

Semi-Annihilating Scalar Dark Matter

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2 \mathbb{Z}_2 and Beyond

- Why is WIMP dark matter stable?
- The simplest symmetry – parity \mathbb{Z}_2
- But also possible: $\mathbb{Z}_3, \mathbb{Z}_4, \dots$

3 New Phenomena for \mathbb{Z}_N , $N > 2$

For several species of dark matter χ_i :

- **Semi-annihilation** $\chi_i \chi_j \rightarrow \chi_k X$,
d'Eramo & Thaler 1003.5912,
Hambye 0811.0172,
Hambye & Tytgat 0907.1007
- **Dark matter conversion** $\chi_2 \chi_2 \leftrightarrow \chi_1 \chi_1$
Liu, Wu & Zhou 1101.4148, Bélanger & Park 1112.4491,
Adulpravitchai, Batell & Pradler 1103.3053

4 \mathbb{Z}_N Symmetries

Field φ with charge X_φ transforms under \mathbb{Z}_N as

$$\varphi \rightarrow e^{i\frac{X_\varphi}{N}2\pi} \varphi$$

- Addition modulo N
- Discrete charges $X = 0, 1, \dots, N - 1$

5 \mathbb{Z}_N Symmetries

- $SO(10) \supset U(1)_X \rightarrow \mathbb{Z}_N$ by a GUT Higgs with $X = N$
- Different assignments of charges can give the same low energy potential
- Limited number of Lagrangian terms due to renormalisability
- For higher N , the $U(1)_X$ symmetric part plus one or two terms

6 Scalar Dark Matter

- Scalars – simplest dark matter
- May be seen via the Higgs portal
- New scalars can improve vacuum stability of the SM Higgs potential

7 Simplest Scalar Dark Matter

- Standard Model Higgs H
- Singlet S
- $\langle H \rangle = \frac{v}{\sqrt{2}}, \langle S \rangle = 0$

8 \mathbb{Z}_3 Invariant Potential

$$V_{\mathbb{Z}_3} = \mu_H^2 |H|^2 + \lambda_H |H|^4 + \mu_S^2 |S|^2 + \lambda_S |S|^4 \\ + \lambda_{SH} |S|^2 |H|^2 + \frac{\mu_3}{2} (S^3 + S^{\dagger 3})$$

with $X_H = 0, X_S = 1$

Bélanger, K. K., Pukhov, Raidal, 1211.1014

Ma, 0708.3371

8 \mathbb{Z}_3 Invariant Potential

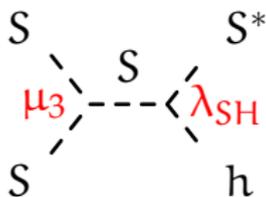
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Semi-annihilation



