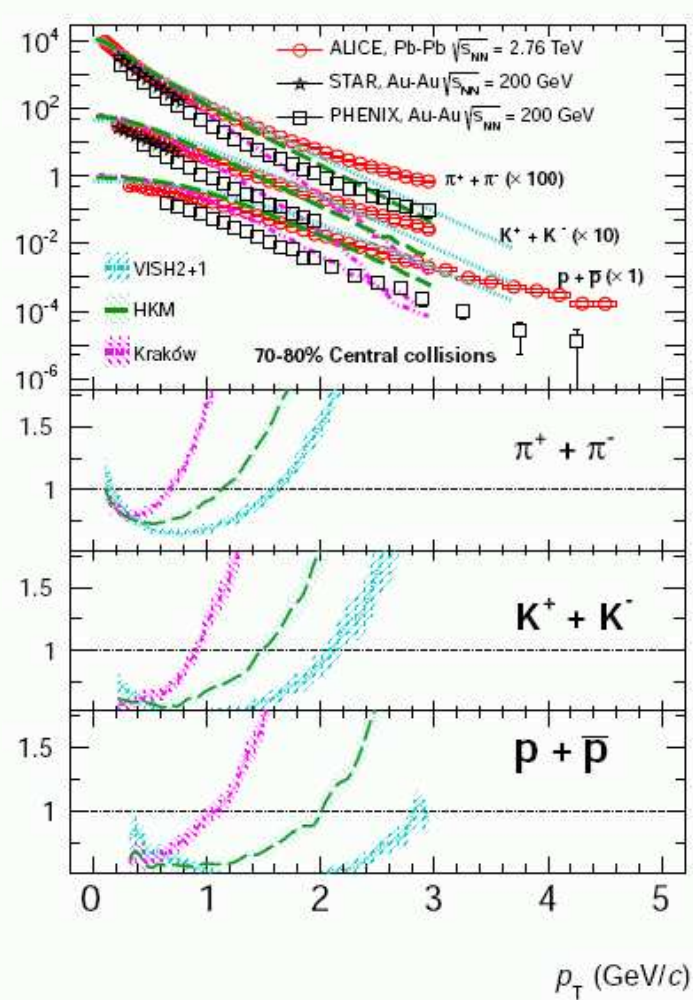
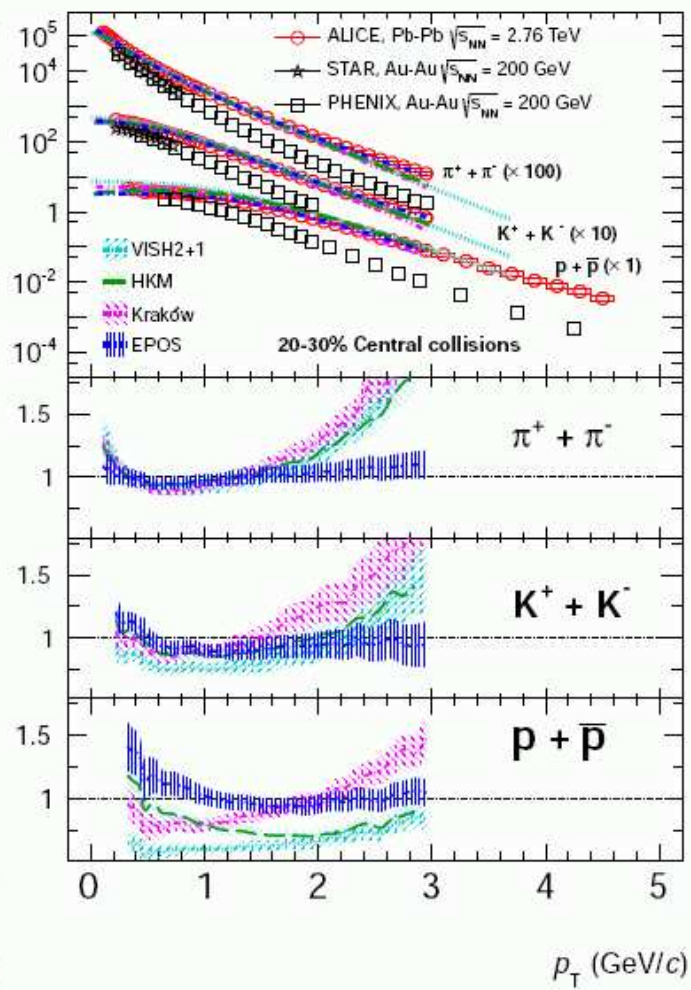
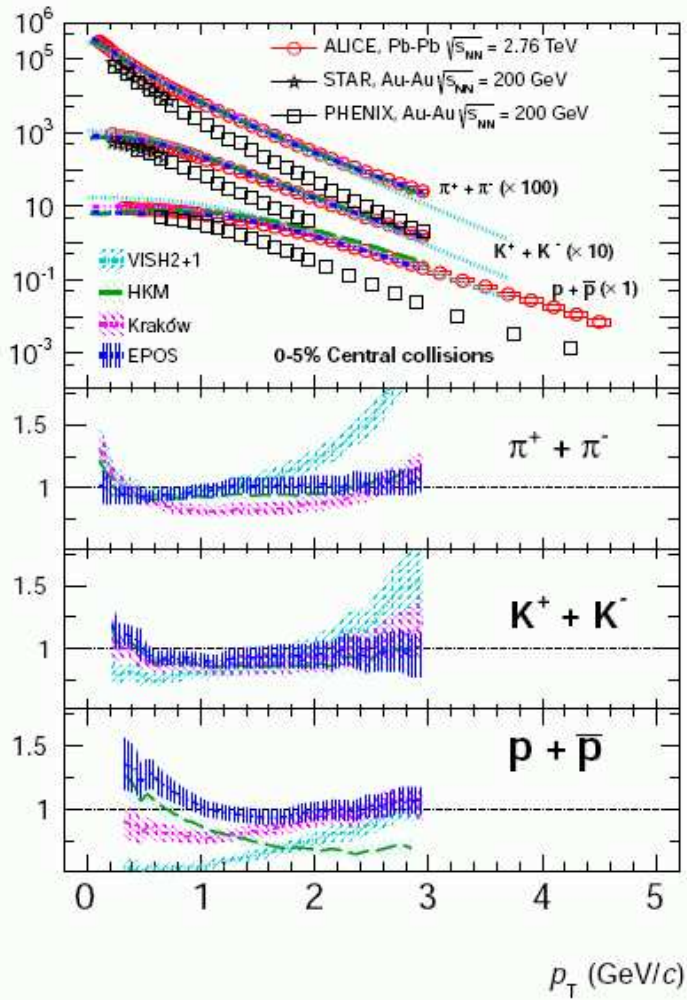
**$v_2(\text{protons}) > v_2(\text{pions})$  beyond 2GeV**

# Summary

## Analyzing $p_t$ -spectra, ratios, and dihadrons correlations for identified hadrons:

- **pPb looks very much like a hydrodynamically expanding system**  
(more clean than PbPb, where hydro and minijets heavily interact, as well as the final hadrons among themselves)





ALICE arXiv:1303.0737