

# Study of leptonic and semileptonic kaon decays at CERN

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on behalf of the NA48 and NA62 Collaborations

EPS HEP 2013

Stockholm, July 18<sup>th</sup>, 2013

# Outline

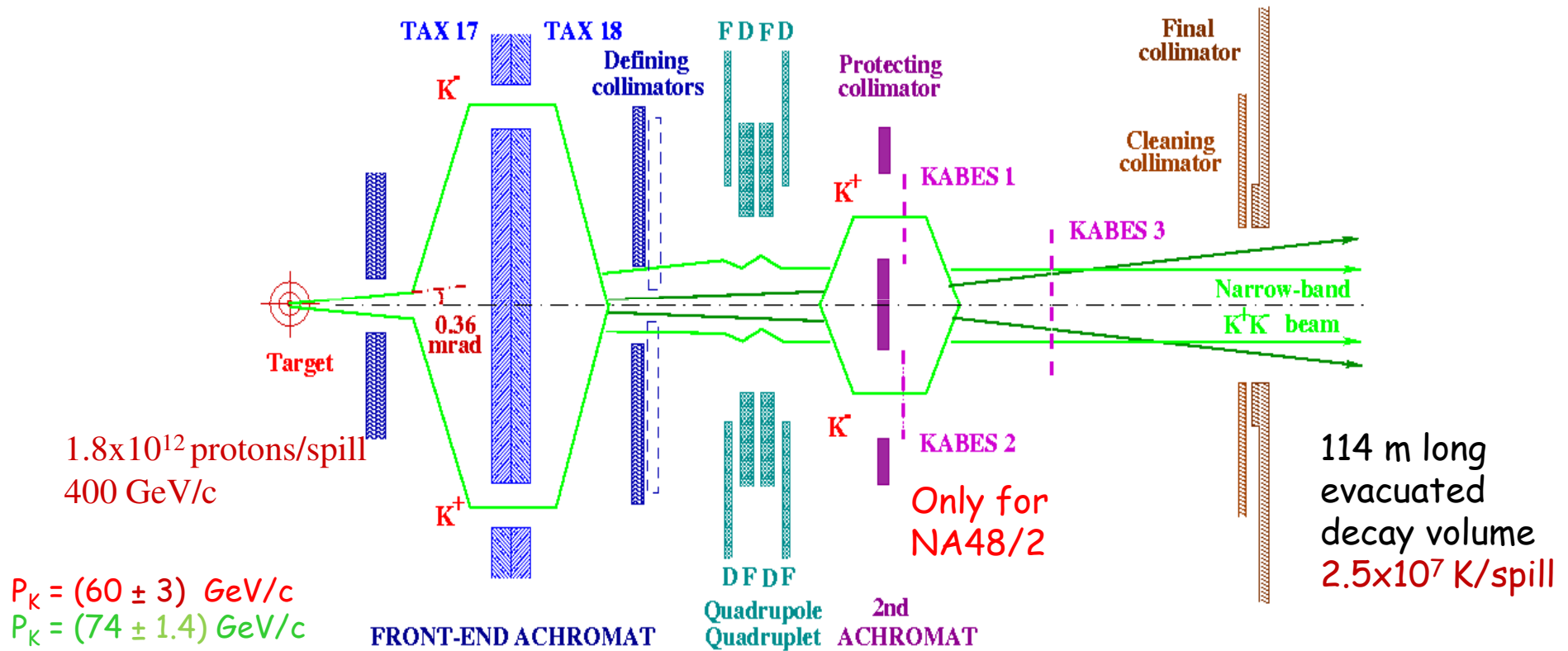
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- The NA48/2-NA62 beams and detector
- NA62 measurement of  $R_K = \frac{\Gamma(K \rightarrow e\nu(\gamma))}{\Gamma(K \rightarrow \mu\nu(\gamma))}$
- NA48/2 results on  $K^\pm \rightarrow \pi^0 e^\pm \nu$  and  $K^\pm \rightarrow \pi^0 \mu^\pm \nu$

# The NA48/2-NA62 Beam

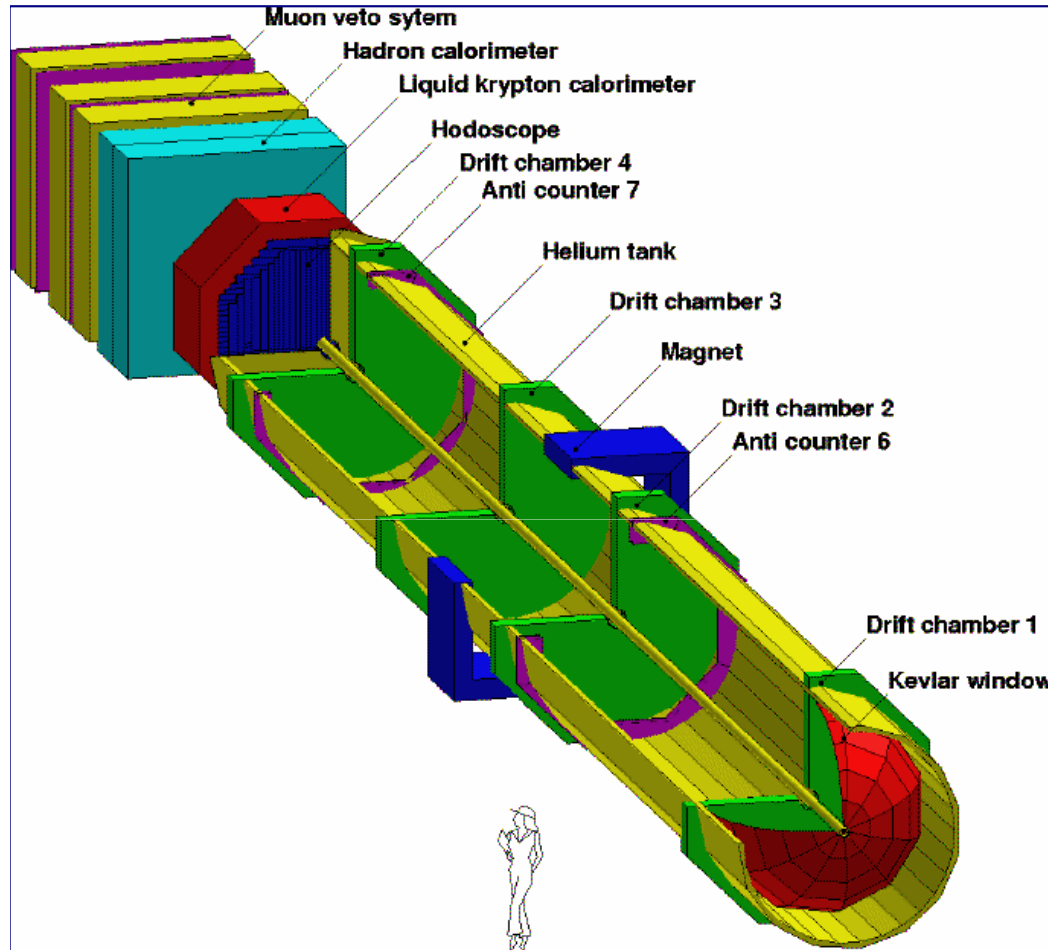
NA48/2 beam (2003-2004): simultaneous  $K^+/K^-$

NA62 beam (2007-2008): simultaneous or single  $K^+/K^-$



$K^+$  decays in the decay volume: 22% (18%)

# The Detector



Used by NA48 and NA62

Spectrometer  $P_T$  kick:

120 MeV/c in 2003-2004

265 MeV/c in 2007-2008

Spectrometer:

$$\sigma(P)/P \cong 1.02\% \oplus 0.044 P[\text{GeV}/c]\% \text{ NA48}$$

$$\sigma(P)/P \cong .48\% \oplus 0.009 P[\text{GeV}/c]\% \text{ NA62}$$

Scintillator hodoscope: fast trigger and good time resolution (150 ps)