9 Bound on μ_3

Too large μ_3 would break \mathbb{Z}_3 , yielding the bound

$$\max \mu_3 \approx 2\sqrt{2} \sqrt{\frac{\lambda_S}{\delta}} M_S,$$

where $0 \leq \delta \leq 2$

- $\delta = 2$ gives absolute stability
- $\delta < 2$ gives metastability

Adams, hep-ph/9302321

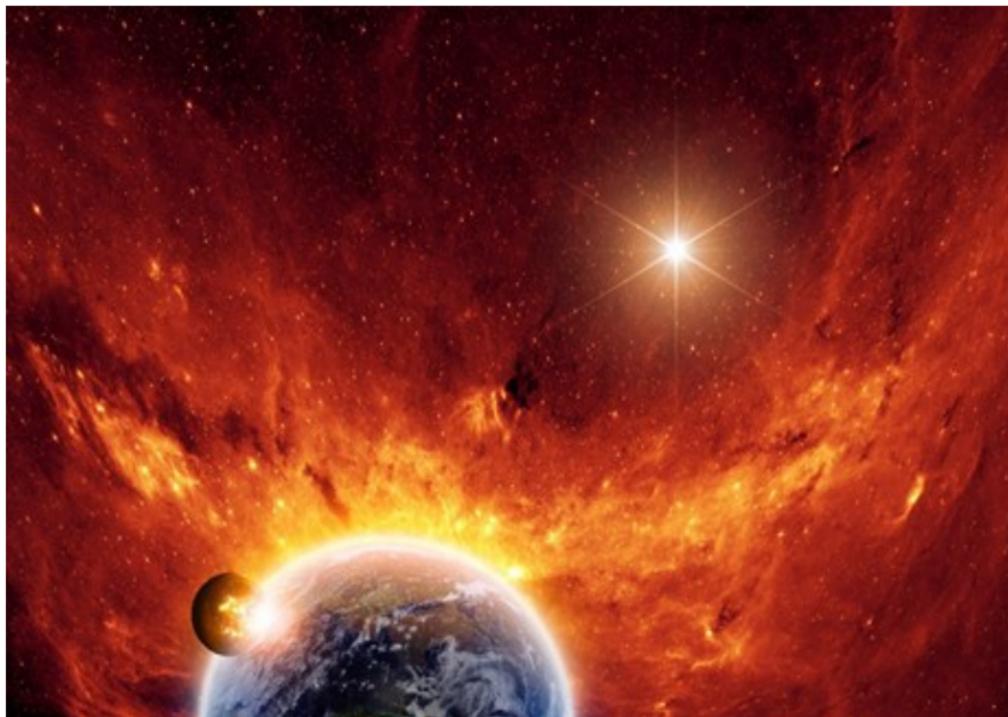
Higgs boson hints at vacuum bubble apocalypse

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Wed, 20 Feb 2013 1:21p.m.



The calculation rests on the mass of the particle believed to be the Higgs boson
(file pic)

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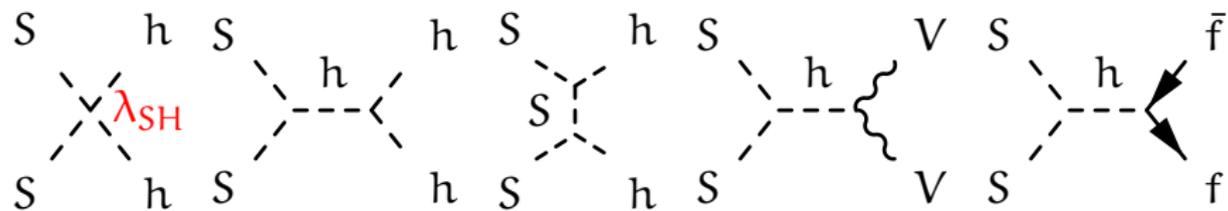
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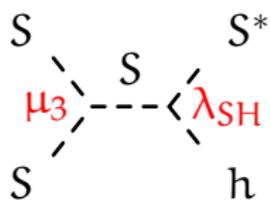
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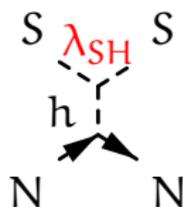
11 Relic Density & Direct Detection



Annihilation



Semi-annihilation



Direct detection

12 Relic Density

$$\begin{aligned}\frac{dn}{dt} &= -v\sigma^{SS^* \rightarrow XX} (n^2 - \bar{n}^2) \\ &\quad - \frac{1}{2}v\sigma^{SS \rightarrow S^*X} (n^2 - n\bar{n}) - 3Hn\end{aligned}$$