LKr Calorimeter:

$$\sigma(E)/E \cong 3.2\%/ \sqrt{E} \oplus 9\%/E \oplus 0.42\%$$

Minimum bias trigger for both decay modes:  
1 track in the hodoscope and  $E_{\text{LKr}} > 10 \text{ GeV}$

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# $R_K$ measurement

# Physics motivations

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$$R_K = \frac{\Gamma(K \rightarrow e\nu(\gamma))}{\Gamma(K \rightarrow \mu\nu(\gamma))} = \frac{m_e^2}{m_\mu^2} \left( \frac{m_K^2 - m_e^2}{m_K^2 - m_\mu^2} \right)^2 (1 + \delta R_K)$$

Test of lepton universality

- Excellent accuracy due to cancellation of hadronic uncertainties in the ratio
- Helicity suppression of electronic mode, enhancement of sensitivity to non-SM effects

$$R_K(\text{SM}) = (2.477 \pm 0.001) \cdot 10^{-5} \quad 0.04\% \text{ precision!!}$$

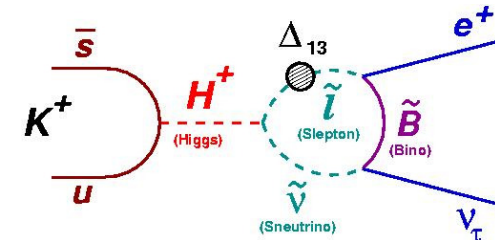
(V. Cirigliano, I. Rosell PRL 99 (2007) 231801)

- $\delta R_K$  due to IB part of the radiative  $K \rightarrow e\nu\gamma$  process
- $K \rightarrow e\nu\gamma(\text{IB})$  included by default in  $R_K$

# $R_K$ beyond the Standard Model

- The value of  $R_K$  could be different in case of SUSY LFV
  - Masiero, Paradisi, Petronzio, *Phys. Rev. D* 74 (2006) 011701
    - "Charged Higgs mediated SUSY LFV contributions can be strongly enhanced in kaon decays into an electron or a muon and a tau neutrino"

$$R_K^{LFV} \approx R_K^{SM} \left[ 1 + \left( \frac{m_K^4}{M_{H^\pm}^4} \right) \left( \frac{m_\tau^2}{M_e^2} \right) |\Delta_{13}|^2 \tan^6 \beta \right]$$



- Sensitive to slepton mixing.  $R_K$  enhancement experimentally accessible
- MSSM: 1% effect possible
  - Girrbach and Nierste, arXiv:1202:4096
  - However limited by recent  $B_s \rightarrow \mu^+ \mu^-$  measurement
- Sensitive to SM extensions with 4<sup>th</sup> generation, sterile  $\nu$

# The experimental situation

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- Three experiments from the 70's
  - $R_K = (2.45 \pm 0.11) \cdot 10^{-5}$
  - $\delta R_K / R_K = 4.5\%$
- 2009: KLOE (LNF) - 2001-2005 data
  - $\sim 13800 K_{e2}$  candidates, 16% bckg
  - $R_K = (2.493 \pm 0.025 \pm 0.019) \cdot 10^{-5}$
  - $\delta R_K / R_K = 1.3\%$
- NA62 2013, full statistics, this talk

- NA62 goals from the proposal
  - $\sim 150000 K_{e2}$  events
  - $\sim 0.4\%$  accuracy
- Data collected in the 2007-2008 run



# NA62 $R_K$ measurement strategy

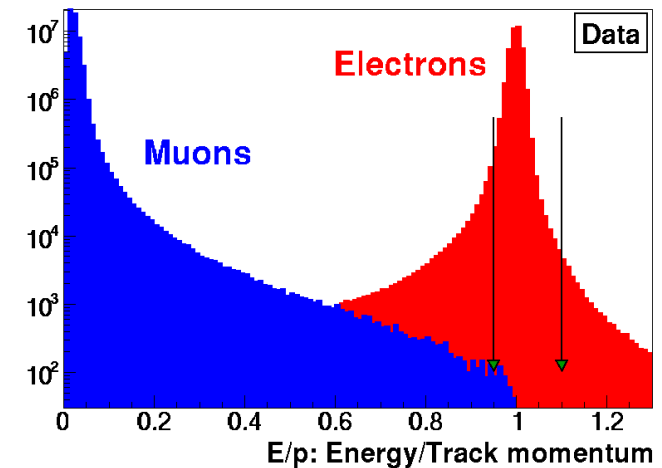
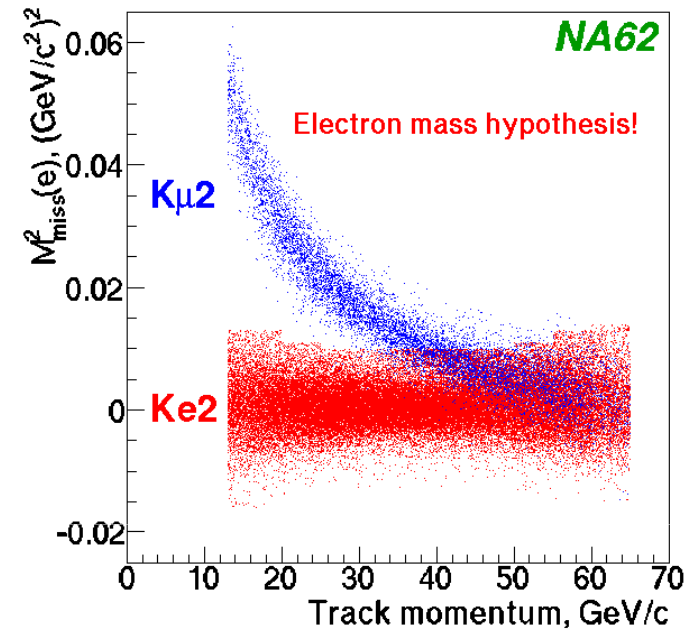
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- $K_{e2}$  and  $K_{\mu2}$  decays collected simultaneously
  - Do not rely on the kaon flux measurement
  - Many systematic effects cancel to first order in the ratio
    - » E.g. reconstruction/trigger efficiencies, time dependent effects
- Limited use of MC simulations
  - Geometric acceptance correction
  - PID, trigger, readout efficiencies **measured directly on data**
- Perform analysis in 10 lepton momentum bins
  - Background composition varies strongly with momentum

$$R_K = \frac{\overset{\text{Selected signal events}}{N(K_{e2}) - N_B(K_{e2})}}{\underset{\substack{\text{Bckg events} \\ \text{Main syst source}}}{N(K_{\mu2}) - N_B(K_{\mu2})}} \cdot \frac{\overset{\text{PID efficiencies}}{A(K_{\mu2}) \times f_\mu \times \mathcal{E}(K_{\mu2})}}{\underset{\text{Acceptances}}{A(K_{e2}) \times f_e \times \mathcal{E}(K_{e2})}} \cdot \frac{1}{\underset{\text{Trigger efficiencies}}{f_{LKr}}} \cdot \frac{1}{\underset{\substack{\text{LKR readout efficiency} \\ \text{K}_{\mu2} \text{ trigger downscaling factor}}}{D}}$$

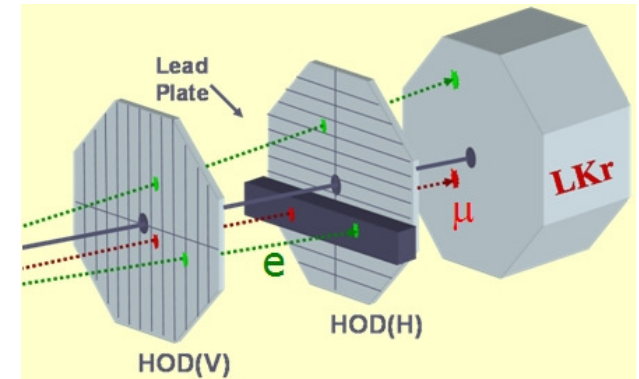
# $K_{e2}$ and $K_{\mu2}$ selection

- Common selection
  - One reconstructed track,  $13 < P < 65 \text{ GeV}/c$
  - Common geometrical cuts
  - Decay vertex defined as closest distance of approach track-nominal K axis
  - Veto extra LKr energy deposition clusters
- Kinematical identification
  - Use missing mass squared  $M_{\text{miss}}^2 = (P_K - P_l)^2$
  - $P_K$  (average) is monitored from the data with  $K \rightarrow 3\pi$ 
    - Enough  $K_{e2}/K_{\mu2}$  separation for  $P_{\text{track}} < 25 \text{ GeV}/c$
- Lepton identification
  - $E_{\text{LKr}}/P_{\text{track}} < 0.85$  for muons, between 0.95 (0.90 below  $25 \text{ GeV}/c$ ) and 1.10 for electrons

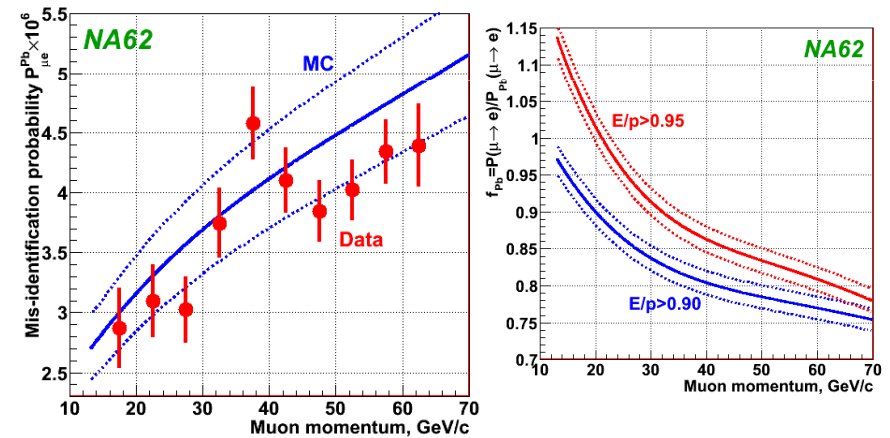


# The major background to $K_{e2}$

- Catastrophic bremsstrahlung of muons in the LKr
  - Gives  $E/p > 0.95 \rightarrow$  tag the event as  $K_{e2}$
  - Probability  $P_{\mu e} \sim 3 \cdot 10^{-6}$  (momentum dependent)
    - $K_{\mu 2}/K_{e2} \sim 40000 \rightarrow$  background  $O(10\%)$
  - Need a direct measurement to validate the muon bremsstrahlung cross section in this region



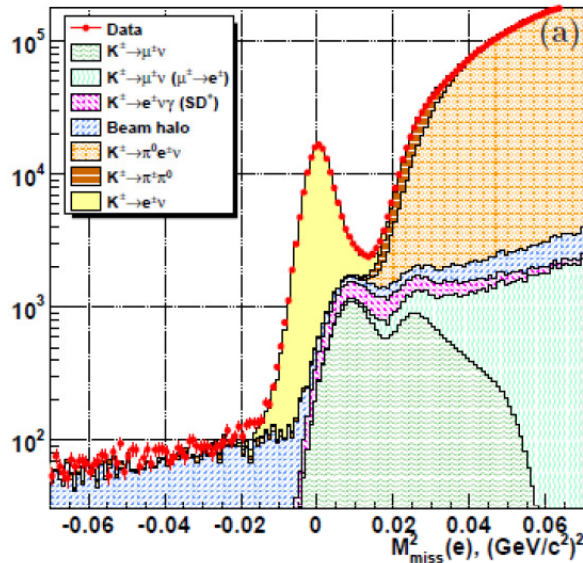
- Measure it putting  $9.2 X_0$  of lead in front of the calorimeter
  - For about 50% of the run time, 18% acceptance reduction
  - Suppress  $10^{-4}$  contamination of  $\mu \rightarrow e$  decays
  - Tracks traversing the lead are pure muons
  - $P_{\mu e}$  is modified by the Pb wall
    - Ionization losses in the Pb (at low p)
    - Bremsstrahlung in Pb (at high p)
  - The correction is evaluated with a dedicated Geant4 simulation



Contribution to background:  $B/(S+B) = 5 \sim 6 \%$

Uncertainty  $\sim 3$  times smaller than simulation alone

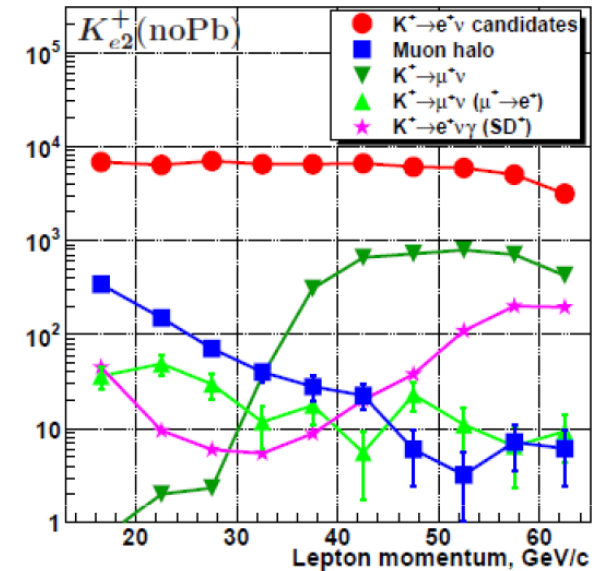
# $K_{e2}$ candidates



145958  $K_{e2}$  candidates

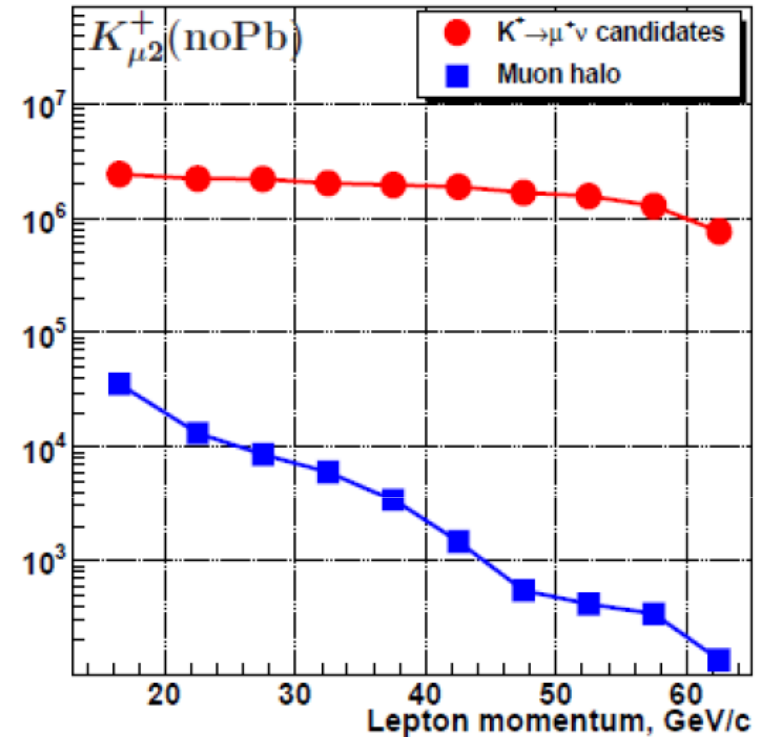
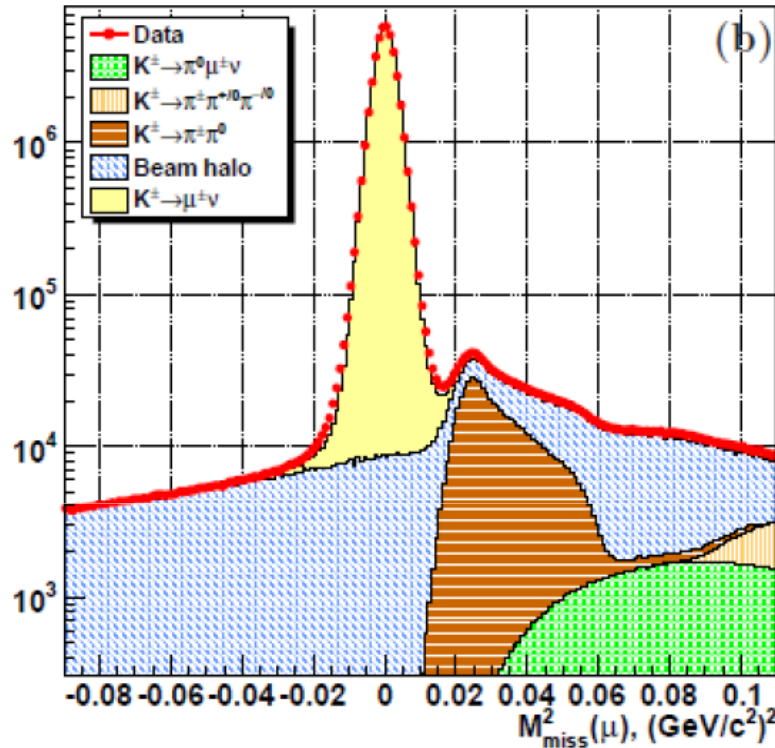
$B/(S+B) = (10.95 \pm 0.27)\%$