- Fraction of semi-annihilation

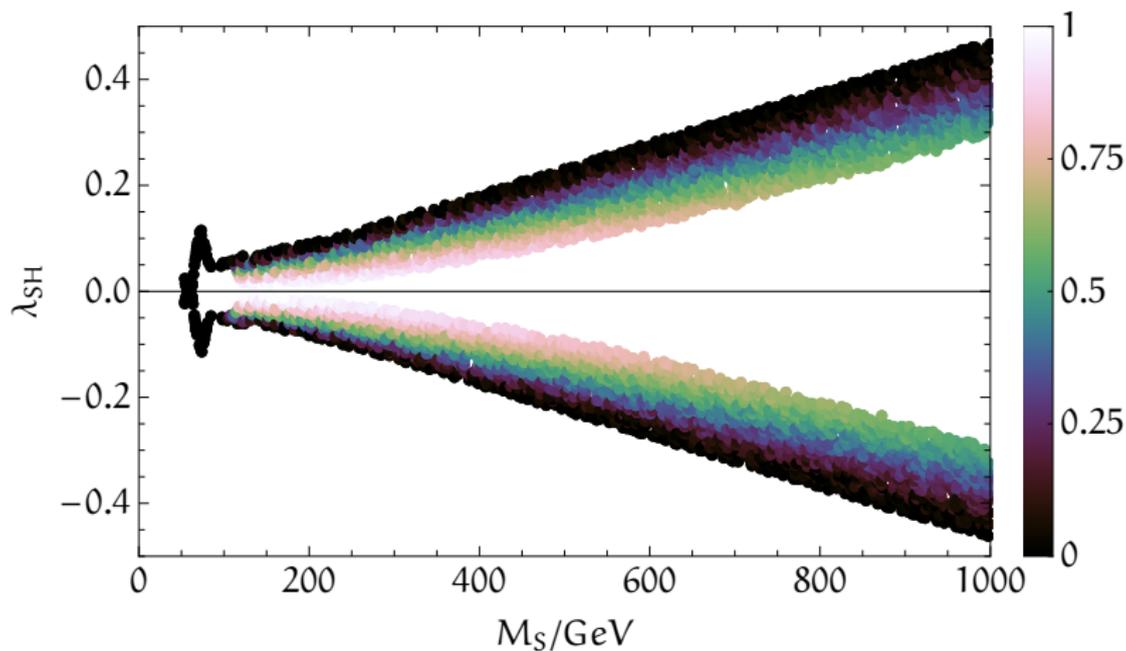
$$\alpha = \frac{1}{2} \frac{v\sigma^{SS \rightarrow S^*X}}{v\sigma^{SS^* \rightarrow XX} + \frac{1}{2}v\sigma^{SS \rightarrow S^*X}}$$

13 Parameter Space

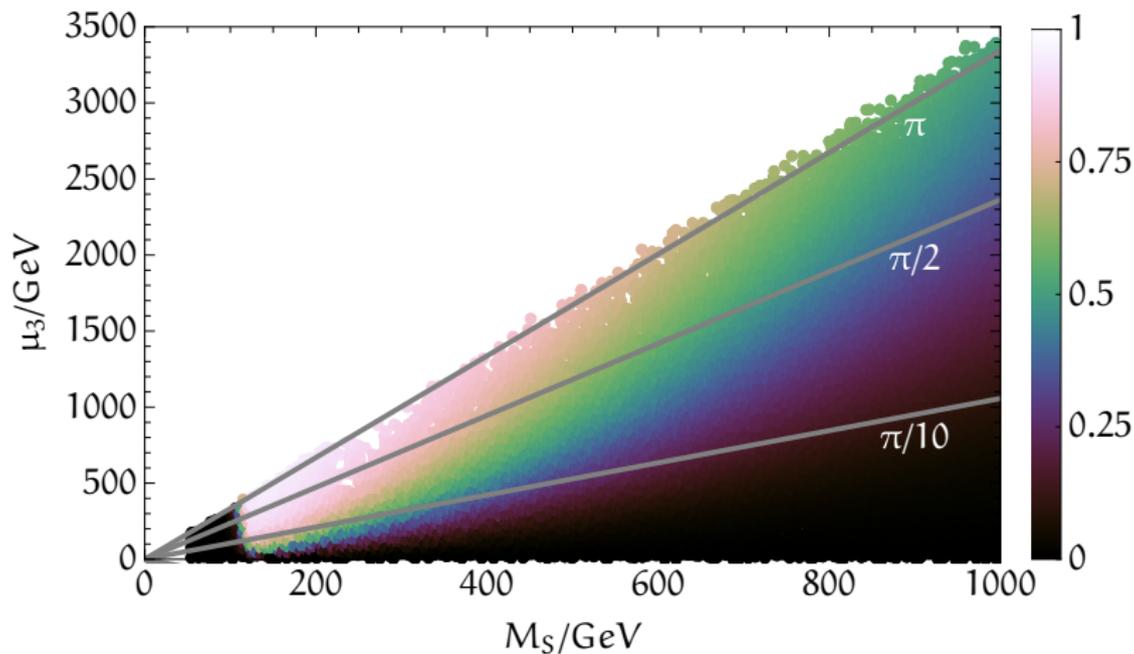
- $1 \text{ GeV} \leq M_S \leq 1000 \text{ GeV}$
- $0 \text{ GeV} \leq \mu_3 \leq 4000 \text{ GeV}$
- $0 \leq \lambda_S \leq \pi$
- $-2\pi \leq \lambda_{SH} \leq 2\pi$
- The WMAP 3σ range