$e^\pm$  ID eff =  $99.28 \pm 0.05\%$



Data sample	$K^+$ (noPb)	$K^+$ (Pb)	$K^-$ (noPb)	$K^-$ (Pb)
$K_{e2}$ candidates	59813	63282	10530	12333
Muon halo	$(1.11 \pm 0.09)\%$	$(1.51 \pm 0.10)\%$	$(4.61 \pm 0.18)\%$	$(7.86 \pm 0.23)\%$
$K_{\mu 2}$	$(6.11 \pm 0.22)\%$	$(5.33 \pm 0.19)\%$	$(5.76 \pm 0.20)\%$	$(4.87 \pm 0.17)\%$
$K_{\mu 2}$ ( $\mu \rightarrow e$ decay)	$(0.26 \pm 0.04)\%$	$(0.27 \pm 0.04)\%$	$(0.31 \pm 0.09)\%$	$(0.19 \pm 0.07)\%$
$K^\pm \rightarrow e^\pm \nu \gamma$ ( $SD^+$ )	$(1.07 \pm 0.05)\%$	$(4.01 \pm 0.18)\%$	$(1.25 \pm 0.06)\%$	$(3.95 \pm 0.17)\%$
$K^\pm \rightarrow \pi^0 e^\pm \nu$	$(0.05 \pm 0.03)\%$	$(0.28 \pm 0.14)\%$	$(0.09 \pm 0.05)\%$	$(0.37 \pm 0.17)\%$
$K^\pm \rightarrow \pi^\pm \pi^0$	$(0.05 \pm 0.03)\%$	$(0.18 \pm 0.09)\%$	$(0.06 \pm 0.03)\%$	$(0.18 \pm 0.09)\%$
Opposite sign $K$	–	$(0.04 \pm 0.01)\%$	–	$(0.25 \pm 0.03)\%$
Total background	$(8.65 \pm 0.25)\%$	$(11.62 \pm 0.33)\%$	$(12.08 \pm 0.29)\%$	$(17.67 \pm 0.39)\%$

# $K_{\mu 2}$ candidates



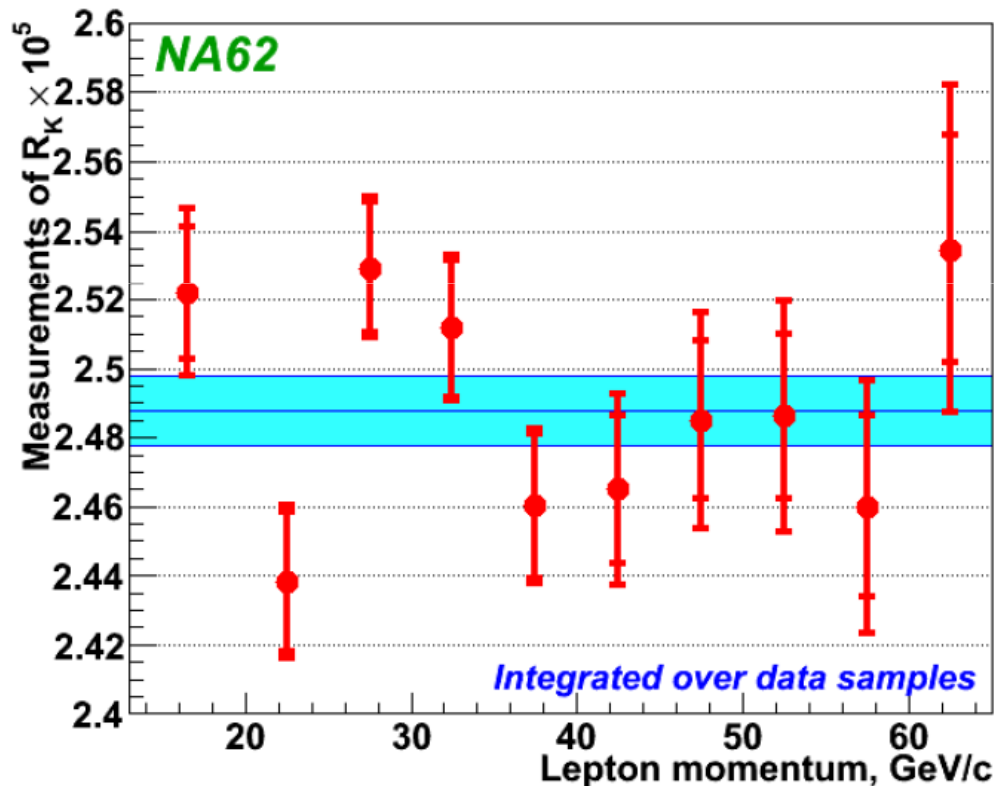
42.8  $10^6$  candidates with low background

	$K^+$ (noPb)	$K^+$ (Pb)	$K^-$ (noPb)	$K^-$ (Pb)
$K_{\mu 2}$ candidates / $10^6$	18.027	18.433	3.069	3.288
Muon halo	0.39%	0.44%	0.77%	1.22%

# NA62 final result

$$R_K = (2.488 \pm 0.007_{\text{stat}} \pm 0.007_{\text{syst}}) \times 10^{-5} = (2.488 \pm 0.010) \times 10^{-5} \quad (\chi^2/\text{ndf} = 47/39)$$

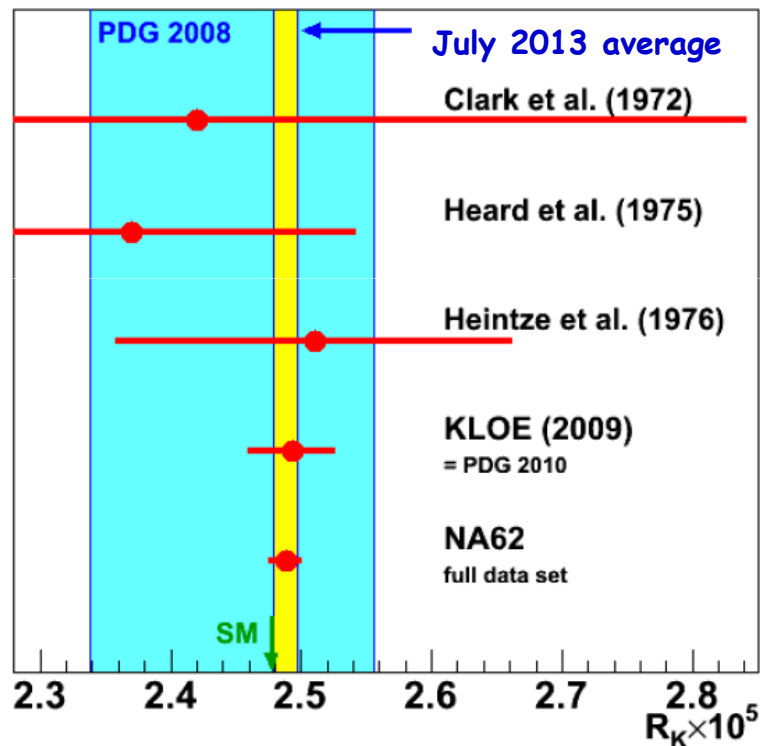
PLB 719 (2013) 326



## Uncertainties

Source	$\delta R_K * 10^5$
Statistical	0.007
Systematic	0.007
$K_{\mu 2}$	0.004
$BR(K_{e2\gamma} SD^+)$	0.002
$K^+ \rightarrow \pi^0 e^+ \nu, K^+ \rightarrow \pi^+ \pi^0$ bkg	0.003
Beam halo	0.002
Material in the spectrometer	0.002
Acceptance	0.002
DCH alignment	0.001
Electron ID eff.	0.001
1-track trigger eff.	0.001
LKr readout ineff.	0.001
<b>Total</b>	<b>0.010</b>

# Result summary



World average	$R_K * 10^5$	Precision
PDG 2008	$2.447 \pm 0.109$	4.5%
Today	$2.488 \pm 0.009$	0.36%

Consistency with older measurements and with the Standard Model

Experimental uncertainty is still an order of magnitude larger than the one in the SM prediction

Motivation for improved precision measurement

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# Measurement of the $K_{\ell 3}^{\pm}$ decay form factors



# Motivation

Master formula to access  $V_{us}$

$$\Gamma(K_{l3}(\gamma)) = \frac{G_f^2 m_K^5}{192\pi^3} C_K^2 S_{EW} |V_{us}|^2 |f_+(0)|^2 I_K^l (1 + 2\delta_{SU(2)}^l + 2\delta_{EM}^l)$$

The phase space integral ( $I_K^l$ ), including the form factor variation over the phase space, is an important ingredient to be measured accurately

Determined by the theory:

$f_+(0)$ : Hadronic form factor at  $q^2=0$  (different for  $K^\pm$  and  $K^0$ )

$\delta_{SU(2)}^l, \delta_{EM}^l$ : Corrections for SU(2) breaking and long-distance EM interactions

Two form factors in  $K_{l3}$  decays:  $f_+(t), f_-(t)$

$$M = \frac{G_F}{2} V_{us} (f_+(t)(P_K + P_\pi)^\mu \bar{u}_1 \gamma_\mu (1 + \gamma_5) u_v + f_-(t) m_1 \bar{u}_1 (1 + \gamma_5) u_v)$$

$f_+$  = vector form factor  
 $f_0$  = scalar form factor

$$f_0(t) = f_+(t) + \frac{t}{(m_K^2 - m_\pi^2)} f_-(t)$$

$f_+(0)$  cannot be measured directly

- Given by theory
- Only relative form factors experimentally accessible

# Form factor parametrizations

- Parameters with physical meaning

- Pole parametrization

Assumes exchange of vector (1-) or scalar (0+) resonances with masses  $m_v$  and  $m_s$

$f_+(t) \rightarrow K^*(892)$

$f_0(t) \rightarrow$  no dominating resonances

- Dispersive parametrization

Free parameters  $\Lambda_+$  and  $\ln C$

Polynomial approximation for the dispersive integrals  $G(t)$  and  $H(t)$  available

PLB638 (2006) 480, PRD 80 (2009) 034034

- Parameters without a physical meaning

- Expansion in the momentum transfer

Linear/Quadratic as a Taylor series

Widely used in the past

Large correlations between parameters (for quadratic expansion)

$$f_{+,0}(t) = \frac{m_{v,s}^2}{m_{v,s}^2 - t}$$

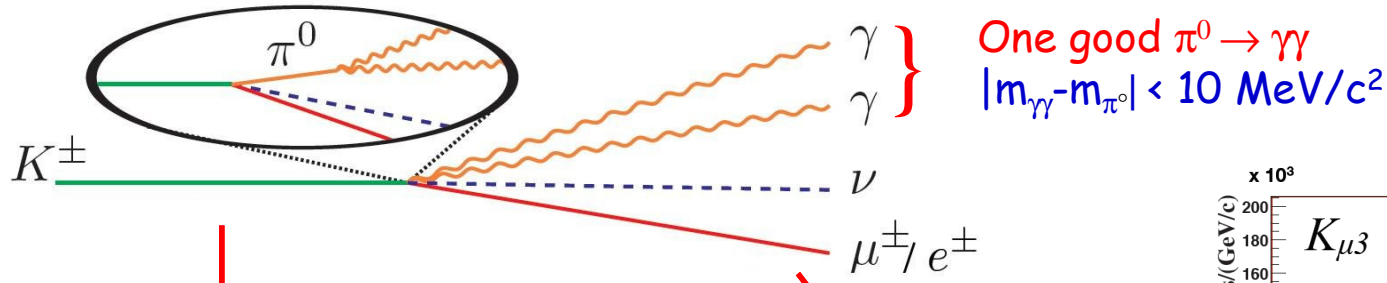
$$\bar{f}_+(t) = \exp\left[\frac{t}{m_\pi^2} (\Lambda_+ + H(t))\right]$$

$$\bar{f}_0(t) = \exp\left[\frac{t}{\Delta_{K\pi}} (\ln C + G(t))\right]$$

$$f_{+,0}(t) = \left[1 + \lambda_{+,0} \frac{t}{m_\pi^2}\right]$$

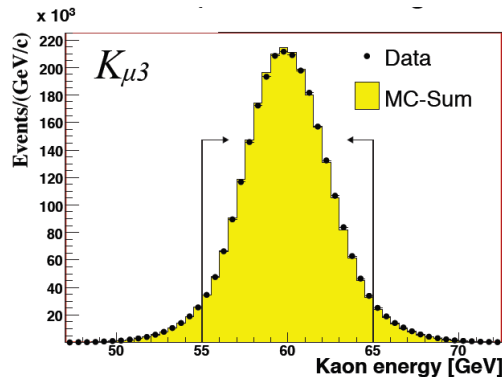
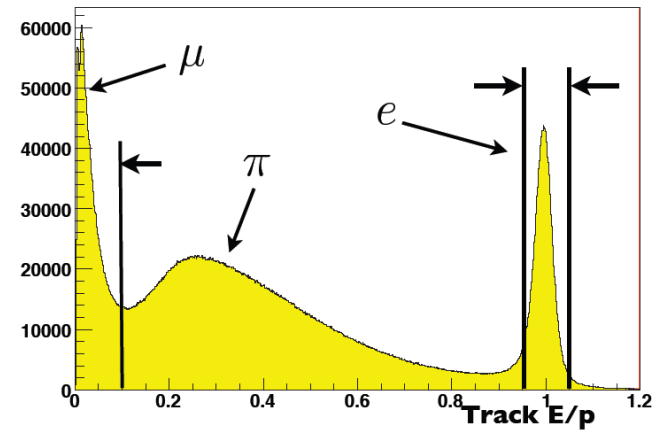
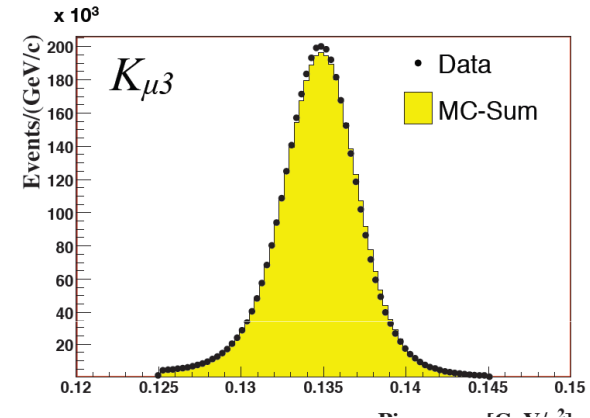
$$f_{+,0}(t) = \left[1 + \lambda'_{+,0} \frac{t}{m_\pi^2} + \frac{1}{2} \lambda''_{+,0} \left(\frac{t}{m_\pi^2}\right)^2\right]$$