$$\Omega h^2 = 0.1009 \pm 0.0056$$

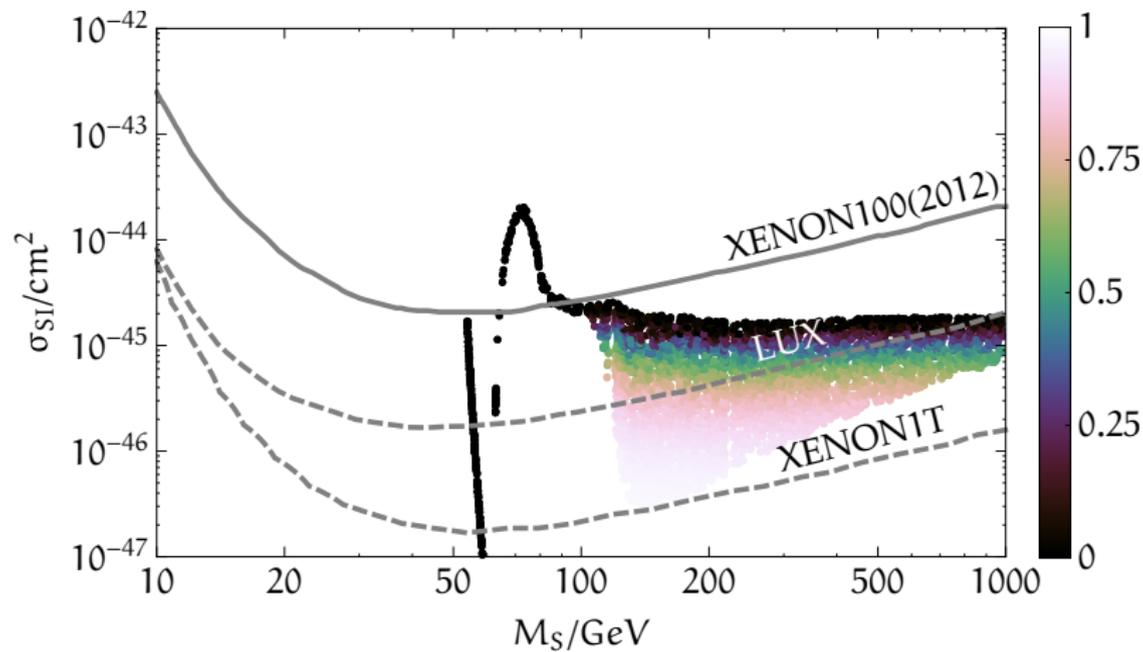
14 $|S|^2|H|^2$ Coupling λ_{SH} vs. M_S



15 Cubic Coupling μ_3 vs. M_S



16 Direct Detection



17 Scale of New Physics

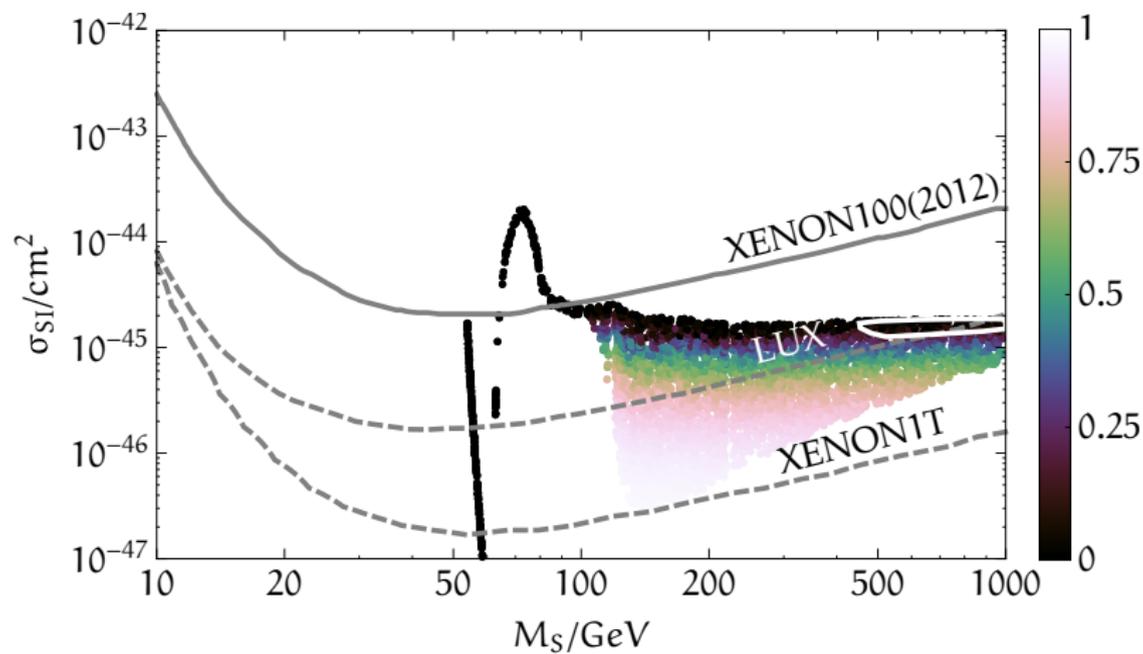
What is the scale of validity from

- perturbativity,
- vacuum stability?

In RGE running to higher energies,

- $\lambda_{SH} > 0$ stabilises the scalar potential
- Large λ_S blows up perturbativity

18 Direct Detection



19 \mathbb{Z}_3 Singlet & Inert Doublet

- Standard Model Higgs H_1
- Inert doublet H_2
- Complex singlet S
- S and H_2^0 mix into $x_1 \approx S$ and $x_2 \approx H_2^0$
with $M_{x_1} < M_{x_2}$

20 \mathbb{Z}_3 Invariant Potential

Quartic semi-annihilation coupling

$$V_{\mathbb{Z}_3} \supset \frac{\lambda_{S12}}{2} (S^2 H_1^\dagger H_2 + S^{\dagger 2} H_2^\dagger H_1)$$