# $K^{\pm}_{l3}$ selection



One good event  
 Photons and track in-time  
 $(\text{missing mass})^2 < 0.01(\text{GeV}/c^2)^2$   
 Reconstructed kaon energy:  
 $55 < E_K < 65 \text{ GeV}$  (missing  $\nu$  hyp)

One good track  
 $\mu$ :  $\mu$  veto and  $E/p$   
 $e$ :  $E/p$



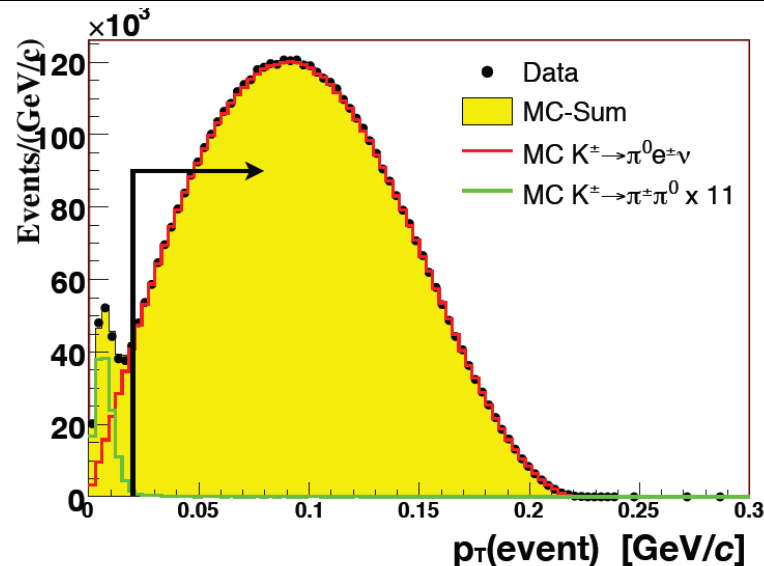
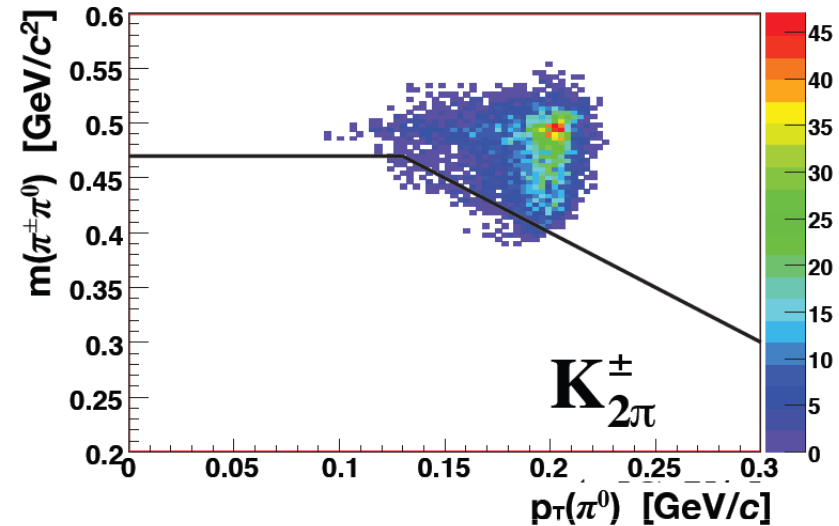
$2.5 \cdot 10^6$   $K_{\mu 3}$  events  
 $4.0 \cdot 10^6$   $K_{e 3}$  events  
 Collected in the 2004 run  
 Minimum bias trigger + reduced K  
 momentum & momentum byte

# Backgrounds

$K_{\mu 3}$ :  $\pi^+\pi^0$  with  $\pi \rightarrow \mu$  mis-ID or decay  
 Without suppression: 20% background

Cut in the invariant  $\pi^+\pi^0$  mass and pion  $p_T$

Background reduced to 0.5%  
 24% acceptance loss



$K_{e3}$ :  $\pi^+\pi^0$  with  $\pi \rightarrow e$  mis-ID if  $E/p > 0.95$

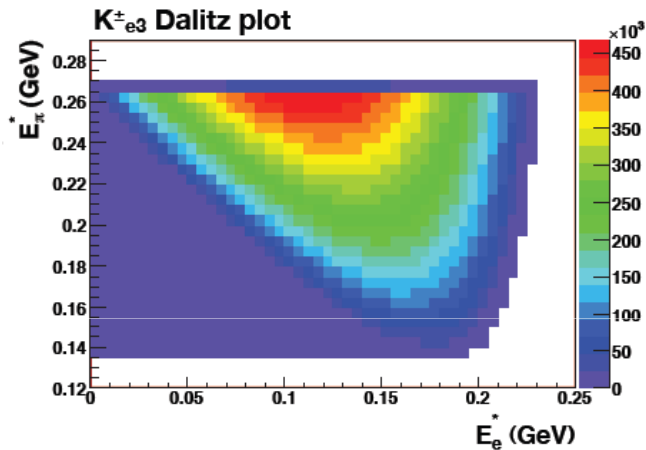
Cut on transverse momentum of the event

Background contamination  $< 0.1\%$   
 Acceptance loss  $\sim 3\%$

# Radiative effects

Include first order radiative corrections to the decay rate  
 Use KLOE simulation code (EPJ C45 (2006) 417)

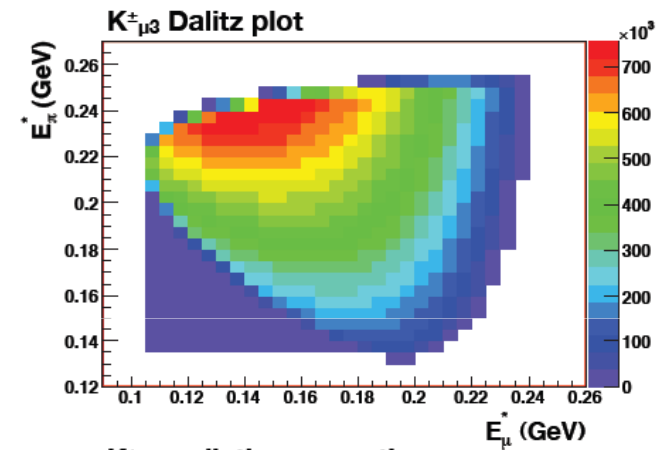
$$\Gamma_{K_{l3}} = \Gamma_{K_{l3}}^0 + \Gamma_{K_{l3}}^1 = \Gamma_{K_{l3}}^0 \left( 1 + 2\delta_{EM}^{Kl} \right)$$



Overall correction  $\delta_{EM}$

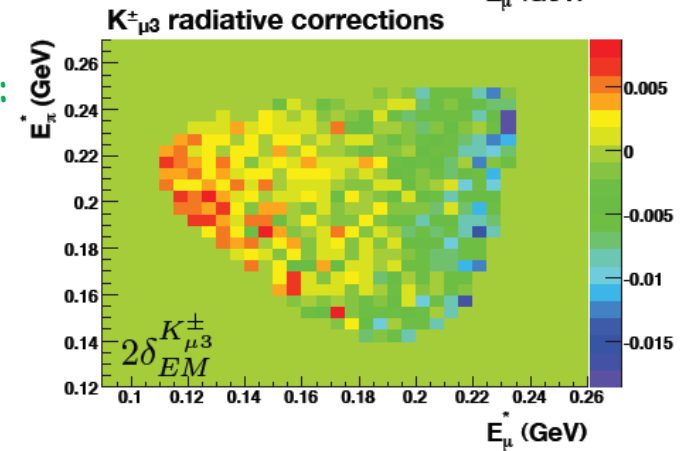
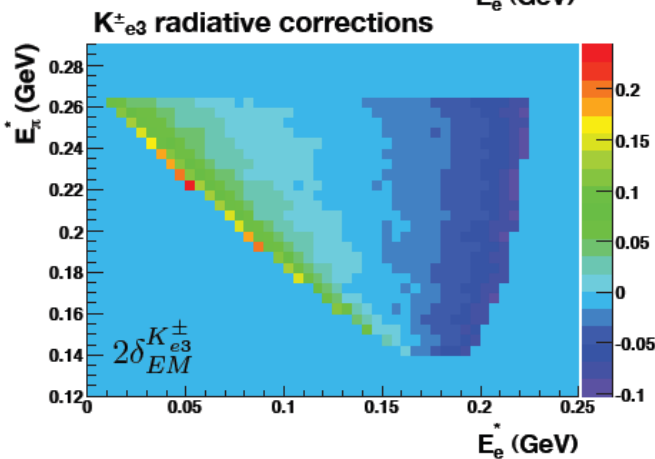
$K_{\mu 3}$  (0.008 ± 0.125)%  
 $K_{e 3}$  (0.050 ± 0.125)%

Small, but:



Effect on Dalitz plot slope:

$K_{\mu 3}$  ~1%  
 $K_{e 3}$  ~10%



# Fit to the Dalitz Plot Density

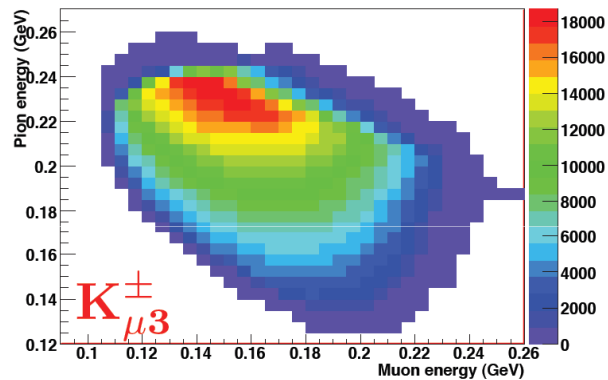
$$\rho(E_l^*, E_\pi^*) = \frac{d^2 N(E_l^*, E_\pi^*)}{dE_l^* dE_\pi^*} \propto Af_+^2(t) + Bf_+(t)(f_0 - f_+) \frac{m_K^2 - m_\pi^2}{t} + C \left[ (f_0 - f_+) \frac{m_K^2 - m_\pi^2}{t} \right]^2$$

$E_l, E_\pi$  = Energies of the lepton and of the pion in the kaon rest frame

A, B, C known kinematical terms

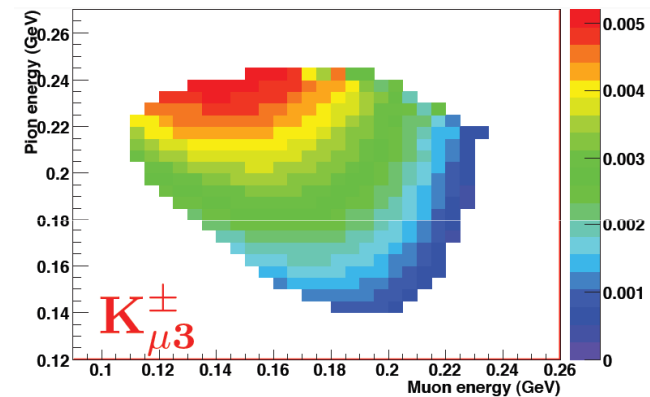
Fit performed in  $5 \times 5 \text{ MeV}^2$  bins

Cells outside or crossing the border of the physical region of the Dalitz plot are not used in the fit

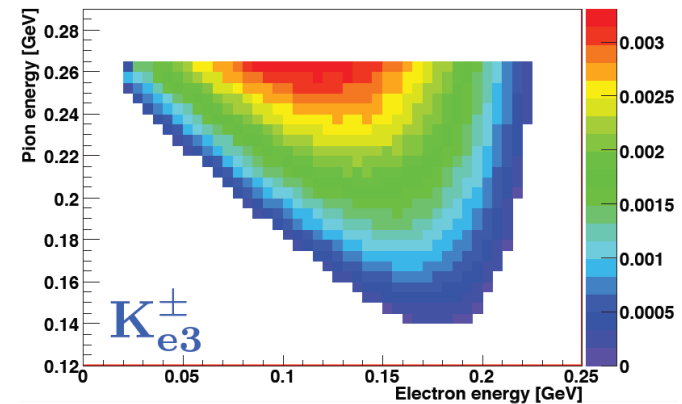
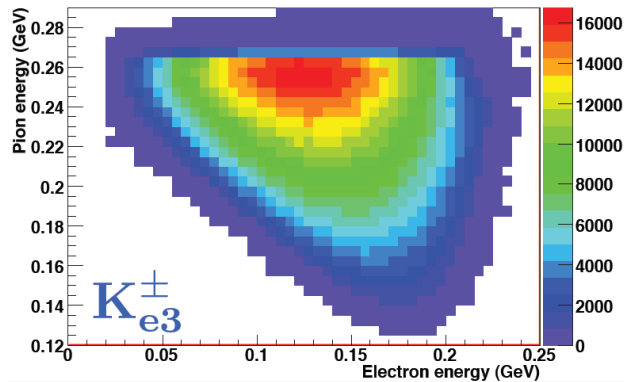


Background subtraction

Acceptance



Radiative effects



# Systematics

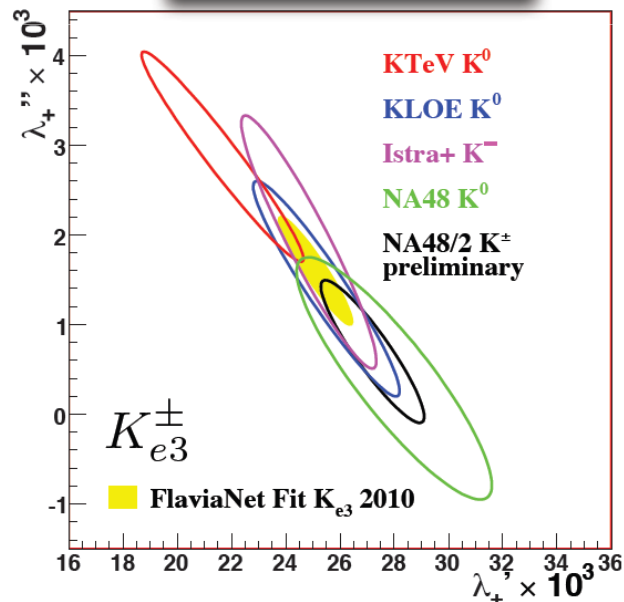
$K_{\mu 3}^{\pm}$	$\Delta\lambda'_+$	$\Delta\lambda''_+$ $\times 10^{-3}$	$\Delta\lambda_0$	$\Delta m_V$ MeV/c <sup>2</sup>	$\Delta m_S$
Kaon Energy	$\pm 0.1$	$\pm 0.0$	$\pm 0.3$	$\pm 1$	$\pm 8$
Vertex	$\pm 1.0$	$\pm 0.5$	$\pm 0.1$	$\pm 2$	$\pm 7$
Bin size	$\pm 0.8$	$\pm 0.4$	$\pm 0.7$	$\pm 3$	$\pm 10$
Energy scale	$\pm 0.3$	$\pm 0.1$	$\pm 0.1$	$\pm 0$	$\pm 1$
Acceptance	$\pm 0.2$	$\pm 0.1$	$\pm 0.3$	$\pm 2$	$\pm 5$
$K_{2\pi}$ background	$\pm 1.7$	$\pm 0.5$	$\pm 0.6$	$\pm 3$	$\pm 0$
2nd Analysis	$\pm 0.1$	$\pm 0.1$	$\pm 0.2$	$\pm 2$	$\pm 5$
FF input	$\pm 0.3$	$\pm 0.8$	$\pm 0.1$	$\pm 7$	$\pm 3$
Systematic	$\pm 2.2$	$\pm 1.1$	$\pm 1.0$	$\pm 9$	$\pm 16$
Statistical	$\pm 3.0$	$\pm 1.1$	$\pm 1.4$	$\pm 8$	$\pm 31$