21 \mathbb{Z}_3 Processes

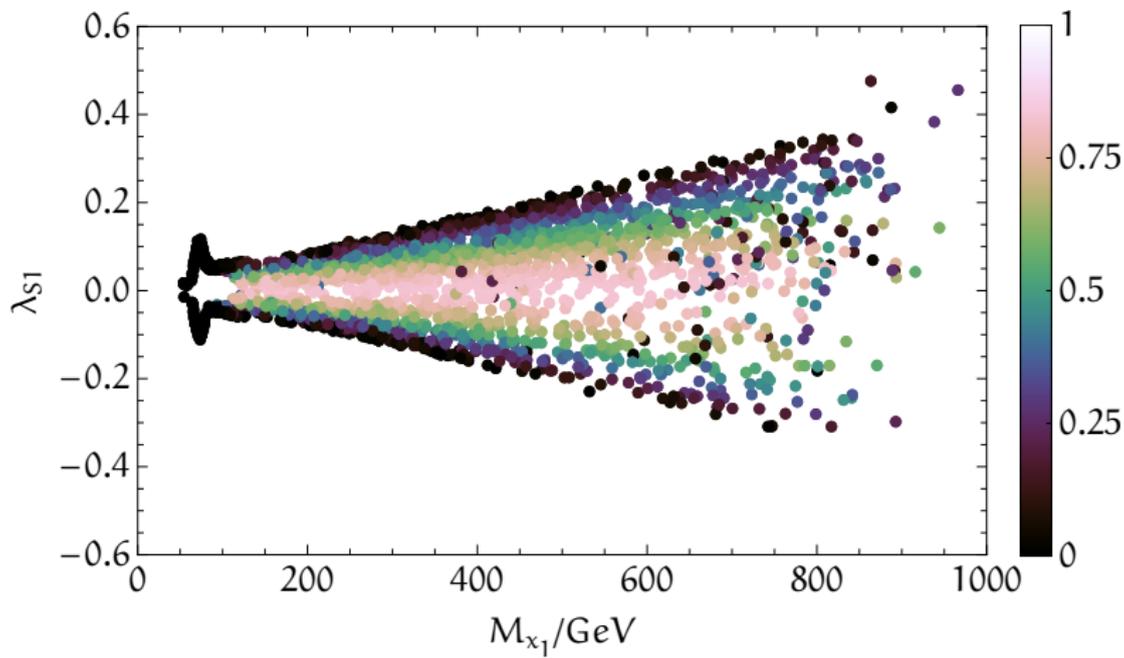
Annihilation

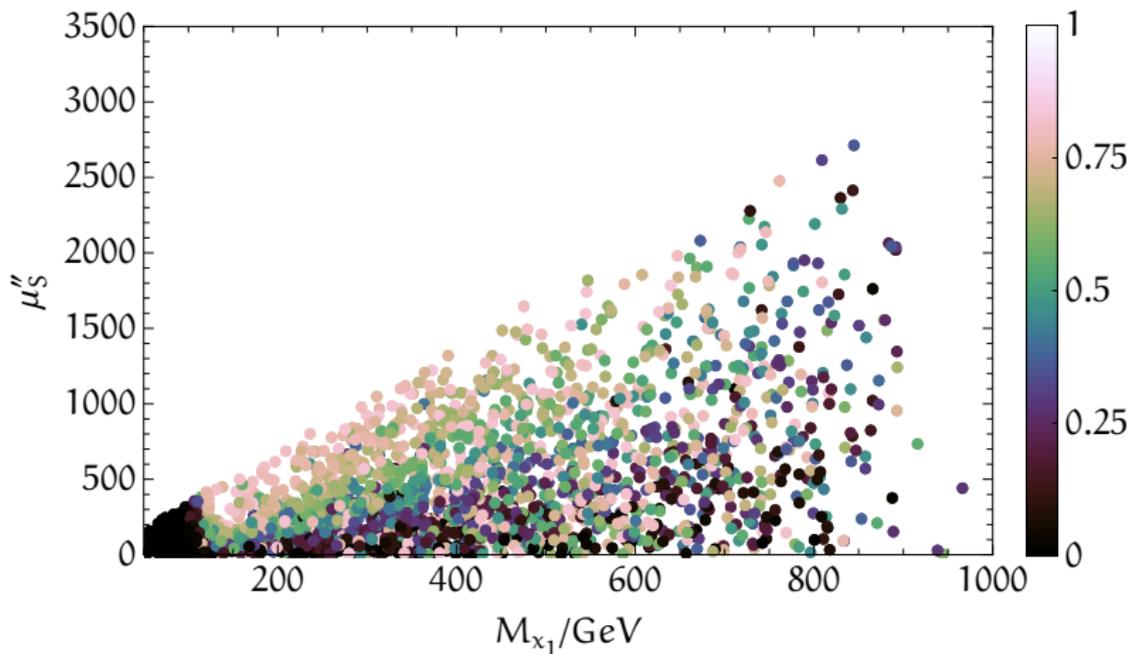
$$x_1 x_1^* \rightarrow \emptyset$$

Semi-annihilation

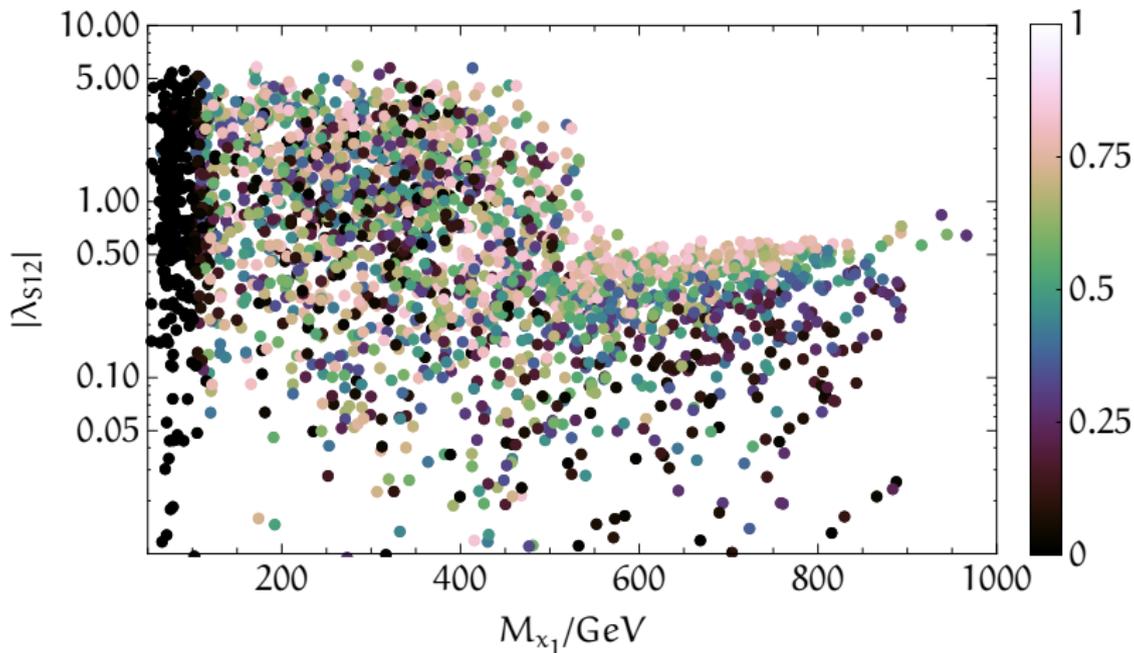
$$x_1 x_1 \rightarrow x_2 \emptyset$$

22 $|S|^2|H_1|^2$ Coupling λ_{S1} vs. M_{χ_1}

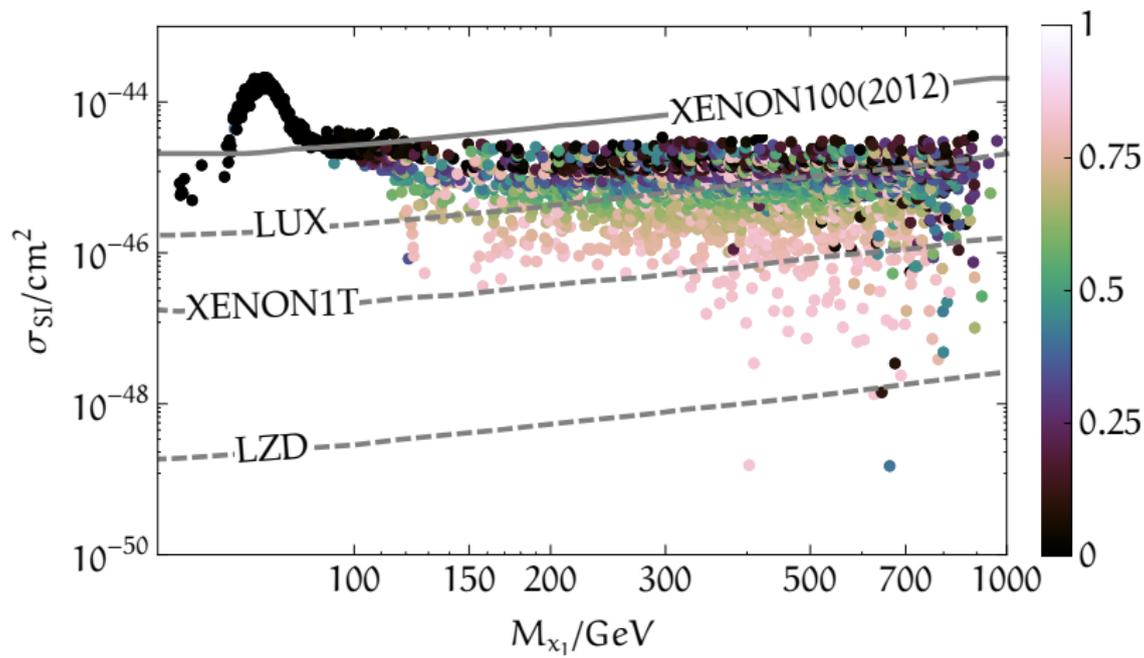


Cubic Coupling μ_S'' vs. M_{x_1} 

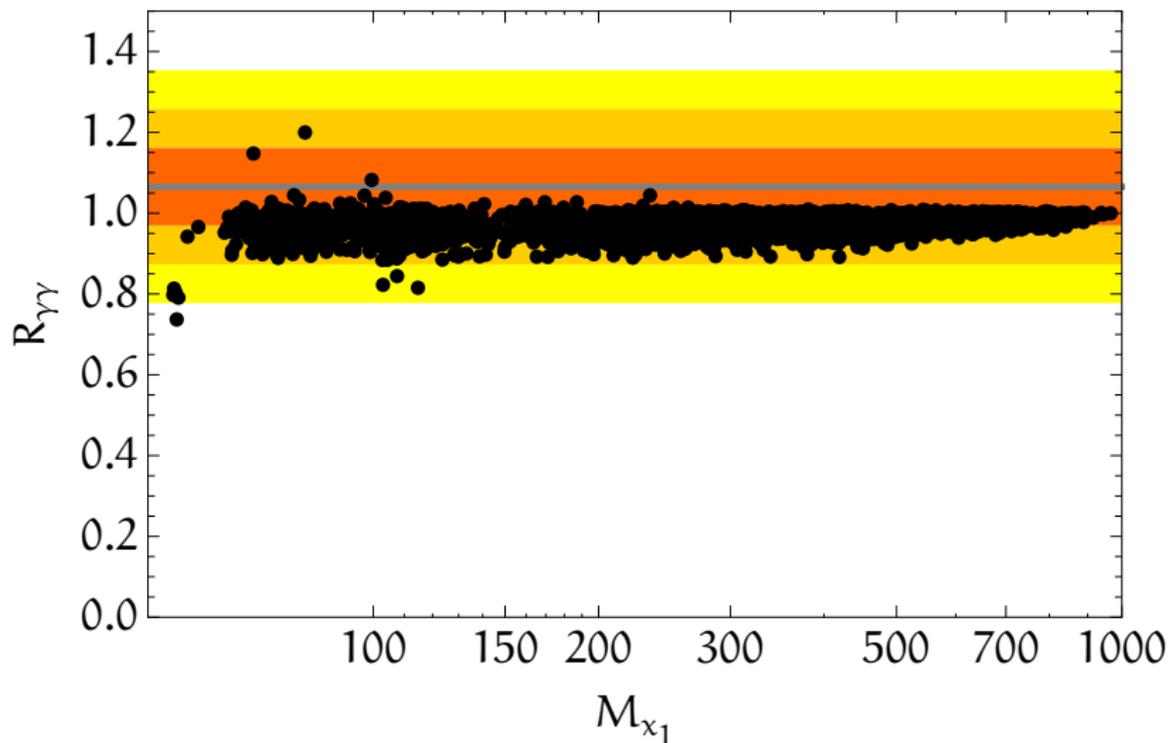
24 $\lambda_{S12} S^2 H_1^\dagger H_2$ Coupling *vs.* M_{x_1}



25 Direct Detection



26 $h \rightarrow \gamma\gamma$ at LHC



27 Conclusions

- *The simplest model with semi-annihilation:*
 \mathbb{Z}_3 scalar singlet dark matter
- Semi-annihilation yields lower σ_{SI} for a given Ω
- Large semi-annihilation needs TeV-scale new physics
- Models with H_1, H_2, S have quartic semi-annihilation terms for $\mathbb{Z}_N, N > 2$
- Work in progress:
 \mathbb{Z}_4 model with two-component DM