$K_{e 3}^{\pm}$	$\Delta\lambda'_+$ $\times 10^{-3}$	$\Delta\lambda''_+$	$\Delta m_V$ MeV/c <sup>2</sup>
Kaon Energy	$\pm 0.3$	$\pm 0.1$	$\pm 6$
Vertex	$\pm 0.2$	$\pm 0.1$	$\pm 0$
Bin size	$\pm 0.0$	$\pm 0.1$	$\pm 2$
Energy scale	$\pm 0.1$	$\pm 0.0$	$\pm 0$
Acceptance	$\pm 0.2$	$\pm 0.0$	$\pm 3$
2nd Analysis	$\pm 0.9$	$\pm 0.4$	$\pm 1$
FF input	$\pm 0.4$	$\pm 0.0$	$\pm 1$
Systematic	$\pm 1.1$	$\pm 0.4$	$\pm 7$
Statistical	$\pm 0.7$	$\pm 0.3$	$\pm 3$

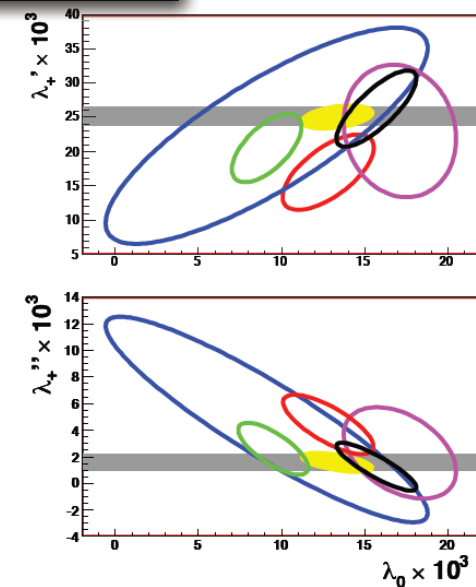
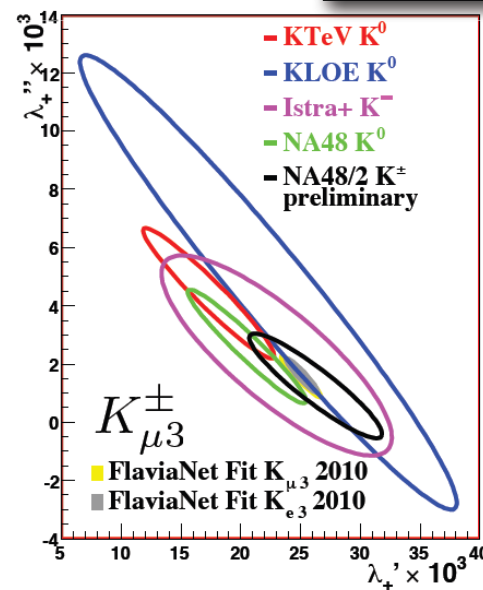
# Results

Quadratic ( $\times 10^{-3}$ )	$\lambda'_+$	$\lambda''_+$	$\lambda_0$
$K_{\mu 3}^\pm$	$26.3 \pm 3.0_{\text{stat}} \pm 2.2_{\text{syst}}$	$1.2 \pm 1.1_{\text{stat}} \pm 1.1_{\text{syst}}$	$15.7 \pm 1.4_{\text{stat}} \pm 1.0_{\text{syst}}$
$K_{e3}^\pm$	$27.2 \pm 0.7_{\text{stat}} \pm 1.1_{\text{syst}}$	$0.7 \pm 0.3_{\text{stat}} \pm 0.4_{\text{syst}}$	
Pole (MeV/c <sup>2</sup> )	$m_\nu$		$m_S$
$K_{\mu 3}^\pm$	$873 \pm 8_{\text{stat}} \pm 9_{\text{syst}}$		$1183 \pm 31_{\text{stat}} \pm 16_{\text{syst}}$
$K_{e3}^\pm$	$879 \pm 3_{\text{stat}} \pm 7_{\text{syst}}$		

68% Confidence level contours



68% Confidence level contours

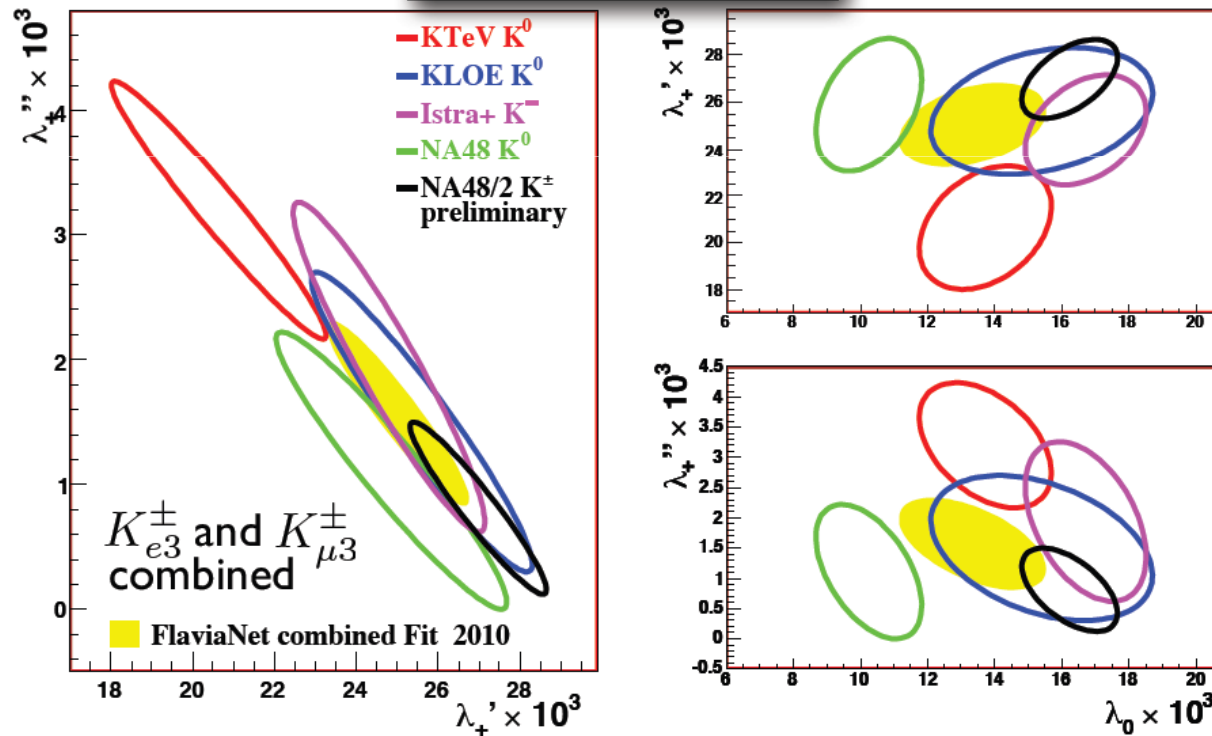




# Combined results

Quadratic ( $\times 10^{-3}$ )	$\lambda'_+$	$\lambda''_+$	$\lambda_0$
	$26.98 \pm 1.11$	$0.81 \pm 0.46$	$16.23 \pm 0.95$
Pole (MeV/c <sup>2</sup> )	$m_\nu$		$m_S$
	$877 \pm 6$		$1176 \pm 31$

68% Confidence level contours



# Summary and outlook

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- NA62 has taken data in 2007-2008 to reach 0.4% precision on  $R_K$
- The analysis of the full data set has been completed
- The measured value is  $R_K = (2.488 \pm 0.010) \cdot 10^{-5}$
- The precision achieved is 0.4%
  
- With data collected in 2004, NA48/2 has studied the semileptonic decays  $K^\pm \rightarrow \pi^0 \mu^\pm \nu$  and  $K^\pm \rightarrow \pi^0 e^\pm \nu$
- Preliminary results on the form factor parametrization have been presented
- More  $K^\pm$  and  $K^0$  data collected by NA62 in 2007 are ready to be analyzed
  - Expected to have  $O(10^7)$   $K^\pm_{l3}$  and  $O(10^6)$   $K^0_{l3}$  decays